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on Hyperfine Interactions and 19th International Symposium
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**Study of Dependence of Quasi-Particle Alignment
on Proton and Neutron Numbers in $A=80$ Mass
Region through g -factor Measurements**

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OUTLINE

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- **Experimental details**
- **Results and Discussion**
- **Summary**

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1, Background

g-factor

$$\mu = gI = \frac{1}{\mu_N} \int \Psi_{J,J}^* M_Z \Psi_{J,J} dt \quad g \rightarrow \Psi_{J,J}$$

physical quantity to characterize nuclear properties

very sensitive to nuclear structure

g-factor measurements

provide direct and definite information

on nuclear structure

**Nuclear structure at high spins
in the mid-weight mass region of $A=80$
possesses many interesting features**

e.g.

Shape co-existence

Structural softness

Strong dependence on spin & particle numbers

Magnetic rotation

Quasi-particle alignment (QPA) in the $g_{9/2}$ orbit

- **QPA(Quasi-particle alignment (QPA) in the $g_{9/2}$ orbit)**
a significant feature
- **The g-factor measurement of intra-band states can provide direct & unique information on QPA**

g-factor of high-j ($g_{9/2}$ orbit) protons

positive and large $g_{\pi} = 1.38$

g-factor of high-j ($g_{9/2}$ orbit) neutrons

negative and small $g_{\nu} = -0.24$

- **The present work**
motivated to measure g-factors of high spin states of ground rotational bands in the mass $A=80$ region in order to study the quasi-particle alignment
- **Experiment performed at HI-13 tandem accelerator in CIAE**

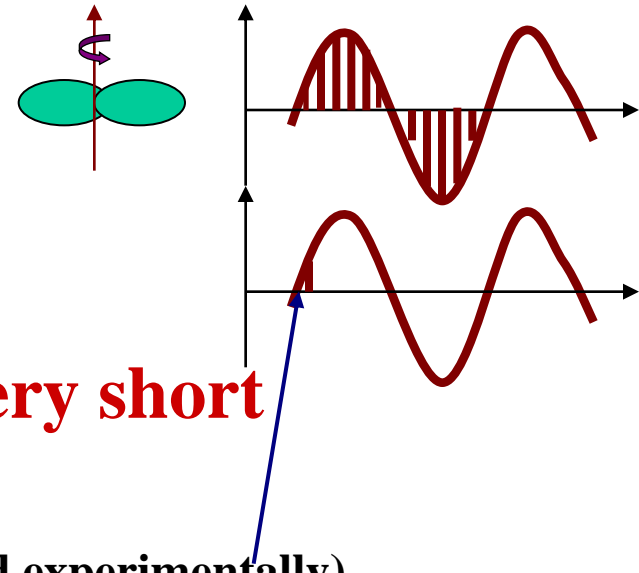
2, Experimental details

- **Requirements**
in measuring g-factor of high spin states
- **TMF-IMPAD method**
- **Population of high spin states**
- **Data Analysis**

Difficult to measure

g-factors of high spin states:

- **Lifetimes of high spin states are very short usually in the range of sub-ps~ps**
(Only a very small part of precession can be measured experimentally)
- **Nuclear states of interest are populated by fusion evaporation reactions**
nuclear precession transfer from higher feeding states to lower states
needs to be carefully considered
(very complicated)



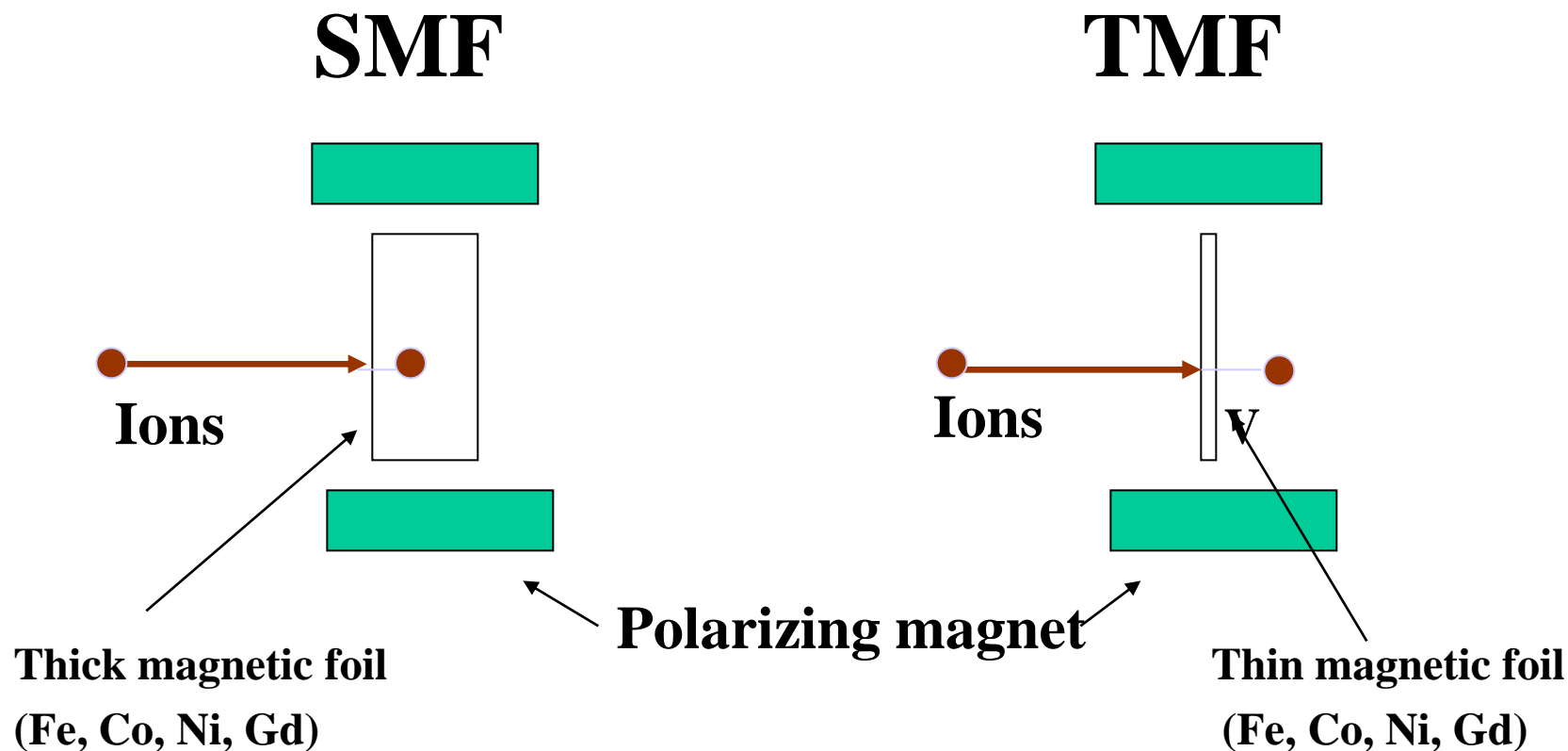
g-factor measurements of high spin states with short lifetimes requirements:

- **Very high magnetic field: $\sim 10^3$ T (TMF)**
- **Knowledge of kinematics from the production of recoil nucleus to its leaving the magnetic foil**
- **Very precise measurement of precession angle**
 $g = 0.31, B = 3.68 \times 10^3$ T, $tr = 0.25$ ps
 $\Delta\theta = \omega_L t = 1.63^\circ$
- **Very high resolution γ ray detection due to complicated g ray spectra**
- **Delicate multi-layer target assembly**

Type of magnets	Magnetic strength /T	Minimum applicable lifetime/sec
Electro-magnet	~2.5	~1.0x10 ⁻⁹
Super-conducting magnet	~9	~2.3x10 ⁻¹⁰
Static magnetic field (SMF)	~20	~1.0x10 ⁻¹⁰
Transient magnetic field (TMF)	~3500	~6.0x10 ⁻¹³

