



Considerations about twisted stack cable for HTS insert

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Outline

- Motivation
- Magnet design based on stack cable hypothesis
- Considerations about stack cable weaknesses
- Sensibility of field homogeneity on current distribution

Insert dipole objectives :

- Inner diameter : 40 mm
- Outer diameter : 100 mm
- Flux density B_0 : 5 T in 13-15 T background
- Field quality : $< 5 \cdot 10^{-4} B_0$ unit

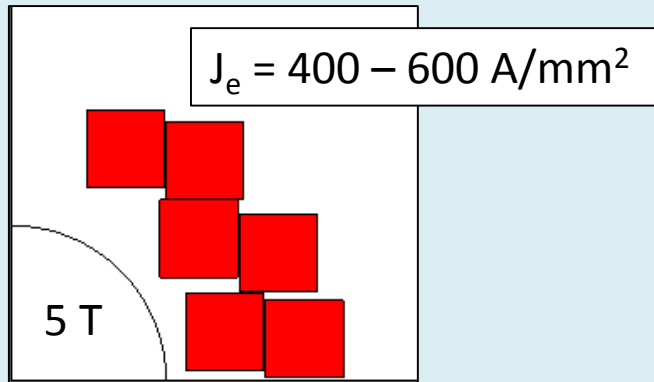
Insert dipole objectives :

- Inner diameter 40 mm
- Outer diameter 100 mm
- Flux density B_0 5 T in 13-15 T background
- Field quality $< 5 \cdot 10^{-4} B_0$ unit
- Current density J_e > 340 likely 400 – 600 A/mm² (20 T, 4,2K)
- Mechanical stress 100 MPa
- Operating current 5 – 10 kA

Magnet design optimization must lower operating current density
Need for compact cable

Stack cable interest :

Magnet design

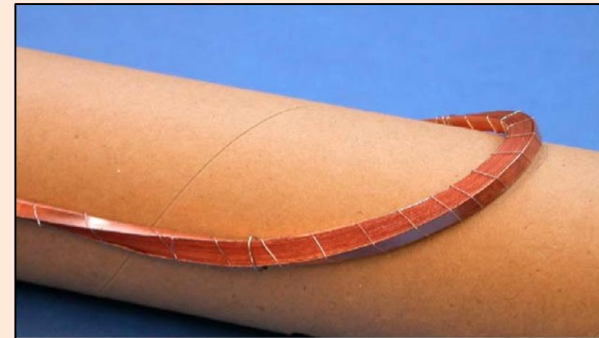


Square blocks : more room for coil topology optimization

Easy to upscale : large current

Tensile/compressive stress = as tape

Cable design



M.Takayasu (MIT), IEEE vol.23 No.3 2013

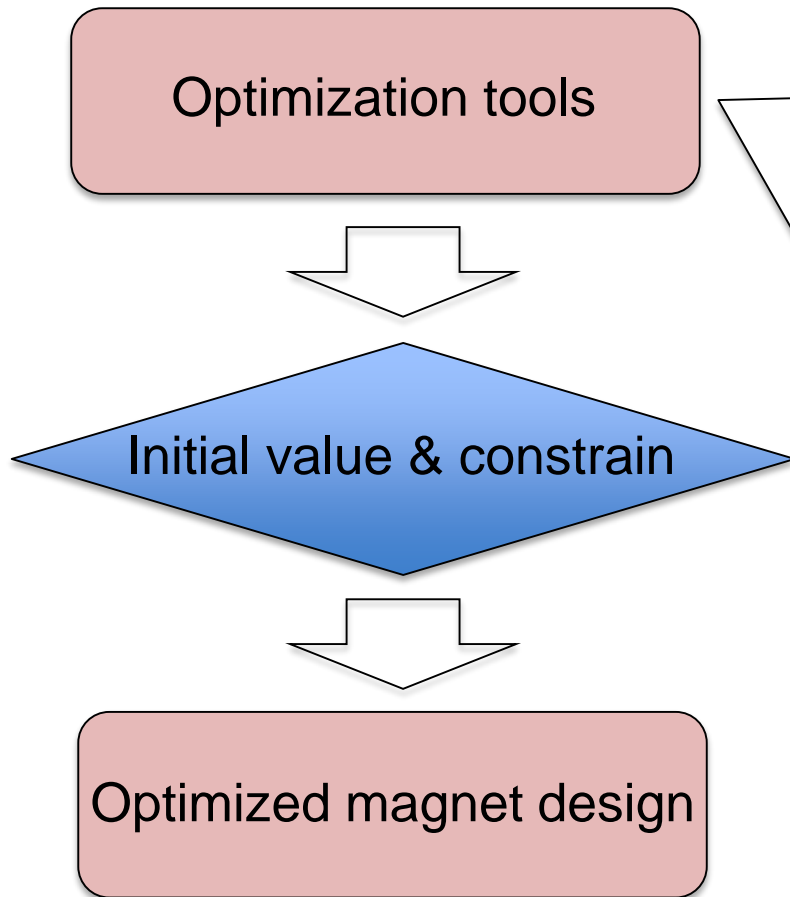
Easy to make, low cost

Good contact with thermal stabilizer and/or mechanical support

No lost space.

Weak points : bending and above all **transposition**

Magnet design : What can we get ?



Analytical model

Using 'fmincon' (Find Minimum of Constrained Nonlinear multivariable function)' of MATLAB optimization tools. It's much faster to gain results than numerical model.

Electromagnetic equation

Equation for block-coil

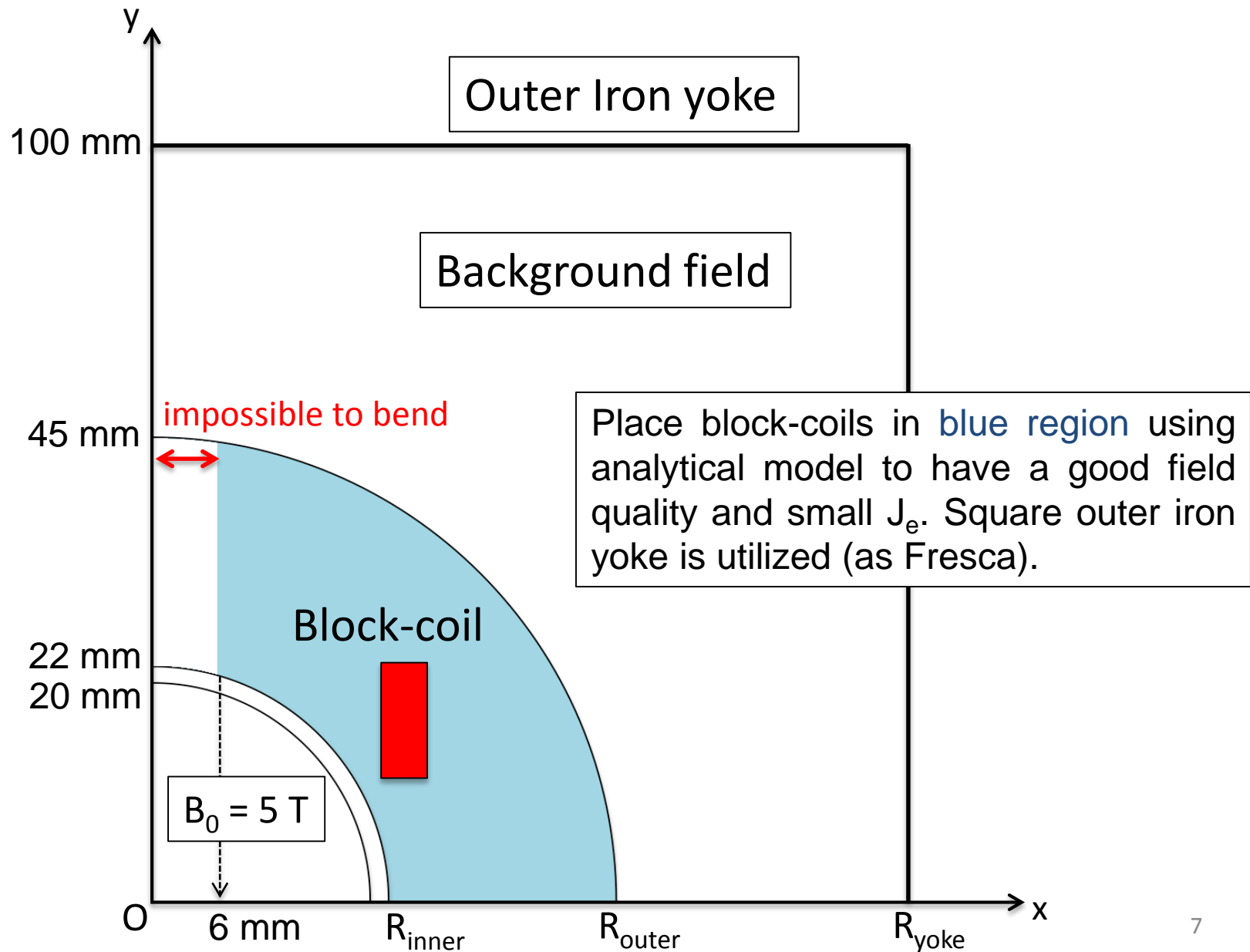
$$B_{y,bloc}(x, y) = \frac{\mu_0 J}{4\pi} \left[\left[(y - b) \ln R^2 + 2(x - a) \arctan \left(\frac{y - b}{x - a} \right) \right]_{a_1}^{a_2} \right]_{b_1}^{b_2}$$

same as CEA

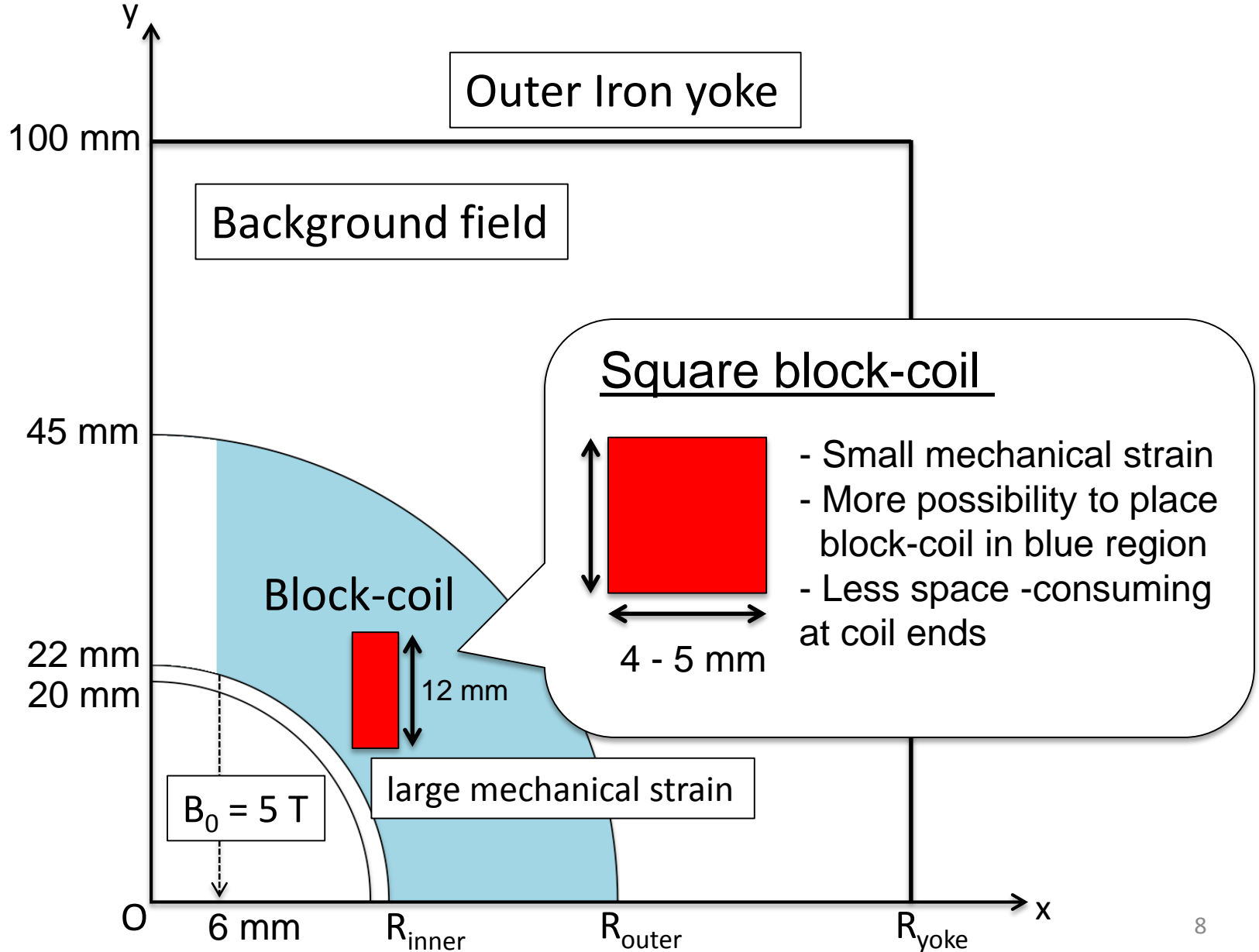
Equation for field quality

$$B_n = \frac{\mu_0 I}{2\pi r_c} \left(\frac{r_0}{r_c} \right)^{n-1} \cos(n\varphi_c)$$

