Neural Network Parton Distributions

Juan Rojo⁵

on behalf of the **NNPDF Collaboration**: R. D. Ball¹, L. Del Debbio¹, S. Forte², A. Guffanti³, J. I. Latorre⁴, A. Piccione², J. R.⁵, M. Ubiali¹

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LHeC 2008 Workshop, Divonne. France



Introduction

- After 40 years of QCD, still issues to be understood in the determination of parton distributions (See yesterday G. Altarelli's talk)
- Problems in standard approach to PDF determination summarized by the 2006 HERA-LHC PDF benchmark analysis
- The NNPDF Collaboration approach is a proposal to overcome various problems in PDF determination with statistically sound techniques
- Important to faithfully estimate impact of PDF behaviour in extrapolation regions as for the LHeC and its potential feedback to LHC
- In this talk → General strategy and results from DIS analysis, (A determination of parton distribution with faithful uncertainty estimation, arxiv:0808.1231)
- See afternoon talk for NNPDF applications to LHeC physics





PDF benchmark analysis

Benchmark partons

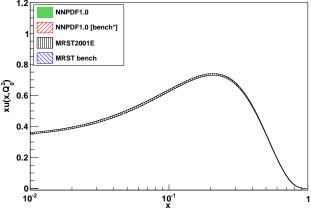
Proposed during the first HERA-LHC workshop → Benchmark PDF fit to a reduced, consistent DIS data set:

Set	$N_{ m dat}$	x_{\min}	x_{max}	Q_{\min}^2	$Q_{\rm max}^2$
BCDMSp	322	$7 \ 10^{-2}$	0.75	10.3	230
NMC	95	0.028	0.48	9	6
NMC-pd	73	0.035	0.67	11.4	99
Z97NC	206	$1.6 \ 10^{-4}$	0.65	10	$2 \ 10^4$
$H197lowQ^2$	77	$3.2 \ 10^{-4}$	0.2	12	150

- Compare results between PDF fitting collaborations and with global fits including more data
- Note for benchmark fit $\Delta\chi^2=1$, while for global fit $\Delta\chi^2_{\rm mrst}=50, \Delta\chi^2_{\rm cteq}=100 \to {\rm Statistical}$ treatment is dataset dependent, also input parametrizations are different

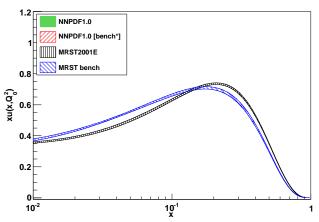


Compare $u(x, Q^2 = 2 \text{ GeV}^2)$ from MRST2001 global PDF determination ...



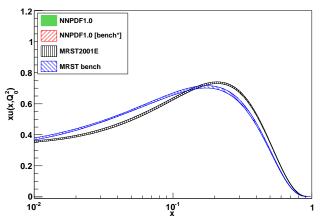


... with MRST HERA-LHC benchmark partons



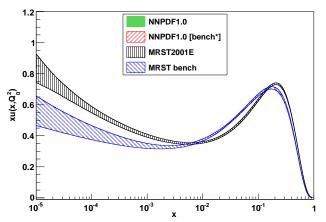


PDFs inconsistent by many $\sigma!$ in data region





Similar inconsistencies in the extrapolation region





Problems in standard PDF determination approach

- Summary of HERA-LHC benchmark fit: Benchmark partons do not agree with global fit partons within uncertainties
- ▶ Implications \rightarrow Both the PDF input parametrization (and flavour assumptions) and the statistical treatment (value of $\Delta\chi^2$) need to be tuned to experimental data set for standard approach
- Situation not satisfactory, specially problematic to predict behaviour of PDFs in extrapolation regions like in the LHeC case
- ► Global fits introduce large tolerances \rightarrow Error blow-up by a factor $S = \sqrt{\Delta\chi^2/2.7}$ (B. Cousins, PDF4LHC) \rightarrow $S_{\rm cteq} \sim$ 6, $S_{\rm mstw} \sim$ 4.5 both in input measurements and in output PDFs
- Need statistically reliable way to determine if such large values of *S* are indeed mandatory. Note $\Delta \chi^2 \sim 1$ in DIS+DY fits (Alekhin)



