

# Lifetimes of $B^0$ , $B_s$ and $\Lambda_b$



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*on behalf of the LHCb collaboration*



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# Outline

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- $B_s^0 \rightarrow D_s^- \pi^+$
- $B_s^0 \rightarrow D_s^- D_s^+$
- $B_s^0 \rightarrow K^+ K^-$
- $B_s^0 \rightarrow J/\Psi f_0$
- $B_{(s)} \rightarrow J/\Psi X$
- $\Lambda_b \rightarrow J/\Psi p K^-$

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Submitted to journal



PRL 109, 152002 (2012)

JHEP04(2014)114

PLB, 734, (2014) 122

- Comparison of results:  $\Gamma_s - \Delta\Gamma_s$  plane



*Topics NOT covered by this talk:*

Semileptonic  $B_c \rightarrow J/\Psi \mu\nu(X)$ : **Katharina Kreplin** (next talk)

Other beauty baryon lifetimes: **Steve Blusk** talk on Thursday!

# Introduction

- Lifetimes are fundamental properties of particles
  - Decays are essentially exponential:
    - But mixing can occur in neutral mesons
    - CP violation can occur
  - Decay shape can be modified (not a pure exponential)
- Heavy Quark Expansion (HQE) predicts b-hadron lifetimes
  - $\tau$  is expressed as an expansion in terms of mass(heavy quark)
  - HQE can also be used to extract values of  $|V_{ub}|$  &  $|V_{cb}|$
  - See the inspiring review by **A. Lenz: arXiv:1405.3601v1**

$$\frac{\tau(B^+)}{\tau(B_d)}^{\text{HQE 2014}} = 1.04^{+0.07}_{-0.03} ,$$

$$\frac{\tau(B_s)}{\tau(B_d)}^{\text{HQE 2014}} = 1.001 \pm 0.002 ,$$

$$\frac{\tau(\Lambda_b)}{\tau(B_d)}^{\text{HQE 2014}} = 0.935 \pm 0.054 ,$$

# Effective Lifetime (1)

- For charged B mesons → decay is purely exponential
- For neutral B mesons → can oscillate + can have CP violation

*in case of mixing and CP violation, equations become:*

$$\begin{aligned}\Gamma[f, t] &= \Gamma(B_s(t) \rightarrow f) + \Gamma(\bar{B}_s(t) \rightarrow f) \\ &= \mathcal{N}_f \left[ e^{-\Gamma_L t} |\langle f | B_L \rangle|^2 + e^{-\Gamma_H t} |\langle f | B_H \rangle|^2 \right] \\ &= \mathcal{N}_f |A_f|^2 \left[ 1 + |\lambda_f|^2 \right] e^{-\Gamma t} \boxed{\left\{ \cosh \frac{\Delta\Gamma t}{2} + \sinh \frac{\Delta\Gamma t}{2} \mathcal{A}_{\Delta\Gamma} \right\}}\end{aligned}$$

*Extra term dependent on t  
Shape is not purely exponential*

$$\text{CPV } \mathcal{A}_{\Delta\Gamma} \equiv -2 \left( 1 + |\lambda_f|^2 \right) \text{Re}(\lambda_f)$$
$$\lambda_f = \frac{q A_f}{p A_f}$$

# Effective Lifetime (2)

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- **For  $B^0$  mesons:**  $\Delta\Gamma_d \ll \Gamma_d$   
simple exponential is a good approximation
- **For  $B_s^0$  mesons:**  
 $\Delta\Gamma_s$  is not small and  $A_{\Delta\Gamma}$  depends on the mode considered
- **If  $B_s^0 \rightarrow$  flavour specific:**  
decay is the exact sum of two exponential

$$\Gamma_s = \boxed{\Gamma_{\text{flavor specific}}} \left( 1 - \left( \frac{\Delta\Gamma_s}{2\Gamma_s} \right)^2 \right) / \left( 1 + \left( \frac{\Delta\Gamma_s}{2\Gamma_s} \right)^2 \right)$$



*Result of a single  
exponential fit*

# Methods

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We performed lifetime measurements with two different approaches

## Relative measurement

- The lifetime is measured relative to a control mode with well known lifetime
- Signal mode and control mode have similar topology
- PROs: measure ratios → systematic uncertainties cancel
- CONSs: irreducible systematic uncertainty from input lifetime

## Absolute measurement

- Fit decay distributions with exponentials convolved with resolution functions
- PROs: absolute measurement → no input needed
- CONSs: need to understand acceptance functions
- Data driven methods required to obtain desired precision

- Idea: measure signal yield in lifetime bins
- Signal decay distribution: Acceptance and convolution with resolution
- Measure the ratio of decay time distributions:

$$R(t) = \frac{F_{B_s}}{F_{B_x}} = \frac{A_{B_s}(t) \times [e^{-t/\tau_{B_s}} \otimes G(t, \sigma_{B_s})]}{A_{B_x}(t) \times [e^{-t/\tau_{B_x}} \otimes G(t, \sigma_{B_x})]}$$

- Fit the ratio  $R(t)$

$$\left. \begin{aligned} R(t) &= R_0 e^{-t(1/\tau_{B_s} - 1/\tau_{B_x})} \\ &= R_0 e^{-t(\Gamma_{B_s} - \Gamma_{B_x})} \\ &= R_0 e^{-t\Delta_{B_s B_x}} \end{aligned} \right\} \text{Use Precise } B^+, B^0 \text{ lifetimes as input}$$

Relative lifetime between  $B_s \rightarrow D_s \pi^+$ ,  $D_s \rightarrow K \bar{K}^+ \pi^-$  and

–  $B^0 \rightarrow D^+ \pi^+$ ,  $D^+ \rightarrow K^+ \pi^+ \pi^-$

(Same number of tracks, very different D lifetimes)

–  $B^+ \rightarrow D^0 \pi^+$ ,  $D^0 \rightarrow K^+ \pi^-$

(Different number of tracks, similar D lifetimes)

