

Ist ECFA-CERN LHeC Workshop  
Divonne-les-Bains, September 2nd 2008

# From ep to AB collisions

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See the talks by G. Altarelli, S. J. Brodsky, J. Bartels, P. Newman, D.  
d'Enterria, F. Arleo,...

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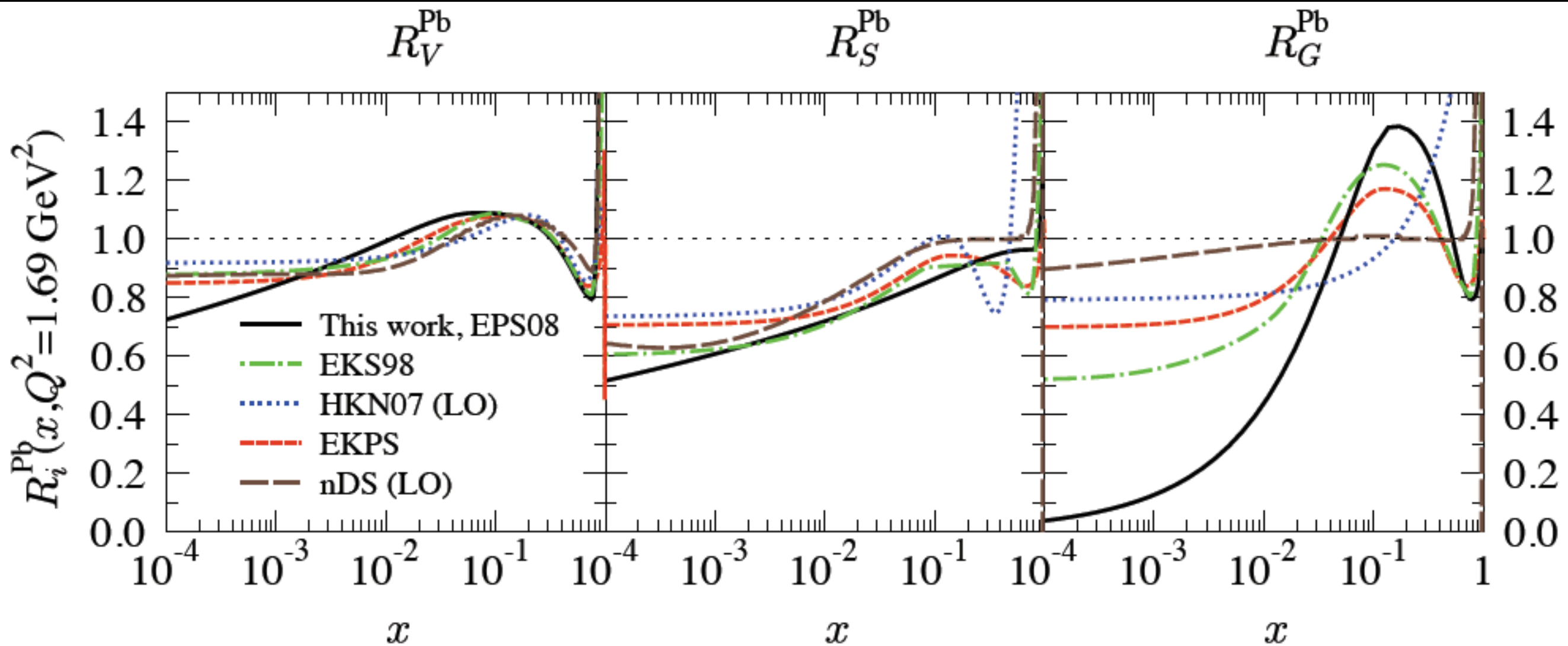
2.5. LHC.

## 3. Summary.

# I. Introduction (I):

⇒ **From ep to particle production in AB:** nucleon and nuclear pdf's plus factorization (collinear for large scales-DGLAP,  $k_T$ ? for intermediate scales-BFKL/BK?).  $E_{cm} \gg (\sim)Q \gg \Lambda_{QCD}$

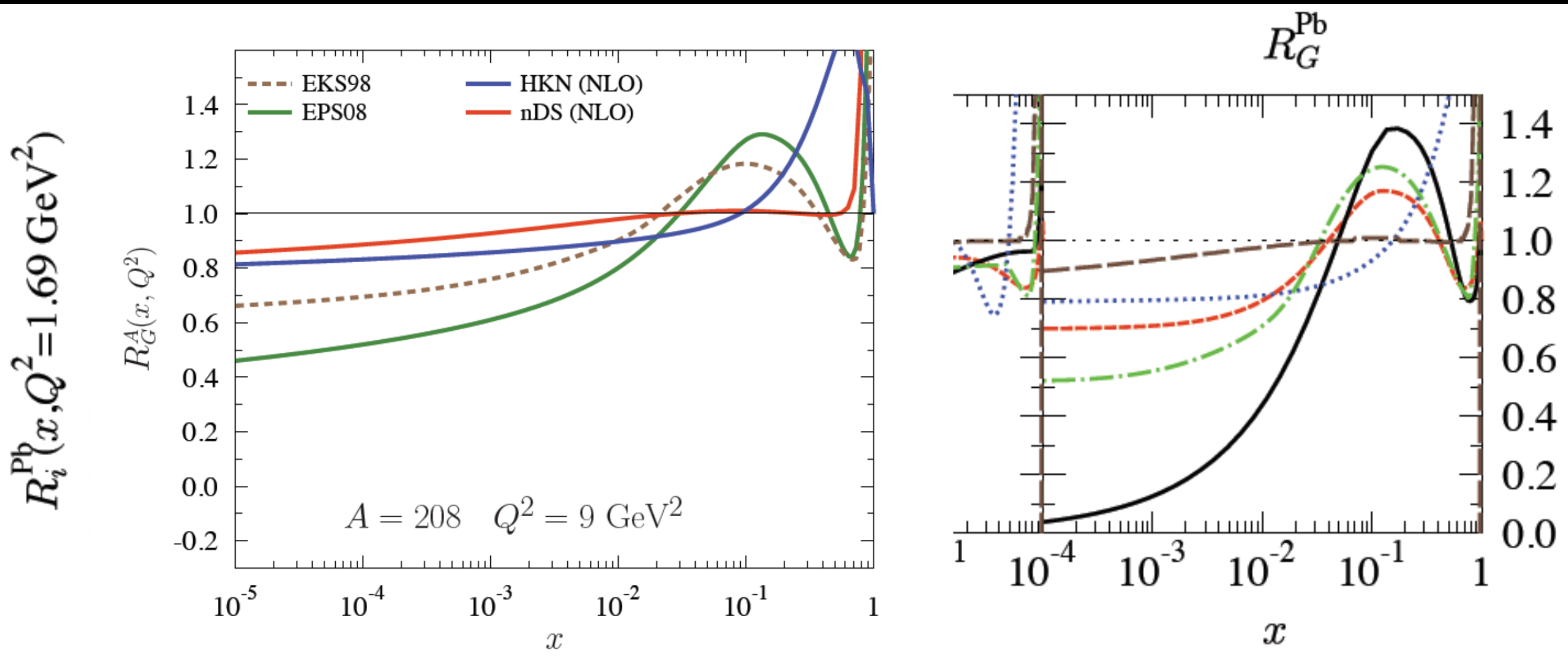
⇒ **Uncertainties in standard DGLAP npdf's are huge at small  $x$  and small  $Q^2$  for gluons: few/no data available.**



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From eA to AA at RHIC and the LHC.

# I. Introduction (II):

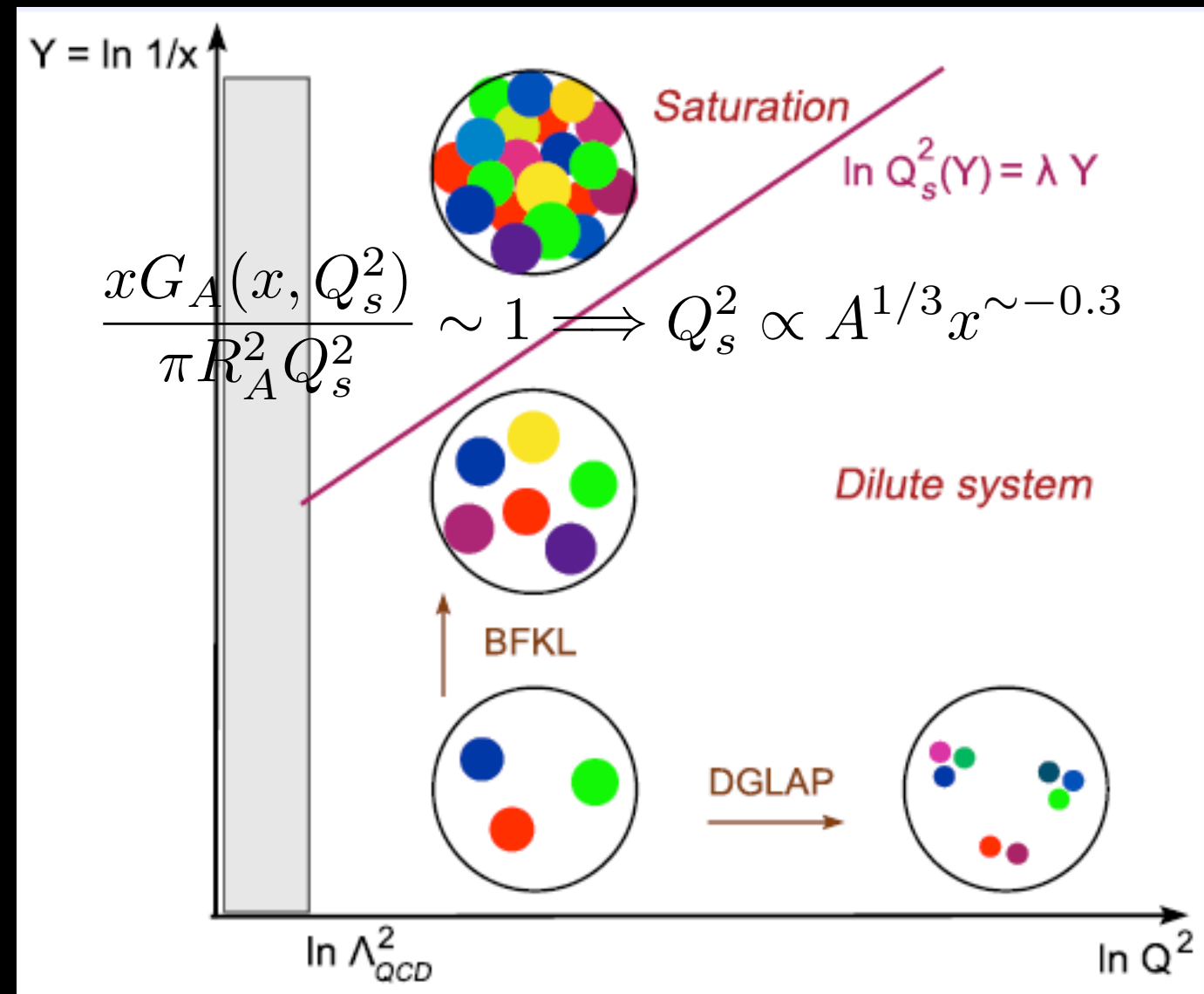
⇒ **Saturation physics**: framework to discuss ep and eA, and bulk production in pA and AB.

⇒ At **small enough x**, the **CGC** offers a description of the hadron WFs. The x-evolution equation is **Balitsky-Kovchegov** (LO, NLO).

$$x \leq \frac{1}{2m_N R_A} \sim 0.1 A^{-1/3}$$

⇒ **Our aims: understanding** Unitarity in a QFT; The behavior of QCD at large energies; **The initial conditions in HIC.**

⇒ **(No)  $k_T$ -like factorization in pA (AB)** (Gelis, Venugopalan,...) with BK (?): use geometric scaling to discuss the way from ep to AB.



# 2. Phenomenology:

2.1. ep.

2.2 eA.

2.3. pA at RHIC.

2.4. AA at RHIC.

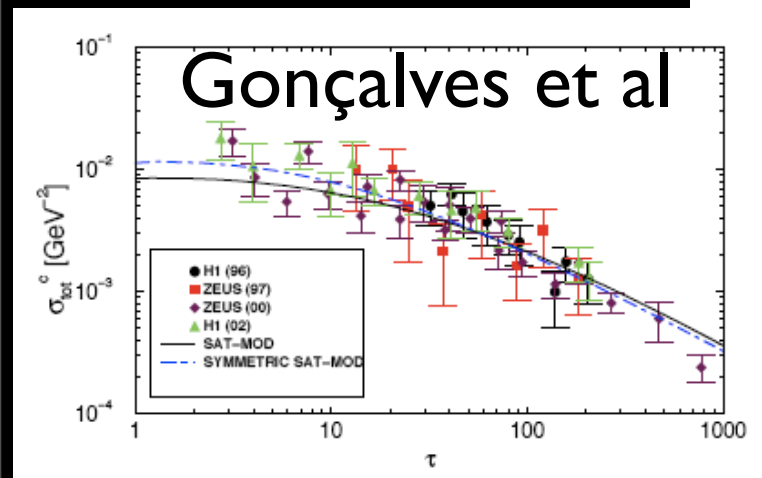
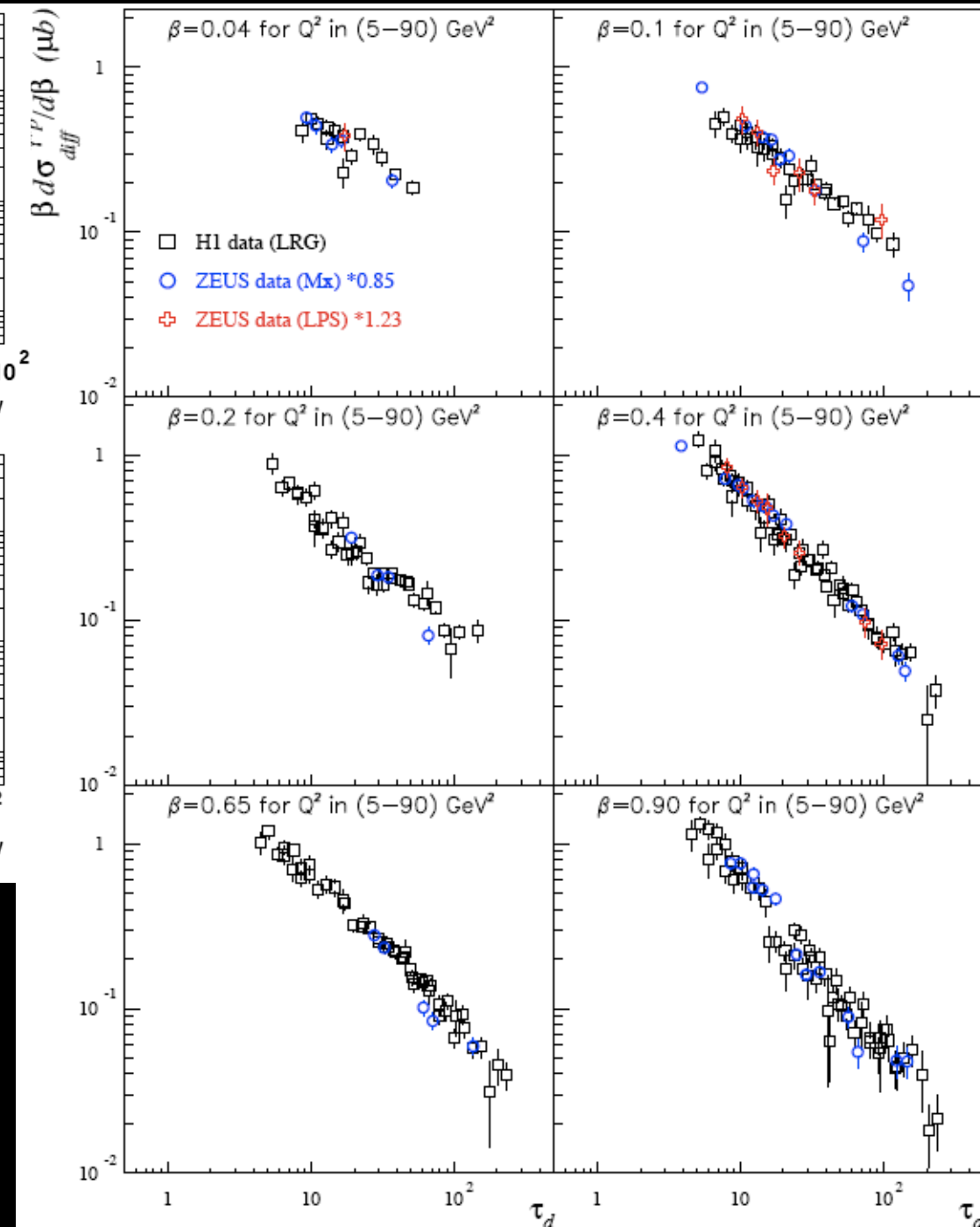
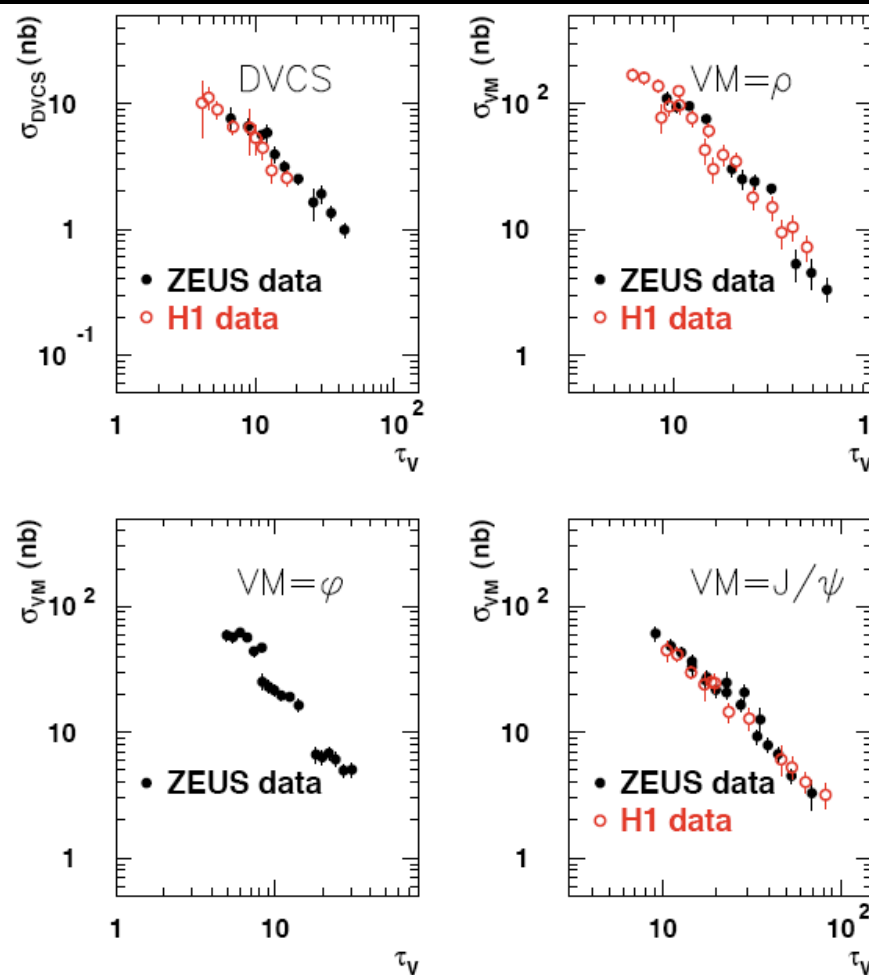
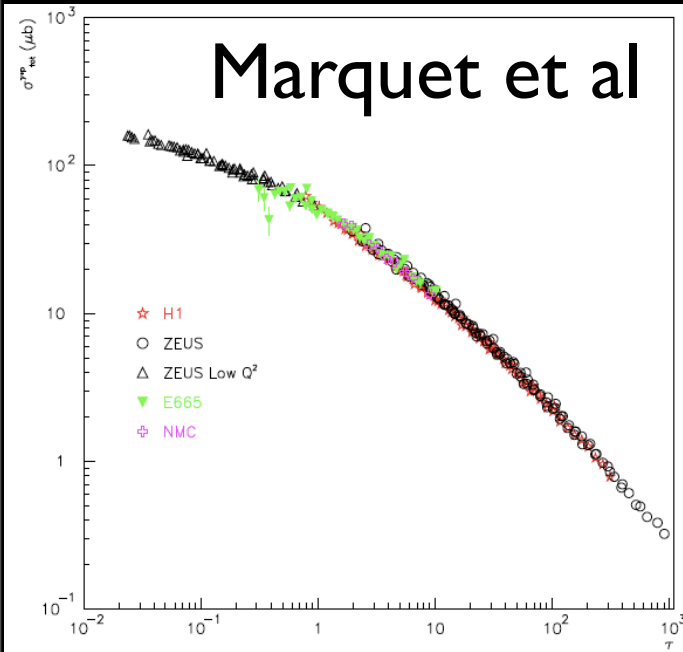
2.5. LHC (arXiv:0711.0974, now in JPG).