Benchmark partons

THE NNPDF APPROACH



▶ Generate N_{rep} Monte Carlo replicas $F_i^{(\text{art})(k)}$ of the original data $F_i^{(\text{exp})}$

$$F_i^{(\mathrm{art})(k)} = \left(1 + r_N^{(k)} \sigma_N\right) \left(F_i^{(\mathrm{exp})} + \sum_{p=1}^{N_{\mathrm{sys}}} r_p^{(k)} \sigma_{i,p} + r_i^{(k)} \sigma_{i,s}\right)$$

lacktriangle Evolve each PDF parametrized with Neural Nets $q_lpha^{({
m net})(k)}(x,Q_0^2)$

$$F_i^{(\mathrm{net})(\mathrm{k})}(x,Q^2) = C_{i\alpha}(x,\alpha(Q^2)) \otimes q_{\alpha}^{(\mathrm{net})(k)}\left(x,Q^2\right)$$

ightharpoonup Training: Minimize χ^2 using Genetic Algs. + Dynamical Stopping:

$$\chi^{2(k)} = \frac{1}{N_{\text{dat}}} \sum_{i,j=1}^{N_{\text{dat}}} \left(F_i^{(\text{art})(k)} - F_i^{(\text{net})(k)} \right) \left(\text{cov}_{ij}^{-1} \right) \left(F_j^{(\text{art})(k)} - F_j^{(\text{net})(k)} \right)$$

lacktriangle Set of trained NNs ightarrow Representation of the PDFs probability density

$$\left\langle \mathcal{F}\left[q_{lpha}^{(\mathrm{net})}
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angle =rac{1}{N_{\mathrm{rep}}}\sum_{}^{N_{\mathrm{rep}}}\mathcal{F}\left[q_{lpha}^{-(\mathrm{net})(k)}
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$$\left\langle \mathcal{F} \left[q_{lpha}^{(\mathrm{net})}
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angle = rac{1}{N} - \sum_{k}^{N_{\mathrm{rep}}} \mathcal{F} \left[q_{lpha}^{-(\mathrm{net})(k)}
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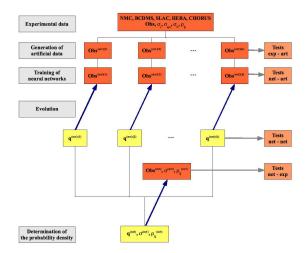
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Dynamical stopping

In a standard fit, look for minimum χ^2 for given parametrization.

- If basis too large → convergence never reached
- ▶ If basis too small → parametrization bias

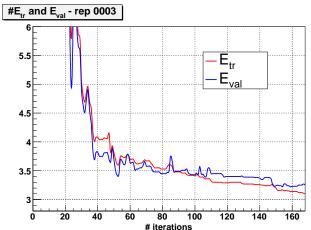
How can one obtain an unbiased compromise? For NNs, smoothness decreases as fit quality improves \rightarrow Stop before fitting statistical noise (overlearning).

- 1. Divide the data set into training and validation sets
- 2. Minimize χ^2 of training set, monitor χ^2 of validation set
- 3. Stop minimization when validation χ^2 begins to rise (overlearning)



Dynamical stopping

Stop minimization when validation χ^2 begins to rise (overlearning)

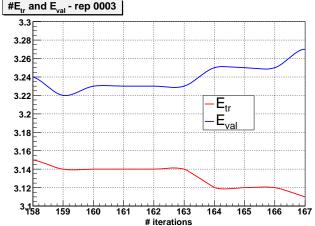




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Dynamical stopping

Stop minimization when validation χ^2 begins to rise (overlearning)



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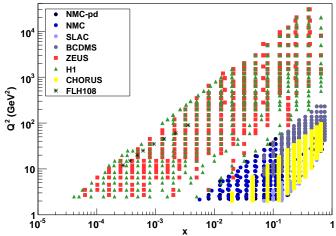


