

Inclusive radiative and semileptonic B decays as a probe for New Physics

- Motivation

- CP-Violation in the Standard Model

- Radiative Penguin Decays

- Inclusive $B \rightarrow X_s \gamma$ Decays

- Constraints on New Physics

- Semileptonic B Decays

- Inclusive Decays: $|V_{cb}|$ & $|V_{ub}|$

- Heavy Quark Parameters: $m_b, m_c, \mu_\pi^2, \dots$

- Consistency of Standard Model

Henning Flächer
CERN

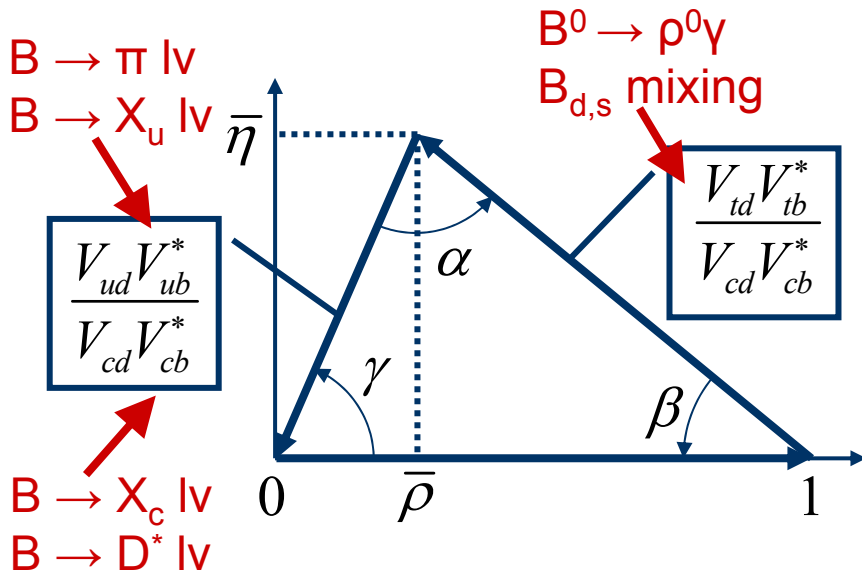
CKM-Matrix and Unitarity Triangle

In the Standard Model, couplings between quarks of different flavour are described by the CKM matrix. It relates weak to mass eigenstates.

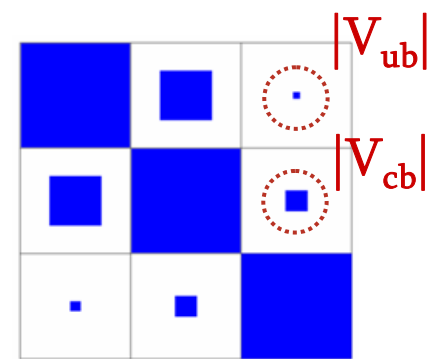
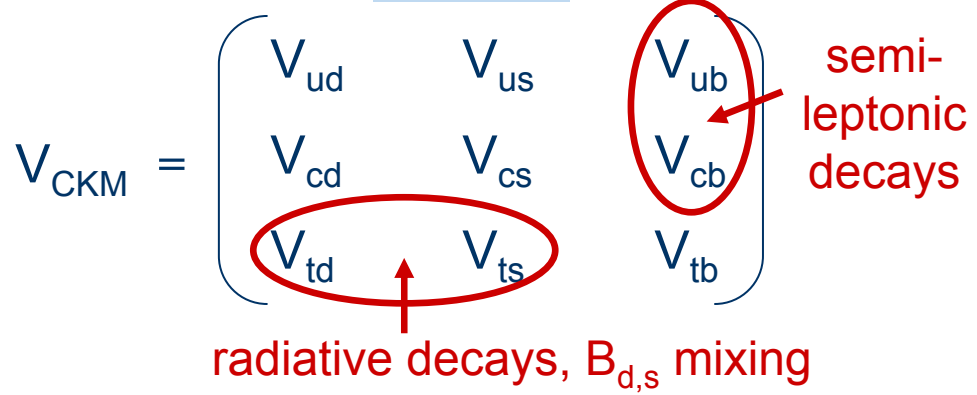
Unitarity condition

$$1 + \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0$$

can be visualised as triangle:



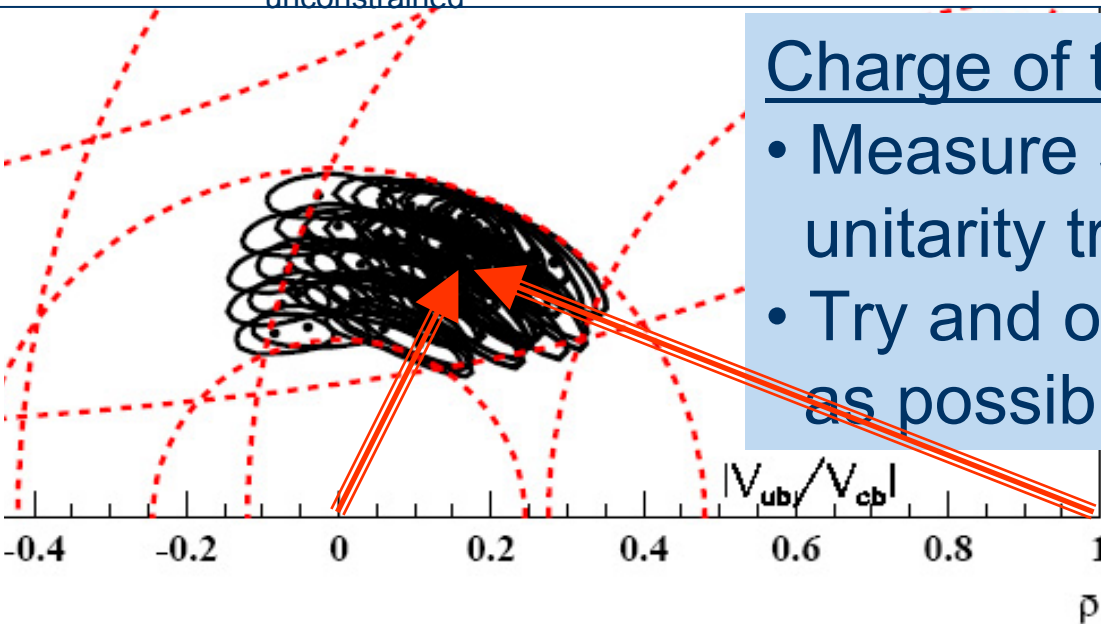
unitary!



A look at the past...

~1998

- unitarity triangle basically unconstrained



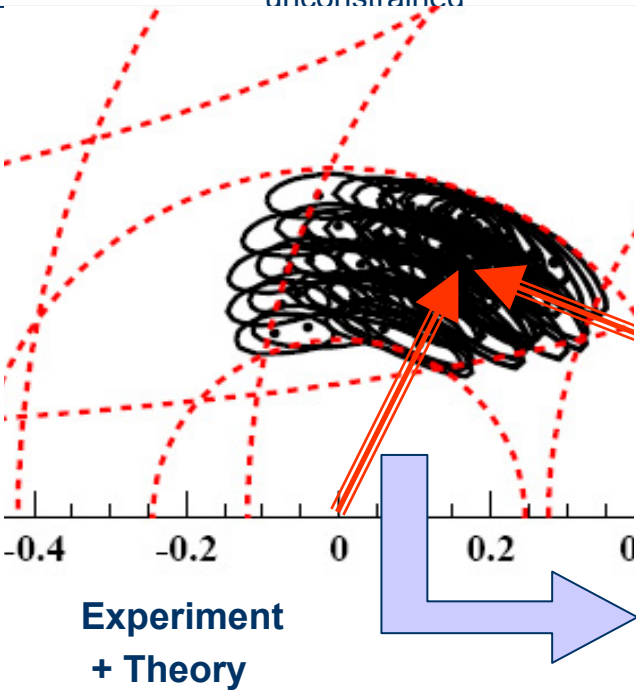
Charge of the B-Factories:

- Measure sides and angles of the unitarity triangle
- Try and overconstrain UT as much as possible

The situation today

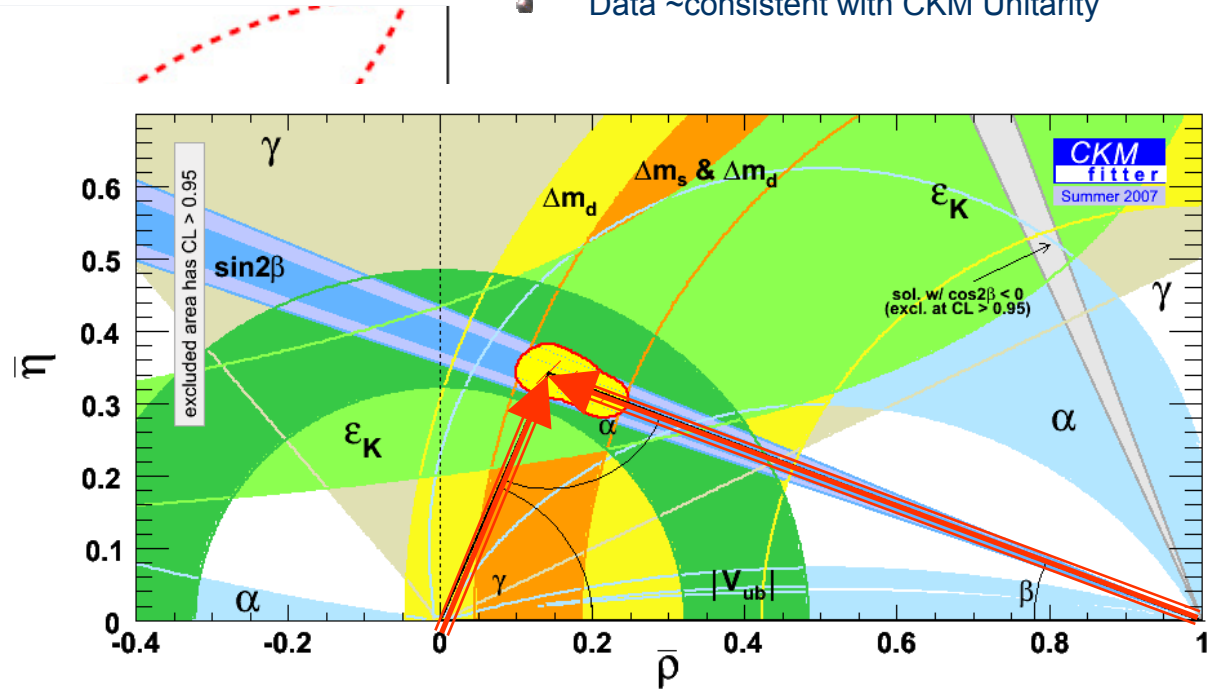
~1998

- unitarity triangle basically unconstrained



2007

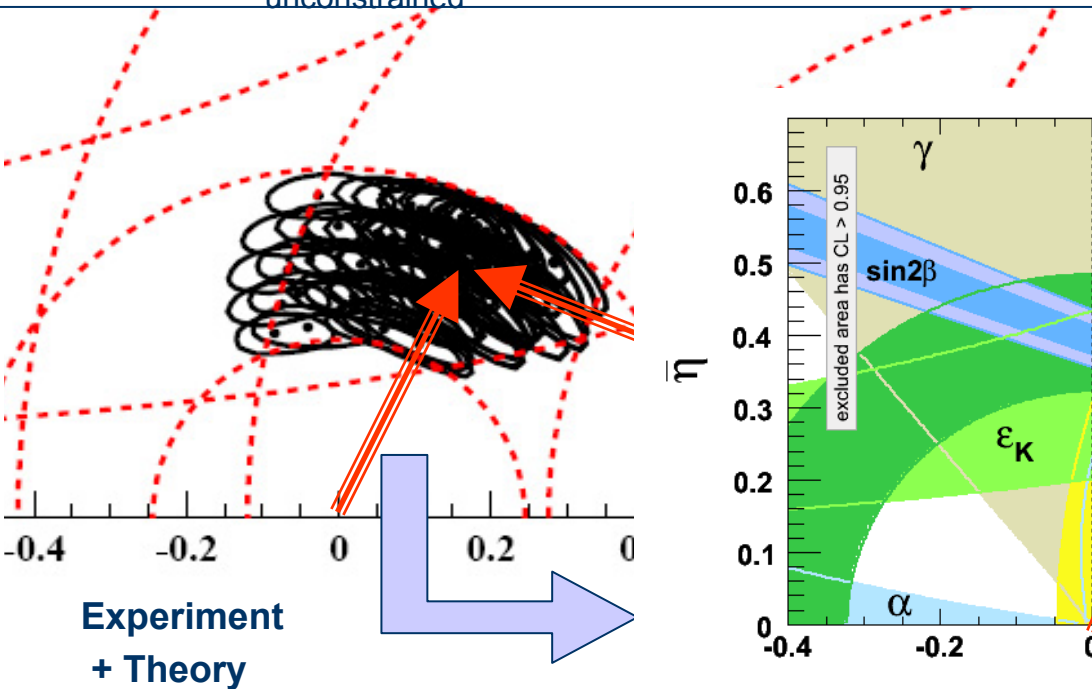
- precision measurement
- Data ~consistent with CKM Unitarity



The situation today

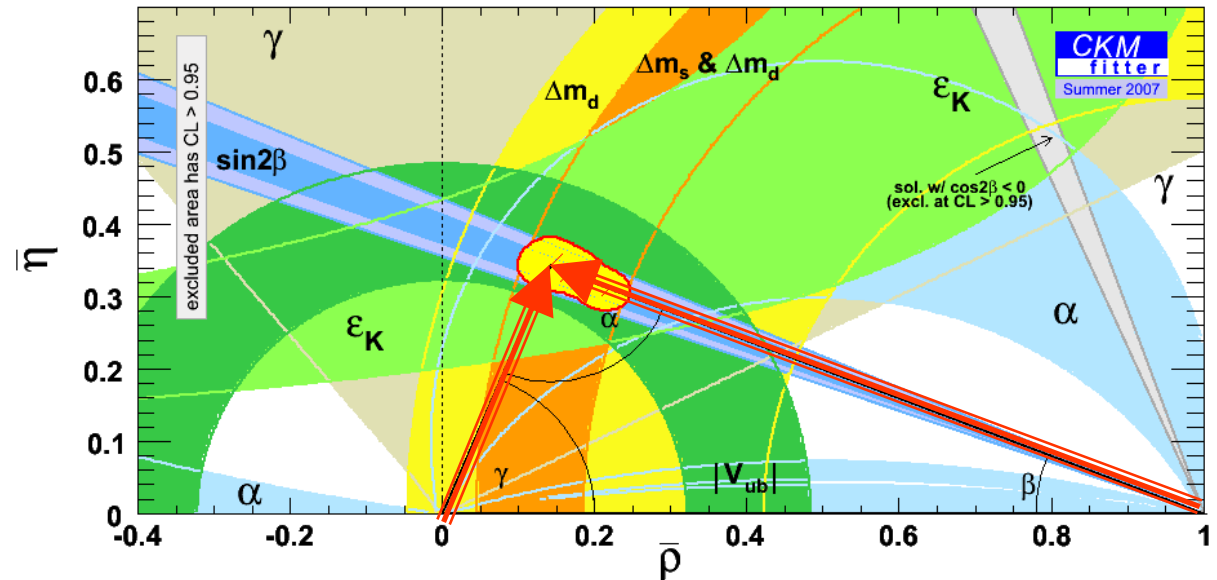
~1998

- unitarity triangle basically unconstrained



2007

- precision measurement
- Data ~consistent with CKM Unitarity



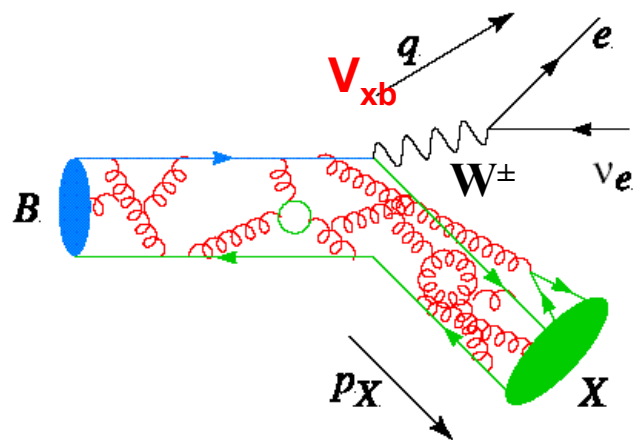
Standard Model description of CP violation is a success!

We are looking for small deviations from SM when looking for New Physics.

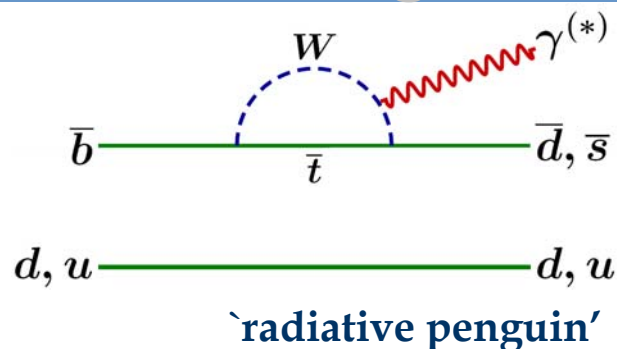
In this talk: Agreement between $\sin 2\beta$ and $|V_{ub}|$

What makes semileptonic and radiative B decays so interesting?