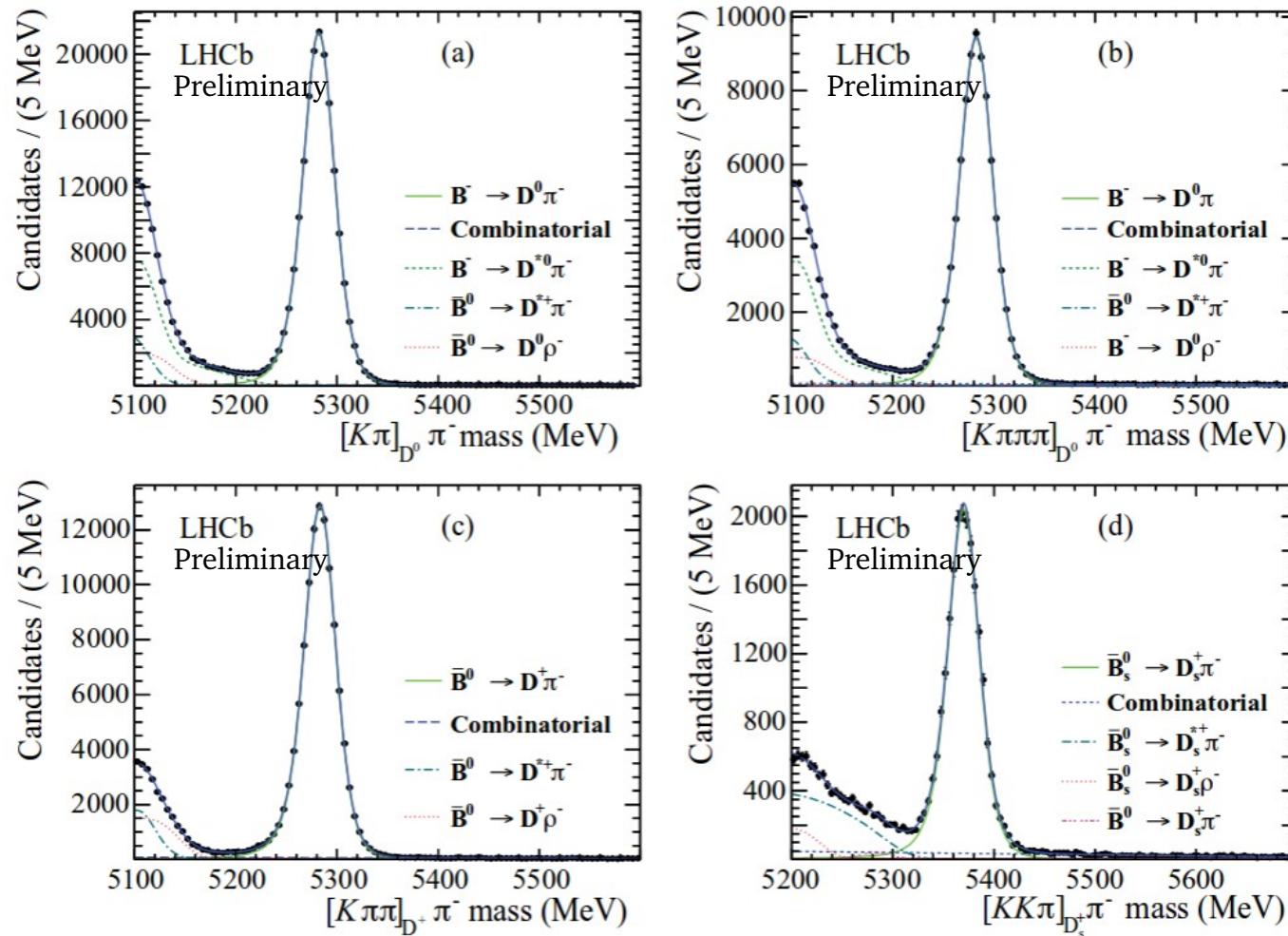
–  $B^+ \rightarrow D^0 \pi^+$ ,  $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$

(Different number of tracks, similar D lifetimes)

# $B_s \rightarrow D_s^- \pi^+$ Lifetime

New!

- 2011 data set ( $1 \text{ fb}^{-1}$ )  
21000 signal  $B_s$  events



# $B_s \rightarrow D_s^- \pi^+$ Lifetime

New!

- 2011 data set ( $1 \text{ fb}^{-1}$ )
- 21000 signal  $B_s$  events

$$\tau_{fs}(\bar{B}_s^0)/\tau(\bar{B}^0) = 1/(1 + \tau(\bar{B}^0)\Delta_{B_s^0 B^0})$$

$$1.010 \pm 0.010 \pm 0.008$$

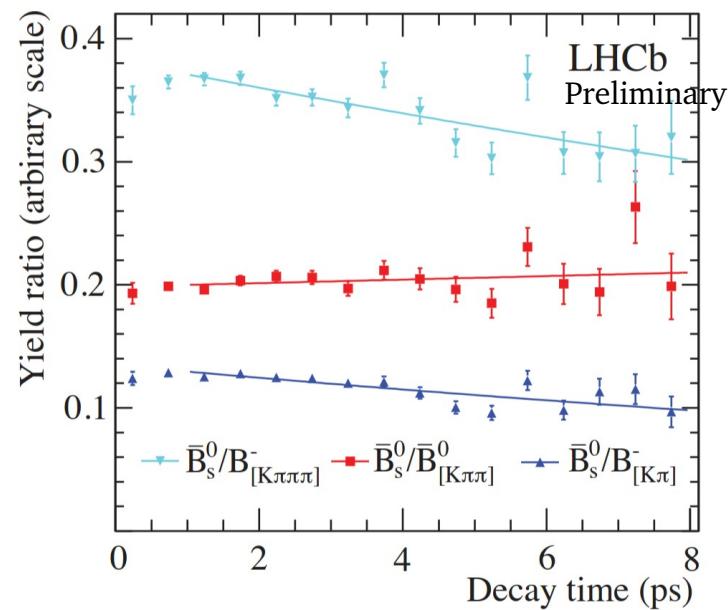
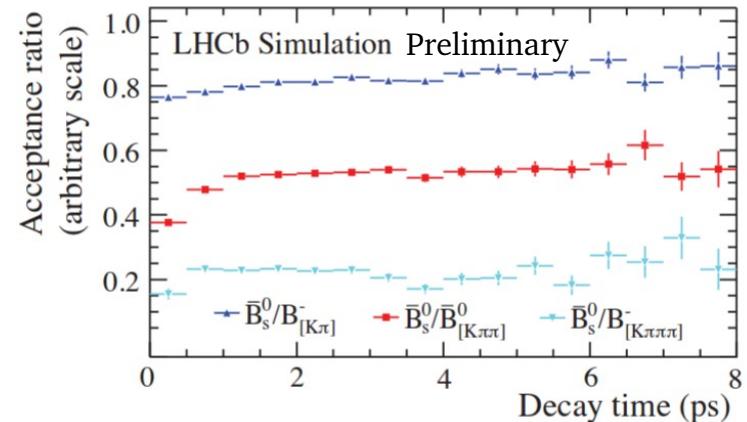
Consistent with HQE =  $1.009 \pm 0.004$

$$\tau_{fs} = 1.535 \pm 0.015 \pm 0.012 \pm 0.007 \text{ ps}$$

↓

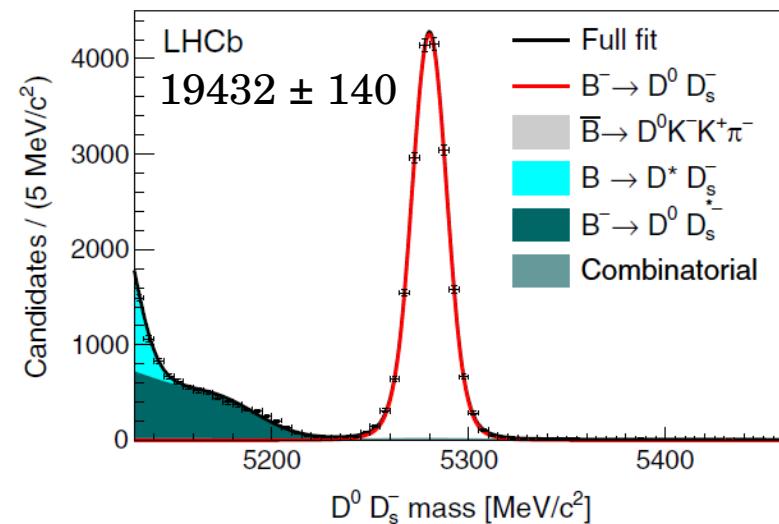
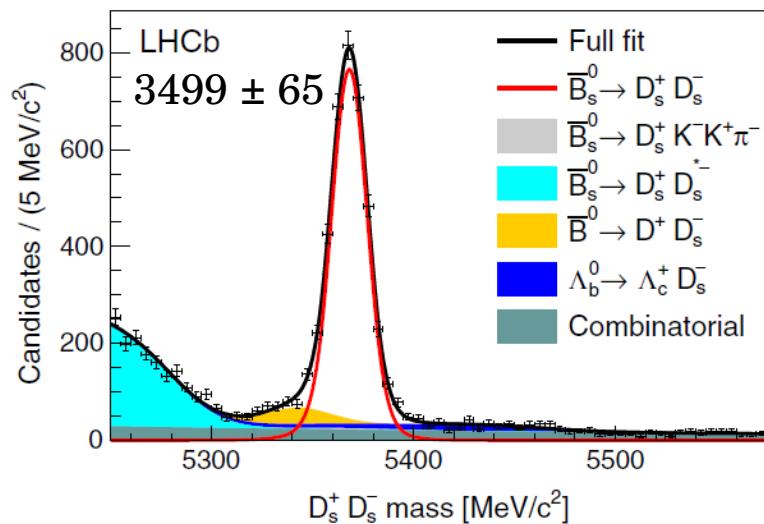
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- This is the most precise measurement to date
- Consistent with previously available flavour specific measurements