NNPDF1.0 - details

- NNPDF1.0 → PDF set determination from all relevant DIS experimental data (~ 3000 data points)
- ▶ 5 PDFs $(\Sigma(x), V(x), T_3(x), \Delta_S(x))$ and g(x) parametrized with NNs at $Q_0^2 = 2 \text{ GeV}^2$ (37 free params each)
- Valence and momentum sum rules incorporated
- ► Flavour assumptions $\rightarrow s(x) = \bar{s}(x) = C_s/2(\bar{u}(x) + \bar{d}(x))$
- ▶ NLO evolution with ZM-VFN scheme for heavy quarks

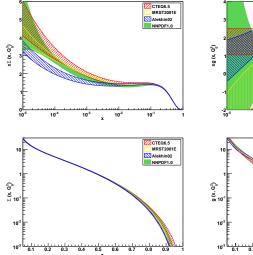


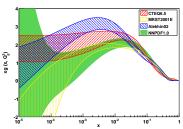
Data set

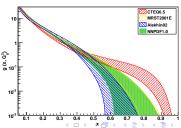




Results - Singlet PDFs



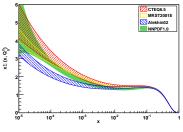


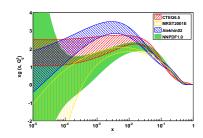




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Results - Singlet PDFs

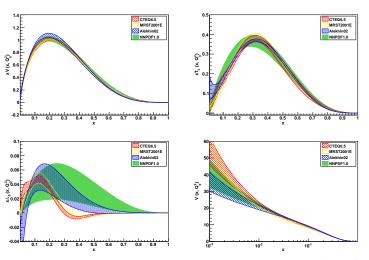




(See also G. Altarelli's plenary talk)

- ► NNPDF1.0 uncertainties faithfully determined
- PDF error larger than other PDF sets in some regions (extrapolation), smaller in others (not artificially inflated by large $\Delta\chi^2 \sim 50/100$)
- ▶ In general close to CTEQ6.5 in data region







Parametrization independence

Quantify statistical differences between PDF sets \rightarrow Distances between two probability distributions which describe two sets of PDFs (i.e. the gluon $\{g_{ik}^{(1)} = g_k^{(1)}(x_i, Q_0^2)\}$):

$$\langle d[g] \rangle = \sqrt{\left\langle \frac{\left(\langle g_i \rangle_{(1)} - \langle g_i \rangle_{(2)}\right)^2}{\sigma^2[g_i^{(1)}] + \sigma^2[g_i^{(2)}]} \right\rangle_{\text{dat}}}$$

 $\langle d[g] \rangle \rightarrow$ Distance between PDF in units of the variance of expectation value $\langle g \rangle$

For statistically equivalent PDF sets: $\langle d[g] \rangle \sim \langle d[\sigma_g] \rangle \sim 1$



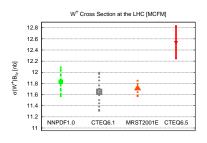
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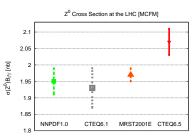
Check stability for NNs arch. from 2-5-3-1 to 2-4-3-1 (6 params less per PDF)

	Data	Extrapolation		
$\Sigma(x,Q_0^2)$	$5 \ 10^{-4} \le x \le 0.1$	$10^{-5} \le x \le 10^{-4}$		
$\langle d[q] \rangle$	0.98	1.25		
$\langle d[\sigma] \rangle$	1.14	1.34		
$g(x, Q_0^2)$	$5 \ 10^{-4} \le x \le 0.1$	$10^{-5} \le x \le 10^{-4}$		
$\langle d[q] \rangle$	1.52	1.15		
$\langle d[\sigma] \rangle$	1.16	1.07		
$T_3(x, Q_0^2)$	$0.05 \le x \le 0.75$	$10^{-3} \le x \le 10^{-2}$		
$\langle d[q] \rangle$	1.00	1.11		
$\langle d[\sigma] \rangle$	1.76	2.27		
$V(x, Q_0^2)$	$0.1 \le x \le 0.6$	$3 \ 10^{-3} \le x \le 3 \ 10^{-2}$		
$\langle d[q] \rangle$	1.30	0.90		
$\langle d[\sigma] \rangle$	1.10	0.98		
$\Delta_S(x,Q_0^2)$	$0.1 \le x \le 0.6$	$3 \ 10^{-3} \le x \le 3 \ 10^{-2}$		
$\langle d[q] \rangle$	1.04	1.91		
$\langle d[\sigma] \rangle$ 1.44		1.80		