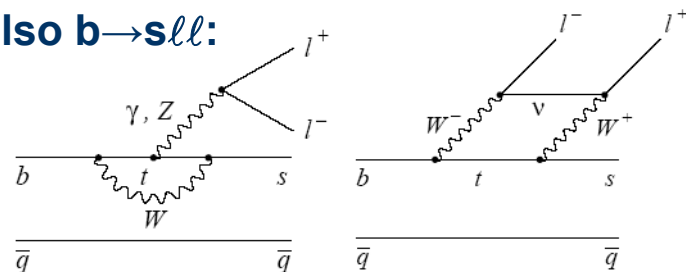
Semileptonic decays are tree-level decays
 → free of New Physics contributions for
 $W \rightarrow e\nu$ and $W \rightarrow \mu\nu$
 c.f. $\sin 2\beta$: mixing (box diagrams)



- Hadronic and leptonic currents factorise
- theoretical uncertainties under control
- reliable determination of $|V_{ub}|$ and $|V_{cb}|$

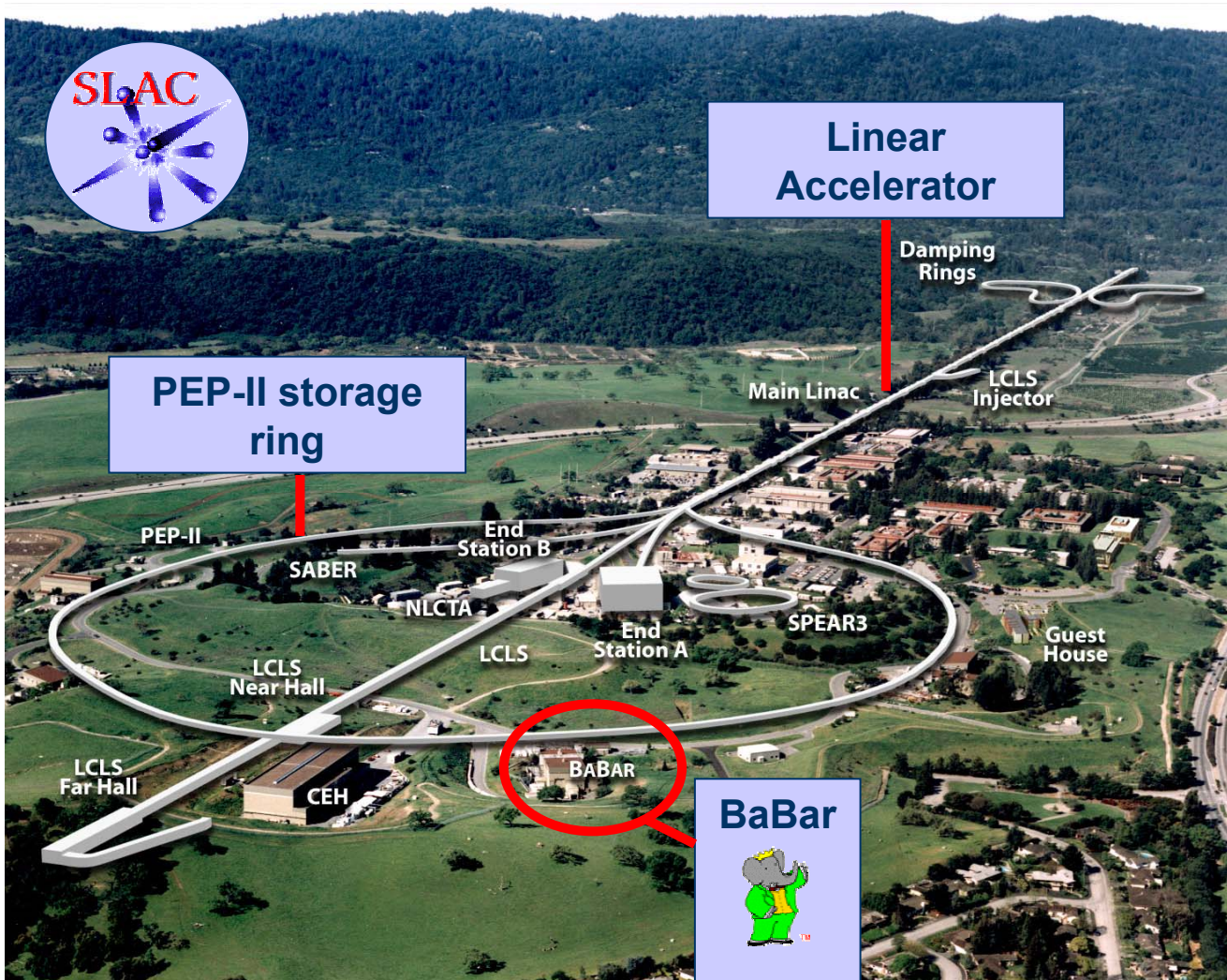


- $b \rightarrow s, d$ transition is a **Flavour Changing Neutral Current**
 - In Standard Model forbidden at tree-level
 - exists only at loop level
- heavy particles dominate in the loop
- But also $b \rightarrow sll$:



Both decays can be treated in the framework of Heavy Quark Effective Theory, relating parton level decay rate to meson decay rate with the help of Operator Product Expansions

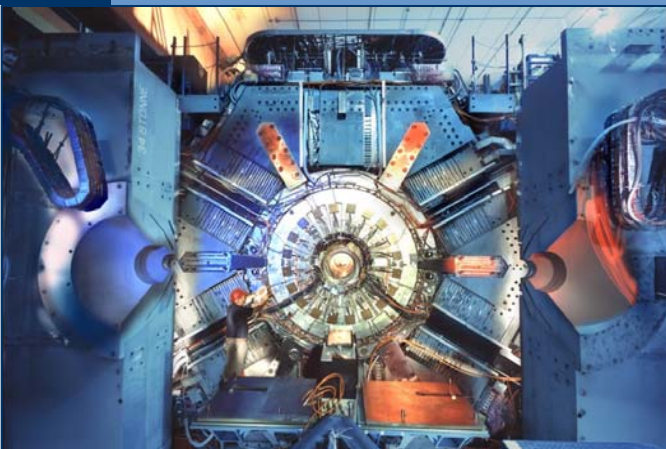
PEP-II and BaBar at SLAC



- asymmetric e^+e^- storage ring
- 9 GeV e^- on
3.1 GeV e^+
- Y(4S) boost $\beta\gamma \sim 0.56$

Peak luminosity of
 $1.2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
(more than 3x design!)

BaBar Detector



Electromagnetic Calorimeter

6580 CsI crystals
 e^+ ID, π^0 and γ reco

Instrumented Flux Return

19 layers of RPCs (+LSTs)
 μ ID

Cherenkov Detector

144 quartz bars
 K , π , p separation

Drift Chamber

40 layers
tracking + dE/dx

Silicon Vertex Tracker

5 layers (double-sided Si strips)
vertexing + tracking (+ dE/dx)

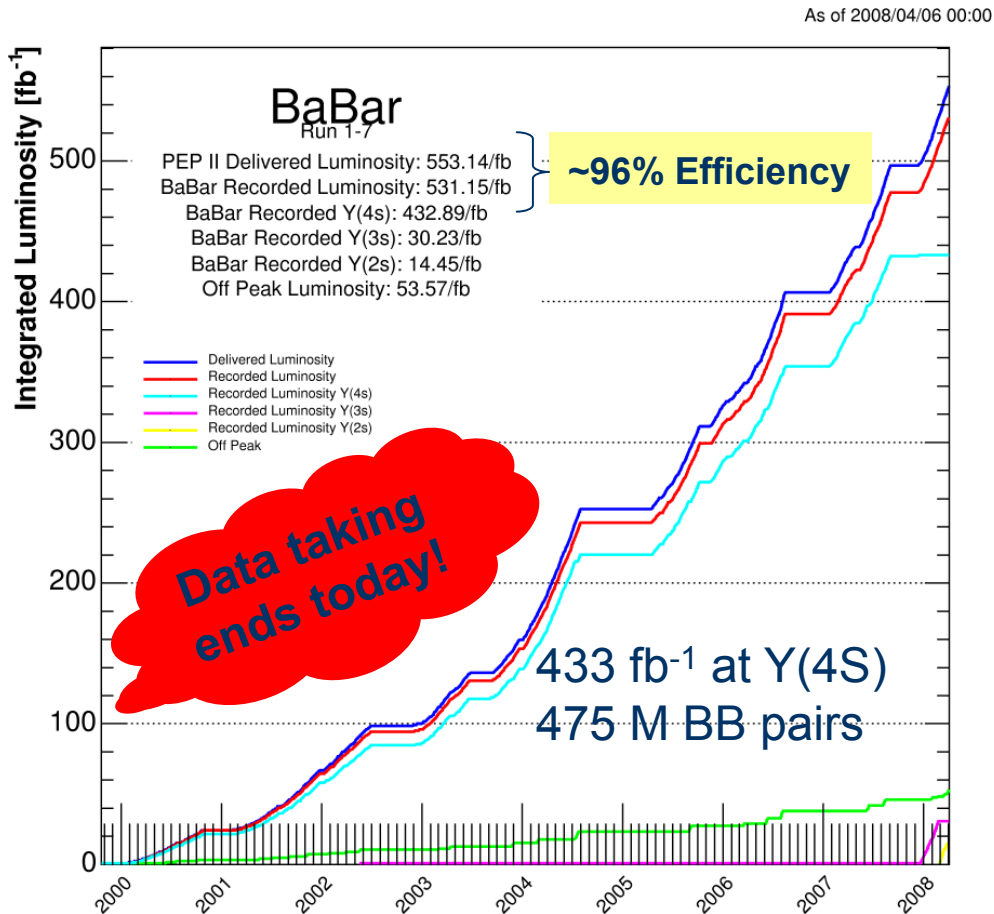
1.5T Magnet

e^+ [3.1 GeV]

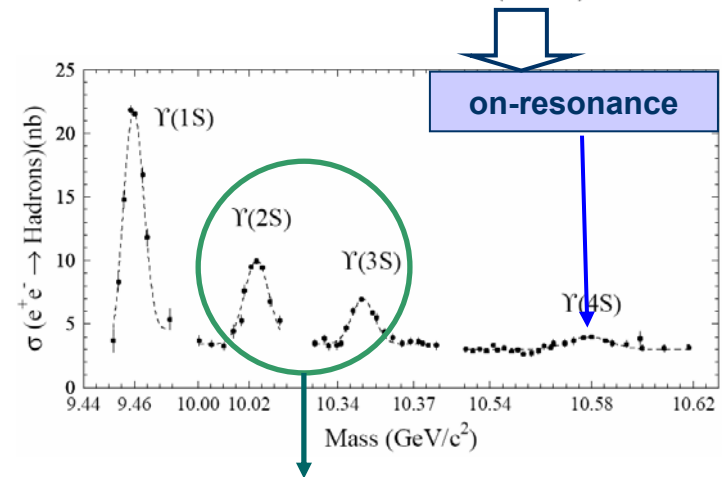
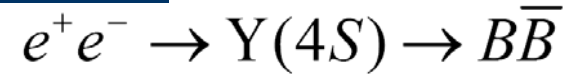
e^- [9 GeV]

Production of B-Mesons

- For the study of rare decays it needs millions of B-mesons
- Branching fractions of 10^{-6} and less!



Mechanism:

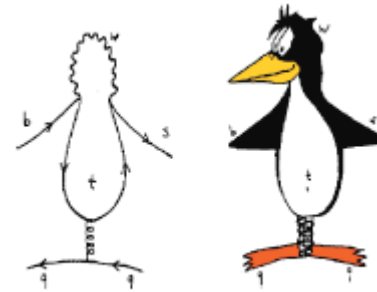
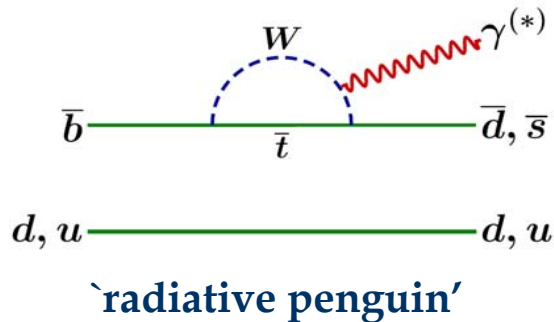


- since December:
 centre-of-mass energy at Y(3S) and Y(2S) resonances
- Aim: Search for rare decays (deviations from SM) and detailed bottomonium spectroscopy with 140 million Y(3S) and Y(2S) decays each

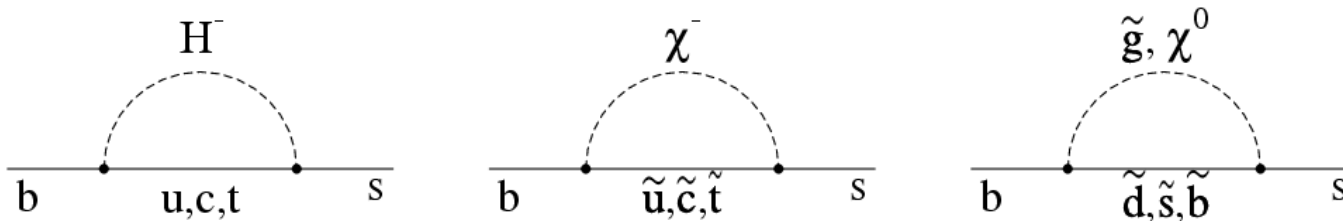
B → **X_sγ**

Electroweak Penguin Decays

- $b \rightarrow s, d$ transition with high-energetic photon in final state



- FCNC, New Physics appears at same order as SM process



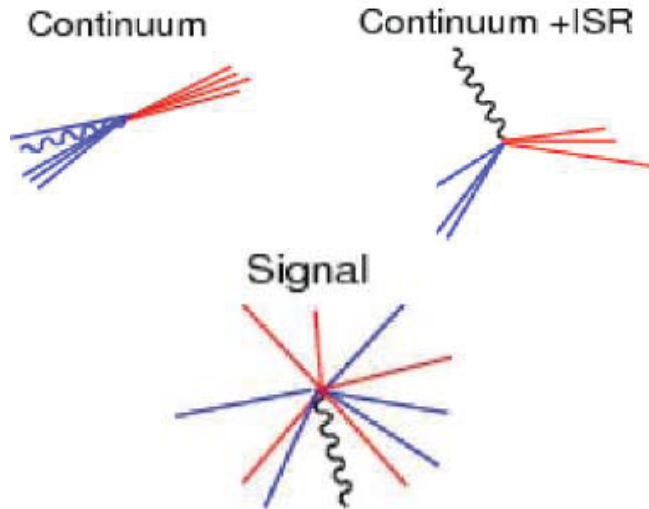
- Measurement of $B \rightarrow X_s \gamma$ branching fraction can constrain parameter space of many SUSY models

- Interesting with regard to LHC

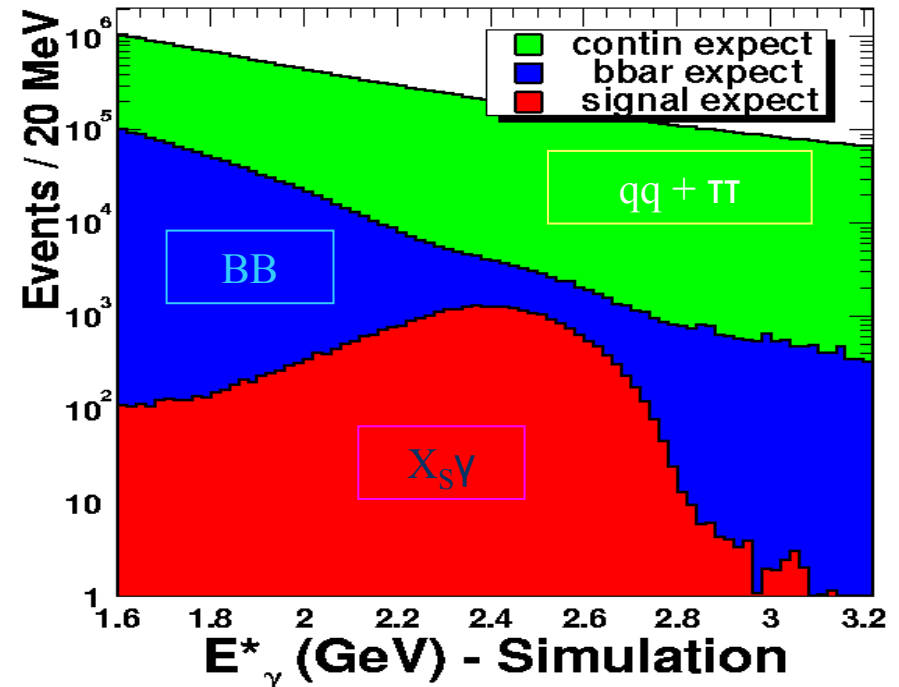
The radiative decay $b \rightarrow s\gamma$

- Experimental challenge:
- overwhelming photon background from continuum (u,d,s,c) and other B decays

- make use of event shape variables



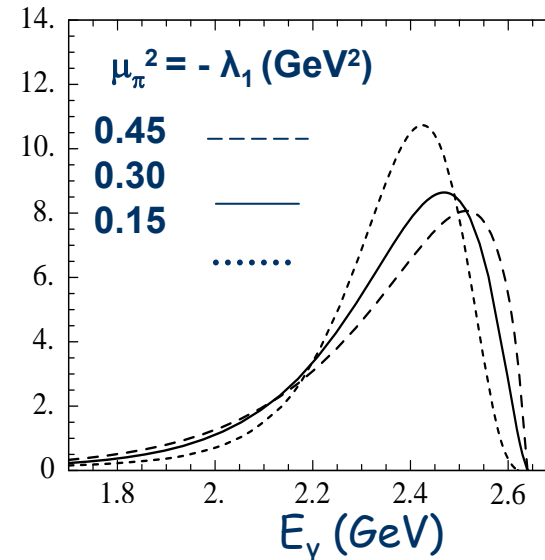
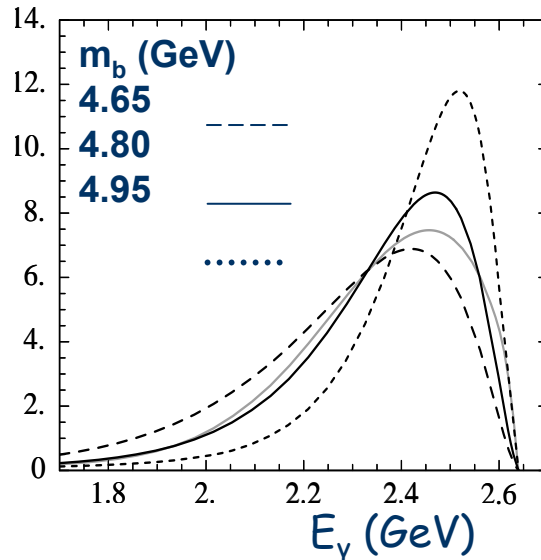
- Veto π^0 and η decays
 - on average 3.4 π^0 in continuum
 - 2.3 π^0 in $Y(4S)$ events
- measure to E_γ as low as possible



- Theoretical predictions:
 NNLO calculations of $E_\gamma > 1.6$ GeV:
 - Misiak et al: $\text{BF}(B \rightarrow X_{s\gamma}) = (3.15 \pm 0.23) \cdot 10^{-4}$
 - Becher et al: $\text{BF}(B \rightarrow X_{s\gamma}) = (2.98 \pm 0.26) \cdot 10^{-4}$
 - Andersen et al: $\text{BF}(B \rightarrow X_{s\gamma}) = (3.47 \pm 0.48) \cdot 10^{-4}$

The radiative decay $b \rightarrow s\gamma$

Spectrum modelled with help of two Heavy Quark parameters:
b-quark mass and **Fermi momentum μ_π^2** (motion of b-quark within B meson)



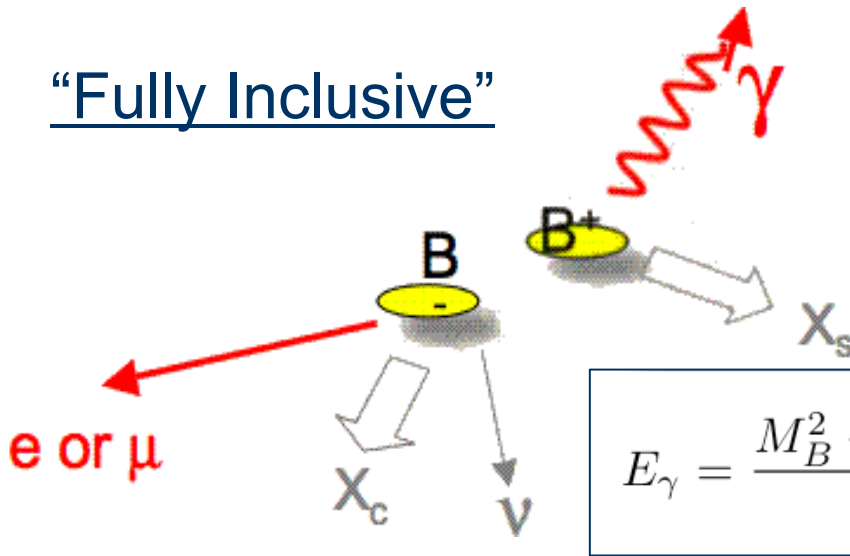
Eur.Phys.J.C7:5-27,1999

Moments of the photon spectrum:

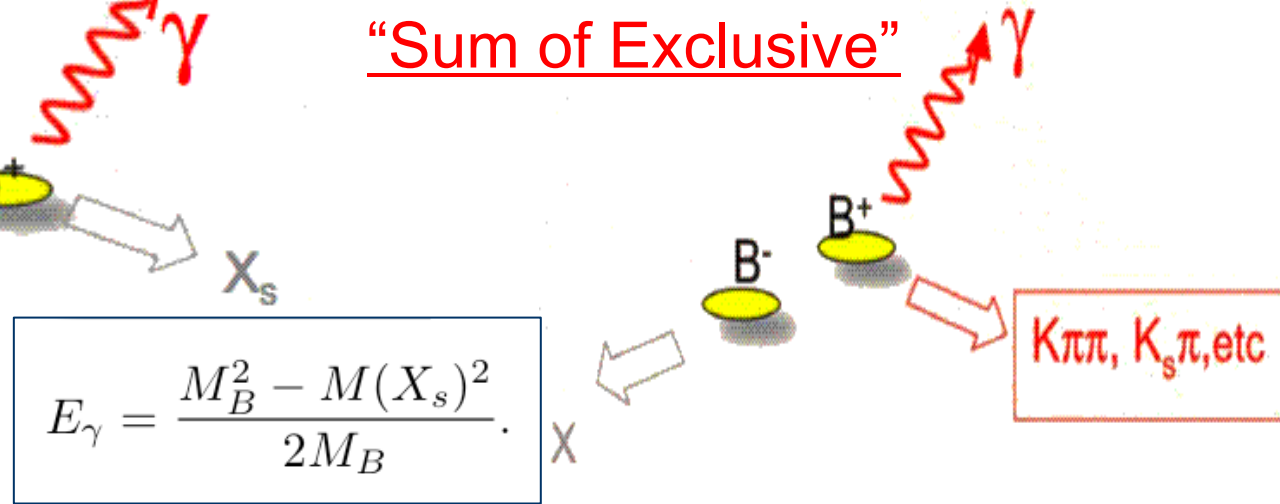
- Sensitive to HQ parameters
- $m_b \sim E_\gamma/2$
- $\mu_\pi^2 \sim \langle E^2 - \langle E \rangle^2 \rangle$
- b-quark mass interesting as SM parameter
- HQ parameter important input for $|V_{ub}|$

