

# Charmless B decays: 2 body and $B \rightarrow VV$

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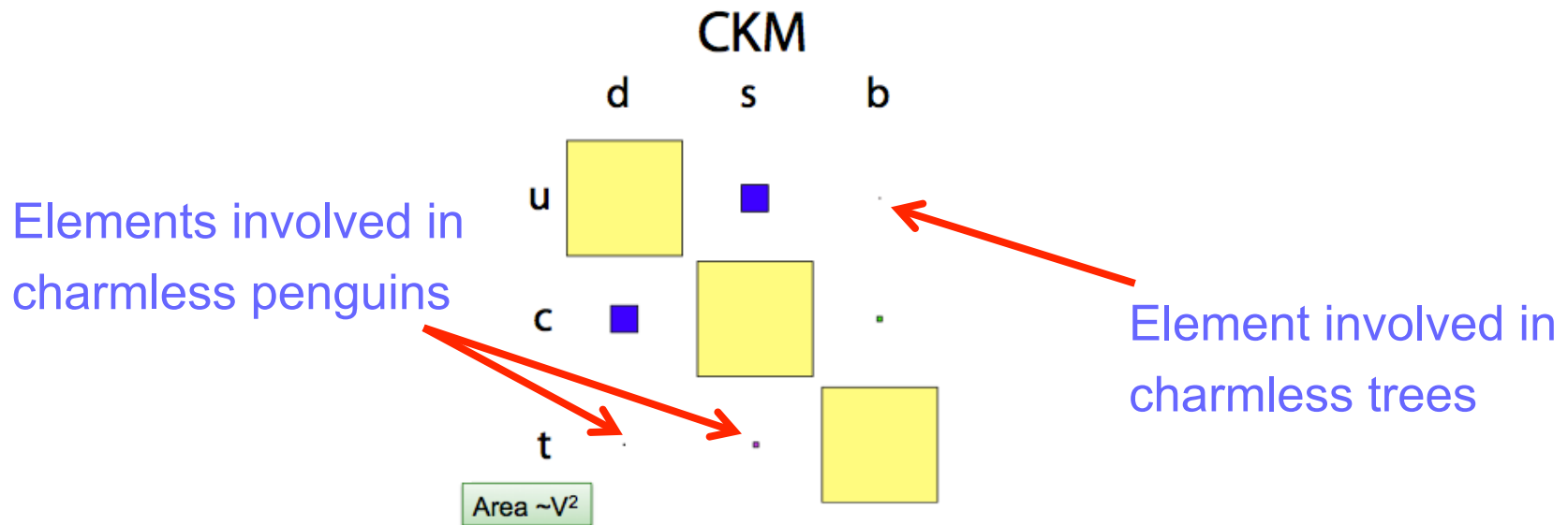
# Outline

- Introduction.
- B decays into  $K^{*\pm}h^{\mp}$ .
  - $B_s^0 \rightarrow K^{*\pm}K^{\mp}$  discovery.
  - $B_s^0 \rightarrow K^{*}\pi^+$  evidence.
  - Branching fraction measurements.
- $B \rightarrow V_1 V_2$  decays.
  - $B^0 \rightarrow \phi K^{*0}$ .
    - Angular analysis.
    - Direct and CP-asymmetries.
    - Triple products.
  - $B_s^0 \rightarrow \phi\phi$ .
    - Time-angular analysis.
    - Polarization parameters.
    - CP-violating phase measurement  $\phi_s$ .
    - Direct CP parameter  $|\lambda|$ .
    - Triple products.
- Conclusions.



# Charmless decays

- Suppressed compared to charmed:
  - $b \rightarrow u$  tree.
  - $b \rightarrow s, b \rightarrow d$  loops.
- More sensitive to New Physics.



# Direct CP Violation in B meson decays

Decays with Tree and Penguin contributions: interfere  $\Rightarrow$  CPV

$-\phi_{1,2}$  weak phases.

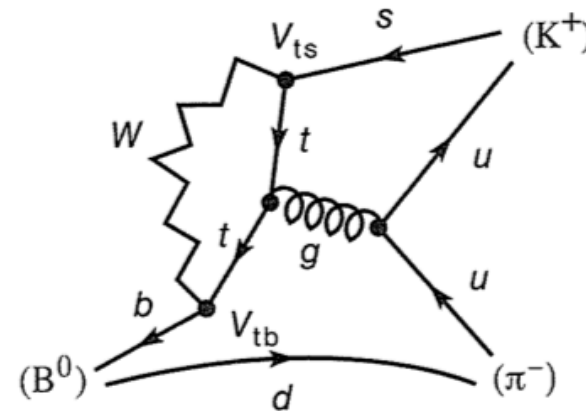
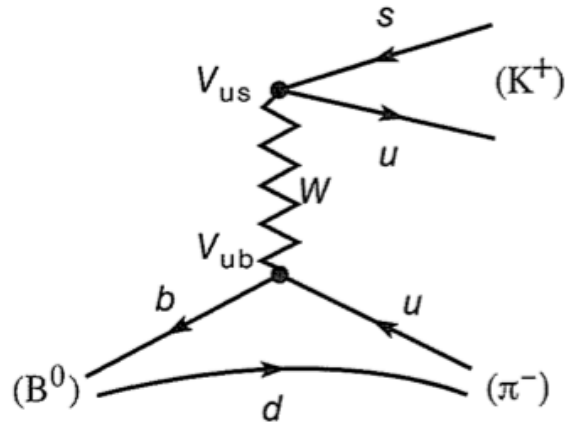
$-\theta_{1,2}$  strong phases.

$$A_1 = |A_1| e^{i\phi_1} e^{i\theta_1}$$

$$\bar{A}_1 = |A_1| e^{-i\phi_1} e^{i\theta_1}$$

$$A_2 = |A_2| e^{i\phi_2} e^{i\theta_2}$$

$$\bar{A}_2 = |A_2| e^{-i\phi_2} e^{i\theta_2}$$

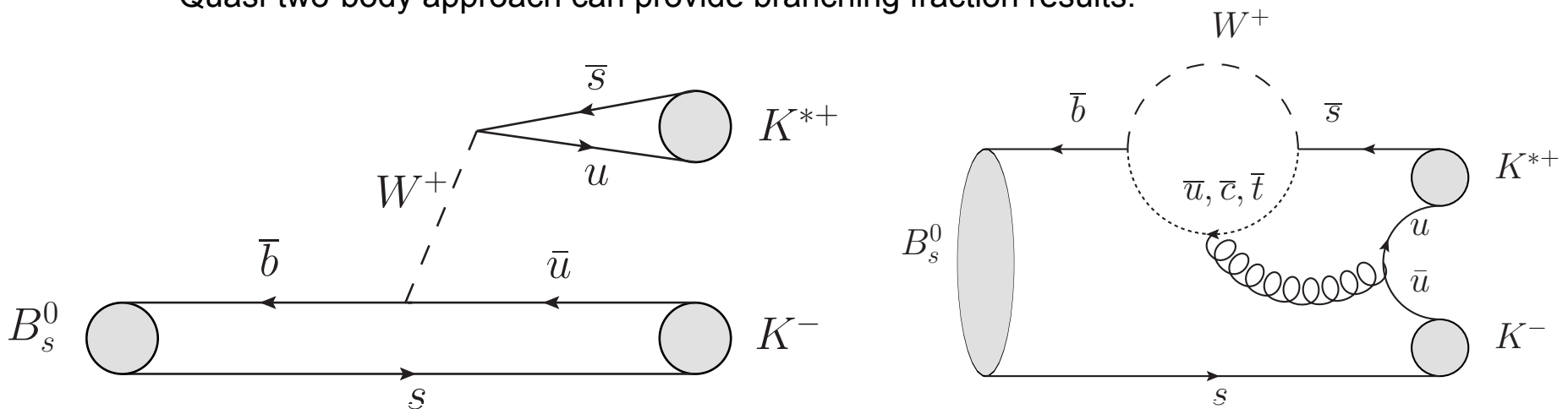


$$\left| \frac{\bar{A}}{A} \right|^2 = \left| \frac{\bar{A}_1 + \bar{A}_2}{A_1 + A_2} \right|^2 \neq 1 \Leftrightarrow \phi_1 \neq \phi_2 \ \&\& \ \theta_1 \neq \theta_2$$

# B decays into $K^{*\pm}h^\mp$

NEW

- 1 fb<sup>-1</sup> 2011 data sample.
- $B_{d,s}^0 \rightarrow K^{*\pm}h^\mp$  charmless VP modes.
  - Decay into  $K_S^0(\pi^+\pi^-)\pi^+h^-$  final states.
  - If  $h=\pi$  only  $B_s^0 \rightarrow K^{*-}\pi^+$ .
- Interference of penguin and tree contributions at the origin of CP-violating effects.
- Tests of U-spin symmetry, probe New Physics in loops and measure gamma.
- Full Dalitz plot treatment required to obtain better control of the hadronic uncertainties.
  - Eg. information on the relative phase between  $B^0 \rightarrow K^{*+}h^-$  and  $B^0 \rightarrow K_S^0\rho^0$ .
  - Will only be possible in the future with larger data samples.
- Undiscovered channels.
  - Quasi-two-body approach can provide branching fraction results.