$g = 0.3$ 和 $\Delta\theta = 1.72^\circ$ used in calculation

T (Tesla) = 10⁴ G (gauss)



TMF combined with the time integral perturbed angular distribution (PAD) method is a unique way to measure g-factors of high spin states with short lifetimes

TMF-IMPAD used to measure g-factors of intra-band states of ground rotational bands

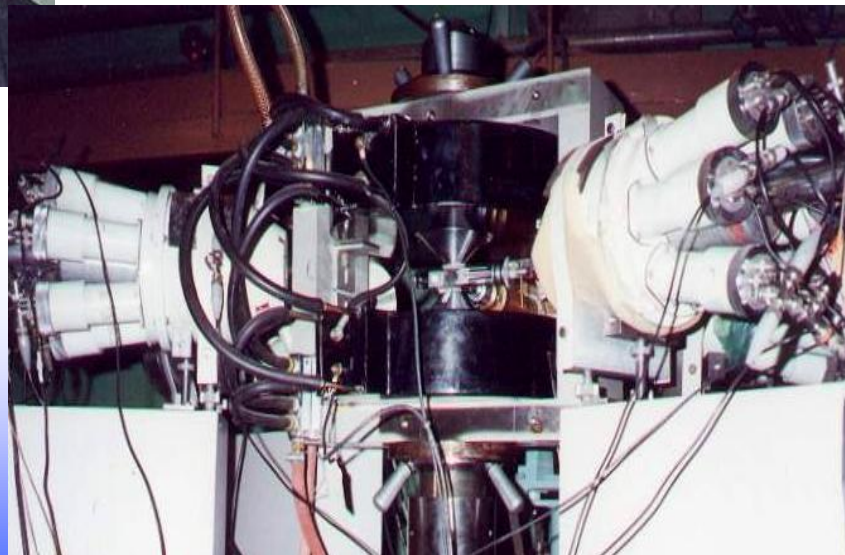
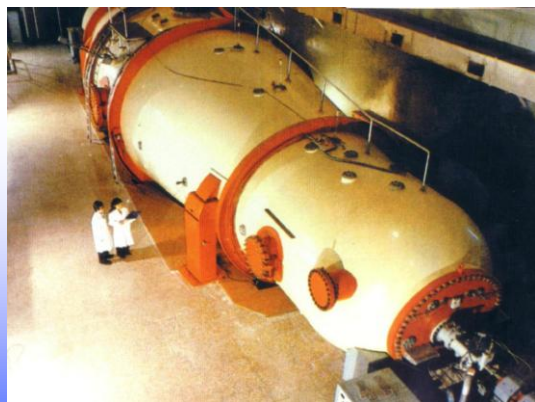
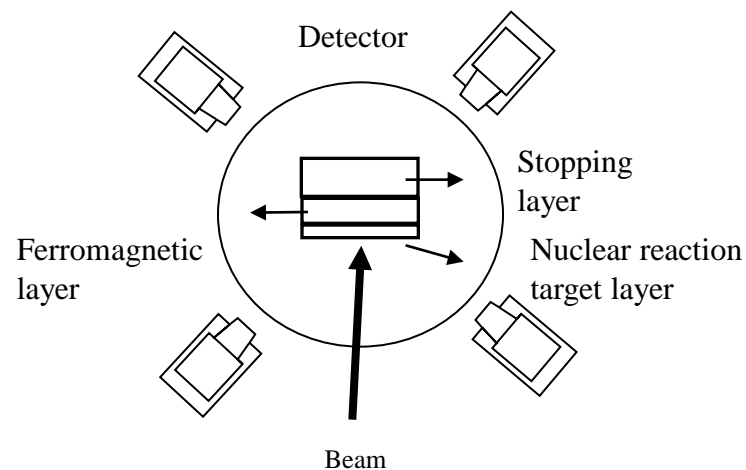
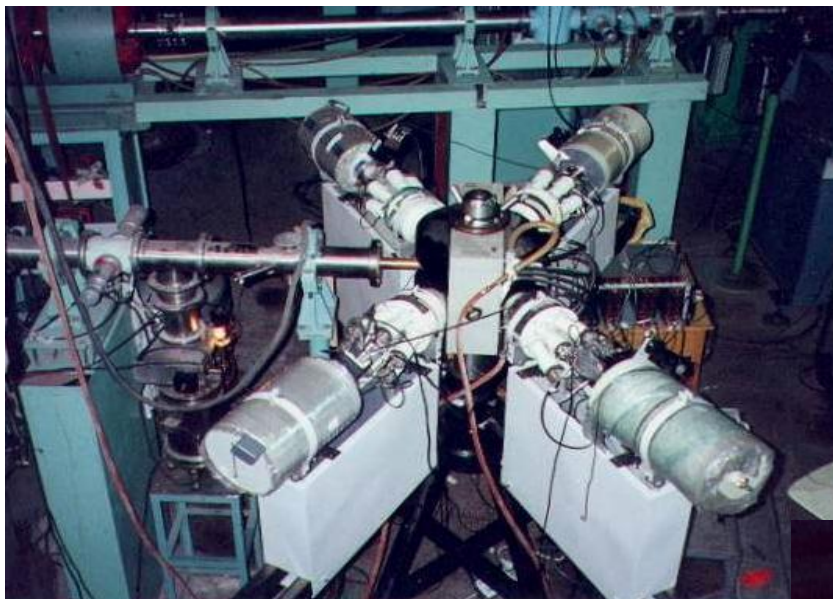
which can precisely determine precession angle $\Delta\theta$

Then g-factor can be deduced through





$$g = (\Delta\theta) \hbar / B_{\text{TMF}} t \mu_N$$

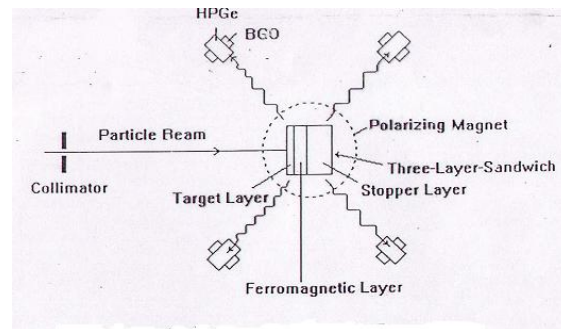
(t precession time)