See the talk by J. L. Albacete at Hard Probes 2008.

# 2.1.ep:

⇒ The key feature of data is **geometric scaling** (Golec-Biernat et al).

$$\tau = \frac{Q^2}{Q_s^2(x)}, \quad \tau_D = \frac{Q^2}{Q_s^2(x_P)} \quad \text{at fixed } \beta, \quad \tau_V = \frac{Q^2 + M_V^2}{Q_s^2(x_P)}$$



$$Q_s^2(x) = \left(\frac{x_0}{x}\right)^\lambda$$

$$\lambda_{(GBW)} \sim 0.25 \div 0.3$$

# 2.2. eA:

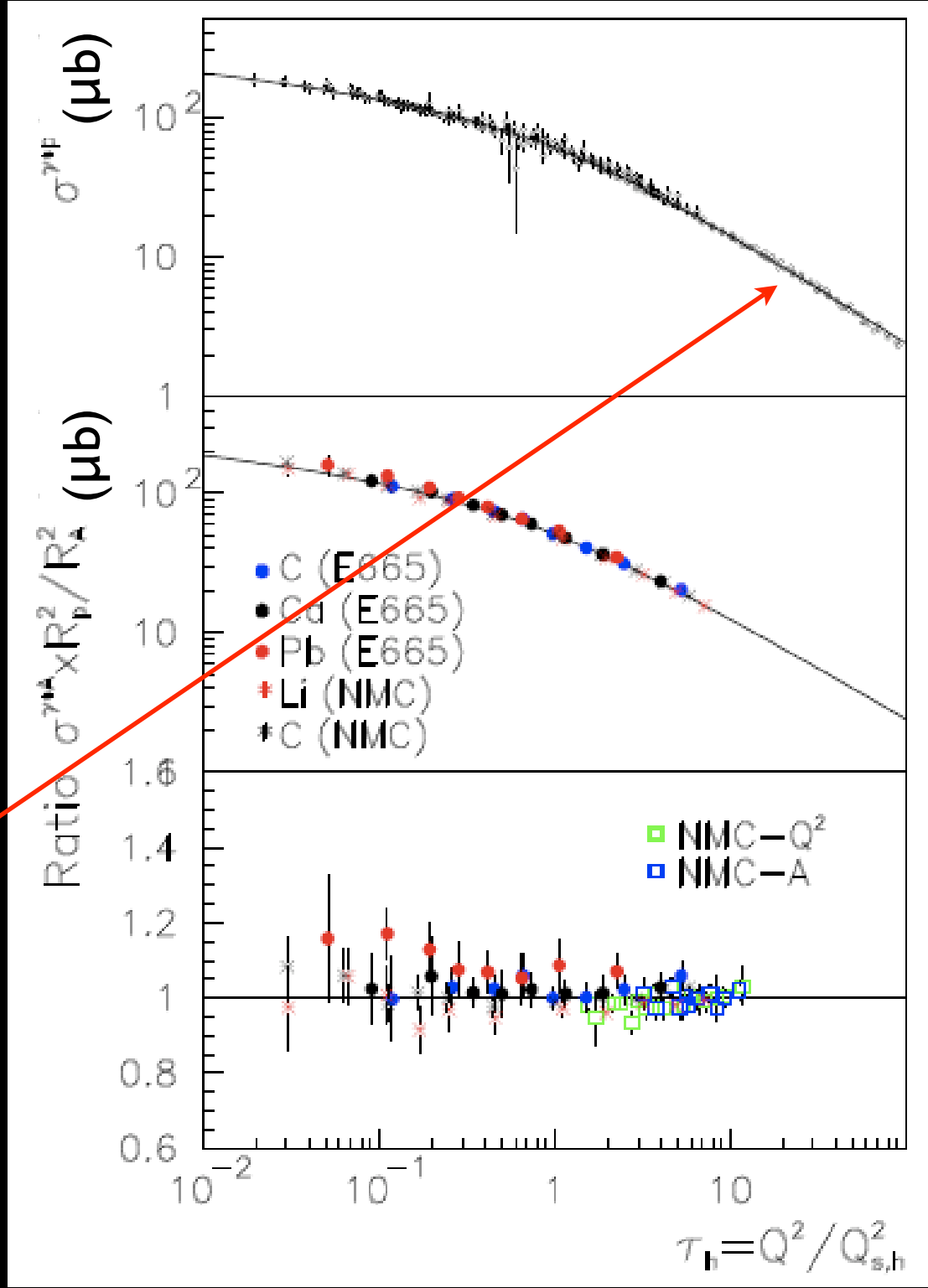
⇒ Geometric scaling also found in eA  
(Rummukainen et al, NA et al).

$$\frac{\sigma^{\gamma^* A}(\tau_A)}{\pi R_A^2} = \frac{\sigma^{\gamma^* P}(\tau_A)}{\pi R_p^2}$$

$$\frac{Q_{s,A}^2}{Q_{s,P}^2} = \left( \frac{A\pi R_p^2}{\pi R_A^2} \right)^{\frac{1}{\delta}} \Rightarrow \frac{\tau_A}{\tau_p} = \left( \frac{\pi R_A^2}{A\pi R_p^2} \right)^{\frac{1}{\delta}}$$

$\delta = 0.79 \pm 0.02$  ( $x < 0.02$ ).

BK/data	$\lambda$	$\delta$	$\gamma$
Data	0.25-0.3	$\leq 1$	0.75
fc	$4.88\alpha_s$	i.c.	0.63
rc	OK	small evol.	?





# 2.3. pA at RHIC (I):

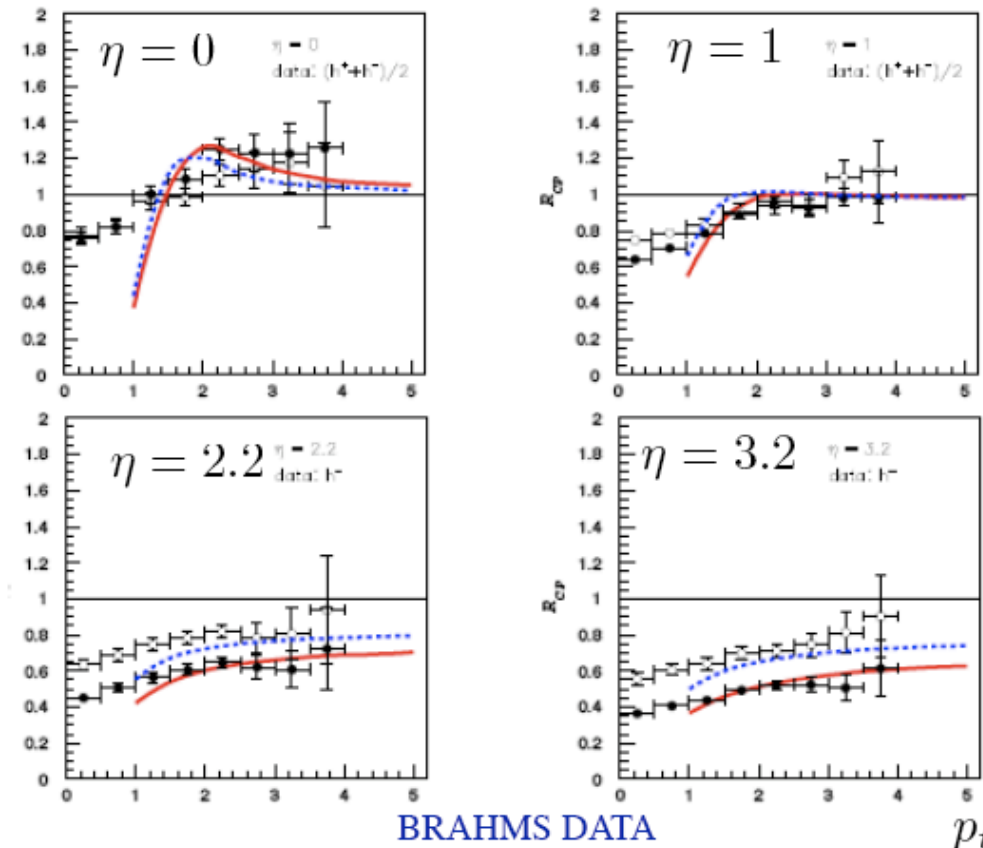
⇒ **Control experiment for initial state effects in AA:** Cronin effect in dAu at midrapidity ruled out initial state effects as the explanation for the suppression observed in AA.

⇒ **Suppression at forward rapidities was predicted by small-x evolution (BK).**

$$R_{dAu} = \frac{\frac{dN^{dAu}}{d\eta d^2bd^2p}}{N_{coll} \frac{dN^{pp}}{d\eta d^2bd^2p}}$$

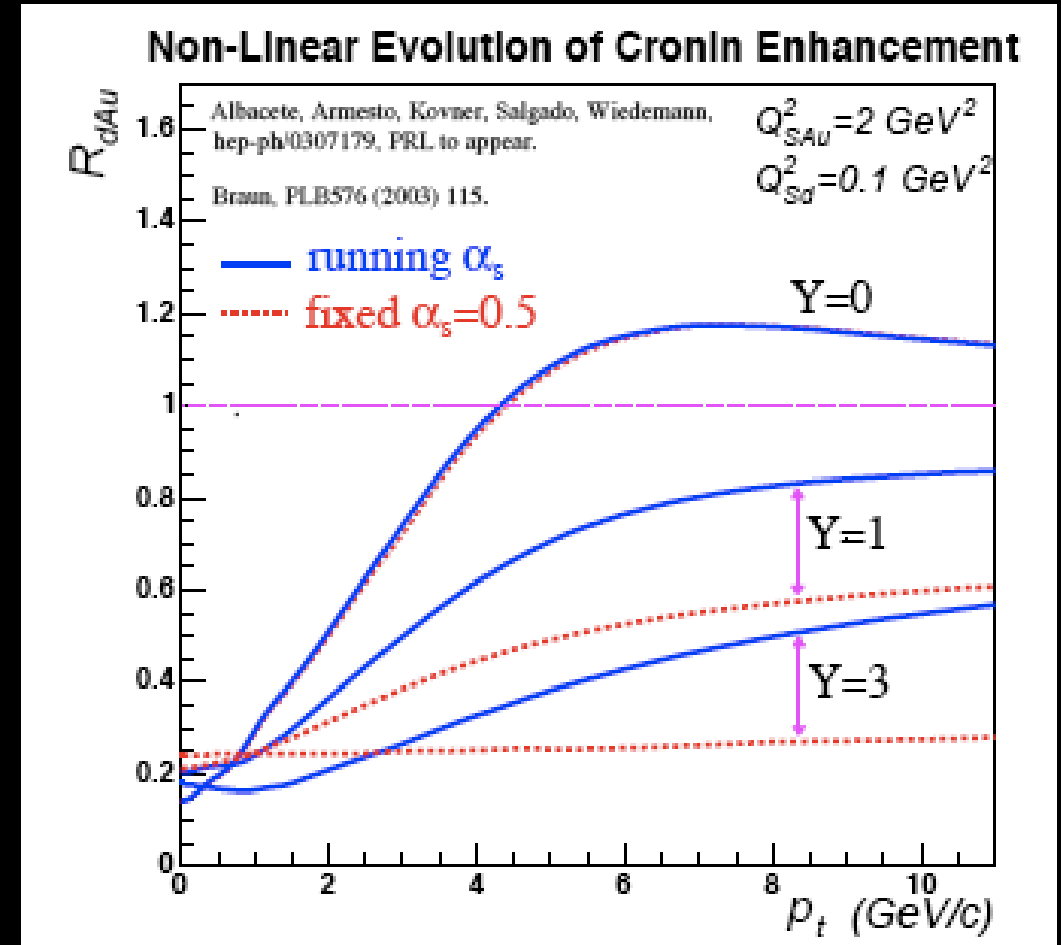
JLA-Armesto-Kovner-Salgado-Wiedemann  
Kharzeev-Kovchegov-Tuchin

$R_{CP}$



BRAHMS DATA

$p_t$

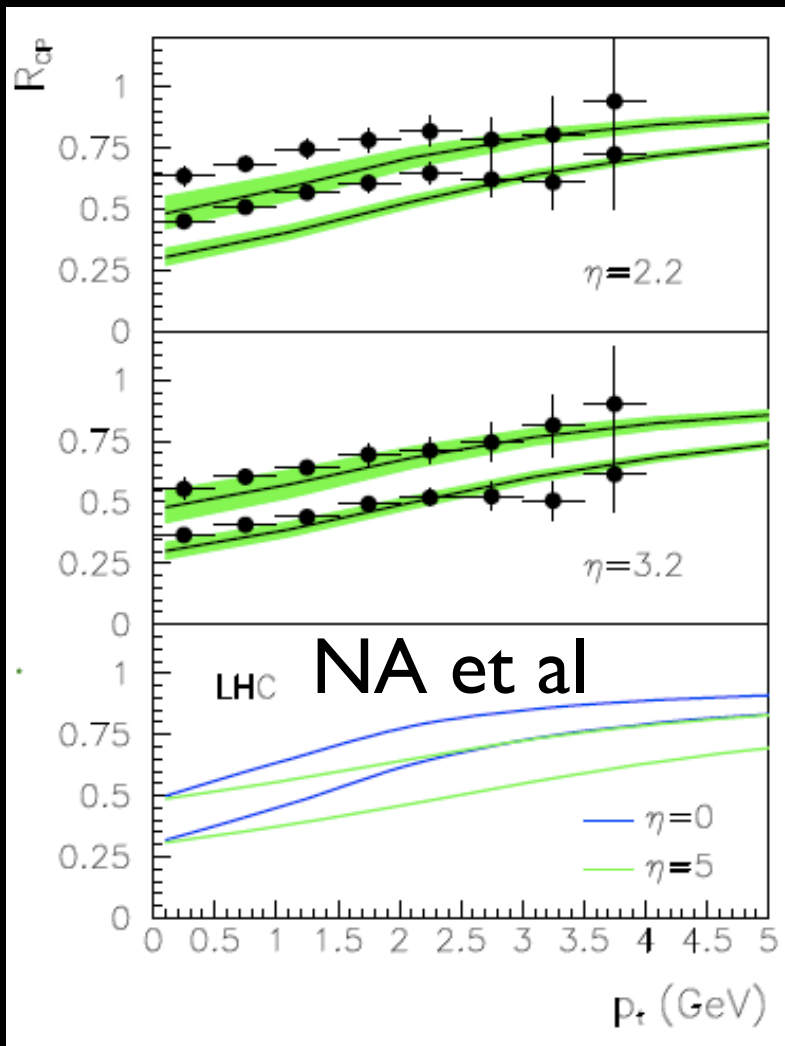
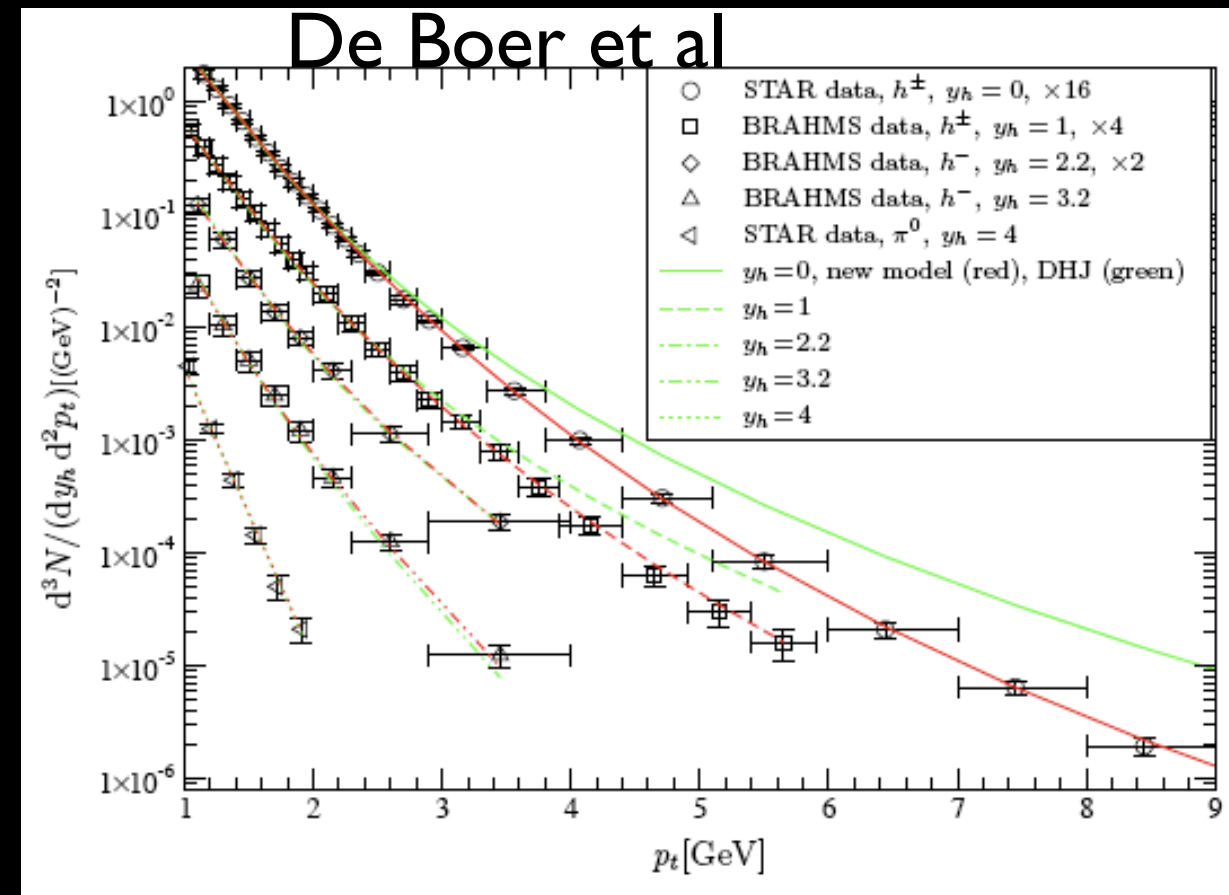


$$R_{dAu} \xrightarrow{y \rightarrow \infty} A^{-(1-\gamma/\delta)/3} (fc)$$

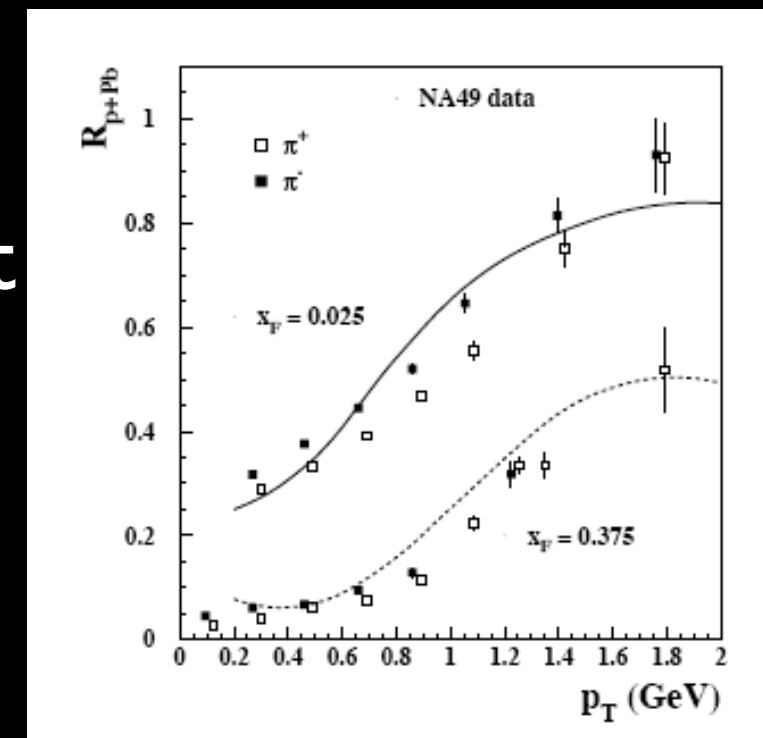
Kharzeev et al, Baier et al.

