

Low-x physics at LHeC with NNPDFs (Exploratory studies)

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LHeC 2008 Workshop, Divonne. France

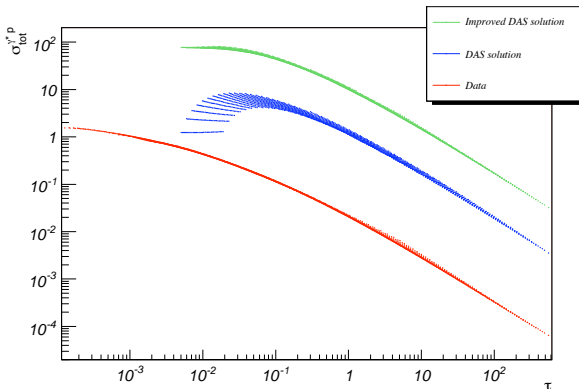
Introduction

- ▶ The study of Quantum Chromodynamics and the structure of the proton at **very low-x** is an important aspect of the **LHeC** potential (with implications for **LHC precision physics**)
- ▶ **Standard PDF determinations** neither not flexible enough nor with trustable uncertainties in **LHeC (extrapolation) regions** → Need statistically sound methods: **the NNPDF approach** (see morning talk)
- ▶ With such approach one can address questions **quantitatively** like whether or not **LHeC** can disentangle **saturation/resummation/higher orders** ...
- ▶ Related studies in this workshop in **P. Newmann's** talks (+ **J. Forshaw** talk at DIS08)
- ▶ Disclaimer → **Very preliminary studies** (no quantitative conclusions possible)

NNPDFs @ LHeC

Saturation

- ▶ **Saturation** has been extensively studied at HERA ...
- ▶ ... but so far no undisputed **smoking gun** has appeared
- ▶ Example: **Geometric Scaling** in $\sigma^{\gamma^*P}(x, Q^2)$ reproduced also within **DGLAP** (Caola, Forte 08)



Probing saturation

Two extreme views: saturation effects either **large for all observables** or **can always be absorbed in DGLAP analysis**. Truth probably in the middle ...

How to **quantify if LHeC** can disentangle saturation or related effects?

1. Generate pseudo-data in LHeC kinematics with realistic uncertainties
2. Assume different underlying physics (**saturation, NLO/NNLO DGLAP with different PDFs, DGLAP + small- x resummation ...**)
3. Perform a DGLAP PDF analysis and check if data can be reproduced

Need PDFs with **flexible enough parametrizations** and whose **uncertainty statistical analysis is independent of the data set** → **the NNPDF approach**

Simulated LHeC data

First exercise → Take **simulated LHeC data** from FS04 saturation model for $F_2(x, Q^2)$ and $F_L(x, Q^2)$ (Forshaw and Shaw 2004)

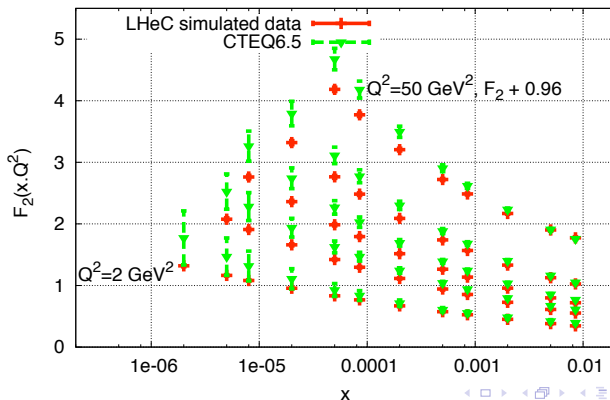
Set	N_{dat}	x_{min}	x_{max}	Q_{min}^2	Q_{max}^2	σ_{tot}
LHeCF2	50	$2 \cdot 10^{-6}$	$8.5 \cdot 10^{-3}$	2	50	2%
LHeCFL	32	$2 \cdot 10^{-6}$	$6.1 \cdot 10^{-4}$	2	30	14%

Expectations for F_L uncertainties a factor of 7 of F_2 uncertainties (Caveat → Pseudo-data taken from LHeC webpage. Would be very useful to have all pseudo-data shown by M. Klein publicly available!)