Results - Predictions for LHC





	$\sigma_{W^+} \mathcal{B}_{I^+ \nu_I}$	$\Delta \sigma_{W^+}/\sigma_{W^+}$	$\sigma_W - B_{I-\nu_I}$	$\Delta \sigma_{W^-}/\sigma_{W^-}$	$\sigma_Z \mathcal{B}_{I^+I^-}$	$\Delta \sigma_Z / \sigma_Z$
NNPDF1.0	11.83 ± 0.26	2.2%	8.41 ± 0.20	2.4%	1.95 ± 0.04	2.1%
CTEQ6.1	11.65 ± 0.34	2.9%	8.56 ± 0.26	3.0%	1.93 ± 0.06	3.1%
MRST01	11.71 ± 0.14	1.2%	8.70 ± 0.10	1.1%	1.97 ± 0.02	1.0%
CTEQ6.5	12.54 ± 0.29	2.3%	9.19 ± 0.22	2.4%	2.07 ± 0.04	1.9%

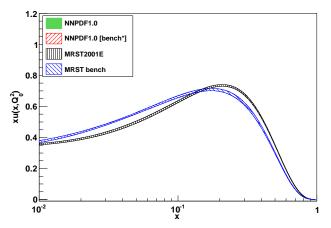


PDF benchmark analysis

- ▶ Does the NNPDF approach solve the problem with MRST benchmark partons?
- Compare NNPDF1.0 partons with a PDF set obtained from the reduced data set of the HERA-LHC workshop
- For a complete NNPDF version of the HERA-LHC PDF benchmark, see A. Piccione's talk at PDF4LHC later this week

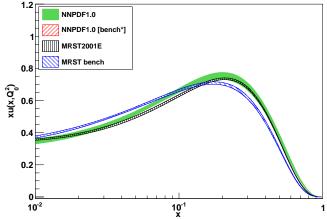


PDFs inconsistent by many $\sigma!$ in data region in standard approach ...



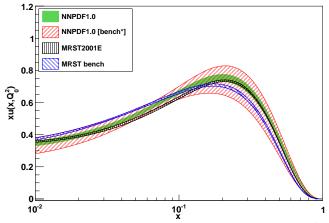


... but not within the NNPDF approach: Full DIS fit

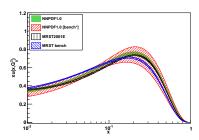




... but not within the NNPDF approach: Benchlike fit



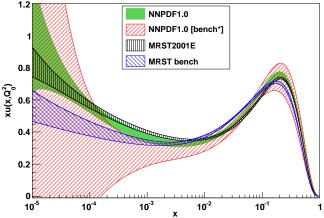




- NNPDF1.0 consistent with MRST global fit
- NNPDF benchlike consistent with both NNPDF1.0 and MRST global and benchmark fits
- Error determination understimated in standard aproach to PDF determination (central values ok)

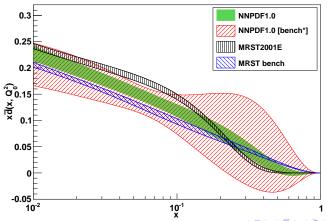


Problems also cured in (low-x) extrapolation region



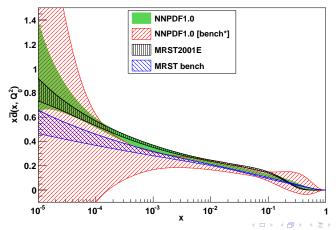


Same for other PDFs - $\bar{d}(x, Q_0^2)$ in data region



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Same for other PDFs - $\bar{d}(x, Q_0^2)$ in extrapolation region



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OUTLOOK



Outlook

- ► NNPDF1.0 → DIS NNPDF set completed and available from the LHAPDF interface
- ► Faithful determination of uncertainties → Suited to studies in extrapolation regions like LHeC (see afternoon's talk) and for its feedback to precision LHC physics
- Work in progress to add hadronic data and heavy quark effects, and detailed studies of PDF uncertainty impact on LHC physics

Thanks for your attention!