# Selection of $B \rightarrow K^{*\pm} h^{\mp}$

NEW

- L0 Trigger (hardware):
  - Removes events with large occupancies in the scintillating-pad detector.
  - Requires one candidate with  $ET > 3.5$  GeV.
- High Level Trigger (software):
  - 2-4 track secondary vertex.
  - High sum of the pT of the tracks.
  - Significant displacement from the primary pp vertices.
- 1st filter with loose selections on topological variables:
  - Flight distance of the B candidate.
  - Direction of B momentum.
- Combinations of tracks consistent signal hypothesis categorized:
  - **“Long”**: both tracks from the  $K_S^0 \rightarrow \pi^+ \pi^-$  decay contain VELO hits.
  - **“Downstream”**: none of these tracks contain VELO hits.
- Long candidates: better mass, momentum and vertex resolution.
  - Different selection requirements for the two categories.
- Muon veto on the two “bachelor” tracks.
- Mass vetoes on charm and charmonia intermediate states.
- Particle identification mainly based on RICH information.
- NeuroBayes Multivariate discriminator with input variables:
  - Impact parameter  $\chi^2$ .
  - Vertex  $\chi^2$  for the  $K_S^0$  and B candidates.
  - Angle between the B candidate flight direction and PV-SV line.
  - The  $\chi^2$  of the separation between the PV and the decay vertex.
  - The B candidate  $p_T$ .
- Trained with simulated data and high four-body mass sideband.
- Optimized for maximizing the signal significance.

Trigger

Generic Offline Selection

Multivariate Selection

# Mass Spectra and Yields of $B \rightarrow K^{*\pm} h^\mp$ NEW

- Extended unbinned maximum likelihood fit of candidates with masses inside windows:
  - $5000 < m(K_S^0 h^\pm \pi^\mp) < 5500 \text{ MeV}/c^2$
  - $650 < m(K_S^0 \pi^\mp) < 1200 \text{ MeV}/c^2$
- Single 4- and 3-body simultaneous fit to candidates with both  $K_S^0$  categories.**
- Separate fits performed for  $K^{*\pm} K^\mp$  and  $K^{*\pm} \pi^\mp$  candidates.
- Fit components:
  - $B^0$  and  $B_s^0$  signal.
  - $B^0$  and  $B_s^0$  non-resonant components.
  - Misidentified  $B^0 \rightarrow K^{*\pm} h^\mp$  cross-feed.
  - Backgrounds from charmless decays with missing particles:  $\Lambda_b^0 \rightarrow K^{*-} p$  and  $B^+ \rightarrow D^0 h^+$ ,  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ .
  - Combinatorial background.
- Several pdf parameters constrained with simulated data and known physics magnitudes.

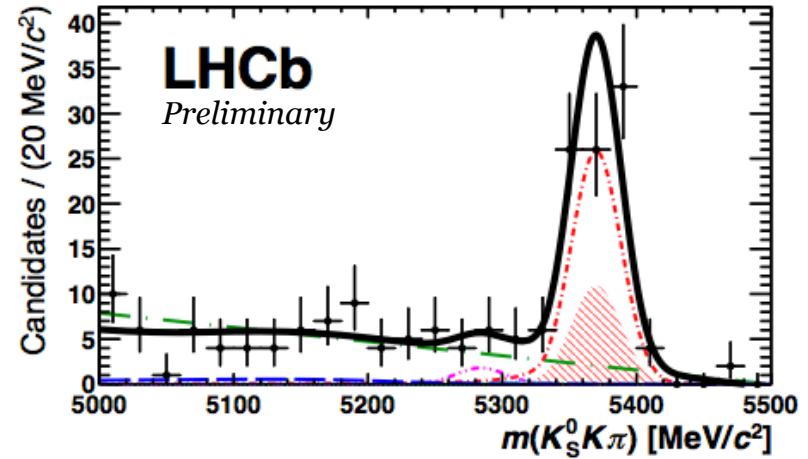
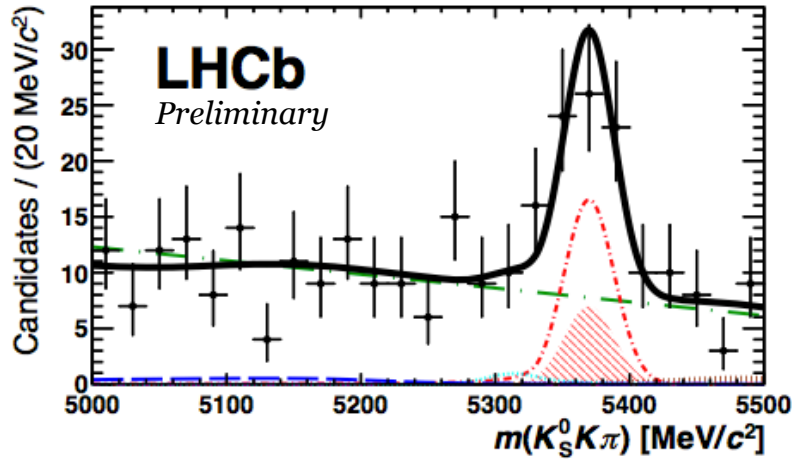
	$B^0$		$B_s^0$	
	long	downstream	long	downstream
$K^{*\pm} K^\mp$	$0 \pm 4$	$4 \pm 3$	$40 \pm 8$	$62 \pm 10$
$K^{*\pm} \pi^\mp$	$80 \pm 10$	$165 \pm 16$	$5 \pm 4$	$23 \pm 8$

# $K^{*\pm}K^{\mp}$ and $K^{*0}K^0$ Mass Spectra

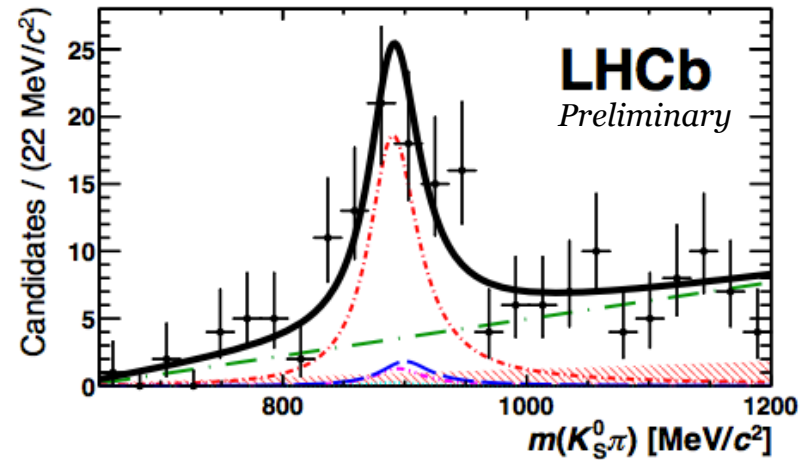
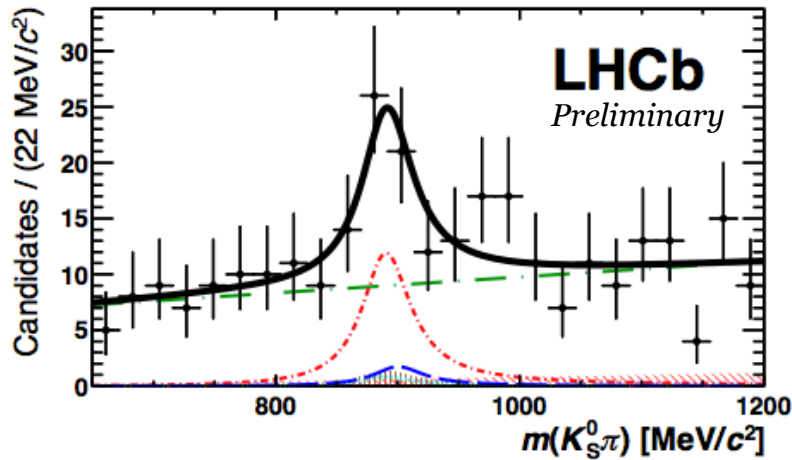
NEW