Experimental Strategies for $B \rightarrow X_s \gamma$

“Fully Inclusive”



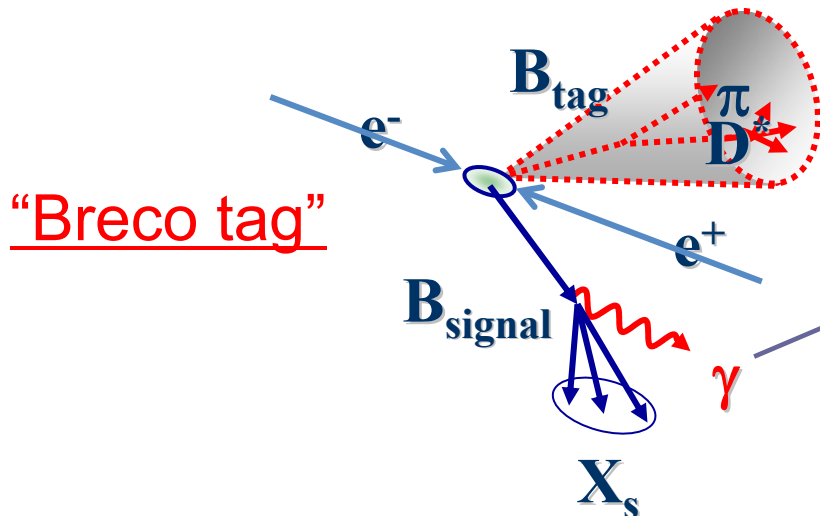
“Sum of Exclusive”



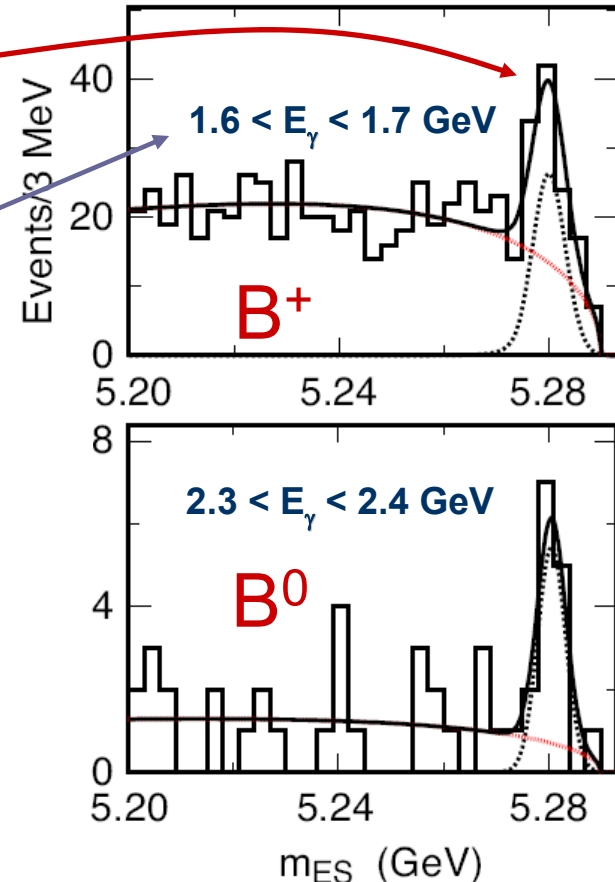
$$E_\gamma = \frac{M_B^2 - M(X_s)^2}{2M_B} \cdot X$$

- Ignore X_s system
- Reconstruct only the γ
- Pros
 - No X_s fragmentation sensitivity
 - theoretically clean
- Cons
 - High background
 - Measure E_γ^* in $Y(4S)$ frame
- Fully reconstruct subset of X_s final states
- Pros
 - Lower background
 - Good E_γ resolution in B-frame
- Cons
 - X_s fragmentation systematic
 - Missing X_s decay modes

Fully inclusive with B tag



- identification of one isolated photon
- possibility to reconstruct the X_s
- Pros:
 - 4-momentum, charge and flavour determined!
 - asymmetry measurements: A_{CP} , Δ_0 -
 - photon spectrum in B frame
 - number of tag Bs gives normalisation
 - small efficiency extrapolation
 - continuum subtracted through m_{ES} fit
- Cons
 - small efficiency for full B reconstruction: $\sim 0.4\%$

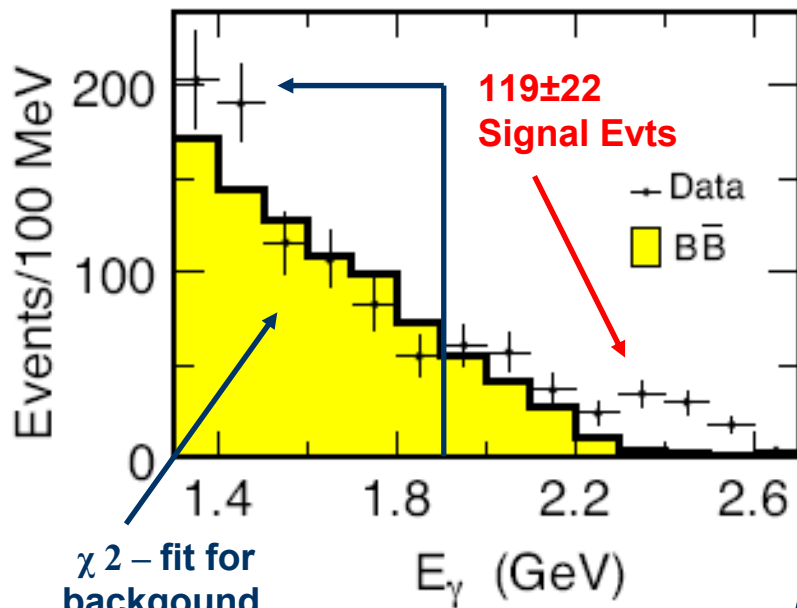


Signal and BB background determined from fit to m_{ES} distribution in bins of photon energy:

$$m_{ES} = \sqrt{(E_{beam}^*)^2 - P_{Breco}^2}$$

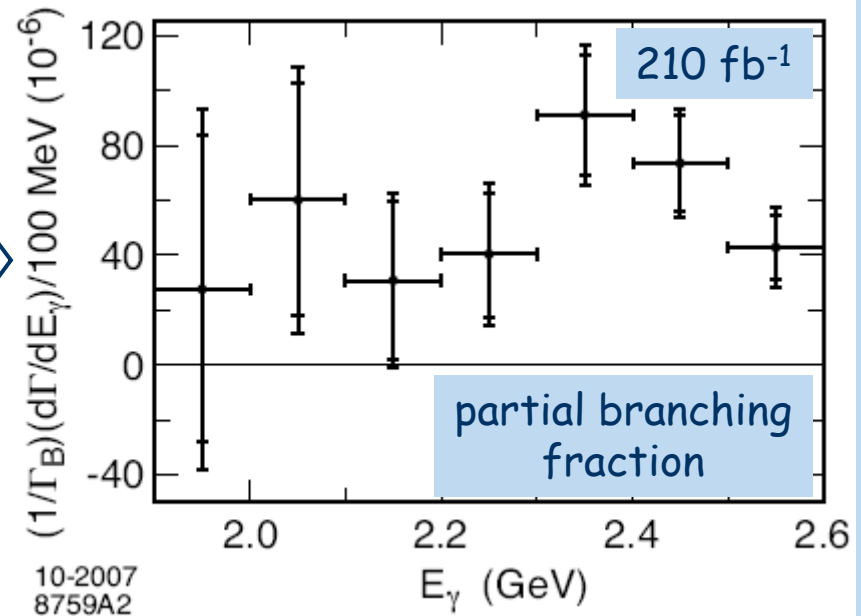
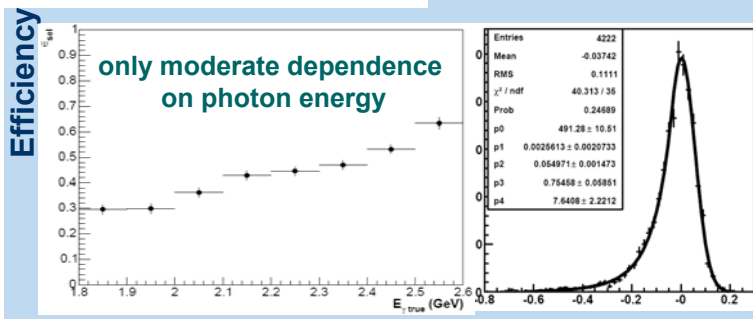
Phys.Rev.D77, 051103 (2008)

$B \rightarrow X_s \gamma : E_\gamma$ spectrum



χ^2 - fit for background normalisation

resolution and efficiency correction



Branching fraction ($E_\gamma > 1.9$ GeV):

$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.66 \pm 0.85_{\text{stat}} \pm 0.60_{\text{syst}}) \times 10^{-4}$$

CP asymmetry:

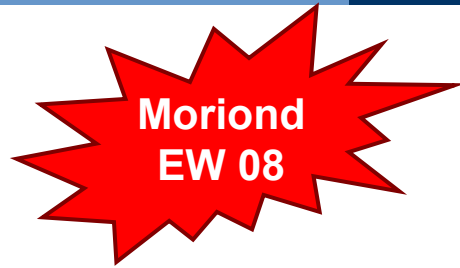
$$A_{CP} = 0.10 \pm 0.18_{\text{stat}} \pm 0.05_{\text{syst}}$$

Isospin asymmetry:

$$\Delta_{0-} = -0.06 \pm 0.15_{\text{stat}} \pm 0.07_{\text{syst}}$$

New Belle measurement

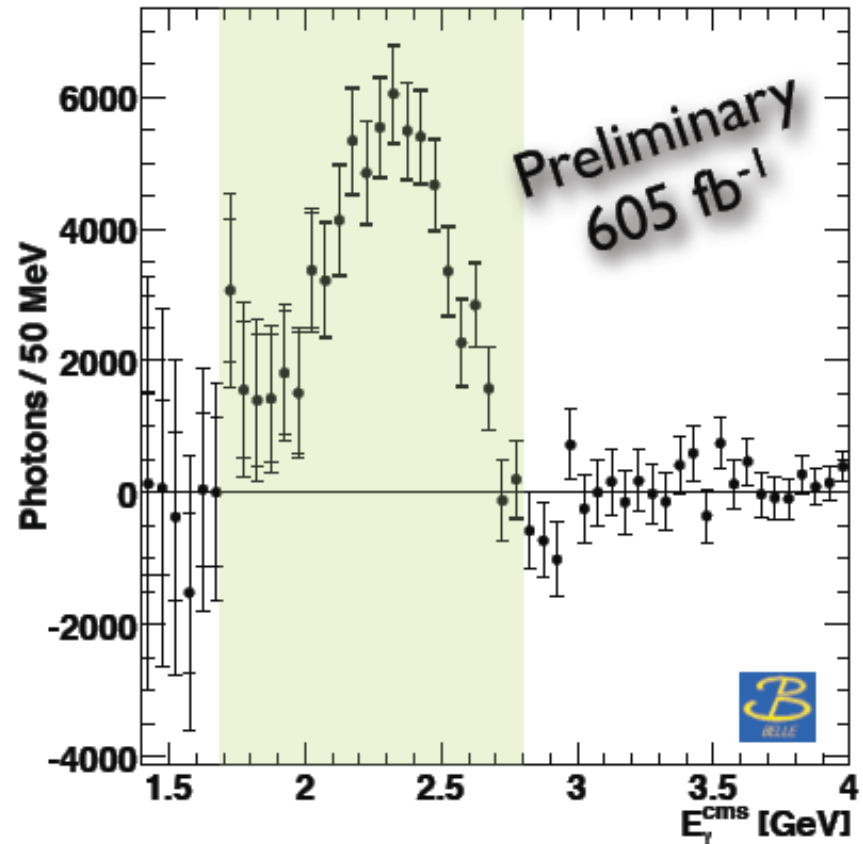
3-7 times larger data sample compared to existing measurements!



- X_s system ignored
- only photon reconstructed
- Pros
 - No uncertainty through X_s fragmentation model
 - theoretically clean
- Cons
 - very large background \rightarrow continuum
 - E_γ^* measurement in $Y(4s)$ frame

Branching fraction:

E(cut) [GeV]	PBF [10 ⁻⁴]
1.70	3.31 ± 0.16 ± 0.37 ± 0.01
1.80	3.24 ± 0.15 ± 0.24 ± 0.01
1.90	3.12 ± 0.14 ± 0.16 ± 0.02
2.00	2.94 ± 0.13 ± 0.12 ± 0.02
2.10	2.62 ± 0.12 ± 0.10 ± 0.05



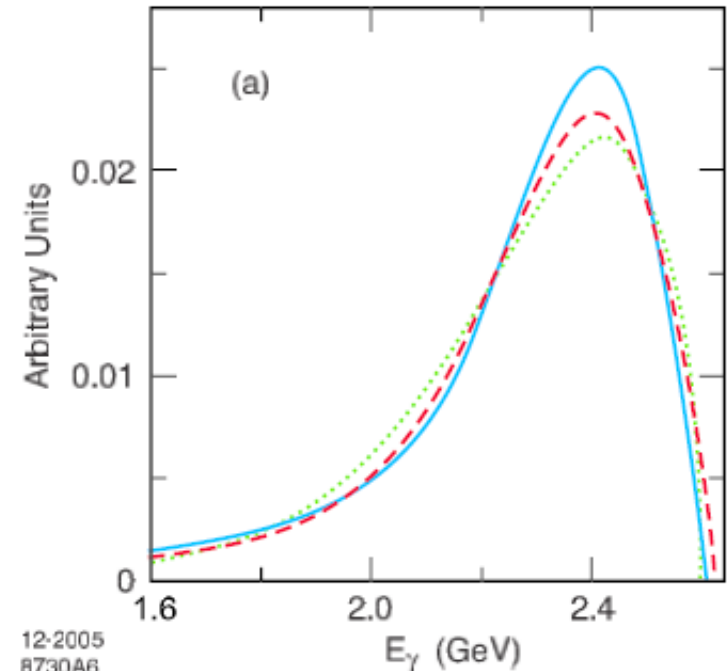
World average for $BR(B \rightarrow X_s \gamma)$

- Partial branching fractions are measured above different photon energies
- Need to be extrapolated to $E_\gamma > 1.6$ GeV to compare with theory
- Extrapolation factors based on HQE fit to $b \rightarrow c\ell\nu$ and $b \rightarrow s\gamma$ moments

Branching fractions (10^{-4})

Mode	Reported \mathcal{B}	E_{\min}	\mathcal{B} at E_{\min}
CLEO Inc. [5]	$321 \pm 43 \pm 27^{+18}_{-10}$	2.0	$306 \pm 41 \pm 26$
Belle Semi.[6]	$336 \pm 53 \pm 42^{+50}_{-54}$	2.24	—
BABAR Semi.[7]	$327 \pm 18^{+55+4}_{-40-9}$	1.9	$327 \pm 18^{+55+4}_{-40-9}$
BABAR Inc. [8]	—	1.9	$367 \pm 29 \pm 34 \pm 29$
BABAR Full [3]	$366 \pm 85 \pm 60$	1.9	$366 \pm 85 \pm 60$
Belle Inc.[4]	$332 \pm 16 \pm 37 \pm 1$	1.7	$332 \pm 16 \pm 37 \pm 1$

photon energy spectrum
constrained with m_b and μ_π^2



SM prediction:

$3.15 \pm 0.23 \times 10^{-4}$ Misiak et al. (hep-ph/0609232)

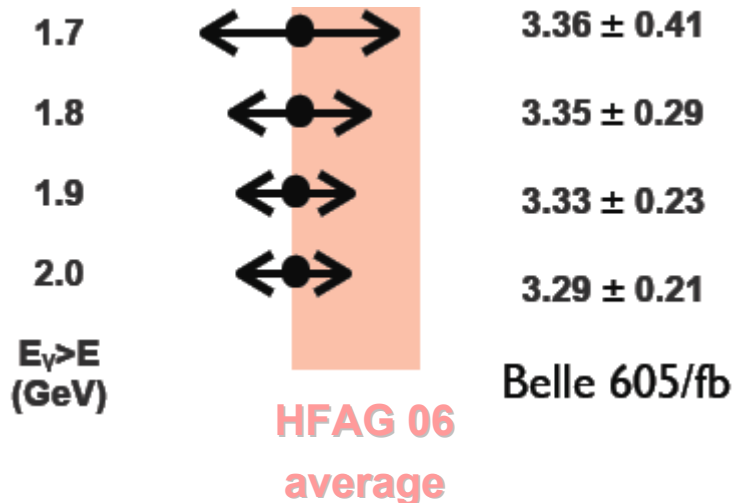
$2.98 \pm 0.26 \times 10^{-4}$ Becher et. al. (hep-ph/0610067)

$3.47 \pm 0.48 \times 10^{-4}$ Andersen et al. (hep-ph/0609250)

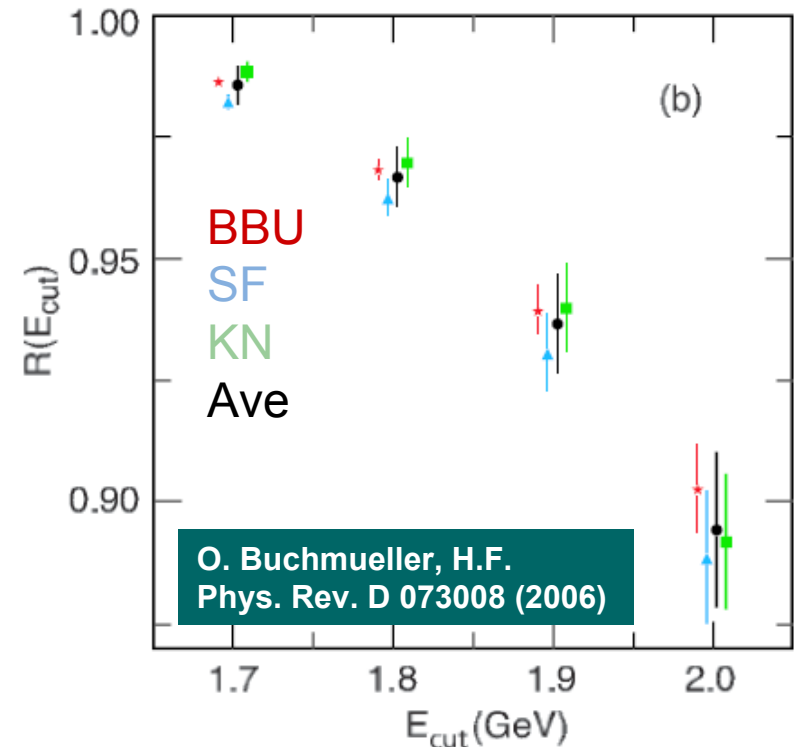
World average for $BR(B \rightarrow X_s \gamma)$

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Application of extrapolation factors to new Belle analysis:



Extrapolation factors for BF



**Consistent results
when extrapolating
from different E_{\min}**

Summary of measurements

CLEO Phys.Rev.Lett.87,251807(2001)
 $BR(B \rightarrow X_s \gamma) = (3.29 \pm 0.53) \cdot 10^{-4}$ (9.1 fb⁻¹)

Belle Semi Phys.Lett.B511:151(2001)
 $BR(B \rightarrow X_s \gamma) = (3.29 \pm 0.53) \cdot 10^{-4}$ (5.8 fb⁻¹)

BaBar Semi Phys.Rev.D72:052004(2005)
 $BR(B \rightarrow X_s \gamma) = (3.29^{+0.62}_{-0.50}) \cdot 10^{-4}$ (81.5 fb⁻¹)

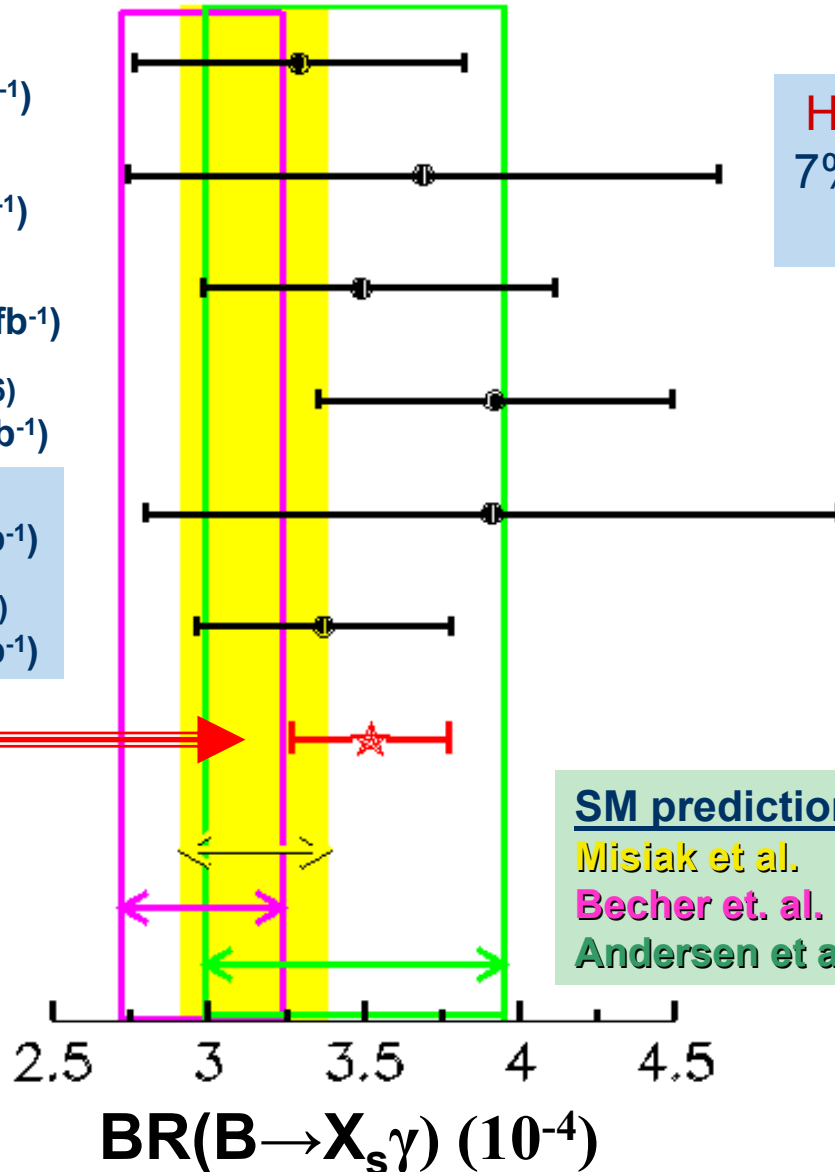
BaBar Incl Phys.Rev.Lett.97:171803(2006)
 $BR(B \rightarrow X_s \gamma) = (3.92 \pm 0.56) \cdot 10^{-4}$ (81.5 fb⁻¹)

BaBar Full Phys.Rev.D77:051103(2008)
 $BR(B \rightarrow X_s \gamma) = (3.91 \pm 1.11) \cdot 10^{-4}$ (210 fb⁻¹)

BELLE Incl (A. Limosani, Moriond EW08)
 $BR(B \rightarrow X_s \gamma) = (3.37 \pm 0.41) \cdot 10^{-4}$ (605 fb⁻¹)

HFAG Average 08 (preliminary)
 $BR(B \rightarrow X_s \gamma) = (3.52 \pm 0.25) \cdot 10^{-4}$

Very good agreement between experiments and analysis methods!



HFAG average:
 7% experimental uncertainty

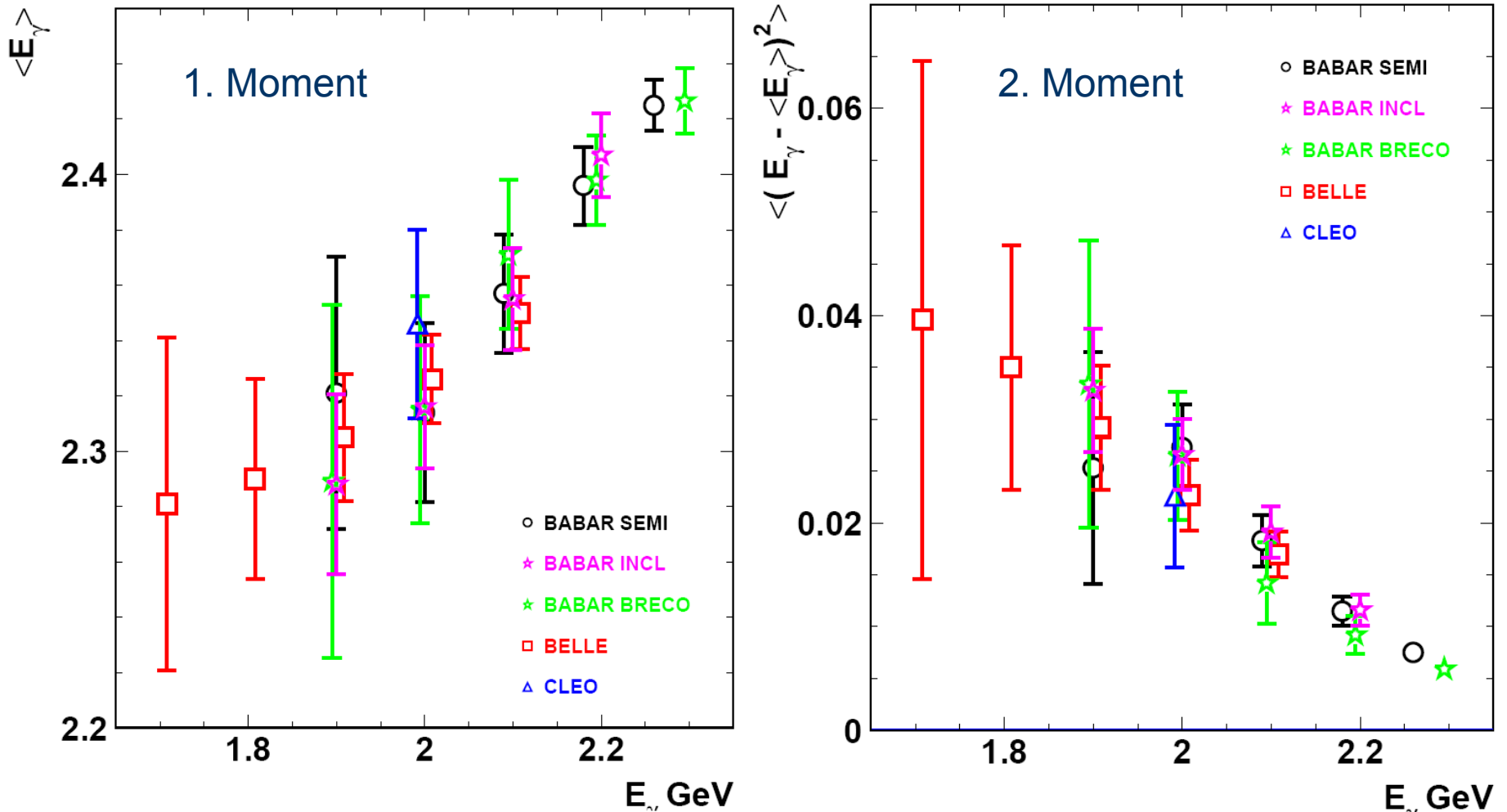
SM predictions:

Misiak et al. (hep-ph/0609232)

Becher et. al. (hep-ph/0610067)

Andersen et al. (hep-ph/0609250)

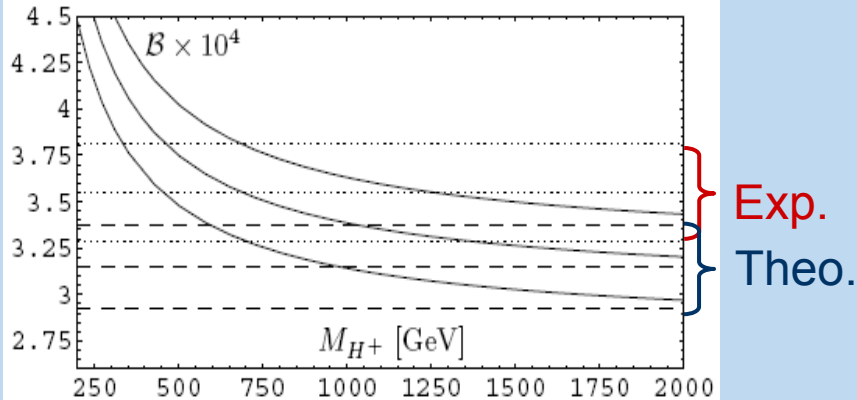
Summary of measurements



Very good agreement between experiments and analysis methods!

Constraint on 2HDM (type II)

BF(B → X_s γ) dependence on M_{H±}



Misiak et. al, Phys.Rev.Lett.98:022002,2007
& Gambino, Misiak, private communication

BF(B → τν) dependence on M_{H±} and tanβ:

$$BR_{2HDM} = BR_{SM} (1 - (\tan\beta m_B/m_{H^\pm})^2)^2$$

Hou, Phys.Rev.D48:2342-2344,1993

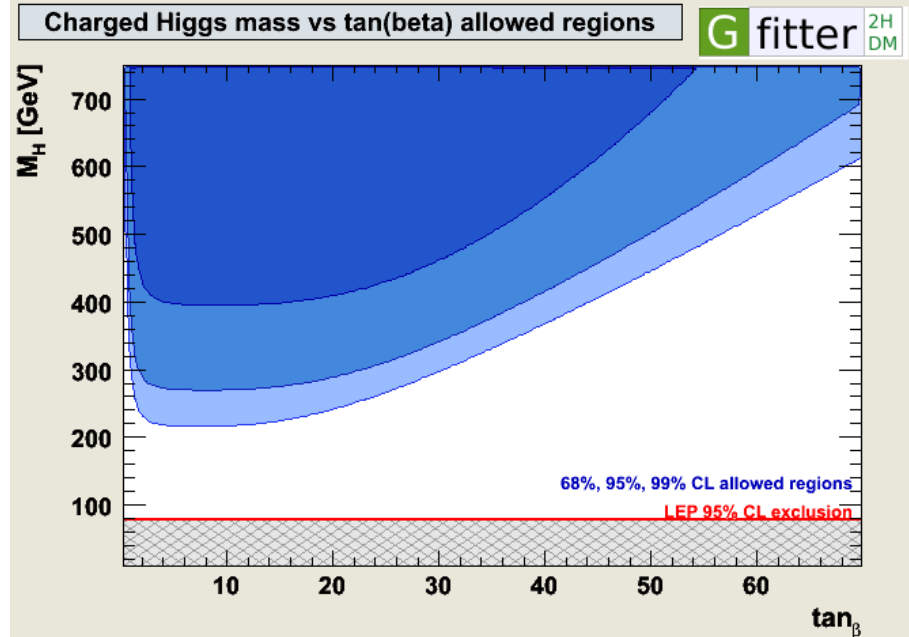
Similar for B → Dτν and K → μν

Experimental measurements:

$$BF(B \rightarrow X_s \gamma) = (3.55 \pm 0.26) 10^{-4}$$

$$BF(B \rightarrow \tau\nu) = (1.41 \pm 0.43) 10^{-4}$$

Combined fit to BF(B → X_s γ) and BF(B → τν) measurements:



Gfitter Project:

H.F., M.Göbel, J.Haller, A.Höcker, K. Mönig, J.Stelzer
<https://twiki.cern.ch/twiki/bin/view/Gfitter/WebHome>

CMSSM (mSugra) parameter space

Importance of $B \rightarrow X_s \gamma$:

Exp: $(3.55 \pm 0.26) 10^{-4}$

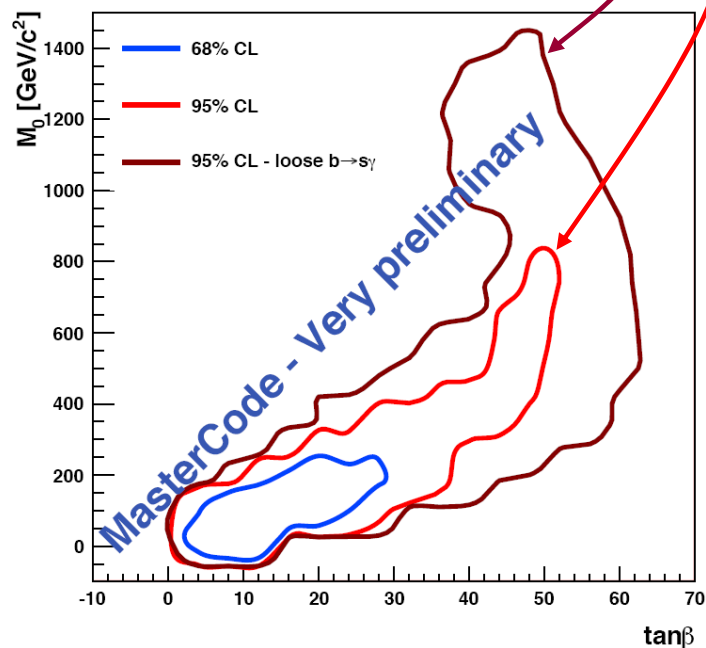
SM : $(3.15 \pm 0.23) 10^{-4}$

→ **Exp/SM = 1.127 ± 0.12**

Uncert. x3: 1.127 ± 0.36

- **5 free parameters**

- M_0 – common scalar mass (at GUT scale)
- $M_{1/2}$ – common gaugino mass (at GUT scale)
- A_0 – tri-linear mass parameter (at GUT scale)
- $\tan\beta$ – ratio of Higgs vacuum expectation values
- $\text{sign}(\mu)$ – sign of Higgs mixing parameter



- uses a total of ca. **30** elektroweak precision observables **and** low-energy observables (e.g. $B \rightarrow X_s \gamma$, $B \rightarrow \tau \nu$, etc.) to constrain CMSSM parameter space
- sampling of parameter space via Markov Chain Monte Carlo

Collaboration of experiment and theory
Phys.Lett.B657:87-94,2007

See also talk by Frederic Ronga:
„Prediction for the lightest Higgs Boson Mass
in the framework of CMSSM“
Rencontres de Physique de la Vallee d'Aoste 08

V_{cb}

from inclusive decay distributions

- can also be determined from exclusive $B \rightarrow D^*$ V_{cb} and $B \rightarrow D$ V_{cb} decays
- still sizable uncertainties from FormFactors (theory)
- Valuable to compare incl. and excl. measurements
- very different theory uncertainties

Fit to Moments of Inclusive Decay Distributions

Heavy Quark Expansions connect the inclusive decay width to $|V_{cb}|$:

Γ_{SL} proportional to $|V_{cb}|^2$, but **perturbative** and **non-perturbative** corrections to free quark decay needed \rightarrow double expansion in α_s and $1/m_b$

$$\Gamma_{clv} = \frac{G_F m_b^5}{192\pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{pert} A_{nonpert} \cong |V_{cb}|^2 f_{OPE}(m_b, m_c, a_i)$$

4 parameters at order α_s^2 and $1/m_b^3$

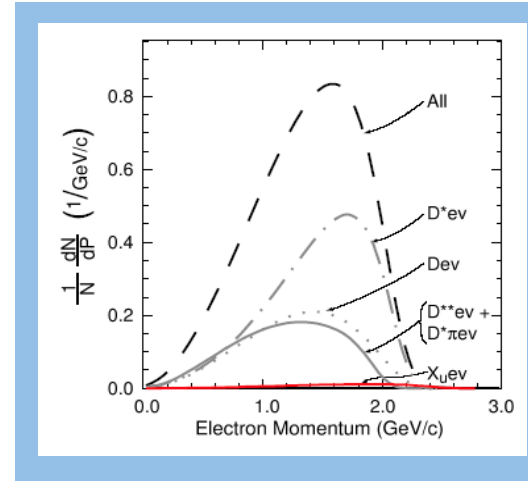
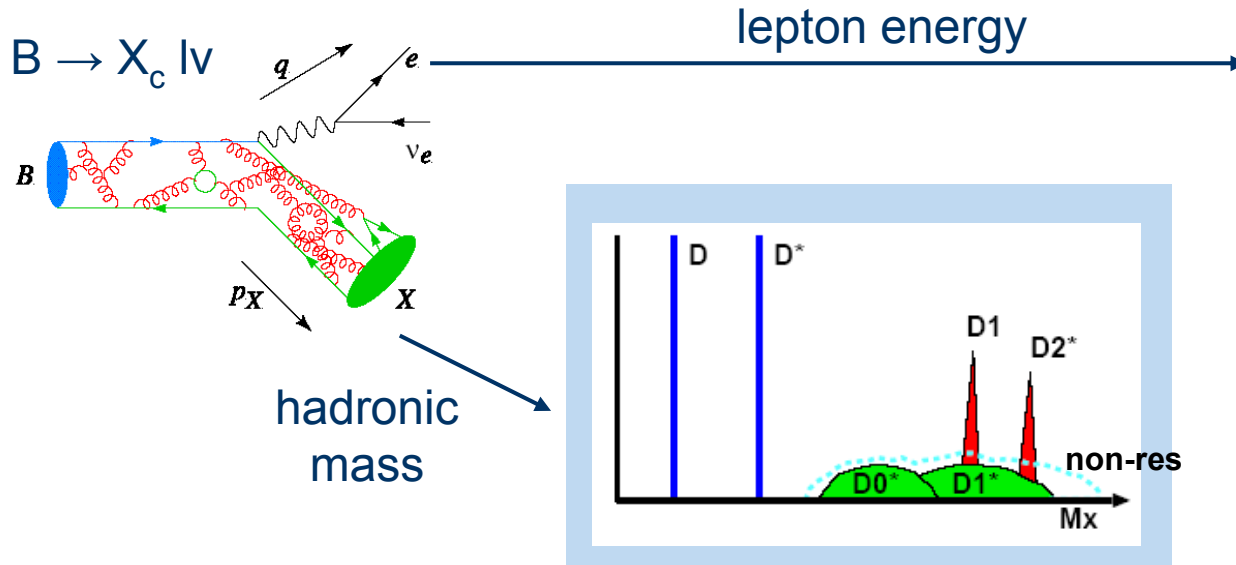
Need to determine non-perturbative parameters!