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Thanks for your attention!



Outlook

Neural Network Parton Distributions



Dependence with preprocessing

R. Thorne, HERA-LHC 2006 proceedings

errors, but these are relatively small. However, the partons extracted using a very limited data set are completely incompatible, even allowing for the uncertainties, with those obtained from a global fit with an identical treatment of errors and a minor difference in theoretical procedure. This implies that the inclusion of more data from a variety of different experiments moves the central values of the partons in a manner indicating either that the different experimental data are inconsistent with each other, or that the theoretical framework is inadequate for correctly describing the full range of data. To a certain extent both explanations are probably true. Some data sets are not entirely consistent with each other (even if they are seemingly equally reliable). Also, there are a wide variety of reasons why NLO perturbative QCD might require modification for some data sets, or in some kinematic regions [89]. Whatever the reason for the inconsistency between the MRST benchmark partons and the MRST01 partons, the comparison exhibits the dangers in extracting partons from a very limited set of data and taking them seriously. It also clearly illustrates the problems in determining the true uncertainty on parton distributions.



Problems in standard PDF determination approach

- Consensus (PDF4LHC workshop): serious problem in PDF fits
- Problem summarized by the HERA-LHC benchmark fit: Benchmark partons do not agree with global fit partons within errors
- Implications → either experiments are incompatible, or parametrizations not flexible enough, or both
- ▶ Global fit solution → Error blow-up by a factor $S = \sqrt{\Delta \chi^2/2.7}$ (B. Cousins, PDF4LHC) → $S_{\rm cteq} \sim$ 6, $S_{\rm mstw} \sim$ 4.5 both in input measurements and in output PDFs (very large!)
- Need statistically reliable way to determine if such large values of S are indeed mandatory. Note $\Delta \chi^2 \sim 1$ in DIS+DY fits (Alekhin)



Experimental data set

Experiment	Set	$N_{ m dat}$	x_{\min}	x_{max}	Q_{\min}^2	$Q_{\rm max}^2$	σ_{tot} (%)	F	Ref.
SLAC									
	SLACp	211 (47)	.07000	.85000	0.6	29.	3.6	F_2^P F_2^d	[51]
BCDMS	SLACd	211 (47)	.07000	.85000	0.6	29.	3.2	F_2^a	[51]
BODMS	BCDMSp	351 (333)	.07000	.75000	7.5	230.	5.5	F_2^p F_2^d F_2^p	[47]
	BCDMSd	254 (248)	.07000	.75000	8.8	230.	6.6	$F_2^{\bar{d}}$	[48]
NMC		288 (245)	.00350	.47450	0.8	61.	5.0		[50]
NMC-pd		260 (153)	.00150	.67500	0.2	99.	2.1	F_{2}^{d}/F_{2}^{p}	[49]
ZEUS								+	
	Z97lowQ2	80	.00006	.03200	2.7	27.	4.9	$\tilde{\sigma}^{NC,e^+}$	[56]
	Z97NC	160	.00080	.65000	35.0	20000.	7.7	$\tilde{\sigma}^{NC,e^+}$	[56]
	Z97CC	29	.01500	.42000	280.0	17000.	34.2	$\tilde{\sigma}^{CC,e^+}$	[57]
	Z02NC	92	.00500	.65000	200.0	30000.	13.2	$\tilde{\sigma}^{NC,e}$	[58]
	Z02CC	26	.01500	.42000	280.0	30000.	40.2	$\tilde{\sigma}^{CC,e}$	[59]
	Z03NC	90	.00500	.65000	200.0	30000.	9.1	$\tilde{\sigma}^{NC,e^+}$	[60]
	Z03CC	30	.00800	.42000	280.0	17000.	31.0	$\tilde{\sigma}^{CC,e+}$	[61]
H1									
	H197mb	67 (55)	.00003	.02000	1.5	12.	4.9	$\tilde{\sigma}^{NC,e^+}$	[52]
	H197lowQ2	80	.00016	.20000	12.0	150.	4.2	$\tilde{\sigma}^{NC,e+}$	[52]
	H197NC	130	.00320	.65000	150.0	30000.	13.3	$\tilde{\sigma}^{NC,e^+}$	[53]
	H197CC	25	.01300	.40000	300.0	15000.	29.8	$\tilde{\sigma}^{CC,e}$	[53]
	H199NC	126	.00320	.65000	150.0	30000.	15.5	$\tilde{\sigma}^{NC,e^-}$	[54]
	H199CC	28	.01300	.40000	300.0	15000.	27.6	$\bar{\sigma}^{CC,e}$	[54]
	H199NChv	13	.00130	.01050	100.0	800.	9.2	$\bar{\sigma}^{NC,e}$	[55]
	H100NC	147	.00131	.65000	100.0	30000.	10.4	$\bar{\sigma}^{NC,e^+}$	[55]
	H100CC	28	.01300	.40000	300.0	15000.	21.8	$\bar{\sigma}^{CC,e+}$	[55]
CHORUS	1110000	20	.01300	.40000	555.0	10000.	21.0		[00]
	$\text{CHORUS}\nu$	607 (471)	.02000	.65000	0.3	95.	11.2	$\tilde{\sigma}^{\nu}_{\bar{\nu}}$	[63]
FLH108	$CHORUS\bar{\nu}$	607 (471) 8	.02000	.65000	0.3 12.0	95. 90.	18.7 69.2	$\tilde{\sigma}^{\bar{\nu}}$ F_L	[63] [62]
Total		3948 (3161)	.00028	.00360	12.0	90.	09.2	r _L	[02]