Extrapolations from global PDF analysis

Compare LHeC pseudo data (FS04sat) with DGLAP extrapolations
 CTEQ6.5 $\rightarrow F_2^{\text{sat}}|_{\text{LHeC}}$ inconsistent with DGLAP extrapolations

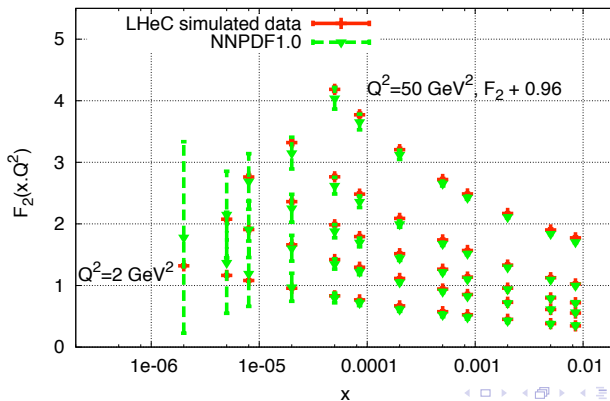
F_2 at the LHeC - Simulated data from FS04 saturation model



Extrapolations from global PDF analysis

Compare LHeC pseudo data (FS04sat) with DGLAP extrapolations
 NNPDF1.0 $\rightarrow F_2^{\text{sat}}|_{\text{LHeC}}$ not that far from DGLAP extrapolations

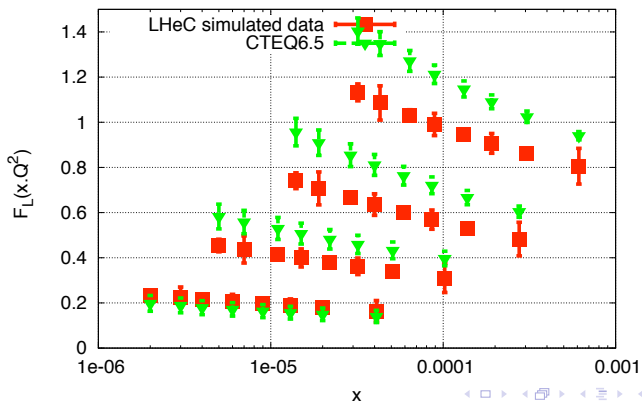
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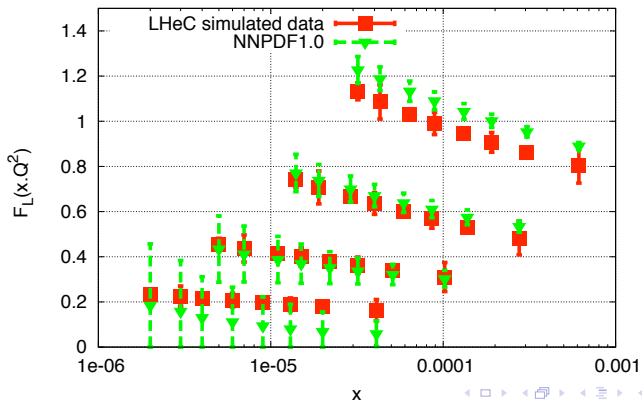
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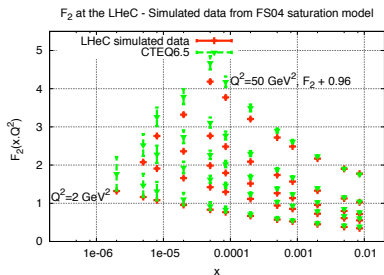
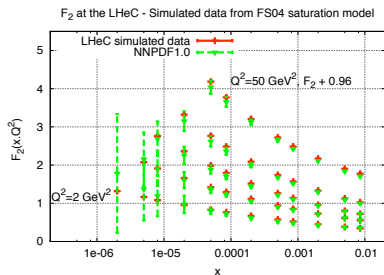
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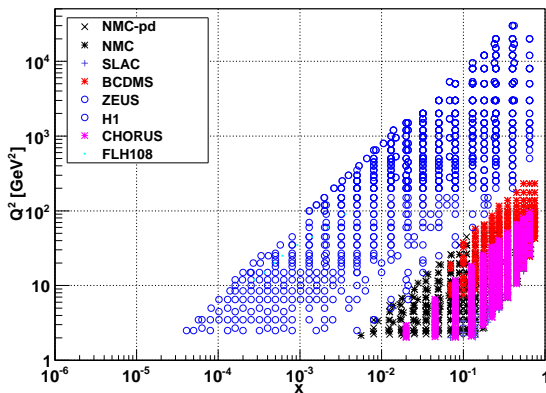


Lesson 1 → Need PDFs with **trustable error** in low- x region to assess how much small- x models differ from DGLAP extrapolations

Include LHeCsat data in NNPDF1.0

Can saturation effects be absorbed in a DGLAP PDF analysis?