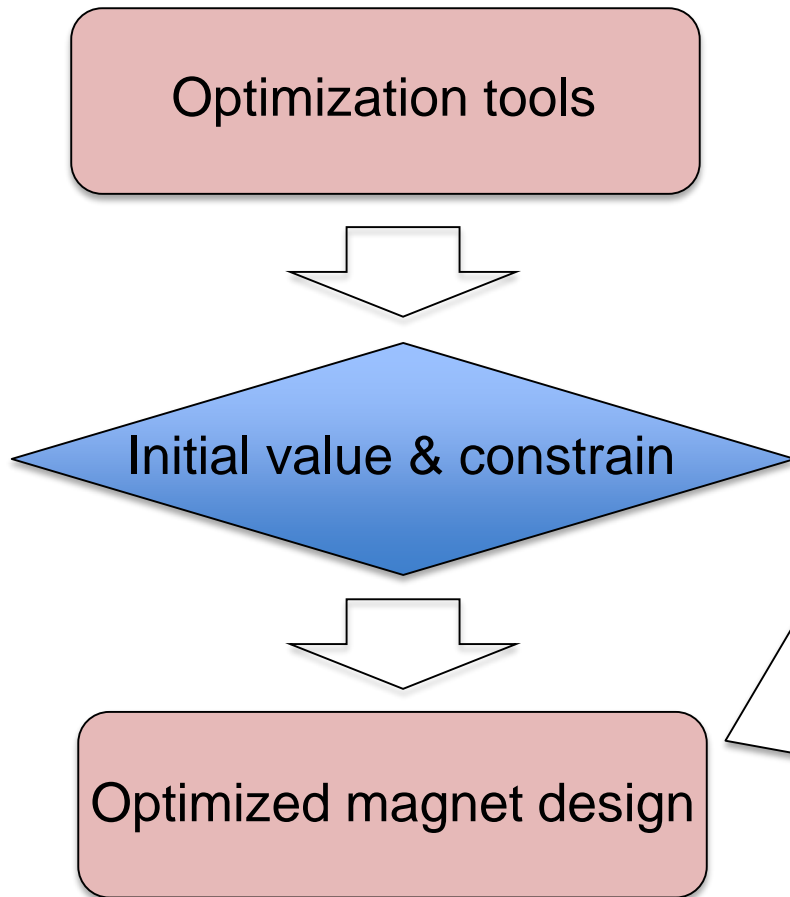
Initial value & constrain for magnet design



Block-coil design



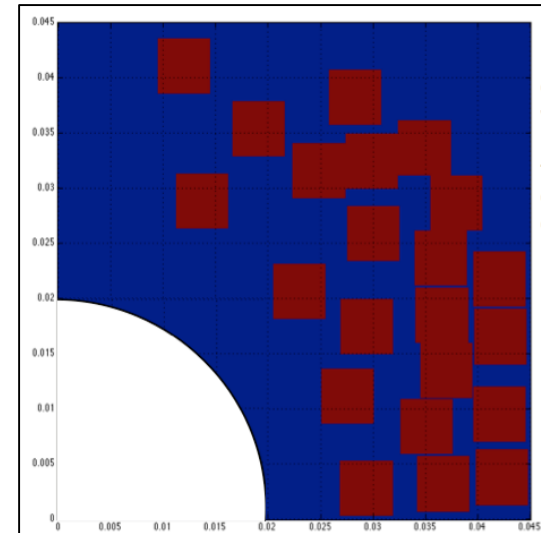
Optimization tools for magnet design



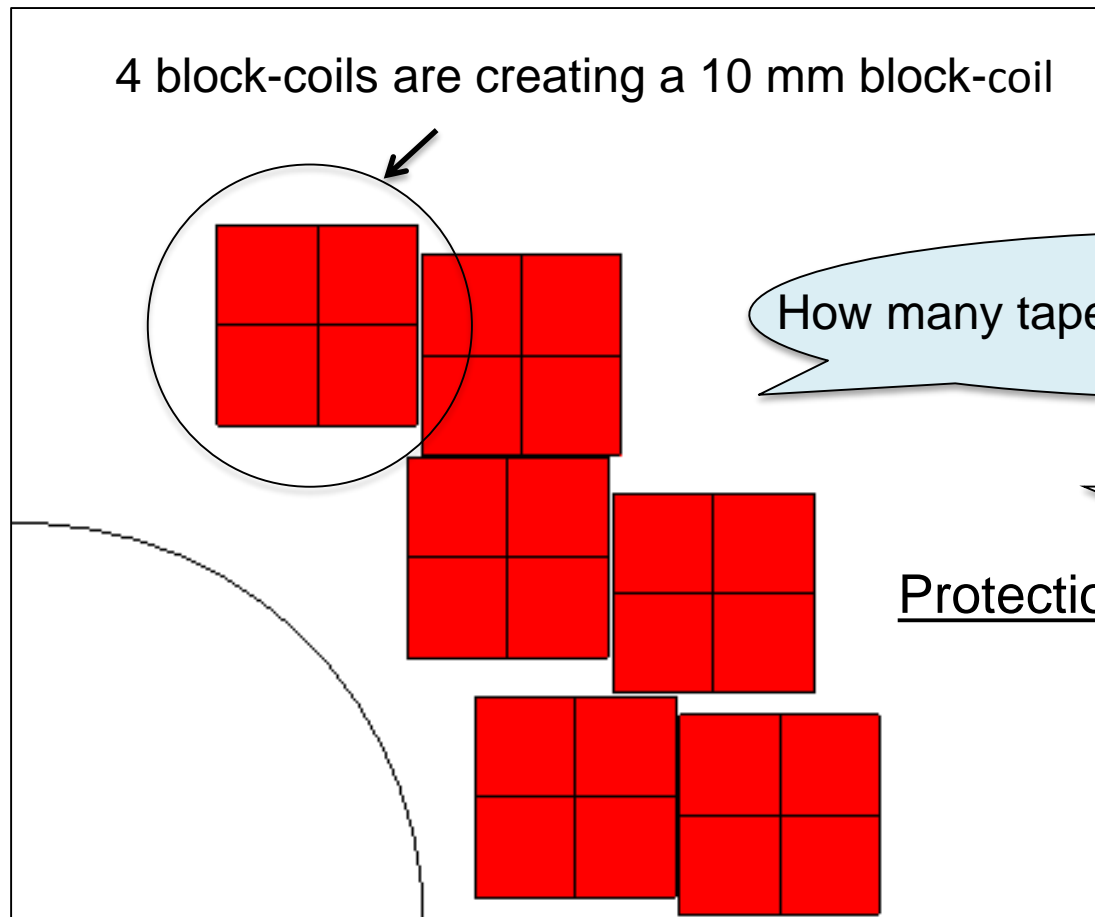
Objective

To obtain good field quality while having small current density J_e . We choose one of the best optimized magnet design that is feasible in terms of manufacturing.

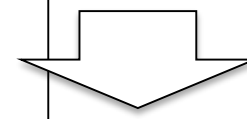
example



First optimized magnet design



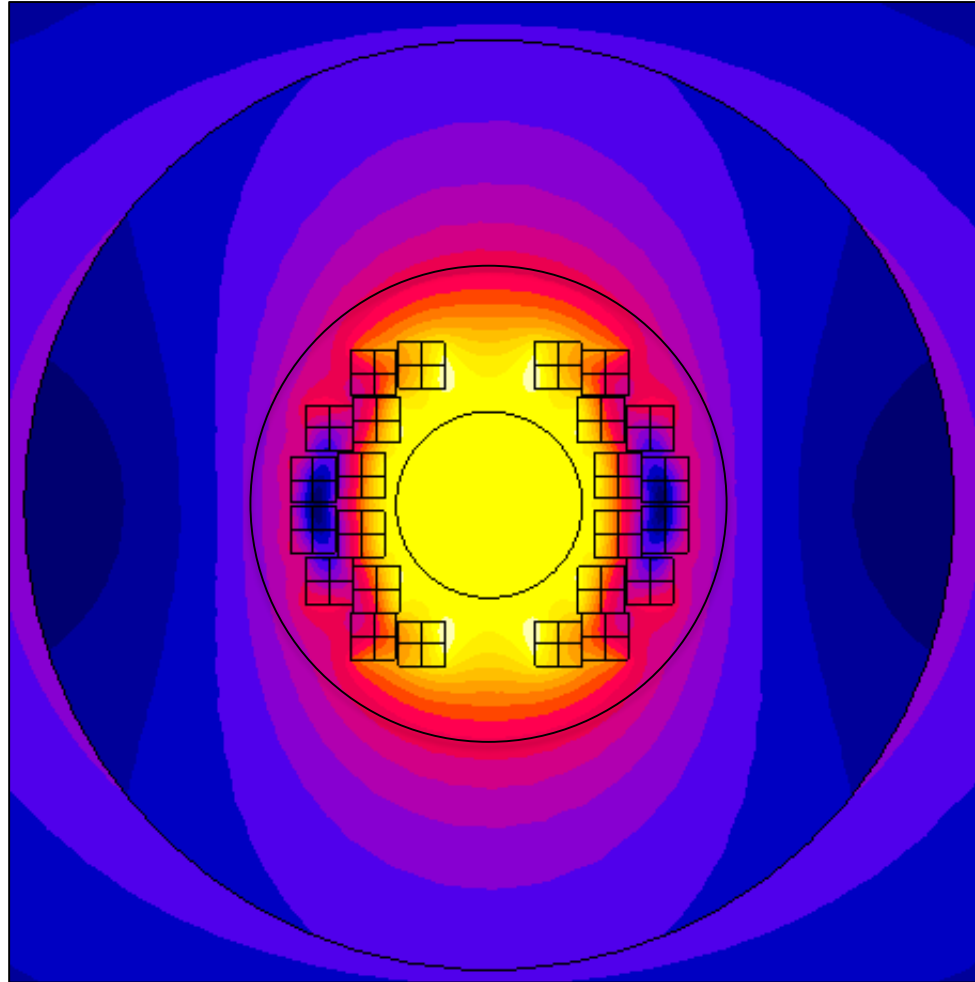
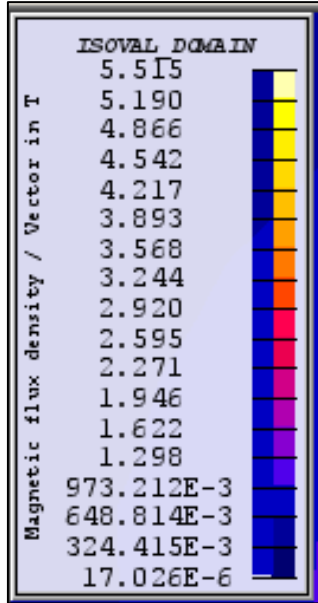
How many tape in parallel in a block-coil?