\rightarrow Use moments of inclusive distributions where **same** parameters appear:

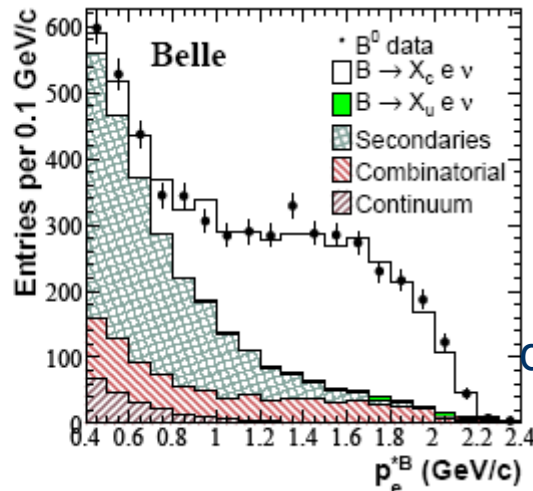
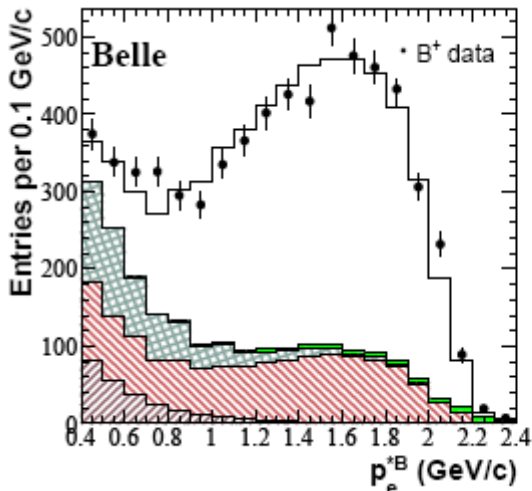
$$\langle X^n \rangle (E_{cut}) = \frac{\int (X - X^0)^n \frac{d\Gamma}{dX} dX}{\int \frac{d\Gamma}{dX} dX} \Bigg|_{E_l > E_{cut}} \cong f'_{OPE}(m_b, m_c, a_i)$$

- Hadronic Mass distribution $\langle M_X^n \rangle \rightarrow \langle M_X \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$
- Lepton Energy spectrum $\langle E_\ell^n \rangle \rightarrow \langle E_\ell \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$
- Photon Energy spectrum $\langle E_\gamma^n \rangle \rightarrow \langle E_\gamma \rangle (m_b, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s)$.

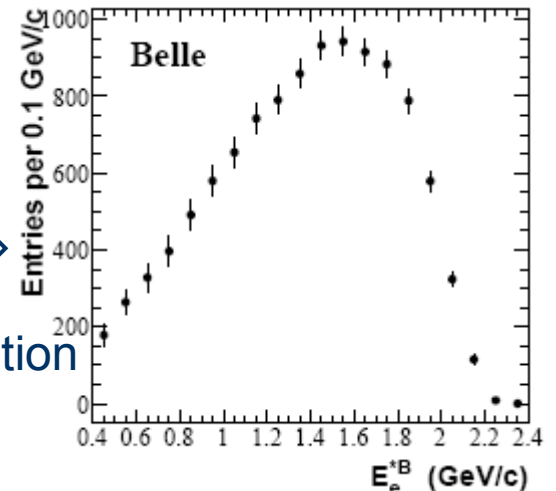
Observables



Belle lepton spectrum:



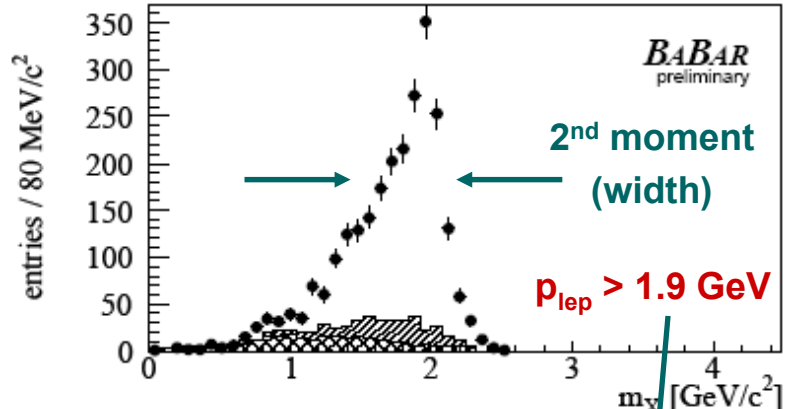
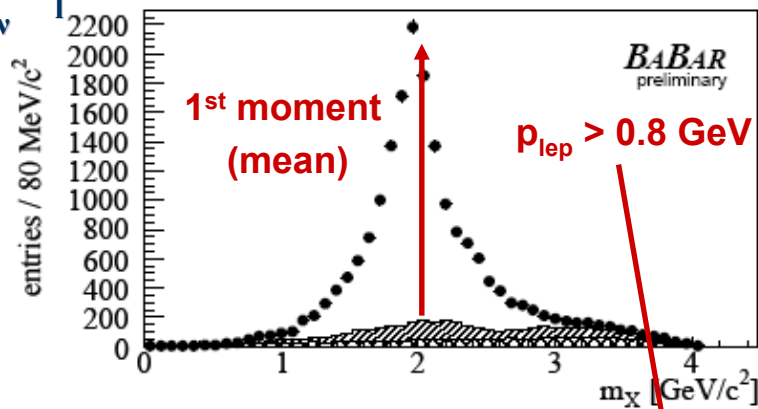
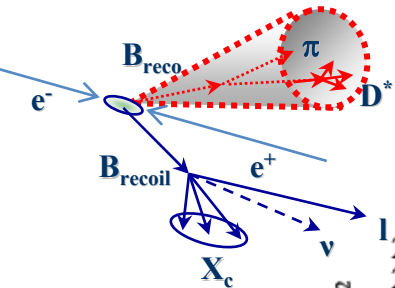
deconvolution



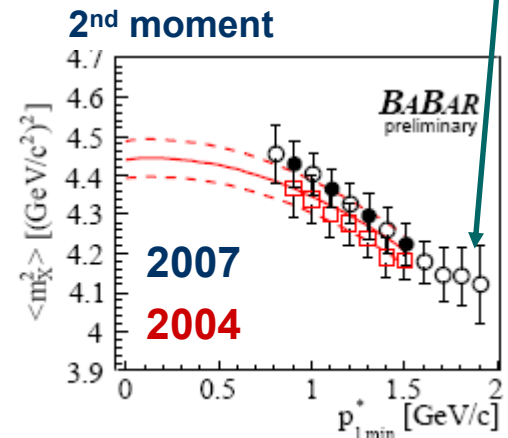
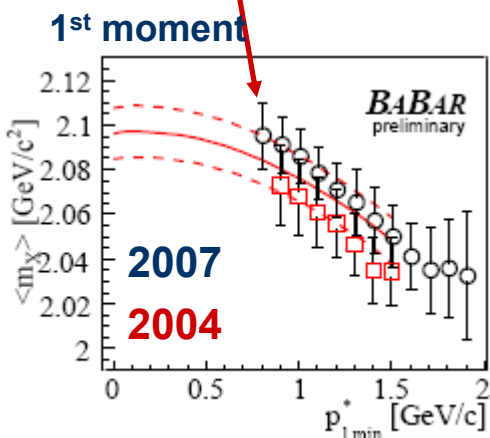
Hadronic mass moments

New BaBar measurement!
Full reconstruction tag

Based on 232M BB events
arXiv:0707.2670 [hep-ex]



Moments as function of minimum lepton momentum: (comparison with previous measurement)



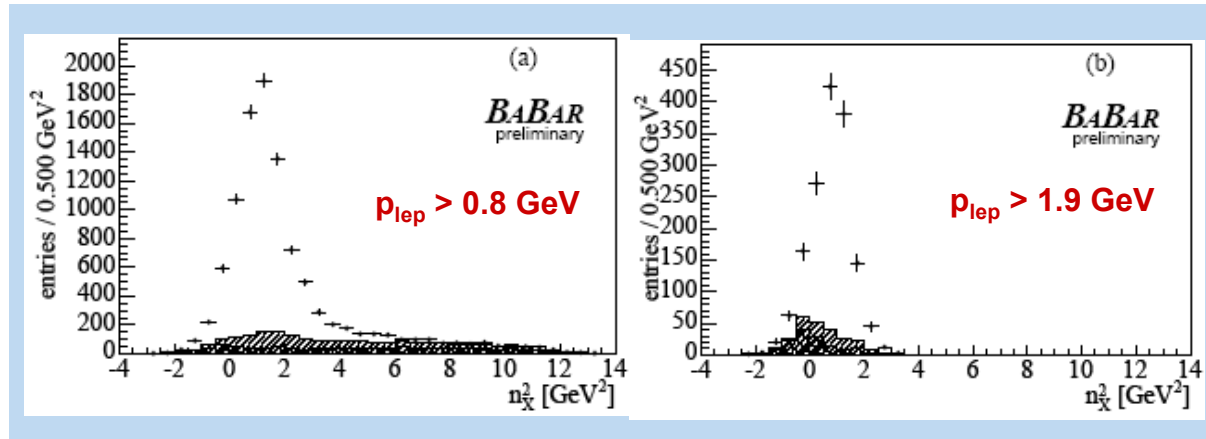
+ higher order moments

Mixed Hadronic Mass and Energy Moments

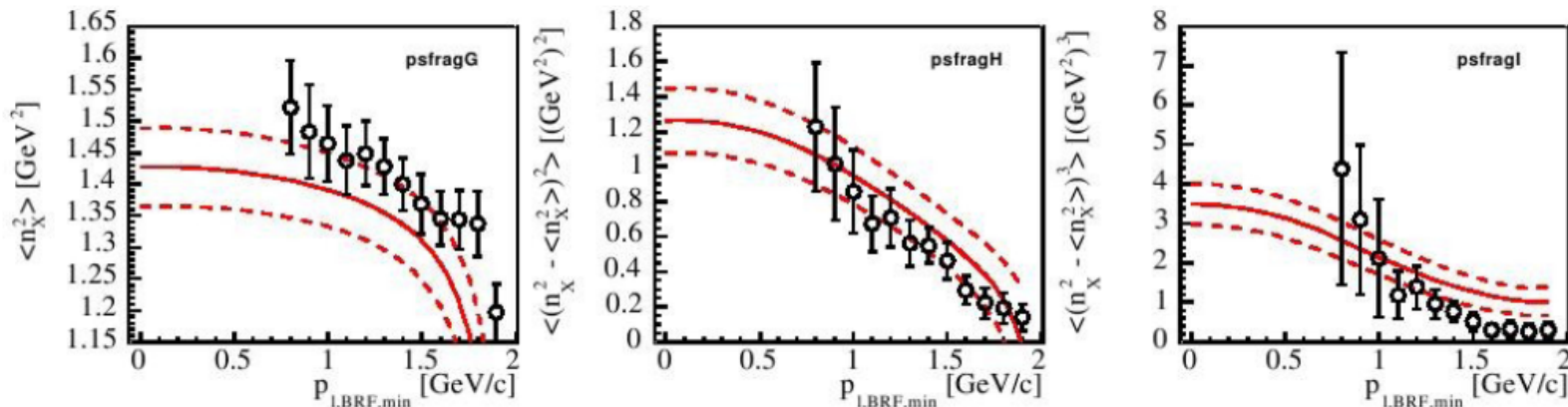
In addition modified moments: $\mathcal{N}_X^2 = M_X^2 - 2\tilde{\Lambda}E_X + \tilde{\Lambda}^2$ ($\Lambda=0.65$ GeV)

combination of hadronic Mass and Energy Moments

→ higher sensitivity to higher order parameters



Preliminary comparison with theo. calculations:

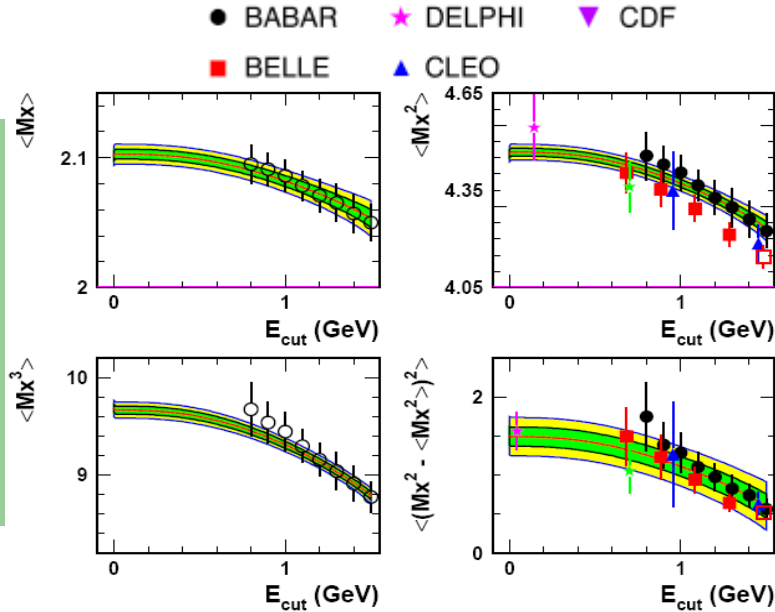


Inclusive $|V_{cb}|$ - Fit to Moments

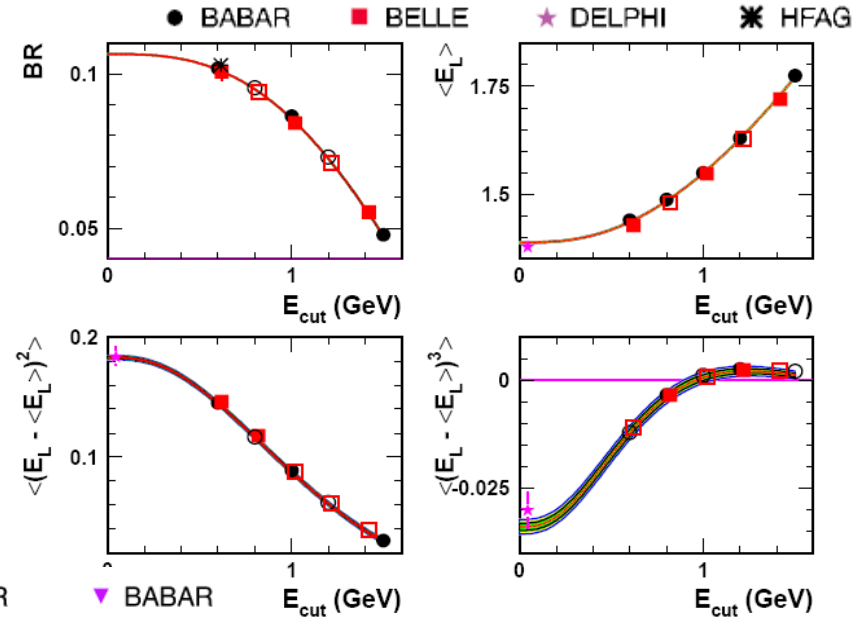
Based on calculations in kinetic scheme:

Benson, Bigi, Mannel & Uraltsev, hep-ph/0410080
 Gambino & Uraltsev, hep-ph/0401063
 Benson, Bigi & Uraltsev, hep-ph/0410080

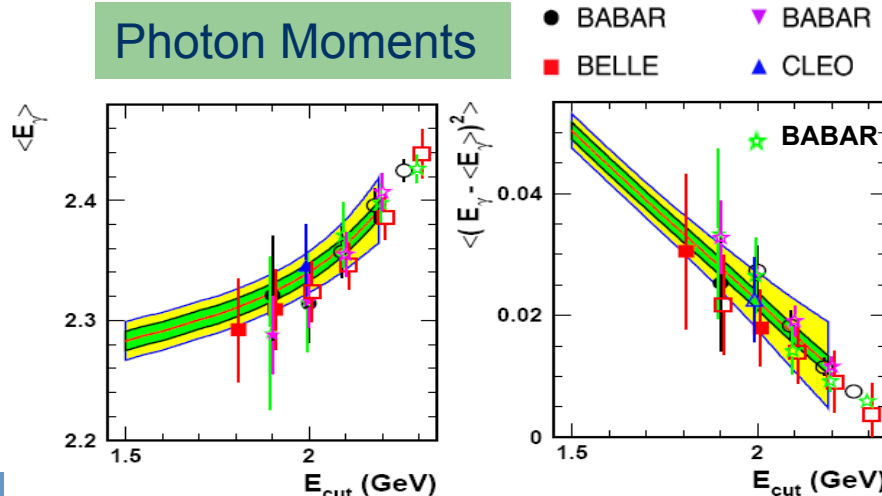
Hadron Moments



Lepton Moments



Photon Moments



Measurements are correlated!

O. Buchmüller, H.F.
 Phys. Rev. D 073008 (2006)
 update for V_{xb} 07, Heidelberg

Inclusive $|V_{cb}|$ Determination

Result of the combined fit in kinetic scheme:

	exp	HQE	Γ_{SL}
$ V_{cb} =$	$(42.04 \pm 0.19 \pm 0.28 \pm 0.59) 10^{-3}$		
$m_b =$	$4.597 \pm 0.021 \pm 0.027$	GeV	
$m_c =$	$1.163 \pm 0.032 \pm 0.039$	GeV	
$\mu_\pi^2 =$	$0.434 \pm 0.016 \pm 0.029$	GeV^2	
$\mu_G^2 =$	$0.267 \pm 0.015 \pm 0.036$	GeV^2	
$\rho_D^3 =$	$0.203 \pm 0.009 \pm 0.018$	GeV^3	
$\rho_{LS}^3 =$	$-0.184 \pm 0.052 \pm 0.068$	GeV^3	
$\text{BR}_{clv} =$	$10.64 \pm 0.09 \pm 0.07$	$\%$	

$|V_{cb}|$ @ 2%
 $m_b < 1\%$
 m_c @ 5%

Comparison of m_b and m_{top} :

$$m_{top} = 172.6 \pm 1.4 \text{ GeV} \quad (0.8\%)$$

$$m_b = 4.597 \pm 0.034 \text{ GeV} \quad (0.7\%)$$

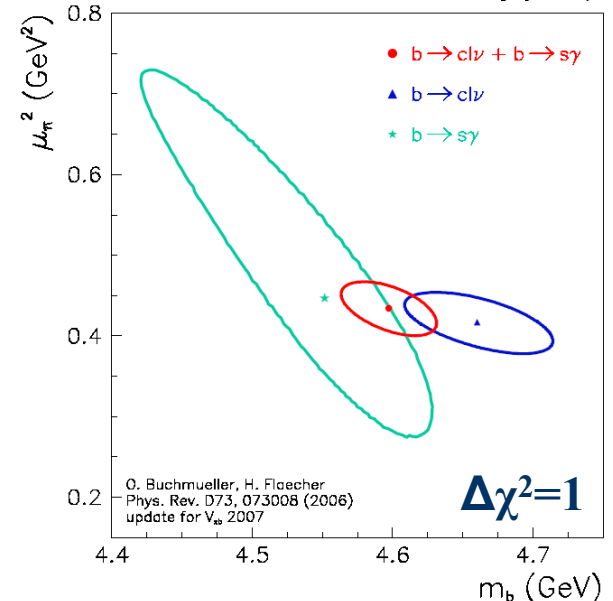
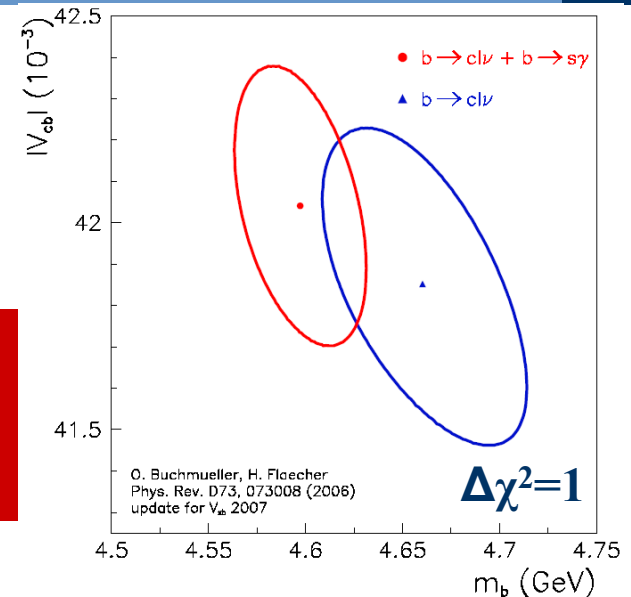
In \overline{MS} scheme:

$$m_b(m_b) = 4.21 \pm 0.04 \text{ GeV}$$

$$m_c(m_c) = 1.26 \pm 0.06 \text{ GeV}$$

Thanks to N.Uraltsev

O. Buchmueller, H.F., Phys. Rev. D 073008 (2006)
 update for V_{cb} 07, Heidelberg



Inclusive $|V_{cb}|$ Determination

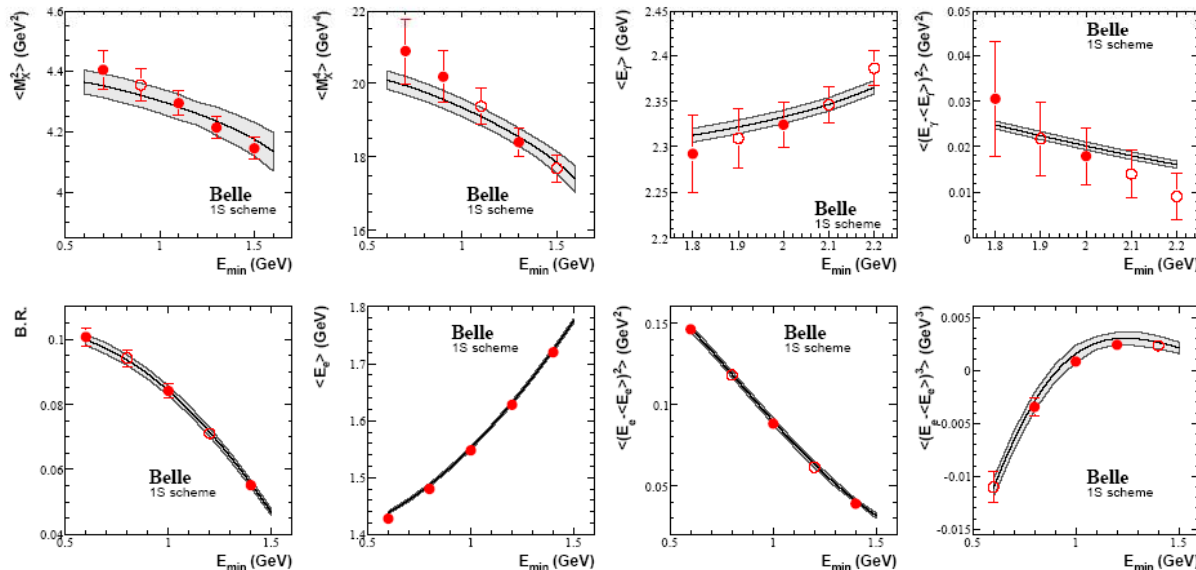
Belle's OPE fit (1S)