$B_s^0 \rightarrow D_s^- D_s^+$ 

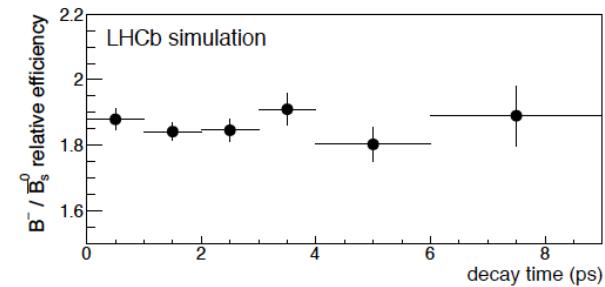
- 2011 + 2012 dataset ( $3 \text{ fb}^{-1}$ )
- Relative measurement wrt  $B^0 \rightarrow D^0 D_s^-$
- First lifetime measurement in this final state
- Also observed  $B_s \rightarrow D^- D_s^+$



- **CP even final state**

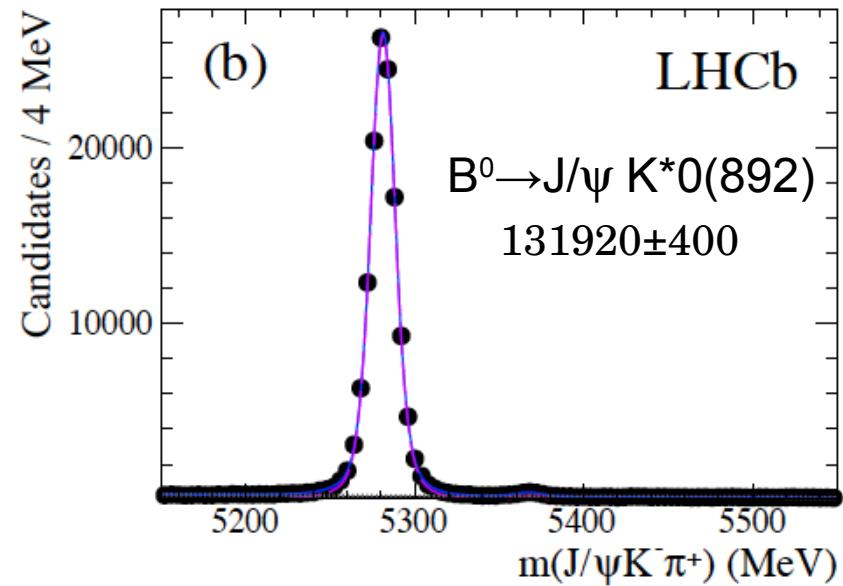
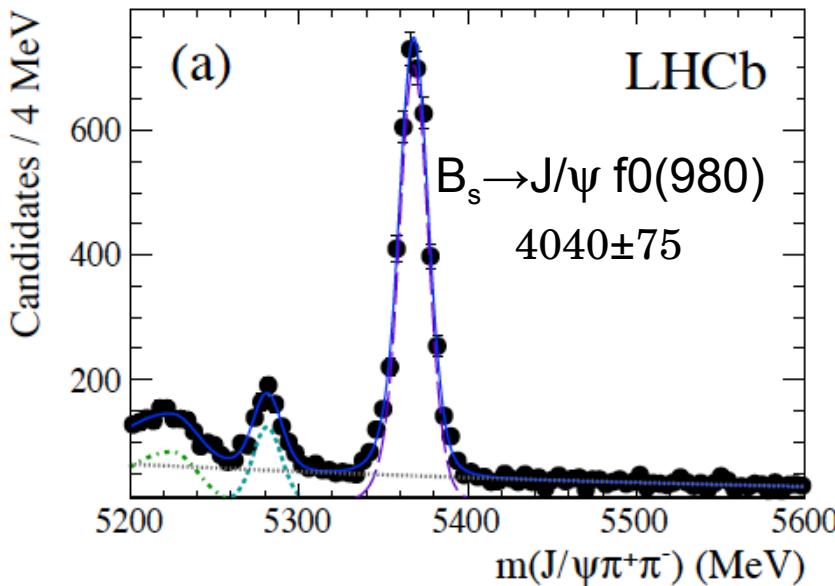
$$1.379 \pm 0.026 \pm 0.017 \text{ ps}$$

$$\Gamma_L = 0.725 \pm 0.014 \pm 0.009 \text{ ps}^{-1}$$



$B_s^0 \rightarrow J/\psi f_0$ 

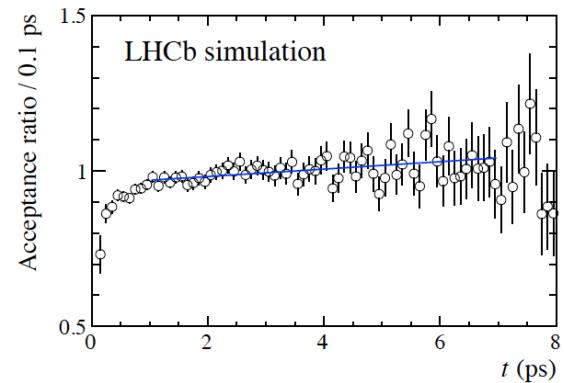
- 2011 dataset ( $1 \text{ fb}^{-1}$ )
- Relative measurement wrt  $B^0 \rightarrow J/\psi K^{*0}(892)$



- Fit starts at 1ps where ratio of decay acceptances is linear
- Slope extracted from MC

$$1.700 \pm 0.040 \pm 0.026 \text{ ps}$$

$$\Gamma_H = 0.588 \pm 0.014 \pm 0.009 \text{ ps}^{-1}$$



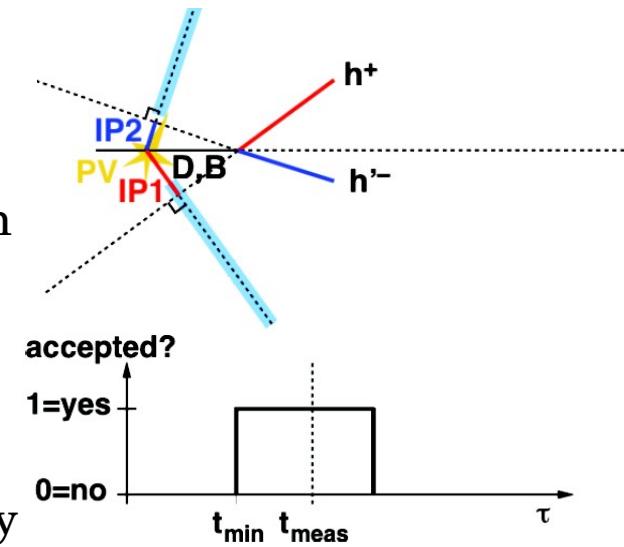
- Two diagrams contributing to the same final state
- CP violation can contribute
- Lifetime formula slightly modified by extra term

$$\Gamma[f, t] \propto e^{-\Gamma t} \left[ 1 + \frac{1}{2} \left( \frac{\Delta\Gamma}{2} t \right)^2 + A_{\Delta\Gamma} \left( \frac{\Delta\Gamma}{2} t \right) \right]$$