Protection & Detection scheme

$$1 \leq N_{\text{para}} \leq 30$$

First optimized magnet design



Block-coil design

Width, Thickness

5 mm

Conductor area

2400 mm²

Magnet design

Field quality

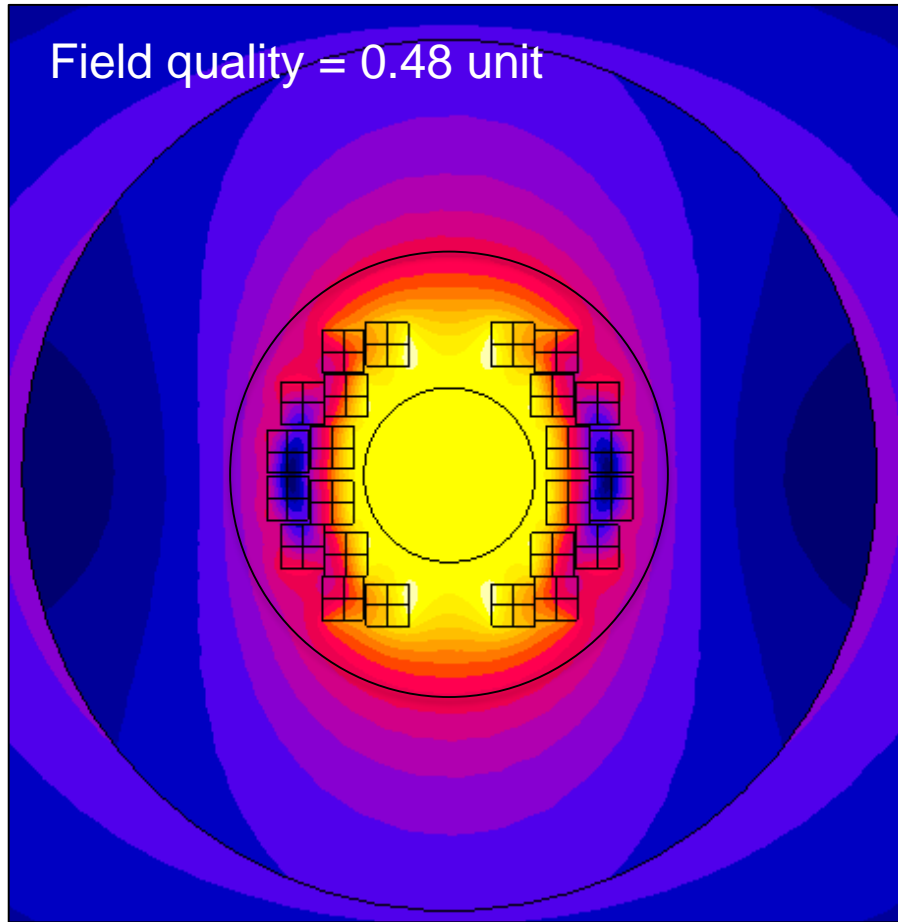
$0.48 \cdot 10^{-4} B_0$

Current density J_e

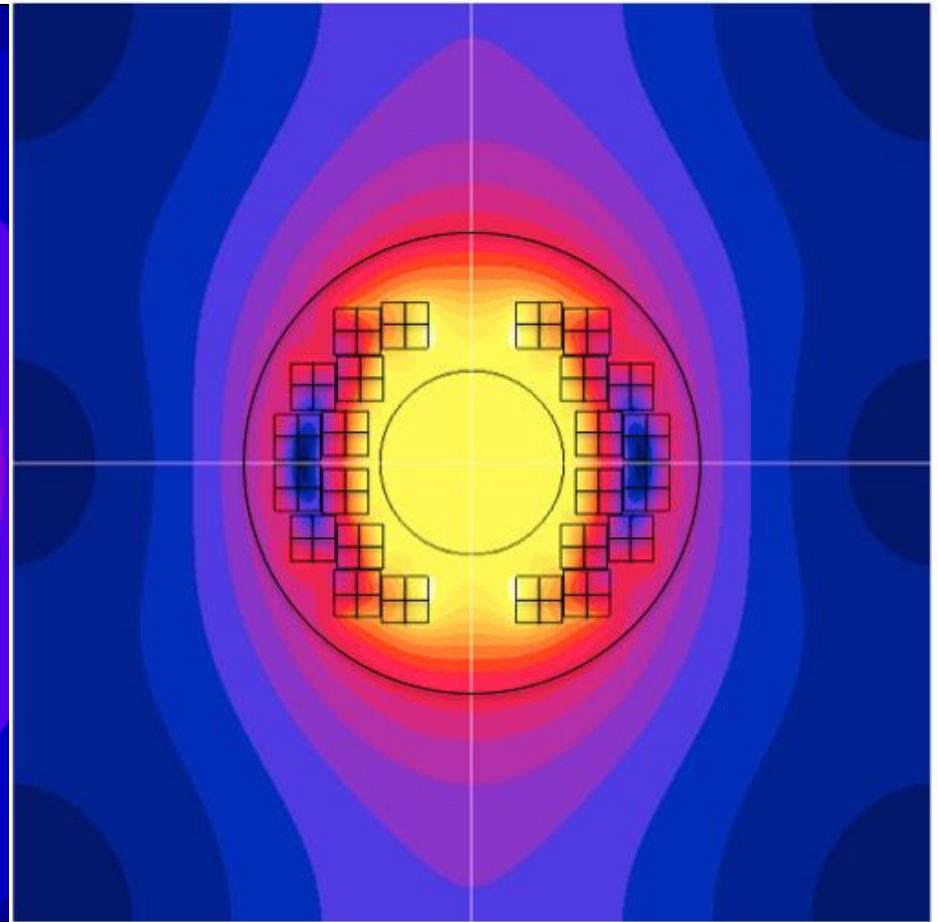
397 A/mm²

First optimized magnet design

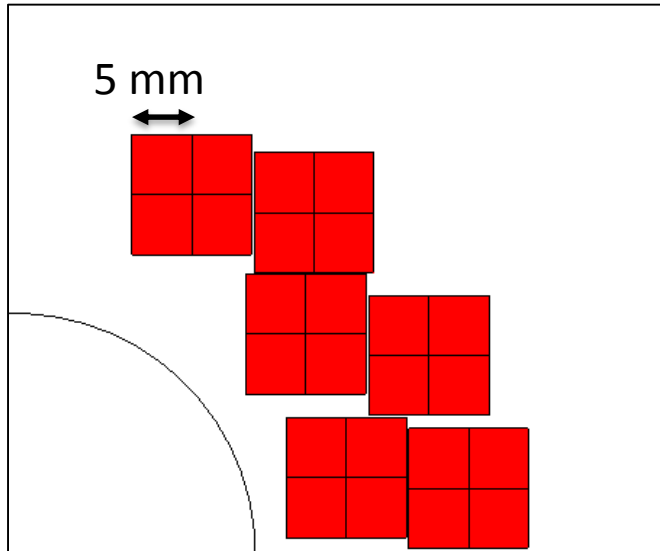
Round outer iron yoke



Rectangular outer iron yoke (Fresca II)



First optimized magnet design : comments



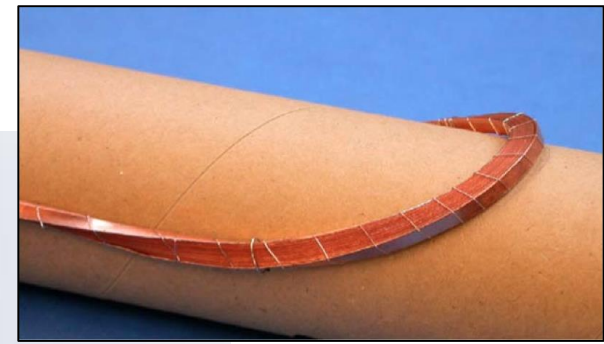
Current density $J_e = 400 \text{ A/mm}^2$

$I_{op} = 10 \text{ kA}$ from a $5 \times 5 \text{ mm}$ cable

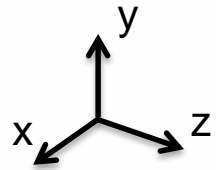
Is it necessary ? If not we can go to smaller cables : $3,5 \times 3,5 \Rightarrow 5 \text{ kA}$

- Significant decrease in J_e compared to designs with less blocks : room for manoeuvre (larger margins, more stabilizer, reinforcement)
- Blocks may be tilted to follow field lines
- How is bending going at the heads ? Better if the width is small
- Transposition is a problem : where do we twist and what does it change ?

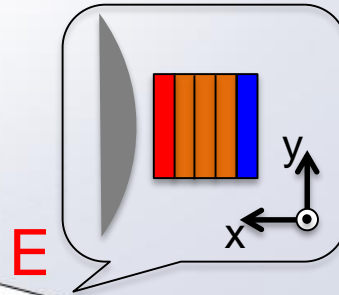
Stacked cable twisting



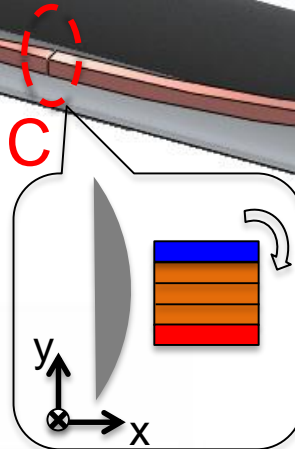
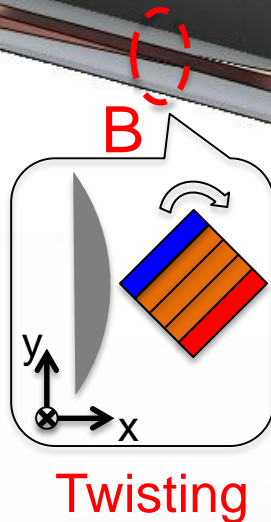
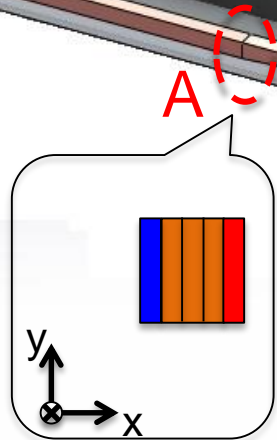
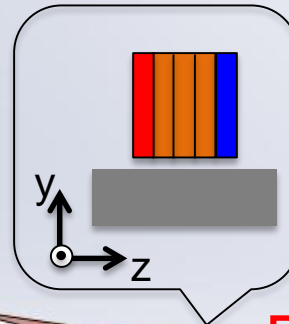
M.Takayasu (MIT), IEEE vol.23 No.3 2013



Stack tape has transposed



Easy bending



Field in c-axis

Small J_e

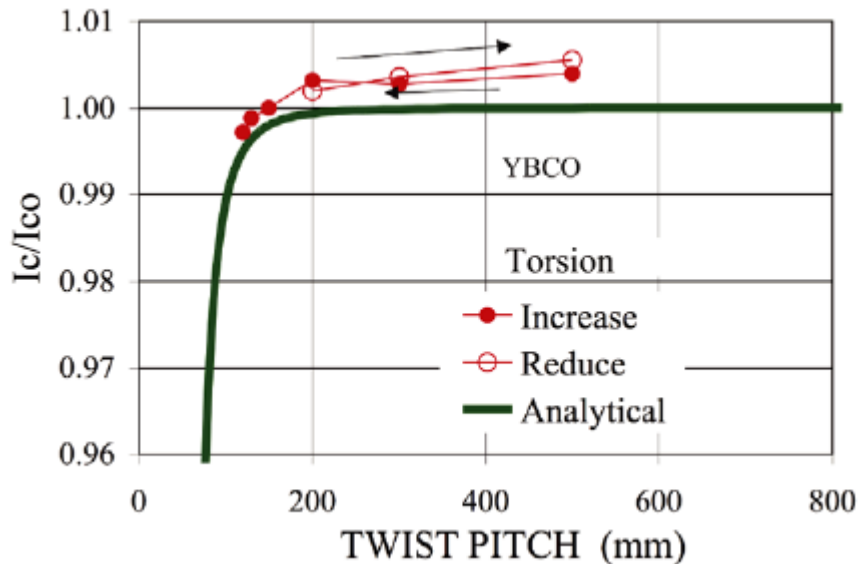
Twisted stack cable issues

- Twisting generate strain
- Part of the cable is fully in c-axis orientation
- Twist occurs one time per turn
- Twisting is not a full transposition

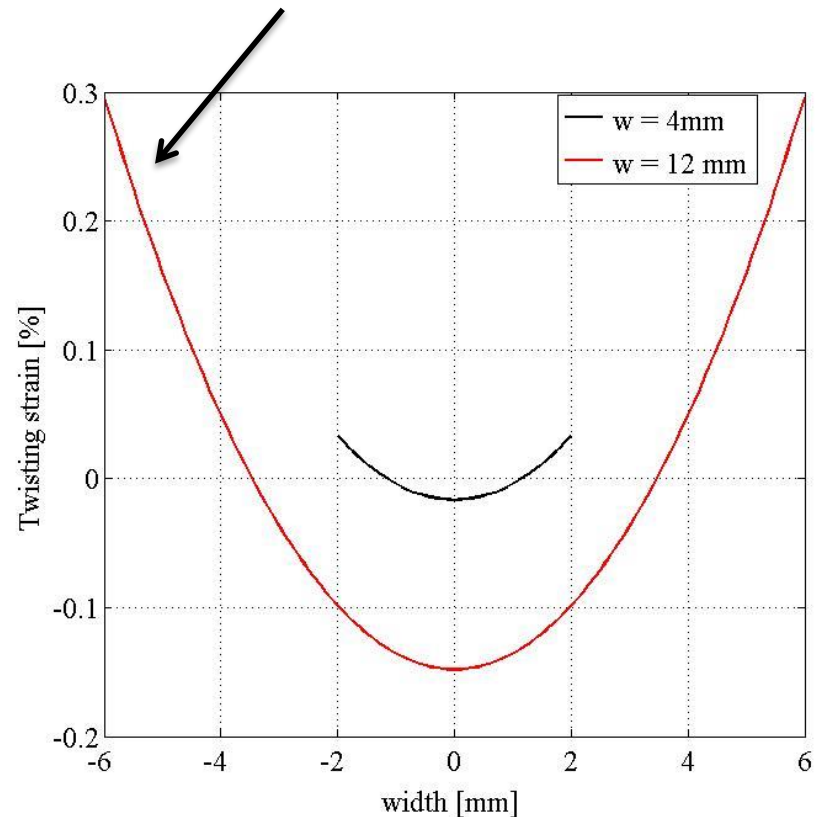
Twist stack cable issues

- Twisting generate strain

Mechanical strain is already large and reaching critical strain 0.33 %.