# 2.3. pA at RHIC (II):

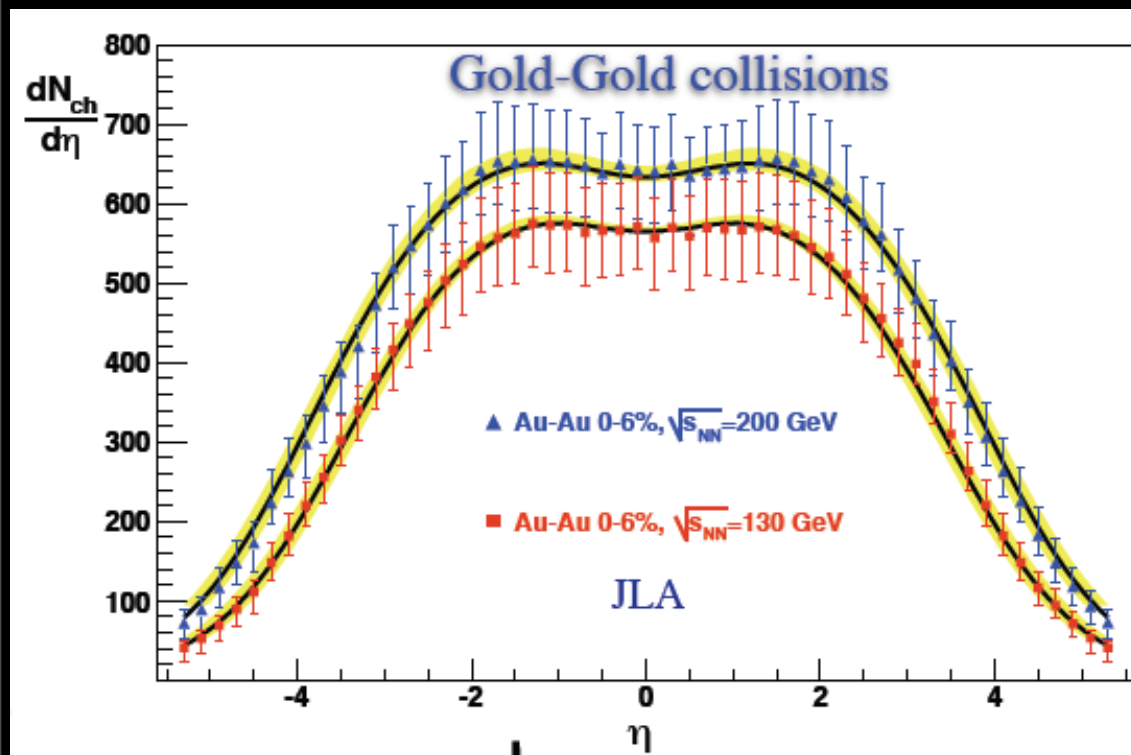
⇒ This suppression is **compatible with ugd+factorization**: ugd's in agreement with  $ep + A^{1/3}$  prescription for  $Q_s^2$ . It is also compatible with the ratio of geometric ep/eA scaling functions.



⇒ **Warning:**  $\langle x_A \rangle > 0.02$  (Guzey et al), and such suppression also happens at SPS/FNAL energies (Nemchik et al, Kopeliovich et al, Capella et al): finite energy corrections, e loss?



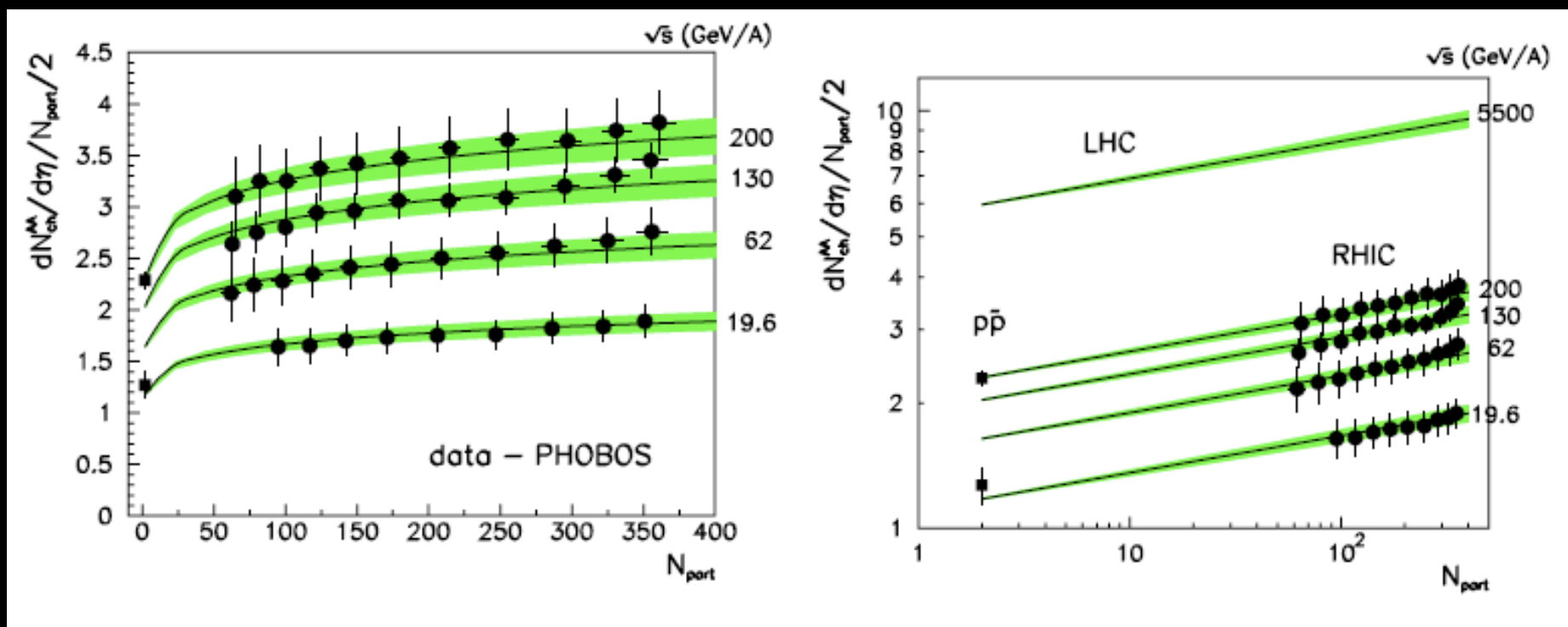
# 2.4. AA at RHIC (I):



⇒ Assuming **factorization**, multiplicities (evolution with centrality and pseudorapidity) can be computed.

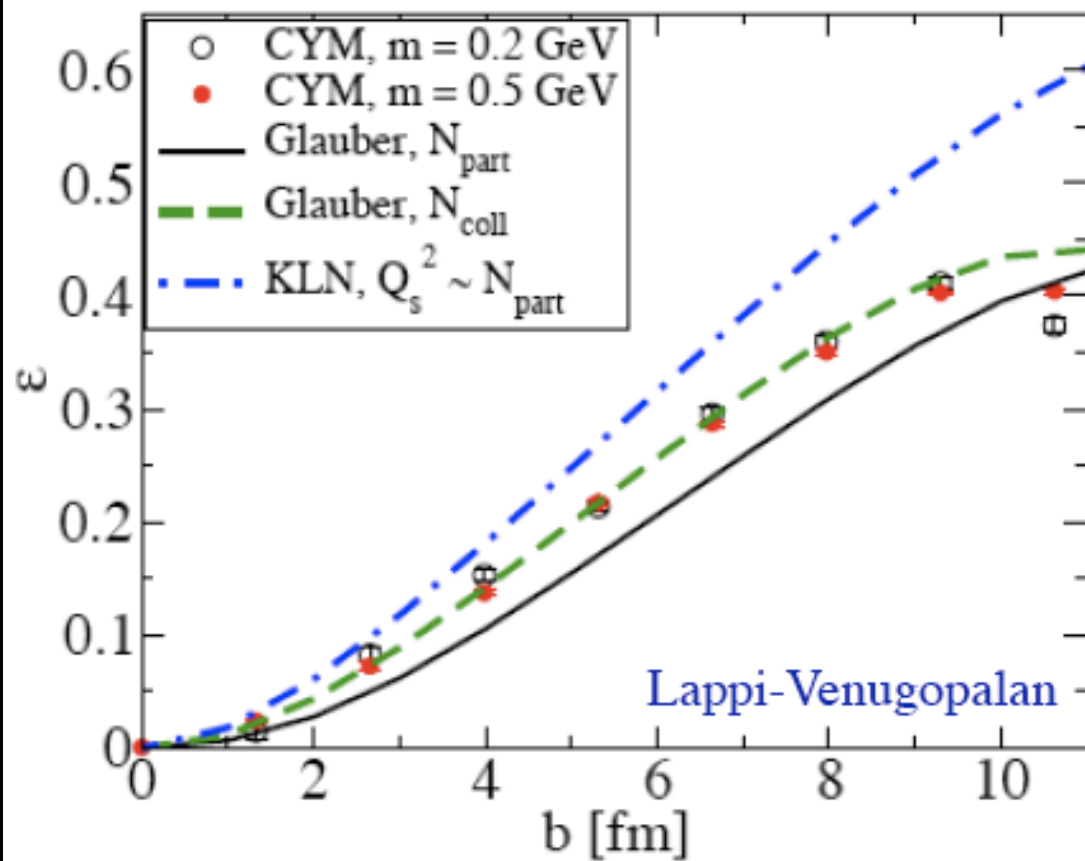
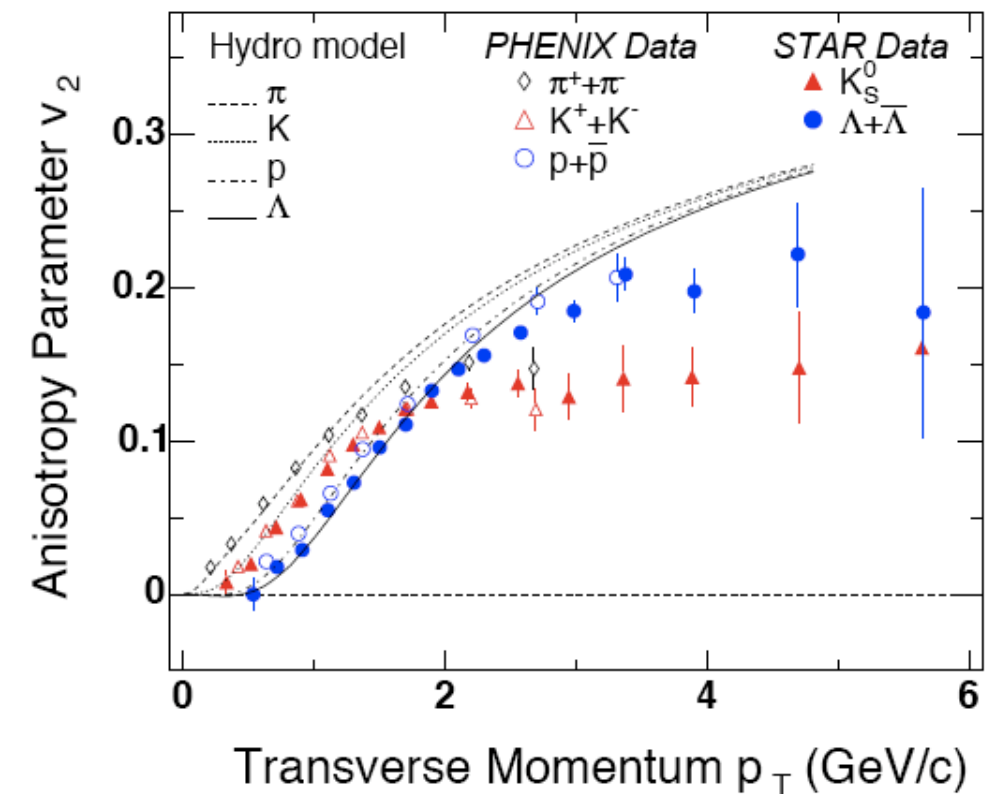
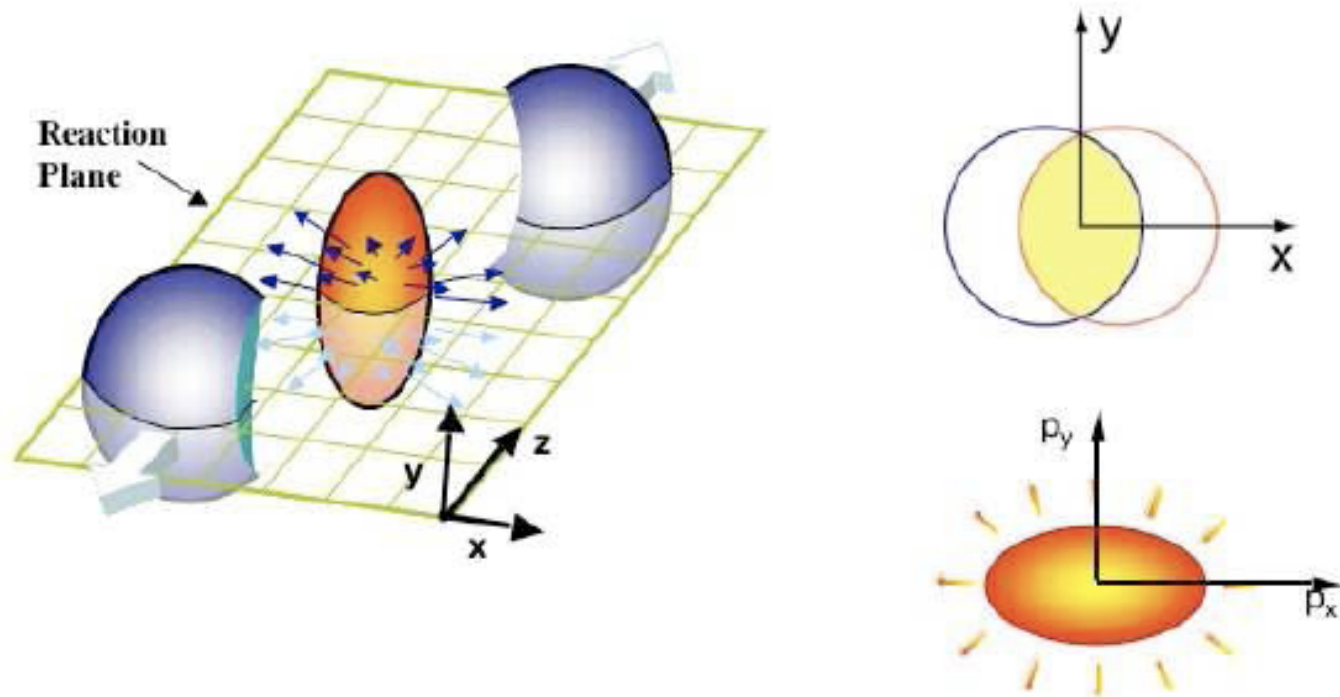
$$\frac{1}{N_{part}} \left. \frac{dN_{AA}^g}{d\eta} \right|_{\eta=0} \approx \begin{cases} \sqrt{s}^\lambda \ln(\sqrt{s}^\lambda N_{part}) & \text{Kharzeev-Levin Nardi} \\ \sqrt{s}^\lambda N_{part}^{\frac{1-\delta}{3\delta}} & \text{Armesto-Salgado Wiedemann} \end{cases}$$

⇒ Now it has been done with the available NLO-BK machinery (Albacete).



⇒ **Geometric scaling is enough:** factorization of geometry and energy dependences.

# 2.4.AA at RHIC (II):

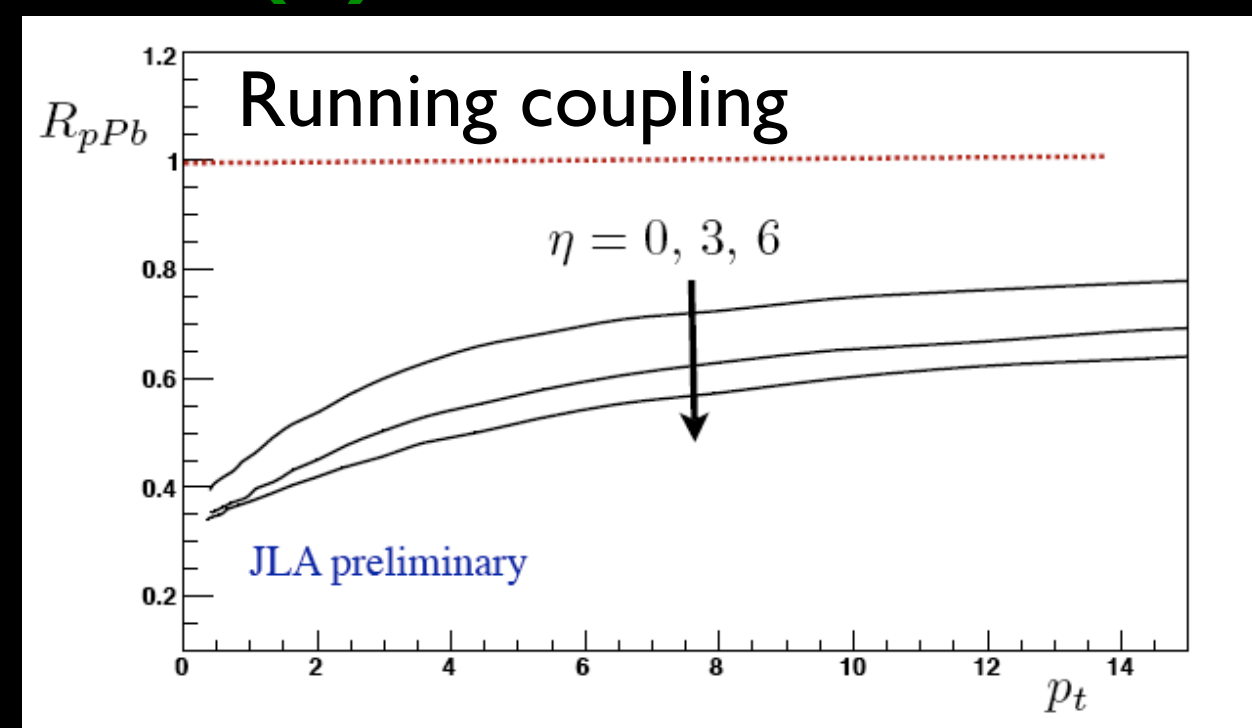
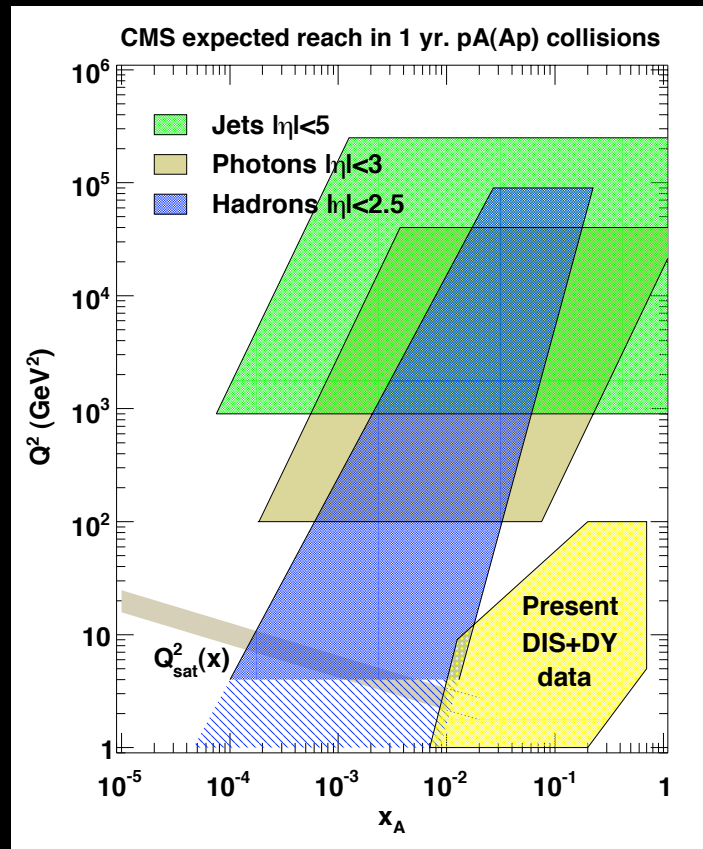
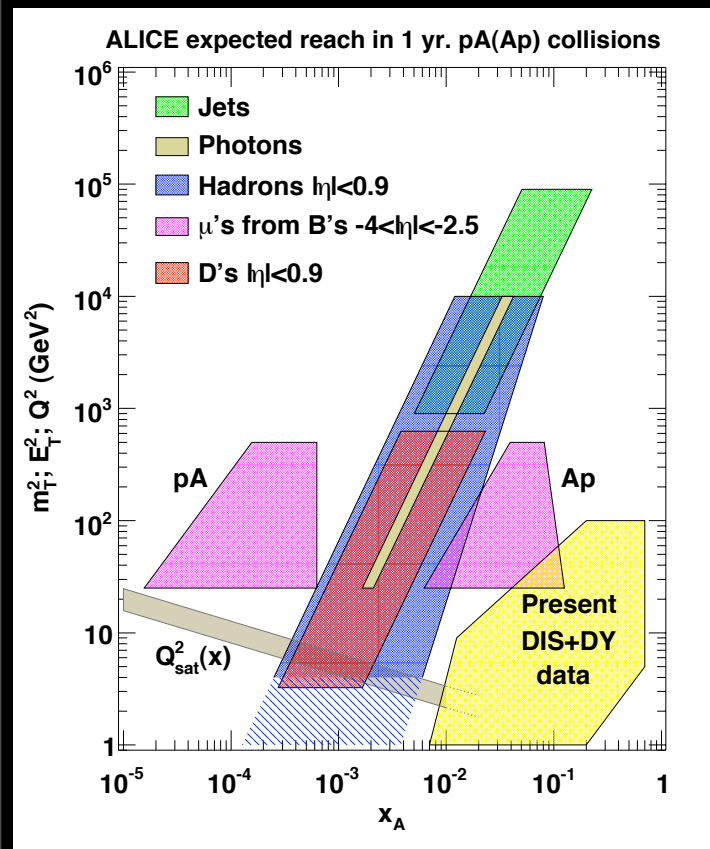


⇒ Initial conditions for hydrodynamical evolution are a key ingredient in those calculations. CGC gives larger eccentricity: room for viscosity or larger equilibration times.