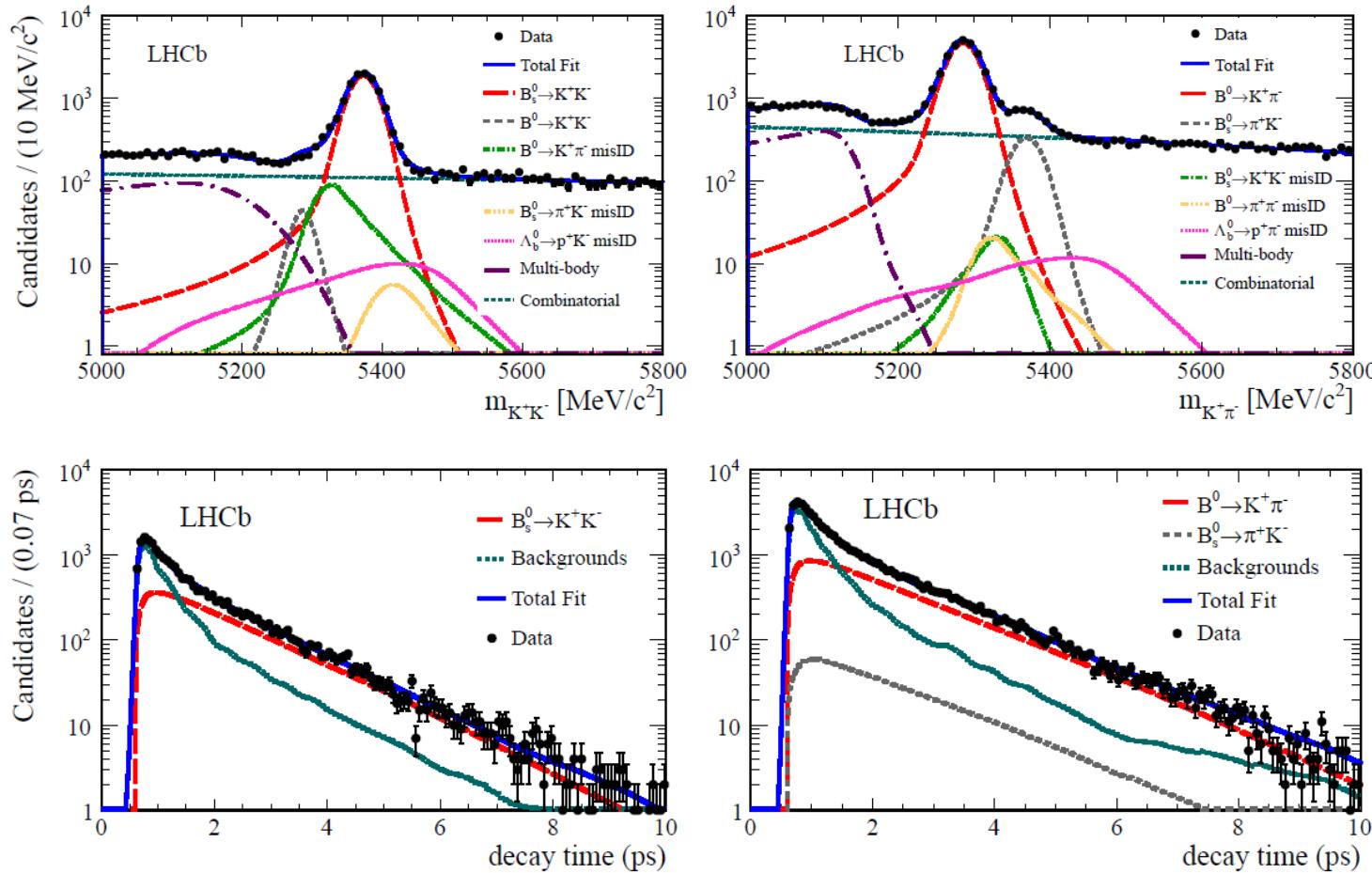
*Expected  $\sim -1$*

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- Absolute measurement
- Uses the so-called “swimming” technique
- Method pioneered by CDF
- Data driven method to get decay acceptance function
- A per-event acceptance function is determined
- Idea is to move the PV along the momentum vector of B and see when particle is accepted
- Measure also lifetime of decays with similar topology



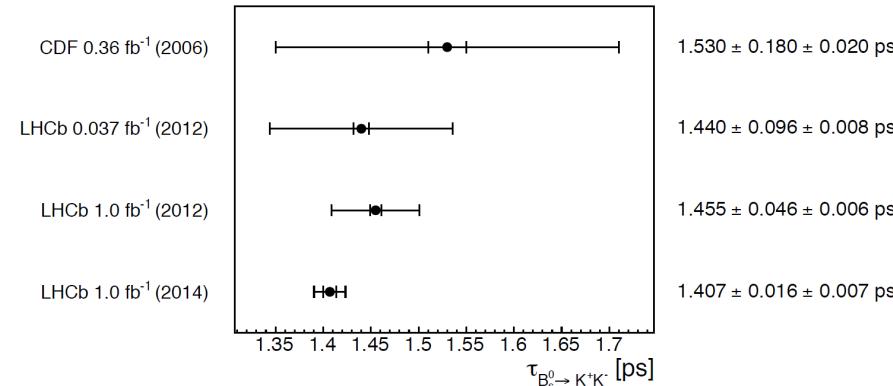
- 2011 dataset ( $1 \text{ fb}^{-1}$ )



# $B_s^0 \rightarrow K^+K^-$

New!

- 2011 dataset ( $1 \text{ fb}^{-1}$ )



$$\tau_{B_s^0 \rightarrow K^+K^-} = 1.407 \pm 0.016 \text{ (stat)} \pm 0.007 \text{ (syst)} \text{ ps},$$

$$\tau_{B_s^0 \rightarrow K^+\pi^-} = 1.524 \pm 0.011 \text{ (stat)} \pm 0.004 \text{ (syst)} \text{ ps},$$

$$\tau_{B_s^0 \rightarrow \pi^+K^-} = 1.60 \pm 0.06 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ ps}.$$

- Can be used to extract:

$$\mathcal{A}_{\Delta\Gamma_s} = \frac{2\Gamma_s^2}{\Delta\Gamma_s} \tau_{B_s^0 \rightarrow K^+K^-} - \frac{2\Gamma_s}{\Delta\Gamma_s} \quad \mathcal{A}_{\Delta\Gamma_s} = -0.87 \pm 0.17 \text{ (stat)} \pm 0.13 \text{ (syst)}$$

Consistent with SM expectation:

$$\mathcal{A}_{\Delta\Gamma_s}(B_s^0 \rightarrow K^+K^-) = -0.972^{+0.014}_{-0.009}$$

- Set of lifetime measurements
- Absolute measurements in final states containing J/Ψ
- 2011 data set ( $1 \text{ fb}^{-1}$ )
- Most precise measurements to date!