View of TMF-IMPAD set up at HI-13 tandem

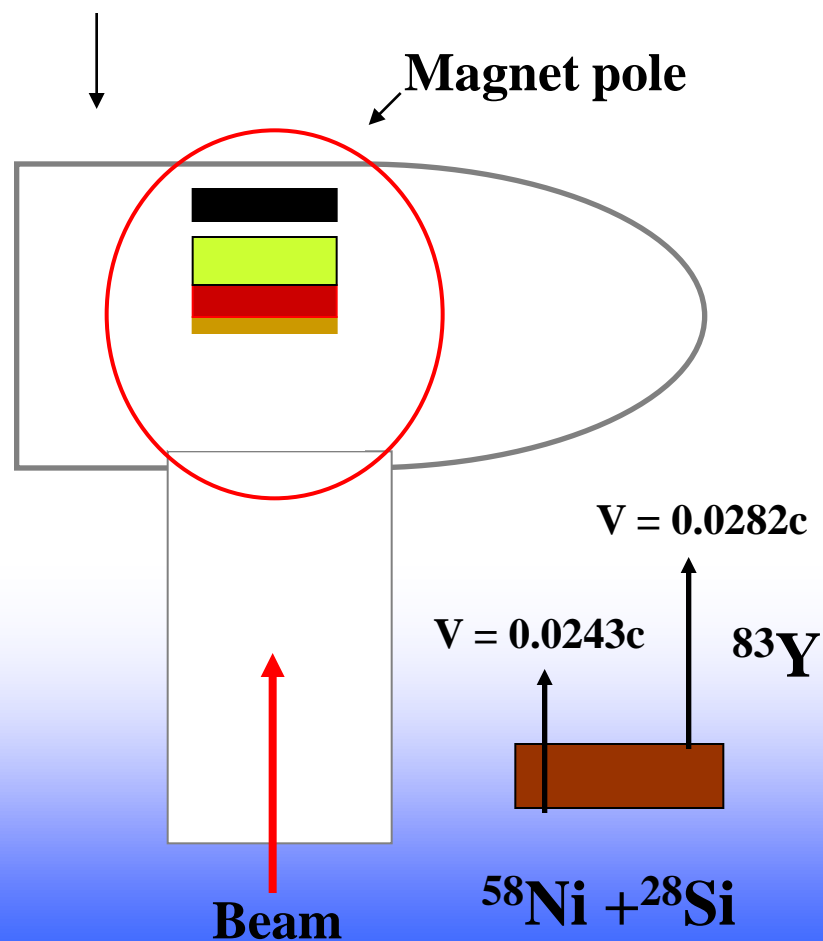


Multi-layer target

- 3-layer target used
- 0.4 mg cm^{-2} target foil enriched to 99.8% 
- Ferro-magnetic Fe foil 1.575 mg cm^{-2} 
- Cu stopper 12 mg cm^{-2} 
- Ta beam catcher 800 mg cm^{-2} 



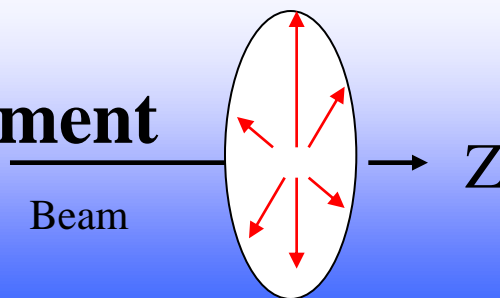
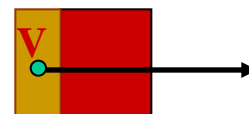
T-shaped bronze chamber



Population of high spin states by fusion evaporation reactions

- Large nuclear reaction cross section
- Many nuclides simultaneously produced
- Populating all high spin states of interest

- **High velocity** of recoil nuclides
- **Large angular momentum transfer**
& **high degree of nuclear alignment**
important for TMF-IMPAD measurement



**The high spin states
of the ground rotational band
in ^{82}Sr , ^{83}Y , ^{84}Zr , ^{85}Nb , ^{85}Zr and ^{86}Zr
were populated by the fusion-evaporation
reactions with the heavy ion beams
from the HI-13 tandem accelerator at CIAE**

- $^{58}\text{Ni}(^{28}\text{Si},3\text{p})^{83}\text{Y}$ $E_{\text{Si}}=98\text{ MeV}$ $\sigma\sim 230\text{ mb}$
- $^{58}\text{Ni}(^{28}\text{Si},4\text{p})^{82}\text{Sr}$ $E_{\text{Si}}=110\text{MeV}$ $\sigma\sim 103\text{ mb}$
- $^{58}\text{Ni}(^{28}\text{Si},\text{p}2\text{n})^{85}\text{Nb}$ $E_{\text{Si}}=110\text{MeV}$ $\sigma\sim 50\text{ mb}$
- $^{60}\text{Ni}(^{28}\text{Si},2\text{pn})^{85}\text{Zr}$ $E_{\text{Si}}=98\text{MeV}$ $\sigma\sim 160\text{ mb}$
- $^{58}\text{Ni}(^{28}\text{Si},2\text{p})^{84}\text{Zr}$ $E_{\text{Si}}=98\text{ MeV}$ $\sigma\sim 40\text{ mb}$
- $^{58}\text{Ni}(^{32}\text{S},4\text{p})^{86}\text{Zr}$ $E_{\text{S}}=110\text{ MeV}$ $\sigma\sim 125\text{ mb}$

projectile energies and reaction cross sections calculated by
a Cascade program and a PACE4 program

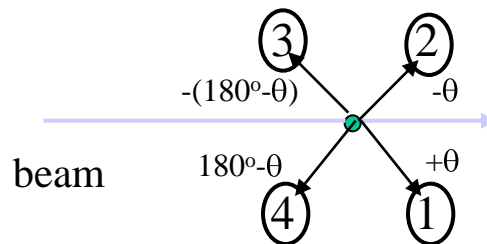
Data Analysis

Double ratio constructed from the field up & down counts to infer the nuclear precession of a state

$$\rho = \frac{\rho_{12}}{\rho_{34}}$$

$$\rho_{12} = \frac{N_1^\uparrow}{N_1^\downarrow} \frac{N_2^\downarrow}{N_2^\uparrow}$$

$$\rho_{34} = \frac{N_4^\uparrow}{N_4^\downarrow} \frac{N_3^\downarrow}{N_3^\uparrow}$$



ρ_{12} and ρ_{34} single ratios formed with the counts N^\uparrow and N^\downarrow of $\pm\theta$ detector pair and $\pm(180^\circ-\theta)$ detector pair for an interested transition

The average precession angle $\Delta\theta$ deduced from

$$\Delta\theta = \varepsilon / S(\theta) \quad \varepsilon = \frac{\rho - 1}{\rho + 1} \quad S(\theta) = \frac{1}{W(\theta)} \frac{dW(\theta)}{d\theta}$$

g-factor obtained from the precession $\Delta\theta$ and transient field B_{TMF}

$$g = \frac{-\Delta\theta \hbar}{\mu_N \int_{in}^{out} B_{TMF}(t) e^{-t/\tau} dt}$$

$$B_{TMF}(v) = 96.7(v/v_0)^{0.45} Z^{1.1} \mu_B N_p$$

μ_N the nuclear magneton, τ the mean lifetime of nuclear stat, $S(\theta)$ logarithmic slope of γ -ray angular distribution, the integration runs over the recoiling ion entry to exit times of the ferromagnetic Fe layer. The parameterization of transient magnetic field $B_{TMF}(t)$ given by Shu et al (Phys.Rev., C21 (1980) 1828)

the Bohr velocity, the velocity of the recoiling nuclei that depends on time.

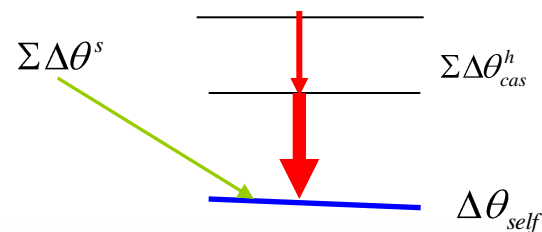
B_{TMF} interpreted as electron polarization transfer from Fe to the s orbit electron of passing ion

B_{TMF} Fe:Co:Ni:Gd = 1.0:0.8:0.3:1.2, Gd needs low temperature.

Precession transfer correction

- The precession of a lower state also reflects the precessions of the higher spin states in a cascade transition and the side feeding states
- **The measured precession of an interested state is an algebraic sum of the precession of itself and the precessions of all states that feed it**

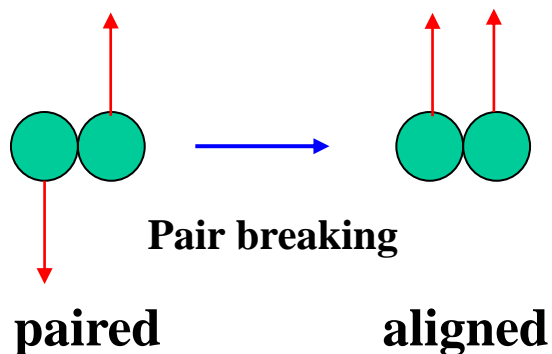
$$\Delta\theta_m = \Sigma\Delta\theta_{cas}^h + \Sigma\Delta\theta^s + \Delta\theta_{self}$$



- To get the net precession of a certain state a computer program was used to follow the time evolution of the recoiling nucleus from its production in the target to its exit from the Fe foil

3, Results and discussion

- Quasi-particle alignment (QPA)