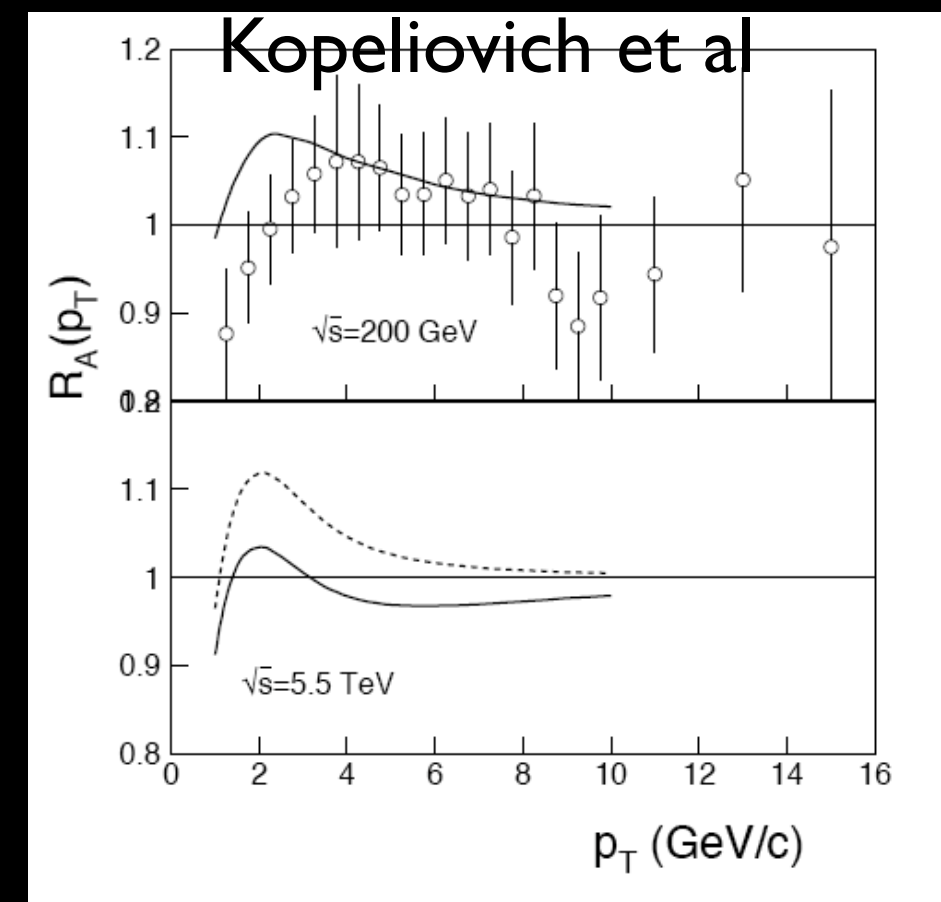
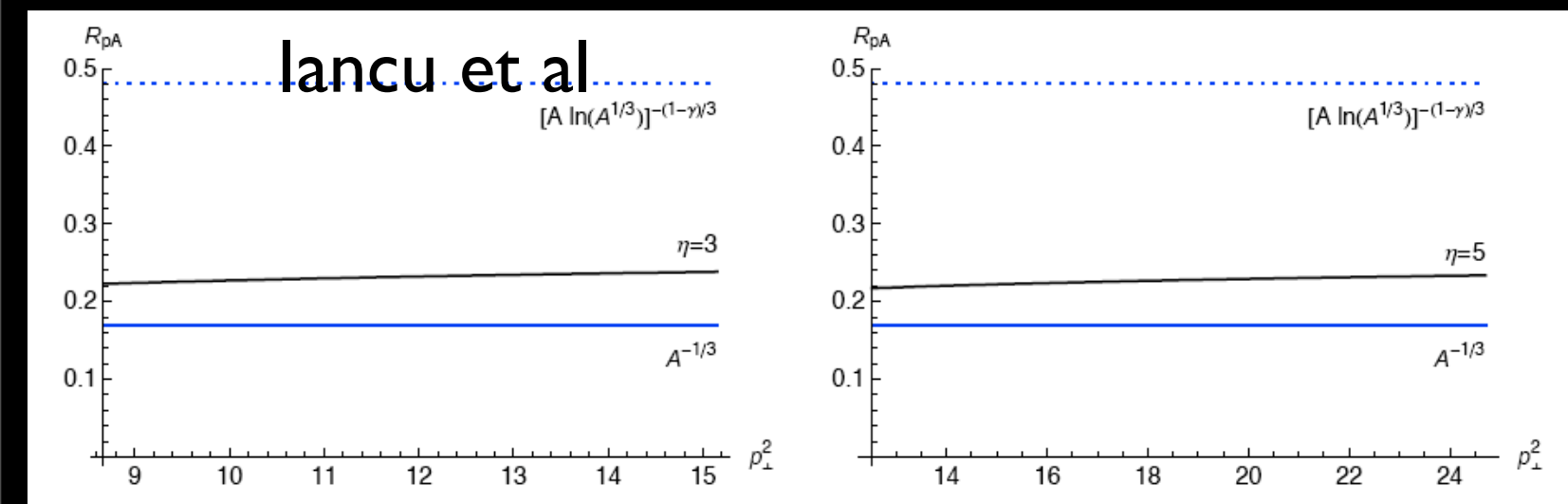
⇒ This initial conditions are not only needed in hydro: transport codes.



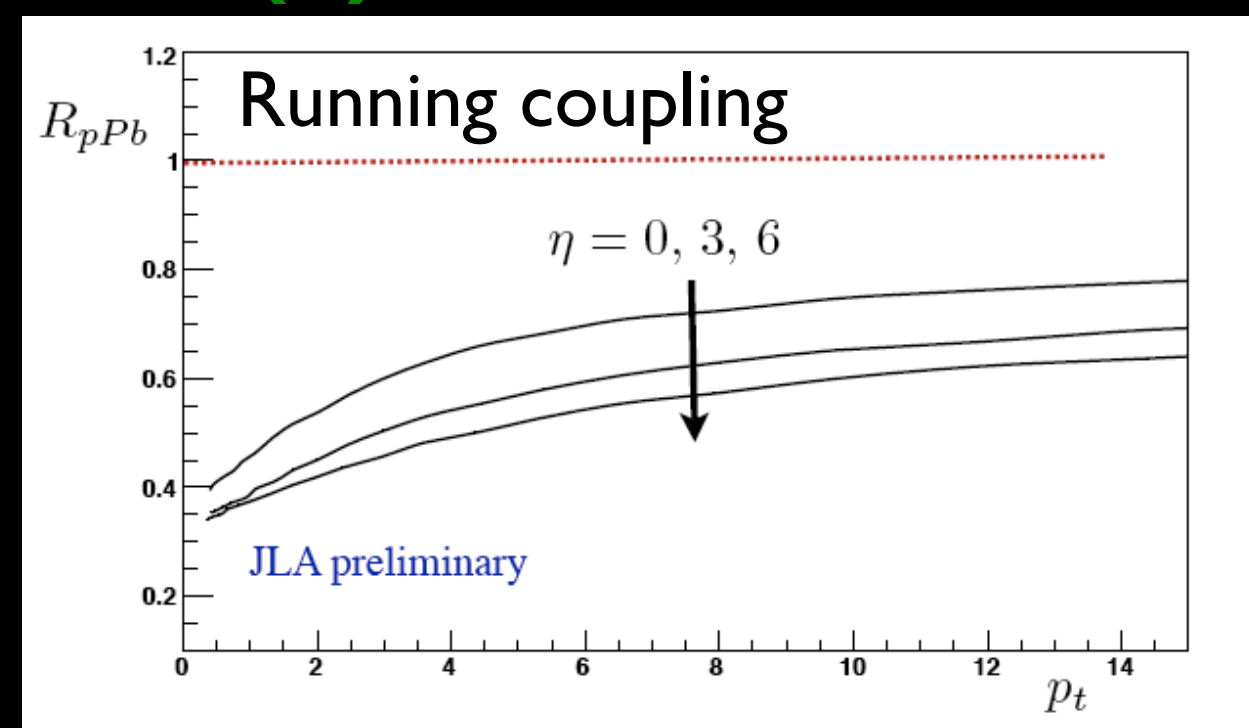
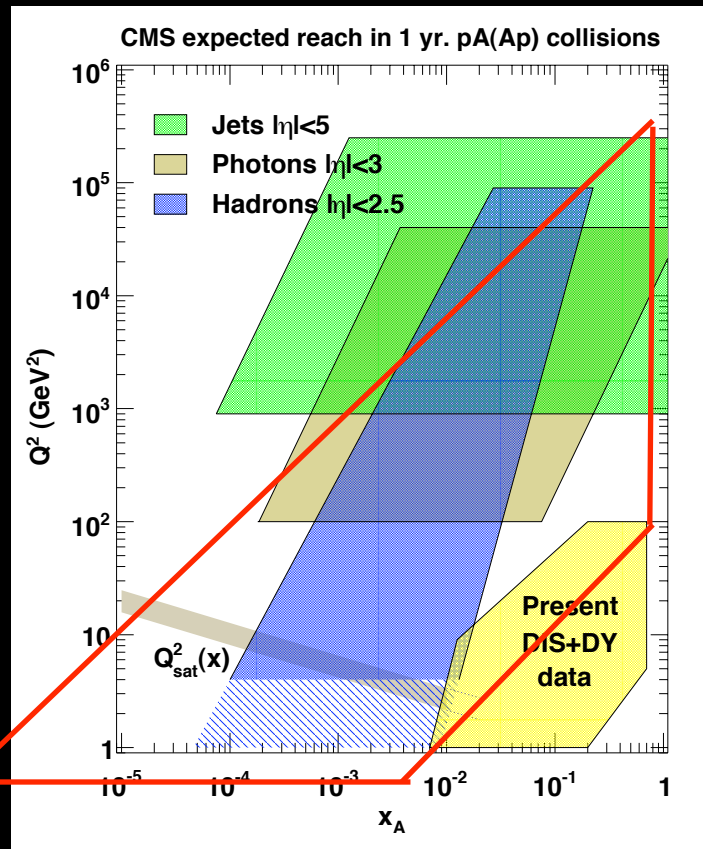
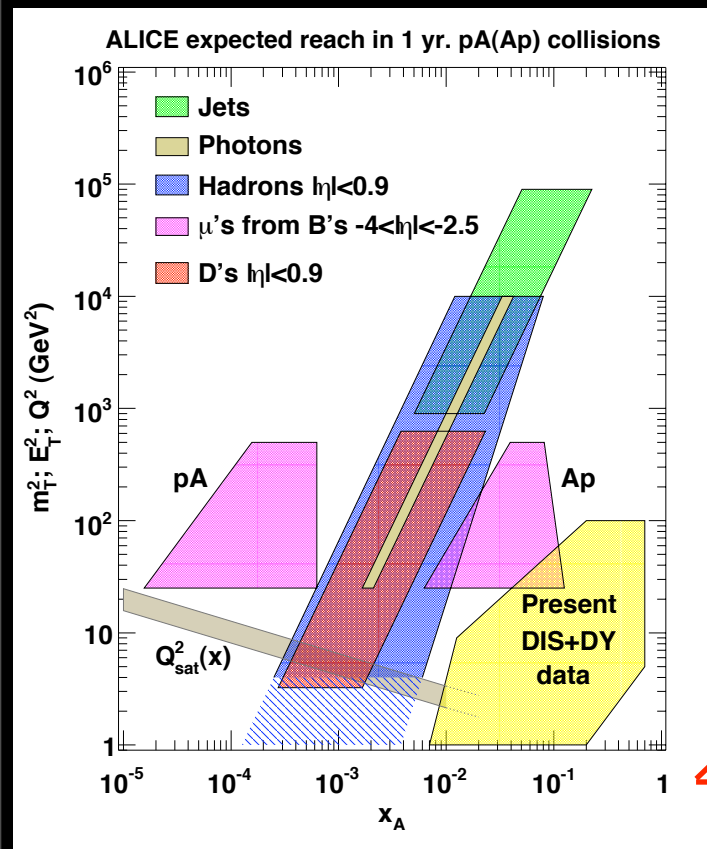
# 2.5. LHC (I):



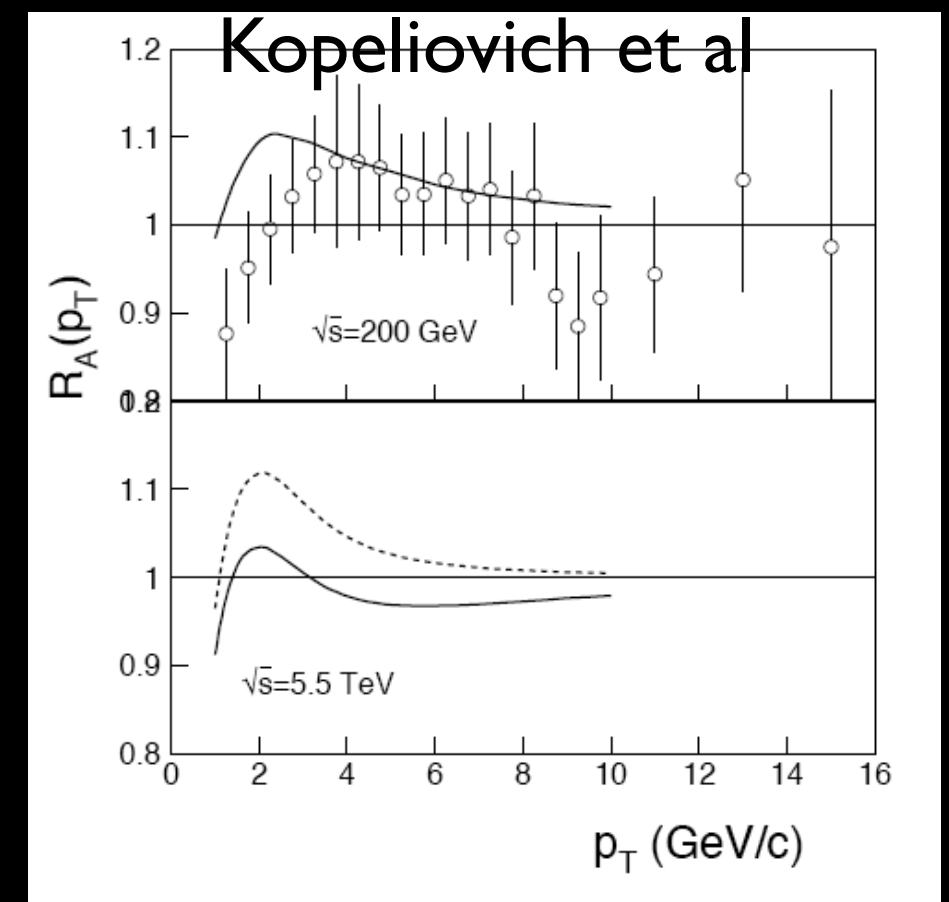
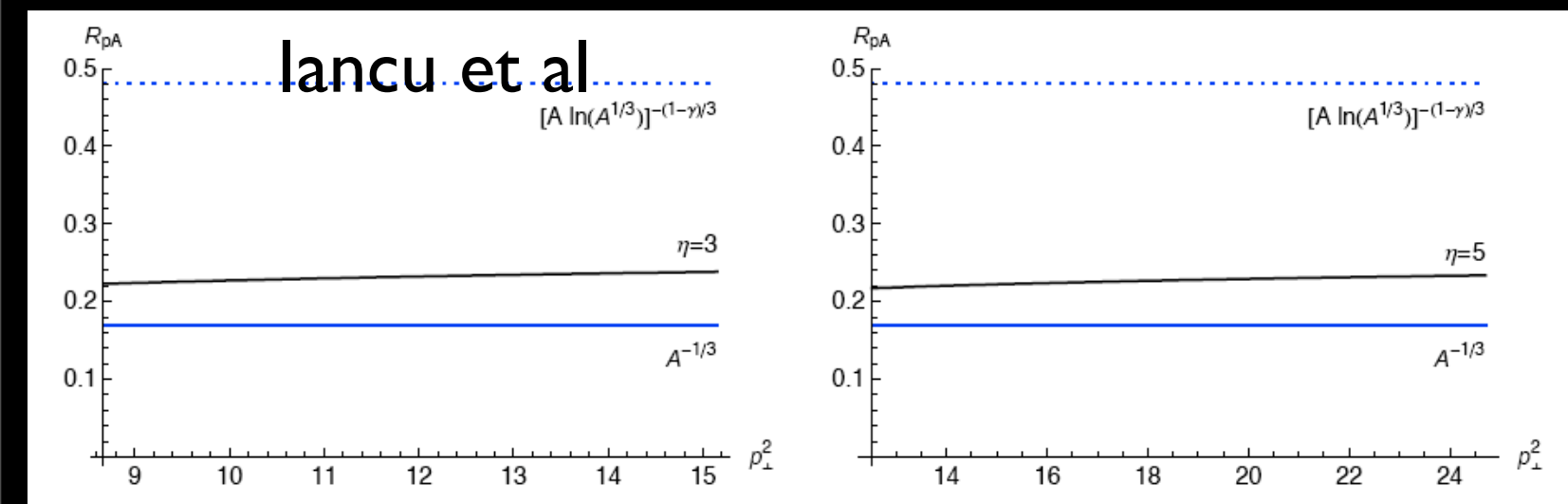
➡ pA (and UPC) at the LHC offer a huge kinematic coverage: testing ground.