Channel	Yield
$B^+ \rightarrow J/\psi K^+$	$229\,434 \pm 503$
$B^0 \rightarrow J/\psi K^{*0}$	$70\,534 \pm 312$
$B^0 \rightarrow J/\psi K_s^0$	$17\,045 \pm 175$
$B_s^0 \rightarrow J/\psi \phi$	$18\,662 \pm 152$
$\Lambda_b^0 \rightarrow J/\psi \Lambda$	$3\,960 \pm 89$

$$\left. \begin{array}{l} \tau_{B^+ \rightarrow J/\psi K^+} = 1.637 \pm 0.004 \pm 0.003 \text{ ps}, \\ \tau_{B^0 \rightarrow J/\psi K^{*0}} = 1.524 \pm 0.006 \pm 0.004 \text{ ps}, \\ \tau_{B^0 \rightarrow J/\psi K_s^0} = 1.499 \pm 0.013 \pm 0.005 \text{ ps}, \\ \tau_{\Lambda_b^0 \rightarrow J/\psi \Lambda} = 1.415 \pm 0.027 \pm 0.006 \text{ ps}, \\ \tau_{B_s^0 \rightarrow J/\psi \phi} = 1.480 \pm 0.011 \pm 0.005 \text{ ps}, \end{array} \right\}$$

$$\Delta \Gamma_d / \Gamma_d = -0.044 \pm 0.025 \pm 0.011 \quad \text{LHCb only} \\ 0.015 \pm 0.018 \text{ by B factories}$$

Prediction arXiv:0412007:

$$(\Delta \Gamma / \Gamma)_{B_d} = (3 \pm 1.2) \cdot 10^{-3}$$

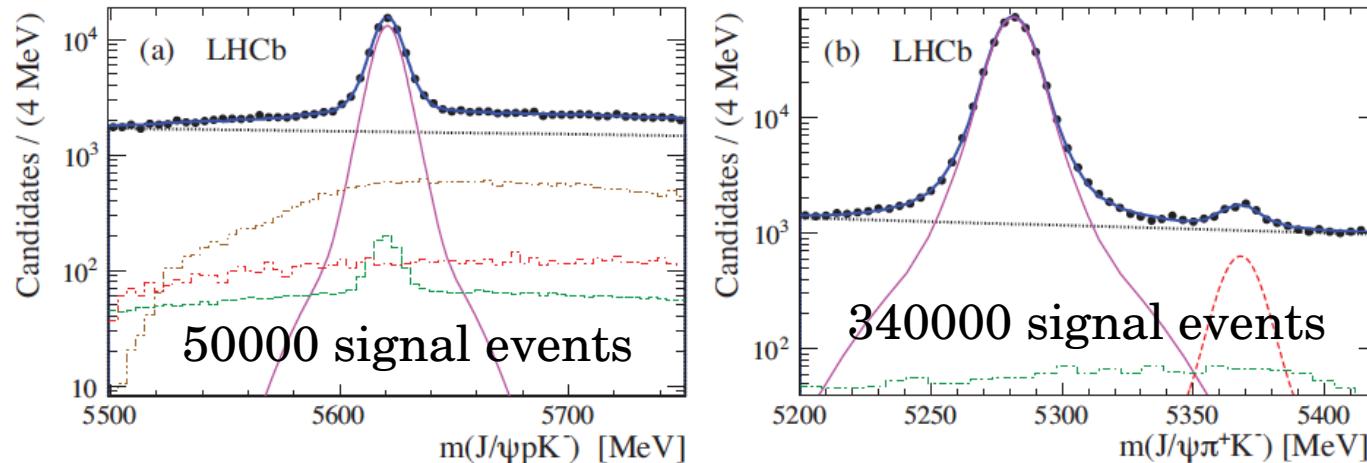
# $\Lambda_b \rightarrow J/\Psi p K^-$

- HQE prediction of the ratio  $\tau(\Lambda_b)/\tau(B^0) = 0.935 \pm 0.054$
- Problem of the  $\Lambda_b$  lifetime: long standing puzzle
- Need a precision measurement

Year	Exp	Decay	$\tau(\Lambda_b)$ [ps]	$\tau(\Lambda_b)/\tau(B_d)$
2010	CDF	$J/\psi\Lambda$	$1.537 \pm 0.047$	$1.020 \pm 0.031$
2009	CDF	$\Lambda_c + \pi^-$	$1.401 \pm 0.058$	$0.922 \pm 0.038$
2007	D0	$\Lambda_c\mu\nu X$	$1.290 \pm 0.150$	$0.849 \pm 0.099$
2007	D0	$J/\psi\Lambda$	$1.218 \pm 0.137$	$0.802 \pm 0.090$
2006	CDF	$J/\psi\Lambda$	$1.593 \pm 0.089$	$1.049 \pm 0.059$
2004	D0	$J/\psi\Lambda$	$1.22 \pm 0.22$	$0.87 \pm 0.17$

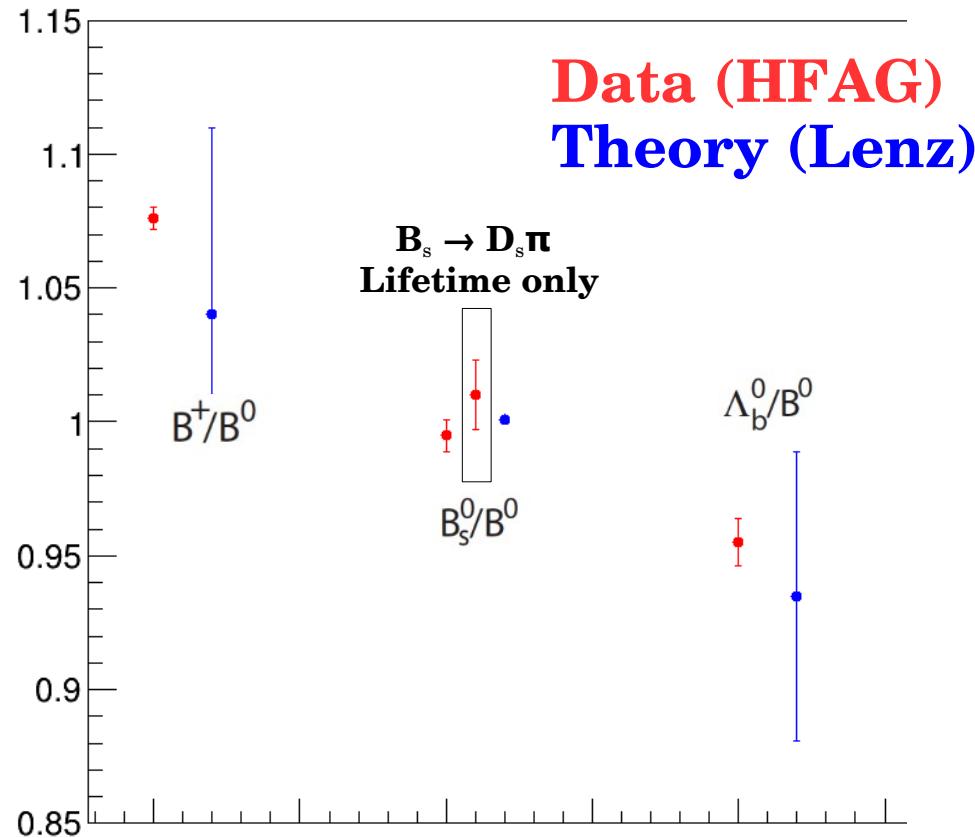
- LHCb measures ratio of lifetime directly
- Uses newly observed  $\Lambda_b$  mode
- Updated to 2011 + 2012 dataset ( $3 \text{ fb}^{-1}$ )

$$\left. \begin{array}{l} \frac{\tau(\Lambda_b^0)}{\tau(B^0)} = 0.974 \pm 0.006 \pm 0.004 \\ \tau(\Lambda_b^0) = 1.479 \pm 0.009 \pm 0.010 \text{ ps} \end{array} \right.$$