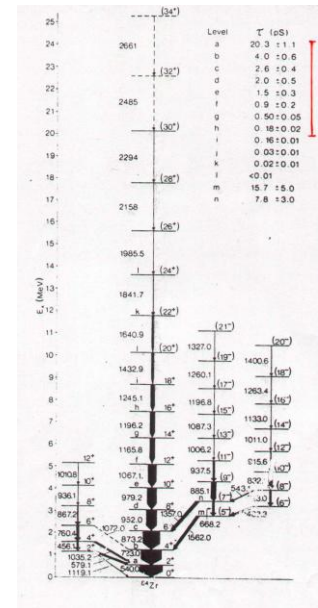
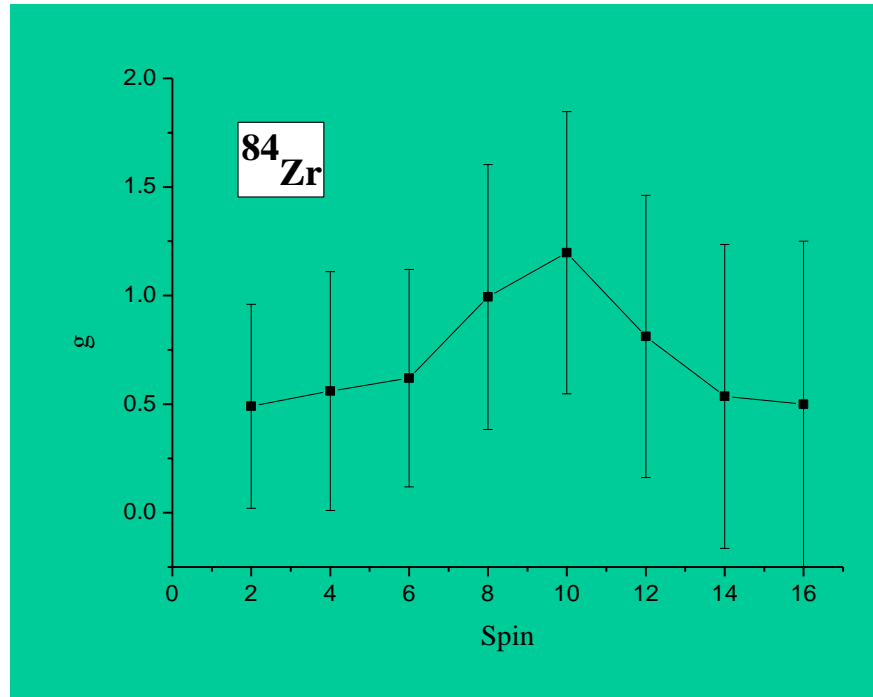
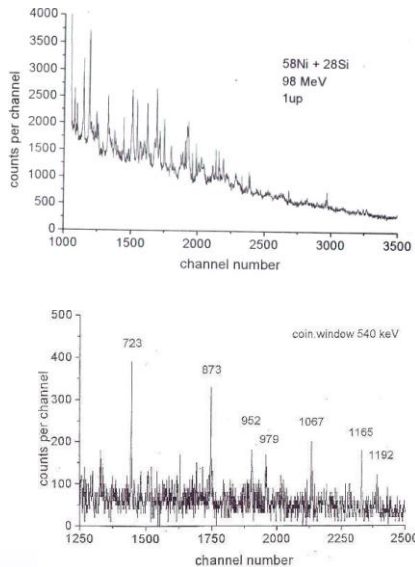
Dependence of QPA on spin

Dependence of QPA on proton number

Dependence of QPA on neutron number

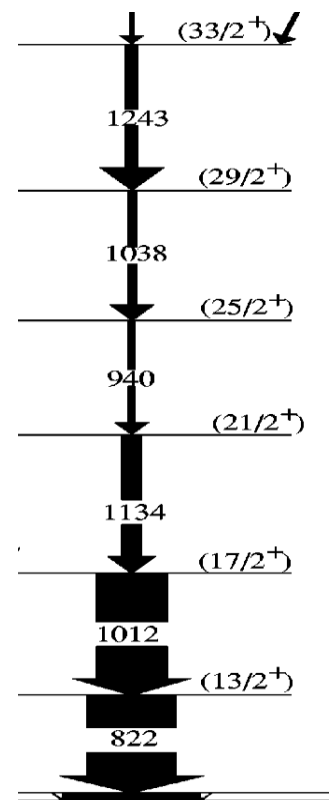
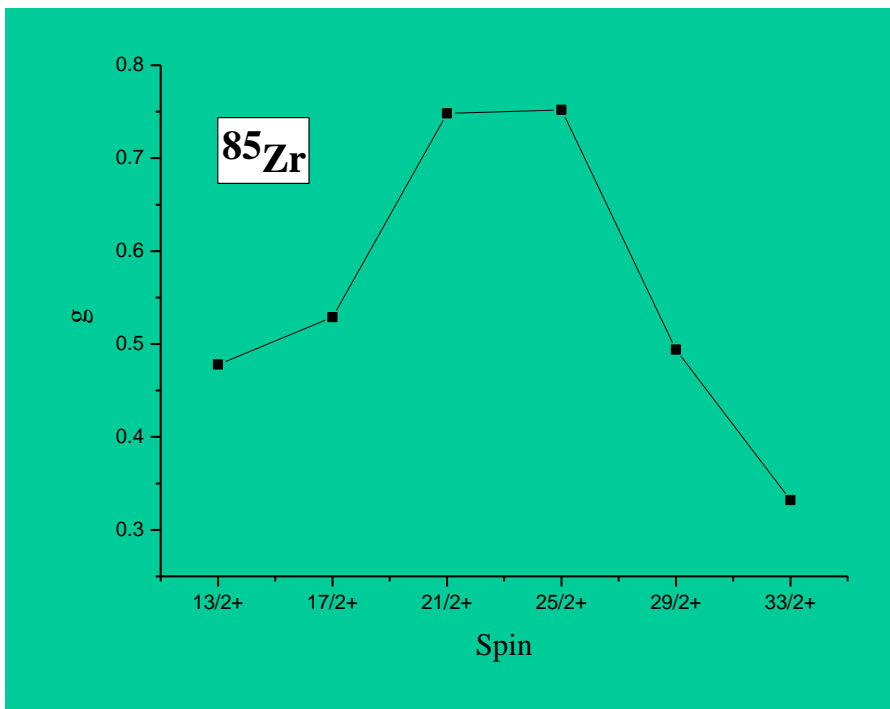
Dependence of quasi particle alignment on spin