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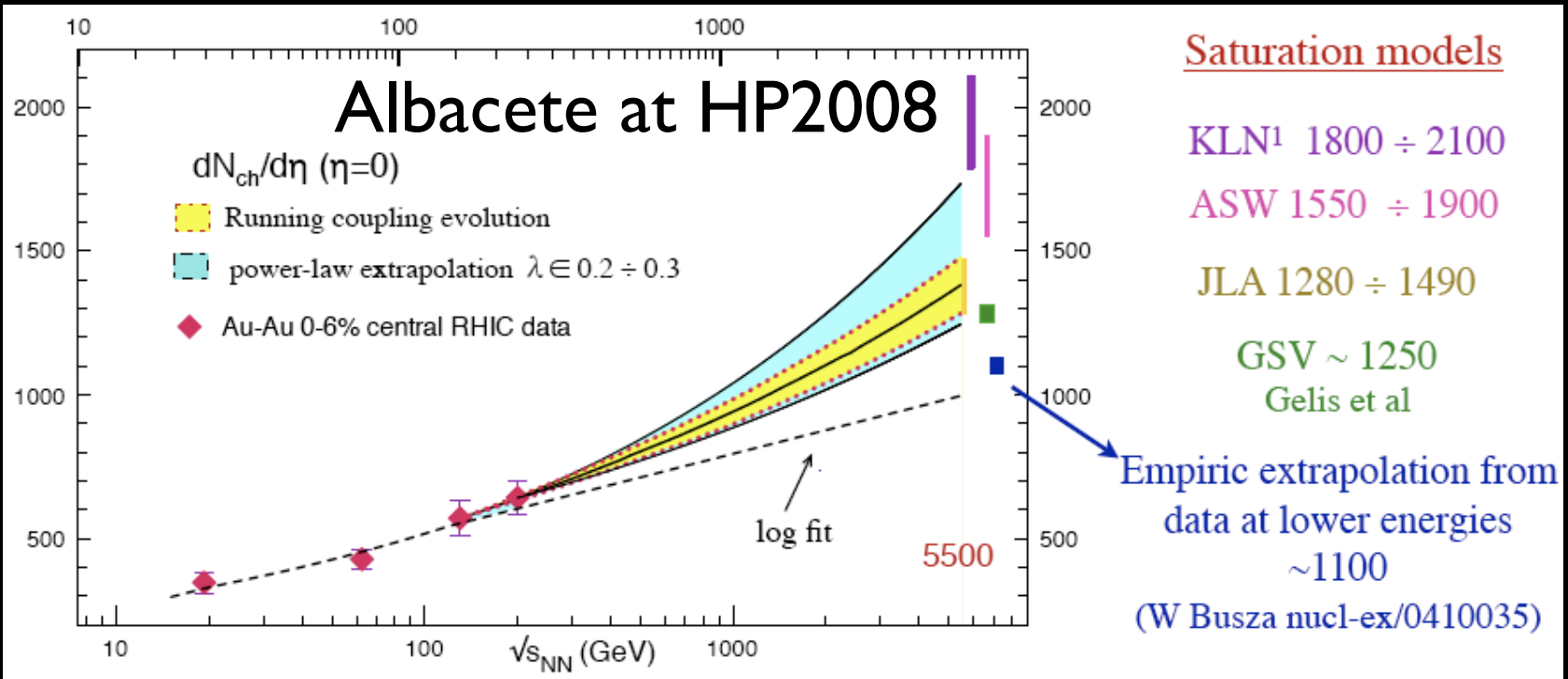


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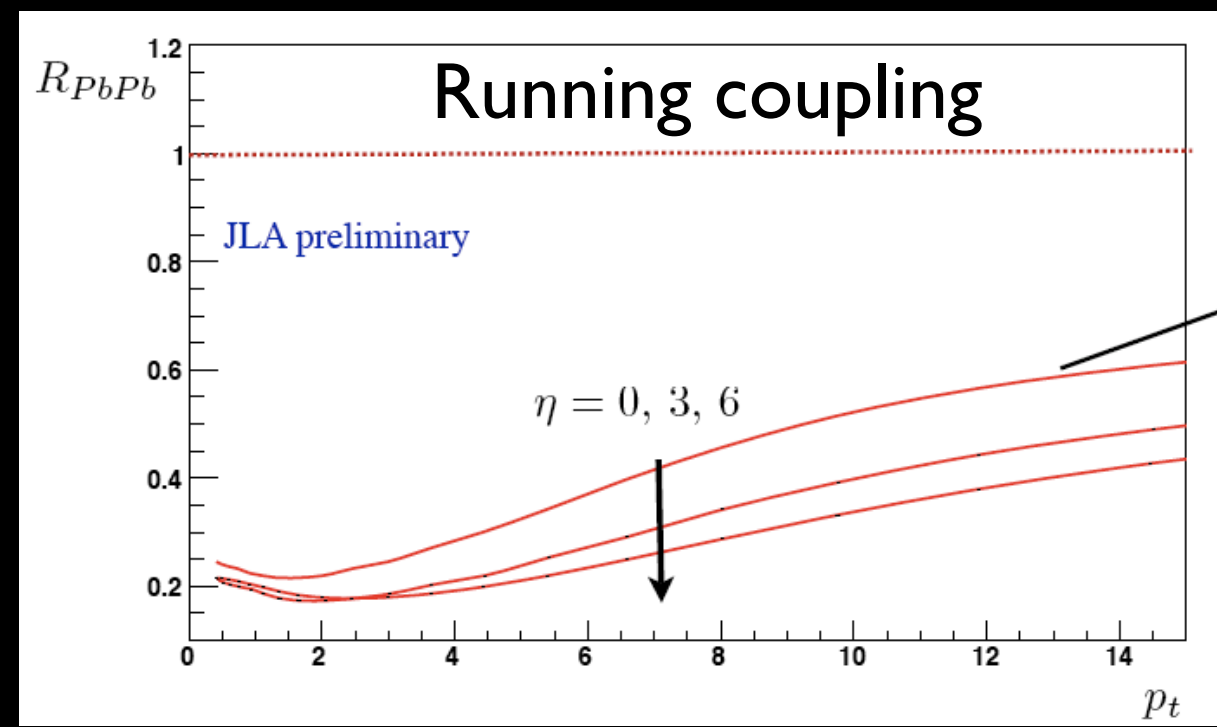
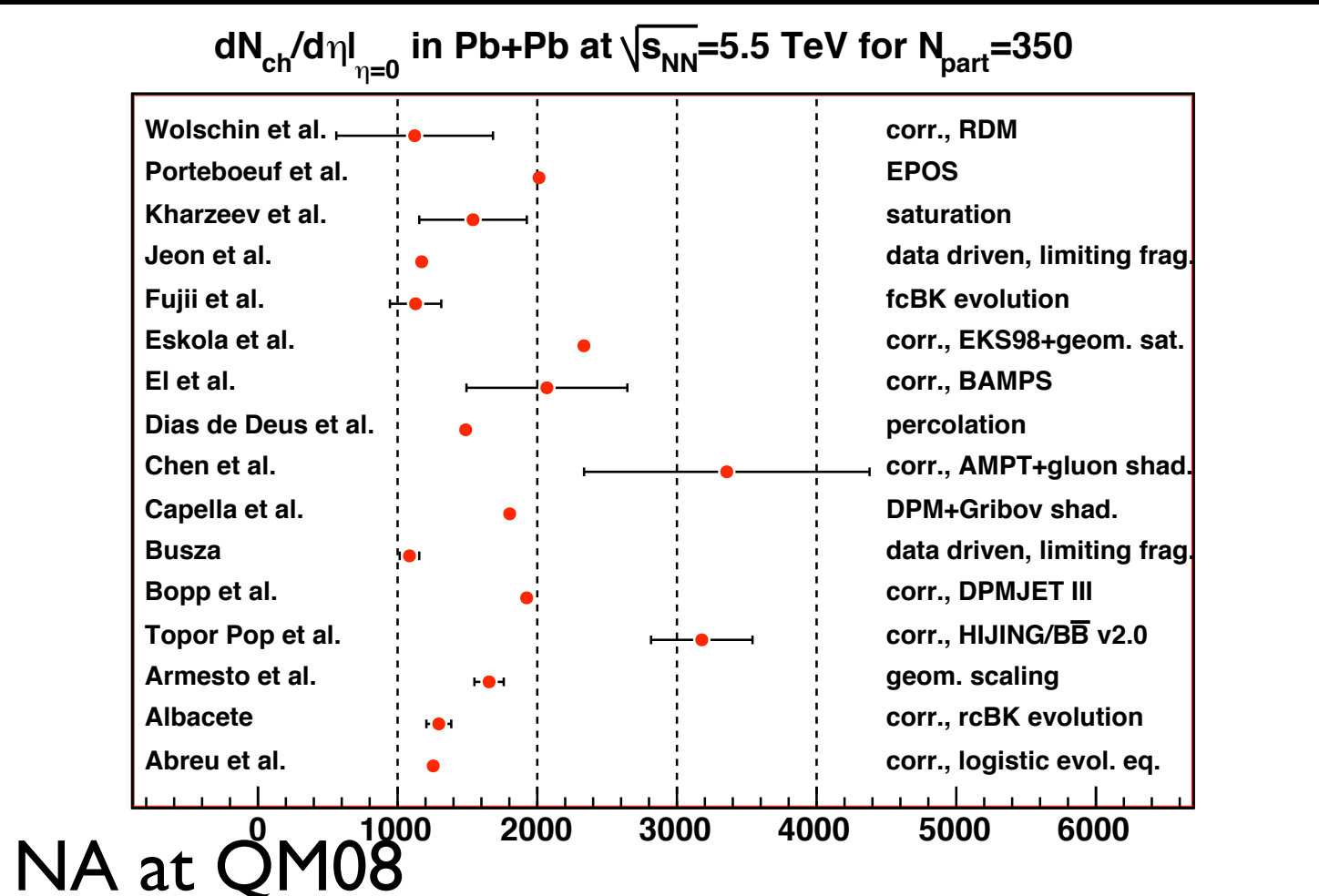
From eA to AA at RHIC and the LHC: 2. Phenomenology.

# 2.5. LHC (II):



⇒ A 1st day observable: charged multiplicity at midrapidity, will have discriminating power on models.

⇒  $dN_{ch}/d\eta|_{\eta=0} > 2000$  will be a challenge for saturation physics.



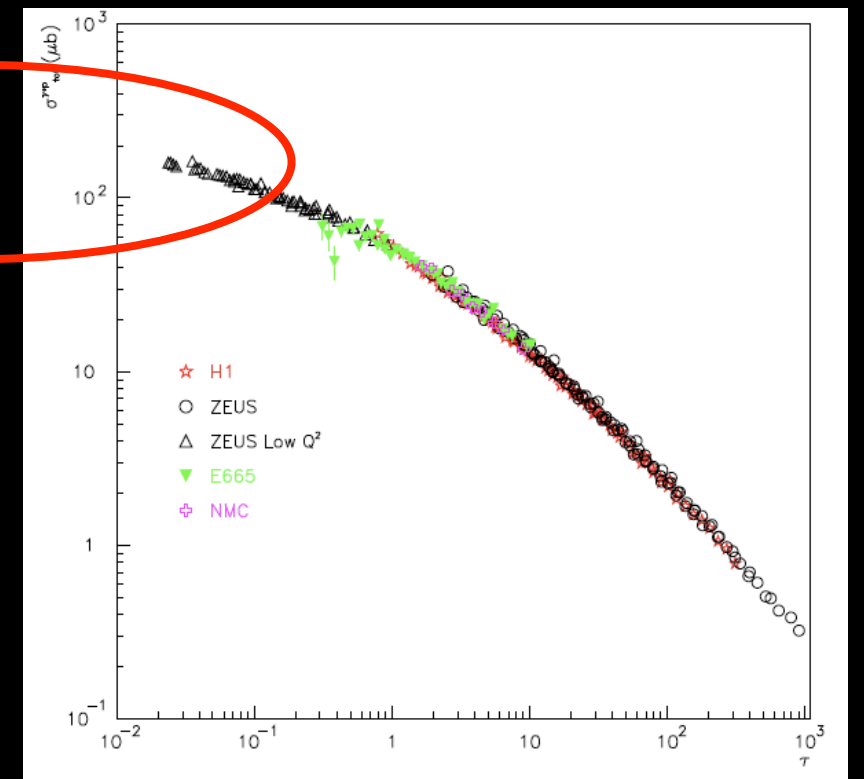
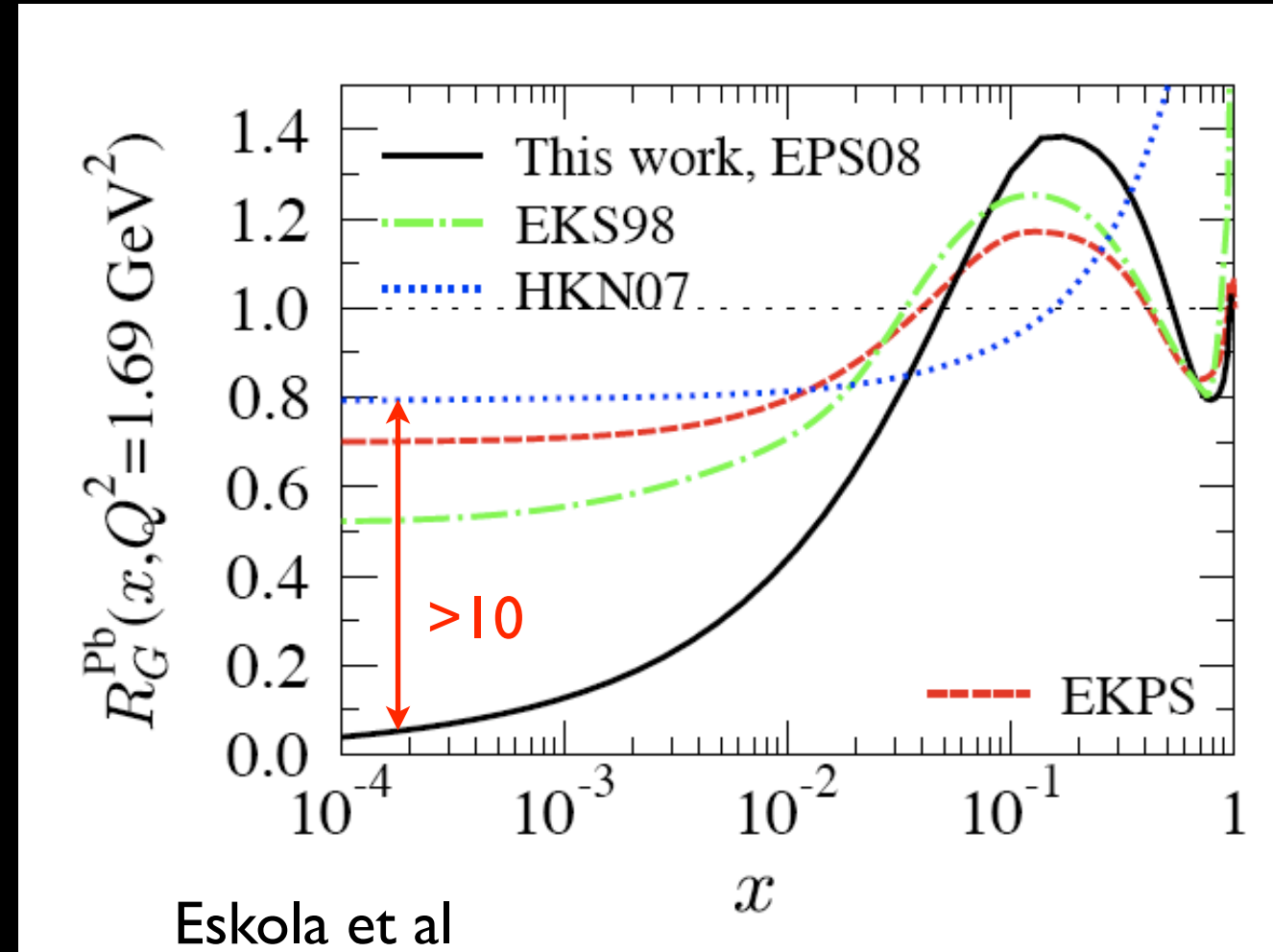
# 3. Summary:

⇒ **Saturation physics:** nice theoretical framework to discuss HIC starting from ep and eA. Still, many things missing.

⇒ **Geometric scaling is the most striking phenomenon.** Saturation models are not the only ones showing it.

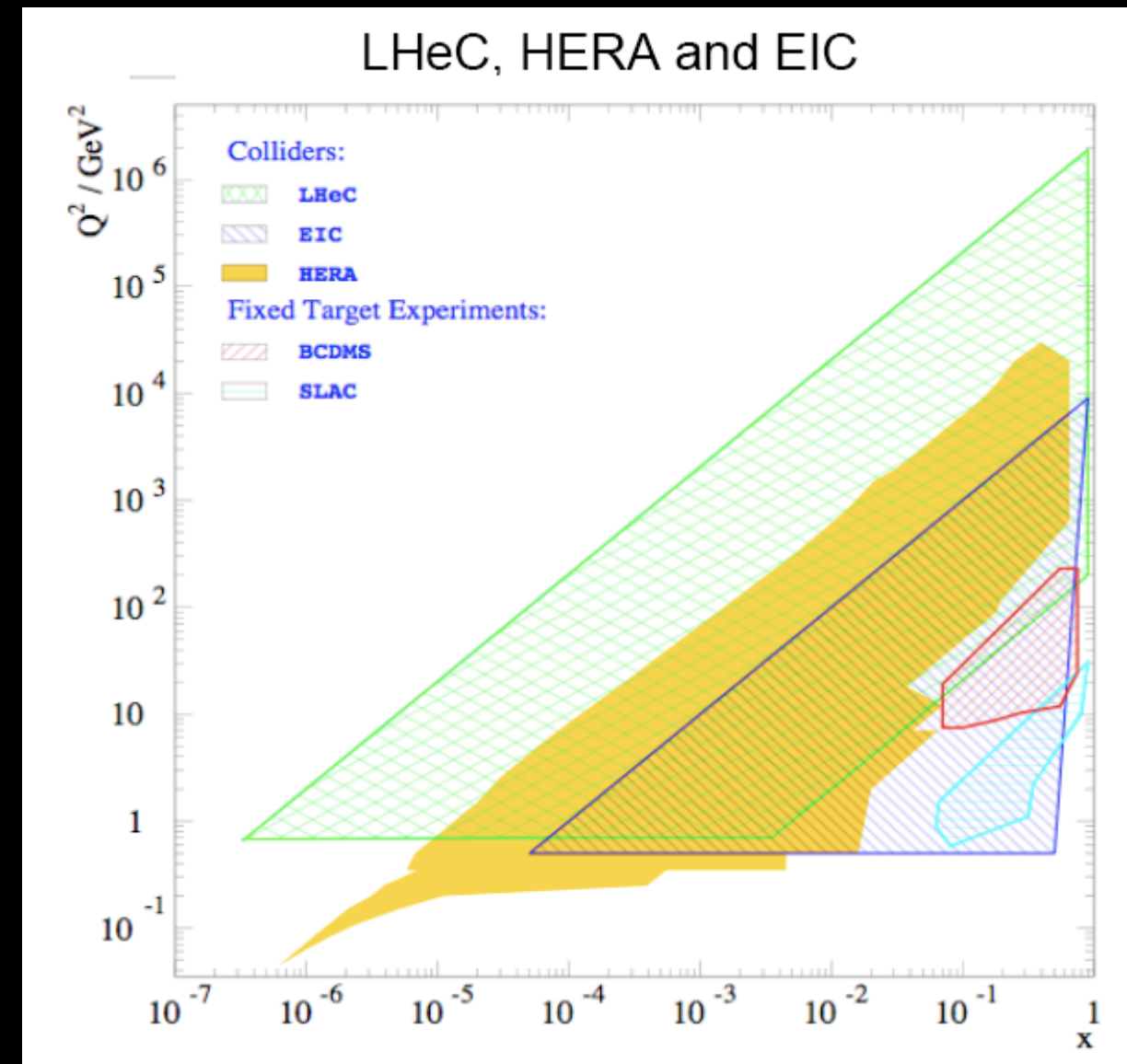
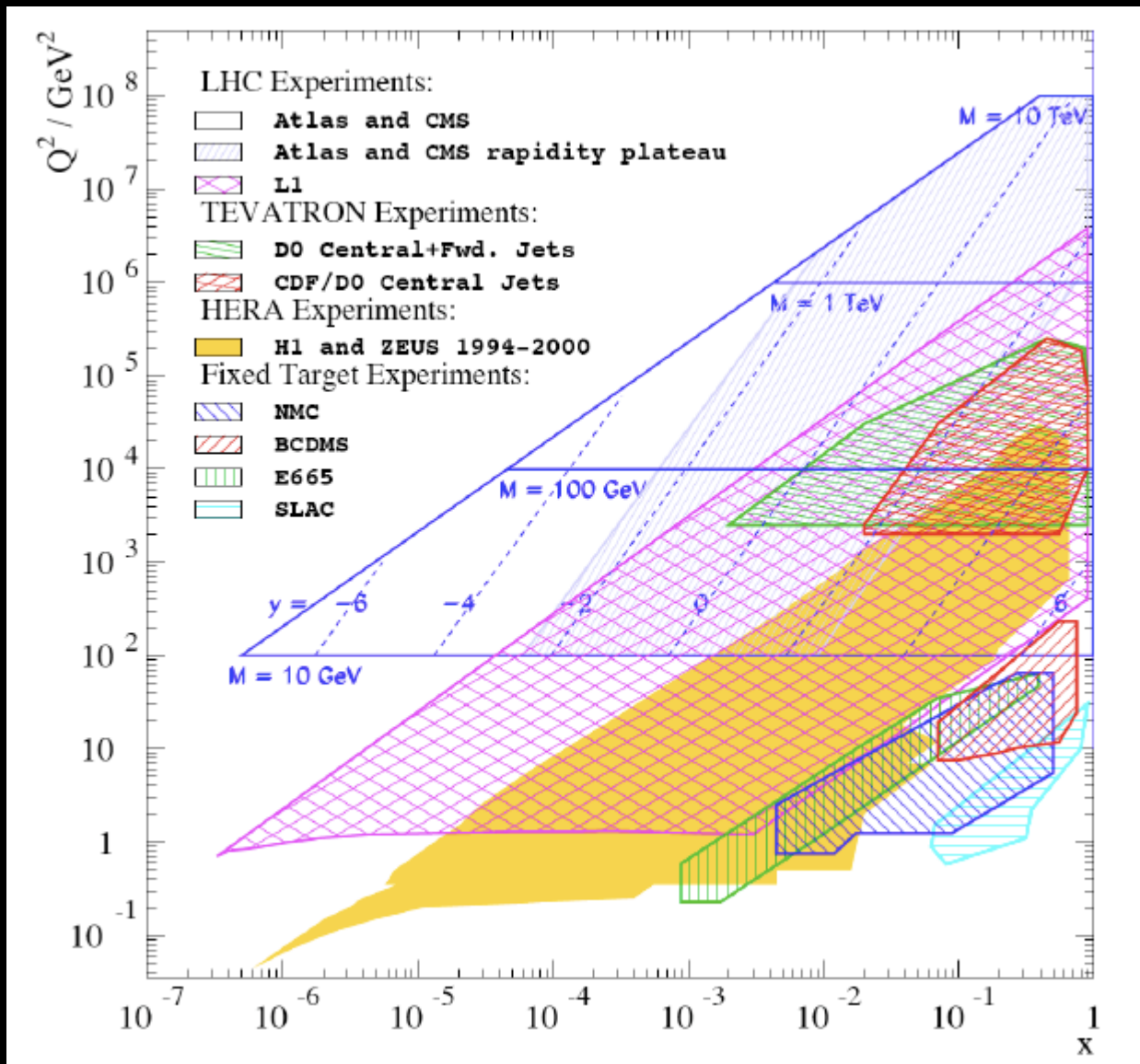
⇒ Uncertainties in standard DGLAP npdf's are huge at small  $x$  and  $Q^2$  for g.