M Takayasu et al, Supercond. Sci. Technol. **25** (2012)



Twisting pitch = 100 mm, Twisting angle = 90°

It seems manageable
(small widths better)

Twist stack cable issues

- Part of the cable is fully in c-axis orientation

→ 3D study of coil ends is needed to evaluate the local field value (ongoing)

The combination of outsert and insert field can be optimized, The coil ends of each must not be at the same position. The possibility of an insert longer than the outsert will be studied

Finally, transverse field may be acceptable if J_e stays in the range of 400 A/mm^2

Twist stack cable issues

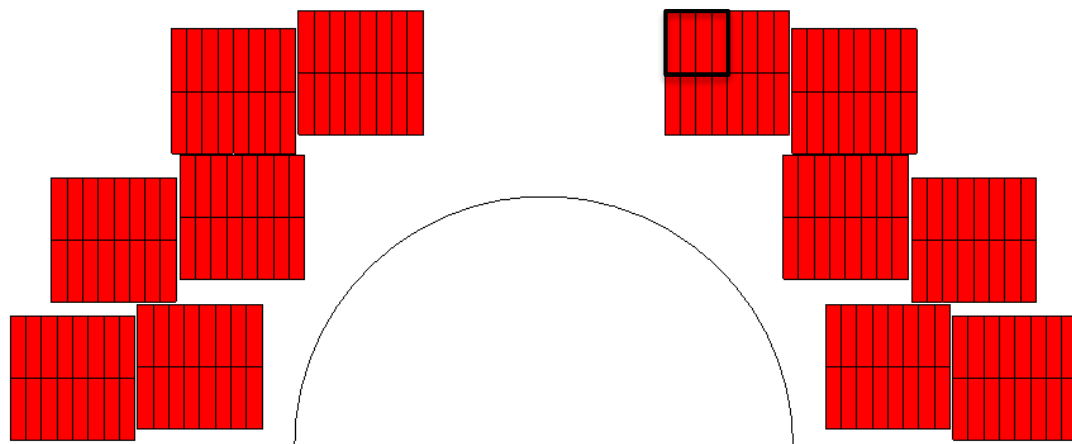
- Twist occurs only one time per turn
- Twisting is not a full transposition

The current distribution in the cable must be studied, with its impact on field homogeneity and losses.

AC losses in CC are largely studied for power applications, and some design tools are available. Behavior in slowly varying high field are well none in principle, but practically evaluating the effects is a challenge.

Especially, experiments are needed to validate the modelling

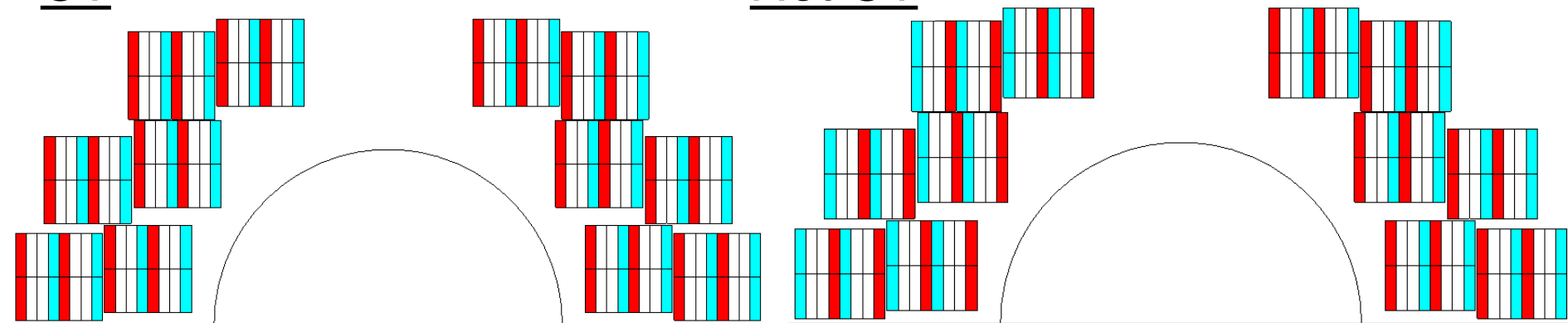
Current transposition effect : First evaluation



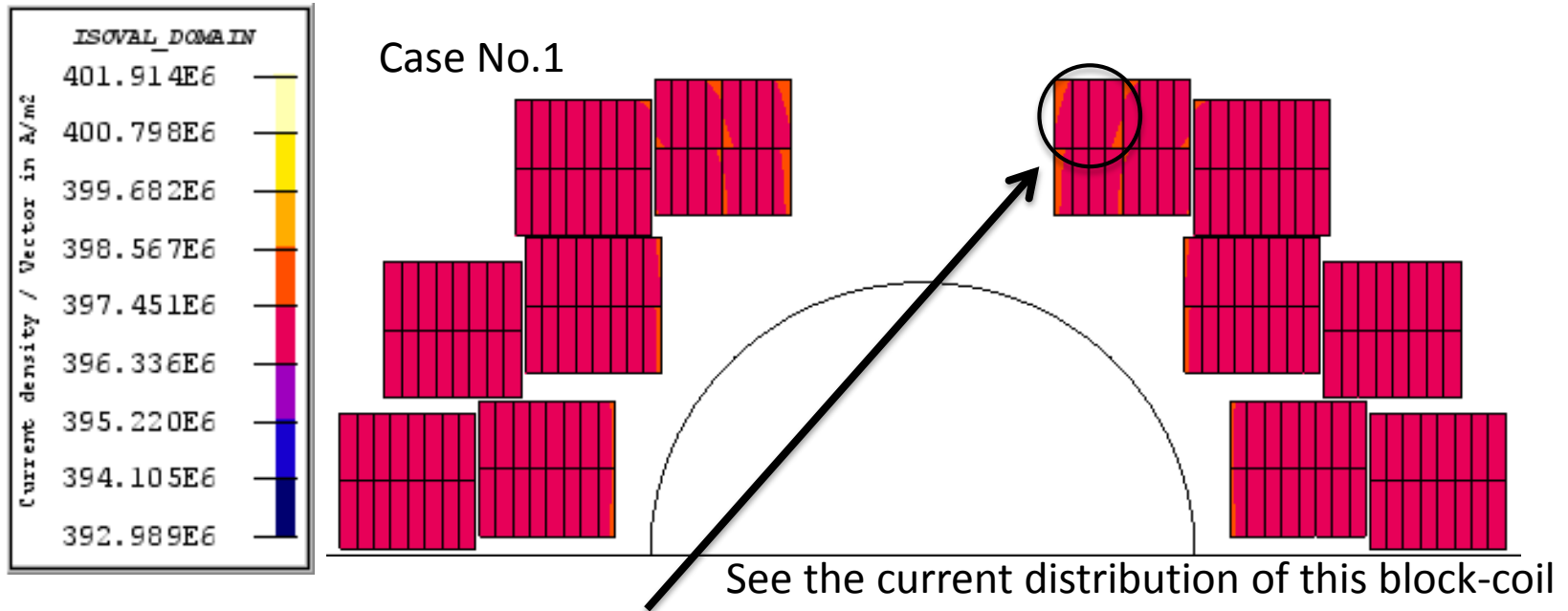
2D simulations in
AC...
With copper !