^{84}Zr



$g_{9/2}$ proton alignment first
 then followed by $g_{9/2}$ neutron alignment

^{85}Zr



$g_{9/2}$ proton alignment first

then followed by $g_{9/2}$ neutron alignment

^{86}Zr

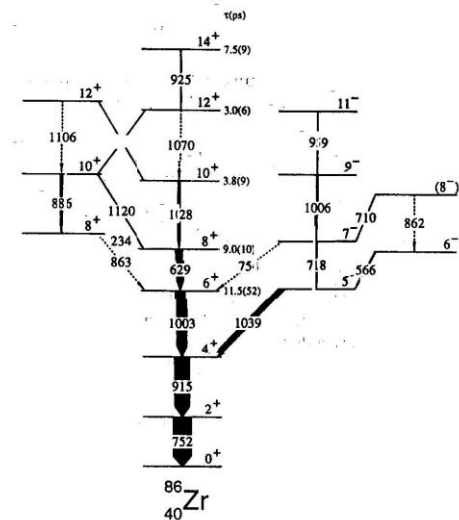
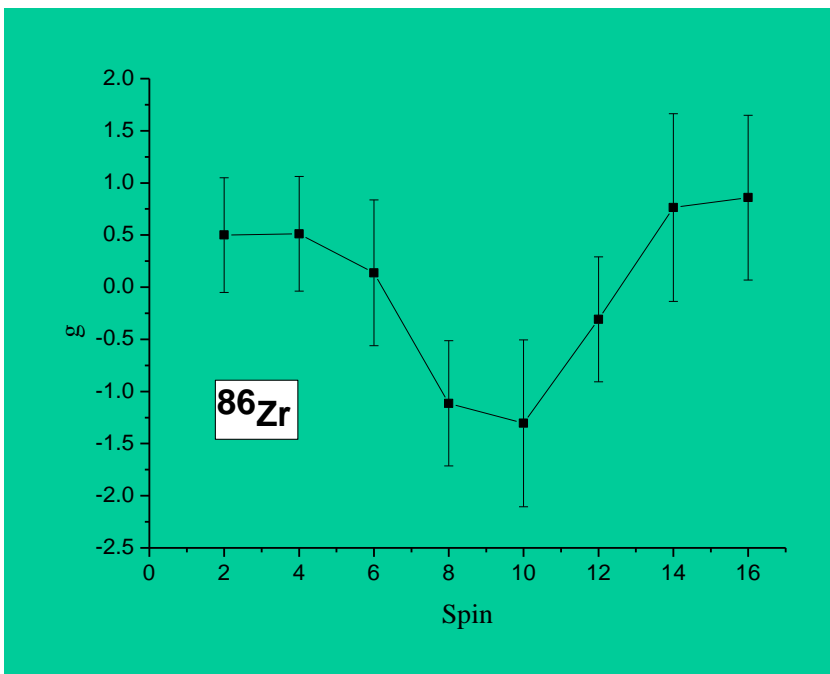
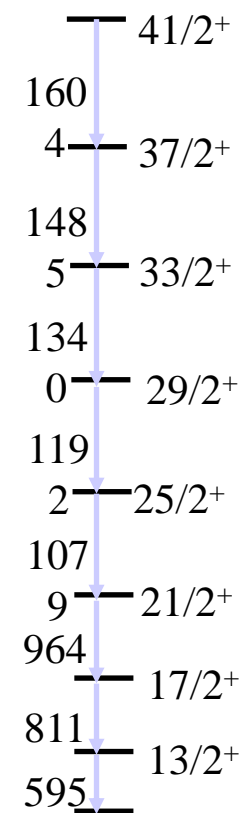
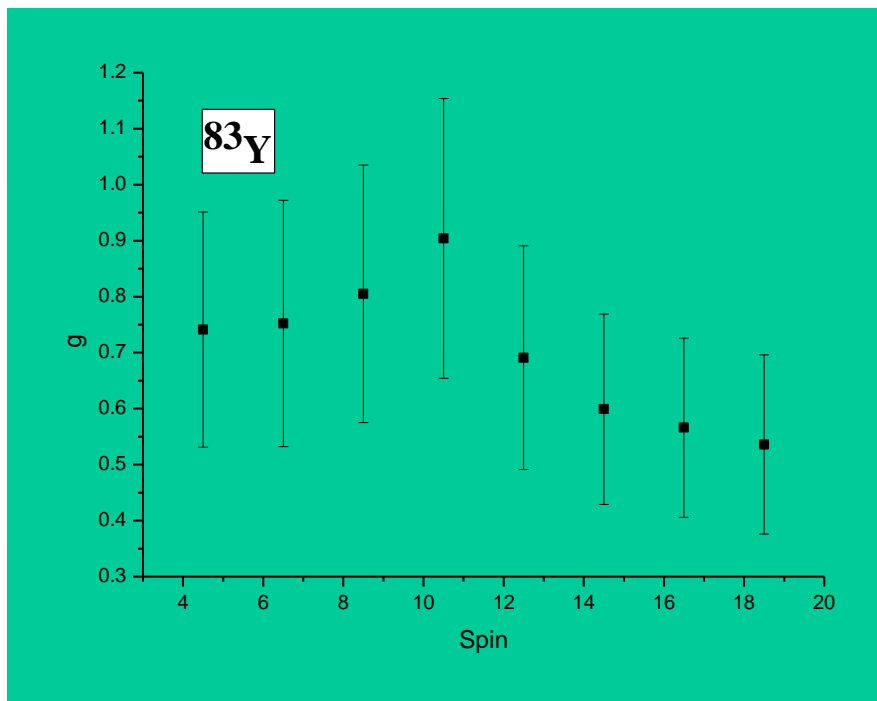
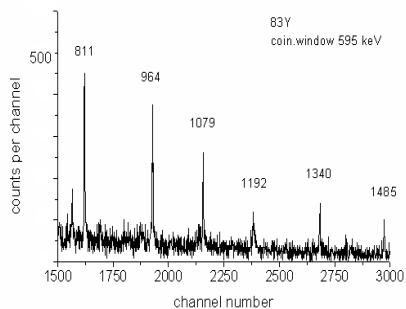


FIG. 1. ^{86}Zr energy levels observed in the $^{12}\text{C}(^{77}\text{Se}, 3n)^{86}\text{Zr}$ reaction at 260 MeV. Transition energies are in keV. The transitions indicated by dotted lines were either doublets, contaminations or very weakly observed.

$g_{9/2}$ neutron alignment first
then followed by $g_{9/2}$ proton alignment

^{83}Y

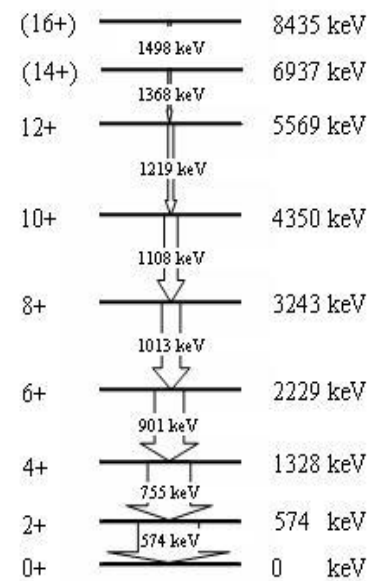
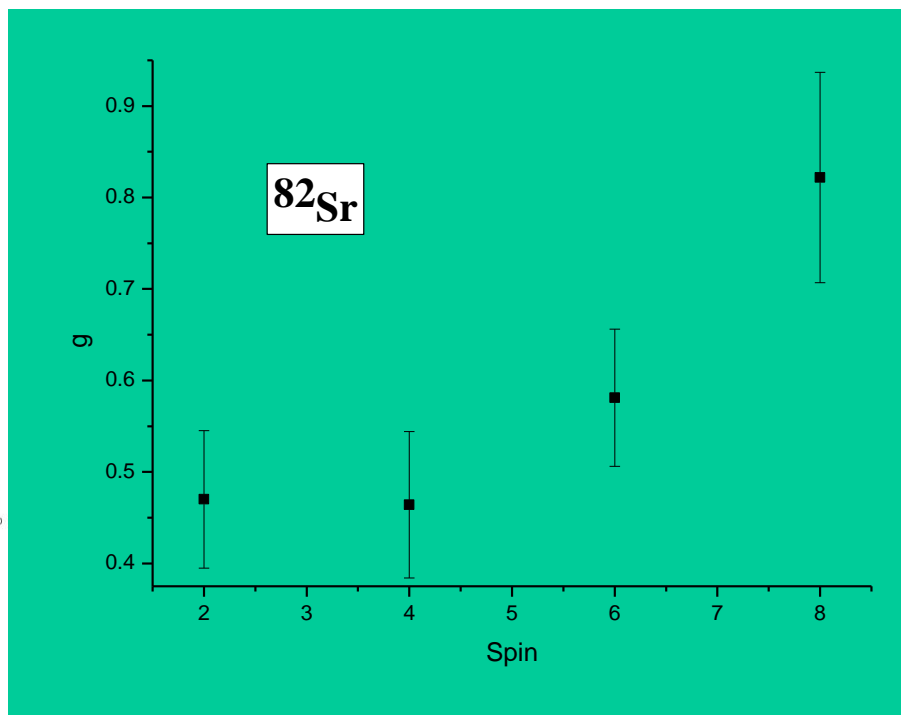
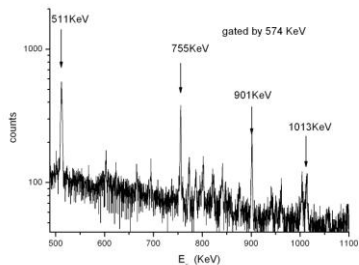