Long Category

Downstream Category



B Candidates



$K^*$  Candidates

$B_s^0 \rightarrow K^{*\pm}K^{\mp}$    
  $B^0 \rightarrow K^{*\pm}K^{\mp}$    
  $B_s^0 \rightarrow K_S^0 \pi^{\pm} K^{\mp}$    
  $\Lambda_b^0 \rightarrow K^{*0} p$    
 Combinatorial+Other   
  $B^0 \rightarrow K^{*0} \pi^-$

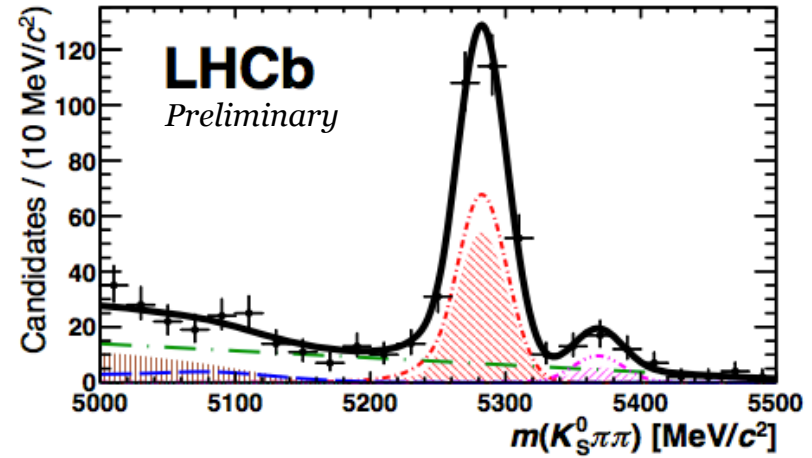
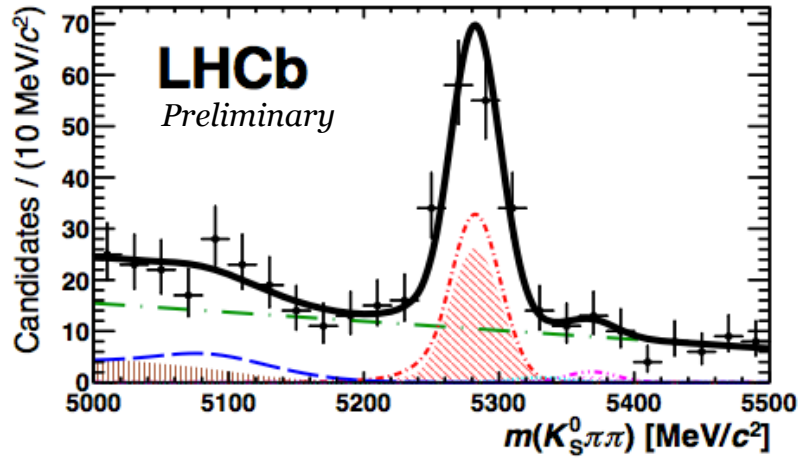


# $K^{*\pm}\pi^{\mp}$ and $K^{*\pm}$ Mass Spectra

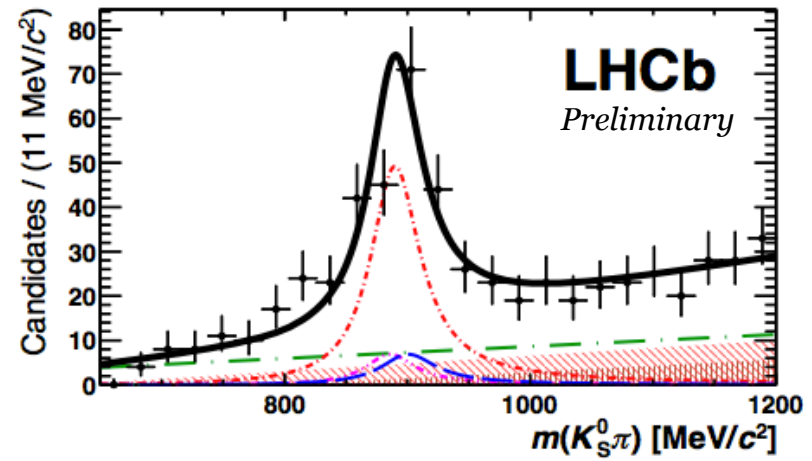
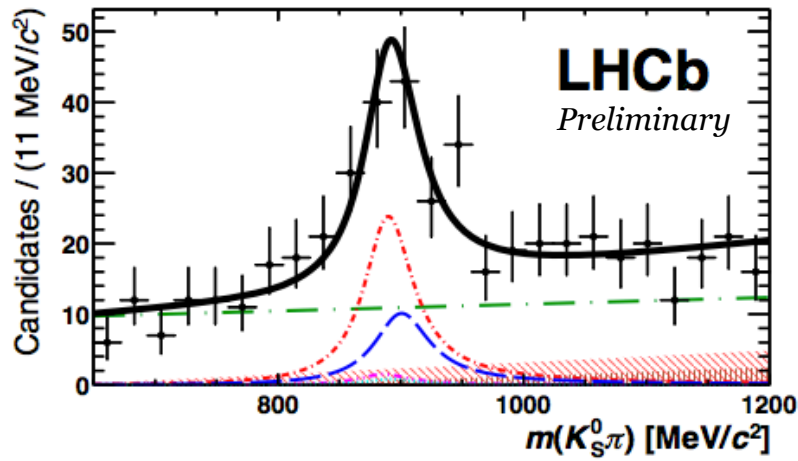
NEW

Long Category

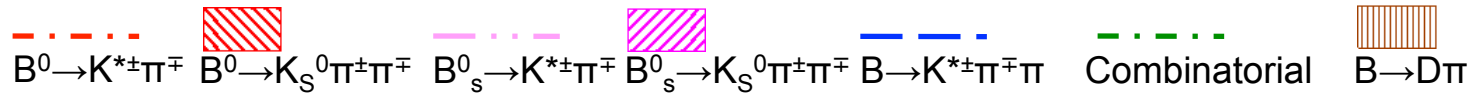
Downstream Category



B Candidates



$K^*$  Candidates



# Branching Fractions of $B_{(s)}^0 \rightarrow K^{*\pm} h^\mp$

- The previous results translate into the measurement of the decay modes  $B_s^0 \rightarrow K^{*\pm} K^\mp$  with  $12.5\sigma$  and  $B_s^0 \rightarrow K^{*-} \pi^+$  with  $3.9\sigma$  significance.
  - The observed signal significance for the decay  $B^0 \rightarrow K^{*\pm} K^\mp$  is below  $2\sigma$ .
- With the obtained yields the corresponding branching fractions are determined.
- The reference channel is  $B^0 \rightarrow K^{*\pm} \pi^\mp$ .
  - $\mathcal{B}(B^0 \rightarrow K^{*+} \pi^-) = (8.5 \pm 0.7) \times 10^{-6}$  [HFAG arXiv:1207.1158]
- And the results:

$$\mathcal{B}(B_s^0 \rightarrow K^{*\pm} K^\mp) = (12.7 \pm 1.9 \text{ (stat)} \pm 1.9 \text{ (syst)}) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow K^{*\pm} K^\mp) = (0.17 \pm 0.15 \text{ (stat)} \pm 0.05 \text{ (syst)}) \times 10^{-6}$$

$$< 0.4 \text{ (0.5)} \times 10^{-6} \text{ at } 90\% \text{ (95\%)} \text{ CL}$$

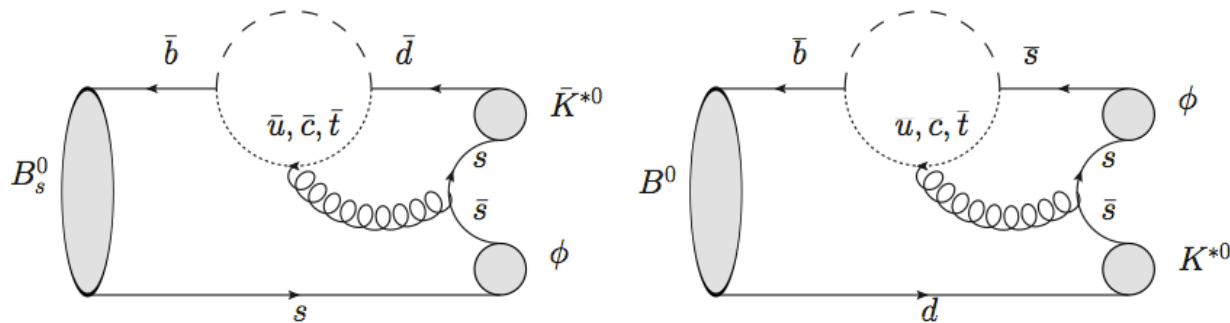
$$\mathcal{B}(B_s^0 \rightarrow K^{*-} \pi^+) = (3.3 \pm 1.1 \text{ (stat)} \pm 0.5 \text{ (syst)}) \times 10^{-6}$$

