

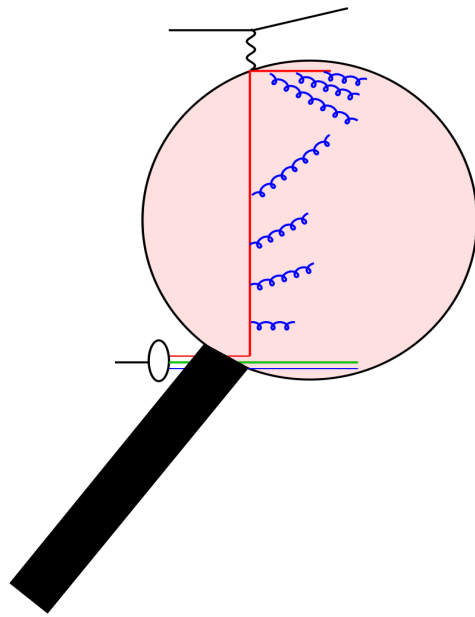
# Small $x$ parton dynamics

H. Jung (DESY)

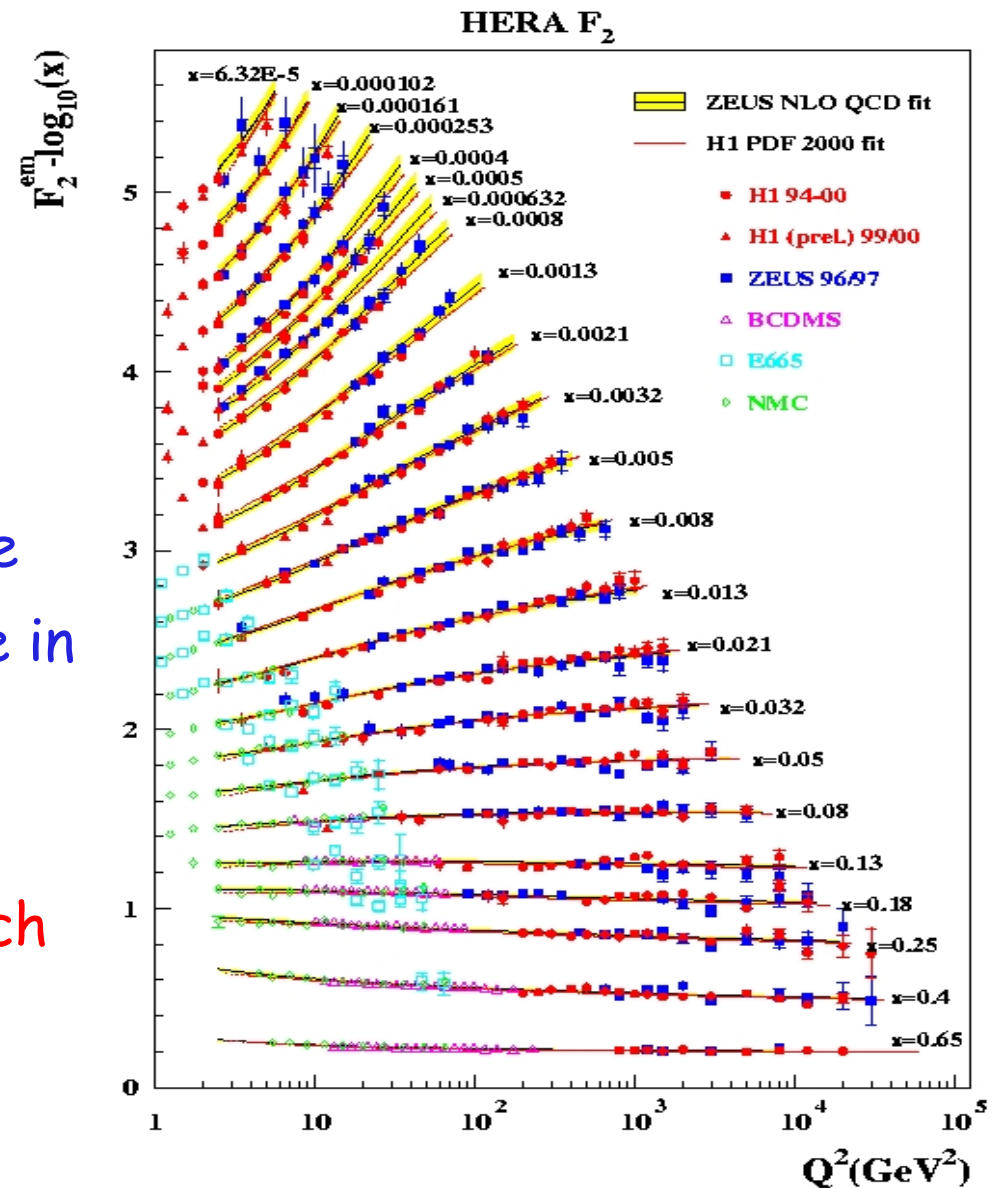
- What did we learn from HERA ?
- What is still open ?
- Where LHeC could contribute ?

# The fun with ep scattering

$$\sigma(e^+p \rightarrow e^+X) = \sum f_i(x, Q^2) \sigma(e^+q_i \rightarrow e^+q_i)$$



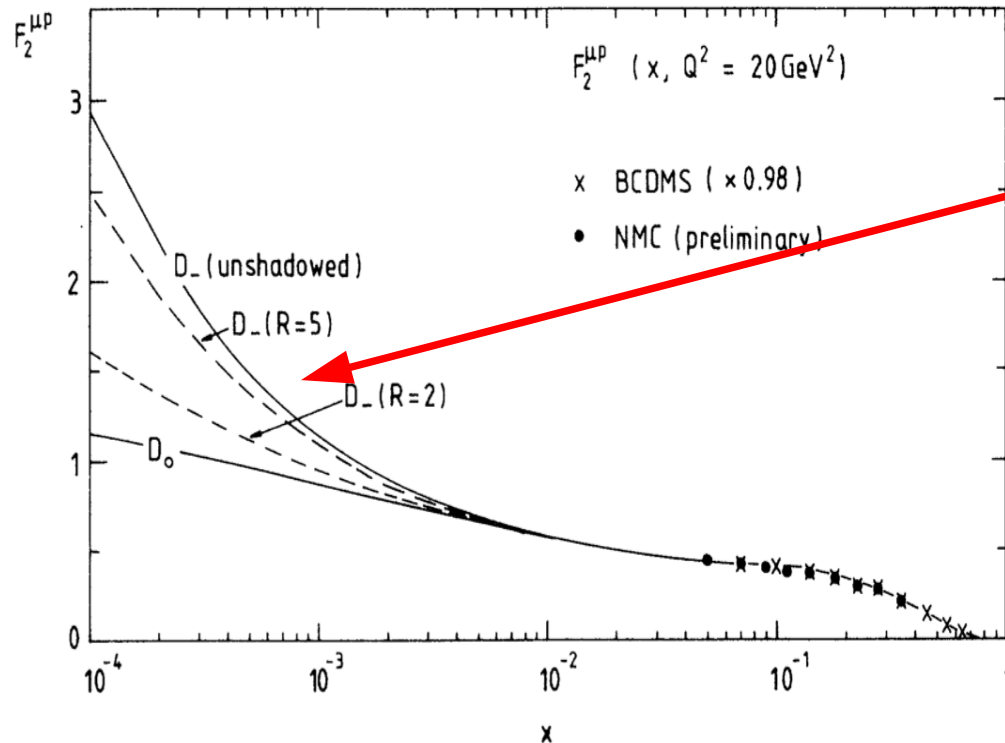
- perfect description of precise measurements of **HUGE** range in  $x$  and  $Q^2$
- Theory works well.....
- ➔ extract parton densities, which are universal
- ➔ to be used at LHC.....



# Remember the pre-HERA times

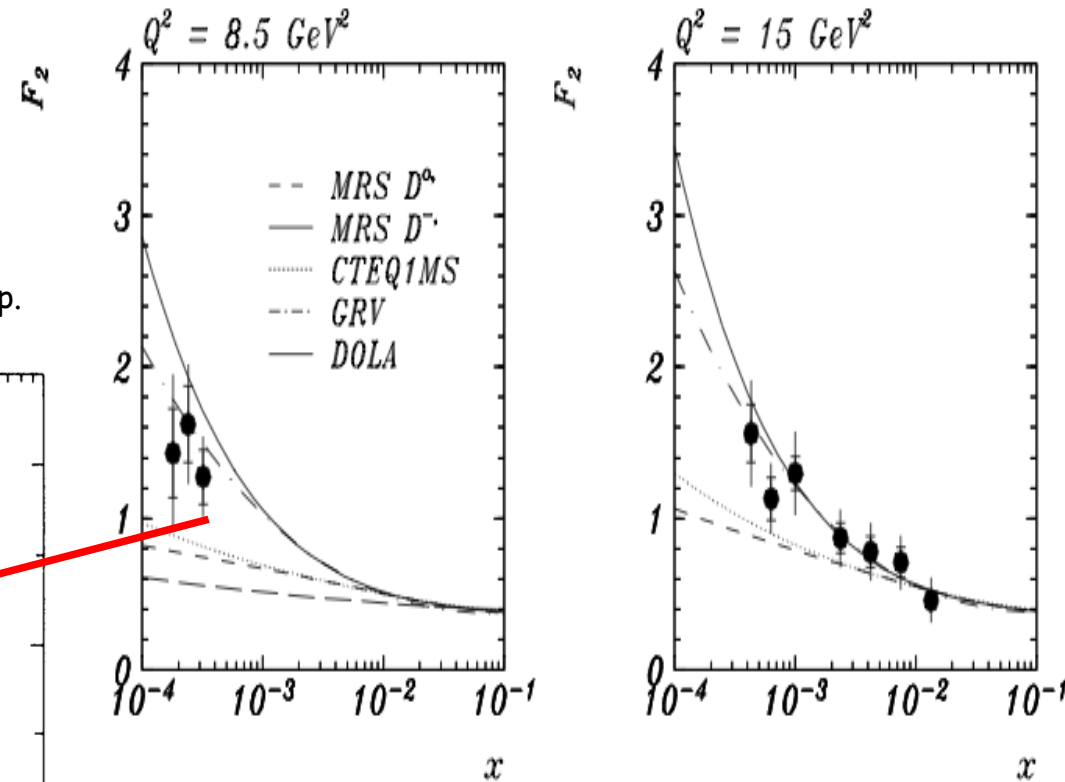
- Just before HERA started in 1992, new PDF fits (NLO DGLAP) were released, using all existing high precision data

Martin, Stirling, Roberts Apr 1992. 49pp.  
Phys.Rev.D47:867-882,1993.



- 1<sup>st</sup> HERA data 1992

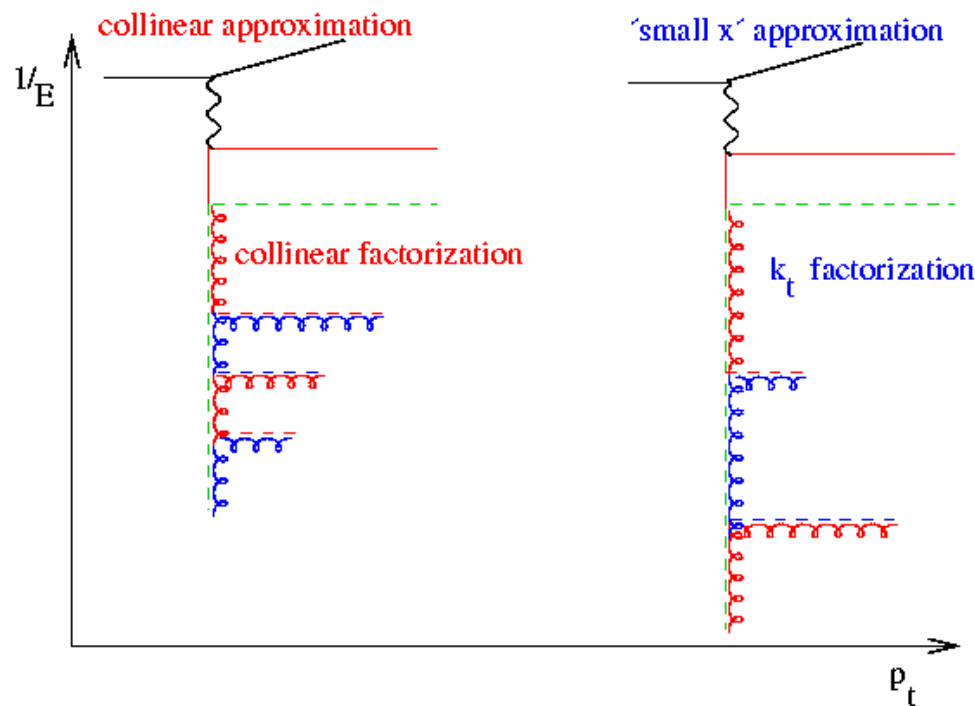
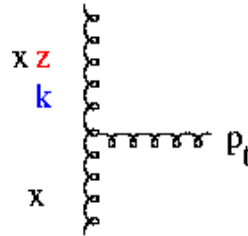
H1 Nucl. Phys. B407 (1993) 515



# Theory recap: what are we doing ?

gluon bremsstrahlung

$$\sim \frac{1}{k^2} \left( \frac{1}{z} + \dots \right)$$



**D**okshitzer **G**ribov **L**ipatov **A**ltarelli **P**arisi

- collinear singularities factorized in pdf
- evolution in  $Q^2 \sim k^2$ , or  $k_t^2$  or ?

$$\sigma = \sigma_0 \int \frac{dz}{z} C^a \left( \frac{x}{z} \right) f_a(z, Q^2)$$

**B**alitski **F**adin **K**uraev **L**ipatov

- $k_t$  dependent pdf  $\rightarrow$  unintegrated pdf

- evolution in  $x$

$$\sigma = \int \frac{dz}{z} d^2 k_t \hat{\sigma} \left( \frac{x}{z}, k_t \right) \mathcal{F}(z, k_t)$$

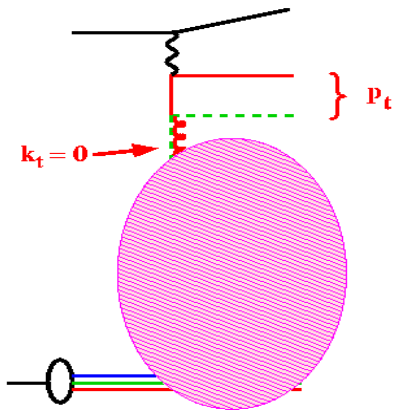
# Questions from this ...

- Strong rise of structure function at small  $x$ :
  - where is it coming from ?
    - typical BFKL behavior ?
    - or
    - steep starting distribution at which scale ?
    - or
    - generated dynamically from a small scale (GRV ansatz) ?
- if high parton density at small  $x$ , do we also observe saturation and parton recombination
- How is initial state parton cascade generated ?