$^{83}\text{Y}_{9/2^+}$

$g_{9/2}$ proton alignment first

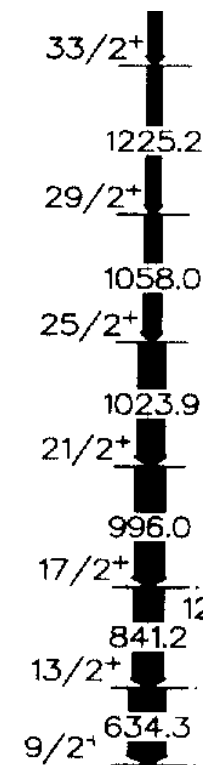
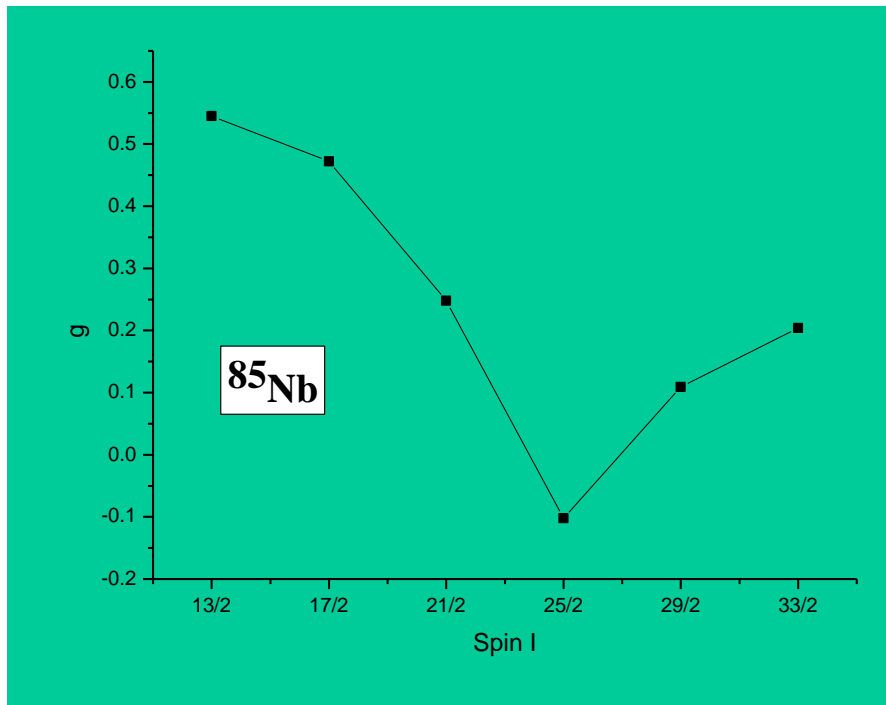
then followed by $g_{9/2}$ neutron alignment

^{82}Sr



$g_{9/2}$ proton alignment only

^{85}Nb



$g_{9/2}$ neutron alignment first

then followed by $g_{9/2}$ proton alignment

Rotor Plus three particle model

g-factor calculation

- **Empirical formula**

based on Cranking shell model

$$g(\omega) = g_g + (g_{jp} - g_g) \frac{i_p(\omega)}{I_x(\omega)} + (g_{jn} - g_g) \frac{i_n(\omega)}{I_x(\omega)}$$

$i_p(\omega)$: proton aligned angular momentum

$i_n(\omega)$: neutron aligned angular momentum

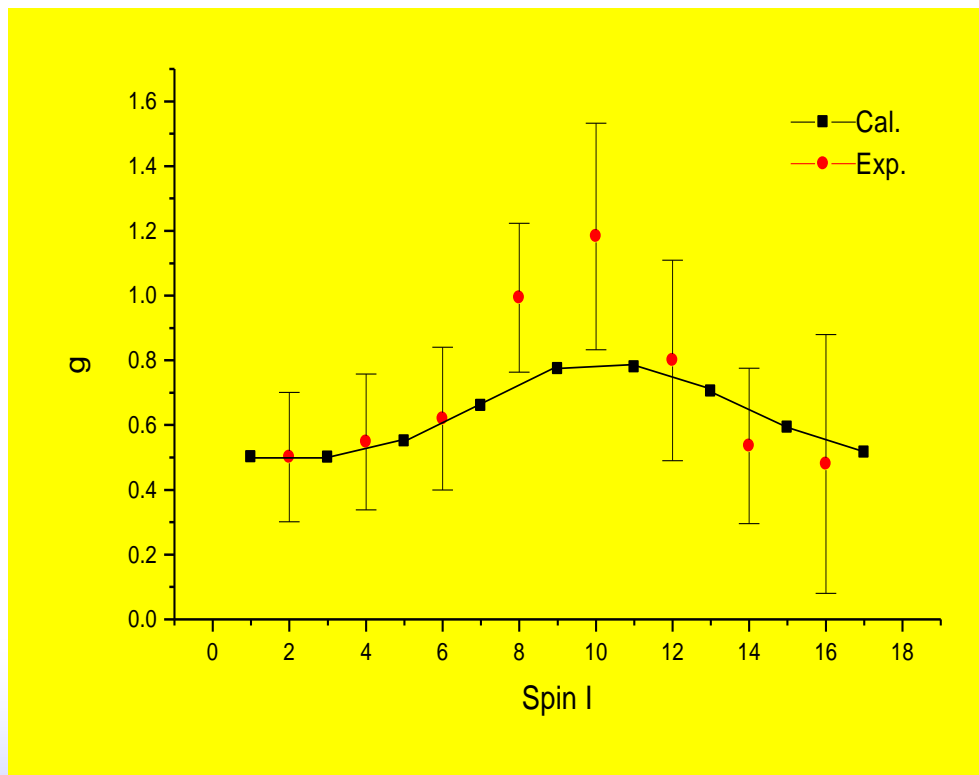
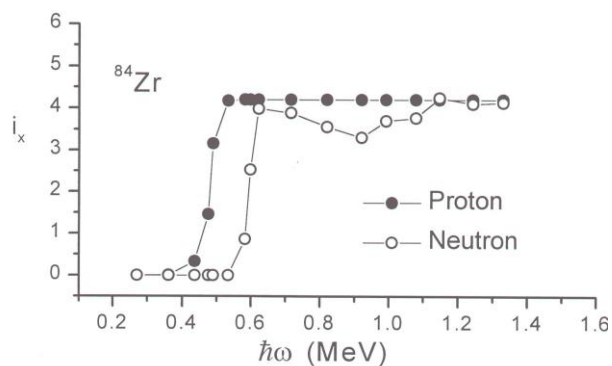
$I_x(\omega)$: total aligned angular momentum