CT

Not CT

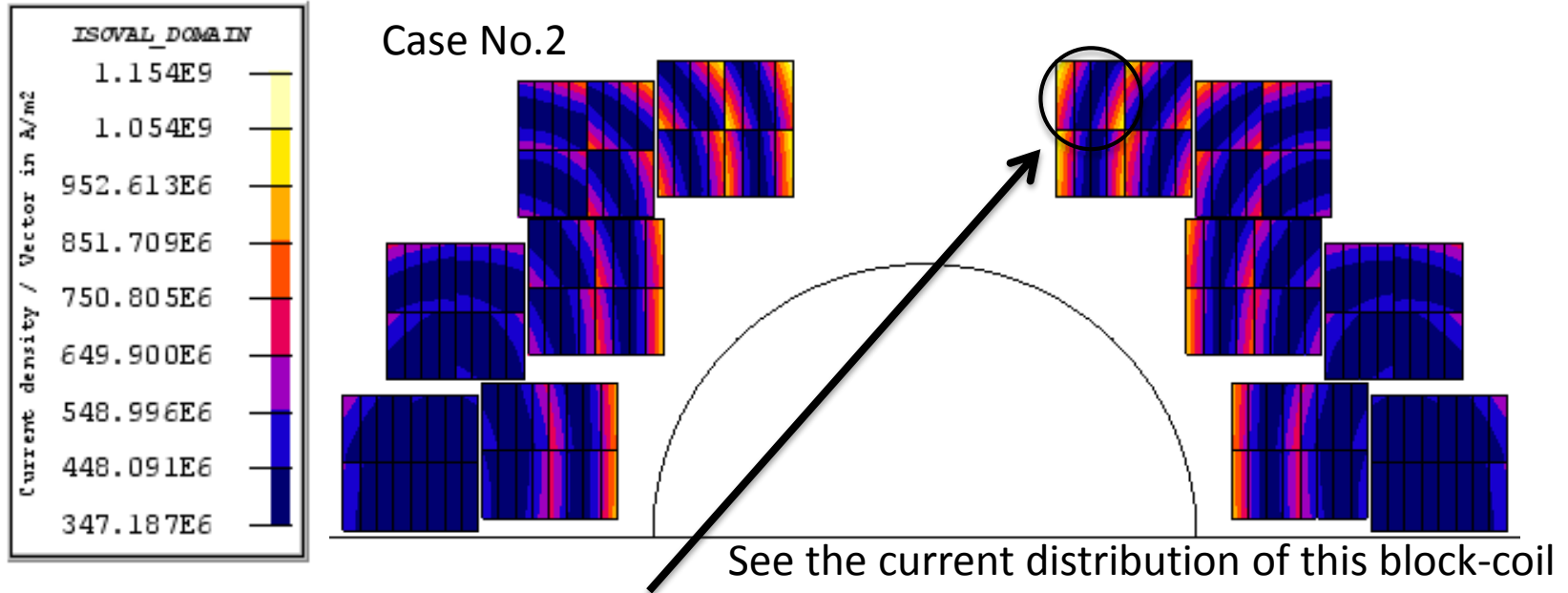


No Current transposition



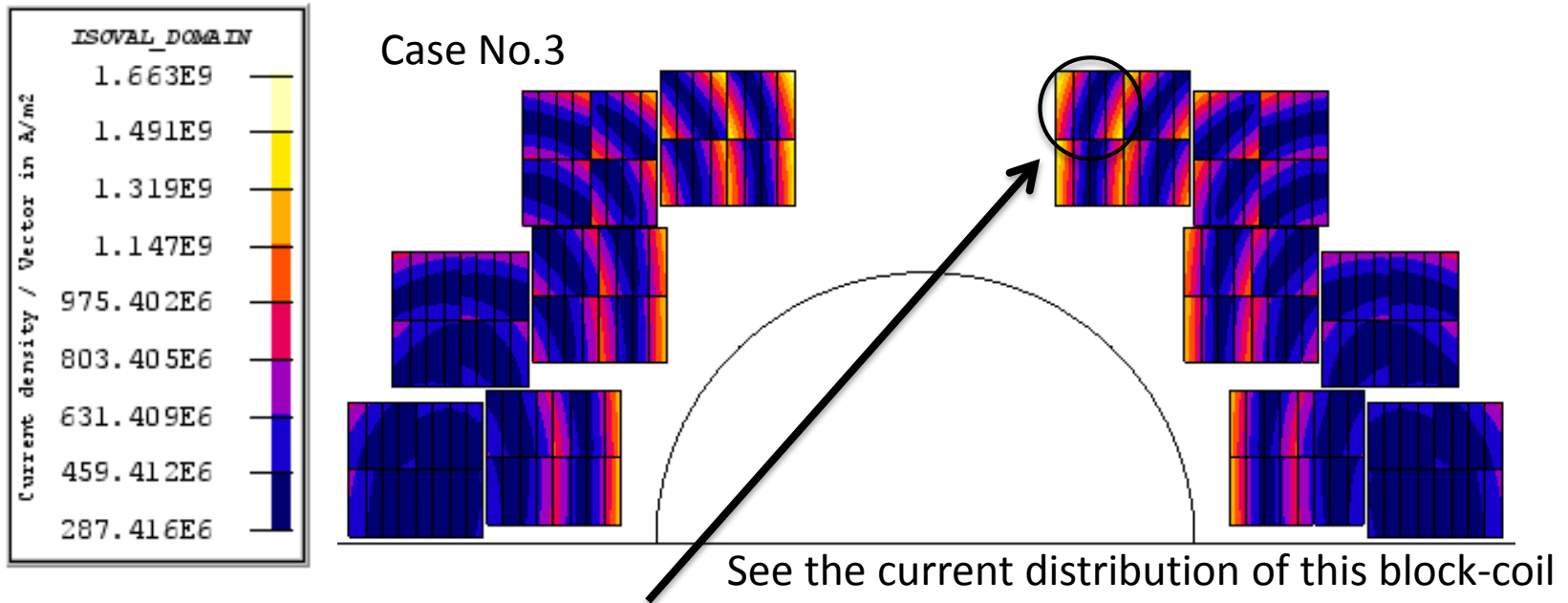
| Case No. | Current distribution | | | | Field quality $10^{-4} \cdot B_0$ |
|----------|----------------------|-------|-------|-------|--------------------------------------|
| | 1 | 2 | 3 | 4 | |
| 1 | 25 % | 25 % | 25 % | 25 % | 0.48 |
| 2 | 29.6% | 26.9% | 22.9% | 20.6% | 2.2945 |
| 3 | 35.1% | 28.5% | 20.3% | 15.4% | 5 |
| 4 | 50.9% | 35.6% | 13.1% | 0.4% | 13.1 |

No Current transposition



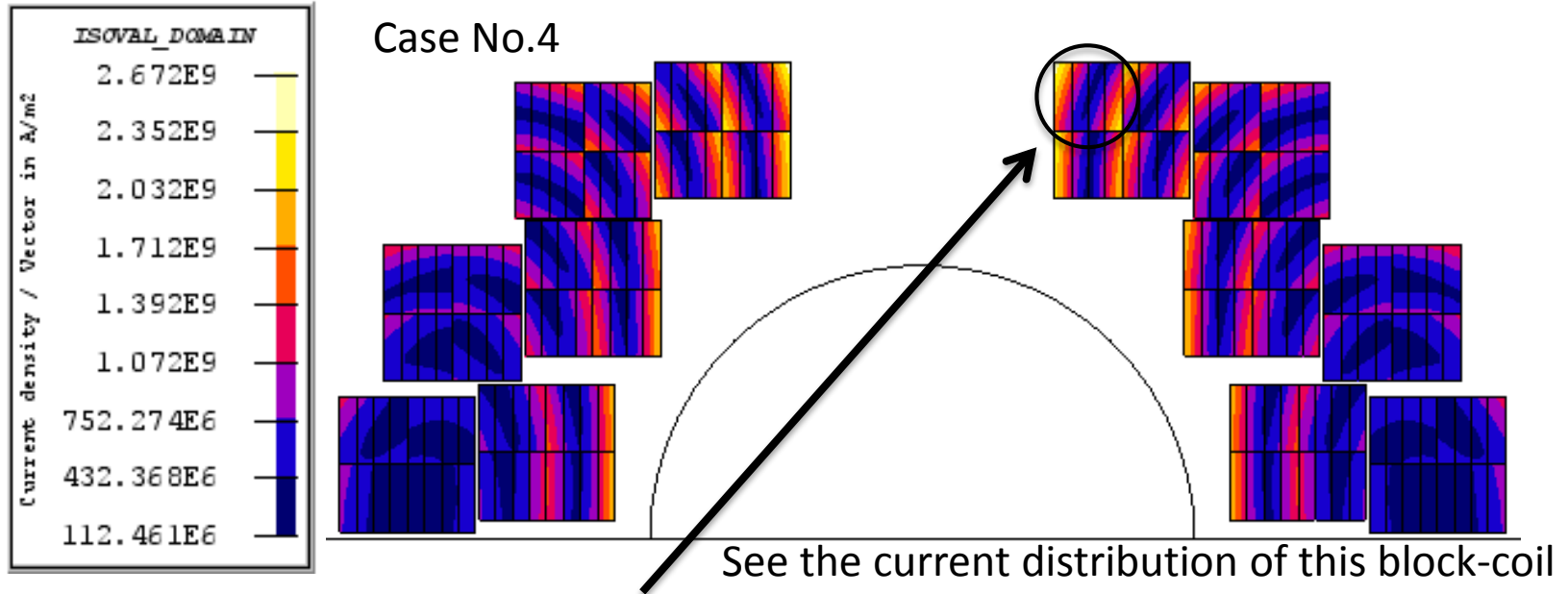
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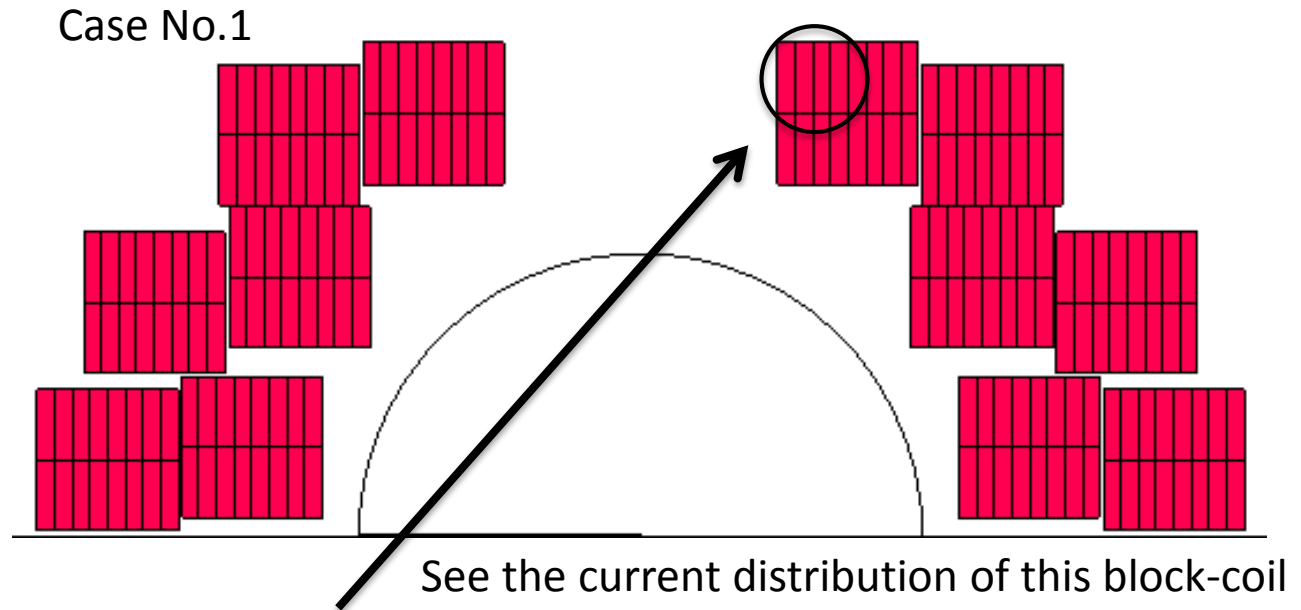
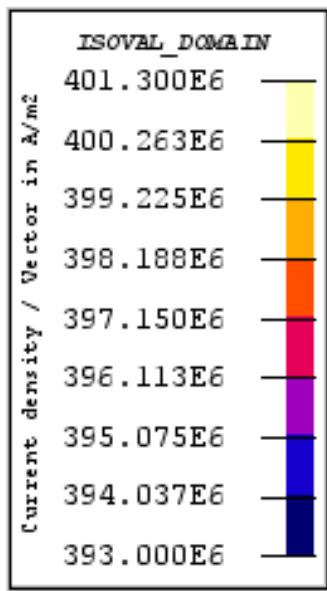
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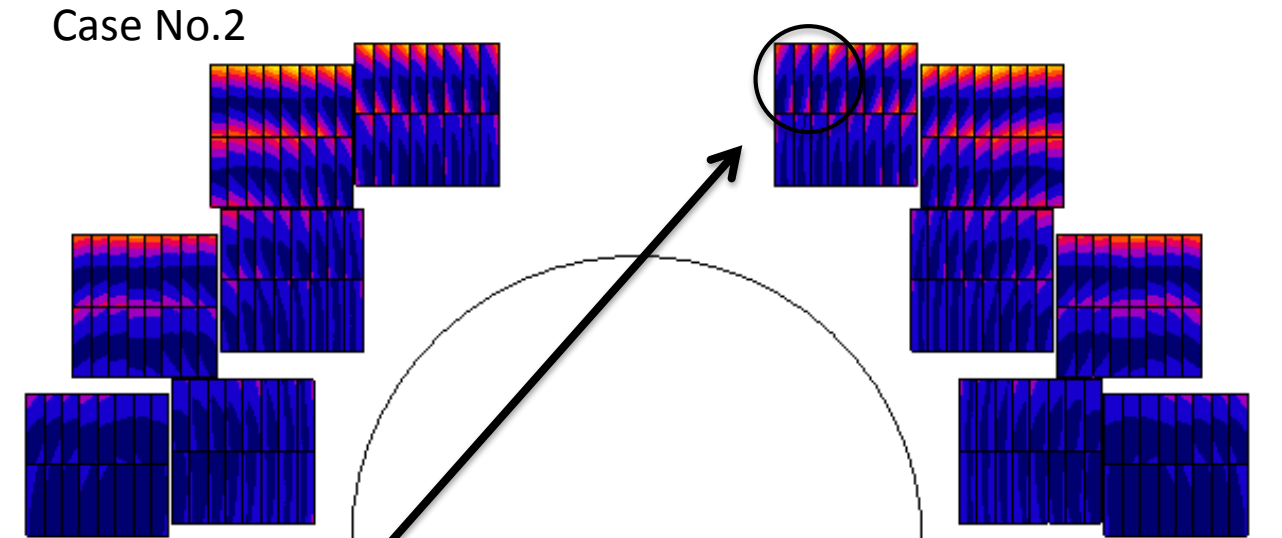
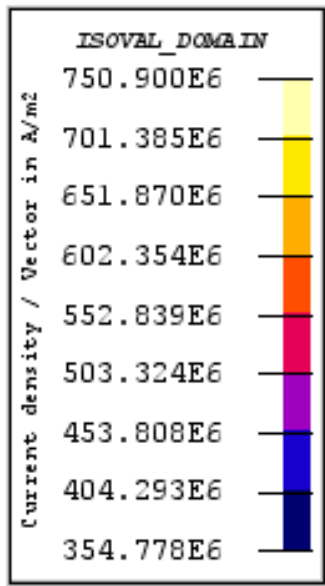
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With Current transposition



| Case No. | Current distribution | | | | Field quality $10^{-4} \cdot B_0$ |
|----------|----------------------|-------|-------|-------|--------------------------------------|
| | 1 | 2 | 3 | 4 | |
| 1 | 25 % | 25 % | 25 % | 25 % | 0.48 |
| 2 | 25.1% | 24.9% | 24.9% | 25.1% | 0.48 |
| 3 | 25.1% | 24.9% | 24.9% | 25.1% | 0.48 |
| 4 | 26.4% | 23.6% | 23.6% | 26.4% | 5.8 |

