

Recent results on semileptonic B meson decays from Belle and Babar



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Topics

(I) exclusive $B \rightarrow D l \nu$ $|V_{cb}|$ [Belle]

(II) exclusive $B \rightarrow D^{(*)} \pi^+ \pi^- l \nu$ [Babar]

(III) semi-inclusive $B_s \rightarrow D_s^{(*)} X l \nu$ [Belle]

(IV) $D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$ [Babar]

All results are based on new analyses
All are preliminary

Belle and Babar

Belle (KEK) 1999-2010:

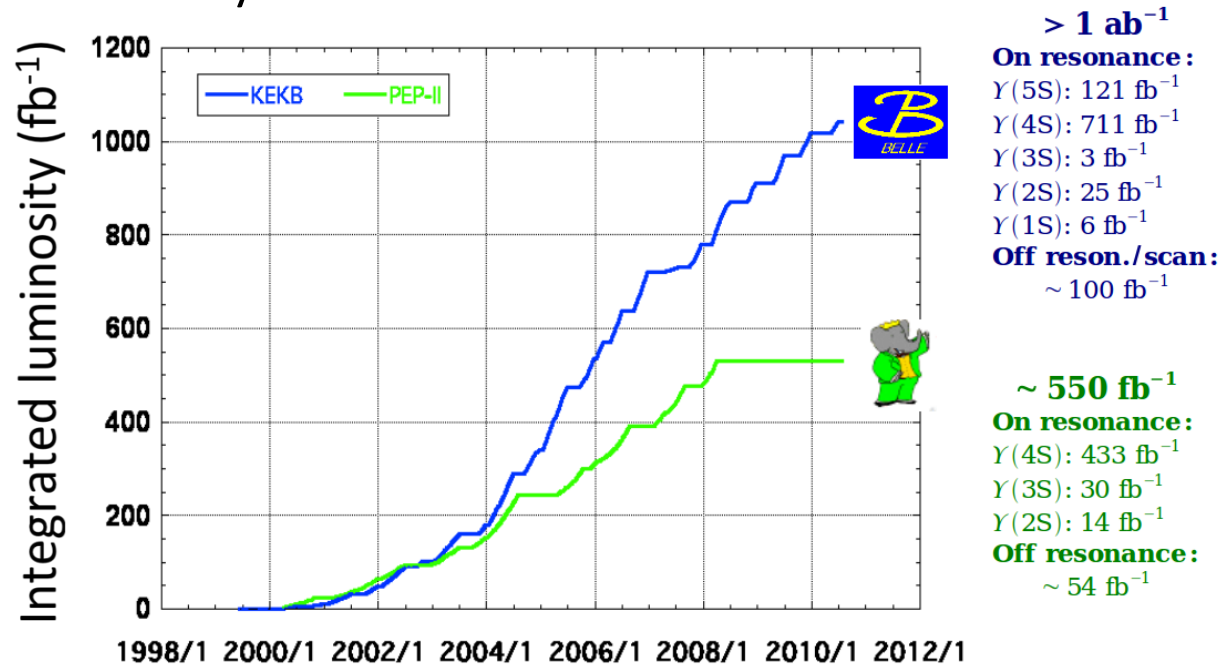
772×10^6 BB pairs at Y(4S)

7.1×10^6 $B_s B_s$ pairs at Y(5S)

Babar (SLAC) 1999-2008:

471×10^6 BB pairs at Y(4S)

History of data collection: Belle and Babar



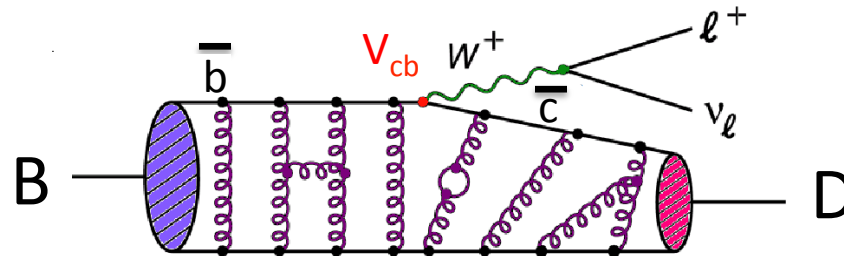


(I) $B \rightarrow Dlv$ from Belle

Updates previous result [PLB526 (2002) 258, 10.2 fb^{-1}]
using the full Belle $Y(4S)$ data sample [711 fb^{-1}]



B → Dℓν and |V_{cb}|



Differential decay rate for exclusive B → Dℓν described by

$$\frac{d\Gamma(B \rightarrow D\ell\nu)}{dw} = \frac{G_F^2}{48\pi^3} m_D^3 (m_B + m_D)^2 (w-1)^{3/2} |\eta_{EW}|^2 |V_{cb}|^2 \mathcal{G}(w)^2$$

$$w = v_B \cdot v_D = \frac{m_B^2 + m_D^2 - q^2}{2m_B m_D} = \text{product of 4-velocities}; \quad q^2 = (p_\ell + p_\nu)^2$$

- $w = 1$ corresponds to zero recoil (D meson produced at rest, q^2 is maximal)
- η_{EW} = electroweak correction = 1.0066 [A. Sirlin, Nucl. Phys. B196 (1982) 83]
- $\mathcal{G}(w)$ = form factor (only one form factor required for $m_l \ll m_B$)



B \rightarrow Dlv and $|V_{cb}|$

- $G(w=1)$ predicted by theory (lattice QCD)
- Extrapolate the measured differential decay rates to $w=1$ using a parameterization of the form factor $G(w)$
- Standard parameterization of $G(w)$: [Caprini et al., Nucl. Phys. B520 (1998) 153]

$$G(w) = G(1)[1 - 8\rho^2 z + (51\rho^2 - 10)z^2 - (252\rho^2 - 84)z^3]$$

$$z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

ρ = the shape parameter

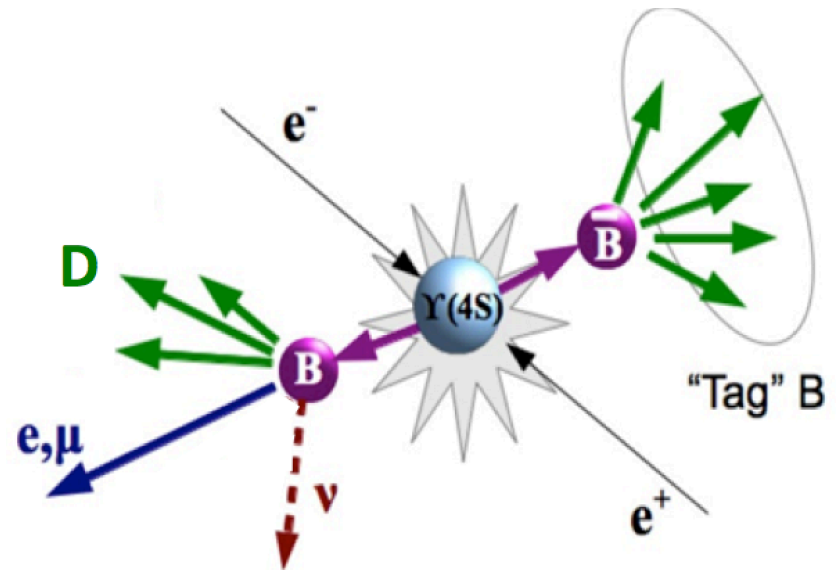
\rightarrow simultaneously determine ρ^2 and the overall normalization $\eta_{EW} G(1) |V_{cb}|$



$B \rightarrow D\ell\nu$ and $|V_{cb}|$

- $770 \times 10^6 Y(4S) \rightarrow BB$ events
- Full reconstruction of the hadronic decay of one B ($=B_{\text{tag}}$)

- More than 1110 distinct exclusive channels
- Allows reconstruction of the 4-momenta of both B mesons and thus of the neutrino





B \rightarrow Dlv and $|V_{cb}|$

- The other B ($=B_{\text{sig}}$) is reconstructed in 1 of 4 final states:
 - $\bar{B}^0 \rightarrow D^+ l^- \bar{\nu}$
 - $B^- \rightarrow \bar{D}^0 l^- \bar{\nu}$
- $l = e, \mu$

D meson reconstruction:

$$D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^- \pi^+, K_S \pi^+ \pi^-, K_S \pi^+ \pi^- \pi^0, \\ K^- K^+, K_S \pi^0, \pi^+ \pi^-$$