⇒ **We need pA data at the LHC, and ep and eA data at smaller  $x$ .**





# 4. Prospects:



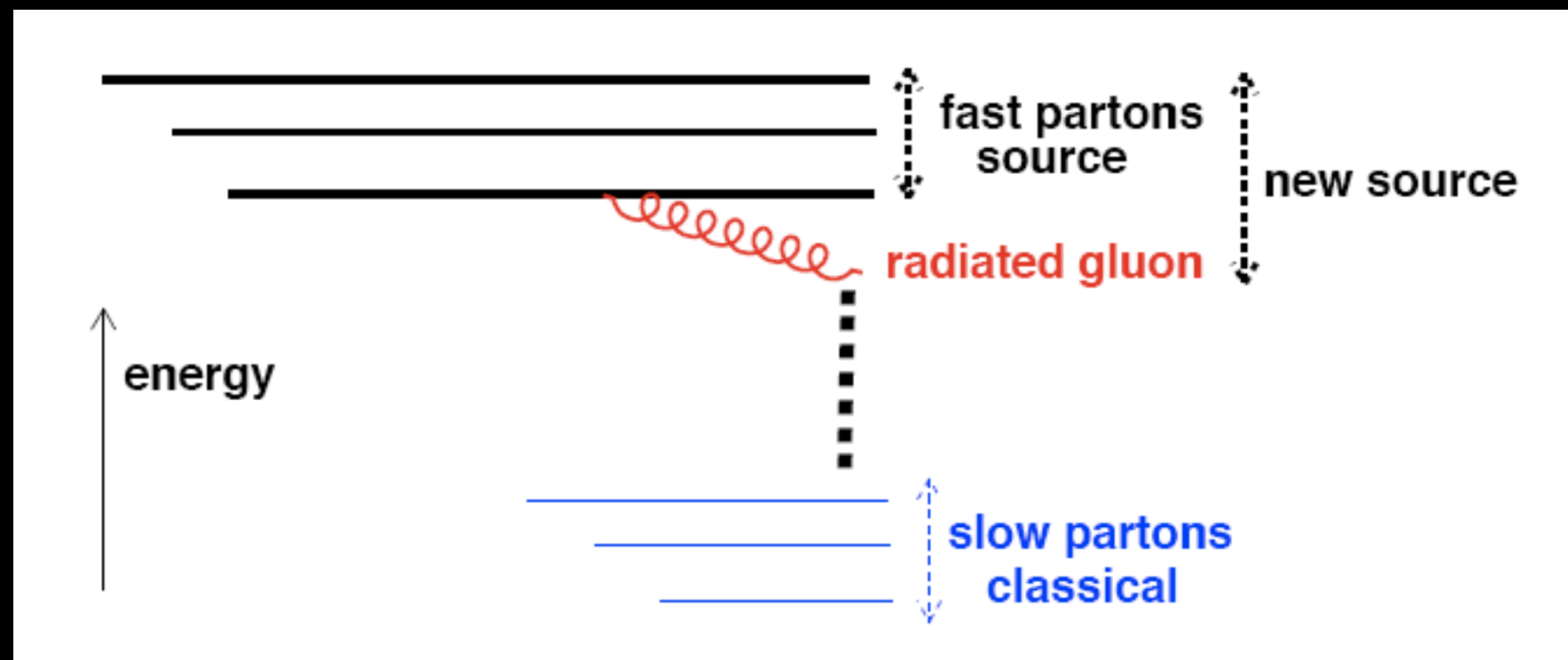
**1st ECFA-CERN LHeC workshop:  
Divonne-Les-Bains, September 1st-3rd 2008.  
Everybody is invited!!!**

# I. Introduction (II):

⇒ At **small enough  $x$**  for the projectile to interact coherently with the whole hadron, the **CGC** offers a description of the hadron wave function.

$$x \leq \frac{1}{2m_N R_A} \sim 0.1 A^{-1/3}$$

⇒ The RG equation for the slow/fast separation (**JIMWLK**) was derived for scattering of a dilute projectile on a dense target.



⇒ Its mean-field version (the **Balitsky-Kovchegov equation**) is the tool for phenomenology.

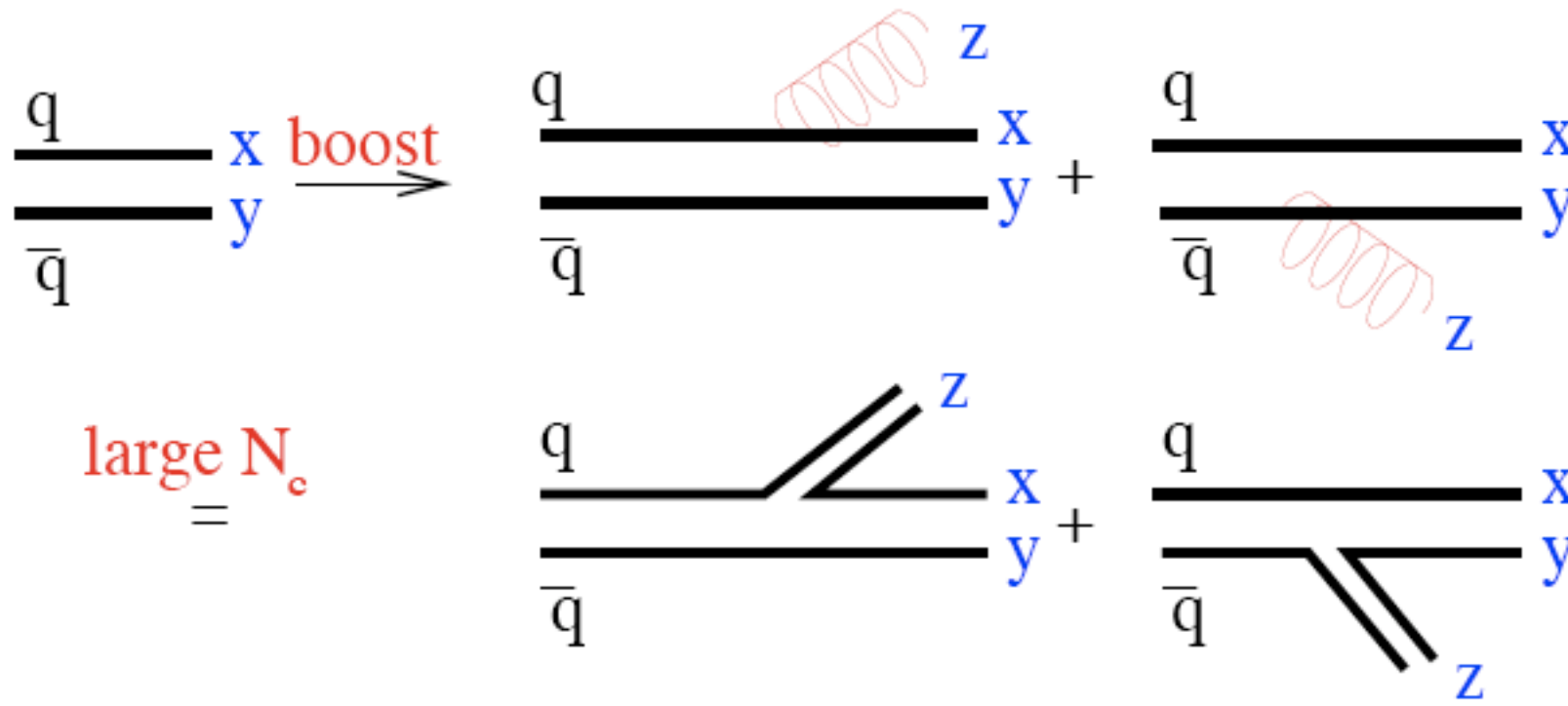
# 2. Theory:

## 2.1. Small- $x$ evolution: BK-JIMWLK:

- \* The Balitsky-Kovchegov equation.
- \* Properties at fixed coupling.
- \* Running coupling.
- \* Impact parameter.
- \* Beyond JIMWLK (see the talk by D. Triantafyllopoulos at Hard Probes 2008).

## 2.2. Factorization.

# 2.1. The BK equation:



large  $N_c$   
=

⇒ Neglecting the difference between  $\langle W^\dagger W W^\dagger W \rangle_{\text{tar}}$

and

$\langle W^\dagger W \rangle_{\text{tar}} \langle W^\dagger W \rangle_{\text{tar}}$ :

**BK equation.**

$$\frac{\partial N(r, Y)}{\partial Y} = \int \frac{d^2 z}{2\pi} K(\vec{r}, \vec{r}_1, \vec{r}_2) [N(r_1, Y) + N(r_2, Y) - N(r, Y) - N(r_1, Y)N(r_2, Y)]$$

$$K(\vec{r}, \vec{r}_1, \vec{r}_2) = \bar{\alpha}_s \frac{r^2}{r_1^2 r_2^2}, \quad \bar{\alpha}_s = \frac{\alpha_s N_c}{\pi}$$

$$\phi(Y, k, b) = \int \frac{d^2 r}{2\pi r^2} e^{i\vec{k} \cdot \vec{r}} N(Y, r, b)$$

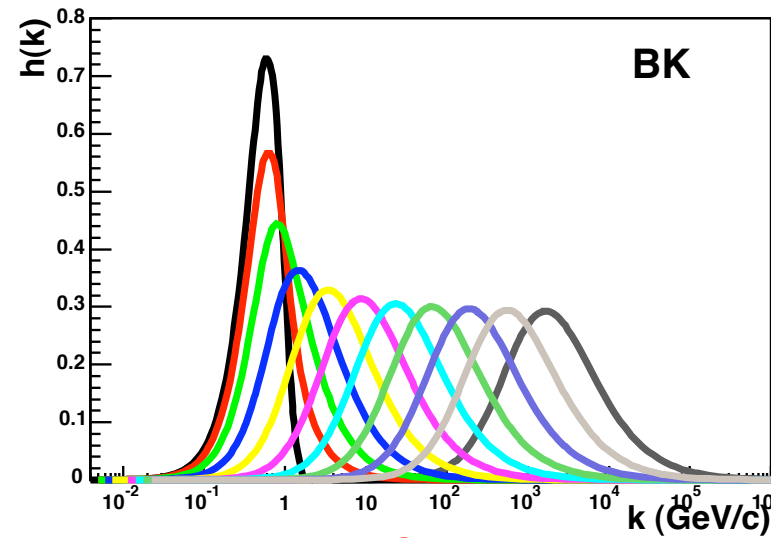
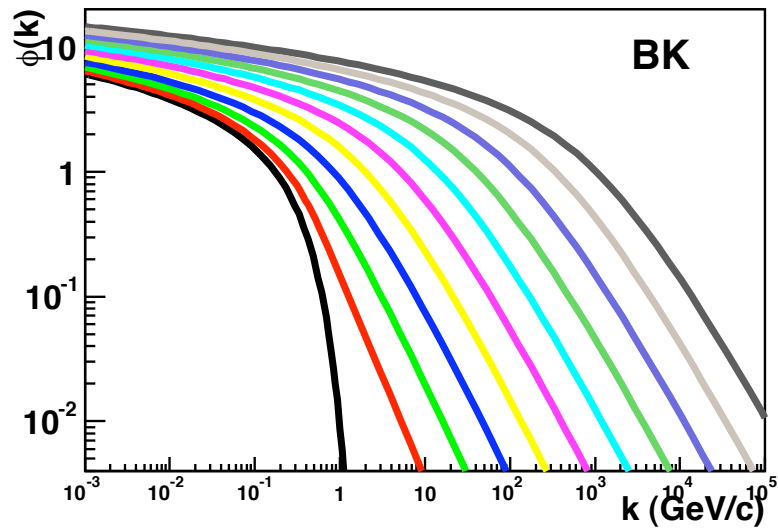
⇒ Neglecting the dependence on impact parameter:

$$\frac{\partial \phi(y, k)}{\partial y} = H_{BFKL} \otimes \phi(y, k) - \phi^2(y, k), \quad y = \bar{\alpha}_s Y$$

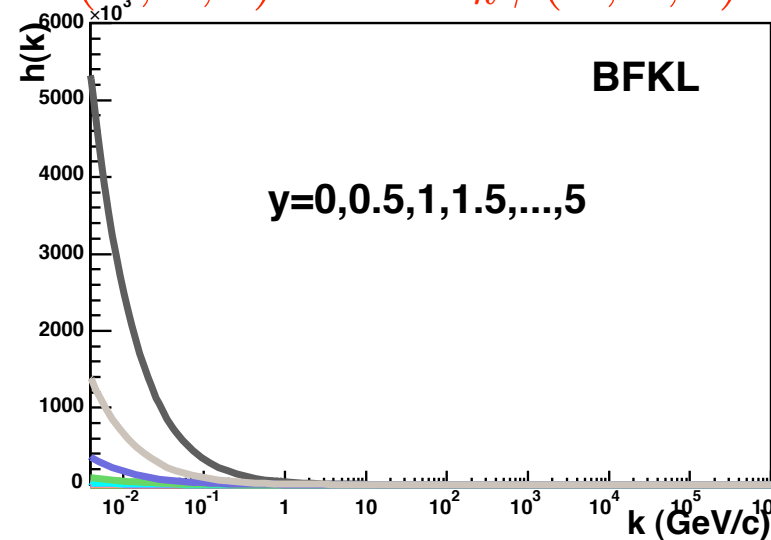
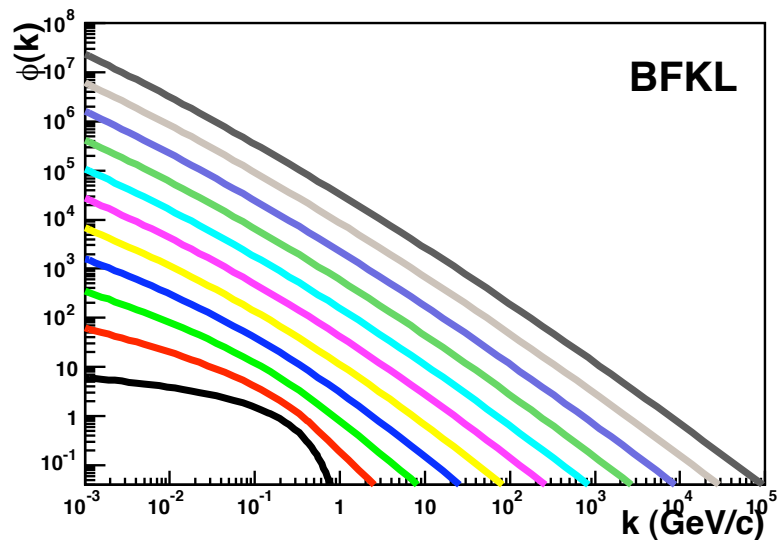
# 2.1. Properties at fc:

⇒ IR safety.

⇒ Solutions tend to a **universal form** independent of the initial condition (NA et al; Lublinsky; Golec-Biernat et al; Munier et al; Iancu et al; Mueller et al): **scaling**.



$$h(Y, k, b) = k^2 \Delta_k \phi(Y, k, b)$$

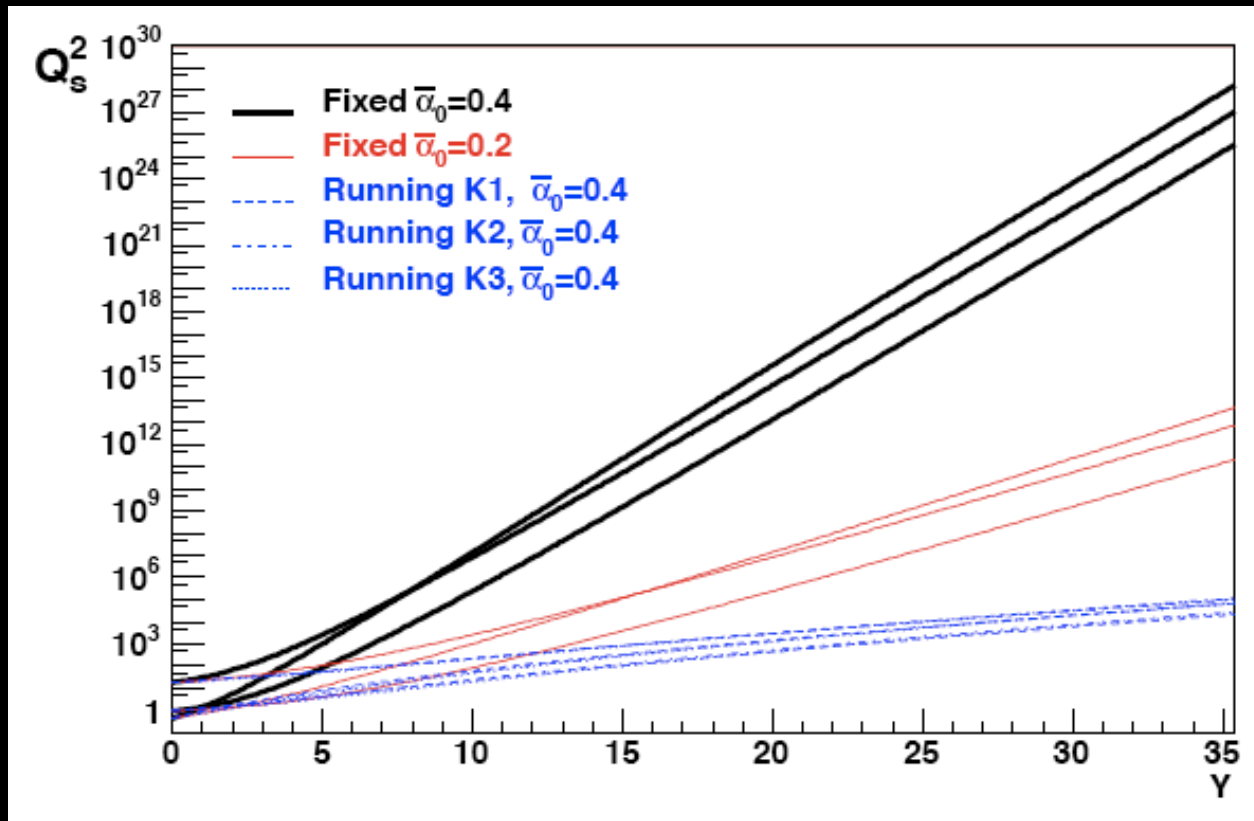


$$\phi(Y, k, b) = \phi\left(\frac{k}{Q_s(Y, b)}\right) \quad Q_s^2(Y) = \exp(\lambda Y), \quad \lambda \simeq 4.88 \bar{\alpha}_s$$

⇒ Shape goes from logarithmic in the  $k < Q_s$  region to power-like  $(1/k^2)^{Y \sim 0.63}$  in the scaling window  $Q_s < k < Q_s^2/k_0$  to  $1/k^2$  at large  $k$ .