# Conclusions (1)

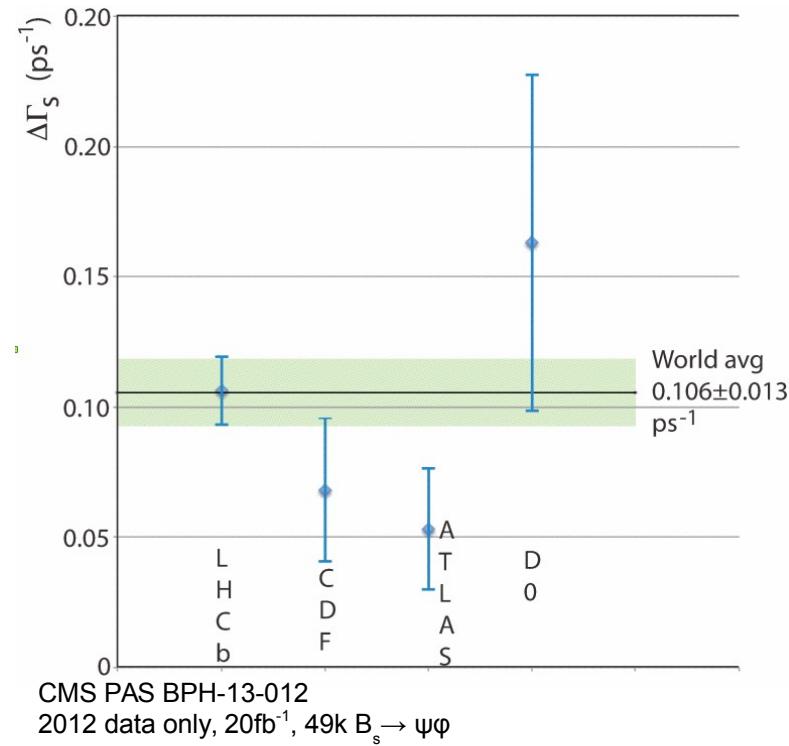
- Recent measurement give a consistent picture of b-hadron lifetimes
- HQE gives very reliable predictions
- Lifetimes ratios known to striking precision



# Conclusions (2)

- $B_s$  sector shows good agreement and it is consistent with SM
- From  $B_s \rightarrow J/\Psi (\pi\pi, KK)$
- Average does not include recent CMS result (ICHEP)

Exp.	$\int L$ ( $\text{fb}^{-1}$ )	$\Gamma_s$ ( $\text{ps}^{-1}$ )	ArXiv
ATLAS	4.9	$0.6700 \pm 0.0070 \pm 0.0040$	1208.0572
CDF	9.6	$0.6545 \pm 0.0081 \pm 0.0039$	1208.2967
D0	8.0	$0.6930 \pm 0.0182$	1109.3166
LHCb	1	$0.6610 \pm 0.0040 \pm 0.0060$	1324.2600
Average		$0.666 \pm 0.0045$	

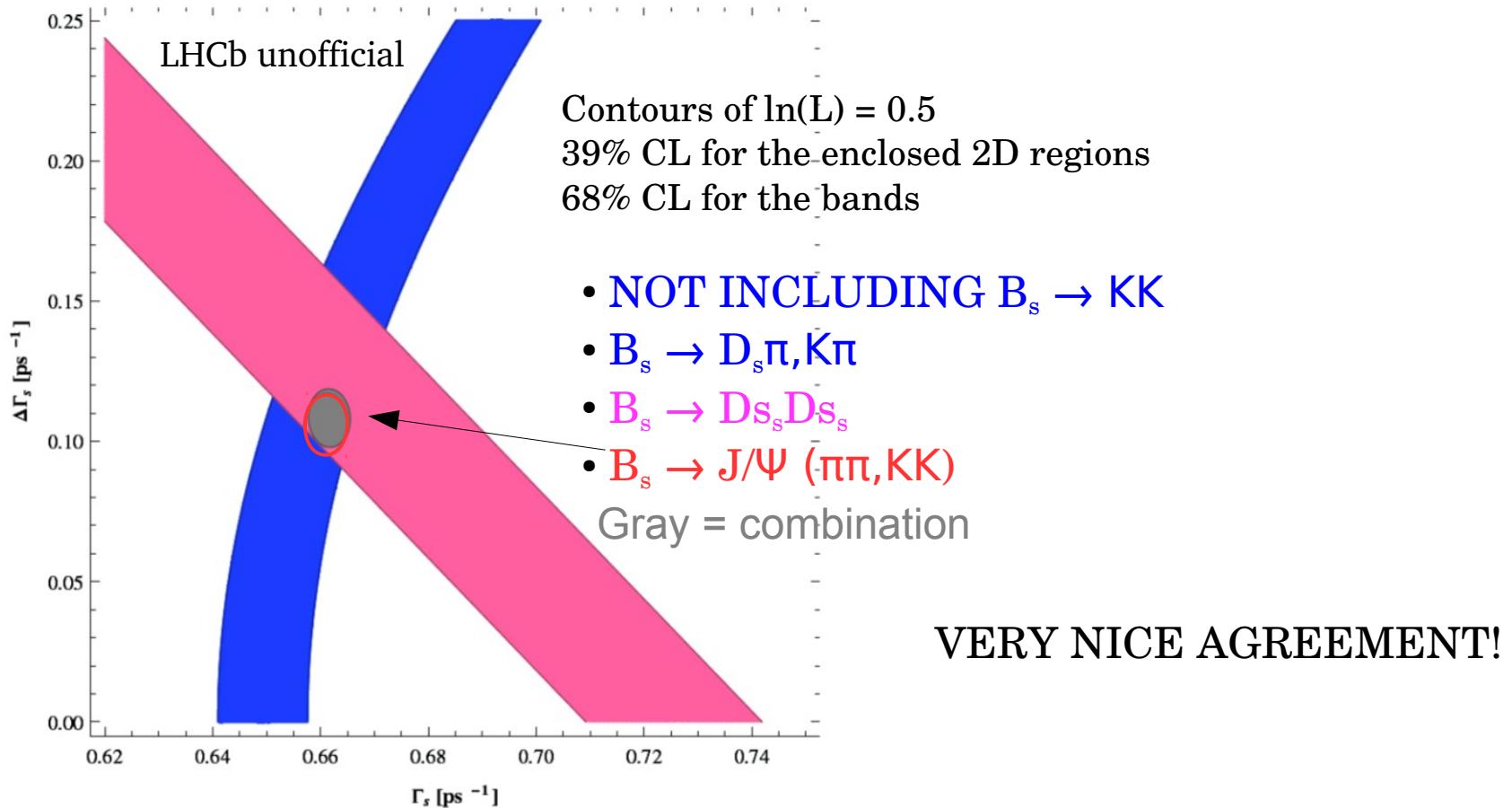


$$\Delta\Gamma_s = 0.096 \pm 0.014 \pm 0.007$$

previous central value was 0.048!