Belle preliminary, update of ICHEP'06

- 1S scheme parameters: $m_b^{1S}, \lambda_1, \tau_1, \tau_2, \tau_3, \rho_1 + |V_{cb}|$
- 7 m_X moments, 11 E_e moments, 3 partial \mathcal{B} , 4 E_γ moments

$$|V_{cb}| = (41.56 \pm 0.68_{\text{fit}} \pm 0.08_{\tau_B}) \times 10^{-3} \quad (\chi^2/ndf = 7.3/18)$$

$$|V_{cb}| = (41.52 \pm 0.69_{\text{fit}} \pm 0.08_{\tau_B} \pm 0.58_{\text{th}}) \times 10^{-3} \quad (\text{Belle kinetic fit})$$



$$\langle m_X^2 \rangle, \langle m_X^4 \rangle, \langle E_\gamma \rangle, \langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle$$

$$\Delta\mathcal{B}, \langle M_n^\ell \rangle$$

New

HQE Fit & $|V_{cb}|$ - Summary

>100 moment measurements and many HQE fit results...

OB & HF Phys.Rev.D73:073008,2006

$$|V_{cb}| = 42.0 \pm 0.2_{\text{exp}} \pm 0.3_{\text{HQE}} \pm 0.6_{\Gamma_{\text{SL}}}$$

BABAR Phys.Rev.Lett.93:011803,2004

$$|V_{cb}| = 41.7 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.6_{\Gamma_{\text{SL}}}^*$$

DELPHI Eur.Phys.J.C45:35-59,2006

$$|V_{cb}| = 41.9 \pm 0.6_{\text{exp}} \pm 0.6_{\text{FIT}} \pm 0.6_{\Gamma_{\text{SL}}}^*$$

BELLE arXiv 0803.2158

$$|V_{cb}| = 41.5 \pm 0.7_{\text{fit}} \pm 0.1_{\tau} \pm 0.6_{\Gamma_{\text{SL}}}$$

Bauer et al. Phys.Rev.D70:094017,2004

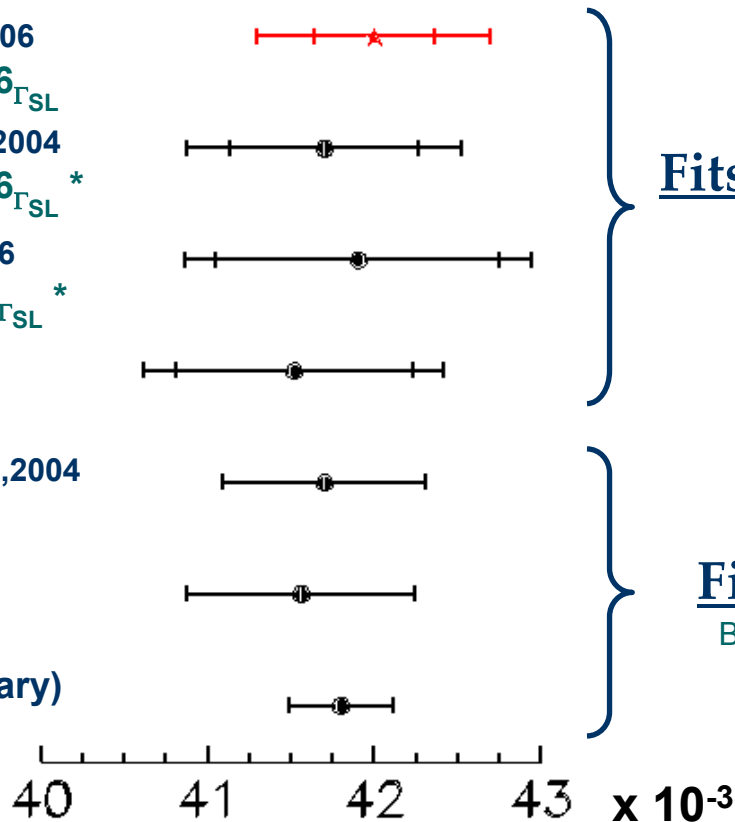
$$|V_{cb}| = 41.7 \pm 0.6_{\text{fit}} \pm 0.1_{\tau}^*$$

BELLE arXiv 0803.2158

$$|V_{cb}| = 41.6 \pm 0.7_{\text{fit}} \pm 0.1_{\tau}$$

BELLE Global V_{xb} 07 (preliminary)

$$|V_{cb}| = 41.8 \pm 0.3_{\text{fit}} \pm 0.1_{\tau}$$



Fits in kinetic scheme

Based on hep-ph/0401063

Fits in 1S scheme

Based on hep-ph/0408002

* rescaled to common lifetime

$$\tau_B = 1.585 \pm 0.007 \text{ ps}$$

all $|V_{cb}|$ values $\times 10^{-3}$

Very good agreement

$|V_{cb}|$ @ <2%

But: comparison with exclusive $|V_{cb}|$

$$(38.8 \pm 0.6_{\text{exp}} \pm 1.0_{\text{theo}}) 10^{-3}$$

incl. - excl. = 3.2 ± 1.3 (2.5σ)

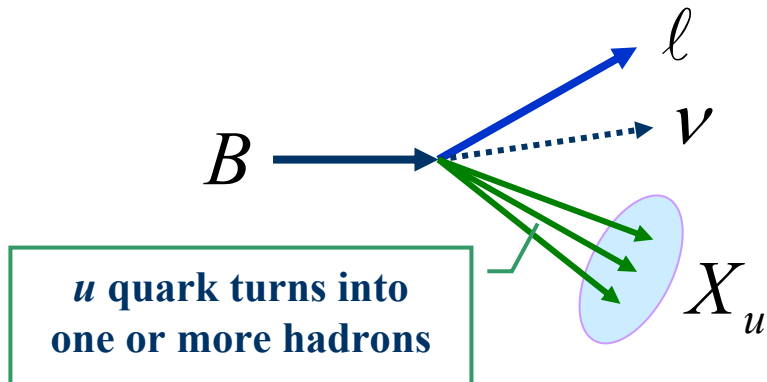
$|V_{ub}|$

from inclusive decay distributions

- can also be determined from exclusive $B \rightarrow \pi l\nu$ and $B \rightarrow \rho l\nu$ decays
- still sizeable uncertainties from FormFactors (theory)
- $B \rightarrow \pi$ FF improved from lattice

Inclusive $b \rightarrow ul\nu$: Strategies

- Very large background from $b \rightarrow cl\nu$ decays: $|V_{cb}|^2 \gg |V_{ub}|^2 \sim 50!$
- We use 3 variables to describe $B \rightarrow Xl\nu$ decays:



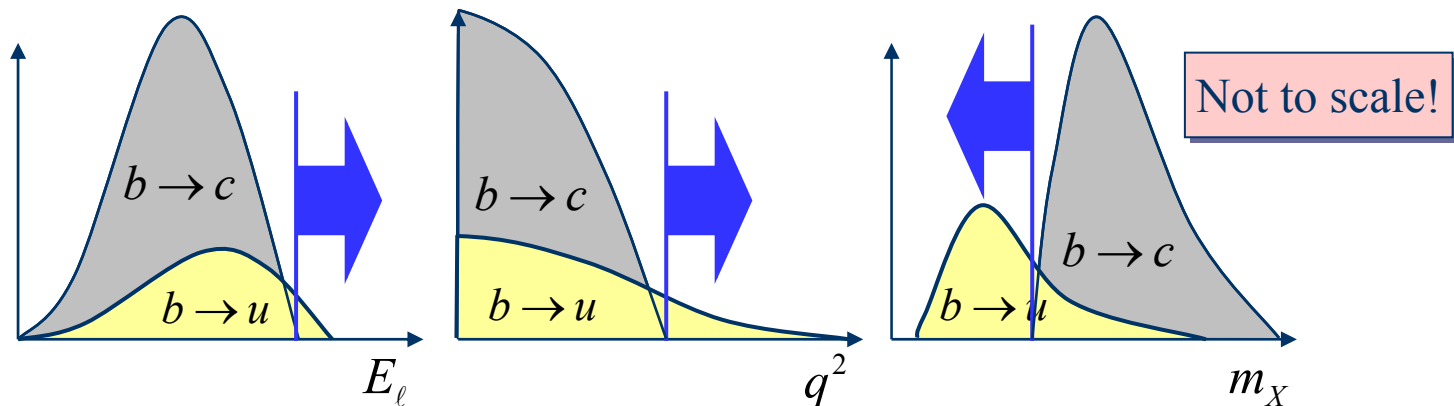
E_ℓ = lepton energy

q^2 = lepton-neutrino mass squared

m_X = hadron system mass

Combine cuts on these variables to maximise phase space and minimise theory uncertainty

- Signal events have smaller $m_X \rightarrow$ larger E_ℓ and q^2



Inclusive Vub

- $|V_{ub}|$ measurement in different regions of phase space
 - consistency!

$|V_{ub}|$ measurement: $\Gamma(B \rightarrow X_u \ell \nu) \times f_C = |V_{ub}|^2 \zeta_C$

signal fraction surviving cuts

Cut dependent constant (from Theory)

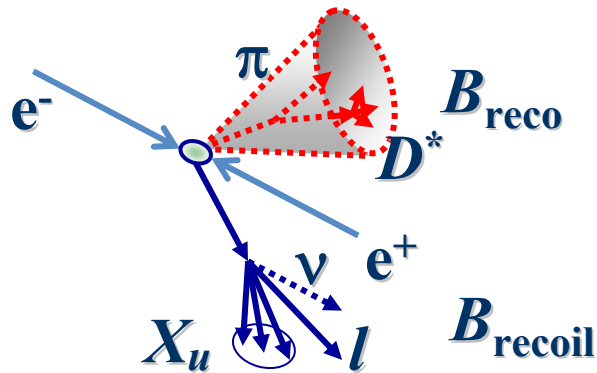
Total rate: $\Gamma(B \rightarrow X_u \ell \nu) \sim |V_{ub}|^2 m_b^5$

largest syst. uncertainty!
Use HQE fit result!

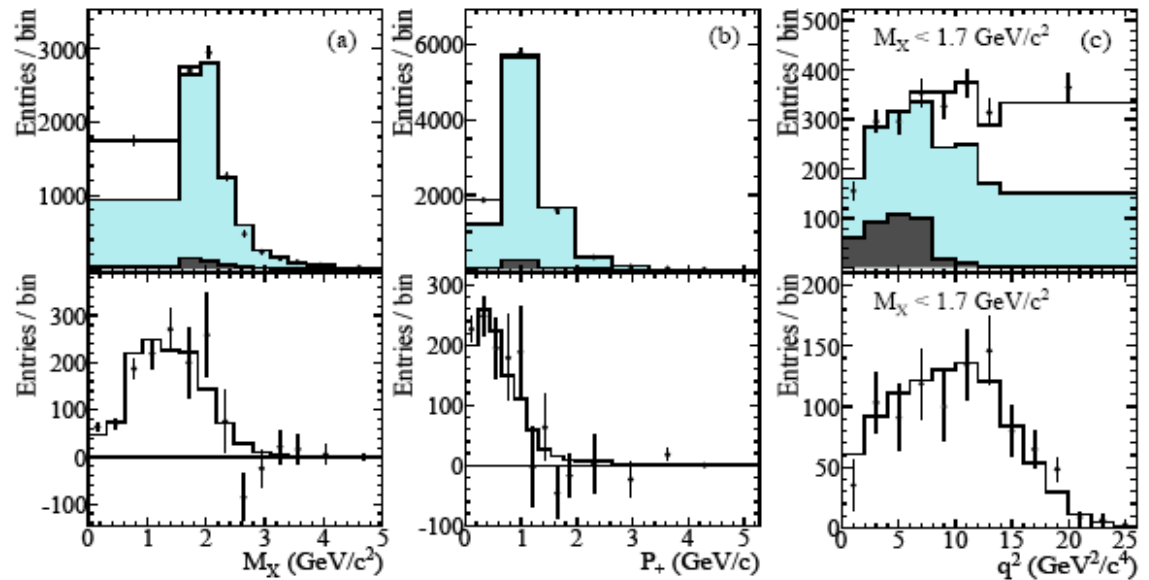
- Connection between $b \rightarrow s\gamma$ and $b \rightarrow ul\nu$
 - restricted kinematics compromise convergence of OPE
 - hadronic physics needs to be encoded in non-perturbative shape function
 - light cone distribution of b-quark (shape function) at leading order the same for $b \rightarrow ul\nu$ and $b \rightarrow s\gamma$ (universal, not process dependent)
 - detailed shape not known, in particular the tail
 - but mean and r.m.s can be constrained from moment measurements in $b \rightarrow cl\nu$, $b \rightarrow s\gamma$

$|V_{ub}|$: Full reconstruction tag

Full reconstruction analysis:



Babar: [arXiv:0708.3702](https://arxiv.org/abs/0708.3702)



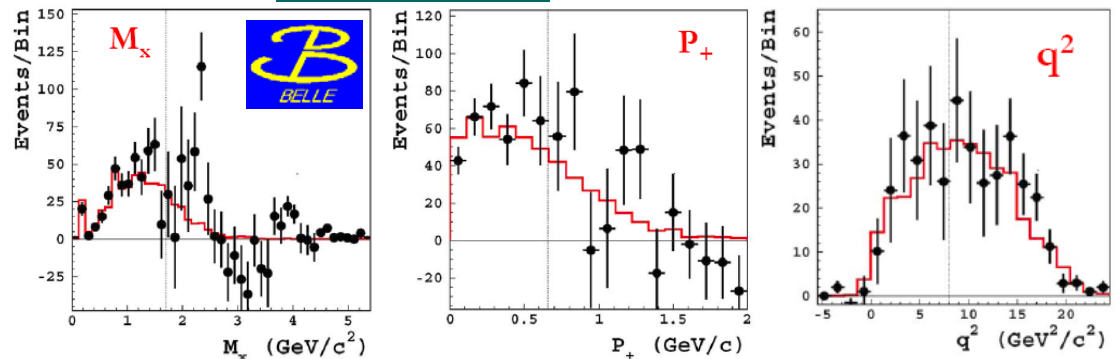
Advantages:

- clean sample
- kinematics known
- B flavour known

Disadvantage:

- low statistics

Belle: [hep-ex/0505088](https://arxiv.org/abs/hep-ex/0505088)



$|V_{ub}|$: Full reconstruction tag

Babar:

arXiv:0708.3702

	Method	N_u	$ V_{ub} \times (10^{-3})$
$M_X < 1.55 \text{ GeV}$	M_X	803 ± 60	$4.27 \pm 0.16 \pm 0.13 \pm 0.30$ [4]
			$4.56 \pm 0.17 \pm 0.14 \pm 0.32$ [5]
$P_+ = E_X - p_X < 0.66$	P_+	633 ± 63	$3.88 \pm 0.19 \pm 0.16 \pm 0.28$ [4]
			$3.99 \pm 0.20 \pm 0.16 \pm 0.24$ [5]
$M_X < 1.7 \text{ GeV}, q^2 > 8 \text{ GeV}^2$	M_X, q^2	562 ± 55	$4.57 \pm 0.22 \pm 0.19 \pm 0.30$ [4]
			$4.64 \pm 0.23 \pm 0.19 \pm 0.25$ [5]
			$4.93 \pm 0.24 \pm 0.20 \pm 0.36$ [6]

[4] Bosch, Lange, Neubert, Paz
Phys.Rev.Lett.93,221801,(2004)
Bosch,Neubert,Paz
Phys.Rev.D72,073006(2005)

[5] Andersen, Gardi
JHEP 0601, 097 (2006)

[6] Bauer, Ligeti, Luke
Phys.Rev.D64,113004(2001)

Around 9% uncertainty
from single analysis

Belle:

Phys.Rev.Lett.95,241801(2005)

$\Delta\Phi$	$ V_{ub} \times 10^3$	stat	syst	$b \rightarrow u$	$b \rightarrow c$	SE	th
M_X/q^2	4.70	5.0	4.4	3.1	2.7	4.2	$+4.8$ -5.2
M_X	4.09	4.6	3.5	3.1	1.1	4.5	$+3.5$ -3.8
P_+	4.19	4.7	4.6	3.2	4.4	5.8	$+3.4$ -3.5

$M_X < 1.7 \text{ GeV}, q^2 > 8 \text{ GeV}^2$

$M_X < 1.7 \text{ GeV}$

$P_+ = E_X - |p_X| < 0.66$

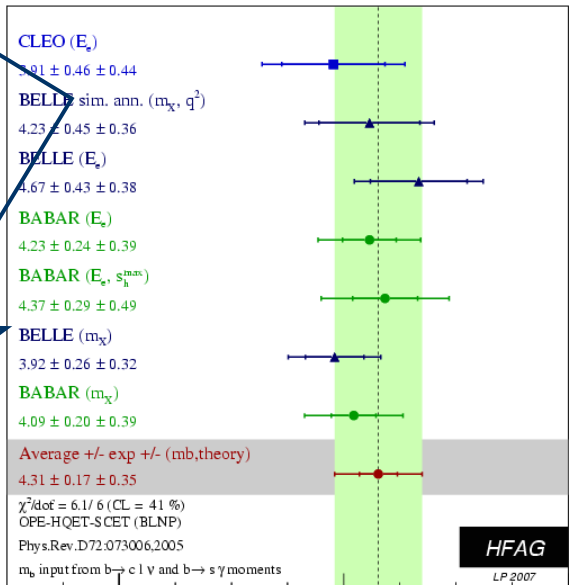
Different phase space acceptances
result in different theory errors!