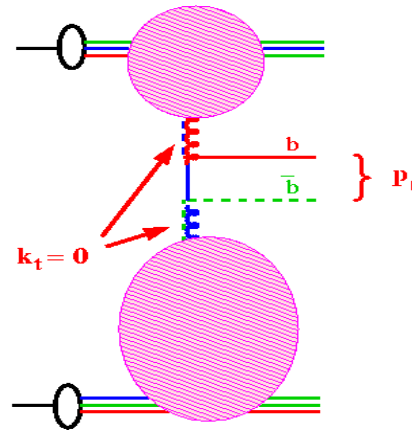
# Problems in Collinear Approximation

J. Collins, H. Jung hep-ph/0508280

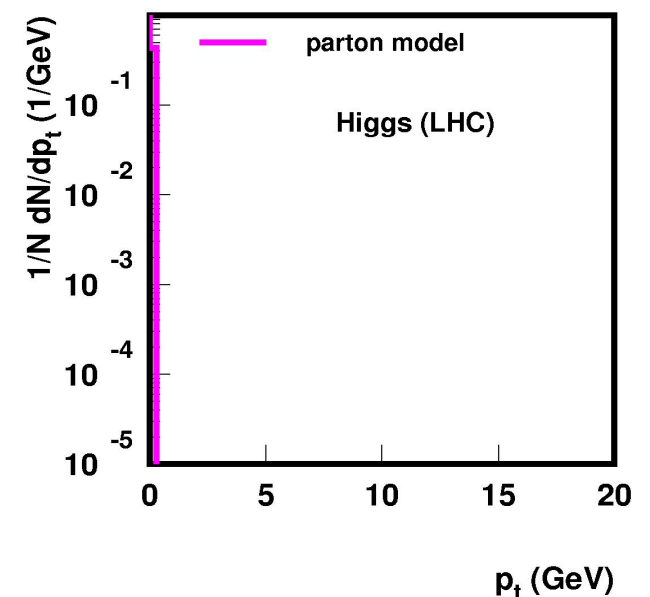
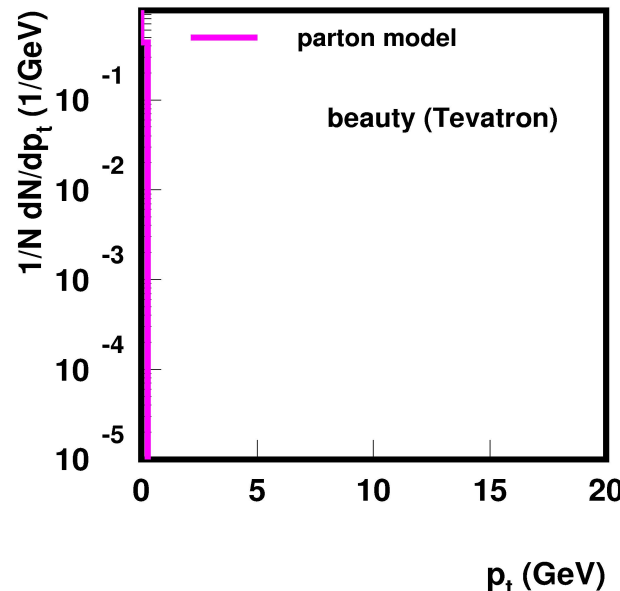
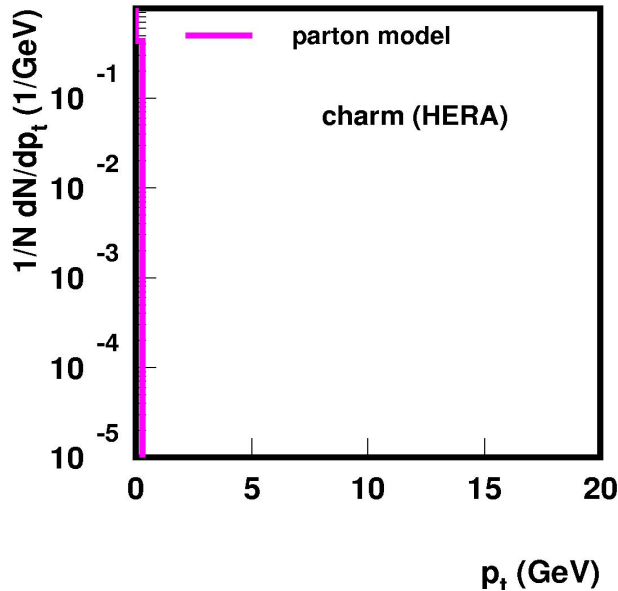
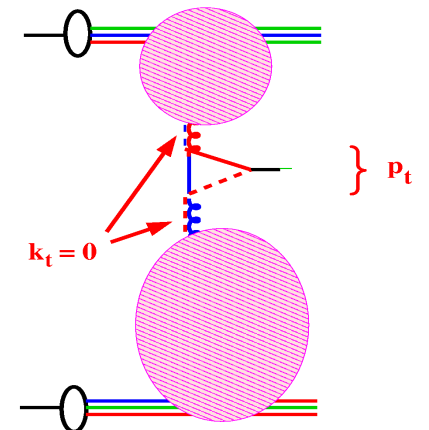
heavy quarks at HERA



heavy quarks in



Higgs in pp

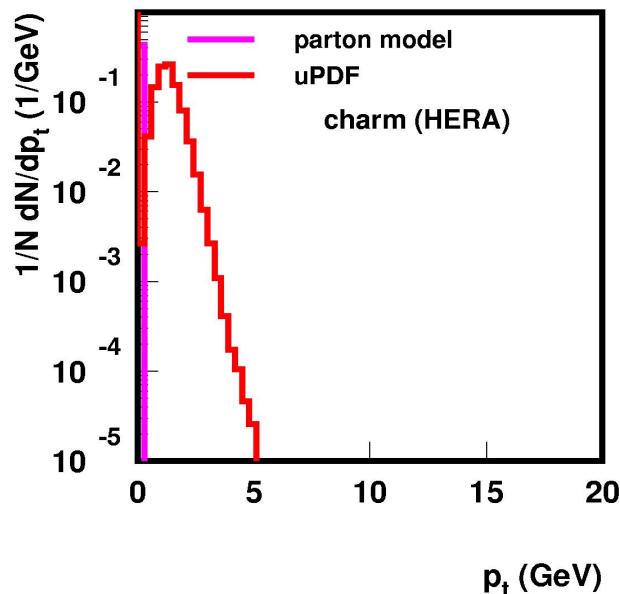
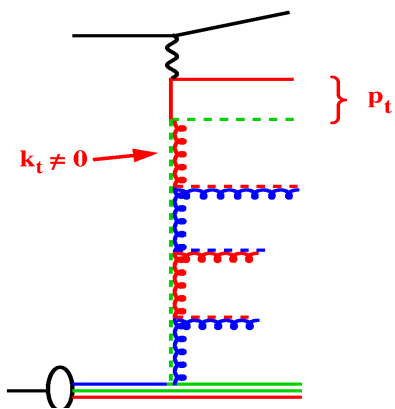


➔ NLO corrections will be very large for these LO processes .....

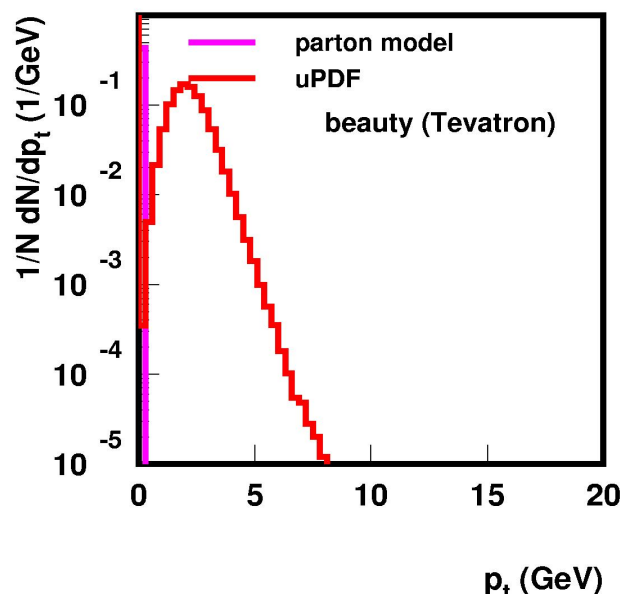
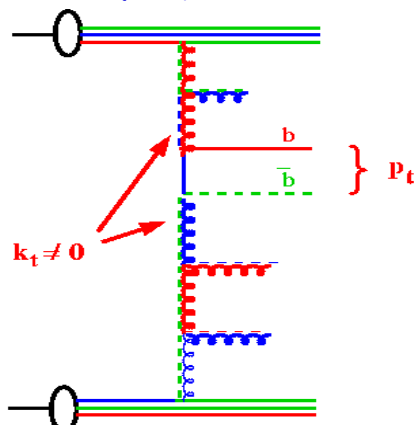
# Doing much better with uPDFs ...

J. Collins, H. Jung hep-ph/0508280

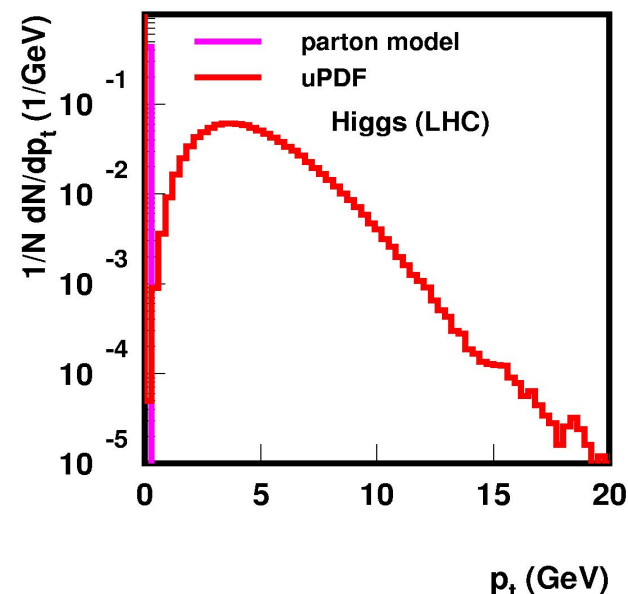
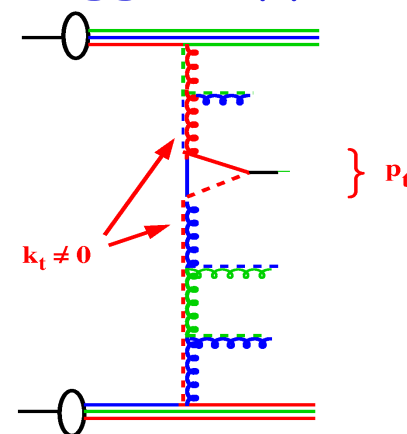
## heavy quarks at HERA



## heavy quarks in



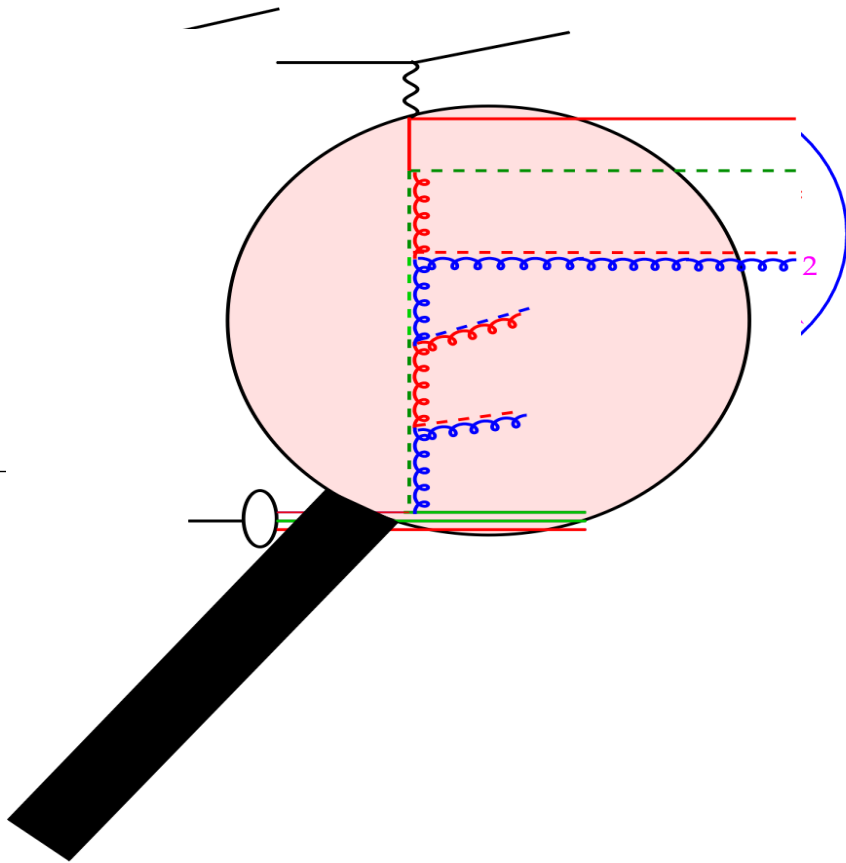
## Higgs in pp



→ doing kinematics correct at LO, reduces NLO corrs,.... NEED uPDFs !!!!

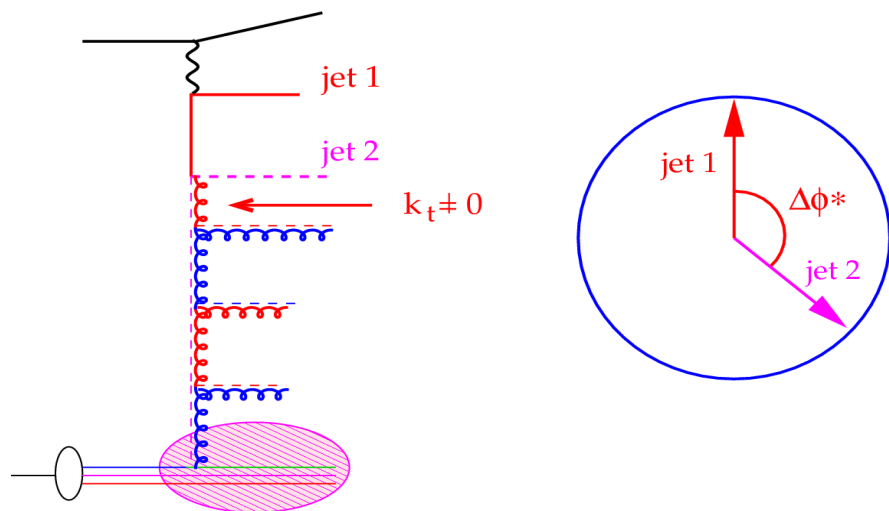
# Walking down the ladder ...