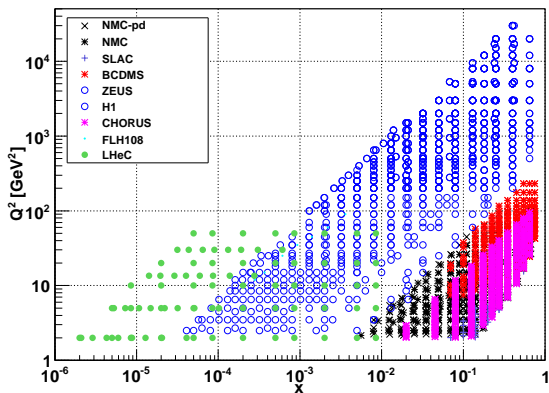
Add $F_L^{\text{sat}}|_{\text{LHeC}}$ and $F_L^{\text{sat}}|_{\text{LHeC}}$ pseudo-data into NNPDF1.0 analysis



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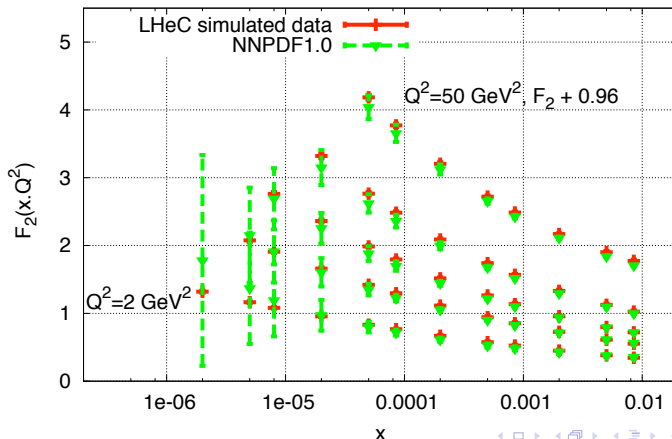
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Include LHeCsat data in NNPDF1.0

Compare saturation with DGLAP extrapolations (NNPDF1.0) for $F_2(x, Q^2)$:

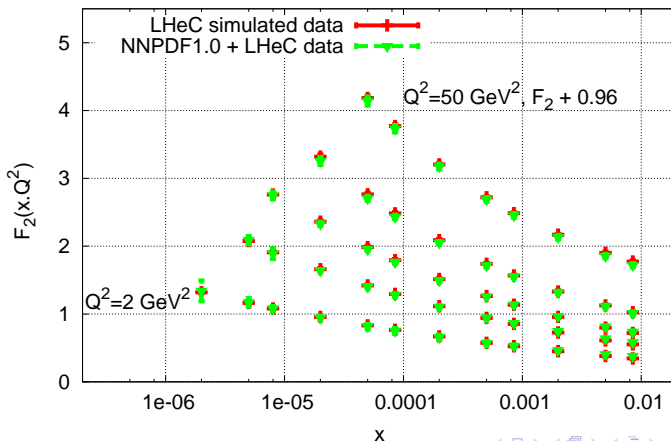
F_2 at the LHeC - Simulated data from FS04 saturation model