$|V_{ub}|$ Summary

Great effort on exp. and theo. side over the past few years reduced uncertainty thanks to more precise measurements of heavy quark parameters

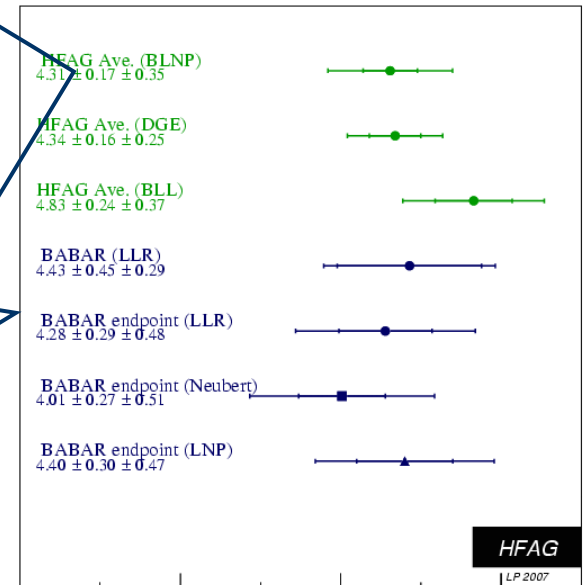
- m_b uncertainty reduced from 60 MeV \rightarrow 35 MeV
- Uncertainty on $|V_{ub}|$ due to HQ Parameters from 8% \rightarrow ~4% - 6%
- **8% total uncertainty (exp + theo)**

Theory: BLNP measurements in different regions of phase space



$|V_{ub}| = (4.31 \pm 0.17 \pm 0.35) \times 10^{-3}$

Many different theoretical calculations



Comparison with exclusive measurement: $|V_{ub}| = 3.17 \pm 0.10^{+0.74}_{-0.44}$ (HPQCD 2007)

incl. - excl. = 1.14 ± 0.84 (1.4σ)

Moments in $B \rightarrow X_u \ell \nu$ decays

arXiv:0801.2985 [hep-ex]

Measure hadronic mass spectrum over full range

OPE as in case for $B \rightarrow X_c \ell \nu$

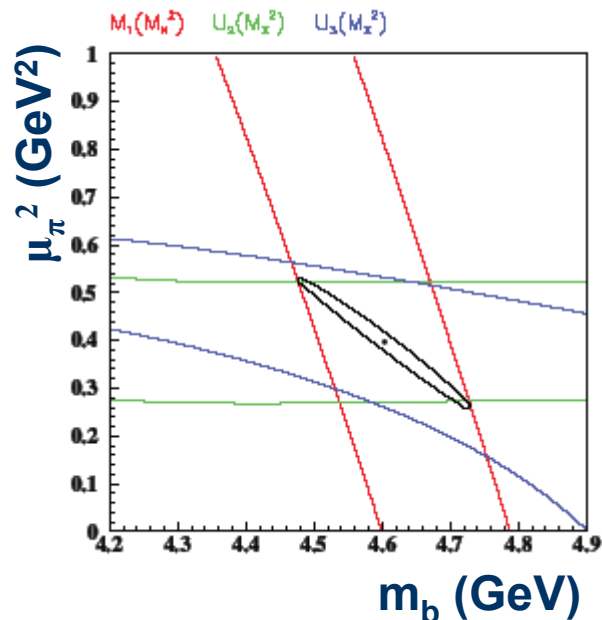
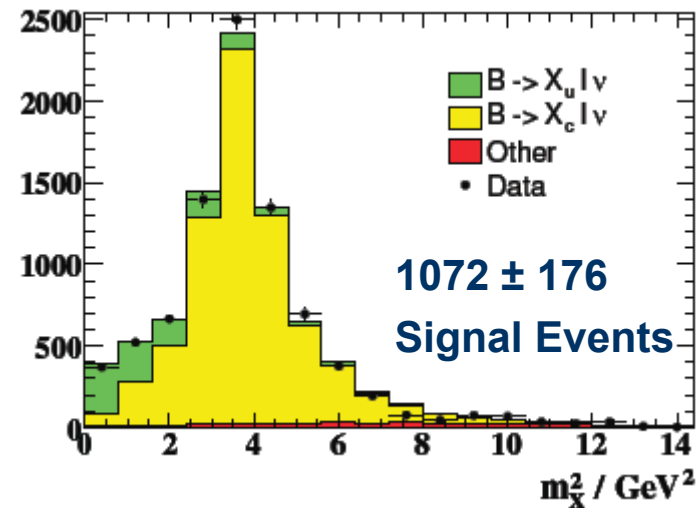
Mass moments related to m_b

$$M_1 = (1.96 \pm 0.34(\text{stat}) \pm 0.53(\text{syst})) \text{ GeV}^2$$

$$U_2 = (1.92 \pm 0.59(\text{stat}) \pm 0.87(\text{syst})) \text{ GeV}^4$$

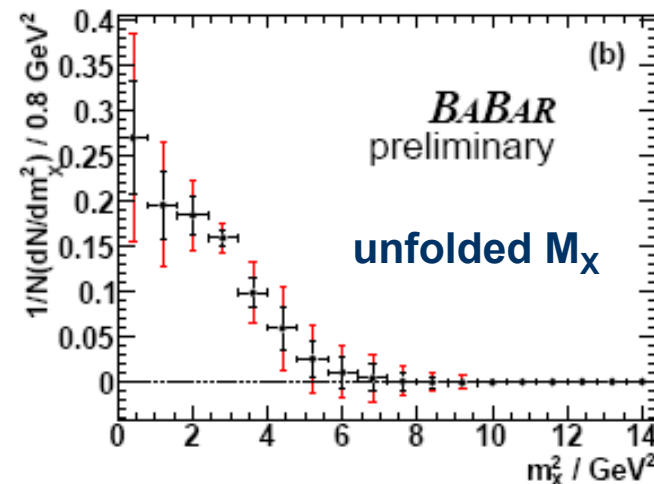
$$U_3 = (1.79 \pm 0.62(\text{stat}) \pm 0.78(\text{syst})) \text{ GeV}^6$$

for $M_X < 6.2 \text{ GeV}$



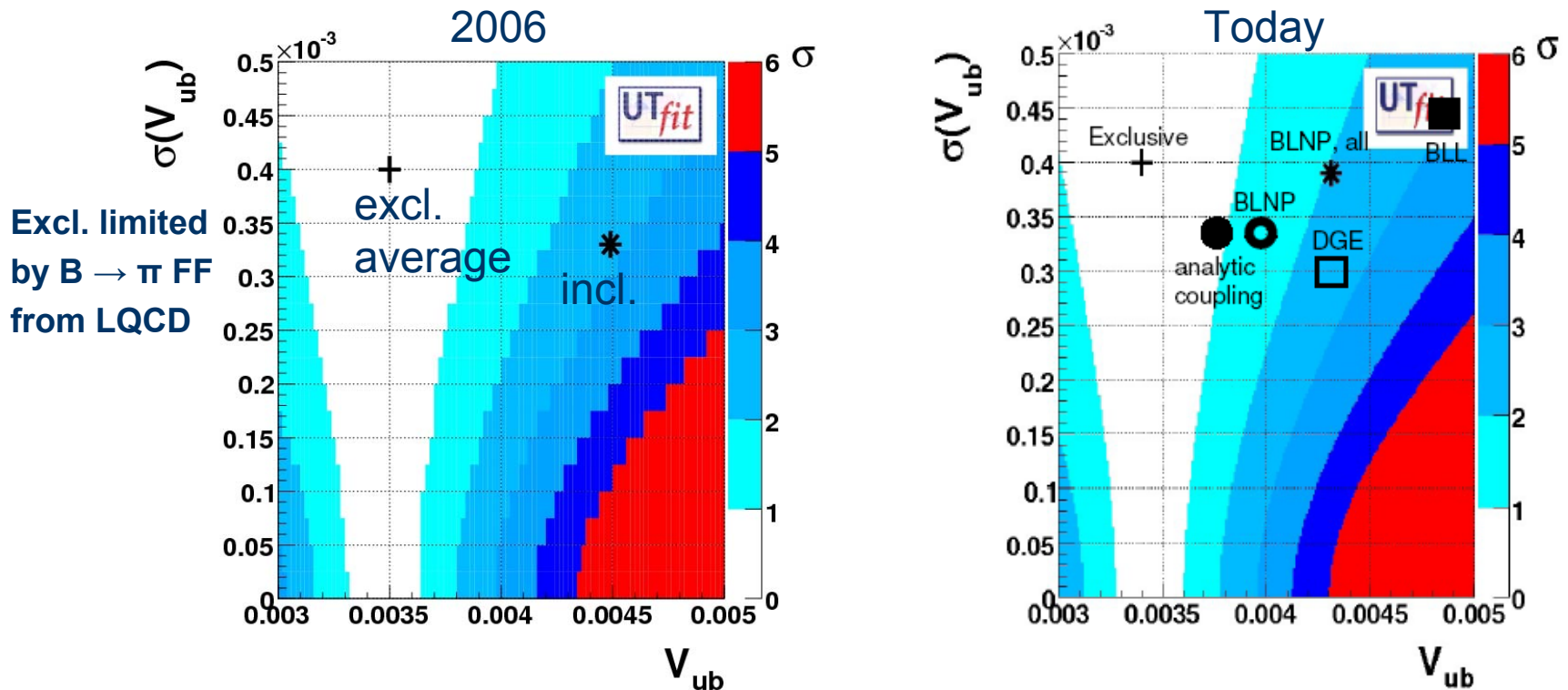
First measurement of m_b in $B \rightarrow X_u \ell \nu$ decays:
 $m_b = 4.604 \pm 0.250 \text{ GeV}$
 (kinetic scheme)

Calculations of
 Gambino, Ossola, Uraltsev
 hep-ph/0505091



Consistency of CKM description

Comparison of indirect determination of $|V_{ub}|$ from CKM fit (prediction through other observables, $\sin 2\beta$ etc.) and directly measured values:



- All inclusive determinations give higher values than excl. average
- Need to have consistent excl. and incl. $|V_{ub}|$ to confront $\sin 2\beta$
- More detailed studies by Theory and Experiment are necessary

Conclusions

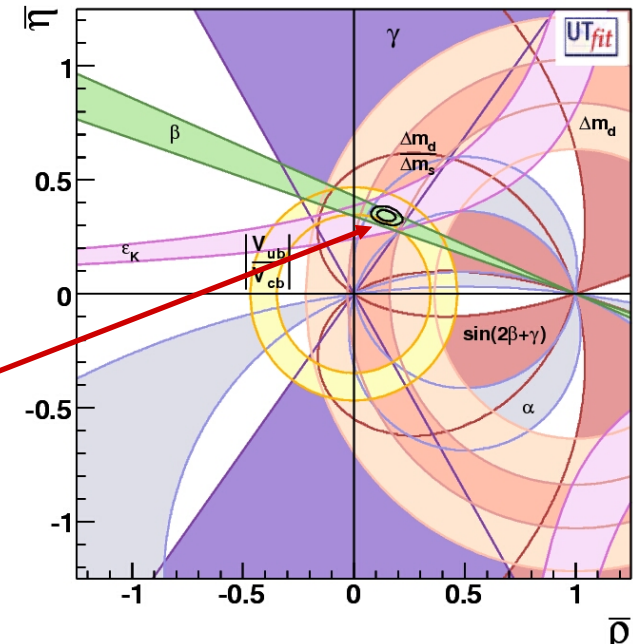
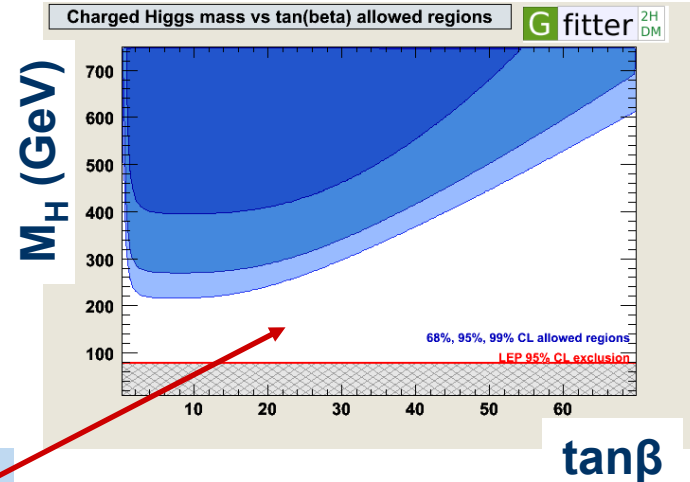
- Analyses on larger datasamples still to come
- Consistency between experimental results for inclusive decay distributions (moments)
- Good agreement for Heavy Quark Parameters from semileptonic and radiative B decays

- Radiative B decays

- $BR(B \rightarrow X_s \gamma) @ 7\%$
- important constraint on many New Physics models
- CP-Asymmetries sensitive to New Physics

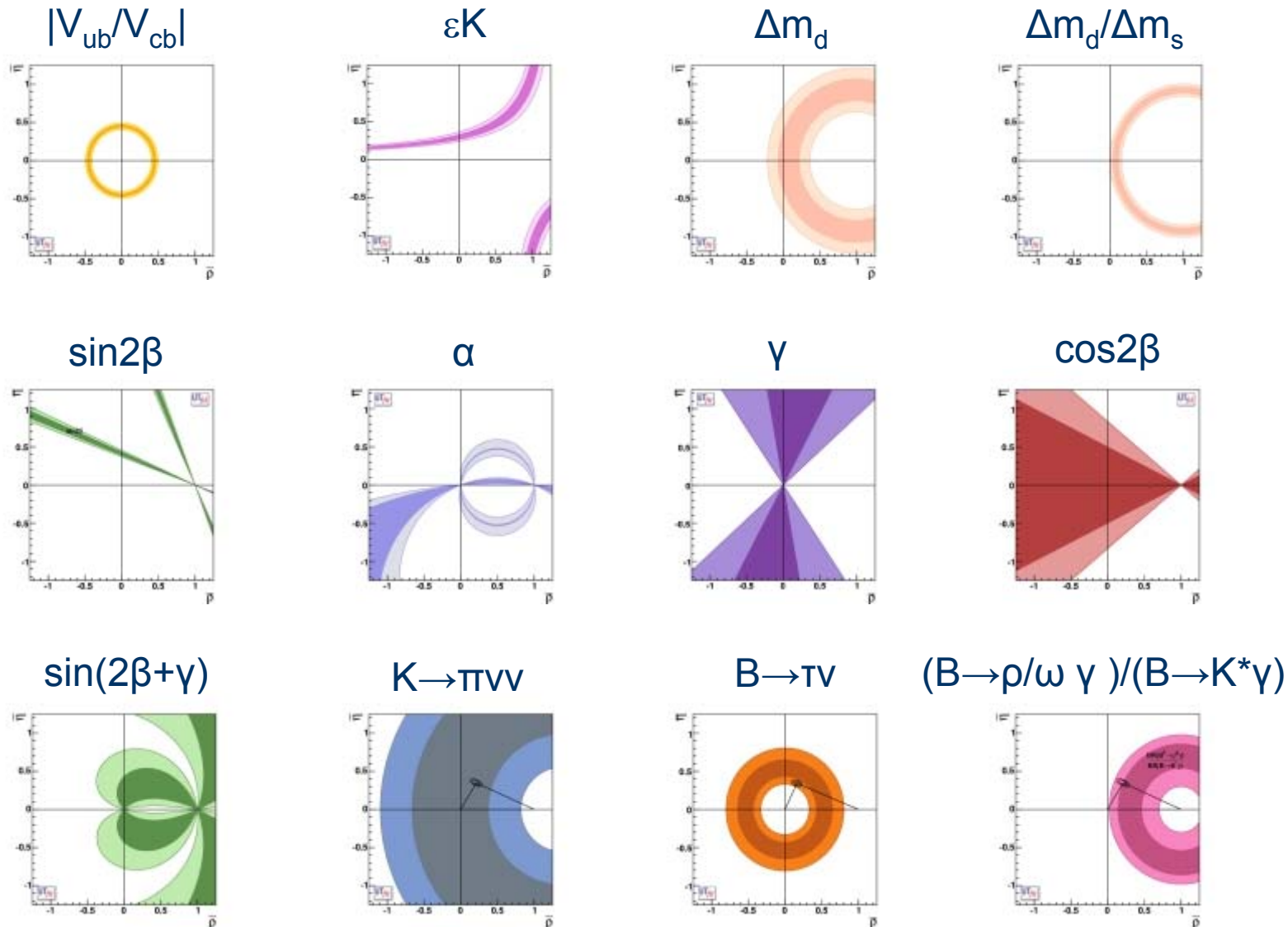
- Precision measurement of 4 SM Parameters:

- $|V_{cb}|$ with 2% uncertainty
- $|V_{ub}|$ with ~8% uncertainty
- testing consistency with $\sin(2\beta)$ and hence SM
- m_b (<1%) and m_c (5%)



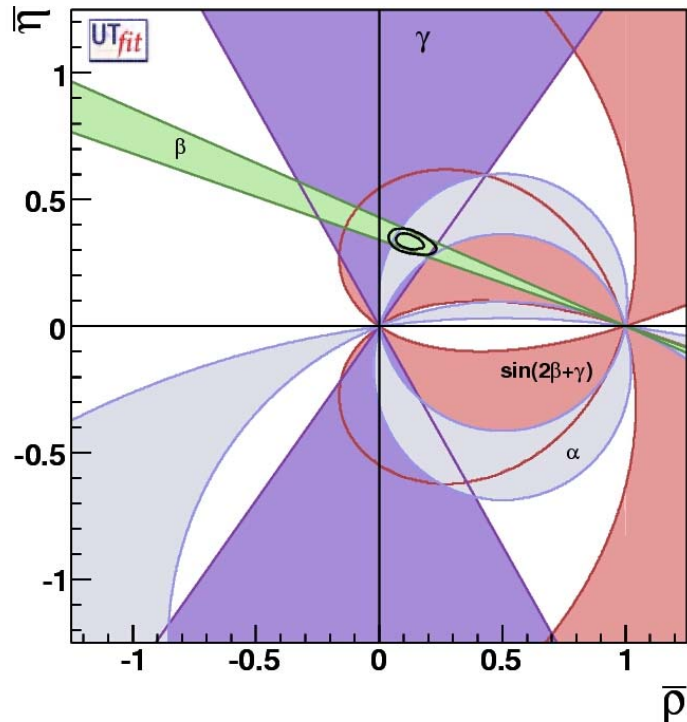
Backup

Constraints on the UT triangle



Vergleich von Seiten und Winkeln

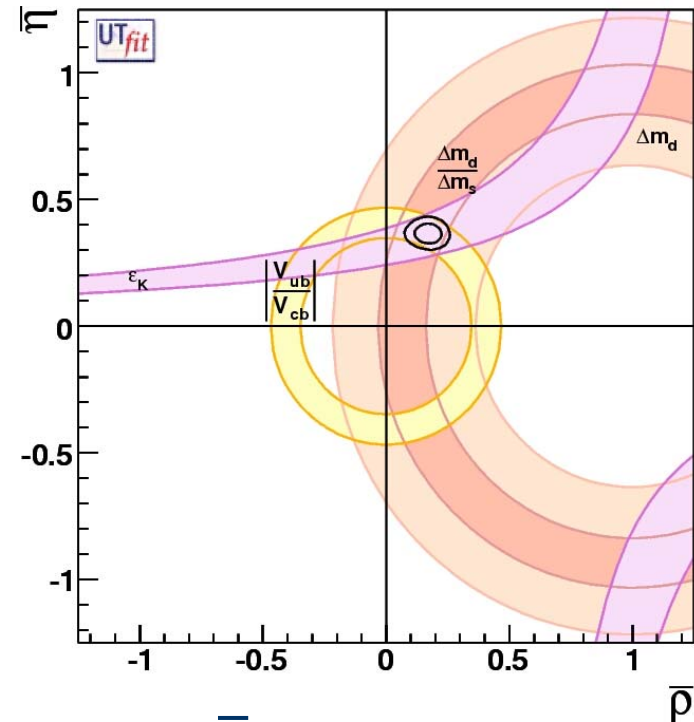
UT from Angles



$$\bar{\rho} = 0.120 \pm 0.038$$

$$\bar{\eta} = 0.332 \pm 0.021$$

UT from Sides



$$\bar{\rho} = 0.172 \pm 0.037$$

$$\bar{\eta} = 0.365 \pm 0.026$$

$$\bar{\rho} - \bar{\rho} = -0.052 \pm 0.053$$

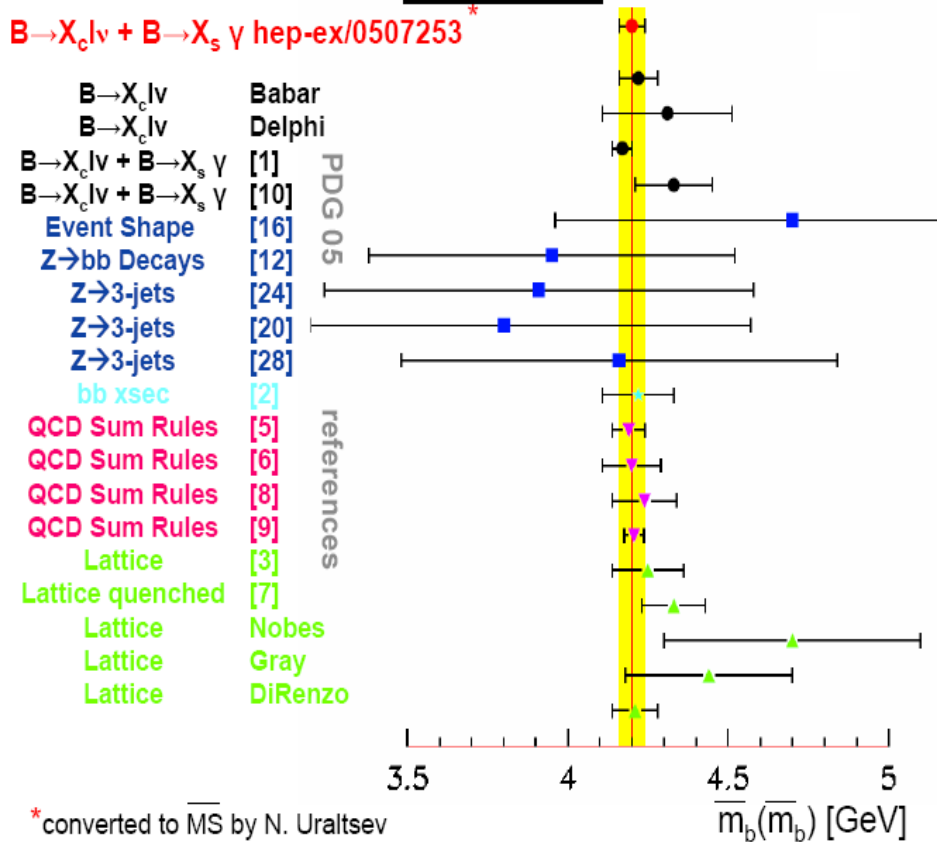
$$\bar{\eta} - \bar{\eta} = -0.033 \pm 0.033$$