# B → V<sub>1</sub>V<sub>2</sub> Penguins

- Dominated by penguin diagrams. No tree level contribution:

$$B_s^0 \rightarrow K^{*0} \bar{K}^{*0} \quad B_s^0 \rightarrow \phi \phi \quad B^0 \rightarrow K^{*0} \bar{K}^{*0}$$

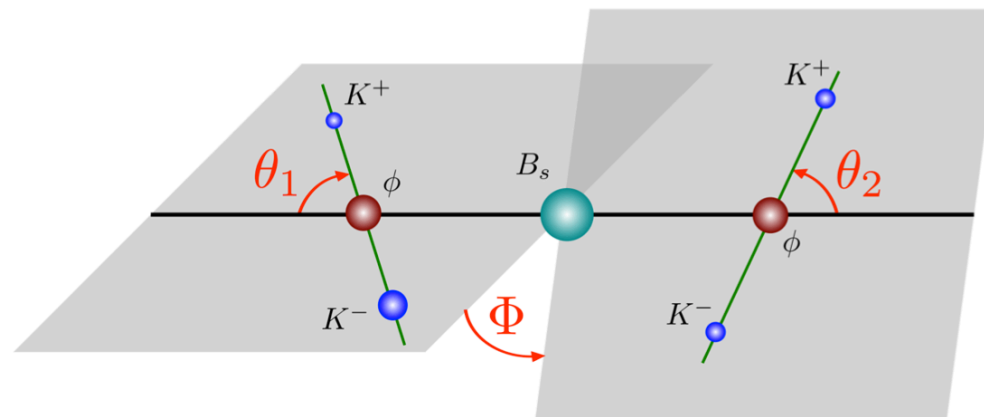
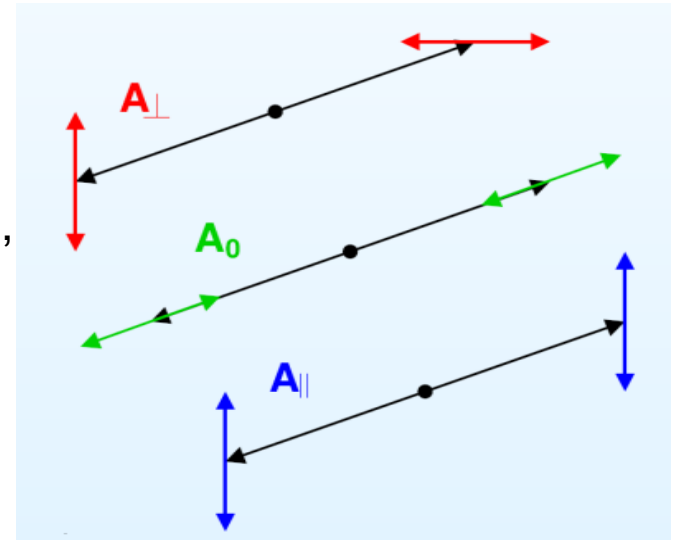
$$B_s^0 \rightarrow \phi \bar{K}^{*0} \quad B^0 \rightarrow \phi K^{*0}$$



- **Angular analysis of Vector mesons** in final state particularly interesting.
- Access to angular variables.
- Sensitive to direct CPV.

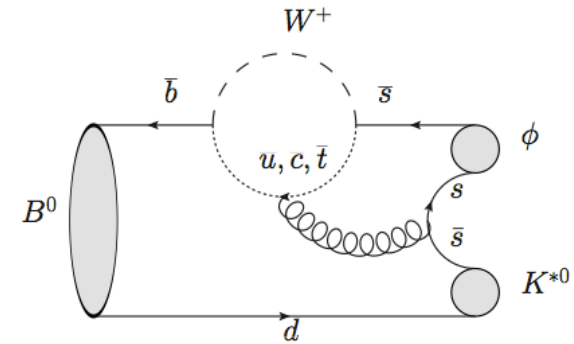
# Angular Analysis of $B \rightarrow V_1 V_2$

- $V_1$  and  $V_2$  can have angular momentum  $L = 0, 1, 2$ .
- High longitudinal polarization naïvely expected:
  - V-A structure of weak interaction.
  - Helicity conservation in strong interaction.
- Accounting for additional effects, such as rescattering, produces smaller polarizations.
- Angular pdf depends on:
  - Polarization fractions:  $|A_0|^2$ ,  $|A_{||}|^2$ ,  $|A_{\perp}|^2$
  - Strong phases:  $\delta_{||}$ ,  $\delta_{\perp}$
  - If the final state is common to  $B_s^0$  and  $\bar{B}_s^0$ :
    - CP-violating phase:  $\phi_s$  in time dependent analysis.



# $B^0 \rightarrow \phi K^{*0}$

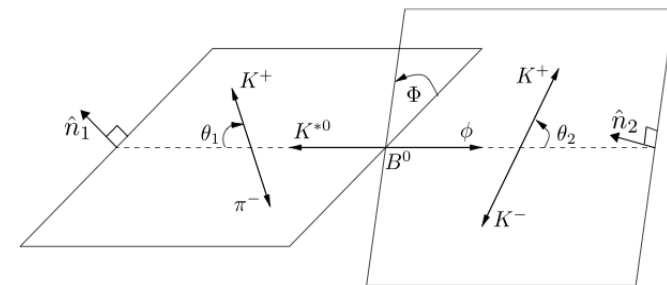
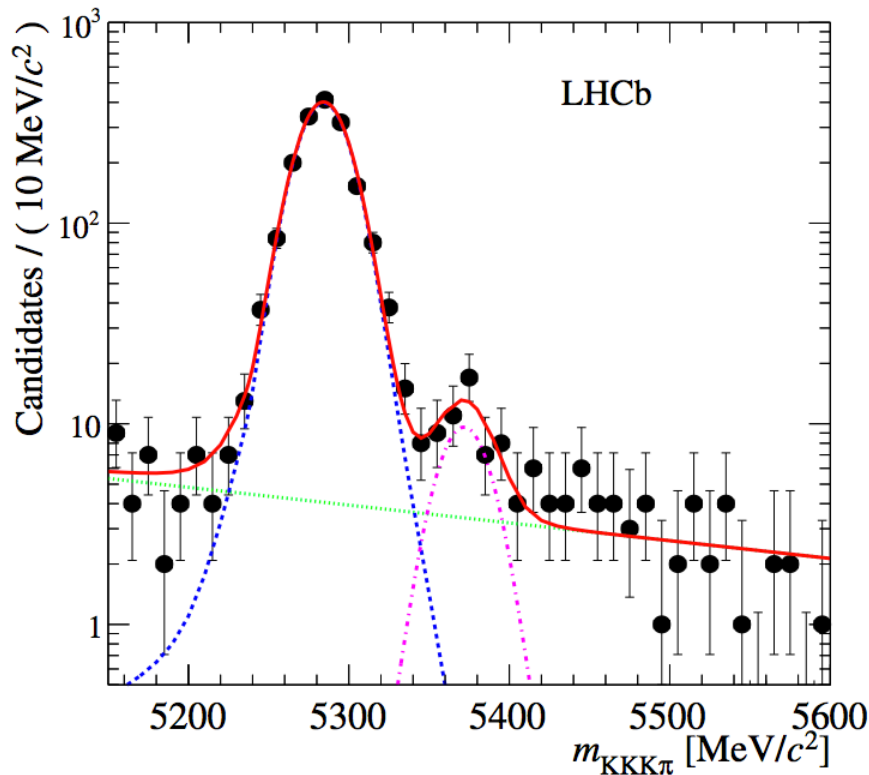
- $b \rightarrow s\bar{s}s$  FCNC penguin in the SM.
- Sensitive to NP contributions in the loop.
- $K^+K^-K^+\pi^-$  final state.
- Self tagged mode.
- $1655 \pm 42$  signal candidates with 2011 data.