- H1 prel data  $5 < Q^2 < 100 \text{ GeV}^2$   
 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$



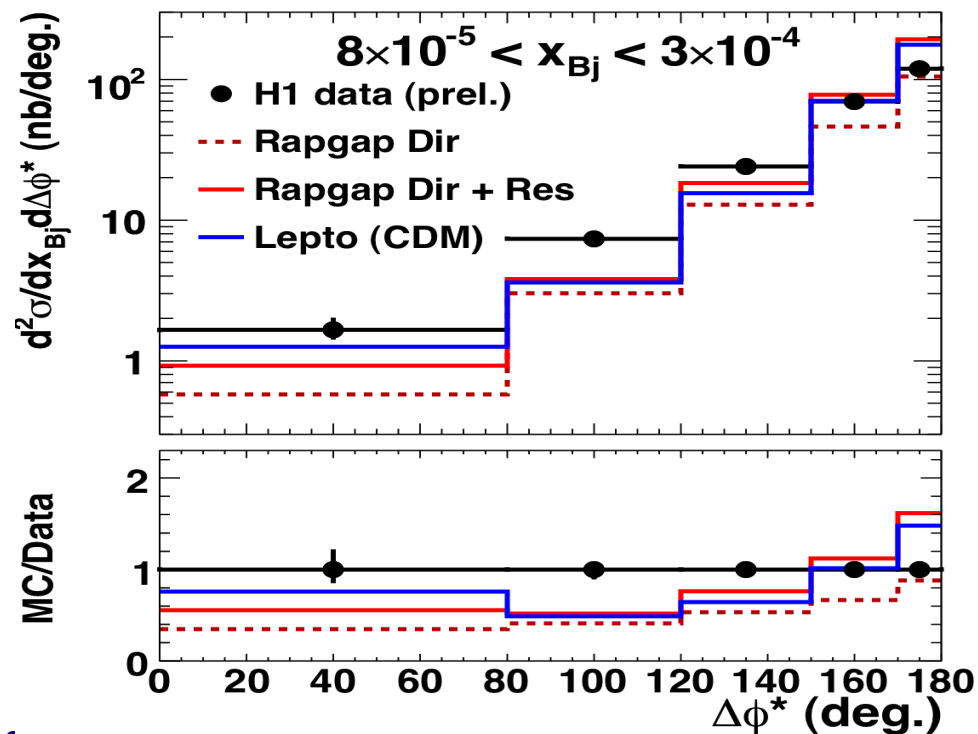
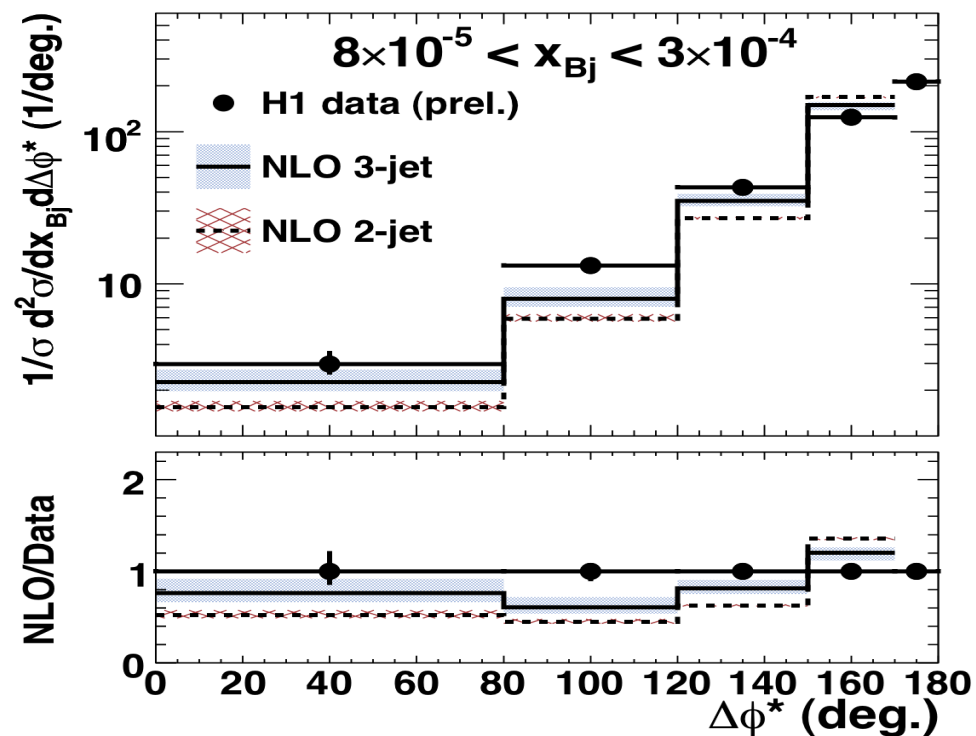


# Walking down the ladder ...



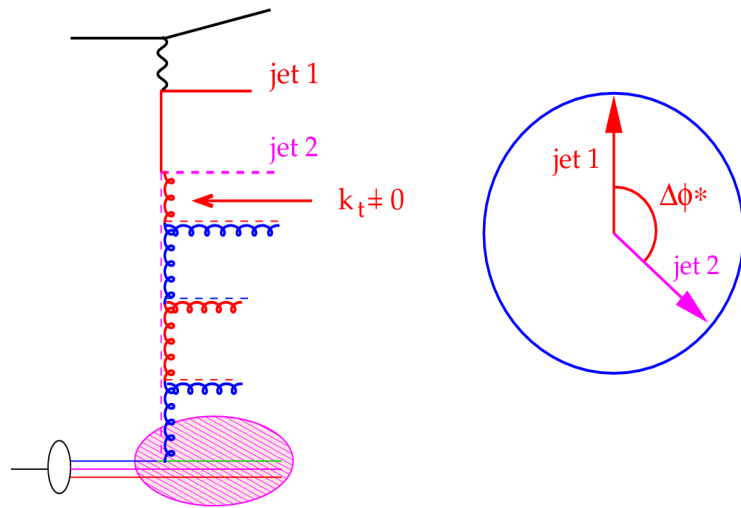
- H1 prel data  $5 < Q^2 < 100 \text{ GeV}^2$   
 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$

→ None of the calculations can describe measurements !!!



# uPDFs from di-jets: $k_{\perp}$ -dependence

Hansson, Jung arXiv:0707.4276

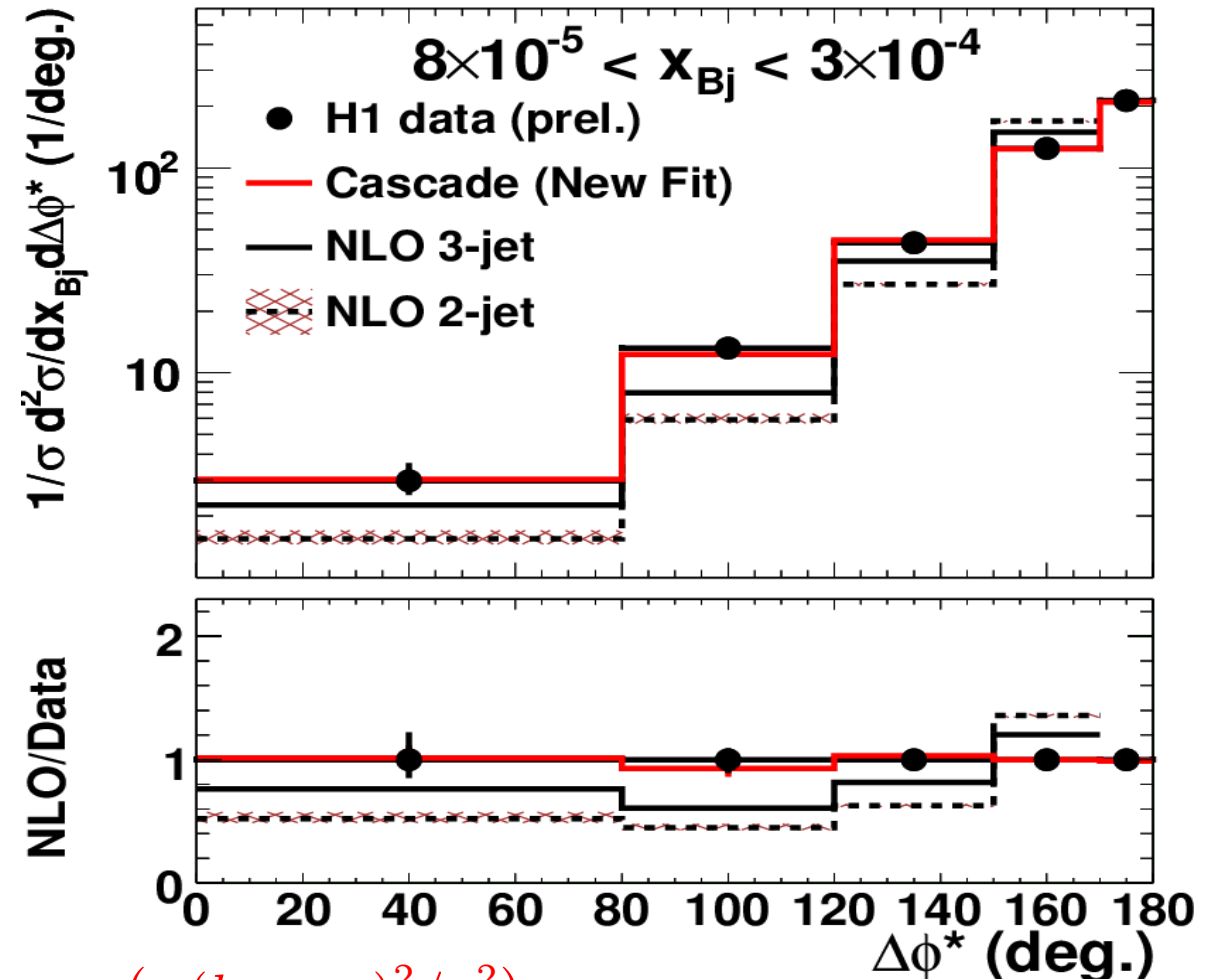


- H1 prel data  
 $5 < Q^2 < 100 \text{ GeV}^2$   
 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$

- determine small  $k_{\perp}$  region with

$$x\mathcal{A}(x, \mu_0^2) = Nx^{-B_g} \cdot (1-x)^4 \cdot \exp\left(-\frac{(k_{t0} - \mu)^2}{\sigma^2}\right)$$

- large  $k_{\perp}$  from evolution



→ perfect description of shape and rate

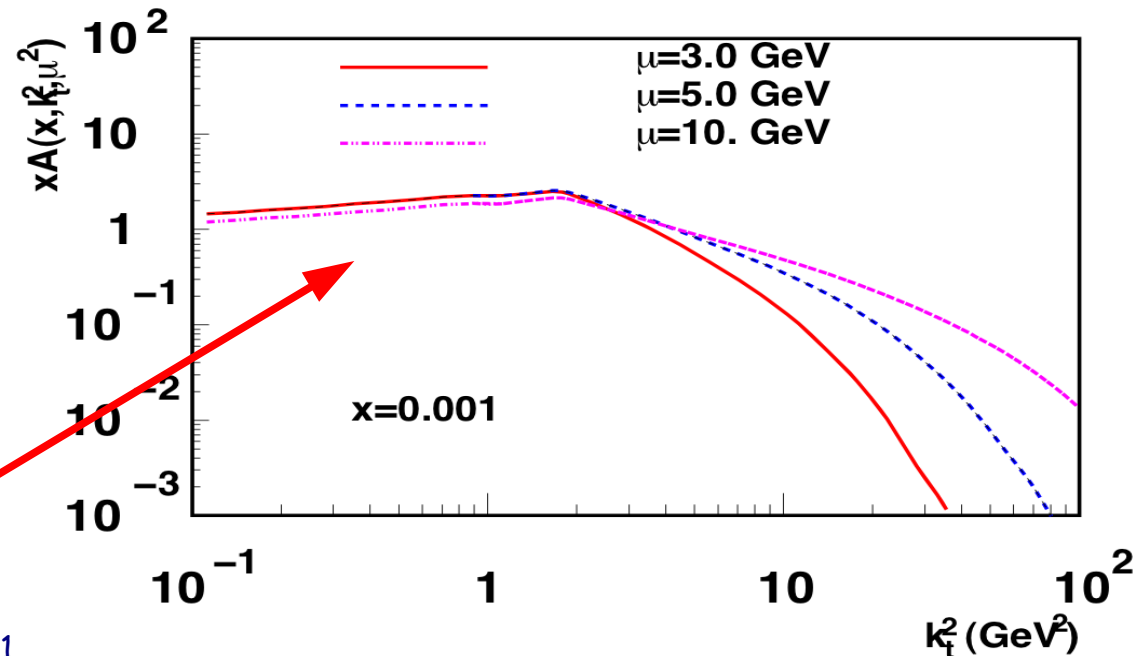
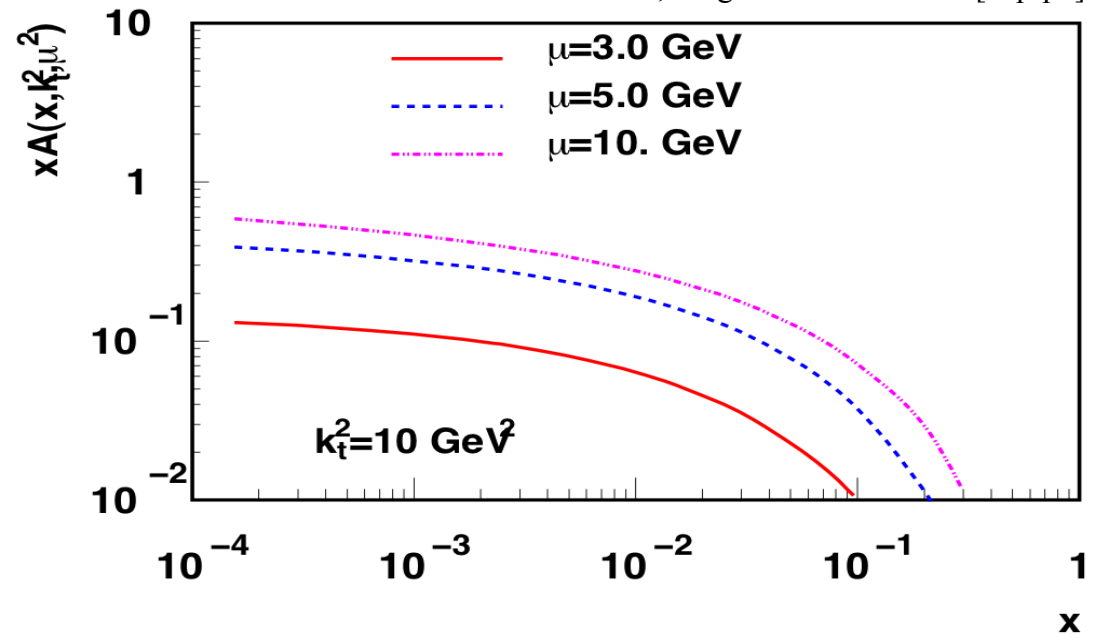
# uPDFs from di-jets: intrinsic $k_{\perp}$

$$x\mathcal{A}(x, k_{\perp}, \bar{q}) = \int dx_0 \mathcal{A}_0(x_0, \mu_0) \times \frac{x}{x_0} \tilde{\mathcal{A}}\left(\frac{x}{x_0}, k_{\perp}, \bar{q}\right)$$

- different intrinsic  $k_{\perp}$ -distributions only **accessible** in **uPDFs**
- **sensitive to the mix of small and large  $k_{\perp}$**
- small  $k_{\perp}$  determines total  $x$ -section
- large  $k_{\perp}$  influences perturbative tails ...

**BUT**

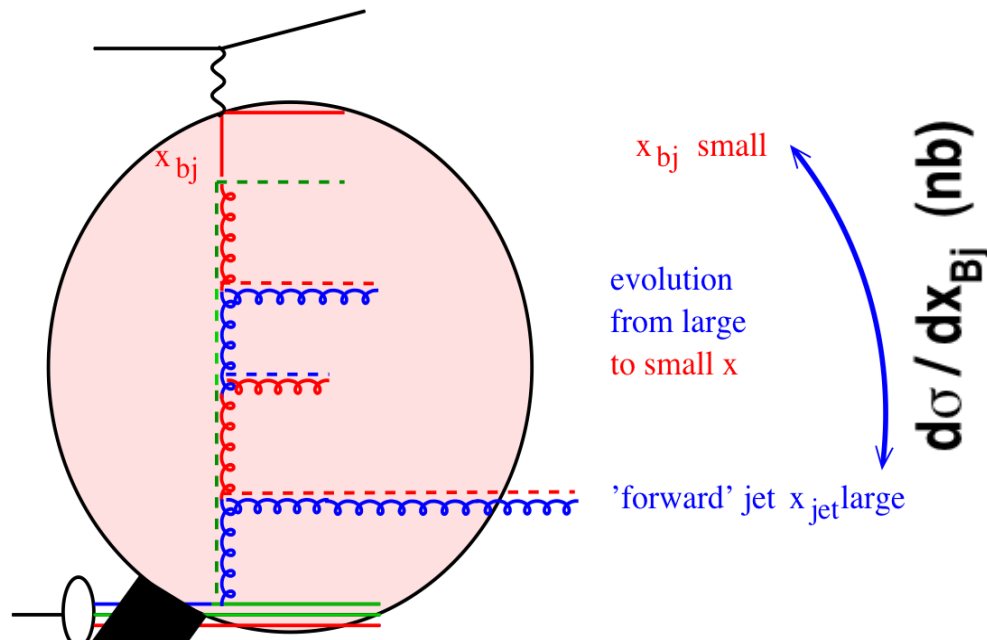
Hautmann, Jung arXiv:0712.0568 [hep-ph]



# Looking forward ...

H1, Eur.Phys.J.C46:27-42,2006.