g_{jp} : g-factors for the aligned protons

g_{jn} : g-factors for the aligned neutrons

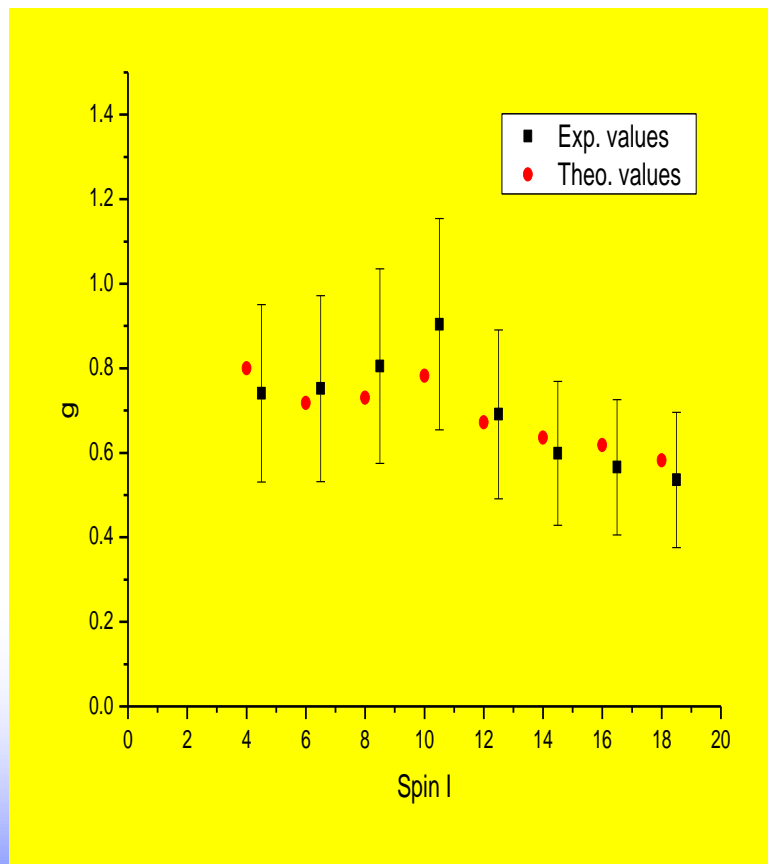
g_g : g-factor close to g_R ($\sim Z/A$)
for the collective rotation

Calculated and measured g-factors for ^{84}Zr



Due to soft to hard structure transition
 the calculated g-factors near the peak are lower

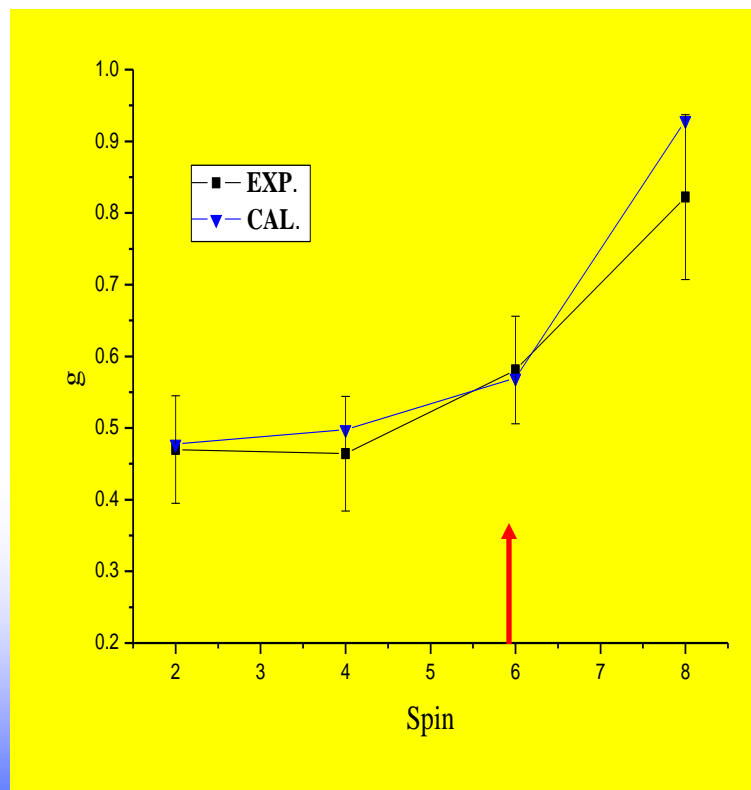
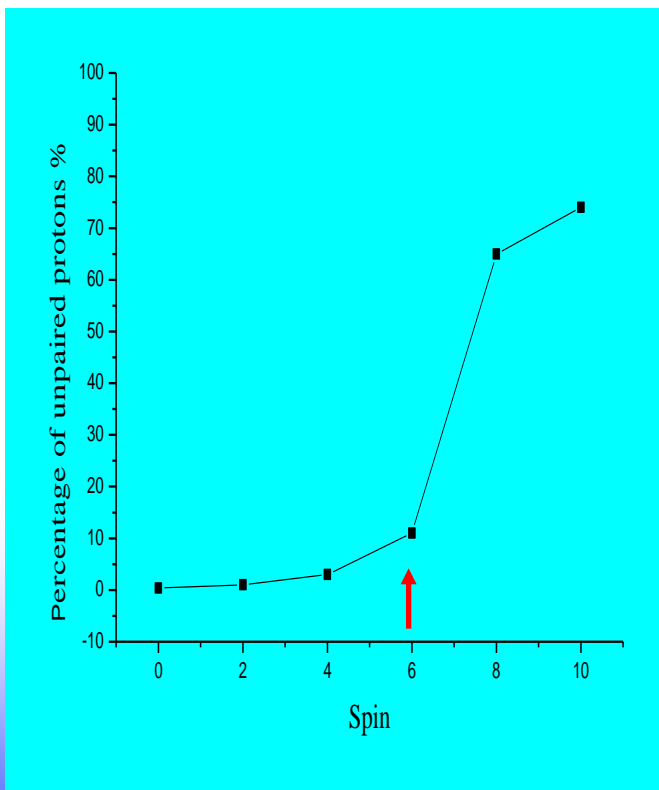
Calculated and measured g-factors for ^{83}Y



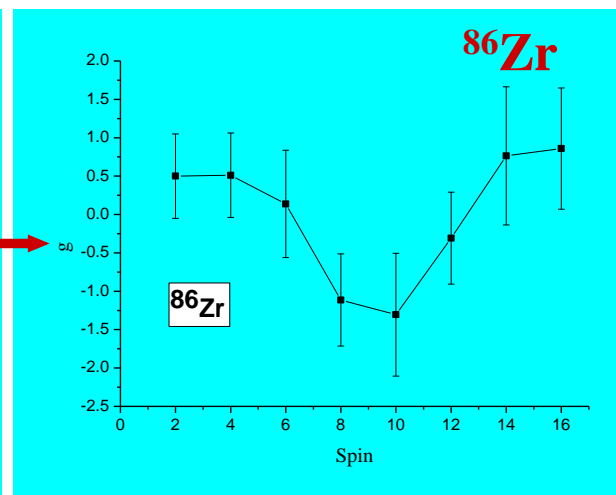
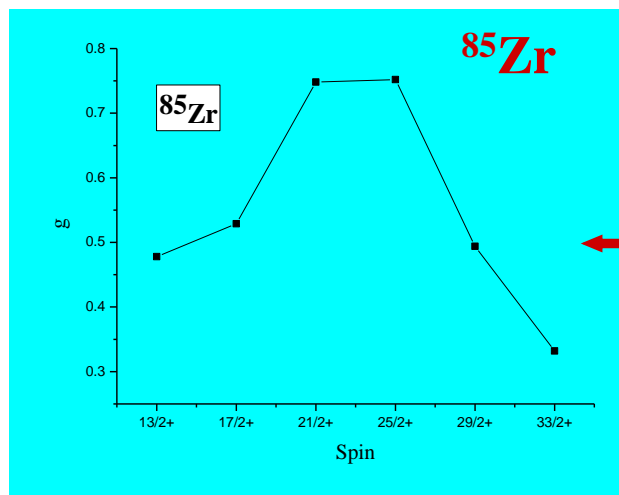
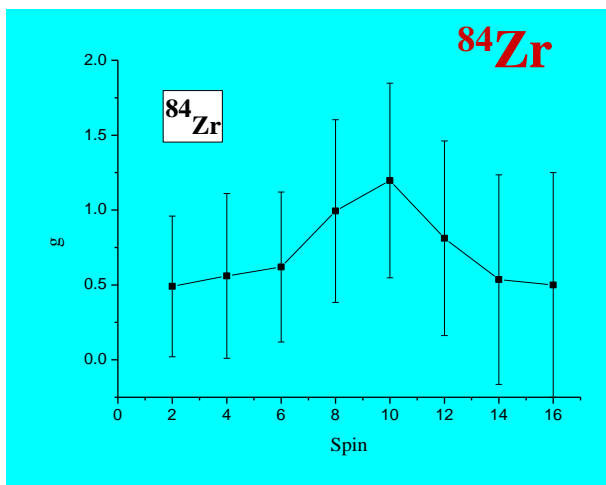
A rotor plus two-particle model (PRM) for ^{82}Sr