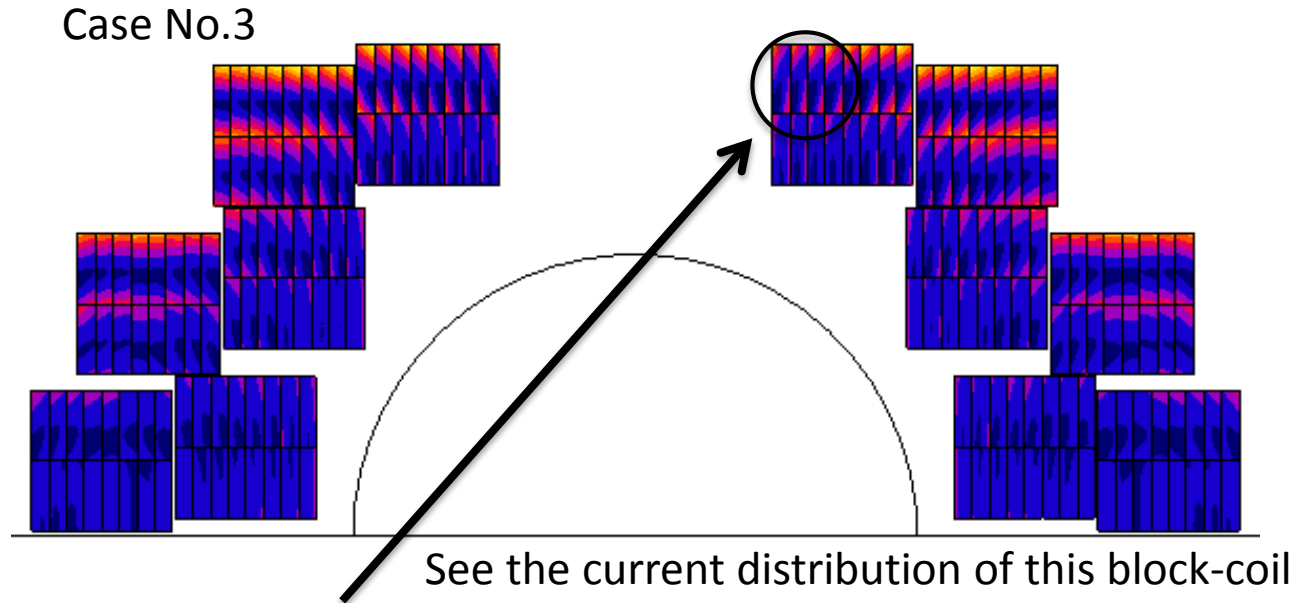
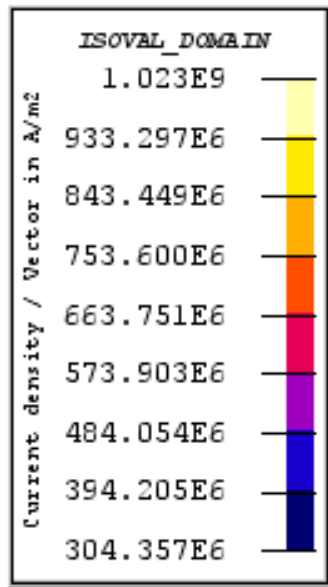
With Current transposition



See the current distribution of this block-coil

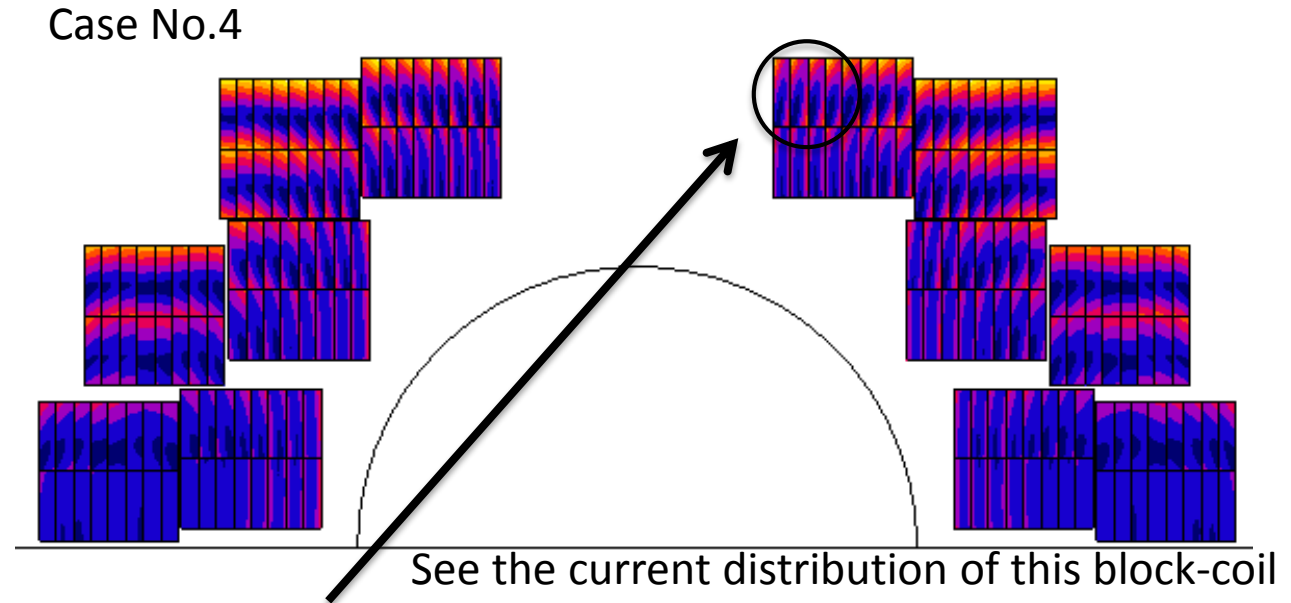
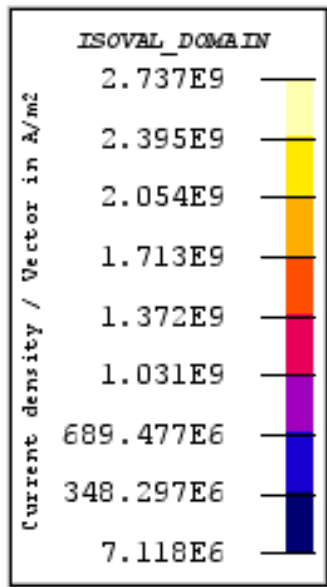
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With Current transposition



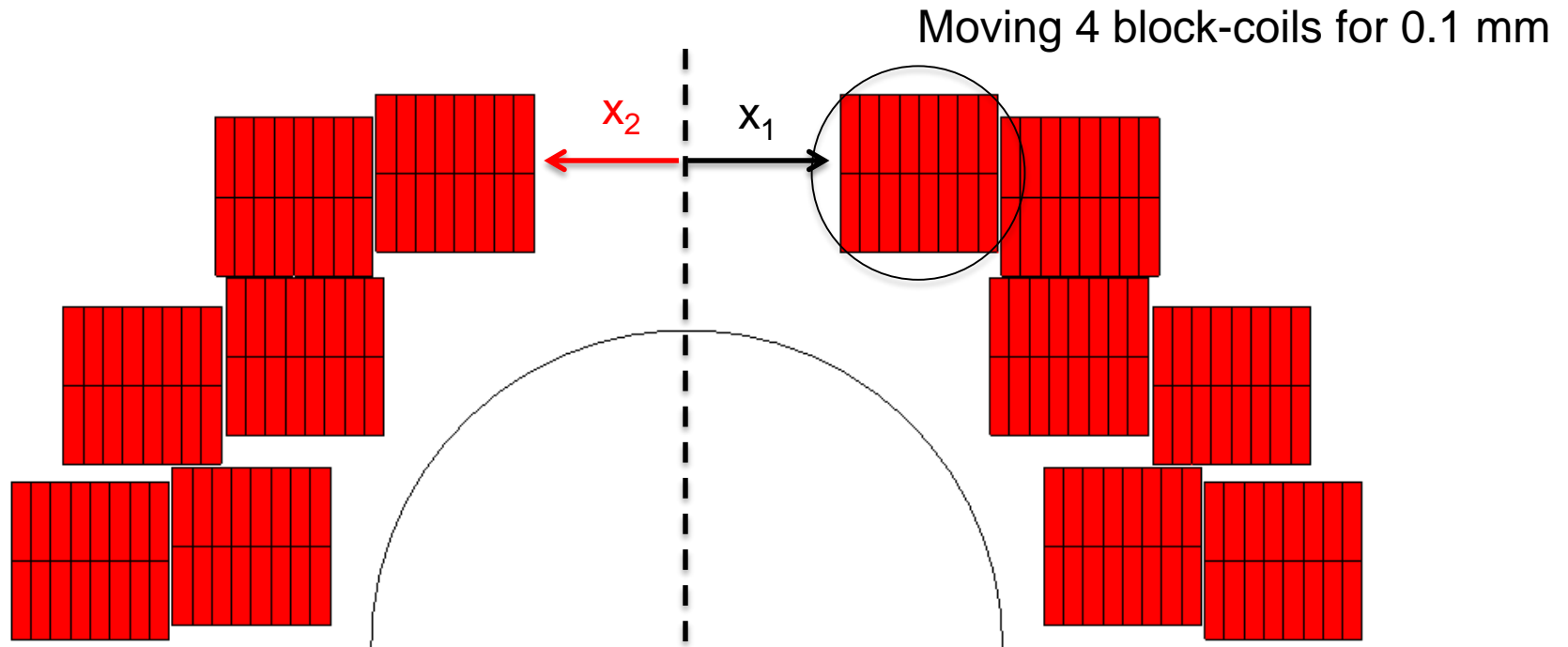
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With Current transposition

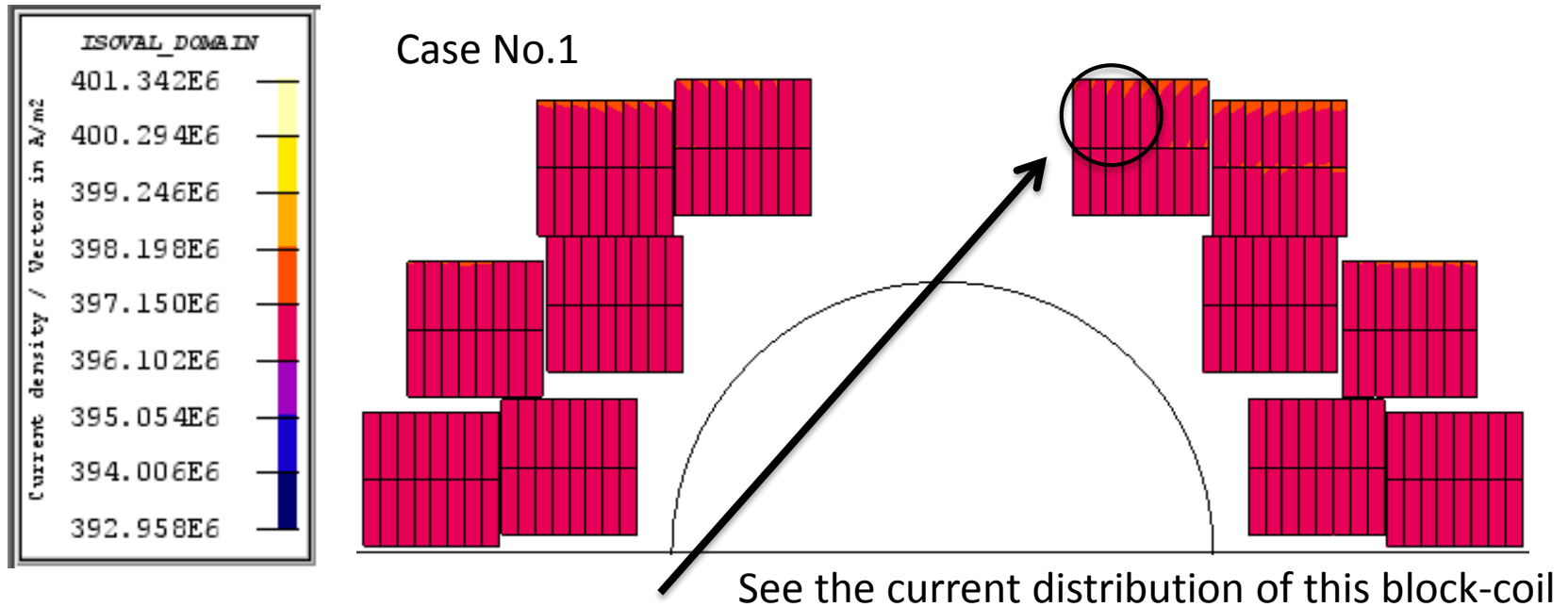


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Current transposition – sensibility to displacement