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Statistical estimators

$\chi^2_{ m tot}$	1.34
$\langle E \rangle$	2.71
$\langle E_{ m tr} angle$	2.68
$\langle \mathit{E}_{\mathrm{val}} angle$	2.72
$\langle { m TL} angle$	824
$\langle \sigma^{(exp)} \rangle_{dat}$ $\langle \sigma^{(net)} \rangle_{dat}$	$5.6 \ 10^{-2}$
	$1.4 \ 10^{-2}$
$\langle \rho^{(exp)} \rangle_{dat}$	0.15
$\langle ho^{ m (net)} angle_{ m dat}$	0.40
$\langle \text{cov}^{(exp)} \rangle_{det}$	$1.0 \ 10^{-3}$
$\langle \text{cov}^{\text{(net)}} \rangle_{\text{dat}}^{\text{dat}}$	$1.6 \ 10^{-4}$

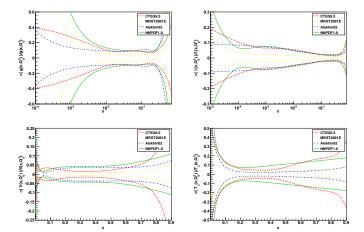


Dependence with preprocessing

Data region								
	$n_v = 0.1$	$n_v = 0.5$	$m_v = 2$	$m_v = 4$	$n_s = 0.8$	$n_s = 1.6$	$m_s = 2$	$m_s = 4$
$\Sigma(x, Q_0^2)$								
$\langle d[q] \rangle$	1.34	1.25	1.37	2.14	1.72	1.38	1.45	1.64
$\langle d[\sigma] \rangle$	1.45	1.44	1.25	1.44	2.03	2.66	0.95	1.35
$g(x, Q_0^2)$								
$\langle d[q] \rangle$	1.31	1.30	2.69	1.15	3.06	2.08	1.20	1.74
$\langle d[\sigma] \rangle$	1.34	1.60	1.56	1.37	3.21	2.44	0.98	1.72
$T_3(x, Q_0^2)$								
$\langle d[q] \rangle$	1.97	2.48	8.35	9.74	1.31	3.23	1.03	1.41
$\langle d[\sigma] \rangle$	1.10	1.47	1.98	1.53	1.10	2.66	1.76	1.99
$V(x, Q_0^2)$								
$\langle d[q] \rangle$	11.03	1.55	3.61	5.60	0.94	2.12	1.25	3.54
$\langle d[\sigma] \rangle$	3.57	4.74	4.04	3.09	1.03	1.10	0.66	1.98
$\Delta_S(x, Q_0^2)$								
$\langle d[q] \rangle$	2.00	2.29	7.51	2.36	1.14	1.70	0.76	0.92
$\langle d[\sigma] \rangle$	1.25	5.20	1.17	3.50	1.00	1.98	0.97	2.05
Extrapolation								
	$n_v = 0.1$	$n_v = 0.5$	$m_v = 2$	$m_v = 4$	$n_s = 0.8$	$n_s = 1.6$	$m_s = 2$	$m_s = 4$
$\Sigma(x, Q_0^2)$							$m_s = z$	$m_s = 4$
$\omega(x,Q_0)$	No - 0.1						$m_s = z$	$m_8 = 4$
$\langle d[q] \rangle$	1.06	1.69	1.49	1.84	7.72	4.67	0.87	3.15
			1.49 2.11	1.84 1.52				
$\langle d[q] \rangle$	1.06	1.69			7.72	4.67	0.87	3.15
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$	1.06	1.69			7.72	4.67	0.87	3.15
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$	1.06 1.12	1.69 1.84	2.11	1.52	7.72 2.47	4.67 3.66	0.87 0.82	3.15 2.34
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$	1.06 1.12	1.69 1.84	2.11	1.52	7.72 2.47	4.67 3.66 4.73	0.87 0.82	3.15 2.34 3.49
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$	1.06 1.12	1.69 1.84	2.11	1.52	7.72 2.47	4.67 3.66 4.73	0.87 0.82	3.15 2.34 3.49