# $\Gamma_s - \Delta\Gamma_s$ plane (LHCb only)

- Combine all the LHCb results
- Plot done in a similar way as HFAG: [http://www.slac.stanford.edu/xorg/hfag/osc/spring\\_2014/](http://www.slac.stanford.edu/xorg/hfag/osc/spring_2014/)
- Systematics assumed uncorrelated



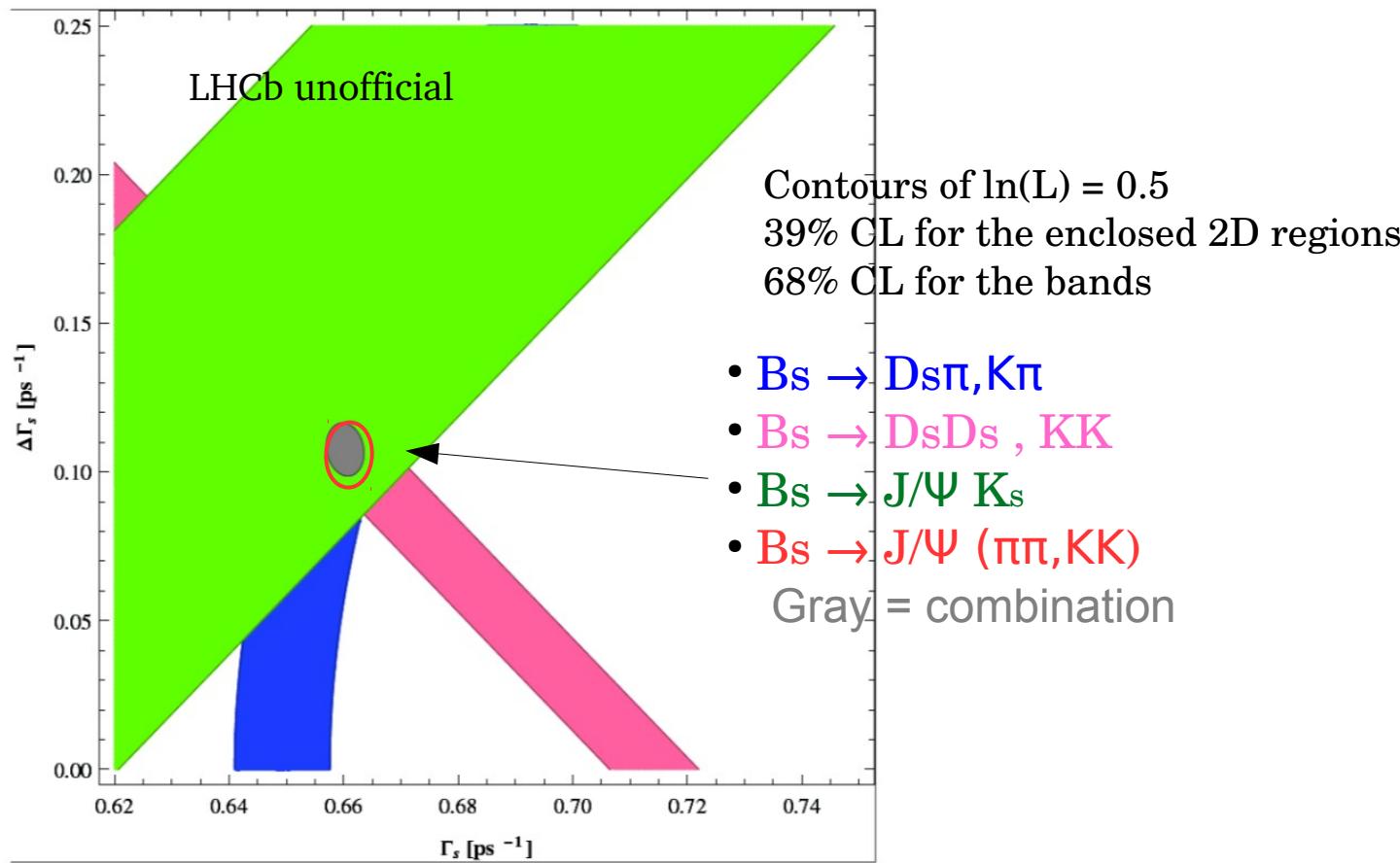
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# Backup Slides



# $\Gamma_s - \Delta\Gamma_s$ plane

- Combine all the LHCb results
- Plot done à la HFAG: [http://www.slac.stanford.edu/xorg/hfag/osc/spring\\_2014/](http://www.slac.stanford.edu/xorg/hfag/osc/spring_2014/)
- Systematics uncorrelated + No direct CP +  $\phi_s=0$



# $\Gamma_s - \Delta\Gamma_s$ plane: numerical results

- Combine all the LHCb results
- Plot done à la HFAG: [http://www.slac.stanford.edu/xorg/hfag/osc/spring\\_2014/](http://www.slac.stanford.edu/xorg/hfag/osc/spring_2014/)
- Systematics uncorrelated + No direct CP +  $\phi_s=0$
- LHCb Unofficial

	$J/\psi$ hh	+eff.lifetime	ALL	removing $KK$ and $J/\psi K_S^0$
$\Delta\Gamma_s (\text{ps}^{-1})$	$0.106 \pm 0.011$	$0.106815^{+0.00918222}_{-0.00916179}$	$0.107544^{+0.00890455}_{-0.00891088}$	$0.108291^{+0.0103867}_{-0.0103722}$
$\Gamma_s (\text{ps}^{-1})$	$0.661 \pm 0.004$	$0.660773^{+0.00363879}_{-0.00363541}$	$0.660268^{+0.00329061}_{-0.00327979}$	$0.661624^{+0.00387548}_{-0.00387389}$
$\rho(\Gamma_s, \Delta\Gamma_s)$	$0.047$	$-0.223708$	$-0.136227$	$-0.0384904$
$\tau_s = 1/\Gamma_s (\text{ps})$	$1.5129 \pm 0.0092$	$1.51338^{+0.00833398}_{-0.00832625}$	$1.51454^{+0.00754808}_{-0.00752325}$	$1.51143^{+0.00885326}_{-0.00884964}$
$\tau_L = 1/\Gamma_L (\text{ps})$	$1.4006 \pm 0.0136$	$1.40021 \pm 0.0101491$	$1.40048 \pm 0.0101239$	$1.3971 \pm 0.0124061$
$\tau_H = 1/\Gamma_H (\text{ps})$	$1.6447 \pm 0.01798$	$1.64646 \pm 0.01751$	$1.64882 \pm 0.0159949$	$1.64615 \pm -0.0178713$
$\Delta\Gamma_s/\Gamma_s$	$0.1604 \pm 0.0166$	$0.161651 \pm 0.0141065$	$0.162879 \pm 0.0136251$	$0.163674 \pm 0.0157539$