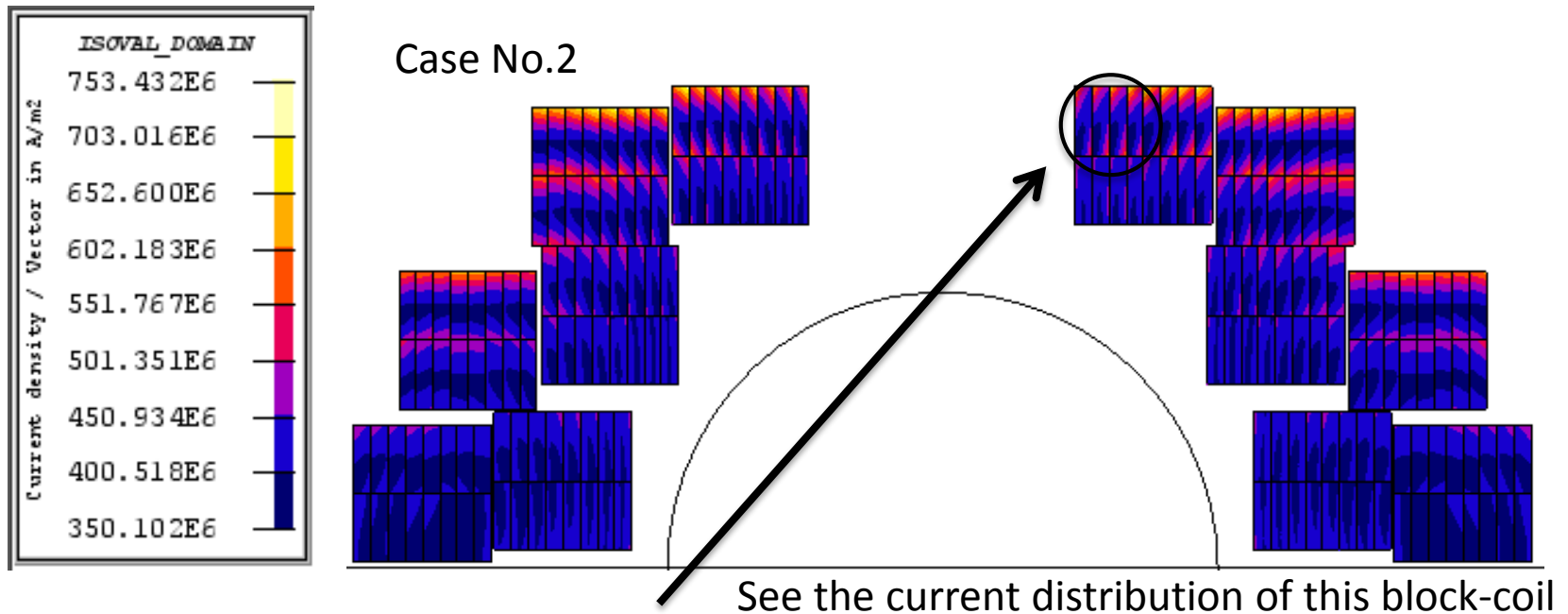


Current transposition – sensibility to displacement



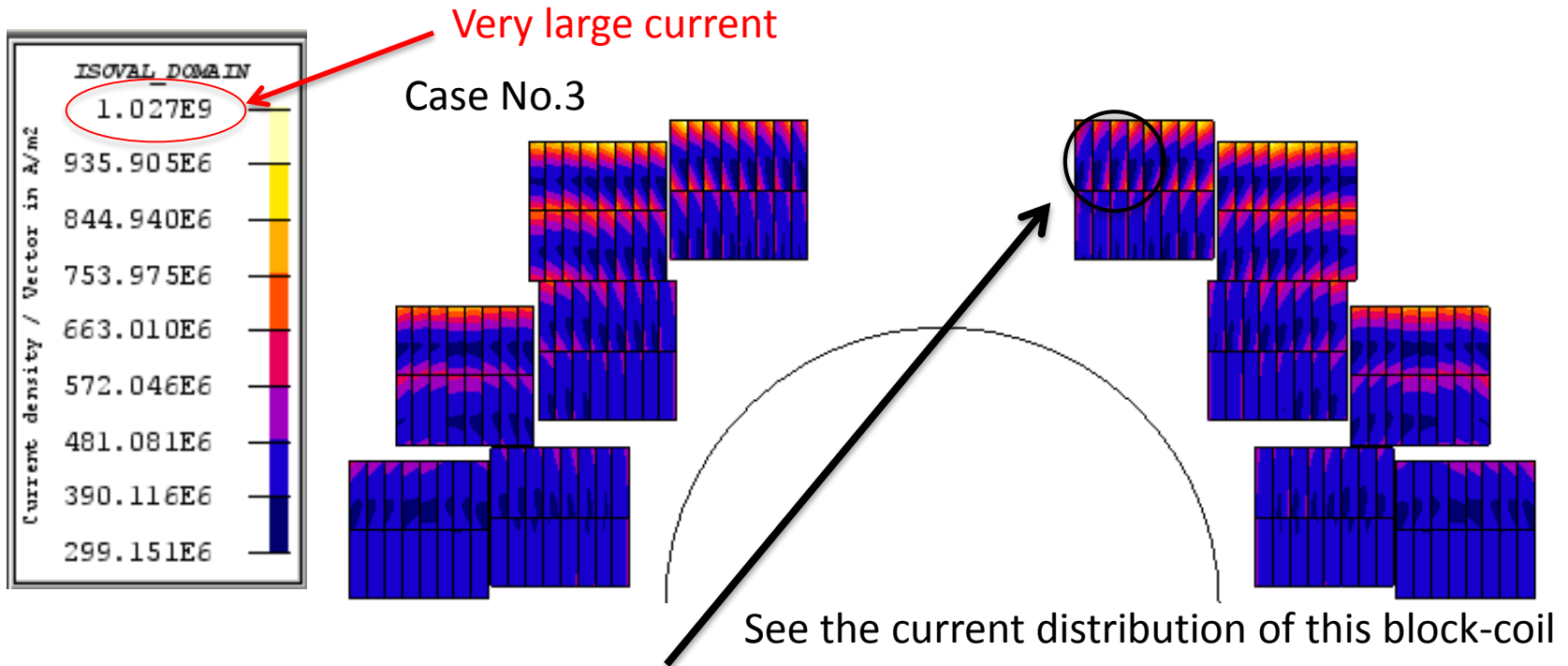
| Case No. | Current distribution | | | | Field quality $10^{-4} \cdot B_0$ | Field quality (aligned) |
|----------|----------------------|-------|-------|-------|--------------------------------------|----------------------------|
| | 1 | 2 | 3 | 4 | | |
| 1 | 25 % | 25 % | 25 % | 25 % | 0.48 | 0.48 |
| 2 | 25.1% | 24.9% | 24.9% | 25.1% | 2.69 | 0.48 |
| 3 | 25.1% | 24.9% | 24.9% | 25.1% | 2.93 | 0.48 |

Current transposition – sensibility to displacement



| Case No. | Current distribution | | | | Field quality $10^{-4} \cdot B_0$ | Field quality (aligned) |
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| | 1 | 2 | 3 | 4 | | |
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| 3 | 25.1% | 24.9% | 24.9% | 25.1% | 2.93 | 0.48 |

Current transposition – sensibility to displacement

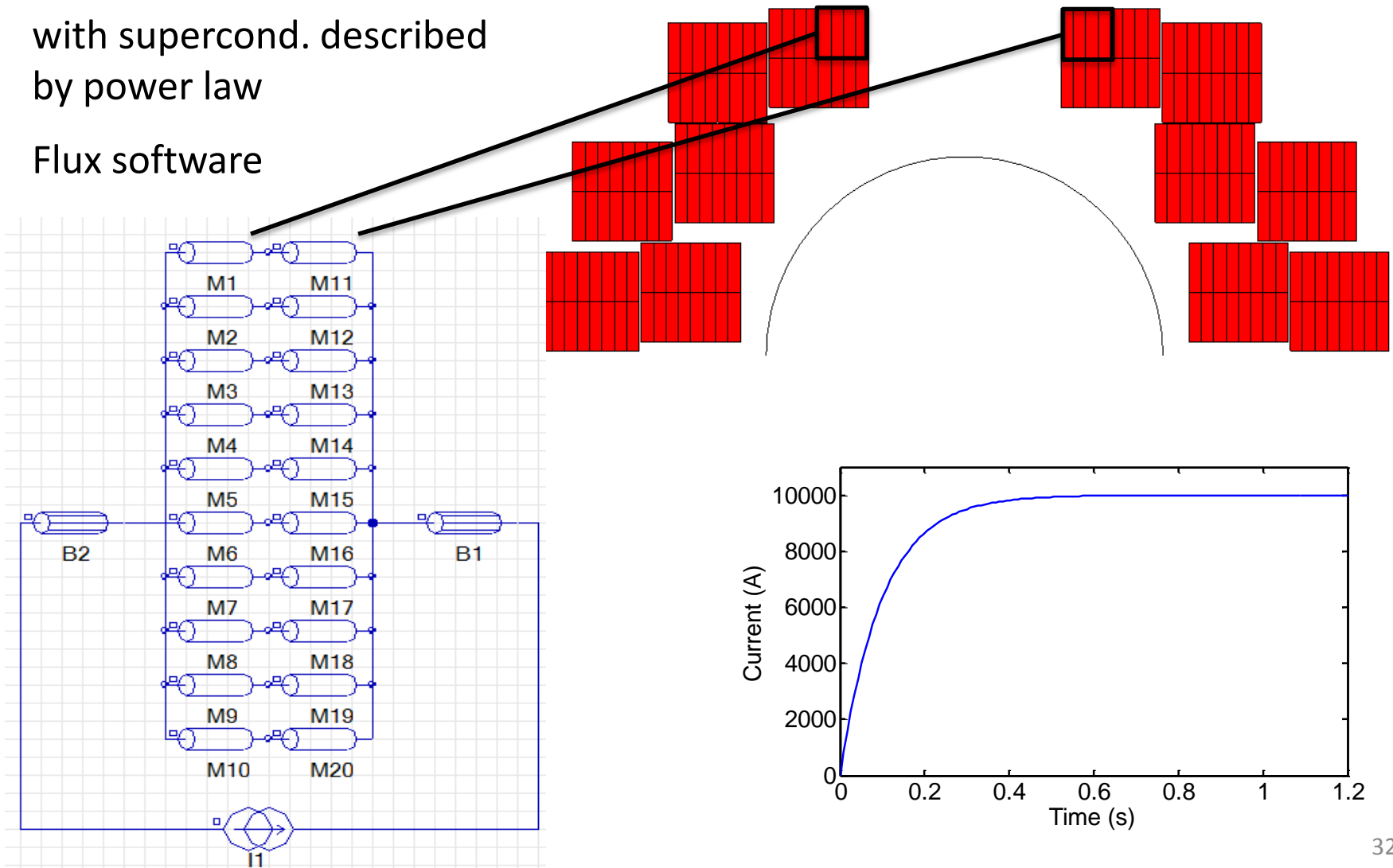


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| 1 | 25 % | 25 % | 25 % | 25 % | 0.48 | 0.48 |
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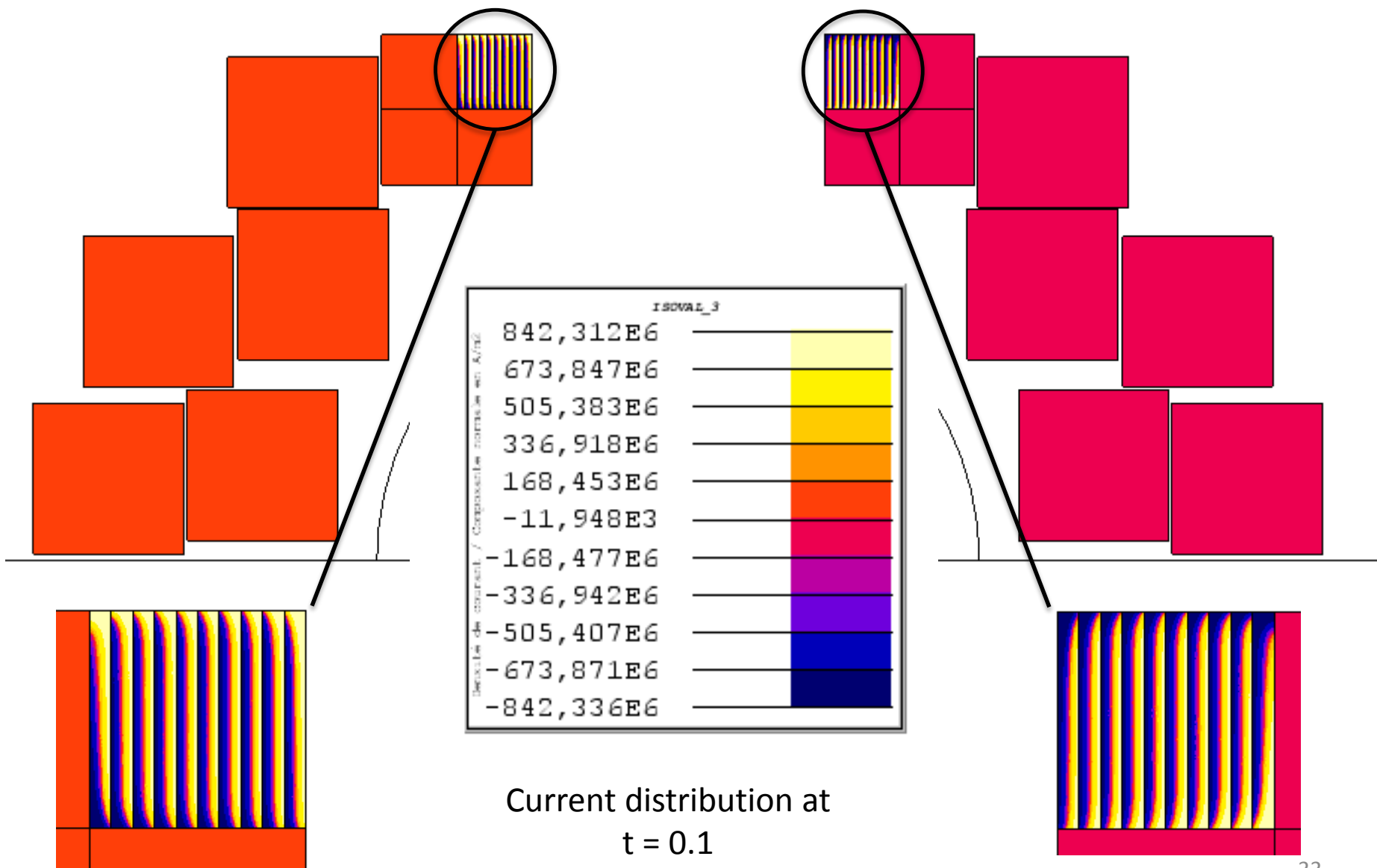
Current transposition effect : 2nd try