Include LHeCsat data in NNPDF1.0

... after LHeCsat pseudo data included in fit

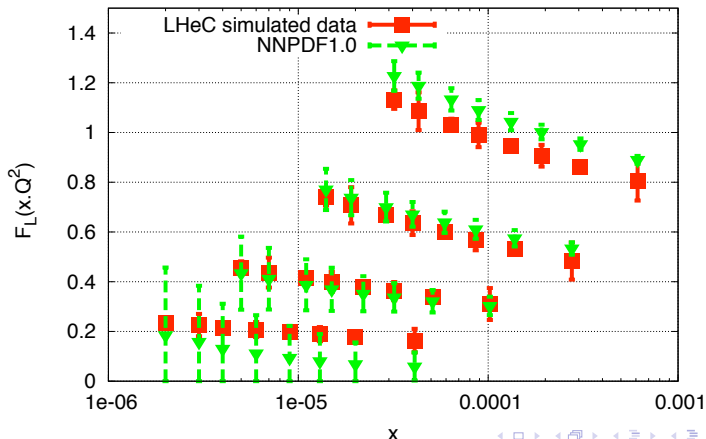
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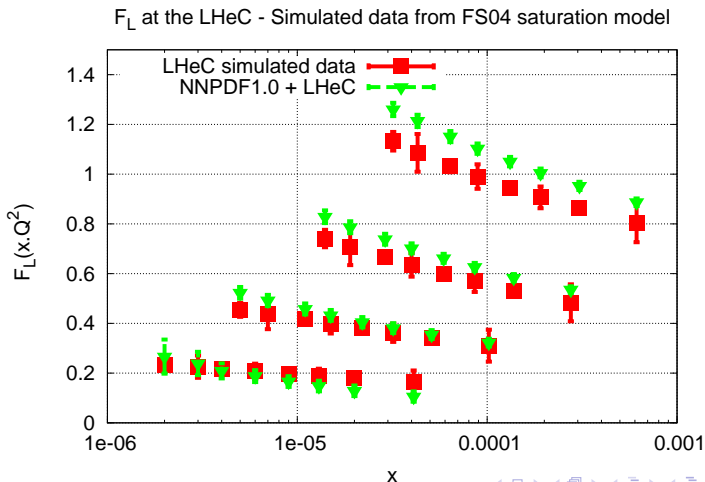
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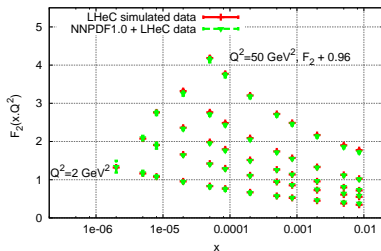
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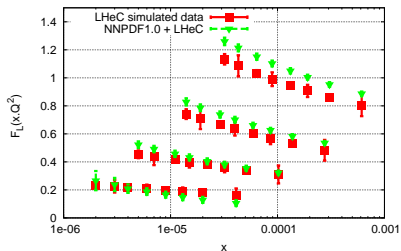


Include LHeCsat data in NNPDF1.0

F_2 at the LHeC - Simulated data from FS04 saturation model



F_L at the LHeC - Simulated data from FS04 saturation model



NLO DGLAP + NNPDFs seem to be able to reproduce $F_2^{\text{sat}}(x, Q^2)$, but more difficulties for $F_L^{\text{sat}}(x, Q^2)$

Lesson II :

1. $F_L(x, Q^2)$ crucial observable to understand low- x QCD at LHeC (But require [precise measurements](#))
2. Not all observables equivalent to disentangle saturation

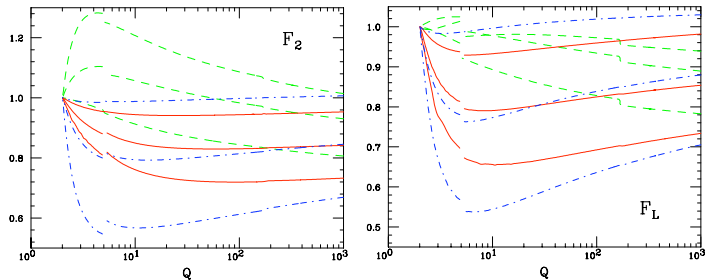
SMALL-X RESUMMATION

Small- x resummation

- ▶ Perturbation theory unstable at small- x (G. Altarelli's plenary talk)
- ▶ Small- x resummations (ABF, CCSS, WT) cures this stability
→ Sizable differences with respect NNLO in x -region relevant for LHeC physics
- ▶ Is low- x resummation required/relevant for LHeC phenomenology? → The need or not for small- x resummed evolution can be studied in the same way as we studied previously saturation

Small- x resummation

- ▶ Resummed **splitting functions** and **DIS coefficient functions** public and available from the ABF group



- ▶ Work in progress \rightarrow Implementation in the public x -space evolution code HOPPET (G. Salam and J.R, arxiv:0804.3755)