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $T_3(x, Q_0^2)$	1.06 1.12 1.41 1.41	1.69 1.84 2.32 1.86	2.11 2.33 1.95	1.52 1.34 1.30	7.72 2.47 1.62 2.15	4.67 3.66 4.73 2.72	0.87 0.82 1.04 0.81	3.15 2.34 3.49 2.38
$ \begin{array}{c} \langle d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \\ g(x,Q_0^2) \\ \langle d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ T_3(x,Q_0^2) \\ \langle d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \end{array} $	1.06 1.12 1.41 1.41 1.71	1.69 1.84 2.32 1.86	2.11 2.33 1.95 7.40	1.52 1.34 1.30	7.72 2.47 1.62 2.15	4.67 3.66 4.73 2.72	0.87 0.82 1.04 0.81	3.15 2.34 3.49 2.38
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $T_3(x, Q_0^2)$ $\langle d[q] \rangle$	1.06 1.12 1.41 1.41 1.71	1.69 1.84 2.32 1.86	2.11 2.33 1.95 7.40	1.52 1.34 1.30	7.72 2.47 1.62 2.15	4.67 3.66 4.73 2.72	0.87 0.82 1.04 0.81	3.15 2.34 3.49 2.38
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $T_3(x, Q_0^2)$ $\langle d[\sigma] \rangle$ $\langle d[\sigma] \rangle$ $V(x, Q_0^2)$	1.06 1.12 1.41 1.41 1.71 4.83	1.69 1.84 2.32 1.86 2.70 4.54	2.33 1.95 7.40 2.89	1.52 1.34 1.30 1.60 5.09	7.72 2.47 1.62 2.15 1.36 1.00	4.67 3.66 4.73 2.72 2.37 1.65	0.87 0.82 1.04 0.81 0.78 0.92	3.15 2.34 3.49 2.38 0.91 1.26
$\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $g(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $T_3(x, Q_0^2)$ $\langle d[q] \rangle$ $\langle d[\sigma] \rangle$ $\langle d[\sigma] \rangle$ $\langle d[\sigma] \rangle$ $\langle d[\sigma] \rangle$	1.06 1.12 1.41 1.41 1.71 4.83	1.69 1.84 2.32 1.86 2.70 4.54	2.11 2.33 1.95 7.40 2.89	1.52 1.34 1.30 1.60 5.09	7.72 2.47 1.62 2.15 1.36 1.00	4.67 3.66 4.73 2.72 2.37 1.65	0.87 0.82 1.04 0.81 0.78 0.92	3.15 2.34 3.49 2.38 0.91 1.26
$ \begin{array}{c} \langle d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ g(x,Q_0^{\sigma}) \\ \\ d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ T_3(x,Q_0^{\sigma}) \\ \langle d[q] \rangle \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \langle d[\sigma] \rangle \\ \langle d[\sigma] \rangle \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \\ \langle d[\sigma] \rangle \\ \end{array} $	1.06 1.12 1.41 1.41 1.71 4.83	1.69 1.84 2.32 1.86 2.70 4.54	2.11 2.33 1.95 7.40 2.89	1.52 1.34 1.30 1.60 5.09	7.72 2.47 1.62 2.15 1.36 1.00	4.67 3.66 4.73 2.72 2.37 1.65	0.87 0.82 1.04 0.81 0.78 0.92	3.15 2.34 3.49 2.38 0.91 1.26