Keine signifikante Diskrepanz

Übersicht Quark Massen:

Measurements and Predictions of the b-Quark Mass

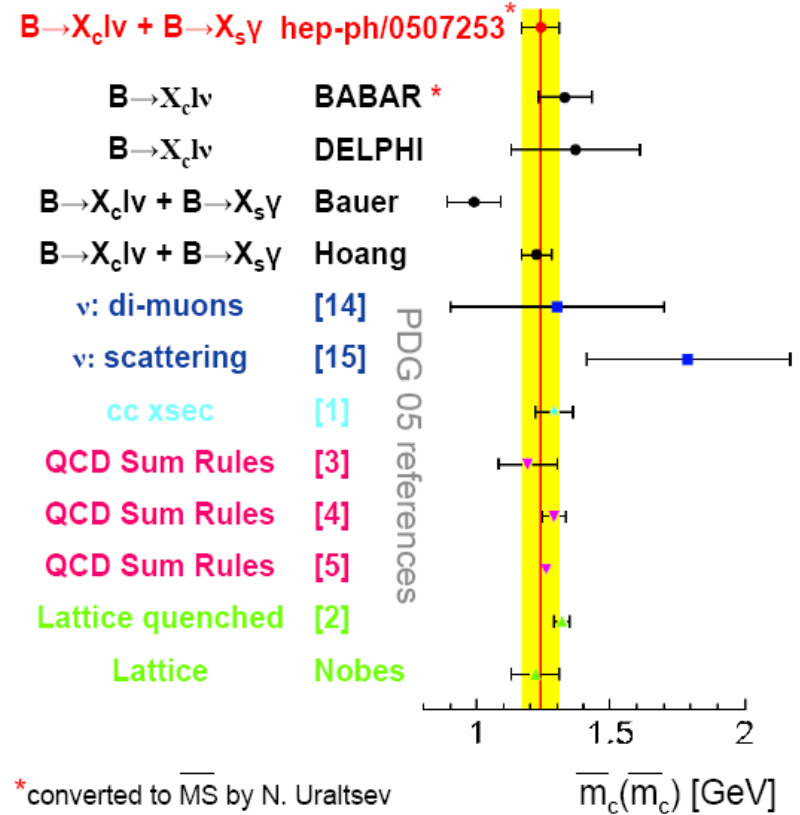
(\overline{MS} scheme)



$$\overline{m}_b(\overline{m}_b) = 4.20 \pm 0.04 \text{ GeV}$$

Measurements and Predictions of the c-Quark Mass

(\overline{MS} scheme)



$$\overline{m}_c(\overline{m}_c) = 1.24 \pm 0.07 \text{ GeV}$$

Conversion from kinetic mass scheme to \overline{MS} scheme with hep-ph/9708372, hep-ph/0302262

See also report from CKM WS hep-ph/0304132

Fit to Moments of Inclusive Decay Distributions

The Operator Product Expansion separates perturbative from non-perturbative scales in a systematic way:

$$\Gamma_{SL}(B \rightarrow X_c l \nu) = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{pert}(r, \mu)$$

kinetic expec. value $\rightarrow \mu_\pi^2 - \mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}$

kinetic scheme $r \equiv (m_c / m_b)^2$

$$\times \left[z_0(r) \left(1 - \frac{\mu_\pi^2 - \mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{2m_b^2} \right) - 2(1-r)^4 \frac{\mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{m_b^2} + d(r) \frac{\rho_D^3}{m_b^3} + O(1/m_b^4) \right]$$

chromomagnetic expec. value μ_G^2

Darwin term $\frac{\rho_D^3 + \rho_{LS}^3}{m_b}$

spin-orbit $d(r) \frac{\rho_D^3}{m_b^3}$

Benson, Bigi, Mannel & Uraltsev, hep-ph/0410080
 Gambino & Uraltsev, Eur.Phys.J. C34, 181 (2004)

Moments of hadronic mass, lepton energy and photon energy in $b \rightarrow sg$ distribution depend on same heavy quark parameters:

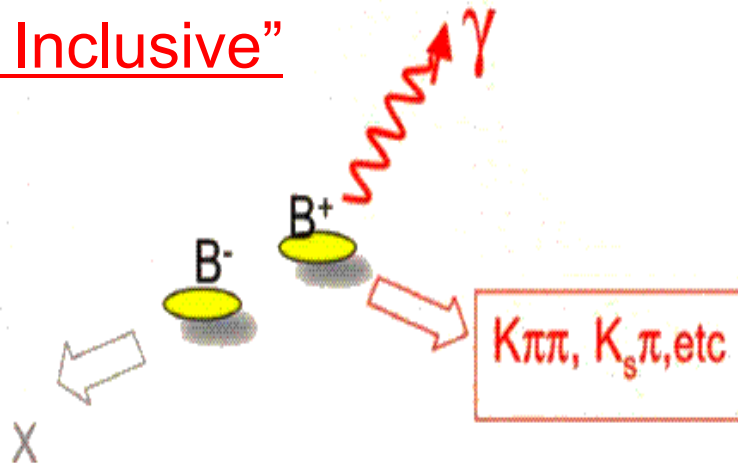
$$\begin{aligned} \langle M_X^n \rangle &\rightarrow \langle M_X \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \\ \langle E_\ell^n \rangle &\rightarrow \langle E_\ell \rangle (m_b, m_c, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \\ \langle E_\gamma^n \rangle &\rightarrow \langle E_\gamma \rangle (m_b, \mu_\pi^2, \mu_G^2, \rho_D^3, \rho_{LS}^3, \alpha_s) \end{aligned}$$

mb and μ_π^2 are used to parameterise both $B \rightarrow X_s \gamma$ and $B \rightarrow X_u l \nu$ spectra

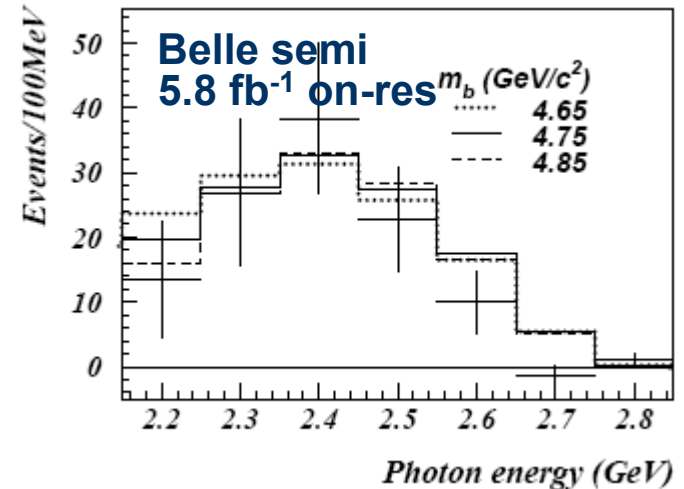
Many moment measurements (~ 50) allow to fit for all parameters up to $1/m_b^3$

Summe exklusiver Endzustände

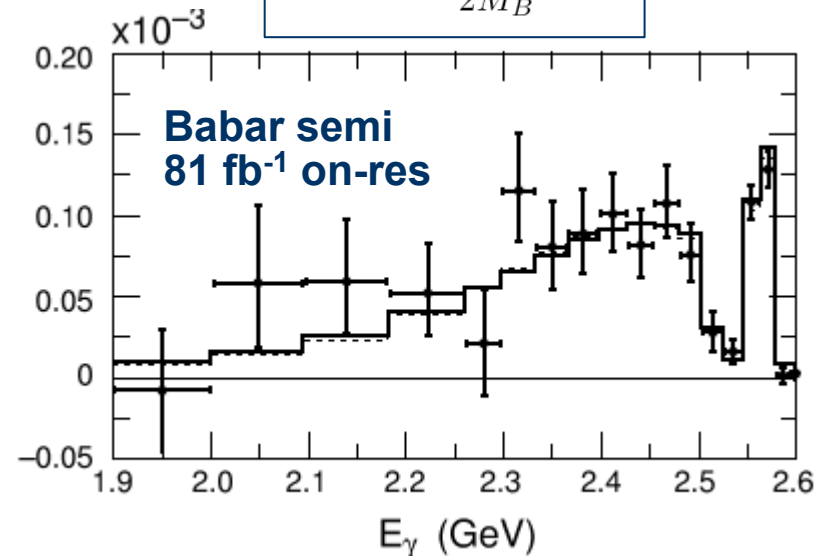
“Semi Inclusive”



- **Volle Rekonstruktion von möglichst vielen X_s Endzuständen (bis zu 38!)**
- **Pros**
 - Niedriger Untergrund
 - Gute E_γ Auflösung im B-Bezugssystem
- **Cons**
 - Systematische Unsicherheiten der X_s Fragmentation
 - Fehlende X_s Zerfallskanäle

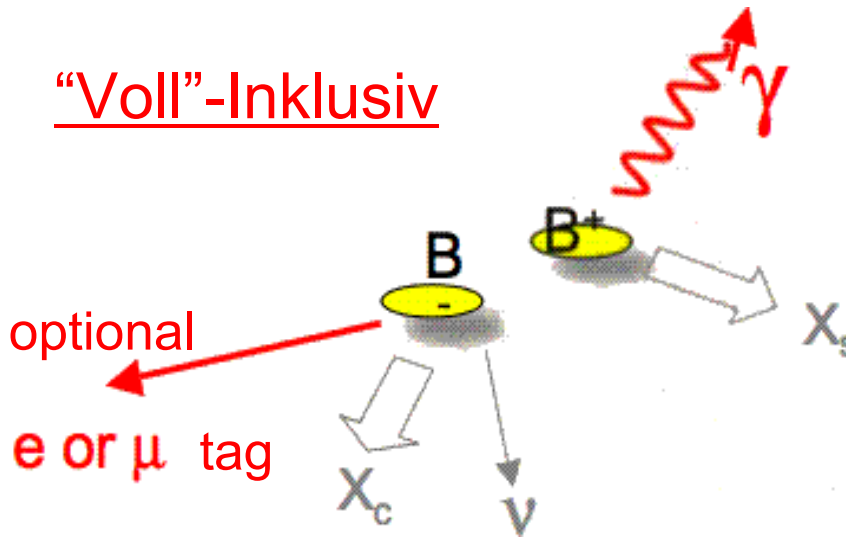


$$E_\gamma = \frac{M_B^2 - M(X_s)^2}{2M_B}$$

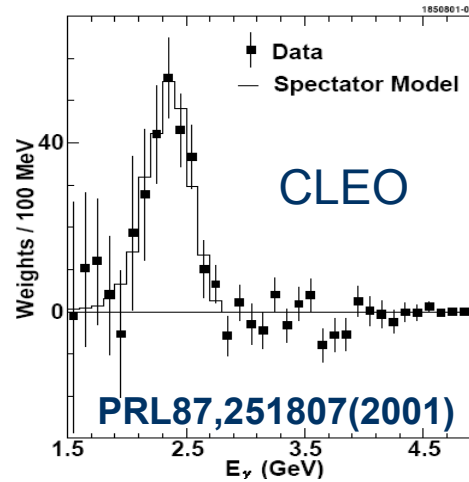


„Voll“-Inklusive Rekonstruktion

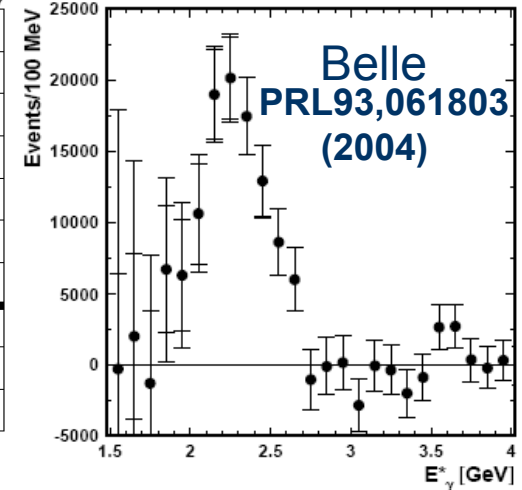
„Voll“-Inklusiv



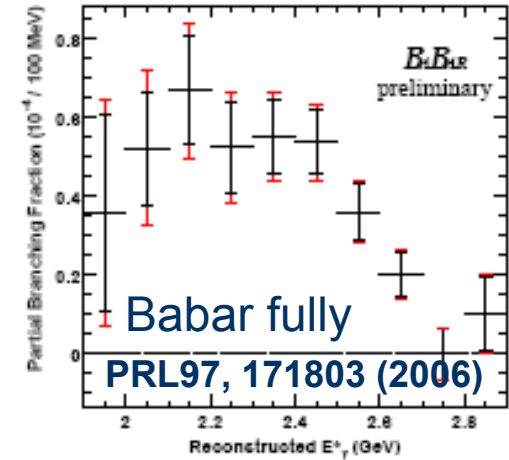
- X_s System wird nicht benötigt
- Nur das Photon wird rekonstruiert
- Pros
 - Keine Unsicherheit durch X_s Fragmentationsmodell
 - theoretisch sauber
- Cons
 - Grosser Untergrund → Kontinuum
 - E_γ^{*} Messung im Y(4s) System



9.1 fb⁻¹ on-res
4.4 fb⁻¹ off-res



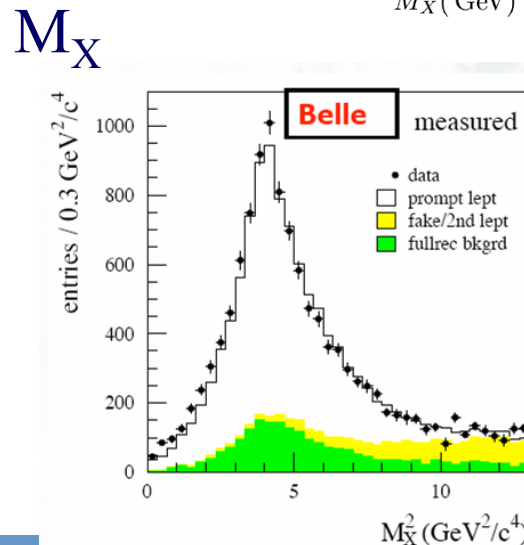
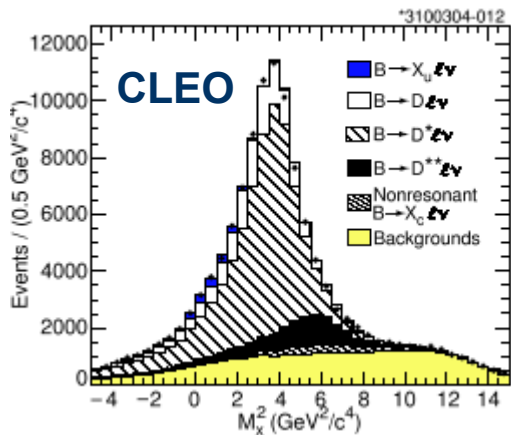
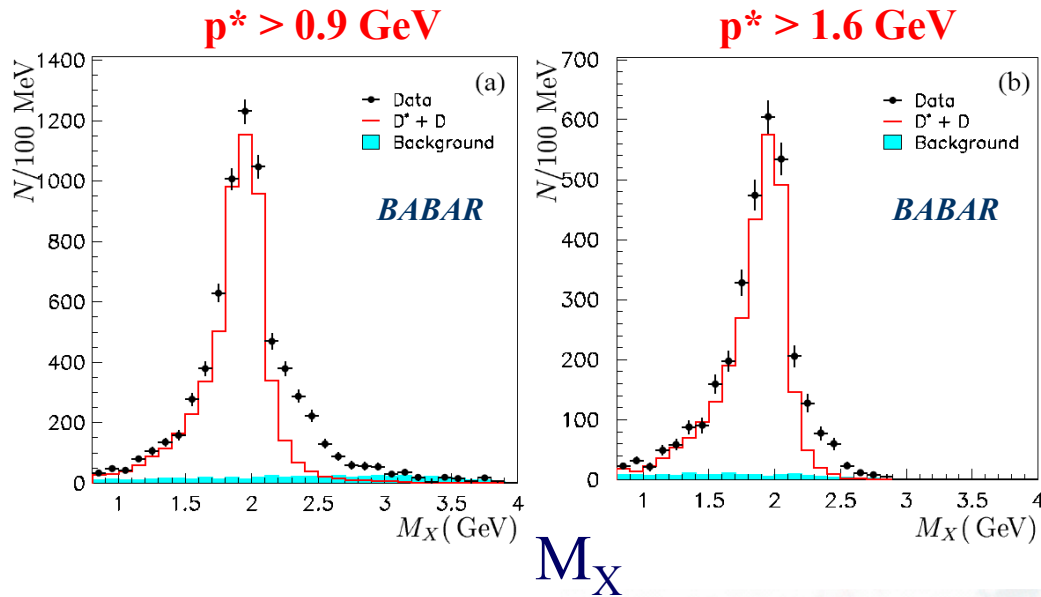
140 fb⁻¹ on-res
15 fb⁻¹ off-res



81.5 fb⁻¹ on-res
9.6 fb⁻¹ off-res

Hadronic Mass Moments

BaBar, Belle and CLEO measure full spectrum



Delphi and CDF only measure higher resonances