^{80}Kr even-even core as a rotor

two valence protons outside the core as two particles



- Dependence of QPA on neutron number
 $Z=40$: ^{84}Zr 、 ^{85}Zr 、 ^{86}Zr



N=44

Proton alignment
followed by neutron
alignment

N=45

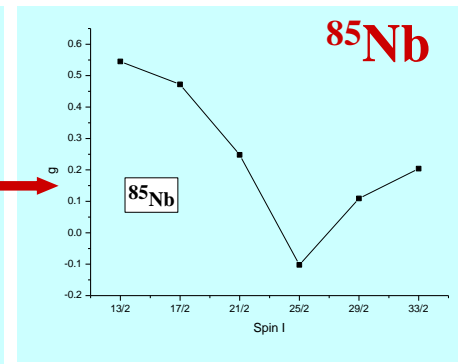
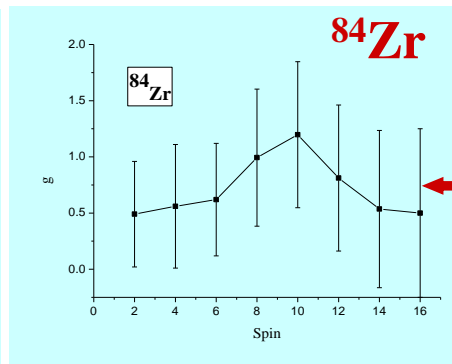
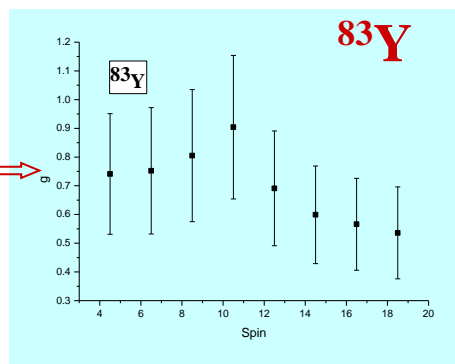
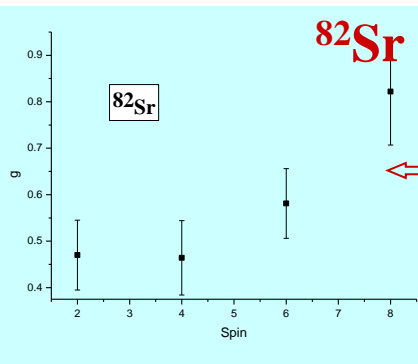
Proton alignment
followed by neutron
alignment

N=46

neutron alignment
followed by
proton alignment

• Dependence of QPA on proton number

$N=44$ $^{82}\text{Sr}(38)$ 、 $^{83}\text{Y}(39)$ 、 $^{84}\text{Zr}(40)$ 、 $^{85}\text{Nb}(41)$



Z=38

Proton alignment only

Z=39

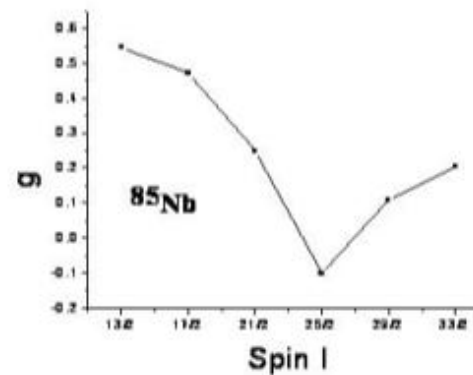
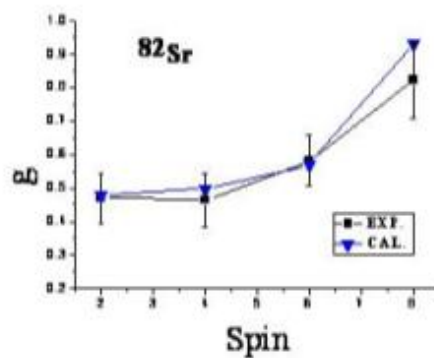
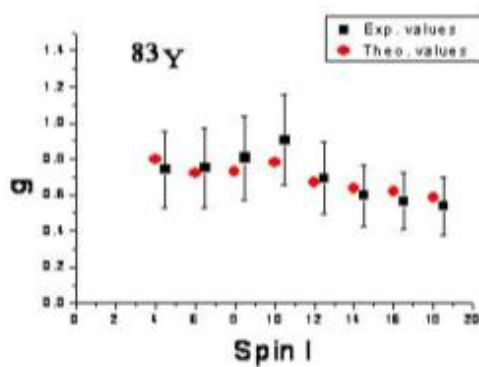
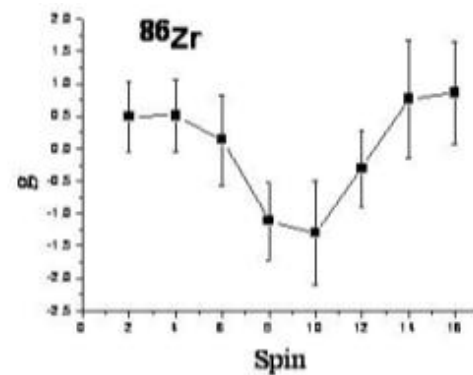
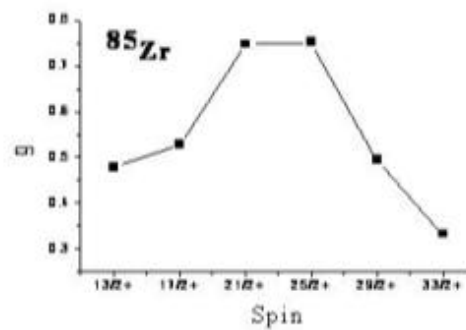
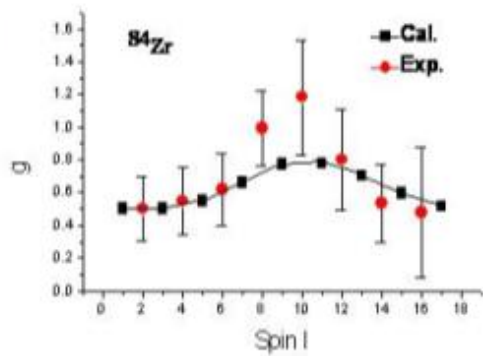
Proton alignment followed by neutron alignment

Z=40

Proton alignment followed by neutron alignment

Z=41

Neutron alignment followed by proton alignment



Summary of the results

**Quasi-particle alignments to large extent
depend on**

Spin

proton number

neutron number

**Quasi-particle alignments lead to
different patterns of variation of g factor
with spin**

4, Summary

- The g-factor is a good probe to study QPA
- The QPA was well investigated for ^{82}Sr , ^{83}Y , ^{84}Zr , ^{85}Nb , ^{85}Zr and ^{86}Zr through g-factor measurements
- The quasi-particle alignments lead to different patterns of variation of g factor with spin
- The alignments depend on the quasi-particle number
 - ① For the nuclides with $Z=40$ the proton alignment is followed by the neutron alignment in ^{84}Zr and ^{85}Zr , while the neutron alignment is followed by the proton alignment in ^{86}Zr
 - ② For the nuclides with $N=44$ the proton aligns only in ^{82}Sr , the proton aligns first and then the neutron starts to align at higher spins in ^{83}Y and ^{84}Zr and the neutron alignment is followed by the proton alignment in ^{85}Nb

Thank You !