## H1 forward jet data



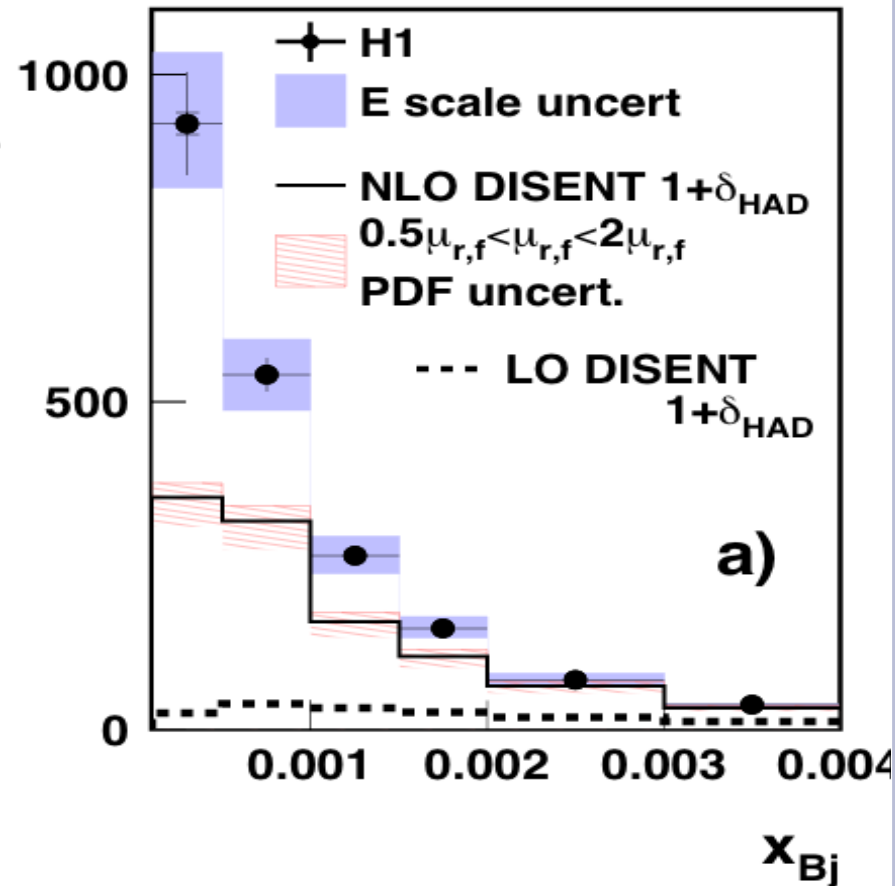
- DIS and forward jet:

$$1.7 < \eta_{jet} < 2.8$$

$$x_{jet} > 0.035$$

$$0.5 < \frac{p_{t,jet}^2}{Q^2} < 5$$

$$\sigma(\text{fwd jet}) / \sigma(\text{DIS}) \sim 1\%$$

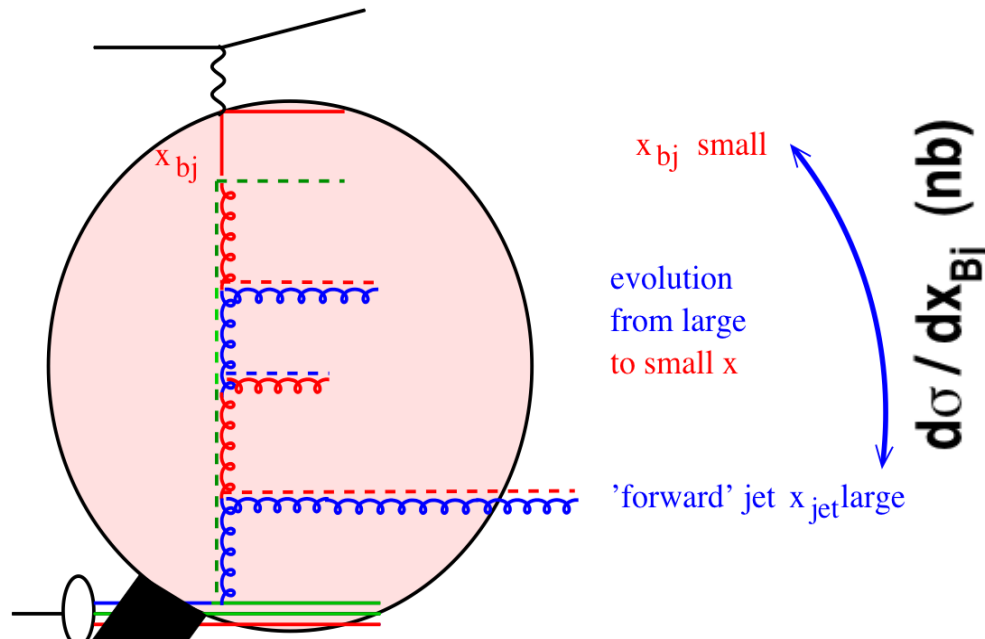


→ NLO calc toooooo low !!!

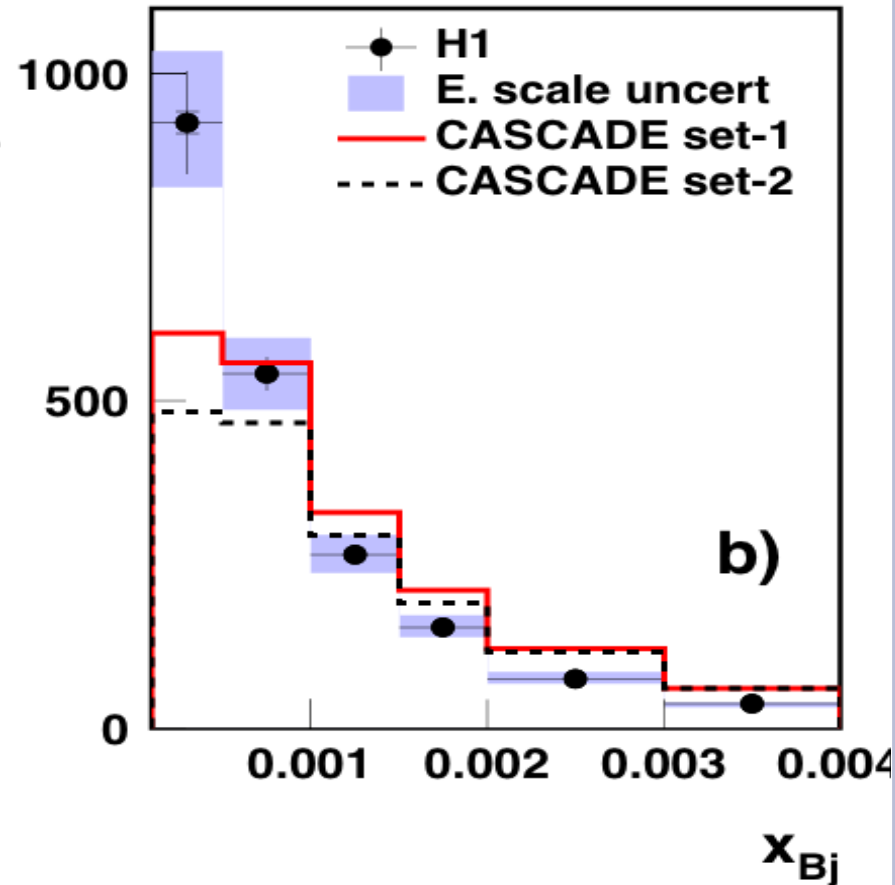
# Looking forward ...

H1, Eur.Phys.J.C46:27-42,2006.

## H1 forward jet data



$d\sigma / dx_{Bj}$  (nb)



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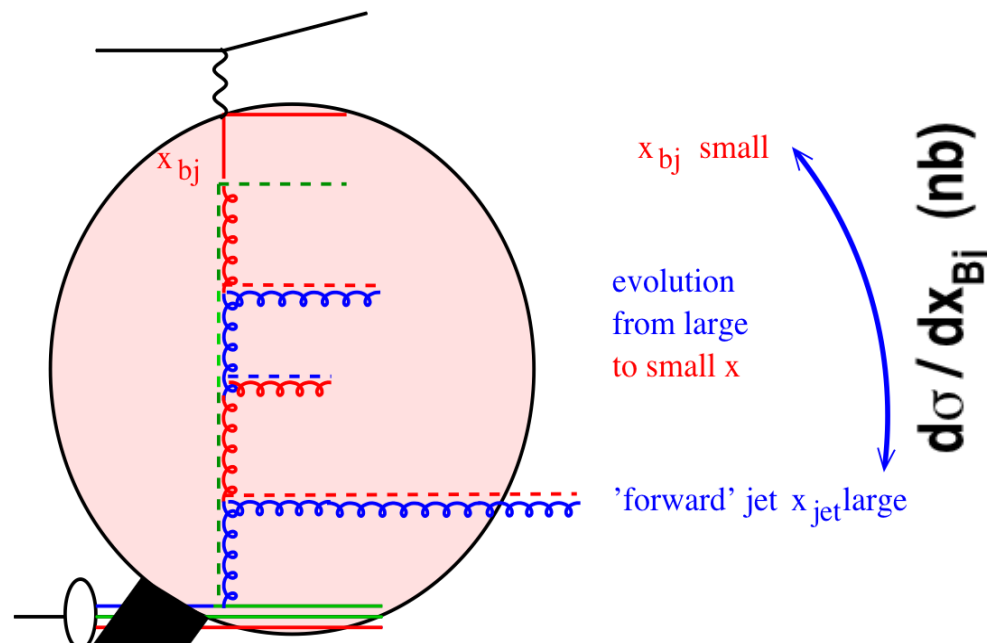
$$\sigma(\text{fwd jet}) / \sigma(\text{DIS}) \sim 1\%$$

→ Hmmmmm,  
not really very good !!!!!

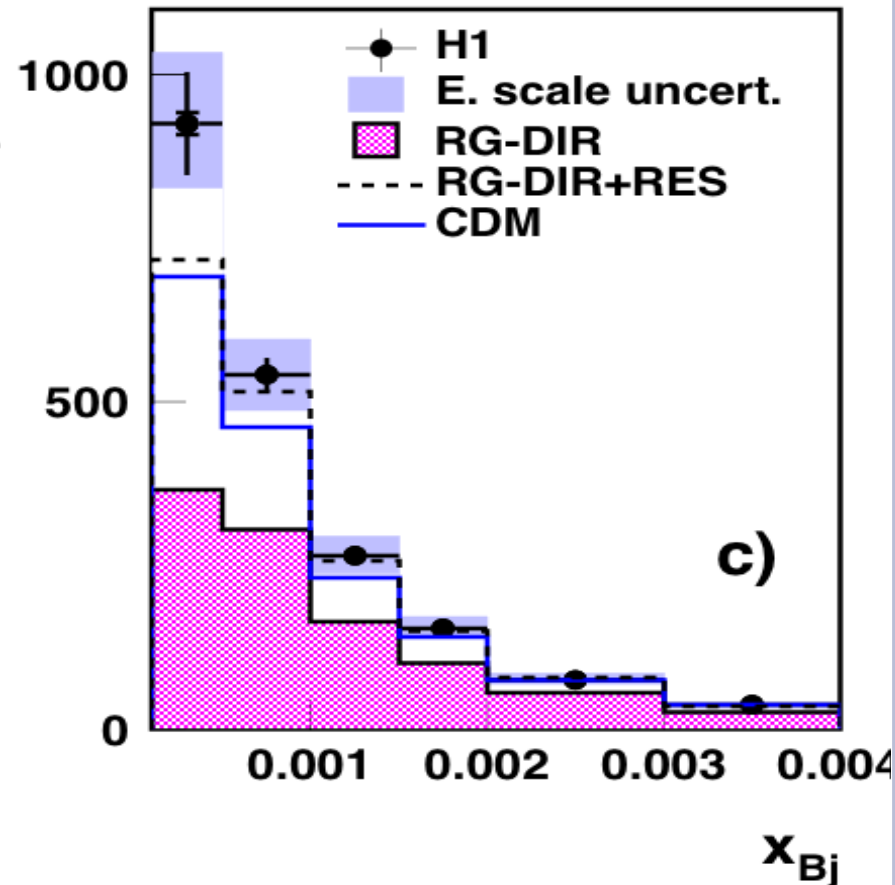
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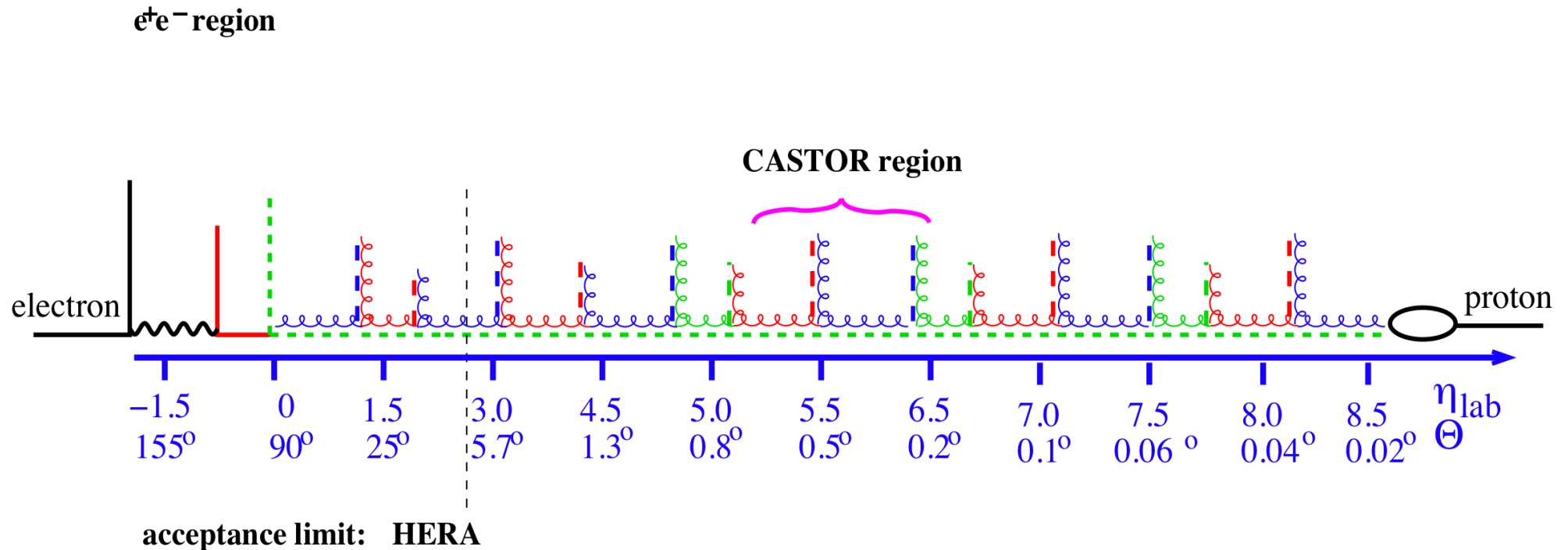
$$\sigma(\text{fwd jet}) / \sigma(\text{DIS}) \sim 1\%$$

→ CDM (ARIADNE) pretty good ....

# what did we learn ...

- inclusive DIS xsection well described by NLO DGLAP
  - xsection rises strongly for small  $x$
  - large gluon/sea quark densities
  - is linear evolution enough ?
  - saturation effects ?
- understanding parton evolution at high energies still challenging:
  - hadronic final state **not really** understood
  - kt distribution, delta phi
  - forward jet production
- best description still by CDM (ARIADNE) although effects from extended dipoles...
- best theory .. (CCFM) still lacking good description.....!!!!

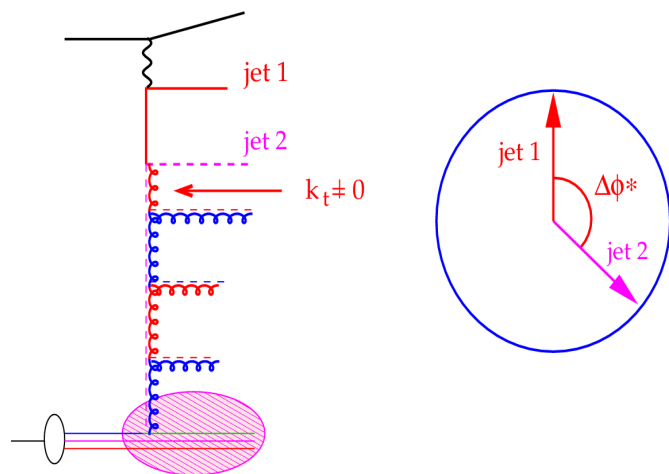
# How to make progress ?