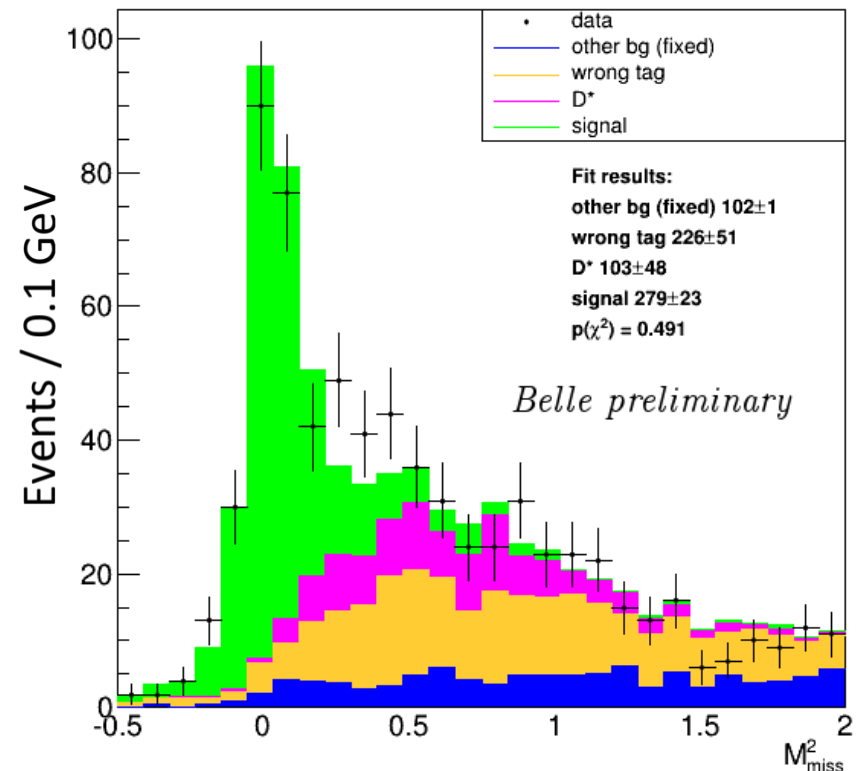
$$D^+ \rightarrow K^- \pi^+ \pi^+, K^- \pi^+ \pi^+ \pi^0, K_S \pi^+, K_S \pi^+ \pi^0, K^- K^+ \pi^+, \\ K_S K^+, K_S \pi^+ \pi^- \pi^+$$



B \rightarrow D ν and $|V_{cb}|$

Calculate the missing mass: $M_{miss}^2 = [p_{\Upsilon(4S)} - p_{B_{tag}} - p_D - p_l]^2$

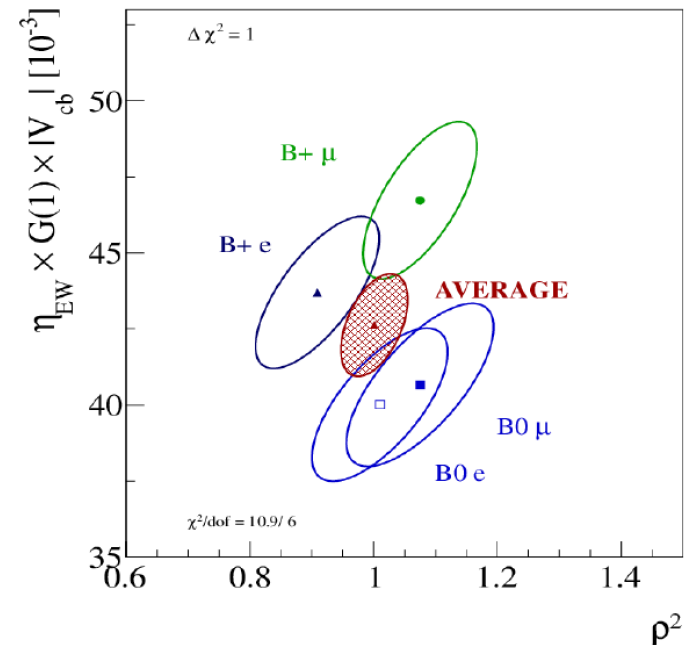
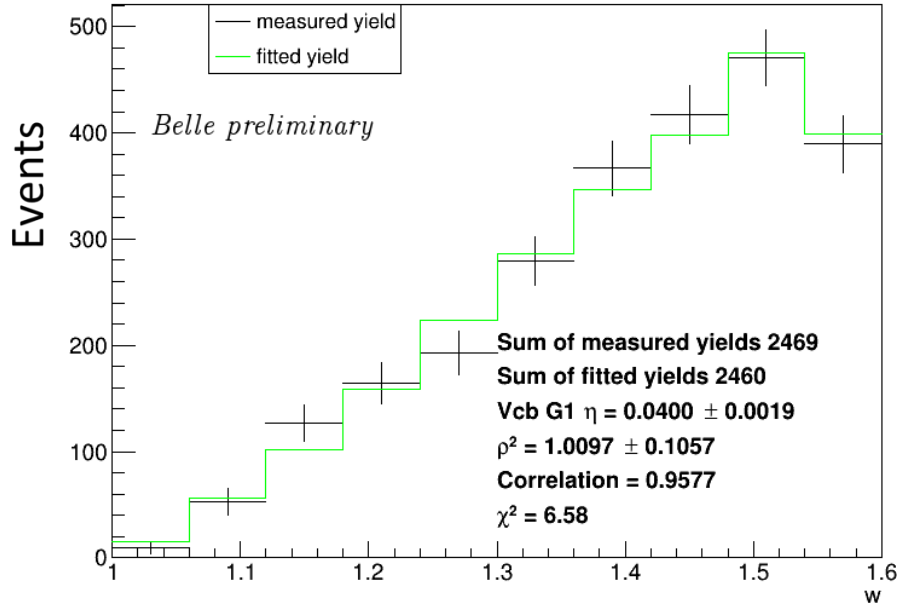
- M_{miss}^2 peaks at zero for events with one missing neutrino
- Events with unreconstructed particles (e.g. $D^* \rightarrow \pi D$) yield larger M_{miss}^2
- Use maximum likelihood fit to determine signal and background yields
- MC used to describe signal and background shapes





B \rightarrow D ν and $|V_{cb}|$

- Determine signal yields in 10 bins of w
- Subtract background and correct for detection efficiency
- Fit form factor $G(w)$ to determine ρ^2 and normalization $\eta_{EW} G(1) |V_{cb}|$





B \rightarrow Dlv and $|V_{cb}|$

Preliminary combined results (4 channels):

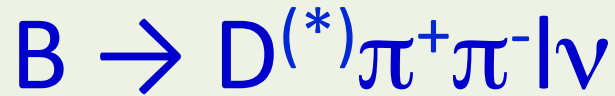
$$\eta_{EW} \mathcal{G}(1) |V_{cb}| = 42.63 \pm 0.96 \text{ (stat)} \pm 1.39 \text{ (syst)} \times 10^{-3}$$
$$\rho^2 = 1.001 \pm 0.051 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

- Improves precision of previous Belle result by a factor of 4
- Most precise single measurement (preliminary)
- Compares well in precision to current world average from Heavy Flavor Averaging Group:

$$\eta_{EW} \mathcal{G}(1) |V_{cb}| = 42.64 \pm 0.72 \text{ (stat)} \pm 1.35 \text{ (syst)} \times 10^{-3}$$
$$\rho^2 = 1.186 \pm 0.036 \text{ (stat)} \pm 0.041 \text{ (syst)}$$



(II) $B \rightarrow D^{(*)} \pi^+ \pi^- \nu$ from Babar



Measurements of exclusive B meson $b \rightarrow cl\nu$ decays exist for:

- $B \rightarrow D^{(*)}l\nu$ [Belle, Babar, CLEO, ARGUS]
- $B \rightarrow D^{(*)}\pi l\nu$ [Belle PRD 77 (2008) 091503;
Babar PRL 100 (2008) 151802]

The sum of measured exclusive rates does not saturate the well-determined inclusive rate: $BF(B \rightarrow X_c l\nu) = 10.92 \pm 0.17\%$

$$BF(B \rightarrow X_c l\nu) - \Sigma [BF(B \rightarrow D^{(*)}l\nu) + BF(B \rightarrow D^{(*)}\pi l\nu)] \\ = 1.45 \pm 0.29\%$$

[Bernlochner, Ligeti, Turczk, PRD 85 (2012) 094033]



$$B \rightarrow D^{(*)}\pi^+\pi^-l\nu$$

It is of interest to identify & measure the “missing” channels

- non-resonant ?
- higher mass D^{**} state ?
- consistency with heavy-quark effective theory (HQET)

Better understanding of higher multiplicity $B \rightarrow X_c l \nu$ decays can potentially reduce systematic uncertainties for

- V_{cb} and V_{ub} (for both, $\sim 3\sigma$ discrepancy between results from inclusive and exclusive decays)
- $B \rightarrow D^{(*)}\tau l \nu$ (Babar observes a 3.4σ discrepancy with the standard model [PRL 109 (2012) 101802 ; PRD 88 (2013) 072012])



$$B \rightarrow D^{(*)}\pi^+\pi^-l\nu$$

- $471 \times 10^6 Y(4S) \rightarrow BB$ events
- Full reconstruction of the hadronic decay of one B ($=B_{\text{tag}}$)