<http://projects.hepforge.org/hoppet/>

Useful tool for **LHeC** studies

OUTLOOK

Outlook

- ▶ The **NNPDF** approach provides a useful technique to quantify if **LHeC** can disentangle **saturation/resummation** from **standard PDF evolution**
- ▶ Work in progress: similar exercises with **LHeC** pseudo-data generated with NLO DGLAP (with **CTEQ6.6** and **NNPDF1.0**) and with low- x resummation
- ▶ In other (safer) kinematical regions:
 - ▶ **Simulate LHeC data** for other structure functions in different kinematical regions
 - ▶ **Include in (NN)PDF analysis** (M. Klein talk)
 - ▶ Study reduction in PDF uncertainties and **implications for precision LHC physics**

Thanks for your attention!

Outlook

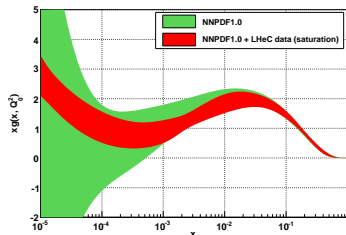
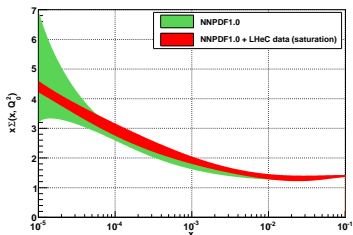
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EXTRA MATERIAL

Preliminary results

Errors at low- x do indeed shrink.



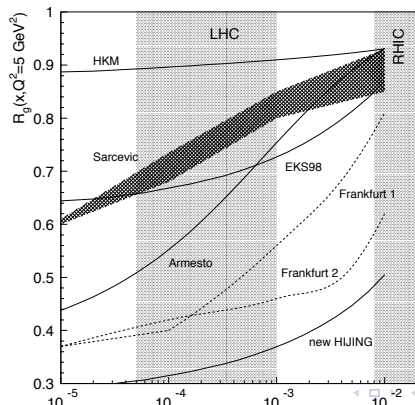
Should be compared with PDFs with LHeC pseudo data simulated with NLO DGLAP extrapolation \rightarrow Further error reduction in this case is expected

NUCLEAR PDFS AT THE LHeC

Nuclear PDFs at the LHeC

- ▶ Nuclear PDFs much less constrained than proton PDFs → No eA runs in HERA

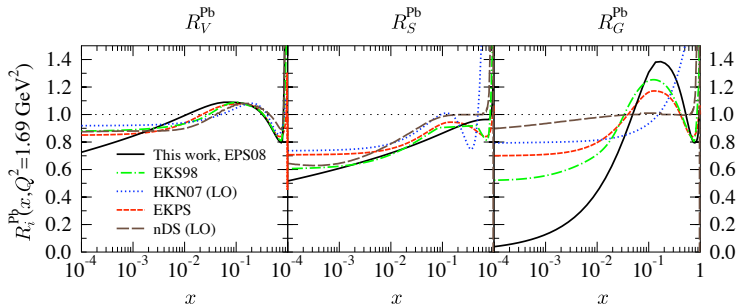
From N. Armesto, ... to Predictions for $R_g(x, Q^2, A) = g^{(A)}/g^{(p)}$



Nuclear PDFs at the LHeC

- ▶ Nuclear PDFs much less constrained than proton PDFs → No eA runs in HERA

From EPS08 global nPDF analysis (K. Eskola et al., arxiv:0802.)



Nuclear PDFs at the LHeC

- ▶ Nuclear PDFs much less constrained than proton PDFs \rightarrow No eA runs in HERA
- ▶ Precise measurement of initial state nuclear effects in pA (LHC) and eA (LHeC) \rightarrow Baseline to discriminate QGP effects in HIC
- ▶ Nuclear PDFs parameterized like proton PDFs, but with extra dependence on A and more uncertain x -dependence \rightarrow Potential functional form bias?
EPS08 analysis (K. Eskola et al., arxiv:0802.)