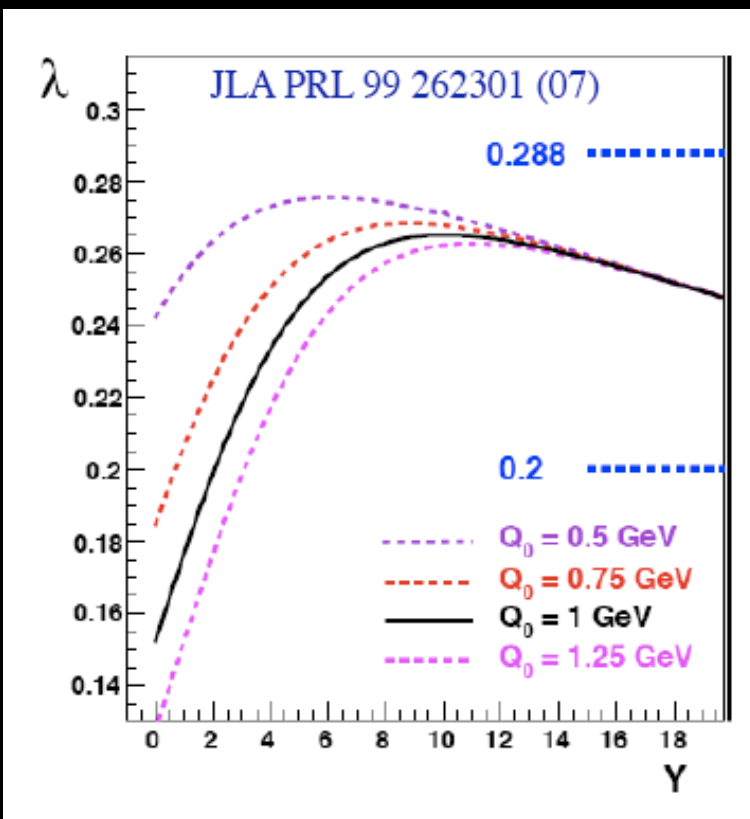


# 2.1. Running coupling:

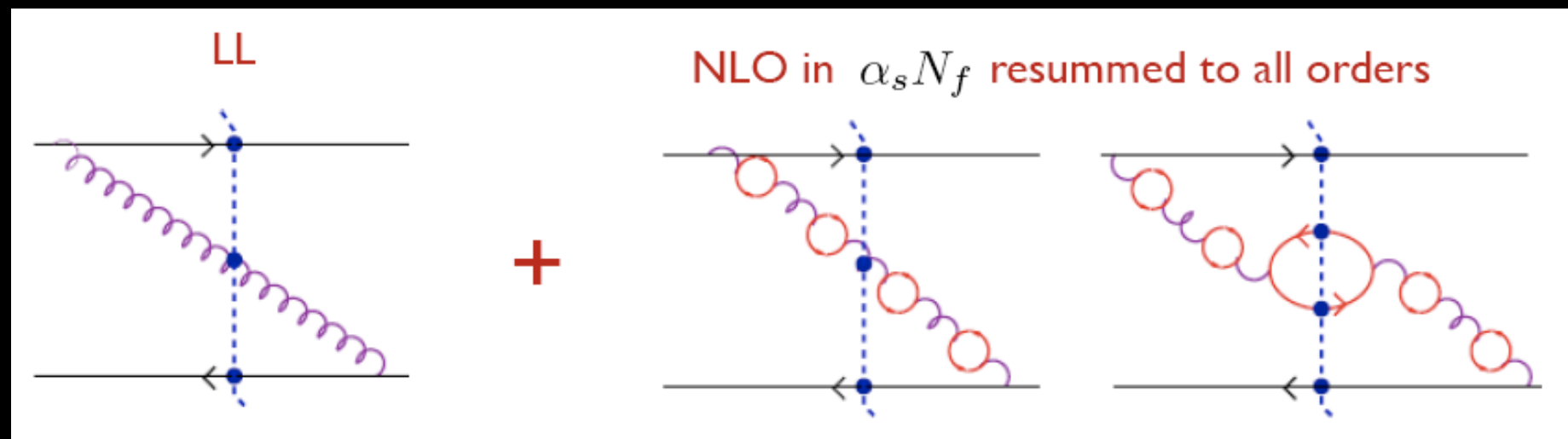


Heuristic implementations (Braun, Albacete et al, Mueller et al, Triantafyllopoulos) showed: **slowing-down of the evolution, scaling, vanishing A-dependence of  $Q_s$ , different shape from fc in the scaling window?!**

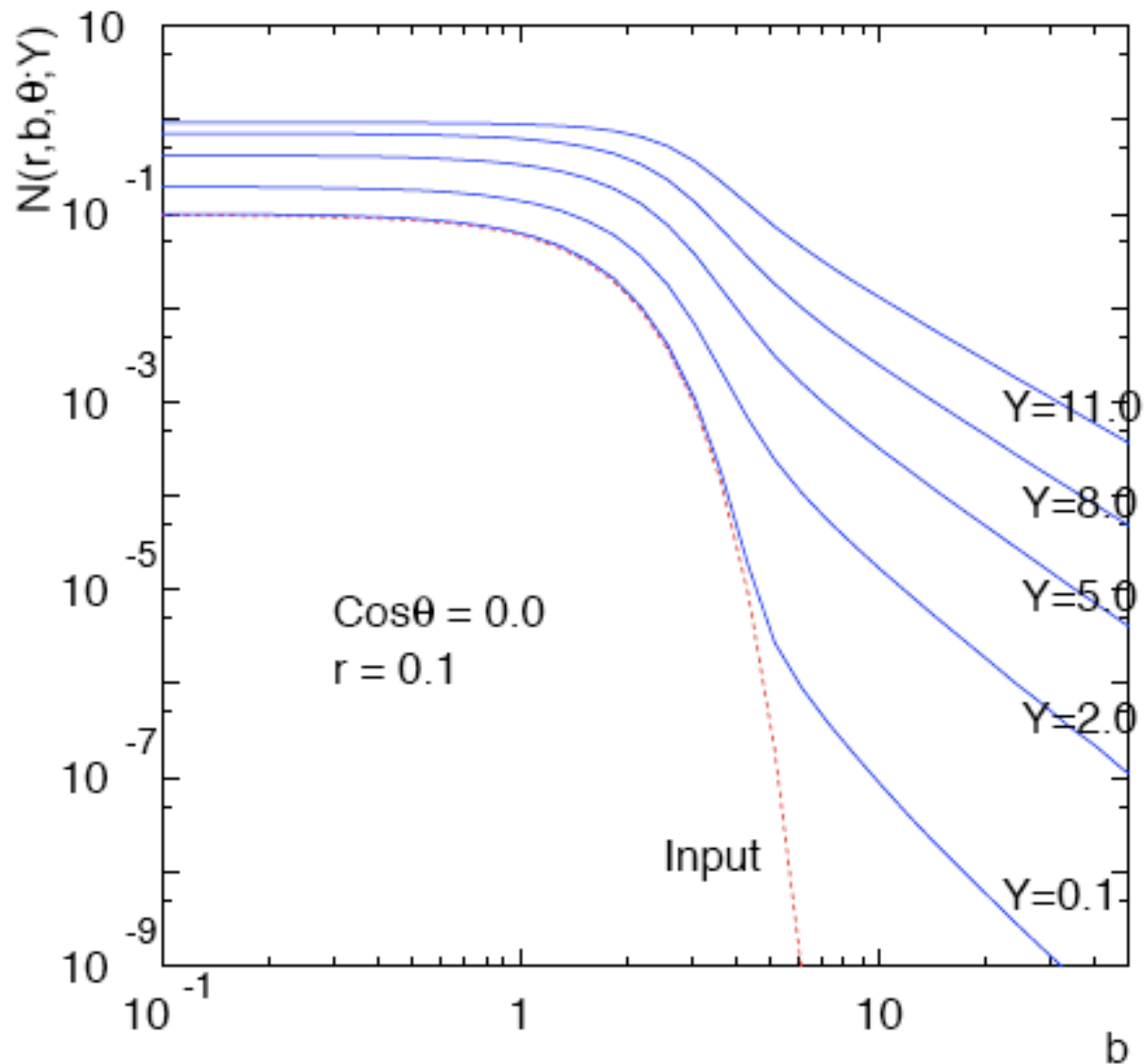
$$Q_s^2(Y) \propto \exp \sqrt{dY + X}$$



Part of the **NLO correction computed** (quark loops used à la BLM): Balitsky, Kovchegov-Weigert-Albacete, Rummukainen et al. IR problems?



# 2.1. Impact parameter:



⇒ Dependence on impact parameter usually neglected: large homogeneous nucleus.

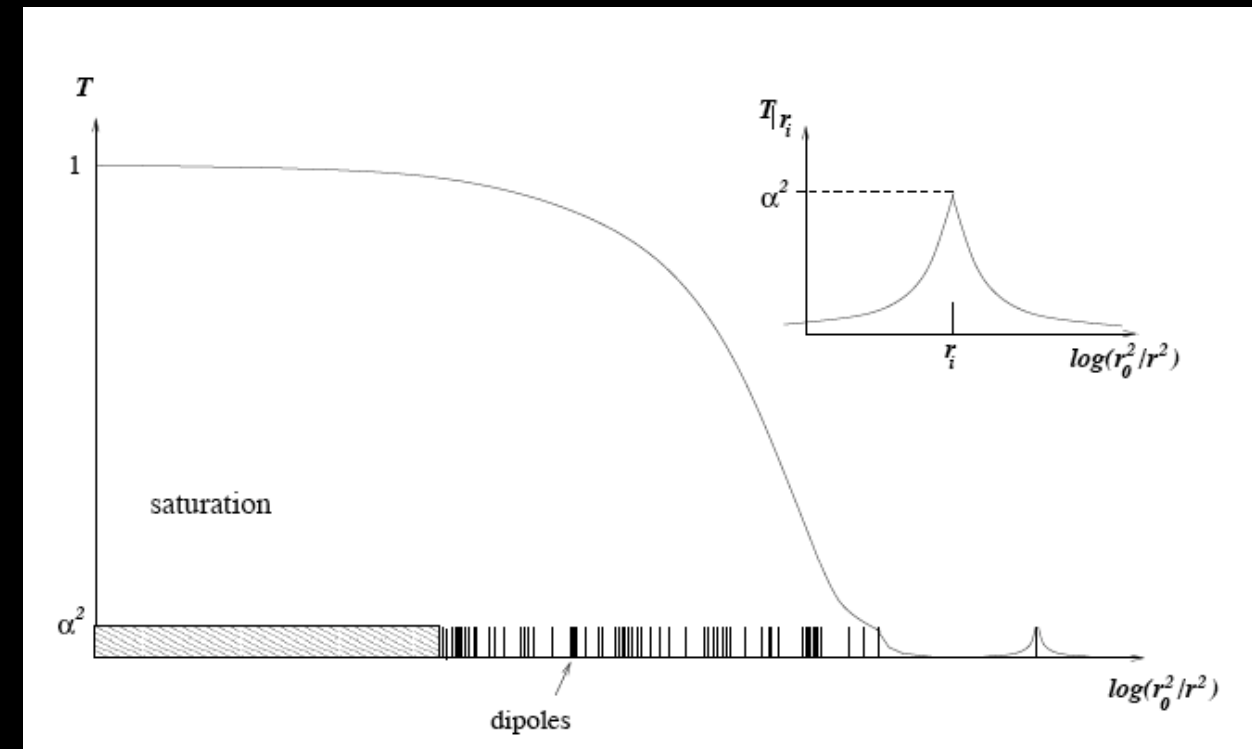
⇒ This dependence is crucial for total cross sections, and for the transition from the dense to the dilute regime at the nuclear edge: behavior of  $Q_s$  with  $b$  required e.g. to use CGC to provide i.c. for hydro.

⇒ BK generates a Coulomb tail ( $1/b^4$ ) independent of the starting i.c. in  $b$ : violation of the Froissart bound (but massless gluons): Kovner et al, Ferreiro et al, McLerran et al, Golec-Biernat et al. Kernel must be made short-range.

# 2.1. Beyond JIMWLK:

⇒ Going **beyond the mean field approximation in JIMWLK** for the 4  $W$  case gives effects  $< 15\%$  (Rummukainen et al).

⇒ **JIMWLK fails in dense-dense and dilute-dilute**: corrections, generically referred to as **Pomeron loops or fluctuations** (from '04 on: Iancu et al, Mueller et al, Kovner et al, Levin et al).



⇒ **Only general properties known**, no full theory, no numerical computation with the existing pieces. Information from **statistical mechanics analogies: reaction-diffusion processes, diffusive scaling**

$$A(\rho, Y) = \frac{1}{\sigma\sqrt{2\pi}} \int d\rho_s T(\rho)|_Y \exp\left(-\frac{(\rho_s - \langle\rho_s\rangle)^2}{2\sigma^2}\right)$$

$$\sigma \propto \sqrt{\bar{\alpha} Y}$$

⇒ Competition of these new LL pieces and NLO corrections (Iancu et al, Bondarenko et al, NA et al, Peschanski).



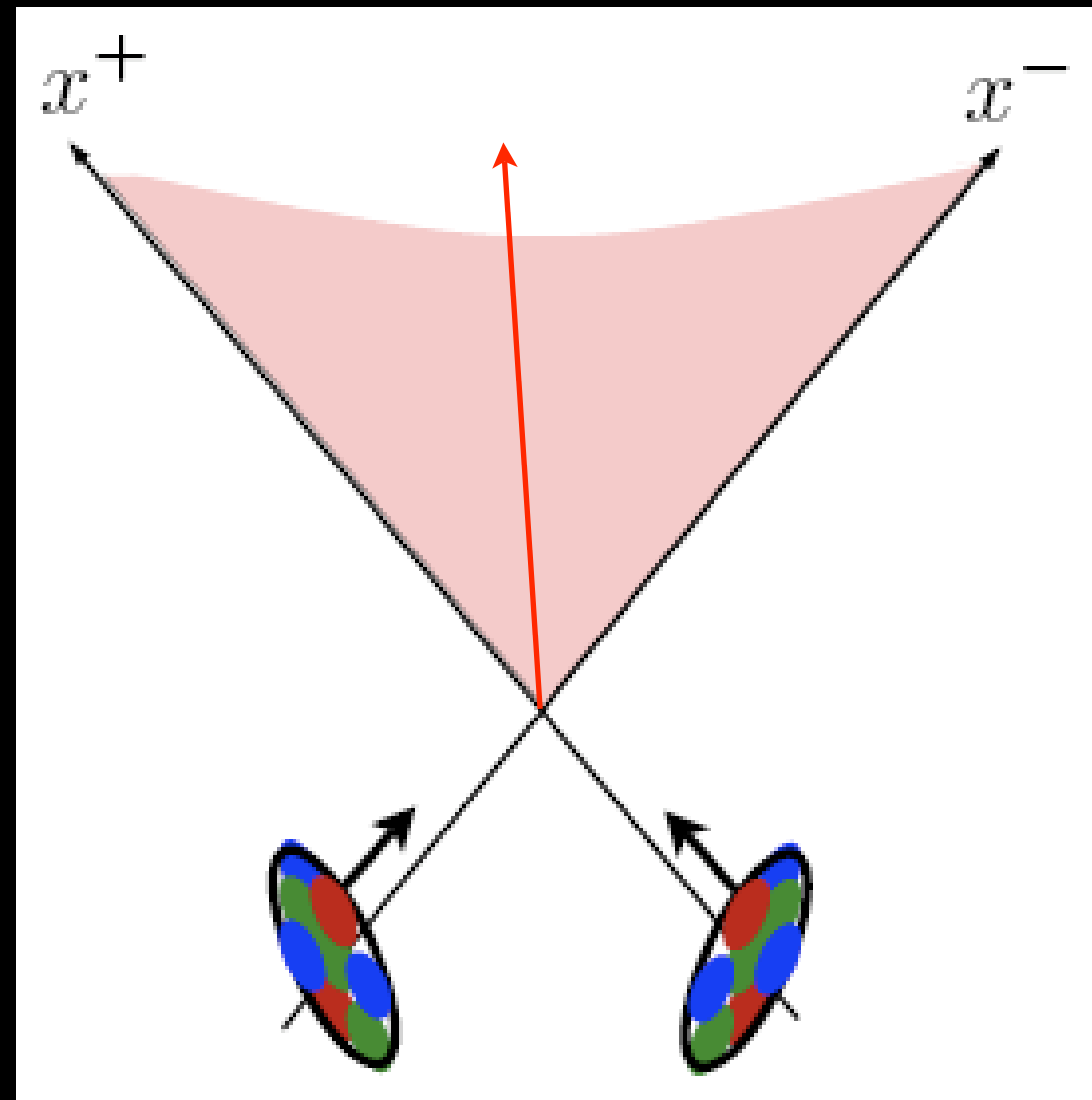
# 2.2. Factorization (I):

⇒ Gluon production on nuclear targets at  $\tau=0$  is usually computed through a generalization of  $k_t$ -factorization: convolution of ugd's (tentatively evolved with BK) with an off-shell matrix element computed in pQCD.

$$\frac{dN_{AB}^g}{d\eta} \sim \int \frac{d^2p}{p^2} \int d^2k \varphi_A(\mathbf{x}_1, k) \varphi_B(\mathbf{x}_2, |p - k|)$$

⇒ Alternatively, you can try and solve **classical gluodynamics** (Krasnitz et al, Lappi).

⇒ After production, **gluons are projected onto hadrons using LHPD or standard fragmentation functions** (evolving with DGLAP in the vacuum, with the eventual effects of a dense created medium as modifications of these ff's).