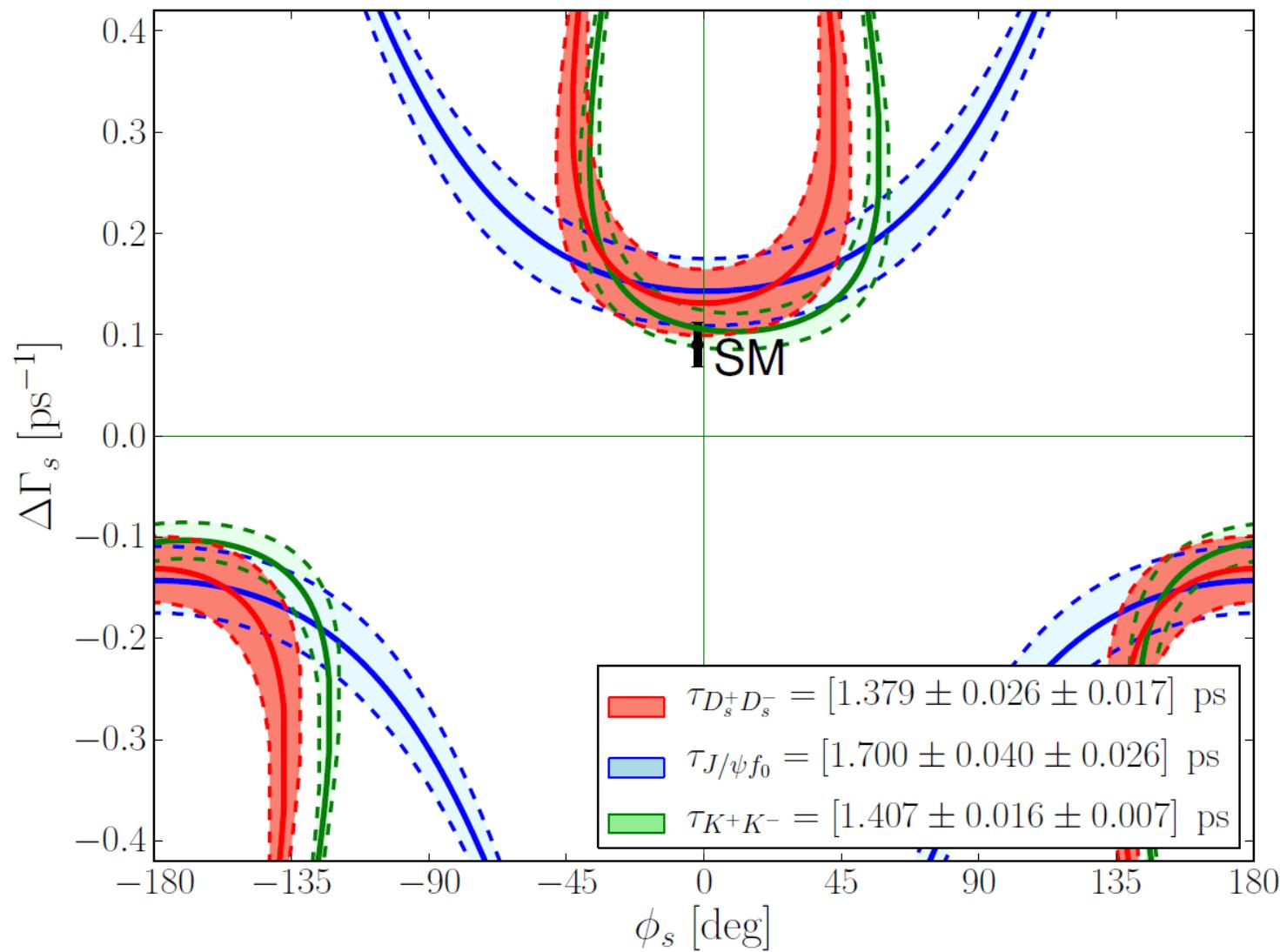
Column1: only  $B_s \rightarrow J/\Psi (\pi\pi, KK)$

Column2:  $J/\Psi(\pi\pi, KK) + KK + DsD\bar{s} + J/\Psi K\bar{s}$

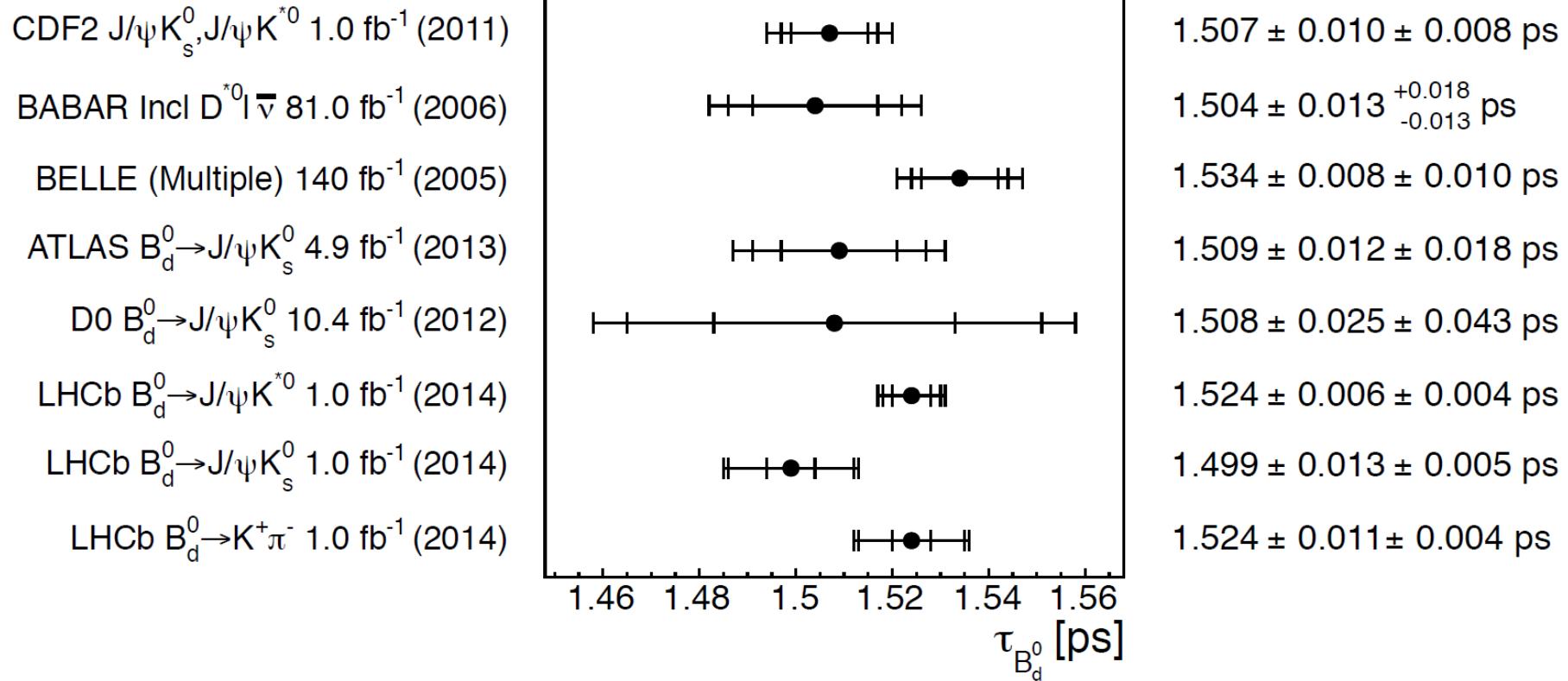
Column3:  $J/\Psi(\pi\pi, KK) + KK + DsD\bar{s} + J/\Psi K\bar{s} + Ds\pi + K\pi$

**Column4:  $J/\Psi(\pi\pi, KK) + DsD\bar{s} + Ds\pi + K\pi$**

# Constraints on $\phi_s$ and $\Delta\Gamma_s$



# B<sub>d</sub> Lifetime



# $B_s$ Flavour Specific (other measurements)

- ALEPH  $B_s \rightarrow D_s \bar{D}_s$  4M  $Z^0$  (1996)  
CDF1  $B_s \rightarrow D_s \bar{D}_s$  110  $\text{pb}^{-1}$  (1999)  
DELPHI  $B_s \rightarrow D_s \bar{D}_s$  3.6M  $Z^0$  (2000)  
OPAL  $B_s \rightarrow D_s \bar{D}_s$  4.4M  $Z^0$  (1998)  
D0  $B_s \rightarrow D_s \bar{D}_s$  0.4  $\text{fb}^{-1}$  (2006)  
CDF2  $B_s \rightarrow D_s \pi(X)$  1.3  $\text{fb}^{-1}$  (2011)  
LHCb  $B_s \rightarrow D^- D_s^+$  1.0  $\text{fb}^{-1}$  (2014)  
LHCb  $B_s \rightarrow \pi^+ K^-$  1.0  $\text{fb}^{-1}$  (2014)