- The other B ($=B_{\text{sig}}$) is reconstructed in 1 of 12 final states:
 $D^{(*)}l\nu$; $D^{(*)}\pi^\pm l\nu$; $D^{(*)}\pi^+\pi^-l\nu$; $l = e, \mu$

- No additional charged tracks

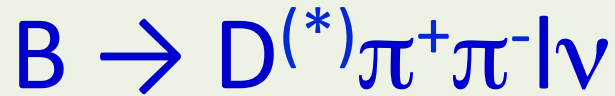
- $D^{(*)}$ meson reconstruction:

$$D^0 \rightarrow K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^-\pi^+, K_S\pi^+\pi^-, K^-K^+, K_S\pi^0, \pi^+\pi^-$$

$$D^+ \rightarrow K^-\pi^+\pi^+, K^-\pi^+\pi^+\pi^0, K_S\pi^+, K_S\pi^+\pi^0, K^-K^+\pi^+, K_SK^+, K_S\pi^+\pi^-\pi^+$$

$$D^{*+} \rightarrow D^0\pi^+, D^+\pi^0$$

$$D^{*0} \rightarrow D^0\pi^0, D^0\gamma$$



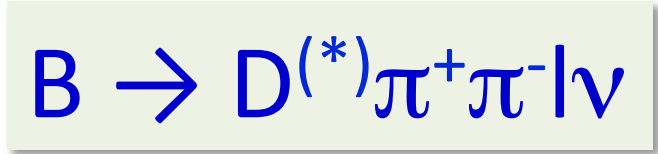
- Determine missing 4-momentum \mathbf{p}_{miss} in event

$$\mathbf{p}_{\text{miss}} = \mathbf{p}_{\Upsilon(4S)} - \mathbf{p}_{\text{Btag}} - \mathbf{p}_{D^{(*)}(\pi)(\pi\pi)l} = (E_{\text{miss}}, \vec{\mathbf{p}}_{\text{miss}})$$

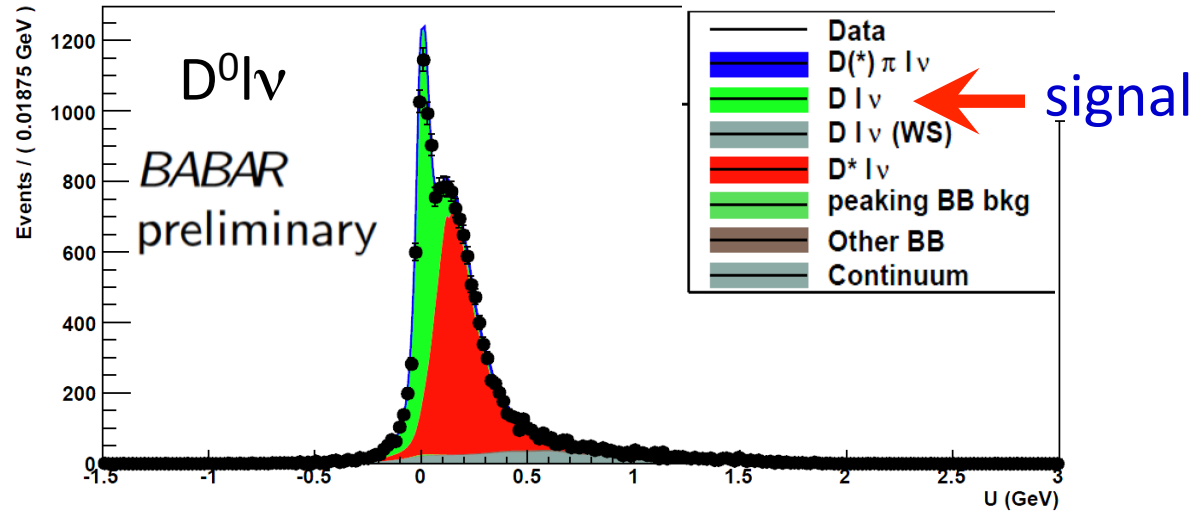
- Define $U \equiv E_{\text{miss}} - |\vec{\mathbf{p}}_{\text{miss}}|$
- U peaks at zero for signal events: $E_{\text{miss}} = |\vec{\mathbf{p}}_{\text{miss}}|$ for neutrinos
- $U \neq 0$ for events with additional unreconstructed particles

Maximum-likelihood fit of the U distribution

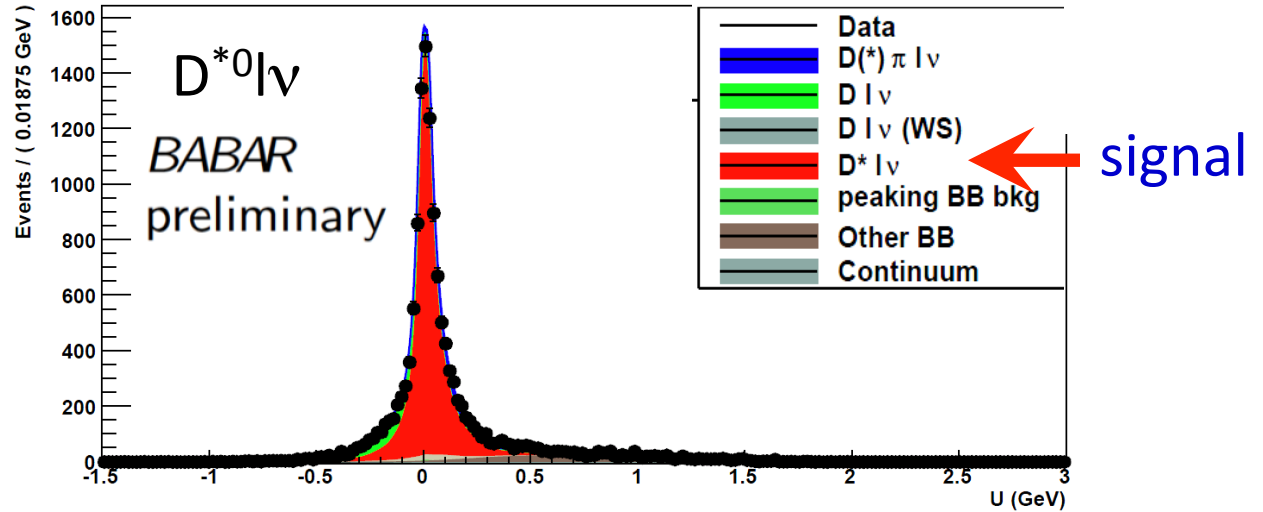
- MC-derived shapes for signal and background components
- Signal and background event yields floated
- Fit procedure validated with toy MC ensembles



Normalization
mode: $D^{(*)0} l \nu$



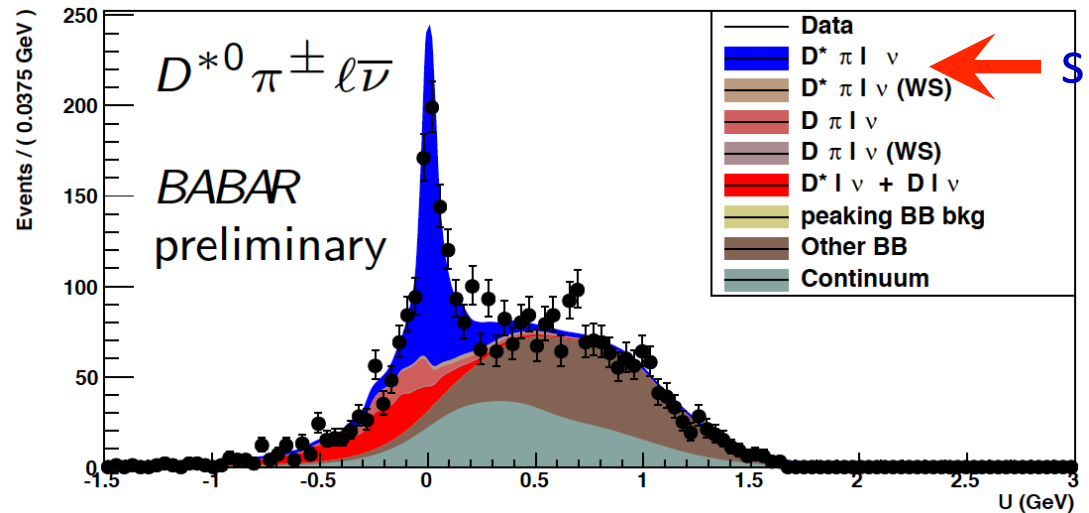
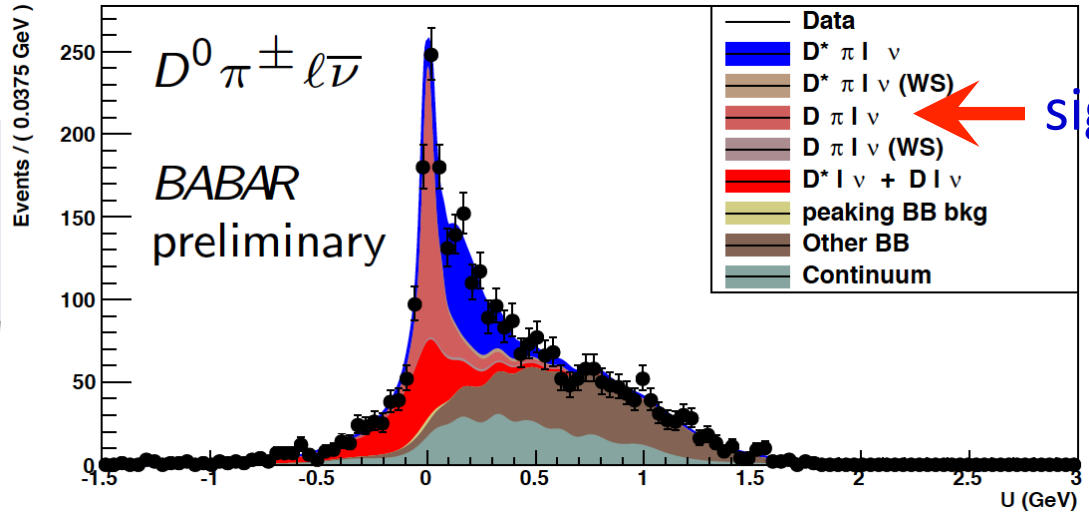
WS = wrong sign
(charge of B_{sig} incorrectly
determined)