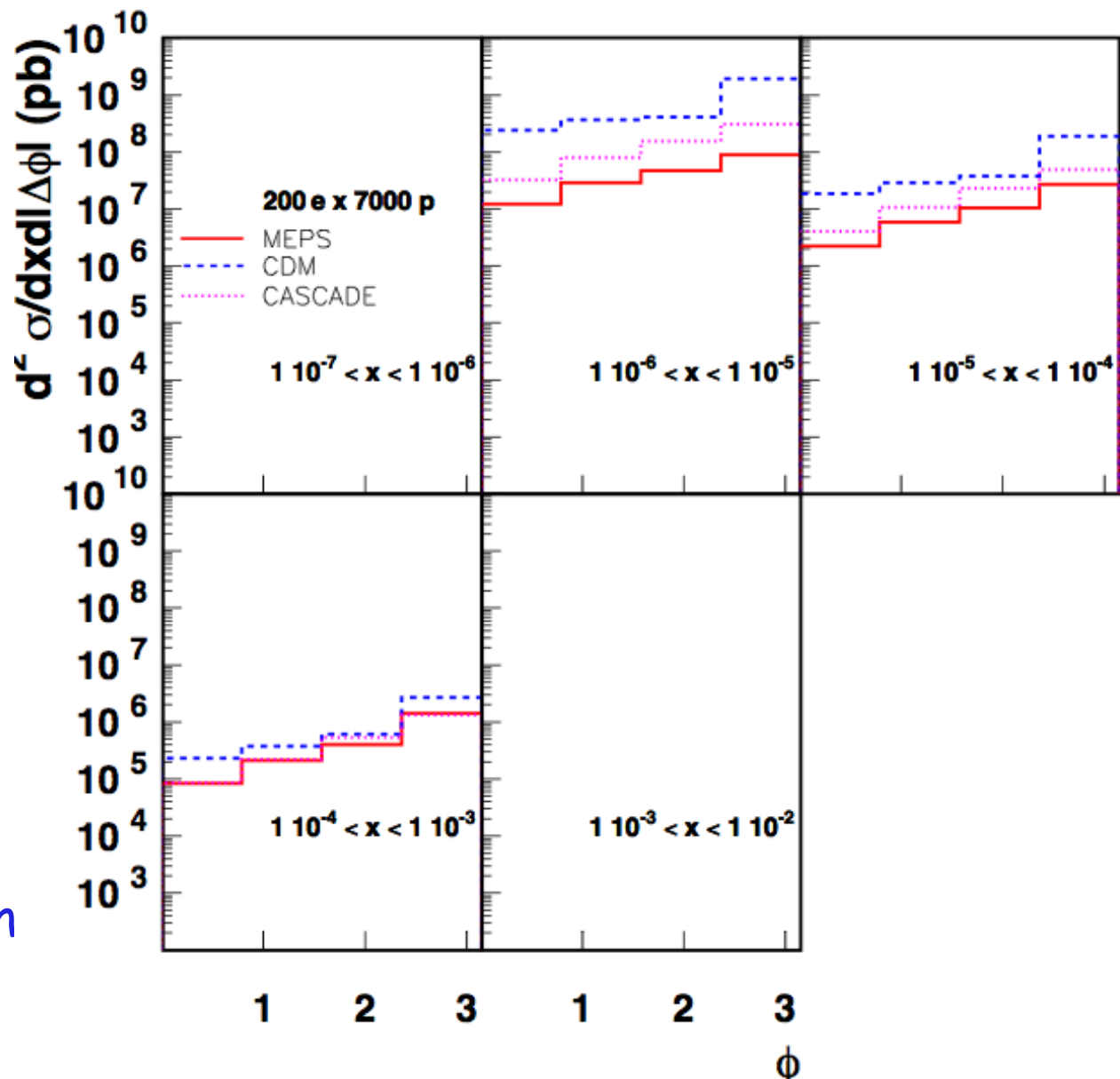
- measure jets in central region
- measure jets in forward region ( $\eta > 3$ ).... extend HERA
- measure jets in very forward region ( $\eta > 5$ )
  - cover at least same range as CMS... (CASTOR)
  - go even more forward to proton fragmentation region



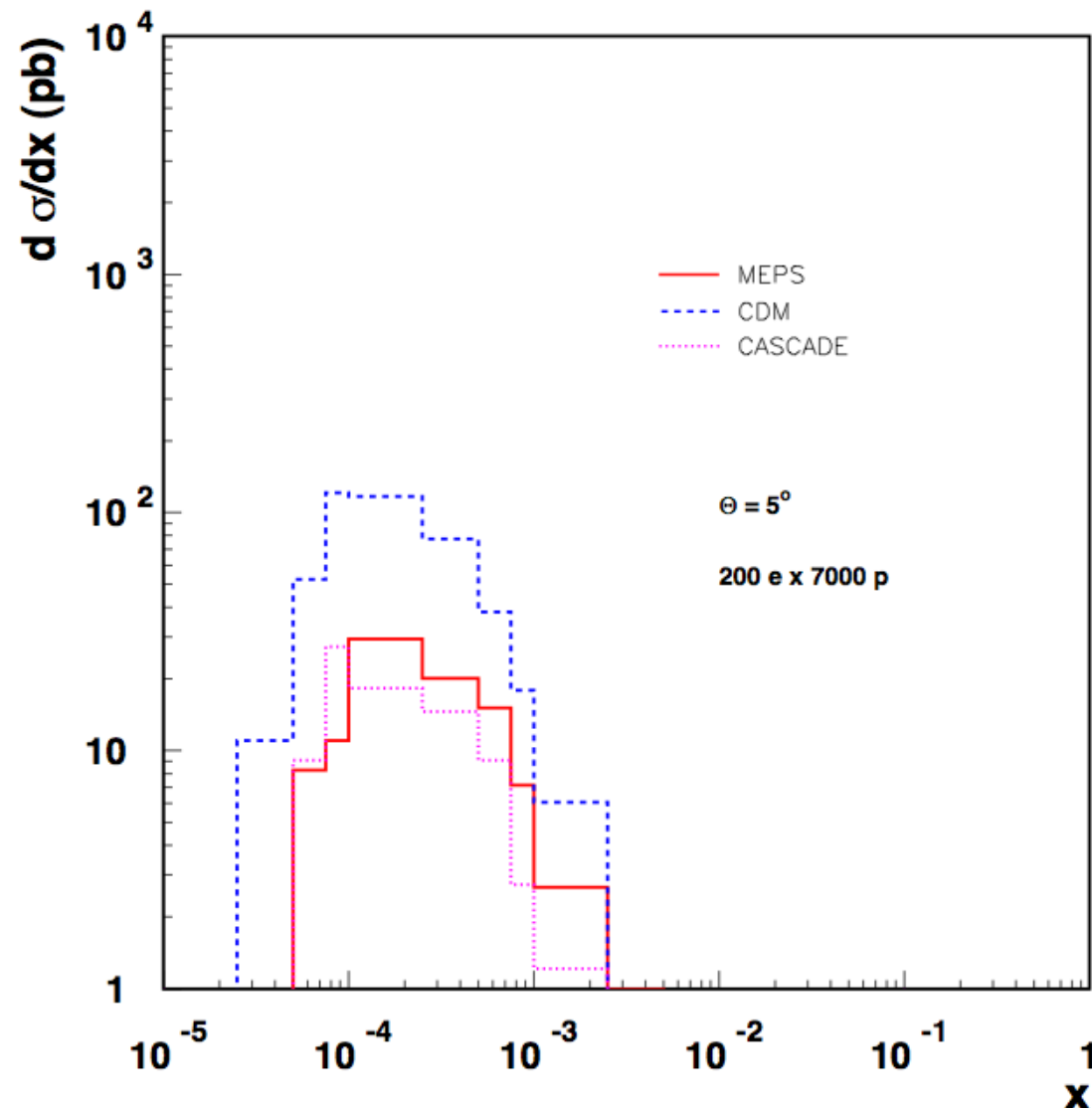
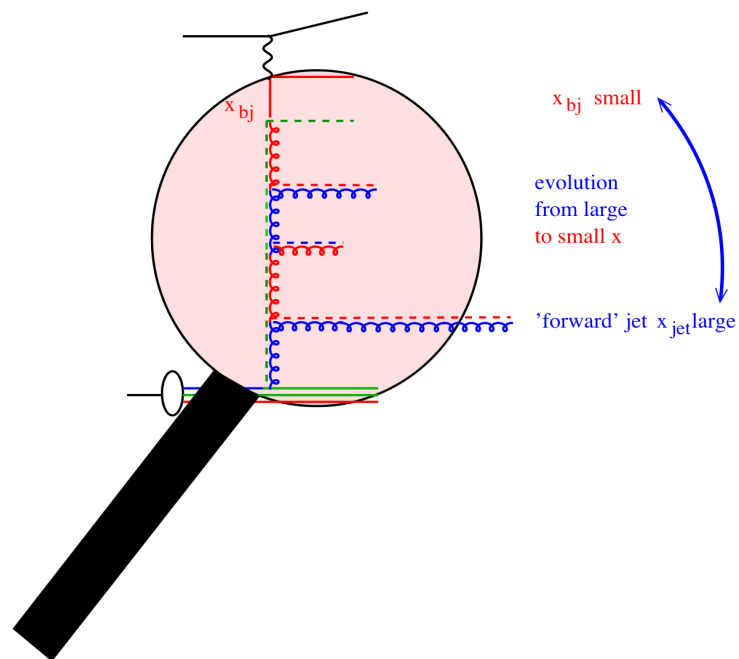
# di-jets: at large energies



- $5 < Q^2 < 100 \text{ GeV}^2$   
 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$
- small  $k_\perp \rightarrow \Delta\phi \sim 180$
- large  $k_\perp$  from evolution



# Forward jets at LHeC

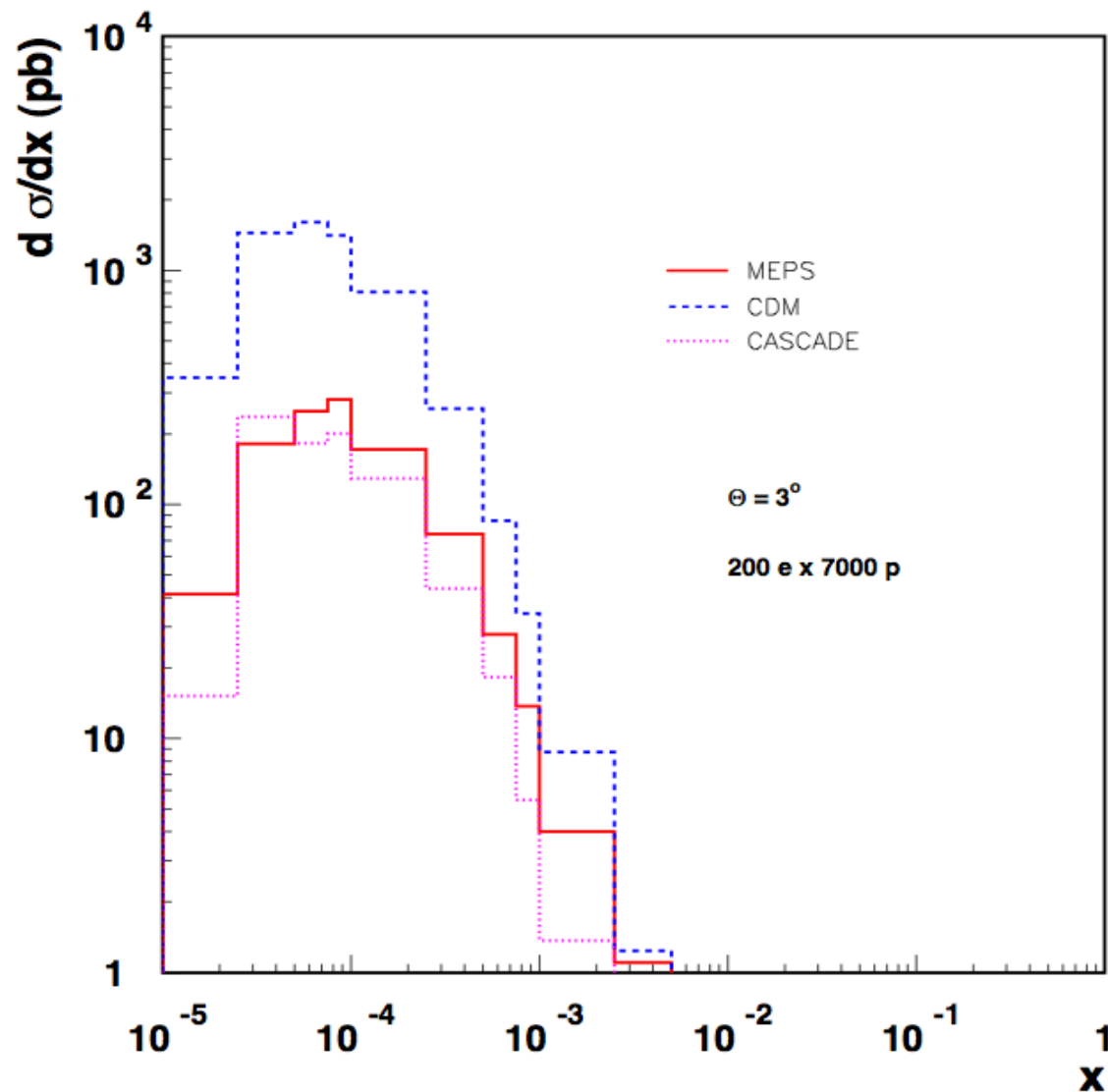
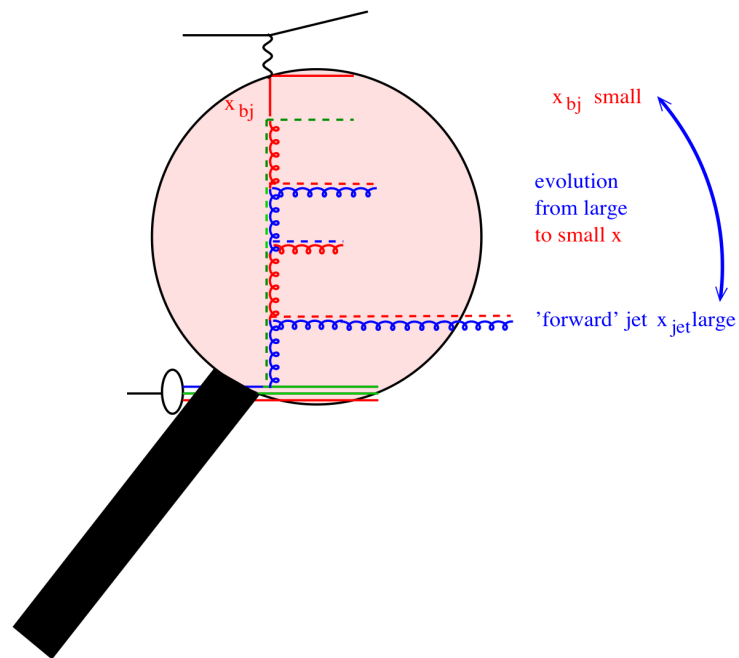