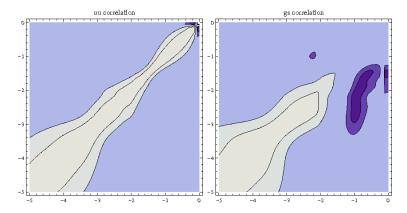


Results - PDF uncertainties





Parton correlations



Compute parton-parton correlations using textbook statistics

$$\rho\left[q(x_1,Q_1^2)\widetilde{q}(x_2,Q_2^2)\right] = \frac{\left\langle q(x_1,Q_1^2)\widetilde{q}(x_2,Q_2^2)\right\rangle_{\mathrm{rep}} - \left\langle q(x_1,Q_1^2)\right\rangle_{\mathrm{rep}} \left\langle \widetilde{q}(x_2,Q_2^2)\right\rangle_{\mathrm{rep}}}{\sigma_q(x_1,Q_1^2)\sigma_{\widetilde{q}}(x_2,Q_2^2)} \;,$$

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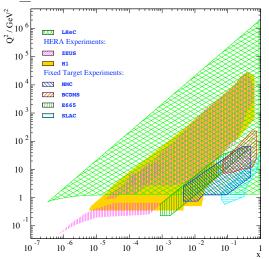
PRECISION QCD AT THE LHeC

References:

J. Dainton et al., *Deep Inelastic Electron-Nucleon Scattering at the LHC*, JINST 1 10001



Precision QCD at the LHeC

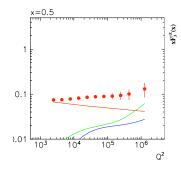


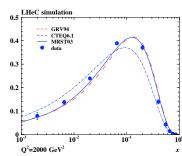


Constraining proton structure at LHeC

LHeC (+ final HERA data), \rightarrow unprecedent improvement on proton structure determination

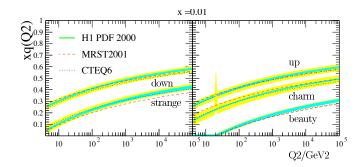
- Precision measurements of NC/CC with large electroweak contributions
- $ightharpoonup F_2^{\gamma Z}
 ightarrow ext{Antiquark sea asymmetry} \ (= 2x \left[a_u e_u (U bar U) + a_d e_d (D \bar{D}) \right]$
- \triangleright u/d ratio at large-x
- ▶ Gluon and quark sea down to $x = 10^{-6}$





Constraining proton structure at LHeC

- ▶ Measurement of heavy flavor SFs, $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ → Important constraints on PDF analysis → Sizable impact on LHC phenomenology (σ_W up by 7% from CTEQ6.1 to CTEQ6.5)
- LHeC potential for very precision heavy flavour measurements





LHeC/LHC interplay

- Accurate determination of PDFs at LHeC could improve the new physics measurements and precision studies at the LHC
- ► Example I: more accurate $g(x,Q^2)$ at small x at LHeC to more accurate $g(x,Q^2)$ at large x (momentum sum rule) \rightarrow More accurate $d\sigma_{\rm jet}/dE_T$ at LHC (window to new physics) + better jet energy scale calibration
- ► Example II: more accurate $F_2^{c\bar{c}}$ at LHeC \rightarrow More accurate $\sigma_{W^{\pm}}, \sigma_Z$ at LHC \rightarrow Luminosity monitors at 1%?