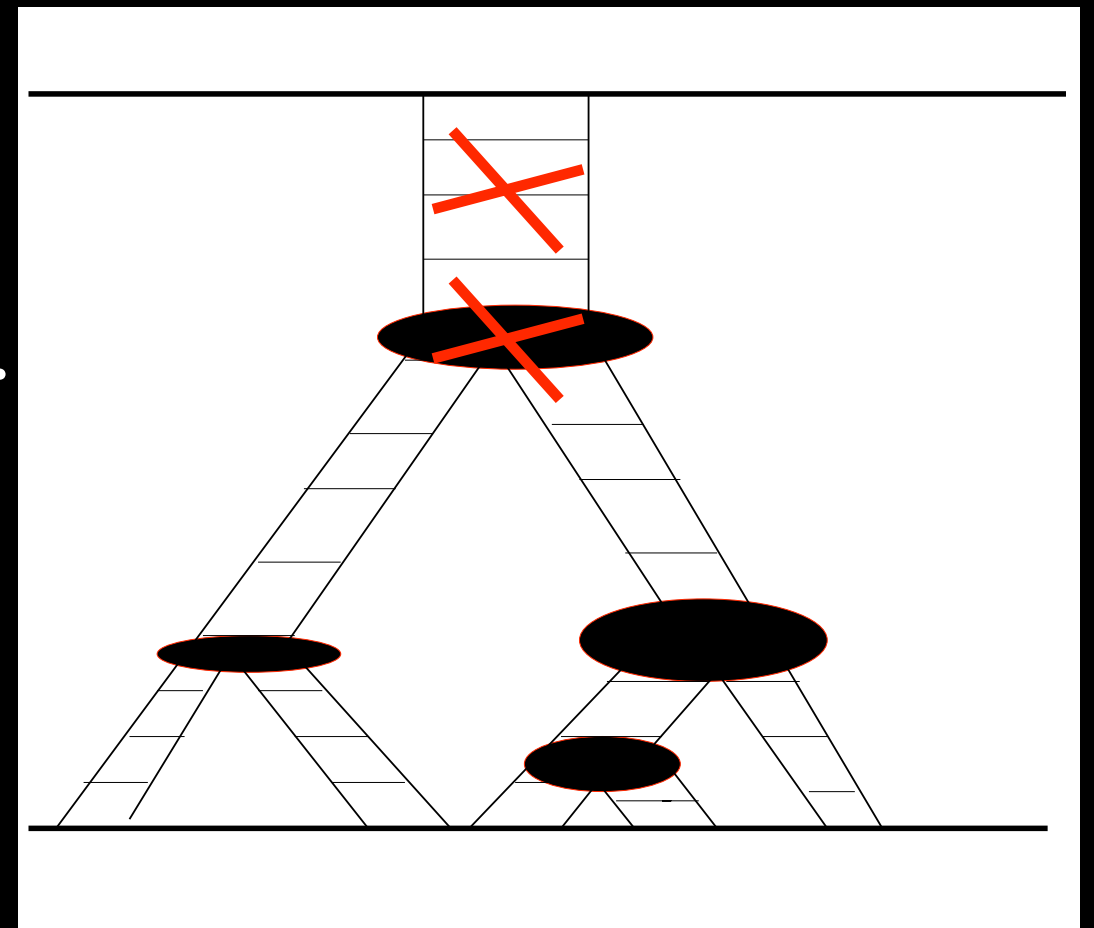
# 2.2. Factorization (II):

⇒ **Proofs or disproofs of these statements in AA are missing.** Several groups attempt to prove factorization formulas for gluon or quark production:

- \* In momentum space, the Pomeron language (Braun, Bartels et al).
- \* In the dipole model (Kovchegov et al).
- \* In classical gluodynamics: expansion in projectile and target densities (Gelis et al, Balitsky et al, McLerran et al, Marquet, Fukushima et al).
- \* Hadron wave function (Nikolaev et al, Kovner et al).

⇒ In **dilute-dense**:  $k_t$ -factorization OK for single gluon, not for quark or for 2 gluons. Several pieces evolving BK-like.

⇒ In **dense-dense**, usual  $k_t$ -factorization not valid (quantitative inaccuracy?); factorization becomes more involved.



# 2.3. pA at RHIC (I):

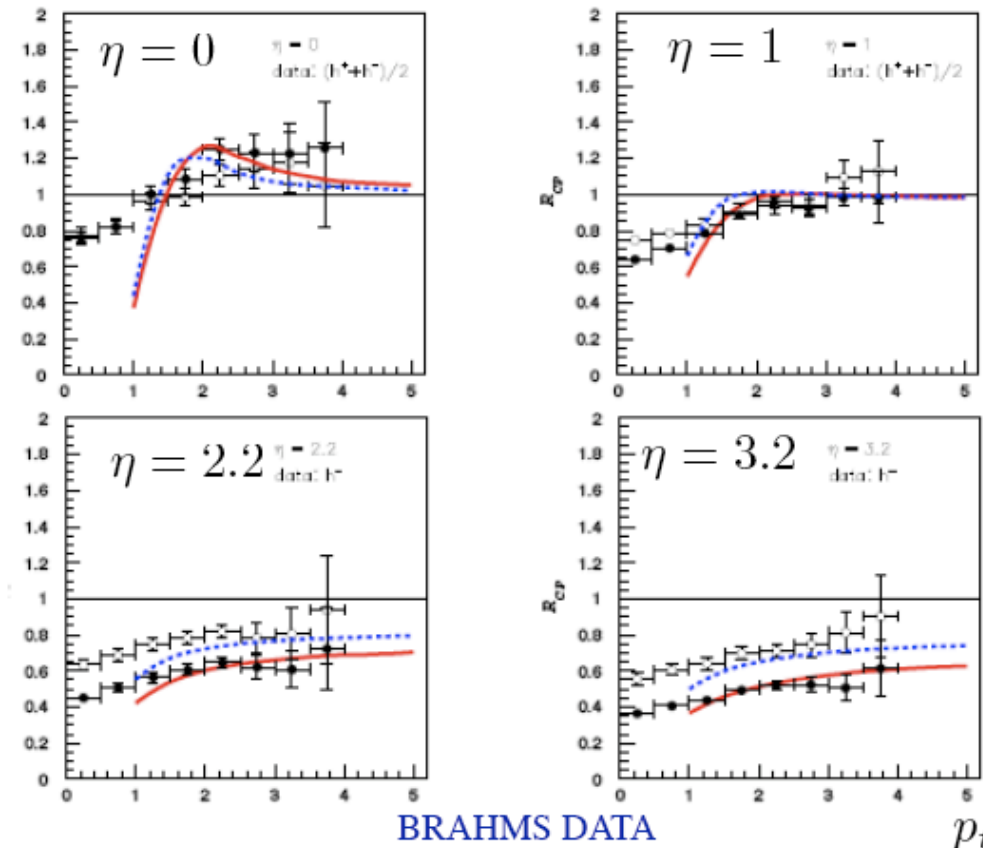
⇒ **Control experiment for initial state effects in AA:** Cronin effect in dAu at midrapidity ruled out initial state effects as the explanation for the suppression observed in AA.

⇒ **Suppression at forward rapidities was predicted by small-x evolution (BK).**

$$R_{dAu} = \frac{\frac{dN^{dAu}}{d\eta d^2bd^2p}}{N_{coll} \frac{dN^{pp}}{d\eta d^2bd^2p}}$$

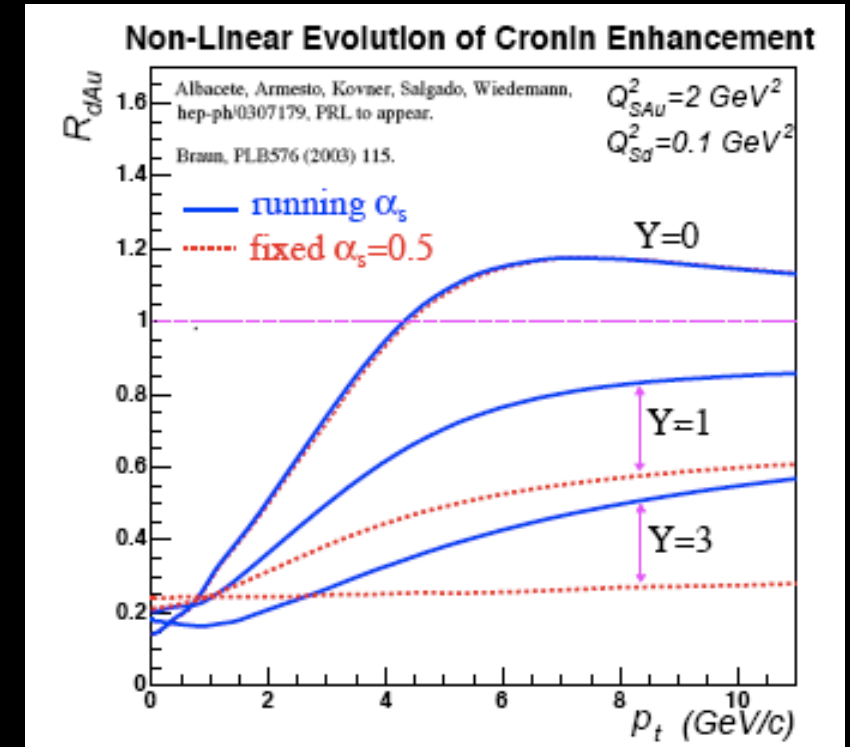
JLA-Armesto-Kovner-Salgado-Wiedemann  
Kharzeev-Kovchegov-Tuchin

$R_{CP}$



BRAHMS DATA

$p_t$



$$R_{dAu} \xrightarrow{y \rightarrow \infty} A^{-(1-\gamma/\delta)/3} (fc)$$

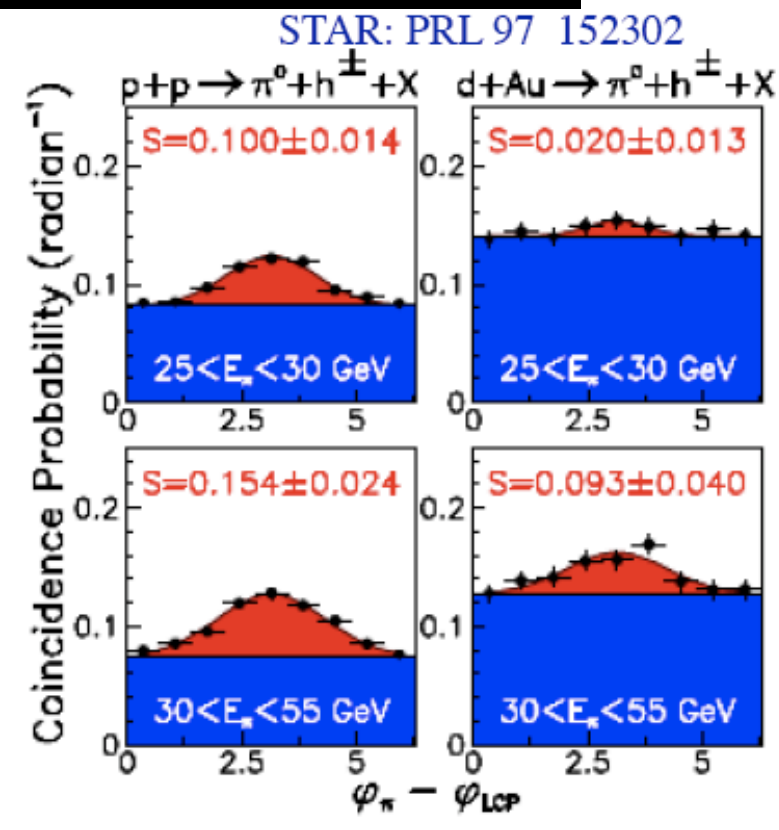
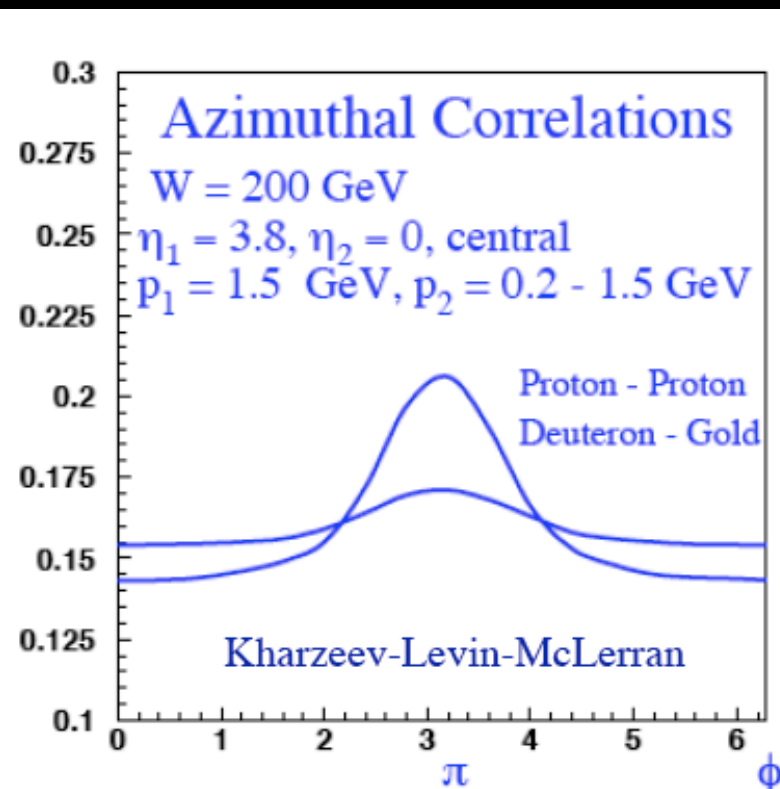
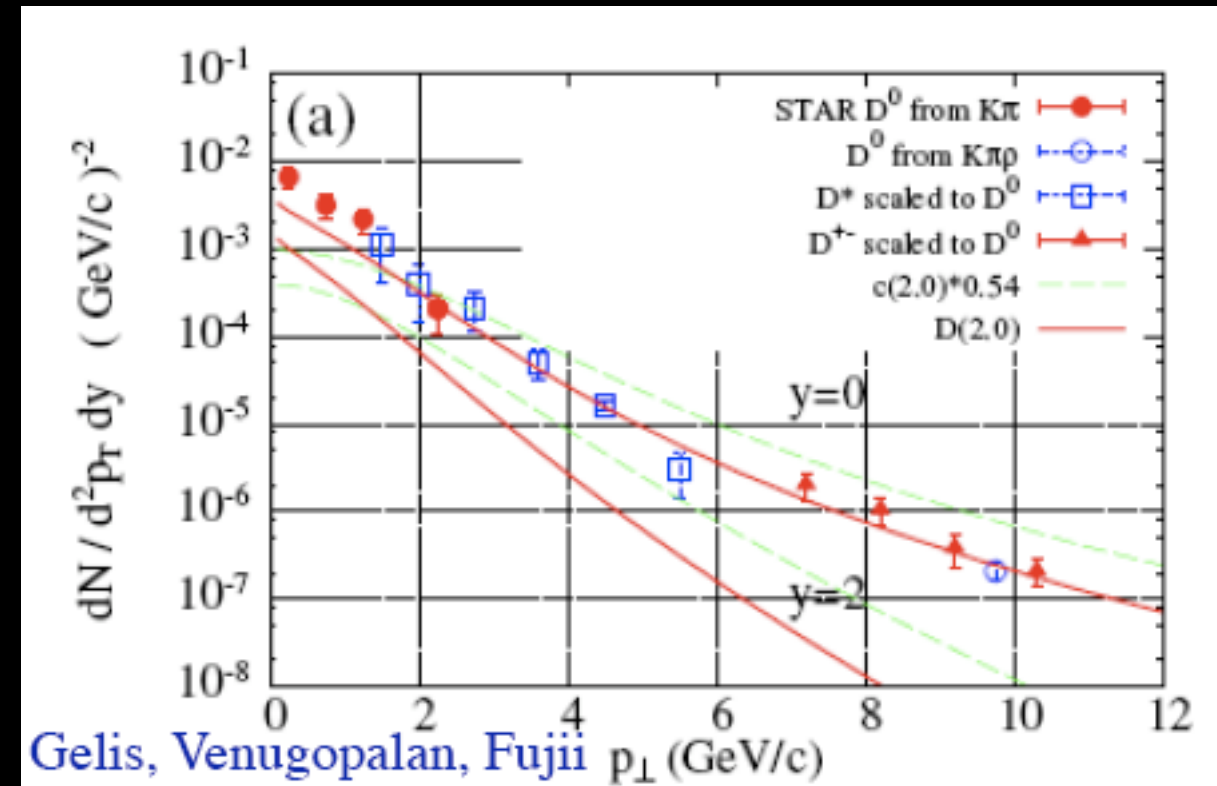
$$A^{-1/3} (rc, fluctuations)$$

Kharzeev et al, Baier et al,  
Iancu et al, Kozlov et al.

# 3.3. pA at RHIC (III):

⇒ **Azimuthal correlations** may also indicate small-x dynamics: tale of the two-particle inclusive distributions (Baier et al, Kovchegov et al, Marquet).

$$\frac{d\sigma}{dy_1 dy_2 d^2p_1 d^2p_2 d\Delta\phi}$$



⇒ **Charm production** described (also Kharzeev et al, Tuchin).

# 3.4.AA at RHIC (III):

⇒ CGC may offer initial conditions for QGP formation: transverse fields transform into longitudinal (**Glasma**) (Lappi et al, Romatschke et al).

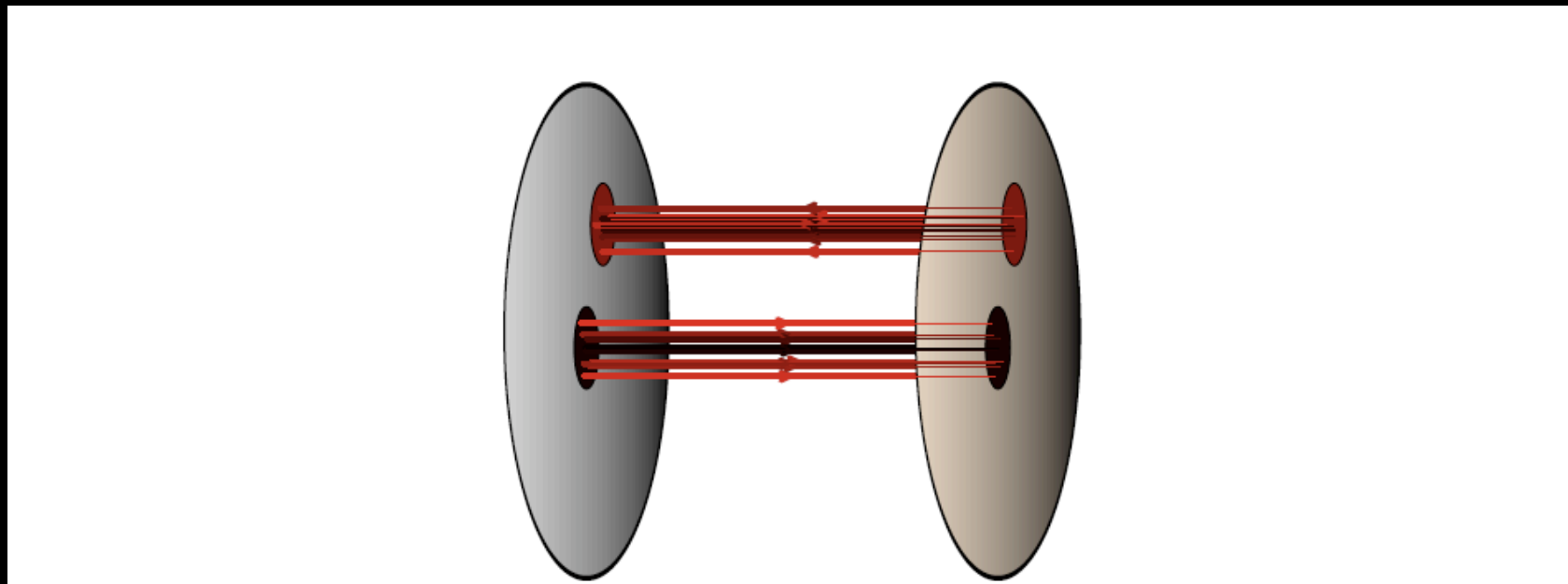


Figure 4: Glasma flux tubes. The transverse size of the flux tubes is of order  $1/Q_s$ .

⇒ QCD basis for good old string models.



$$\langle n_B \rangle_F = a + b n_F, \quad b \equiv D_{FB}^2 / D_{FF}^2,$$

$$b = \frac{1}{1 + c\alpha_s^2}.$$

⇒ **Correlations in rapidity** are a place to look for such origin of particle production (Capella et al, NA et al, Dumitru et al, Fukushima et al).

# 4. Summary:

⇒ **Saturation physics** offers a nice theoretical framework to discuss bulk characteristics of HIC starting from ep and eA.

⇒ **Theory: we miss**

- \* Initial conditions: apart from MV, we have very little.
- \* NLO corrections completed and understood.
- \* Fluctuations/Pomeron loops: are they important?
- \* Factorization/particle production.

⇒ **Phenomenology: we miss**

- \* Geometric scaling: is it too nice to be true?
- \* Treatment of non-perturbative effects and b-dependence.

⇒ **We miss data at smaller x: pA and AA at the LHC, and above all, eA.**