- DIS and forward jet:

$$x_{jet} > 0.03$$

$$0.5 < \frac{p_{t,jet}^2}{Q^2} < 2$$

# Forward jets at LHeC

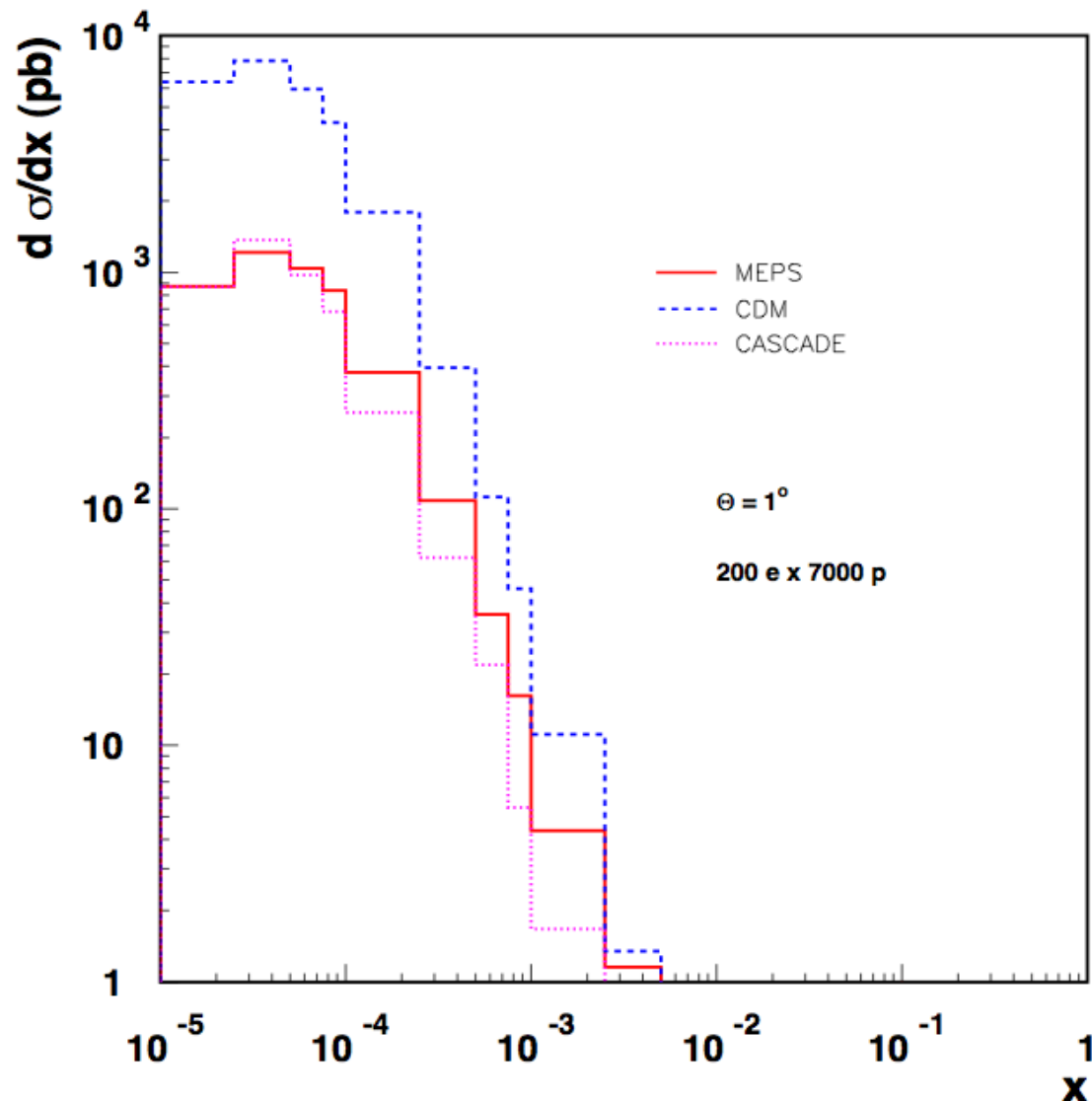
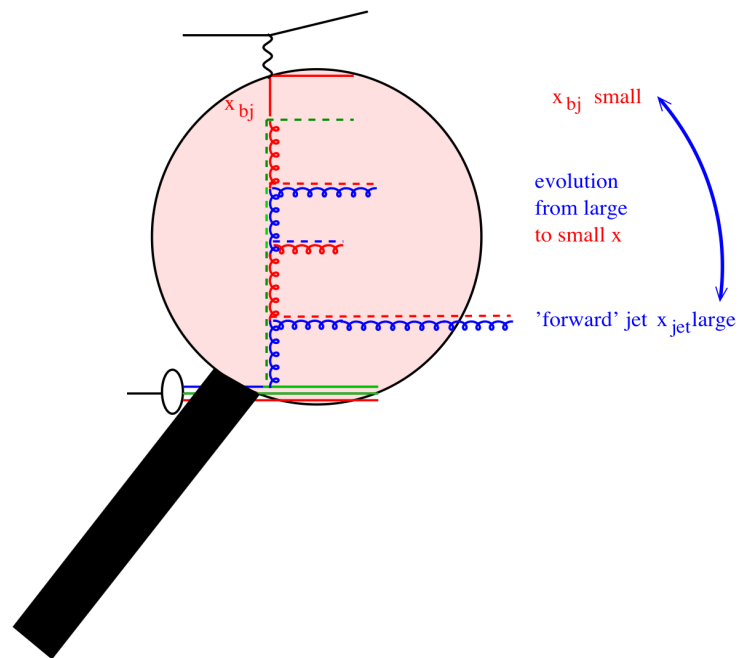


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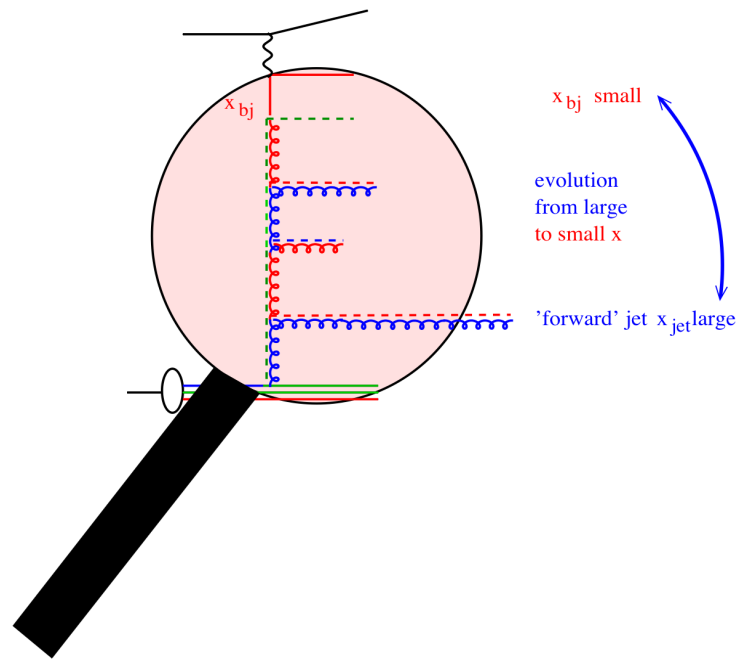


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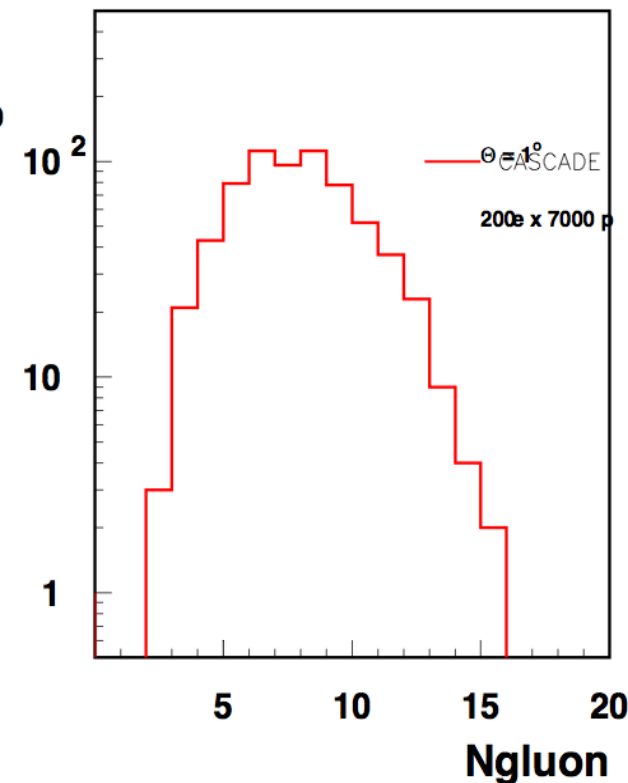
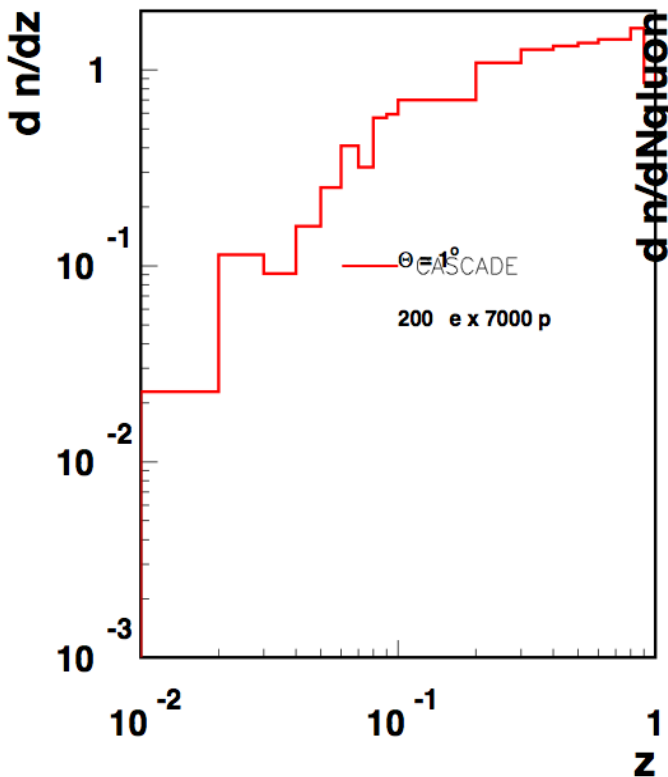


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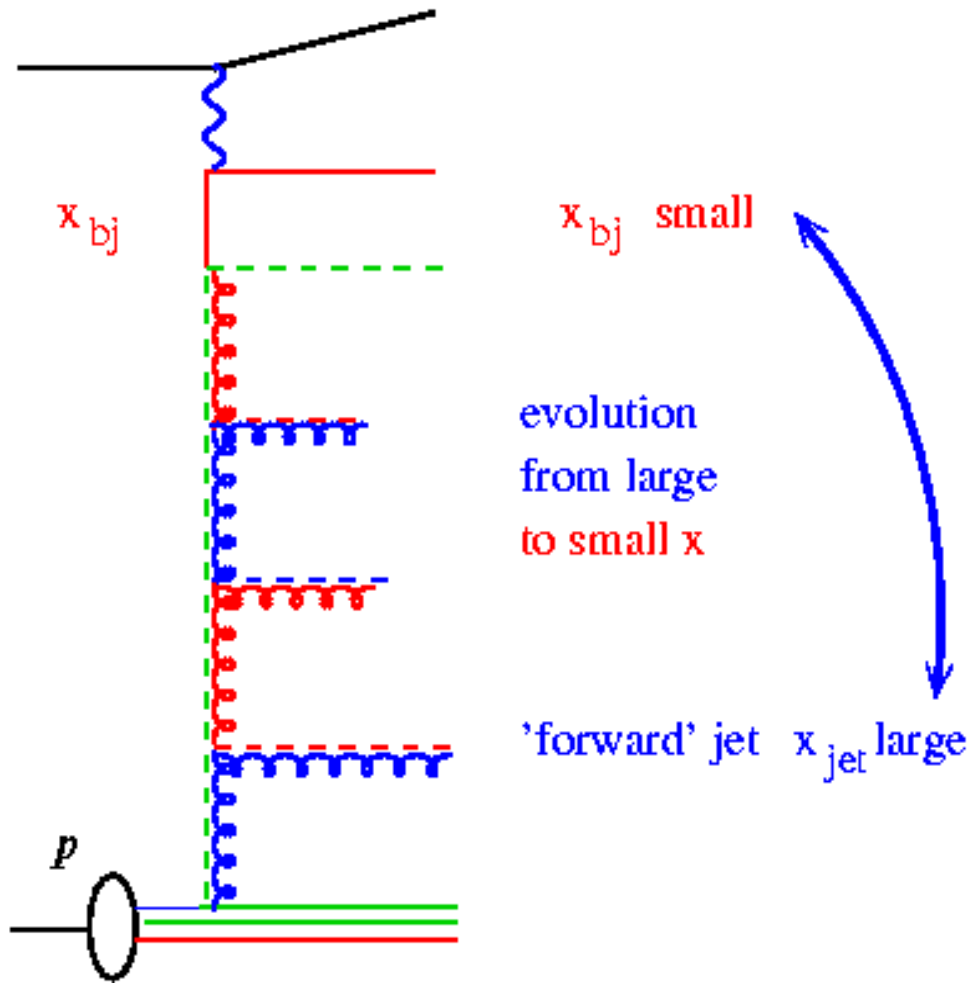
$$0.5 < \frac{p_{t \text{ jet}}^2}{Q^2} < 2$$

- consider all gluons in MCgenerator ( $p_t > 1 \text{ GeV}$ )



- $z$  values in splitting fct are still far from asymptotic region
- large number of gluon radiation...

# forward jet production and rap-gaps



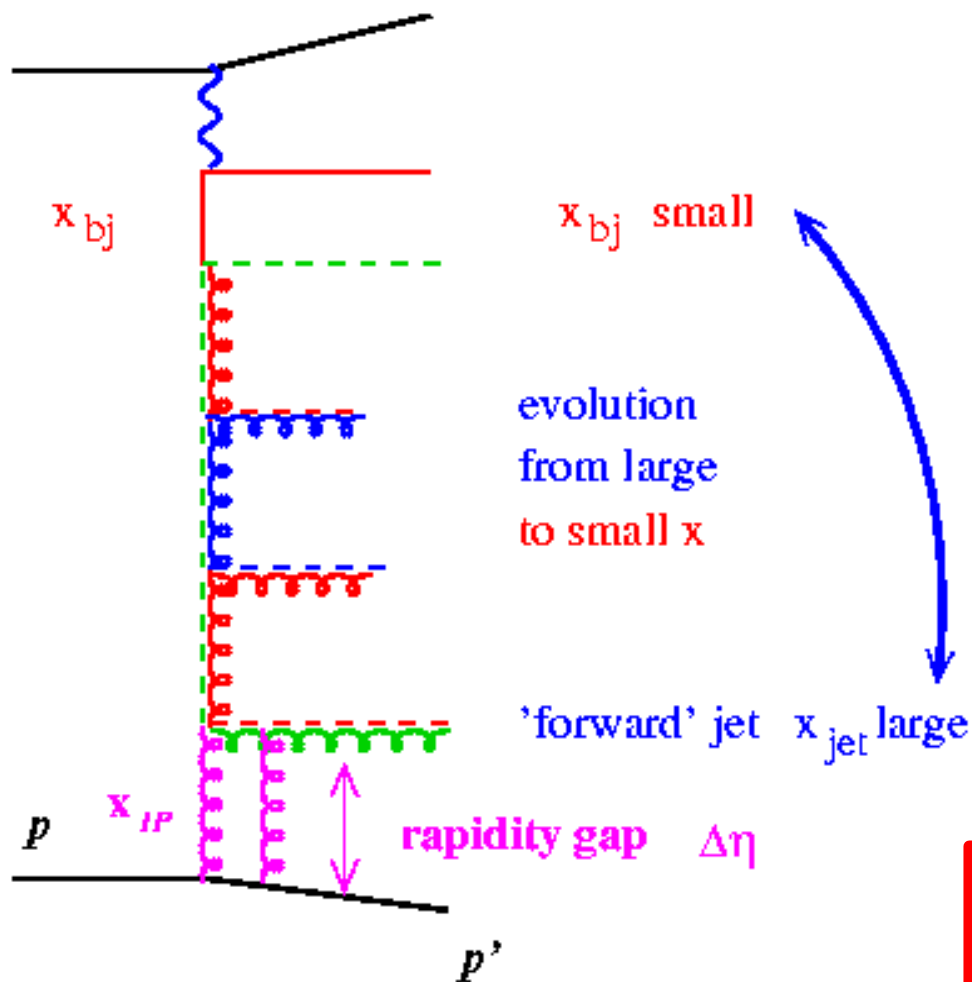
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$$\sigma(\text{fwd jet})/\sigma(\text{DIS}) \sim 1\%$$