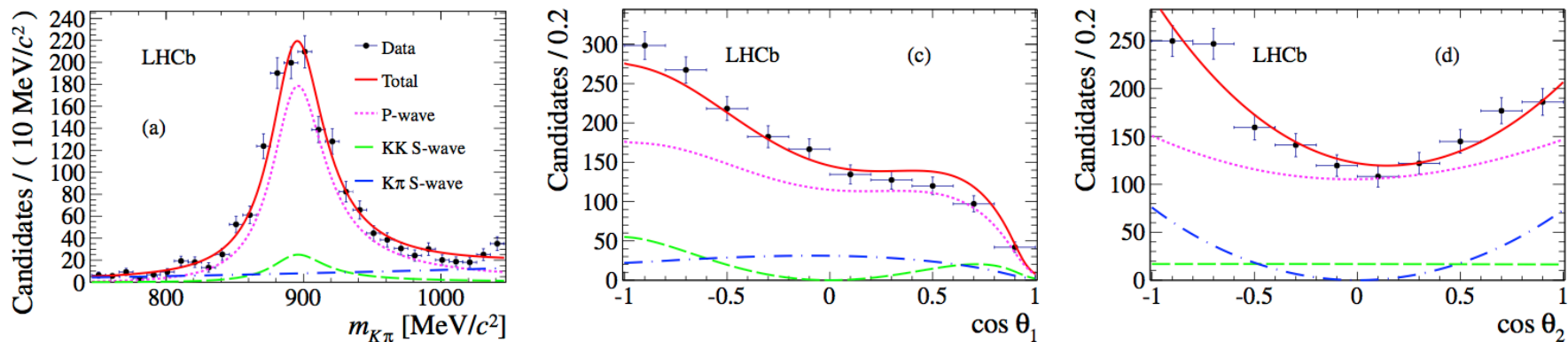
## Selection

- Same relevant selection variables as for  $B_{(s)}^0 \rightarrow K^{*\pm} h^\mp$
- Two steps:
  - Loose rectangular cuts.
  - Powerful Multivariate method combined with Particle ID cuts.
- 5-dimensional unbinned maximum likelihood fit.
  - $M_{KK}, M_{K\pi}, \cos\theta_1, \cos\theta_2, \Phi$

$$d^5\Gamma = \frac{9}{8\pi} \sum_{i=1}^{15} h_i f_i(\theta_1, \theta_2, \Phi) \mathcal{M}_i(m_{K\pi}, m_{KK}) d\Omega(KK\pi)$$



# Polarization of $B^0 \rightarrow \phi K^{*0}$



Intermediate longitudinal polarisation.  
 CP asymmetries compatible with zero.

Parameter	LHCb	BaBar	Belle
$f_L$	$0.497 \pm 0.019 \pm 0.015$	$0.494 \pm 0.034 \pm 0.013$	$0.499 \pm 0.030 \pm 0.018$
$f_{\perp}$	$0.221 \pm 0.016 \pm 0.013$	$0.212 \pm 0.032 \pm 0.013$	$0.238 \pm 0.026 \pm 0.008$
$\delta_{\perp}$	$2.633 \pm 0.062 \pm 0.037$	$2.35 \pm 0.13 \pm 0.09$	$2.37 \pm 0.10 \pm 0.04$
$\delta_{\parallel}$	$2.562 \pm 0.069 \pm 0.040$	$2.40 \pm 0.13 \pm 0.08$	$2.23 \pm 0.10 \pm 0.02$
$\mathcal{A}_0^{CP}$	$-0.003 \pm 0.038 \pm 0.005$	$+0.01 \pm 0.07 \pm 0.02$	$-0.030 \pm 0.061 \pm 0.007$
$\mathcal{A}_{\perp}^{CP}$	$+0.047 \pm 0.072 \pm 0.009$	$-0.04 \pm 0.15 \pm 0.06$	$-0.14 \pm 0.11 \pm 0.01$
$\delta_{\perp}^{CP}$	$+0.062 \pm 0.062 \pm 0.006$	$+0.21 \pm 0.13 \pm 0.08$	$+0.05 \pm 0.10 \pm 0.02$
$\delta_{\parallel}^{CP}$	$+0.045 \pm 0.068 \pm 0.015$	$+0.22 \pm 0.12 \pm 0.08$	$-0.02 \pm 0.10 \pm 0.01$

# Polarization Summary of $B \rightarrow V_1 V_2$

- Large Longitudinal polarization confirmed in  $b \rightarrow u$  tree dominated decays ( $f_L \sim 1$ ).
- Penguin decays show intermediate or small longitudinal polarization fractions.
  - Exception in  $B^0 \rightarrow K^{*0} \bar{K}^{*0}$ .
  - Polarization puzzle.



Decay Mode	$B^0 \rightarrow \rho^+ \rho^-$ BaBar arXiv0607098	$B^0 \rightarrow \rho^0 K^{*0}$ BaBar PRD 85 072005	$B^0 \rightarrow \phi \phi$ LHCb arXiv 1407.2222	$B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$ LHCb PLB709 50	$B^0 \rightarrow K^{*0} \bar{K}^{*0}$ BaBar PRL 100 081801	$B^0 \rightarrow \phi K^{*0}$ LHCb JHEP 1405 069	$B_s^0 \rightarrow \phi \bar{K}^{*0}$ LHCb JHEP 1311 092
$f_L$	0.977 $\pm 0.028$	0.40 $\pm 0.14$	<b>0.364 <math>\pm</math> 0.015</b>	0.31 $\pm$ 0.13	0.80 $\pm$ 0.13	<b>0.497 <math>\pm</math> 0.024</b>	0.51 $\pm$ 0.16



# CP-asymmetries in $B^0 \rightarrow \phi K^{*0}$

Difference in direct CP asymmetries between  $B^0 \rightarrow \phi K^{*0}$  and  $B^0 \rightarrow J/\psi K^{*0}$  decays found to be

$$A_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow \phi \bar{K}^{*0}) - \Gamma(B^0 \rightarrow \phi K^{*0})}{\Gamma(\bar{B}^0 \rightarrow \phi \bar{K}^{*0}) + \Gamma(B^0 \rightarrow \phi K^{*0})}$$

$$\Delta A_{CP} = (+1.5 \pm 3.2 \pm 0.5) \%$$

$$\Delta A_{CP} = A_{CP}(\phi K^{*0}) - A_{CP}(J/\psi K^{*0})$$

- Triple-product asymmetries.
- Non-zero triple-product asymmetries imply a T-violating phase or a CP-conserving phase and final-state interactions.
  - With CPT symmetry a T-violating phase implies CP violation.

$$\sin \Phi = (\hat{n}_{V_1} \times \hat{n}_{V_2}) \cdot \hat{p}_{V_1}$$

$$\sin 2\Phi = 2(\hat{n}_{V_1} \cdot \hat{n}_{V_2})(\hat{n}_{V_1} \times \hat{n}_{V_2}) \cdot \hat{p}_{V_1}$$

$$A_U = \frac{\Gamma(\sin 2\Phi > 0) - \Gamma(\sin 2\Phi < 0)}{\Gamma(\sin 2\Phi > 0) + \Gamma(\sin 2\Phi < 0)}$$

$$A_V = \frac{\Gamma(s \sin \Phi > 0) - \Gamma(s \sin \Phi < 0)}{\Gamma(s \sin \Phi > 0) + \Gamma(s \sin \Phi < 0)}$$

$$s = \text{sign}(\cos \theta_1 \cos \theta_2)$$

Asymmetry	Measured value
$A_U$	$-0.007 \pm 0.012 \pm 0.002$
$A_V$	$+0.004 \pm 0.014 \pm 0.002$

- Two additional Triple-Products based on S-wave also compatible with zero.
- Large fake triple products, relying on flavour identification reveal large strong phases.



# $B_{(s)}^0 - \bar{B}_{(s)}^0$ mixing

Time development of the mixing described by

$$i \frac{d}{dt} \begin{pmatrix} B_{(s)}^0 \\ \bar{B}_{(s)}^0 \end{pmatrix} = \left( M - \frac{i}{2} \Gamma \right) \begin{pmatrix} B_{(s)}^0 \\ \bar{B}_{(s)}^0 \end{pmatrix}$$

$$M = \begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix}; \quad \Gamma = \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix}$$