$$B \rightarrow D^{(*)} \pi^+ \pi^- \ell \bar{\nu}$$

One-pion
mode: $D^{(*)0} \pi^\pm \ell \bar{\nu}$

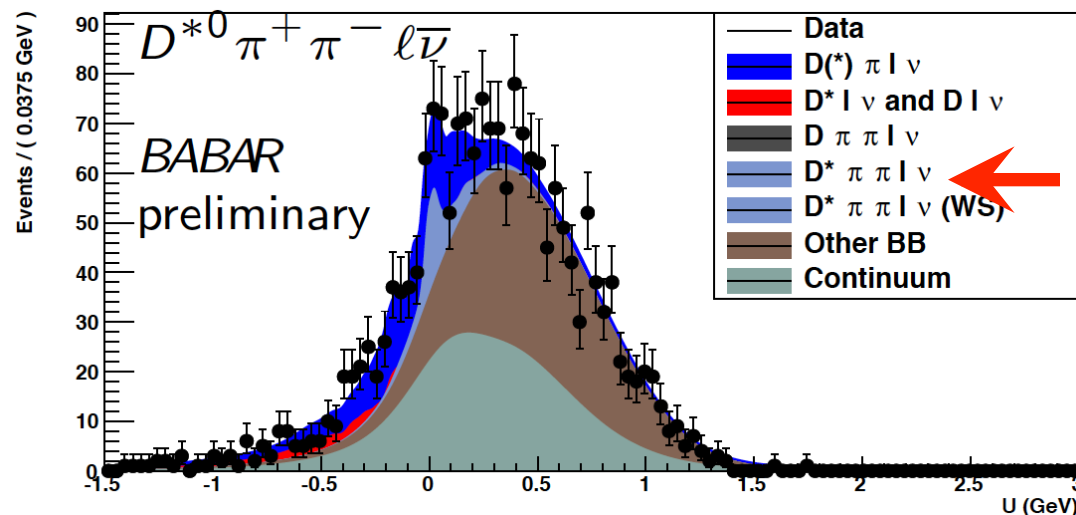
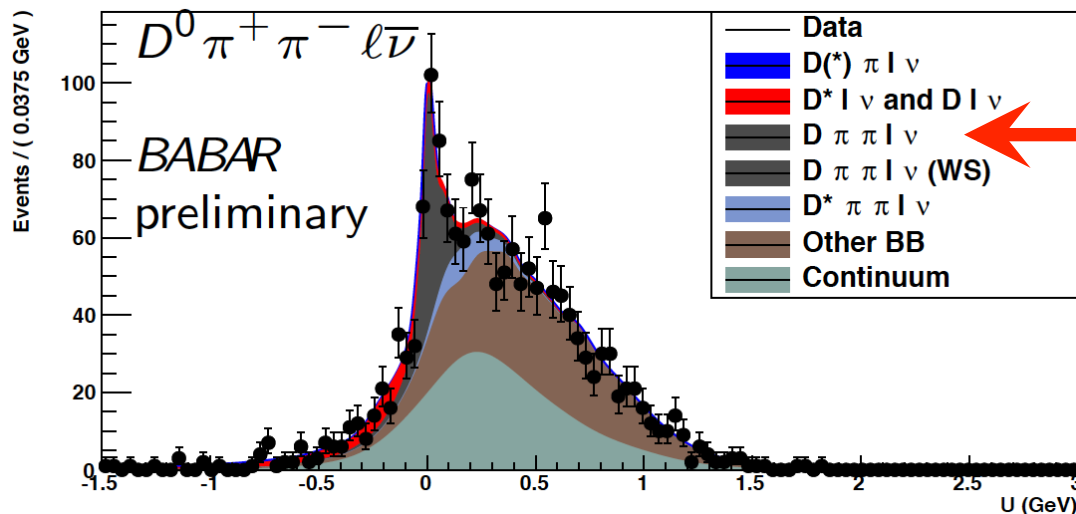




$$B \rightarrow D^{(*)} \pi^+ \pi^- \ell \bar{\nu}$$

Two-pion
mode:
 $D^{(*)0} \pi^+ \pi^- \ell \bar{\nu}$

clear $D^0 \pi \pi \ell \bar{\nu}$
signal: 4.4 σ
 $D^{*0} \pi \pi \ell \bar{\nu}$: 1.9 σ



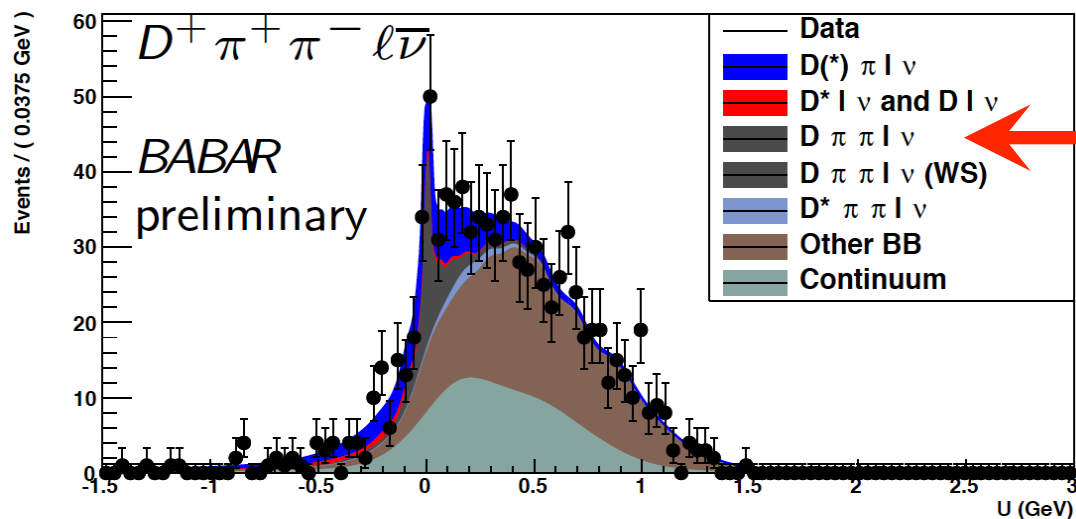


$$B \rightarrow D^{(*)} \pi^+ \pi^- \ell \bar{\nu}$$

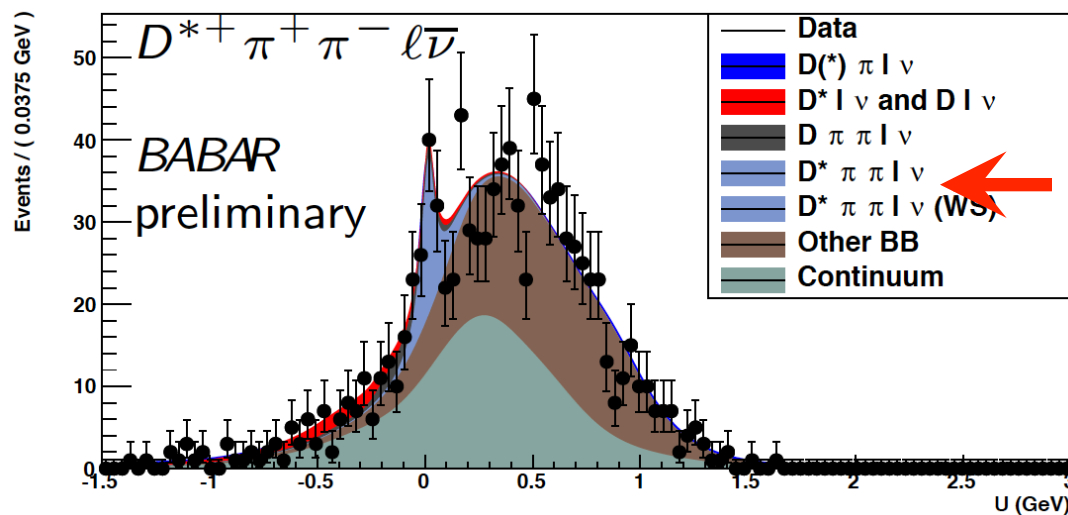
Two-pion
mode:
 $D^{(*)+} \pi^+ \pi^- \ell \bar{\nu}$