# forward jet production and rap-gaps



- DIS and forward jet:

$$x_{jet} > 0.03$$

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- in diffraction: forward jet

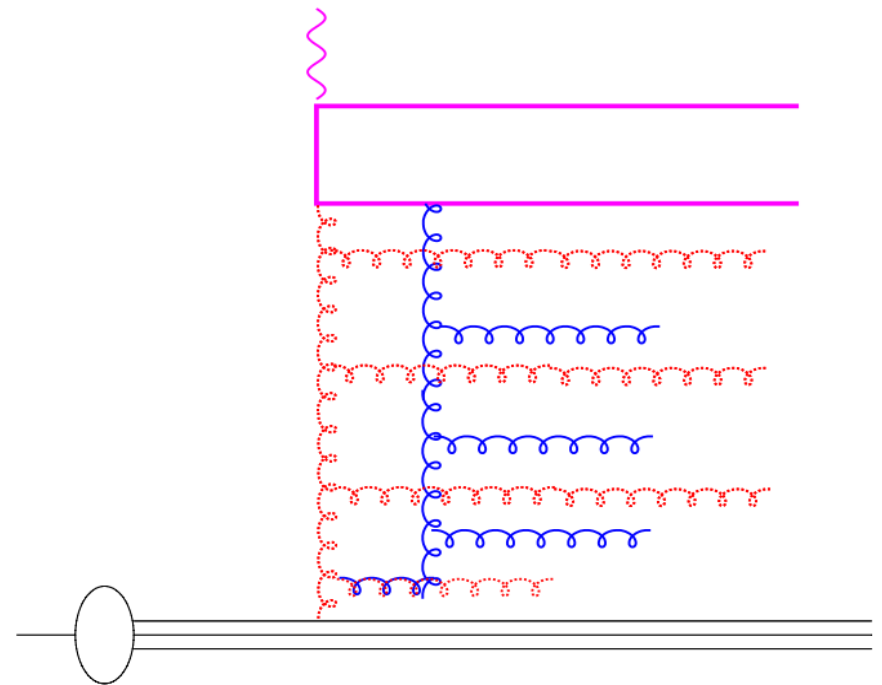
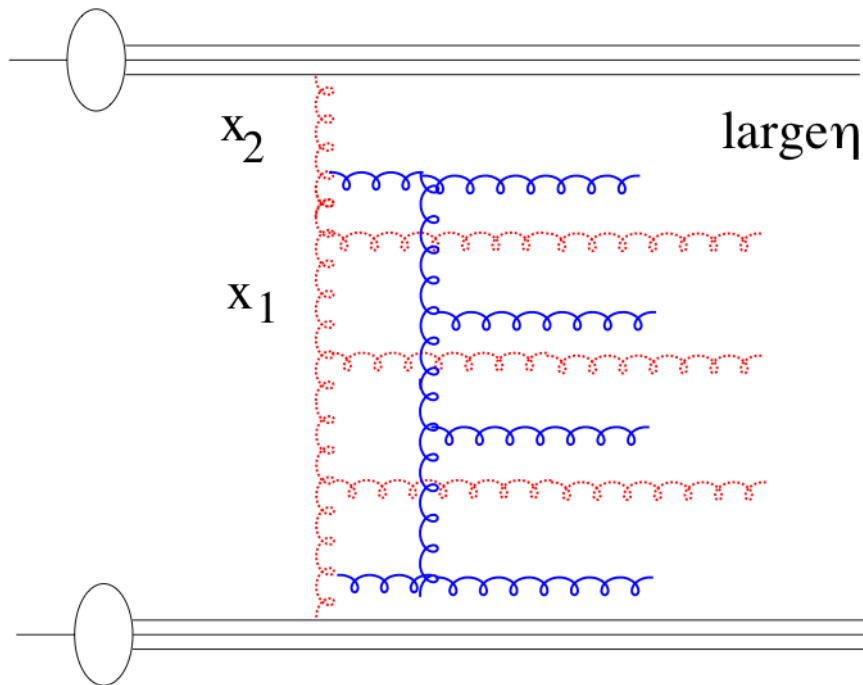
close to rapidity gap

$$\sigma(\text{diff dijet})/\sigma(\text{DIS}) \sim 1\%$$

- understand radiation close to proton  
and radiation close to rapidity

# LHC-pp and LHC-ep

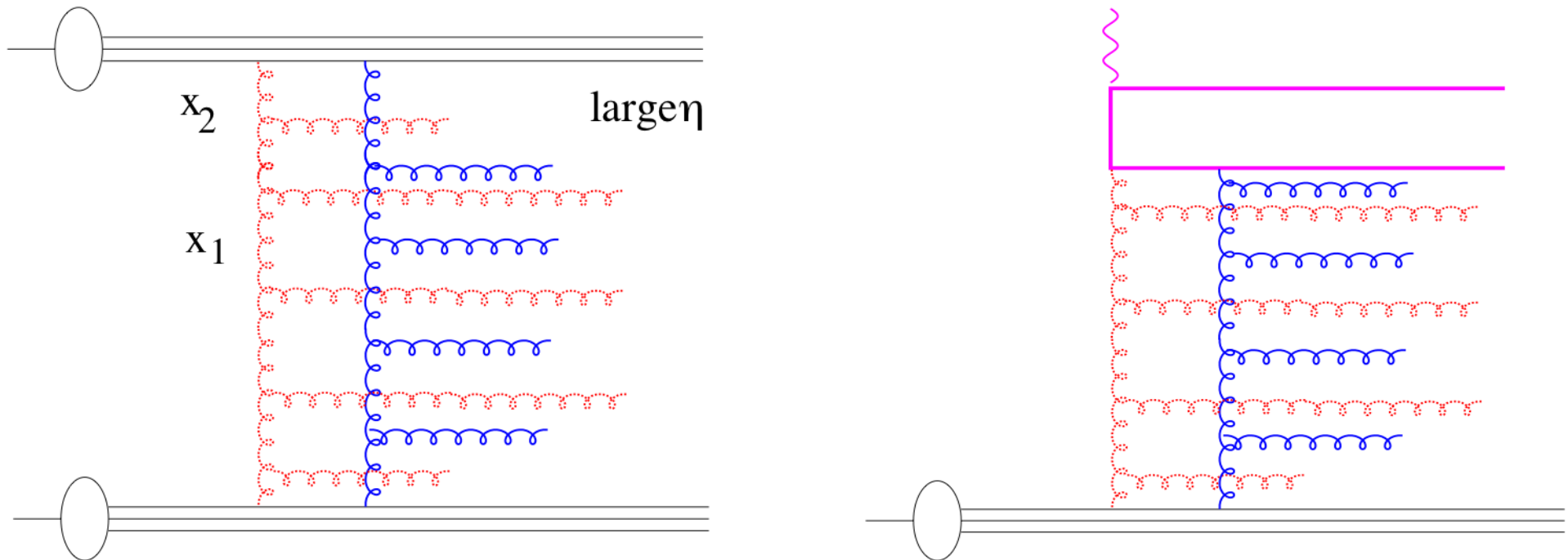
- compare measurements with LHC - pp results
  - one proton side is identical
  - test factorisation and parton evolution
  - multi-parton interaction/saturation/diffraction





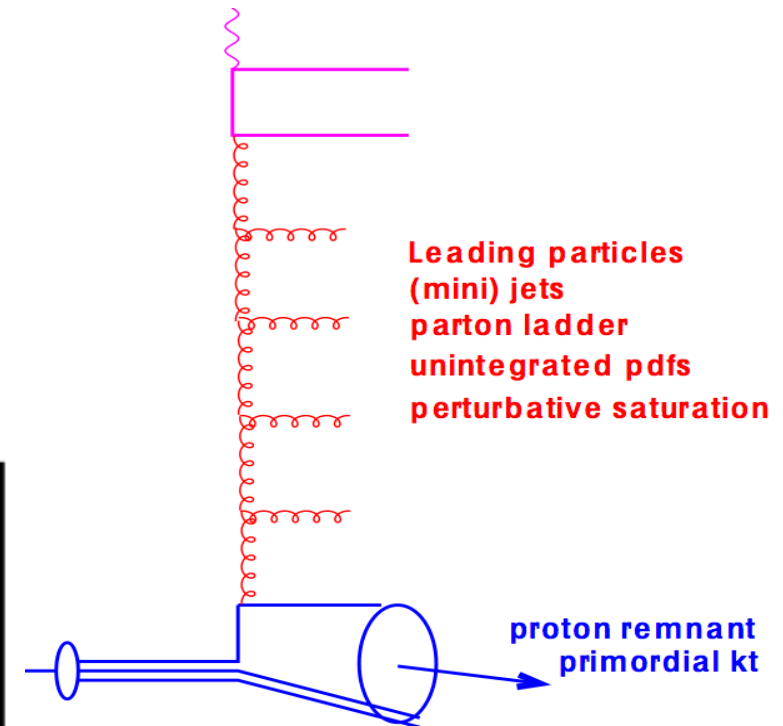
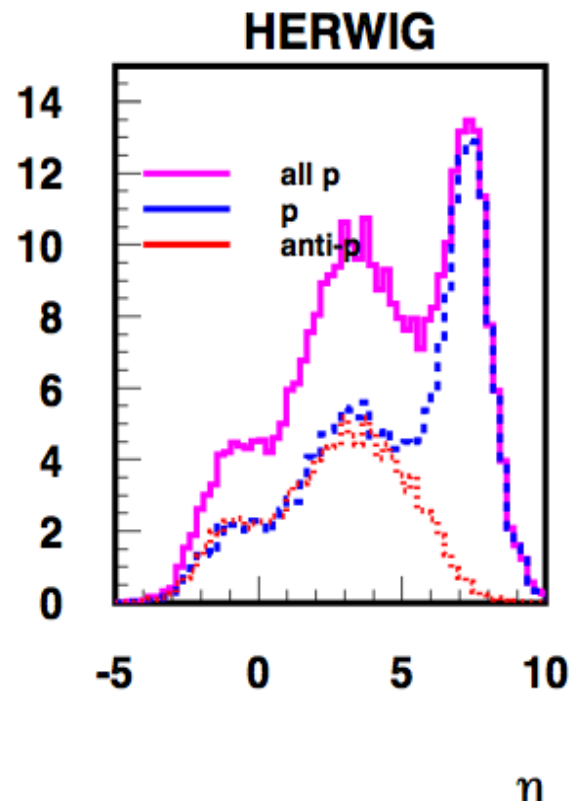
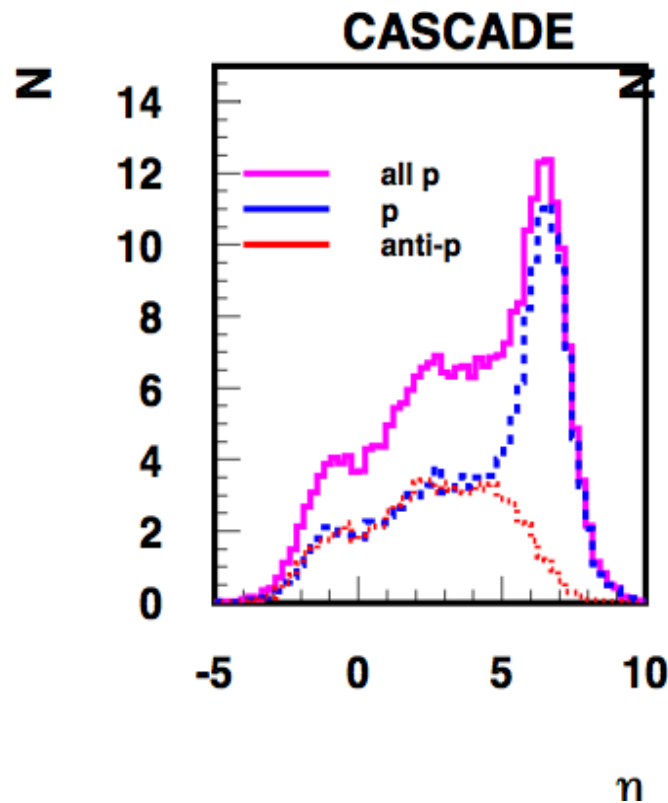
# LHC-pp and LHC-ep

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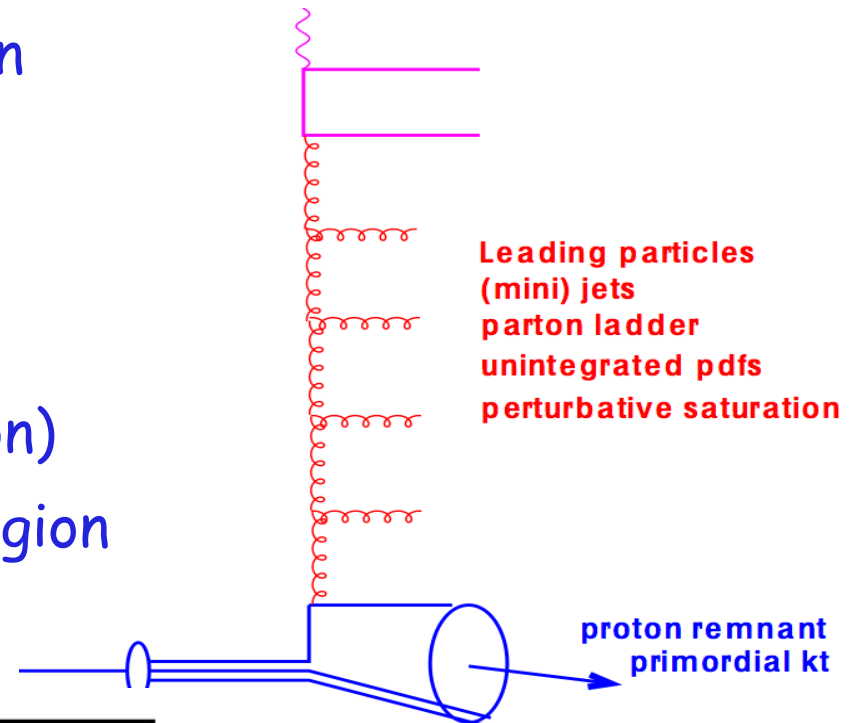
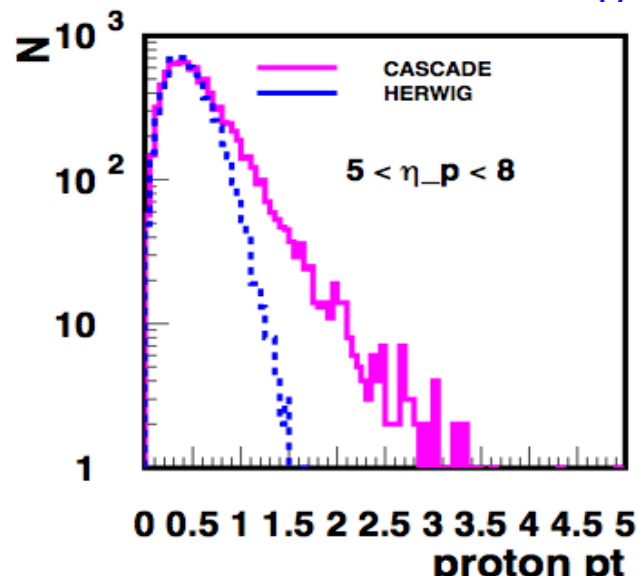
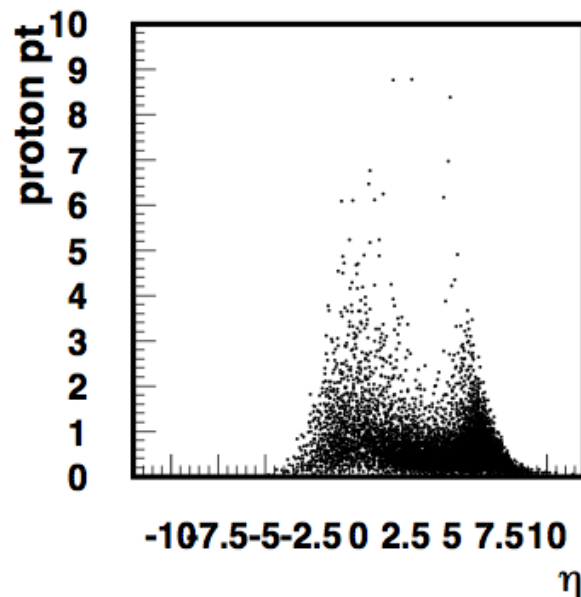
# Universality of fragmentation: ep vrs pp