Diagonalizing in terms of mass eigenstates

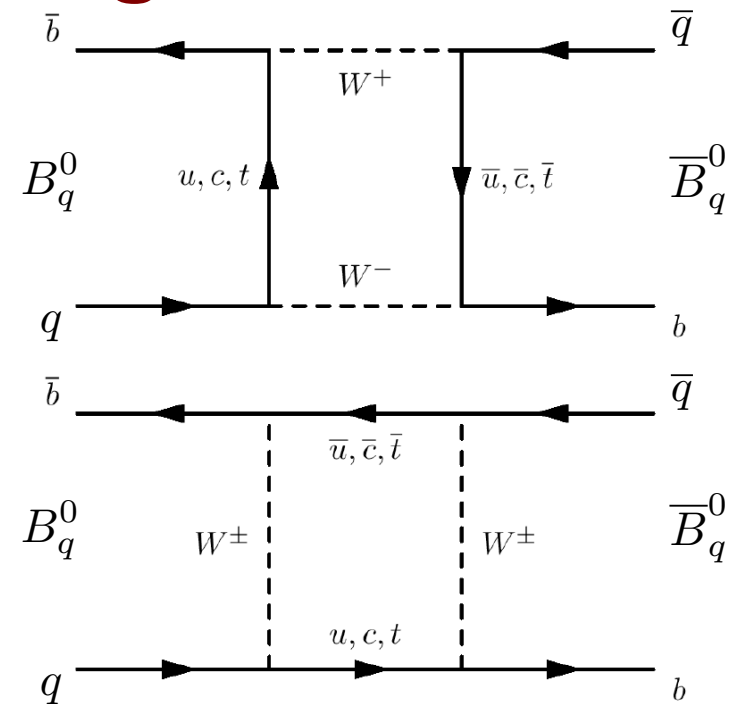
$$i \frac{d}{dt} B_L = (m_L - \frac{i}{2} \Gamma_L) B_L$$

$$i \frac{d}{dt} B_H = (m_H - \frac{i}{2} \Gamma_H) B_H$$

Mass eigenstates  $\neq$  flavour eigenstates

$$|B_L\rangle = p |B_{(s)}^0\rangle + q |\bar{B}_{(s)}^0\rangle$$

$$|B_H\rangle = p |B_{(s)}^0\rangle - q |\bar{B}_{(s)}^0\rangle$$

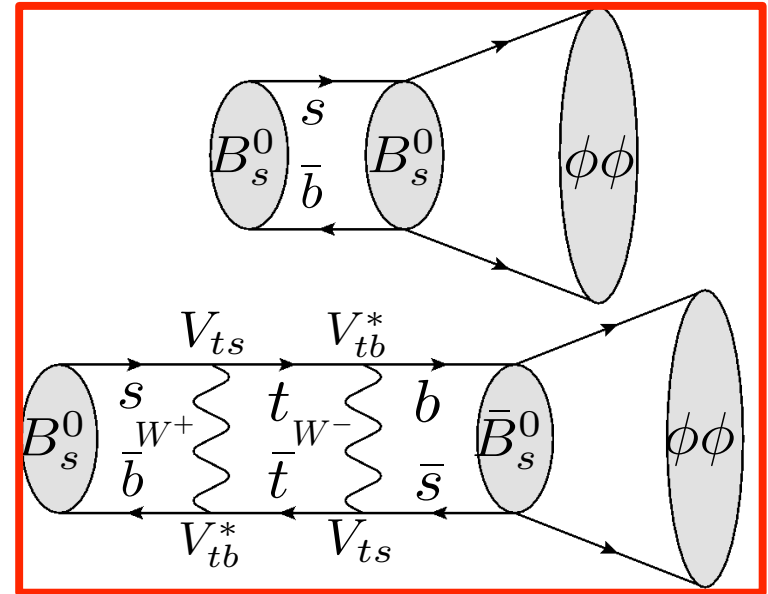
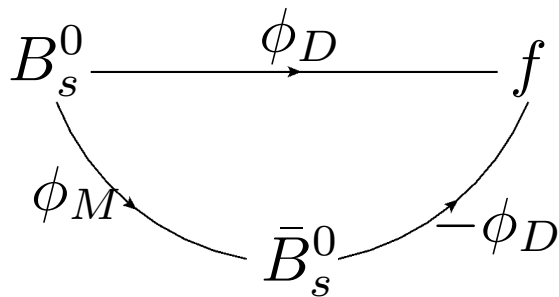


## Mixing Parameters

- Mass difference:  $\Delta m = m_H - m_L$
- Lifetime difference:  $\Delta \Gamma = \Gamma_H - \Gamma_L$
- Mixing phase:  $\phi_M = \arg(-M_{12}/\Gamma_{12})$

# $B_s^0 \rightarrow \phi\phi$ time dependent analysis

- Interference between:
  - Decay.
  - Decay after mixing.



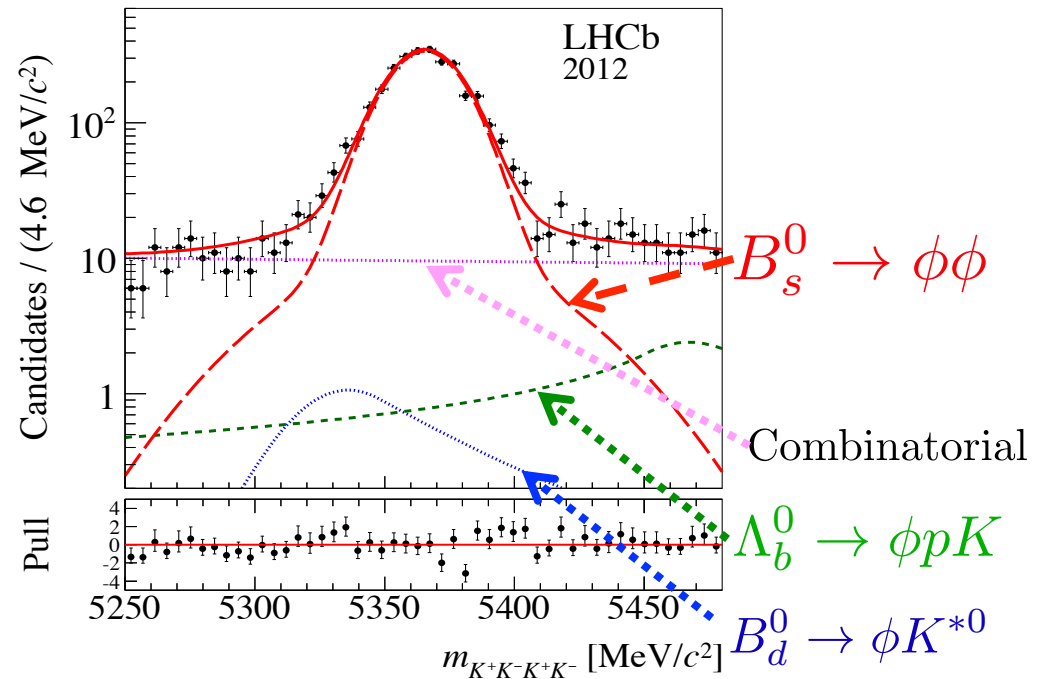
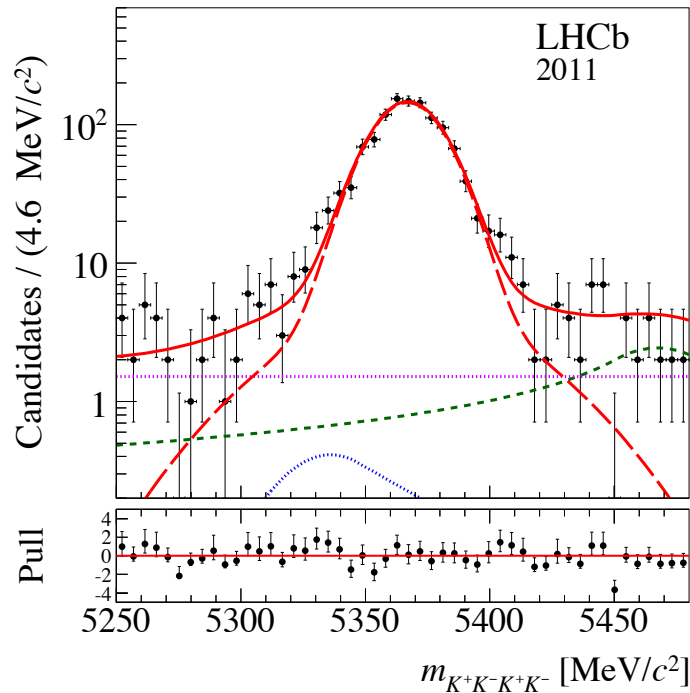
- Observable phase  $\phi_s = -2\beta_s = \Phi_M - 2\Phi_D$
- Standard Model prediction for  $B_s^0 \rightarrow \phi\phi$ .
  - Cancellation between decay + mixing phases:
  - $\phi_s = 0.01 \pm 0.02$  [arXiv:0810.0249]

• Direct CP violation also possible

$$|\lambda| = \left| \frac{q}{p} \cdot \frac{\bar{A}}{A} \right| \quad |\lambda| \neq 1$$