$D^+ \pi \pi \ell \bar{\nu}$: 2.6σ

$D^{*+} \pi \pi \ell \bar{\nu}$: 2.9σ



signal



signal



$$B \rightarrow D^{(*)}\pi^+\pi^-l\nu$$

Babar Preliminary

Signal	Normalization	$R_{n\pi}^{(*)}$	$B \rightarrow D^{(*)}n\pi l\nu$ branching ratio
$D\pi^\pm$	D	$0.1873 \pm 0.0107 \pm 0.0086$	$0.4476 \pm 0.0256 \pm 0.0206 \pm 0.0225$
$D^*\pi^\pm$	D^*	$0.1234 \pm 0.0056 \pm 0.0061$	$0.6108 \pm 0.0277 \pm 0.0302 \pm 0.0136$
$D\pi^+\pi^-$	D	$0.0733 \pm 0.0139 \pm 0.0081$	$0.1752 \pm 0.0332 \pm 0.0194 \pm 0.0088$
$D^*\pi^+\pi^-$	D^*	$0.0214 \pm 0.0062 \pm 0.0030$	$0.1059 \pm 0.0307 \pm 0.0149 \pm 0.0024$

Results for charged and neutral B's are combined



stat



syst



BF of
normalization
mode

- $D^{(*)}\pi^\pm l\nu$ results consistent with current world averages and about 20% more precise

- $D\pi^+\pi^- l\nu$ combined results: $5.1\sigma \rightarrow$ first observation
- $D^*\pi^+\pi^- l\nu$ combined results: $3.5\sigma \rightarrow$ first evidence

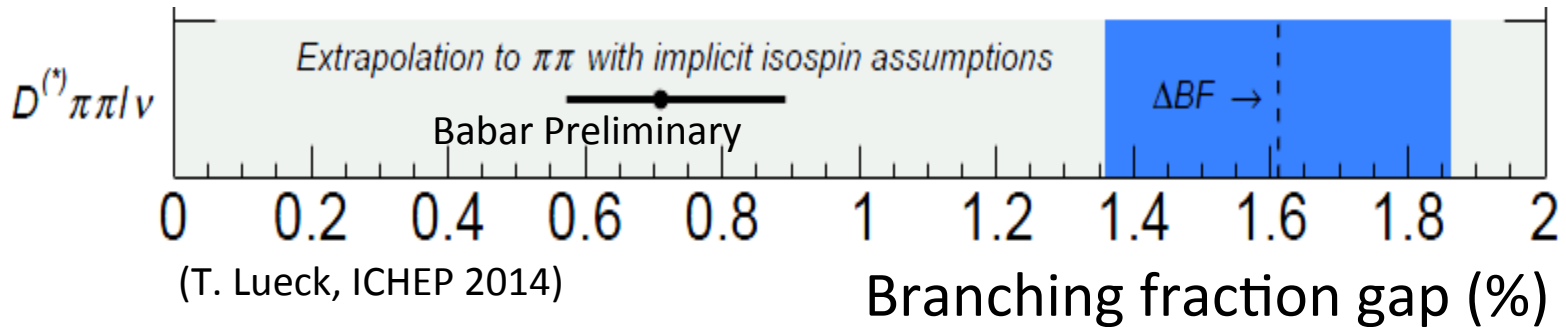


$$B \rightarrow D^{(*)}\pi^+\pi^-l\nu$$

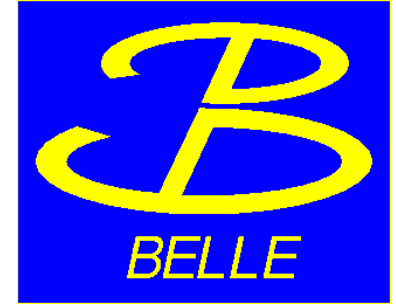
Impact on the inclusive – exclusive branching fraction gap:

$$\begin{aligned} \text{BF}(B \rightarrow X_c l \nu) - \Sigma[\text{BF}(B \rightarrow D^{(*)} l \nu) + \text{BF}(B \rightarrow D^{(*)} \pi l \nu)] \\ = 1.45 \pm 0.29\% \end{aligned}$$

[Bernlochner, Ligeti, Turczk, PRD 85 (2012) 094033]



The gap is reduced by about 60% but not fully explained !



(III) $B_s \rightarrow D_s^{(*)} X l \nu$ from Belle



$$B_s \rightarrow D_s^{(*)} X l \nu$$

- Exploit world's largest $Y(5S)$ sample: 7.1 million $B_s B_s$ events
- Belle uniquely positioned for precision measurements of B_s branching fractions
- Measure $B_s \rightarrow D_s$ and $B_s \rightarrow D_s^*$ inclusive semileptonic transitions: “semi-inclusive”
- $D_s X l \nu$: “X” includes feeddown from D_s^* & D_s^{**}
- $D_s^* X l \nu$: “X” includes feeddown from D_s^{**}

Current PDG entries

- $\text{BF}[B_s \rightarrow D_s X l \nu] = 7.9 \pm 2.4\%$ [Aleph, Delphi, OPAL]
- $\text{BF}[B_s \rightarrow D_s^* X l \nu]$: no results



- D_s^- reconstructed in the $\phi\pi^-$ decay mode with $\phi \rightarrow K^+K^-$
- D_s^{*-} reconstructed in the $D_s^- \gamma$ decay mode
- Require event to contain charged lepton l ($= e, \mu$) of opposite sign to the $D_s^{-(*)}$

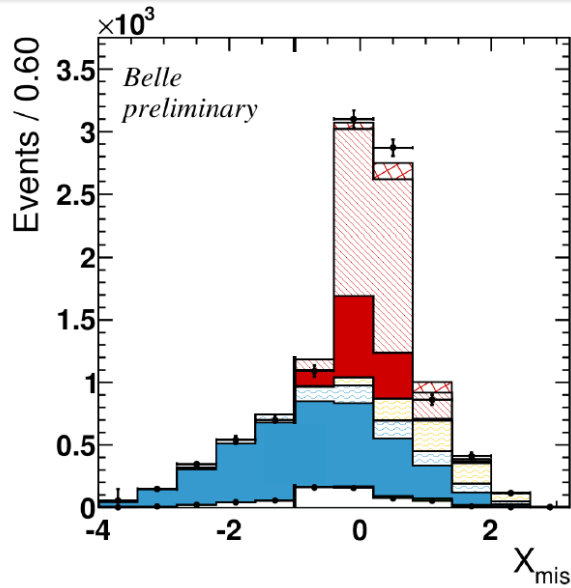
Examine events using the X_{mis} variable

$$X_{\text{mis}} \equiv \frac{E_{\text{beam}}^* - E_{\text{vis}}^* - p_{\text{vis}}^*}{p_{\text{beam}}^*} \quad E_{\text{vis}}^* \ \& \ p_{\text{vis}}^* \ \text{exclude } B_{\text{tag}} \ \text{daughters}$$

X_{mis} peaks at zero for signal events



X_{mis} distribution for $D_s X e \nu$ candidates:



- off res. data (continuum)
- $B \rightarrow D_s K l \nu$
- WS prompt } Wrong side (lepton and $D_s^{(*)}$ from different B_s)
- WS other }
- CS other } Secondary and fake leptons
- $B_s \rightarrow D_s l \nu$ } Signal
- $B_s \rightarrow D_s^* l \nu$ }
- $B_s \rightarrow D_s^{**} l \nu$ }

Two principal background categories:

- 1) “Wrong side”: $D_s^{(*)}$ and lepton arise from different $B_s \rightarrow$ small X_{mis}
- 2) “Fakes”: 2ndry leptons & hadrons misidentified as leptons \rightarrow large X_{mis}



$$B_s \rightarrow D_s^{(*)} X l \nu$$

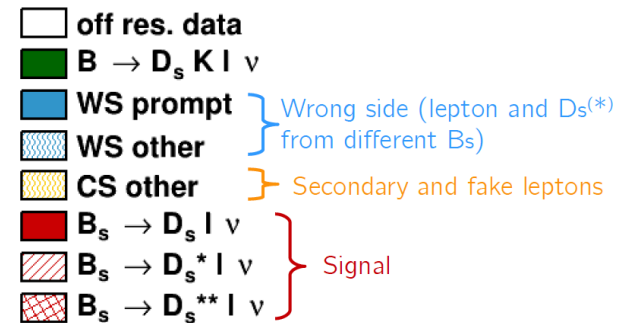
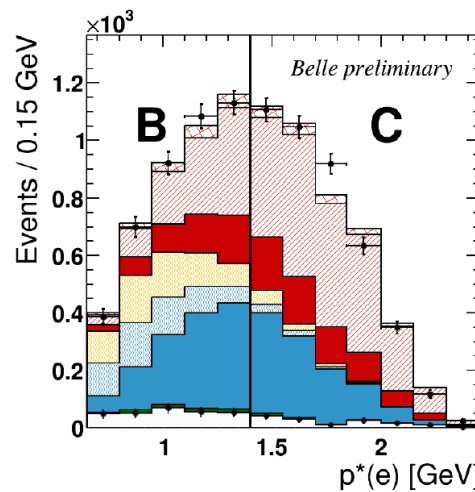
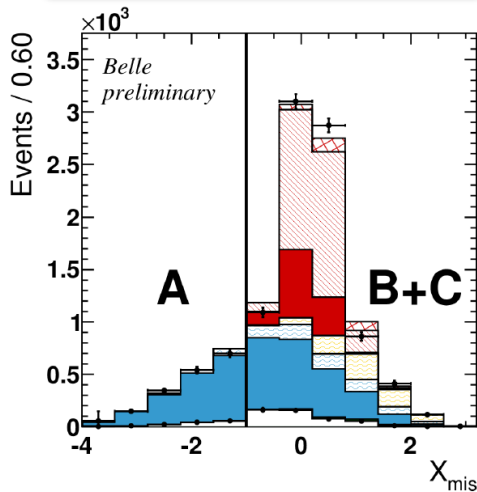
Divide data into three regions: A, B, and C

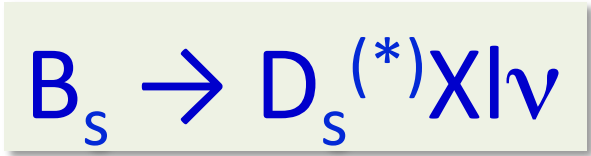
A: $X_{\text{mis}} < -1$: dominated by wrong-side background

B: $X_{\text{mis}} > -1$ and $p_l^* < 1.4$ GeV: enhances fake lepton component

C: $X_{\text{mis}} > -1$ and $p_l^* > 1.4$ GeV: enhanced signal-to-background ratio

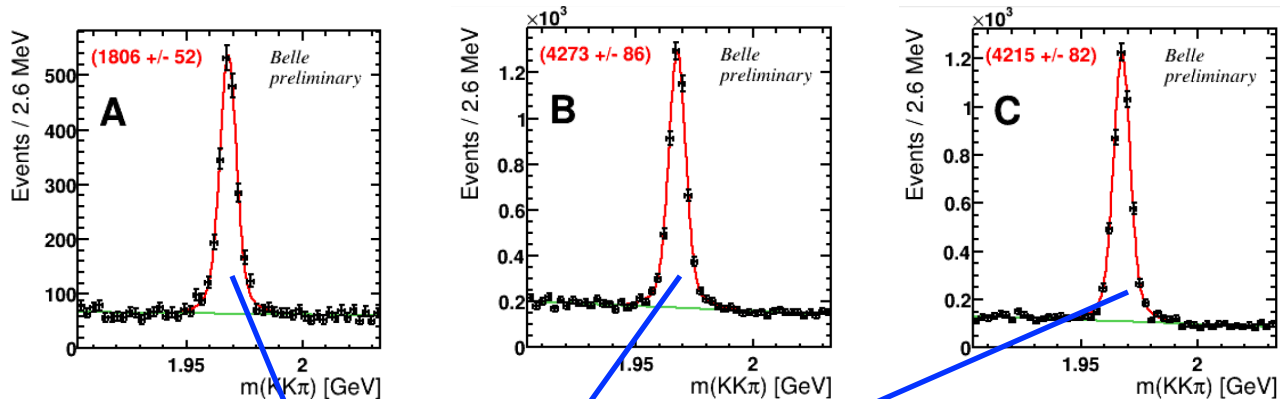
D_s Xev candidates:



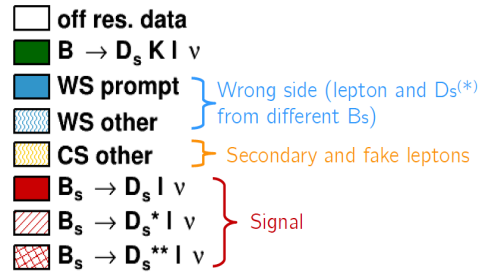
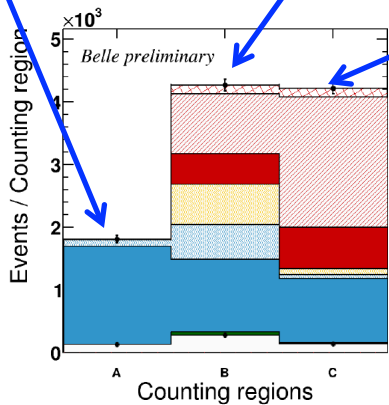


Fit number of D_s candidates in each region using the $m_{KK\pi}$ distribution:

$D_s X e \nu$:



- Subtract continuum & $D_s K l \nu$ backgrounds
- Adjust normalization of signal, WS, and fake (CS) templates to minimize χ^2

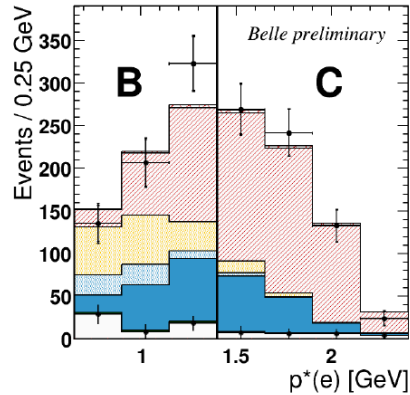
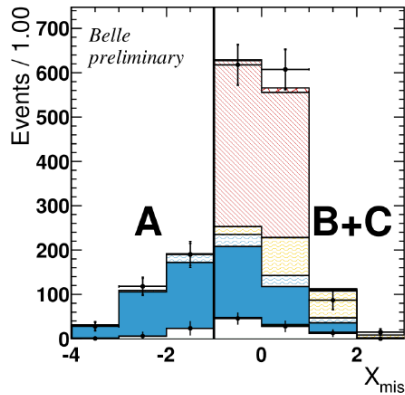




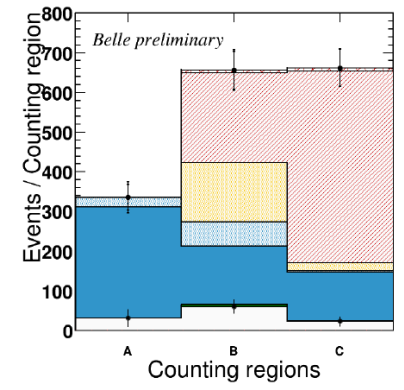
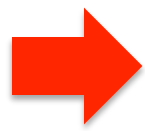
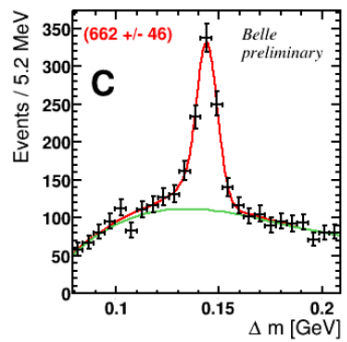
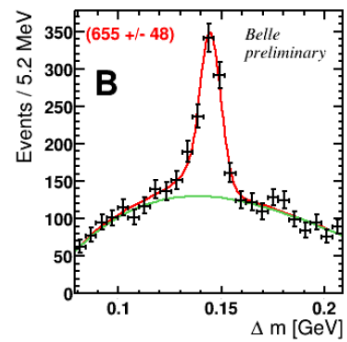
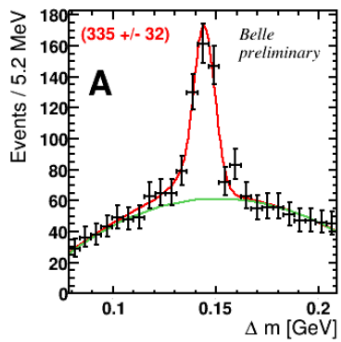
$$B_s \rightarrow D_s^{(*)} X l \nu$$