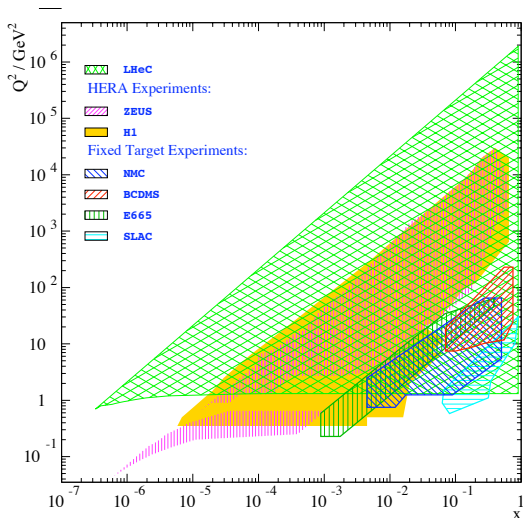
$$\begin{aligned}
 R_1^A(x) &= c_0^A + (c_1^A + c_2^A x^{\alpha^A})[\exp(-x/x_s^A) - \exp(-x_s^A/x)], & x \leq x_a^A \\
 R_2^A(x) &= a_0^A + a_1^A x + a_2^A x^2 + a_3^A x^3, & x_a^A \leq x \leq x_e^A \\
 R_3^A(x) &= \frac{b_0^A - b_1^A x}{(1-x)^{\beta^A}} + b_2^A (x - x_e)^2, & x_e^A \leq x \leq 1.
 \end{aligned}$$

PRECISION QCD AT THE LHeC

References:

J. Dainton et al., *Deep Inelastic Electron-Nucleon Scattering at the LHC*,
JINST 1 10001

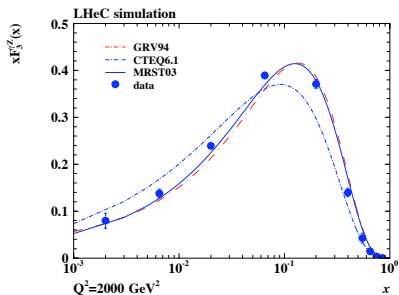
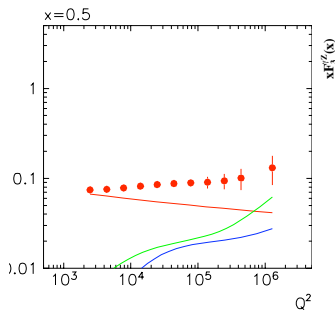
Precision QCD at the LHeC



Constraining proton structure at LHeC

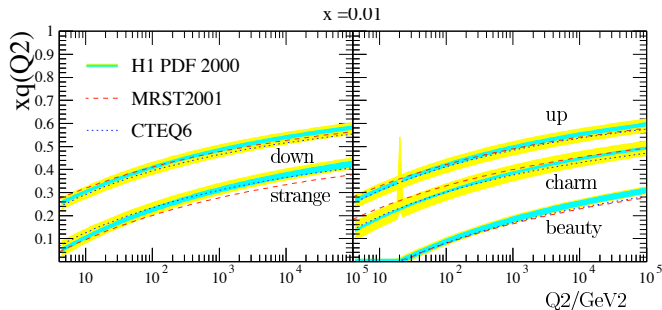
LHeC (+ final HERA data), \rightarrow unprecedented improvement on **proton structure determination**

- ▶ Precision measurements of NC/CC with large electroweak contributions
- ▶ $F_2^{\gamma Z} \rightarrow$ Antiquark sea asymmetry ($= 2x [a_u e_u (U - \bar{u}) + a_d e_d (D - \bar{D})]$)
- ▶ u/d ratio at large- x
- ▶ Gluon and quark sea down to $x = 10^{-6}$



Constraining proton structure at LHeC

- ▶ Measurement of heavy flavor SFs, $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ → Important constraints on PDF analysis → Sizable impact on LHC phenomenology (σ_W up by 7% from CTEQ6.1 to CTEQ6.5)
- ▶ LHeC potential for very precision heavy flavour measurements



LHeC/LHC interplay

- ▶ Accurate determination of PDFs at LHeC could improve the new physics measurements and precision studies at the LHC
- ▶ Example I: more accurate $g(x, Q^2)$ at small x at LHeC to more accurate $g(x, Q^2)$ at large x (momentum sum rule) \rightarrow More accurate $d\sigma_{\text{jet}}/dE_T$ at LHC (window to new physics) + better jet energy scale calibration
- ▶ Example II: more accurate $F_2^{c\bar{c}}$ at LHeC \rightarrow More accurate σ_{W^\pm}, σ_Z at LHC \rightarrow Luminosity monitors at 1%?