Direct CP

# $B_s^0 \rightarrow \phi\phi$ sample

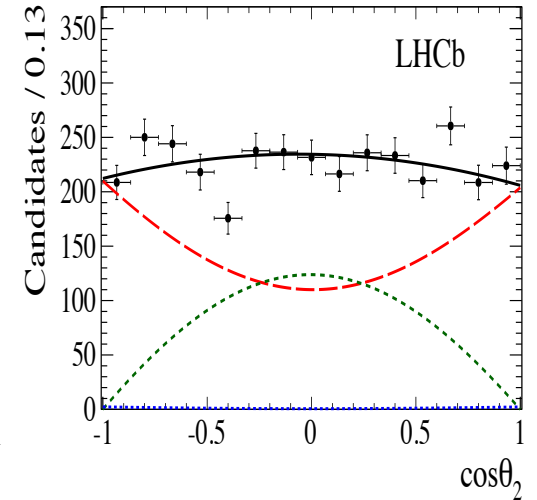
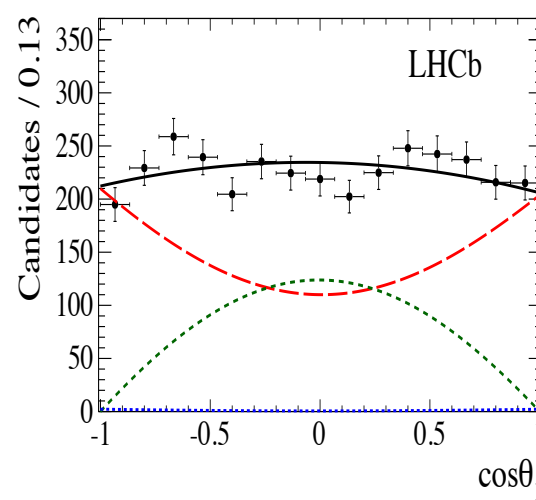
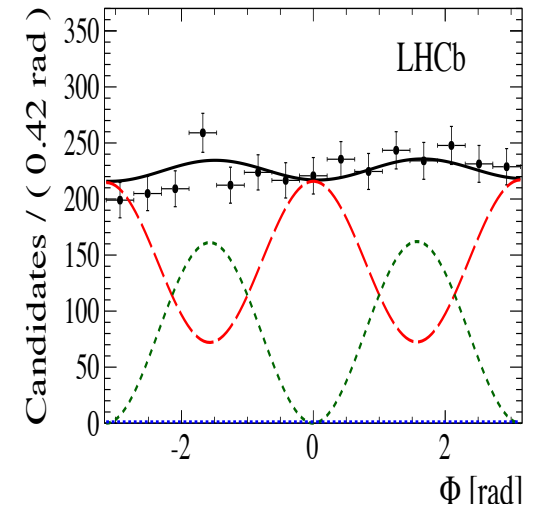
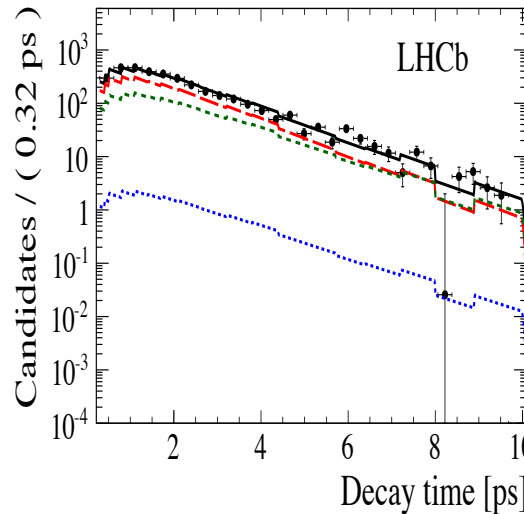
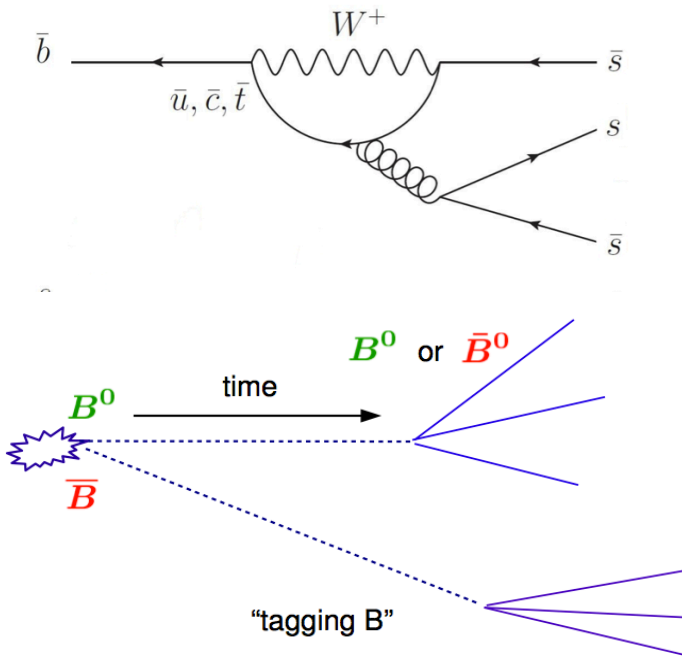


- Full 2011+2012 dataset.
- Re-optimized multivariate selection.
- **3950 signal candidates**
- 4.5 times as many events as in the analysis in [[PRL 110, 241802](#)]

- Unbinned max. likelihood fit.
- 4-dimension: 3 angles + time dependent tagged analysis:
  - $\Gamma_s$  and  $\Delta\Gamma_s$  from  $B_s^0 \rightarrow J/\psi K^+ K^-$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  [LHCb PRD 87 112010](#)
  - $\Delta m_s$  from  $B_s^0 \rightarrow D_s^-(K^+ K^- \pi^-) \pi^+$ , [LHCb New J. Phys. 15 053021](#)
- Time resolution model from simulation. Calibrated on data:  $\sigma_t \sim 43$  fs
- Angular acceptance for signal from simulation
- Time acceptance from  $B_s \rightarrow D_s \pi$  data

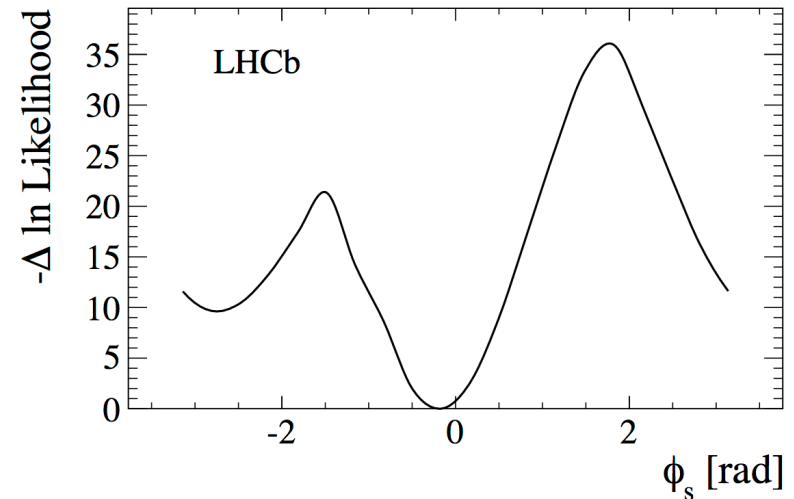
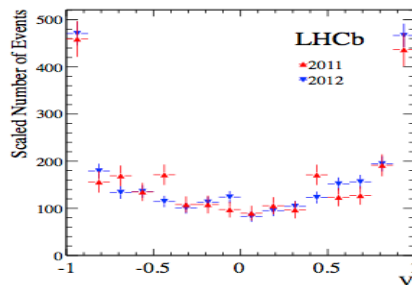
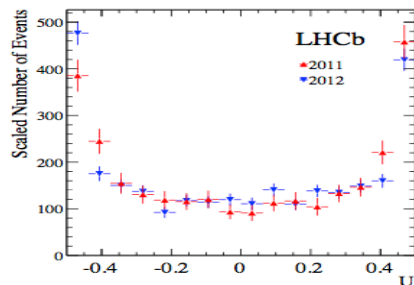


Total    CP-even    CP-odd    S-wave



# $B_s^0 \rightarrow \phi\phi$ results

- No large CP violation present.
  - In  $B_s^0$ - $B_s^0$  mixing.
  - In the  $b \rightarrow s\bar{s}s$  decay amplitude.
- Measured  $f_L$  in  $B_s^0 \rightarrow \phi\phi$  almost equal to  $B_s^0 \rightarrow K^{*0}K^{*0}$ .
  - Agreement with QCD factorization predictions.
  - Disfavours pQCD estimates.
- Triple-product asymmetries determined from separate time integrated fit.
  - $B_s^0$  flavorless decays: non-zero triple products indicate different CP-violating phases for CP-even (0,||) and CP-odd ( $\perp$ ) eigenstates.