2D simulations in transient
with supercond. described
by power law

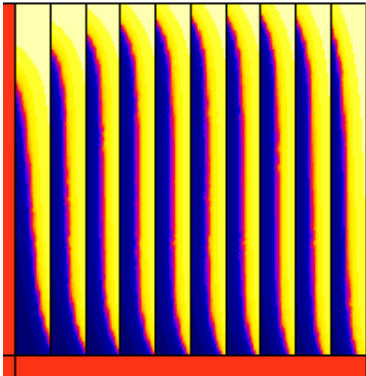
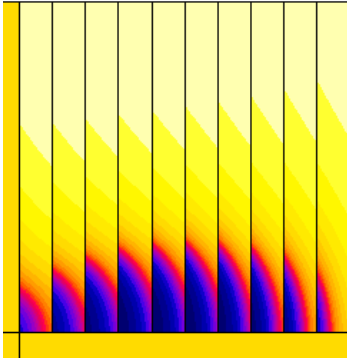
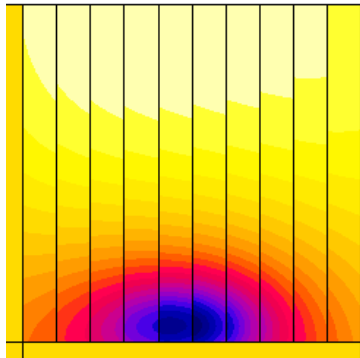
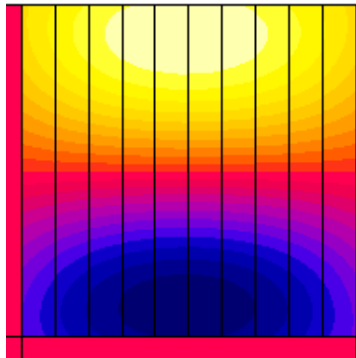
Flux software



Current transposition effect : upper blocks

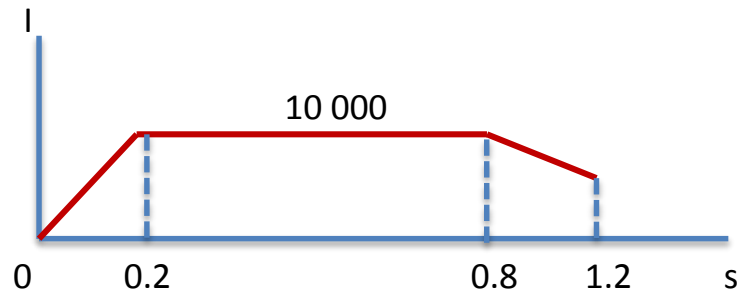


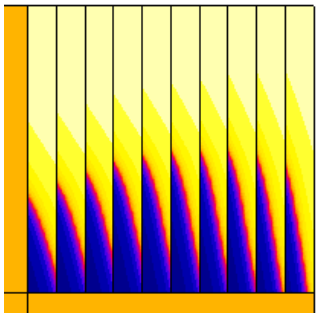
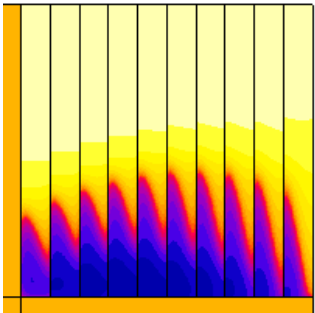
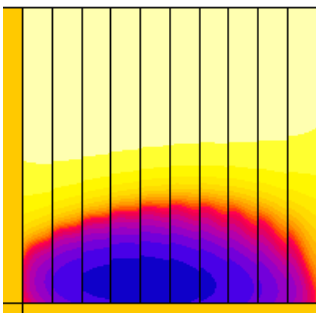
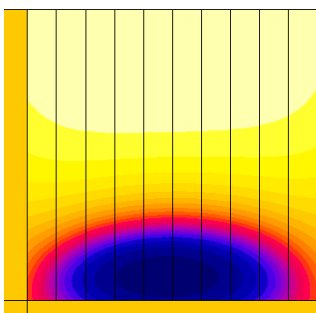
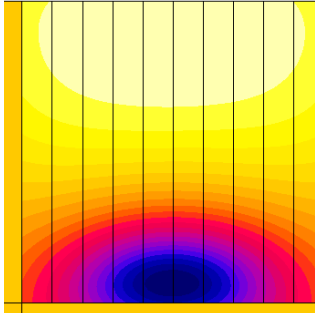
Transposition effect on current density

| $t = 0.15$ | $t = 0.3$ | $t=0.6$ | $t=1.2$ |
|--|---|---|--|
| $I = 7700 \text{ A}$ | $I = 9500 \text{ A}$ | $I = 9975 \text{ A}$ | $I = 10\,000 \text{ A}$ |
| THD = 4.961 | THD = 4.836 | THD = 1.46 | THD = 0.49 |
| 660 A/mm^2 | 578 A/mm^2 | 466 A/mm^2 | 403 A/mm^2 |
|  <p>The image shows a cross-section of a conductor with 12 vertical strands. At $t=0.15$, the current density is highly non-uniform, with the highest values (red) concentrated in the outer strands and the lowest values (blue) in the inner strands. The color scale ranges from -647 to 660 A/mm^2.</p> |  <p>The image shows the same conductor at $t=0.3$. The current density is more uniform than at $t=0.15$, but still shows a slight bias towards the outer strands. The color scale ranges from -396 to 578 A/mm^2.</p> |  <p>The image shows the conductor at $t=0.6$. The current density is significantly more uniform across all strands. The color scale ranges from 147 to 466 A/mm^2.</p> |  <p>The image shows the conductor at $t=1.2$. The current density is nearly uniform across all strands, indicating the transposition effect. The color scale ranges from 396 to 403 A/mm^2.</p> |
| -647 | -396 | 147 | 396 |

Transposition effect on current density

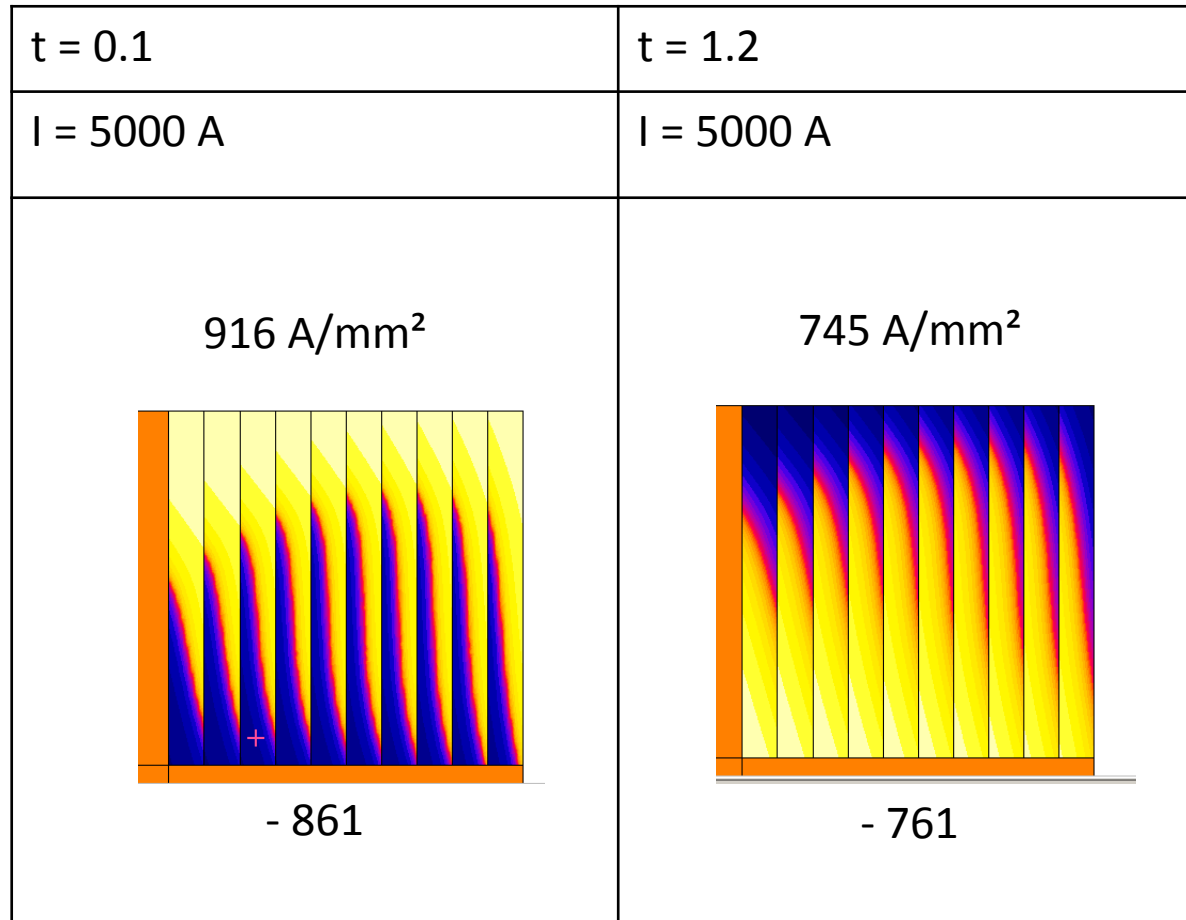
Current density homogenization on plateau



| t = 0.2 | t = 0.205 | t=0.23 | t=0.4 | t=0.8 |
|---|--|---|--|--|
| I = 10 000 A | I = 10 000 A | I = 10 000 A | I = 10 000 A | I = 10 000 A |
| 936 A/mm ² | 883 A/mm ² | 797 A/mm ² | 640 A/mm ² | 512 A/mm ² |
|  |  |  |  |  |
| - 936 | - 714 | -574 | - 297 | 76 |

Transposition effect on current density

Cycling :



Limitations to this work

- The power law considered has constant $J_c = 700 \text{ A/mm}^2$, and n values = 20
Beside, the timeframe is not practical (J is during a time at 120 % J_c)
- Conventional $E = E_c (J/J_c)^n$ leads to a paradox : uniform J in steady state !
- Flux2D good current-conserving formulation is not implemented in 3D
- Tapes are considered uniform SC 0.5mm thick, instead of thin-film multi-layers
- Tapes are considered isolated (high R interface) , it may not be ideal.
if it is not the case, non-uniformity damping will be much longer.



In order to continue, we need some experimental data !

Some experiments on single tapes are to be done in June (small bore) :
test power law models

We applied for magnet time at LNCMI-Grenoble in 280 mm cold bore to
perform tests of stack cable in field varying spatially and temporally

Conclusion

A wide range of studies must be conducted, from magnet to cable, back and forth

- Mechanical stress calculations, at the magnet and cable scale
- Quench modelling and protection development : effect on the range of I_{op}
- Twisting effect on field distribution and field orientation in the coil heads

Some conclusions can be drawn :

- An insert reaching the requirement can be made with $J_e = 400 \text{ A/mm}^2$, knowing that the lower value for perfect $\cos\text{-}\theta$ is 340 A/mm^2 .
- Twisted stack cable offers impressive advantages, the key issue is current distribution : increase the resistance between tapes may be a solution, some solutions can be found on the magnet side (ramping the insert first?)
- We can at least consider continuously twisted stack :
Current density in the tapes reaches 620 A/mm^2 but the surface is not lost