For $D_s^* X l \nu$ channels, fit the $\delta m = m_{kk\pi\gamma} - m_{kk\pi}$ distribution:

$D_s^* X e \nu$:



- off res. data
- $B \rightarrow D_s K l \nu$
- WS prompt
- WS other
- CS other
- $B_s \rightarrow D_s l \nu$
- $B_s \rightarrow D_s^* l \nu$
- $B_s \rightarrow D_s^{**} l \nu$





Results (e and μ channels combined):

Preliminary

Channel	Branching fraction (%)
$B_s \rightarrow D_s X l \nu$	8.2 ± 0.2 (stat) ± 0.8 (syst) ± 1.5 ($N_{B_s B_s}$)
$B_s \rightarrow D_s^* X l \nu$	5.4 ± 0.4 (stat) ± 0.5 (syst) ± 1.0 ($N_{B_s B_s}$)

- First evidence for the $B_s \rightarrow D_s^* X l \nu$ branching fraction ($\sim 4.5\sigma$)
- $B_s \rightarrow D_s X l \nu$ branching fraction agrees with PDG value [= $7.9 \pm 2.4\%$]; uncertainty reduced by 30% (expect to improve further with reductions to $\sigma_{N_{B_s B_s}}$)

- Results consistent with theory predictions for exclusive rates:

$$B_s \rightarrow D_s^* l \nu : 2-8\% \quad ; \quad B_s \rightarrow D_s l \nu + D_s^* l \nu : 3-12\%$$

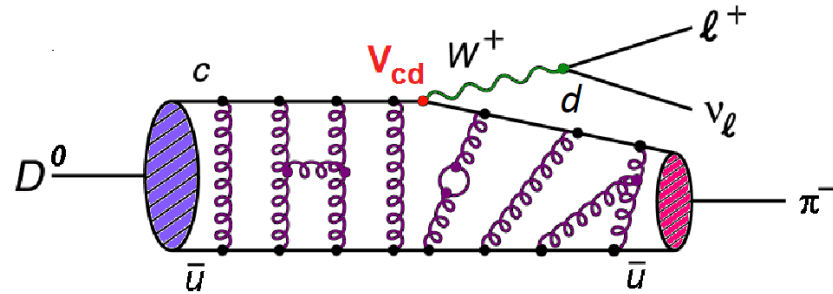


(IV) The $D^0 \rightarrow \pi^- e^+ \nu$ form factor
and $|V_{ub}|$ from Babar



$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$

$D^0 \rightarrow \pi^- e^+ \nu$ decays:



Since $m_e \ll m_D$, only one form factor contributes: $f_{+,D \rightarrow \pi}$

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cd}|^2 p_\pi^3 [f_{+,D \rightarrow \pi}(q^2)]^2$$

$p_\pi = \pi$ momentum in D rest frame

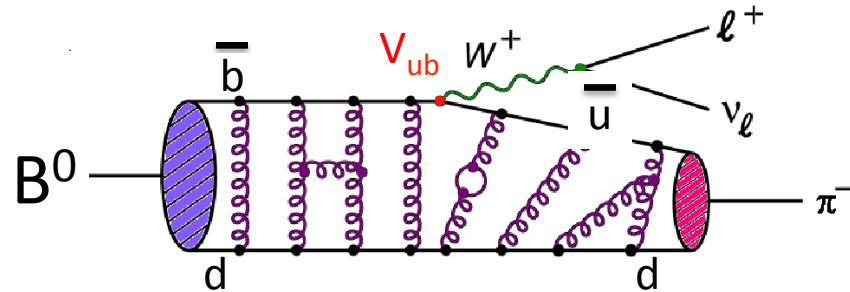
$$q^2 = (p_e + p_\nu)^2$$

- The form factor $f_{+,D \rightarrow \pi}$ can be related to the form factor $f_{+,B \rightarrow \pi}$ for $B^0 \rightarrow \pi^- e^+ \nu$ transitions [Isgur and Wise [PRD 42 (1990) 2388]]
- Provides an alternative theoretical approach to determine $|V_{ub}|$



$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$

$B^0 \rightarrow \pi^- e^+ \nu$ decays:



$$\frac{d\Gamma^B/dw_B}{d\Gamma^D/dw_D} = \frac{m_B}{m_D} \left(\frac{|V_{ub}|}{|V_{cd}|} \right)^2 \left| \frac{f_{+,B}^\pi(w_B)}{f_{+,D}^\pi(w_D)} \right|^2$$

$$w_{B,D} = \frac{M_{B,D}^2 + m_\pi^2 - q^2}{2M_{B,D}m_\pi} = \text{product of 4-velocities} = v_{B,D} \cdot v_\pi$$

$$\left| \frac{f_{+,B}^\pi(w_B)}{f_{+,D}^\pi(w_D)} \right| = \sqrt{\frac{m_B}{m_D}} \left[1 + \mathcal{O}\left(\frac{1}{m_{B,D}}\right) \right] \approx 1.8 \pm 0.2 \text{ (lattice calculations)}$$

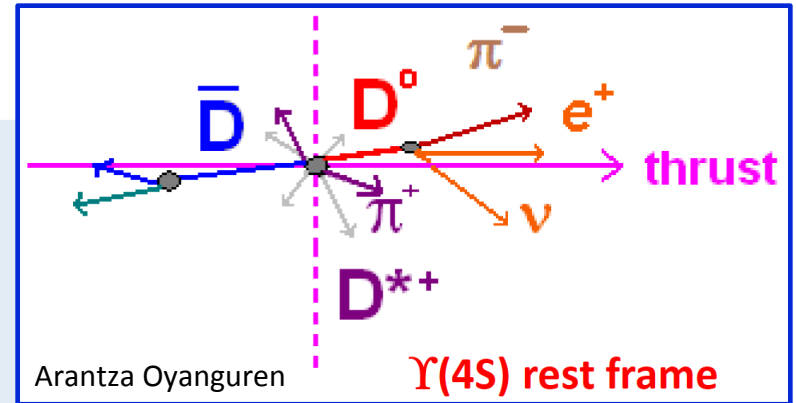
[J. Koponen 1311.6931, E. Dalgic et al., PRD73(2007)074502; J.A. Bailey et al., PRD79(2009)054507]

Use $d\Gamma_B/dw_B$ results from Babar $B^0 \rightarrow \pi^- e^+ \nu$ study in PRD86(2012)092004



$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$

- Select $D^0 \rightarrow \pi^- e^+ \nu$ candidates from $D^{*+} \rightarrow D^0 \pi^+$ decays
 - Divide event into hemispheres using the thrust axis
 - Require an identified π^- and e^+ within a hemisphere
 - Define D^0 momentum from $-\sum p$ over all particles except π^- , e^+
 - Define ν momentum from the missing momentum
 - Impose mass-constrained kinematic fit of $D^{*+} \rightarrow D^0(\rightarrow \pi^- e^+ \nu) \pi^+$ decay chain, require $\chi^2_{\text{fit}} > 0.01$

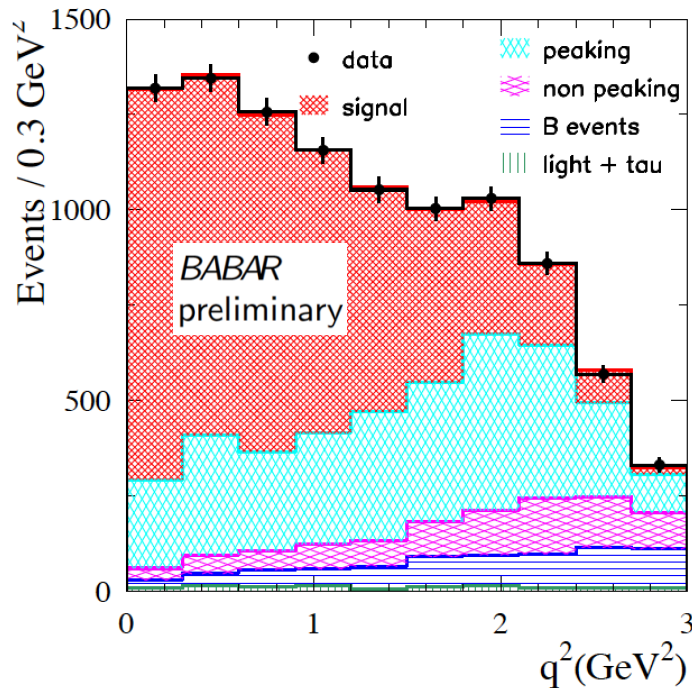


- Background from uds continuum and BB events reduced with Fisher discriminants, cut on $\delta m = m_{D^0 \pi^+} - m_{D^0}$
- “Peaking” background (true D^{*+}): use sideband data control samples.