## Time-dependent analysis

Parameter	Result
$\phi_s$	$-0.17 \pm 0.15 \pm 0.03$
$ \lambda $	$1.04 \pm 0.07 \pm 0.03$
$f_L$	$0.364 \pm 0.012 \pm 0.009$
$f_{\perp}$	$0.305 \pm 0.013 \pm 0.005$

## Time-integrated analysis

Parameter	Result
$A_U$	$-0.003 \pm 0.017 \pm 0.006$
$A_V$	$-0.017 \pm 0.017 \pm 0.006$

# Conclusions

## $B_{(s)}^0 \rightarrow K^{*\pm} h^\mp$

- Observation of the mode  $B_s^0 \rightarrow K^{*\pm} K^\mp$  with  $12.5\sigma$  significance
- Evidence of the  $B_s^0 \rightarrow K^{*\mp} \pi^\pm$  mode with  $3.9\sigma$  significance.
- Branching Fraction measurements:

$$\begin{aligned}\mathcal{B}(B_s^0 \rightarrow K^{*\pm} K^\mp) &= (12.7 \pm 1.9 \text{ (stat)} \pm 1.9 \text{ (syst)}) \times 10^{-6} \\ \mathcal{B}(B_s^0 \rightarrow K^{*\mp} K^\mp) &= (0.17 \pm 0.15 \text{ (stat)} \pm 0.05 \text{ (syst)}) \times 10^{-6} \\ &< 0.4 \text{ (0.5)} \times 10^{-6} \text{ at 90\% (95\%) CL} \\ \mathcal{B}(B_s^0 \rightarrow K^{*-} \pi^+) &= (3.3 \pm 1.1 \text{ (stat)} \pm 0.5 \text{ (syst)}) \times 10^{-6}\end{aligned}$$

## $B^0 \rightarrow \phi K^{*0}$

- Determination of CP-violation asymmetries
  - $\Delta A_{CP} = (+1.5 \pm 3.2 \pm 0.5)\%$
  - $A_U = -0.007 \pm 0.012 \pm 0.002$ ,  $A_V = +0.004 \pm 0.014 \pm 0.002$ .
- Measurement of angular parameters
  - $f_L = 0.497 \pm 0.019 \pm 0.015$

## $B_s^0 \rightarrow \phi\phi$

- Time-angular analysis.
  - Extraction of  $\phi_s = -0.17 \pm 0.015 \pm 0.03$  and  $|\lambda| = 1.04 \pm 0.07 \pm 0.03$ .
  - $f_L = 0.364 \pm 0.012 \pm 0.009$
- Time-integrated analysis.
  - $A_U = -0.003 \pm 0.017 \pm 0.006$ ,  $A_V = -0.017 \pm 0.017 \pm 0.006$ .

Everything seems to be consistent with the small CP-violation of the SM

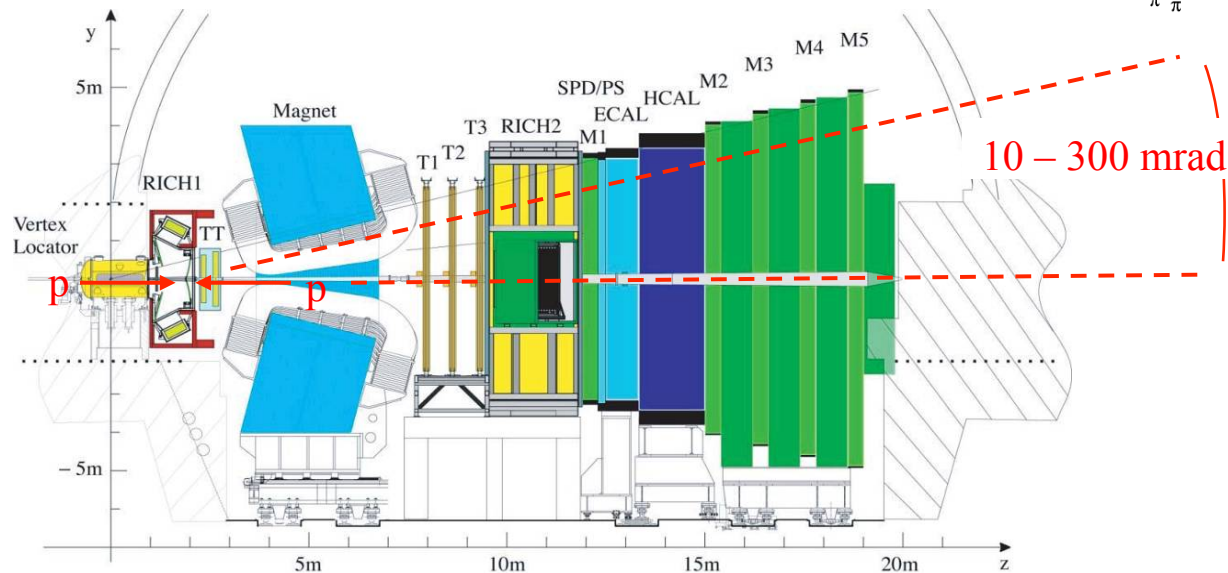
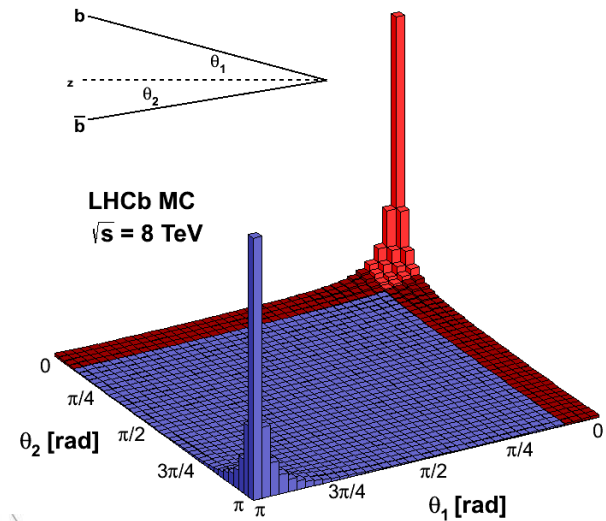
# Thank You

# Backup Slides



- Low angle production → LHCb spectrometer design:
  - forward (operating in collider mode).
- LHC bb x-section =  $284 \pm 53 \mu\text{b}$  (pp at  $\sqrt{s} = 7 \text{ TeV}$ ). [PLB 694 209]
  - ~ 100,000  $b\bar{b}$  pairs produced/second ( $10^4 \times$  B factories)
  - Charm production factor 20 higher! [CONF-2010-013]
- Main features:
  - Decay time resolution.
  - Particle ID.
  - Trigger on hadronic channels.
- Accumulated data 2010:  $37 \text{ pb}^{-1}$ . 2011:  $1.1 \text{ fb}^{-1}$ . 2012:  $2.2 \text{ fb}^{-1}$ .

# LHCb



# Angular Analysis of $B \rightarrow V_1 V_2$

- Final state: identical to decays with intermediate scalar resonances,  $B \rightarrow SV$ ,  $B \rightarrow VS$  or  $B \rightarrow SS$  (S-wave):

$$A(B \rightarrow VV) = \dots + \frac{A_{SV}}{\sqrt{3}} (\cos \theta_1 + \cos \theta_2) + \frac{A_{SS}}{3}$$

- Decay rate:

–  $f_i$ : angular functions.

–  $K_i$ : time dependent terms.

–  $a_i, b_i, c_i, d_i$  coefficients.

$$\frac{d\Gamma}{\Gamma d\Omega dt} = \sum_i K_i(t) f_i(\Omega)$$

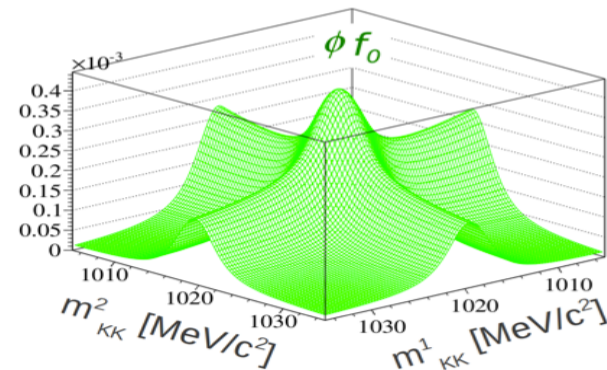
$$K_i(t) = N_i e^{-\Gamma_s t} \left[ \pm c_i \cos(\Delta m_s t) \pm d_i \sin(\Delta m_s t) + a_i \cosh\left(\frac{1}{2} \Delta \Gamma_s t\right) + b_i \sinh\left(\frac{1}{2} \Delta \Gamma_s t\right) \right]$$

- Depend on:

– Polarization fractions:  $|A_0|^2, |A_{||}|^2, |A_{\perp}|^2$

– Strong phases:  $\delta_{||}, \delta_{\perp}$

– CP-violating phase:  $\phi_s$  (CP eigenstates)



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