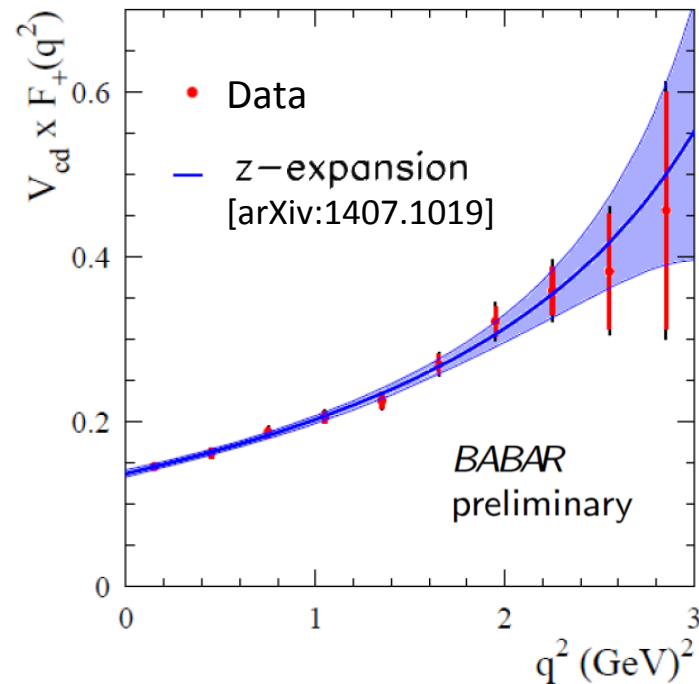


$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$

Extracted $D^0 \rightarrow \pi^- e^+ \nu$ signal yield:



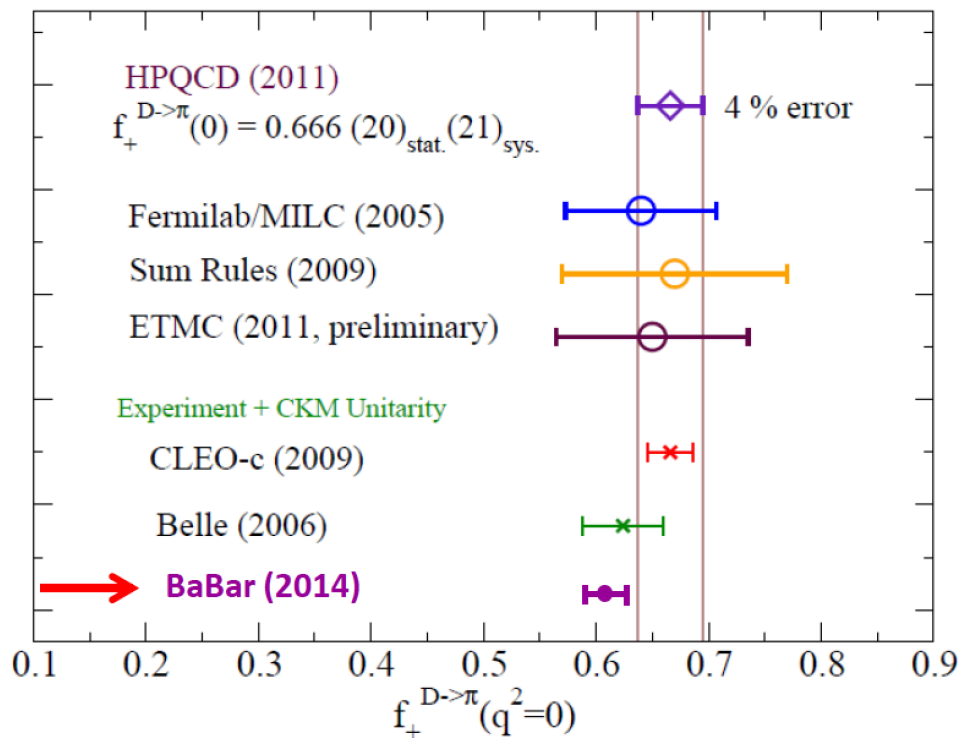
The $D^0 \rightarrow \pi^- e^+ \nu$ form factor:



Use power series (“z expansion”) parameterization of the form factor to extrapolate measured results to $q^2=0$



$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$



$$f_{+,D \rightarrow \pi}(0) = 0.610 \pm 0.017(\text{stat.}) \pm 0.010(\text{syst}) \pm 0.005(|V_{cd}|)$$

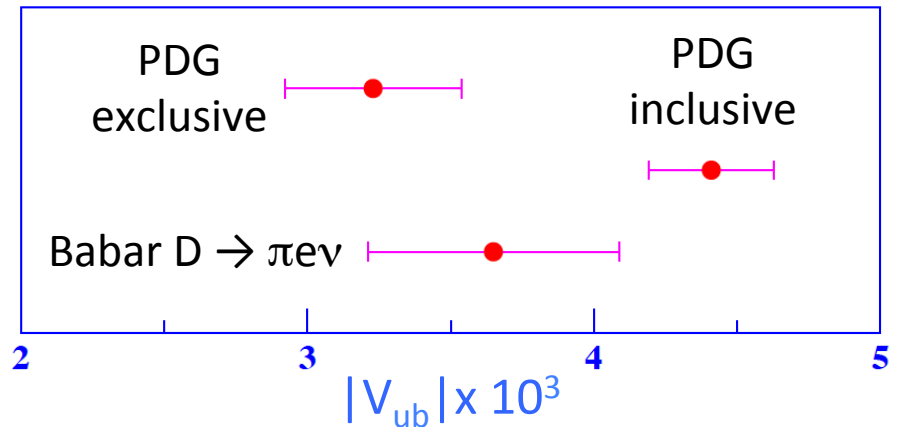
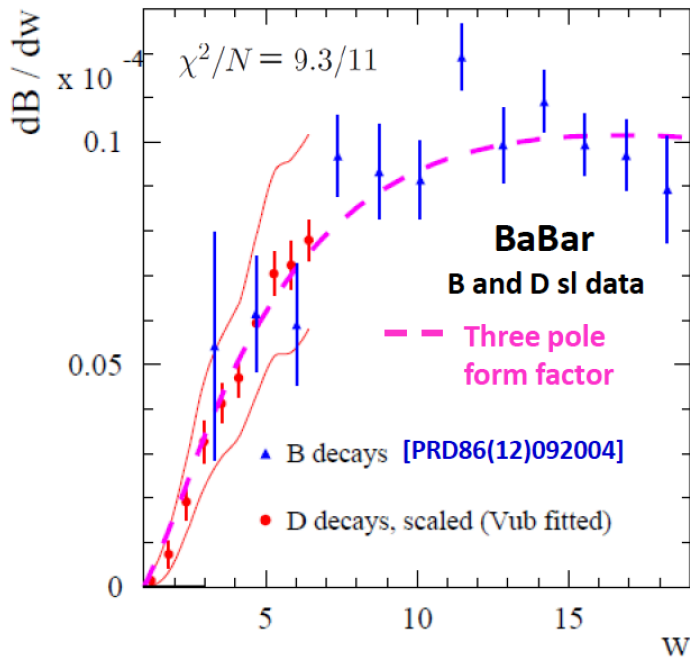
(using $|V_{cd}| = 0.2252 \pm 0.009$)

First result on this topic from Babar



$D^0 \rightarrow \pi^- e^+ \nu$ form factor and $|V_{ub}|$

- Combine $d\Gamma_{D \rightarrow \pi e \nu} / dw_B$ with the $d\Gamma_{B \rightarrow \pi e \nu} / dw_B$ measurements [PRD86(2012)092004]
- Use lattice results for $f_{+,B \rightarrow \pi} / f_{+,D \rightarrow \pi}$



$$\rightarrow |V_{ub}| = 3.65 \pm 0.18(\text{exp}) \pm 0.40(R_{B/D}) \times 10^{-3}$$

Alternative (“3 poles”) parameterization of the form factor:

$$\rightarrow |V_{ub}| = 2.6 \pm 0.2 \pm 0.4 \times 10^{-3}$$

[D. Becirevic et al., arXiv:1407.1019]



Summary



- Updated results (Belle) on $|V_{cb}|$ from exclusive $B \rightarrow Dlv$
→ the most precise single measurement (preliminary)
- First observation (Babar) of exclusive $B \rightarrow D^{(*)}\pi^+\pi^-lv$
→ explains $\sim 60\%$ of the inclusive-exclusive BF gap
in $b \rightarrow clv$ decays
- First evidence (Belle) for the $B_s \rightarrow D_s^*Xlv$ branching fraction
- New approach (Babar) to determine $|V_{ub}|$, based on
measurement of the $D^0 \rightarrow \pi^-e^+\nu$ form factor

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