- leading particles in parton cascade ...  
universality of hadronization



# Universality of proton fragmentation region

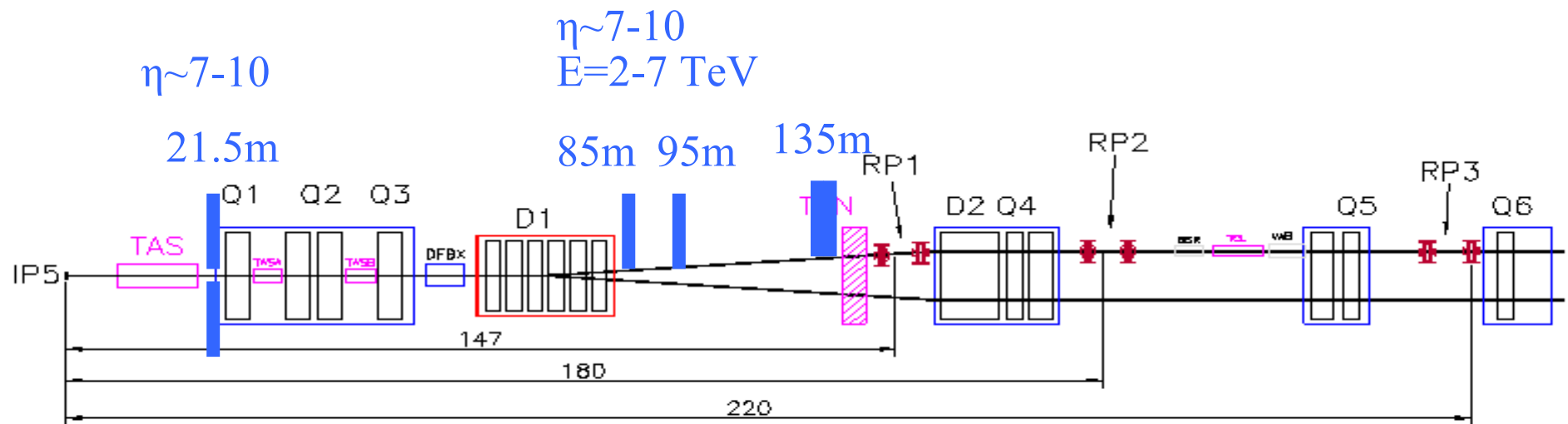
- measuring toward proton fragmentation region
- investigate intrinsic  $k_t$  - saturation effect ?
- measure leading baryon (proton/neutron) production close to p-fragmentation region



# Going even more forward ...

- study on forward coverage for CMS done ...

by V. Andreev, K. Borrás, A. Bunyatian, H. Jung, M. Kapishin, L. Lytkine



- need improved studies... with better performance and coverage
- will be one of the **important issues**....

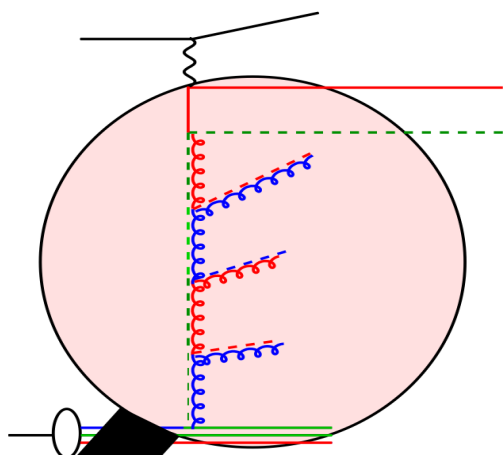
# Conclusions

- HERA has left us with many **questions in small  $x$** 
  - small  $x$  evolution:
    - dijet production: correlations are tricky to describe
    - which approach can describe consistently fwd jets
    - fwd hadron production ?
    - rise of parton densities and saturation ?
- LHeC offers **possibility** to investigate these effects
  - need good central detectors
  - need good forward coverage
  - small  $x$  effects are visible ...
  - need to be comparable to LHC-pp detectors for direct comparison
- Still..... LHeC might be not really in the **asymptotic region**.....

BACKUP SLIDES

# Walking down the ladder ...

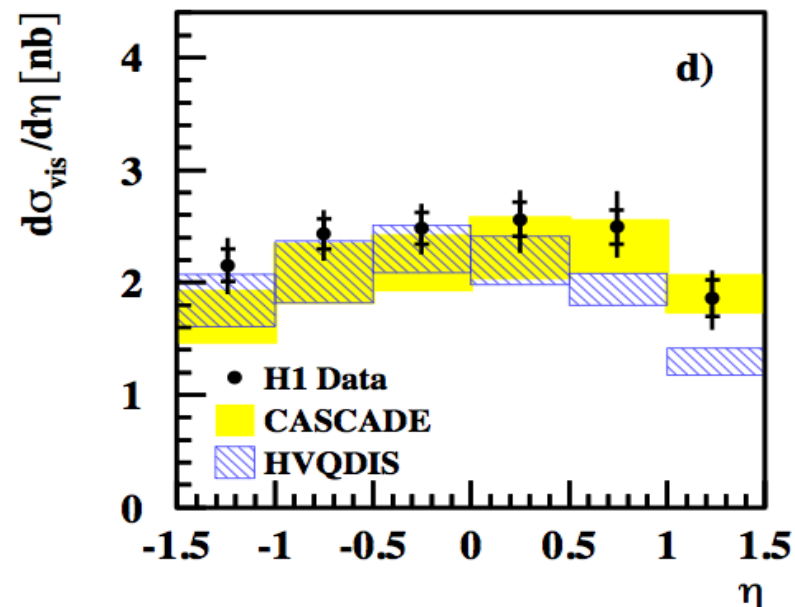
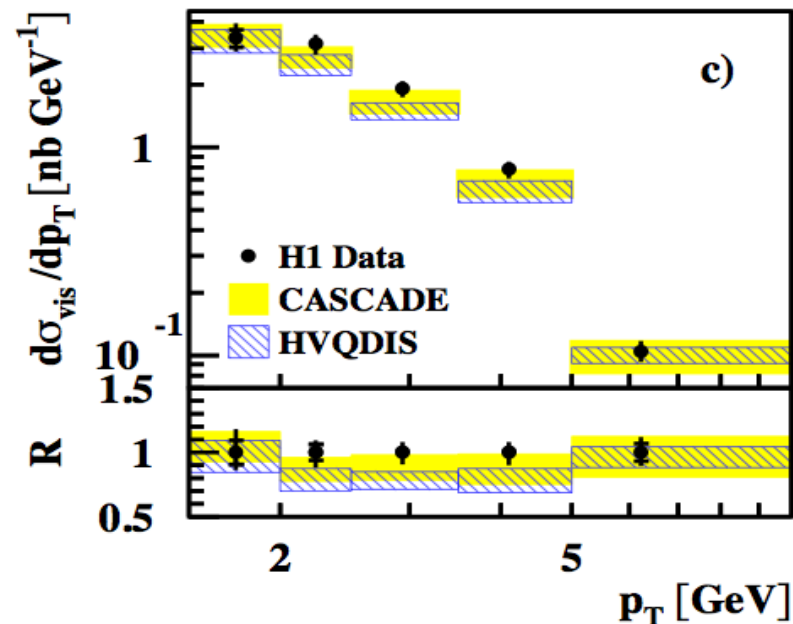
- $D^*$  production in DIS



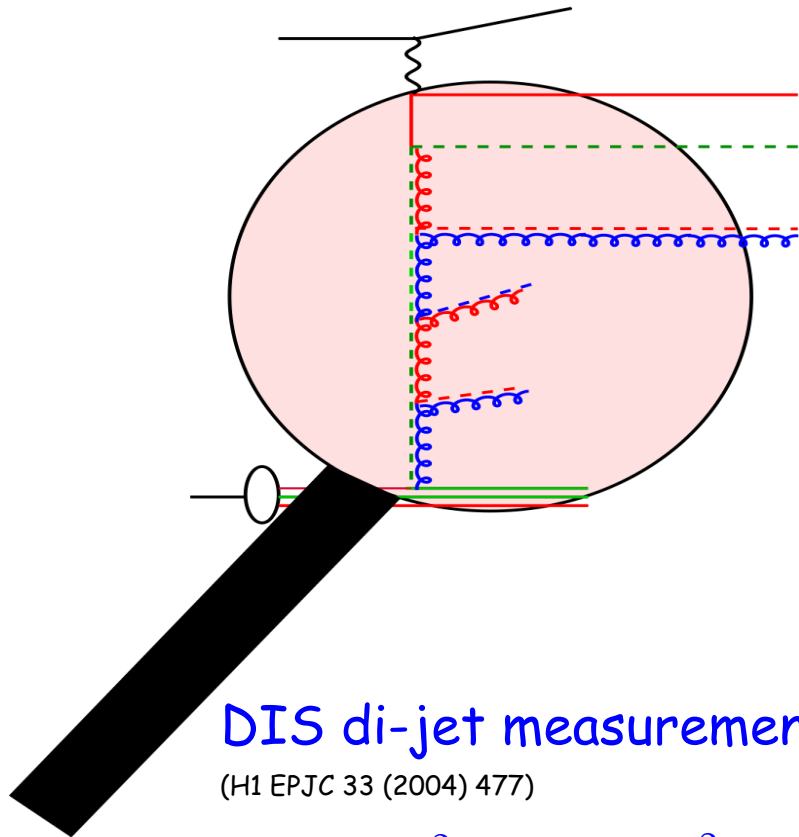
$$2 < Q^2 < 100, \quad 0.05 < y < 0.7$$

$$|\eta^{D^*}| < 1.5, \quad 1.5 < p_T^{D^*} < 15$$

- good description of inclusive  $D^*$  production by NLO (HVQDIS) but also using kt-factorization and uPDFs (CASCADE) .....



# Walking further down the ladder



## DIS di-jet measurements

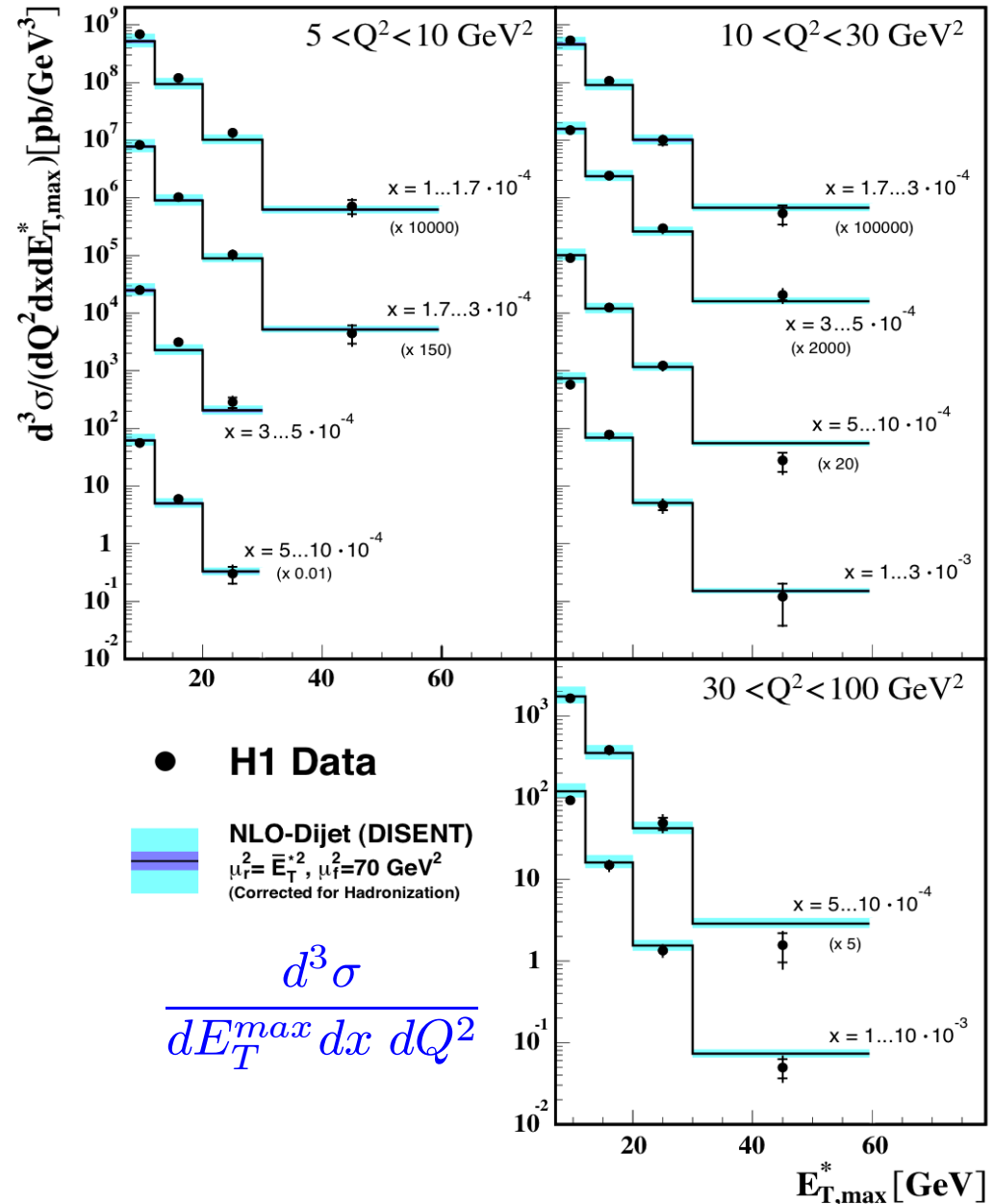
(H1 EPJC 33 (2004) 477)

$$5 < Q^2 < 100 \text{ GeV}^2$$

$$-1 < \eta < 2.5$$

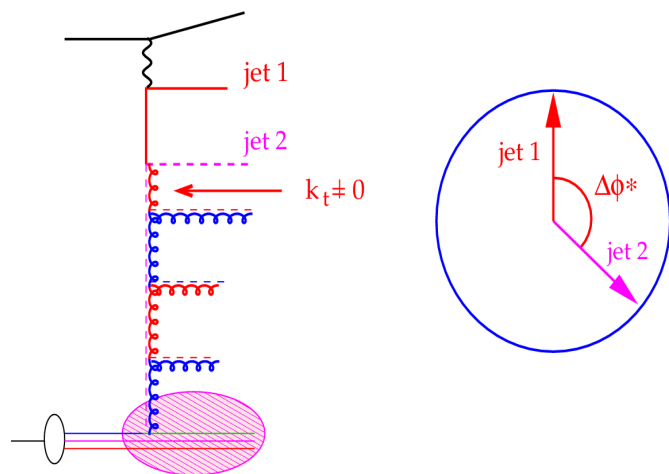
$$E_T > 5 \text{ GeV}$$

→ calculation with at least 3 hard partons essential ...

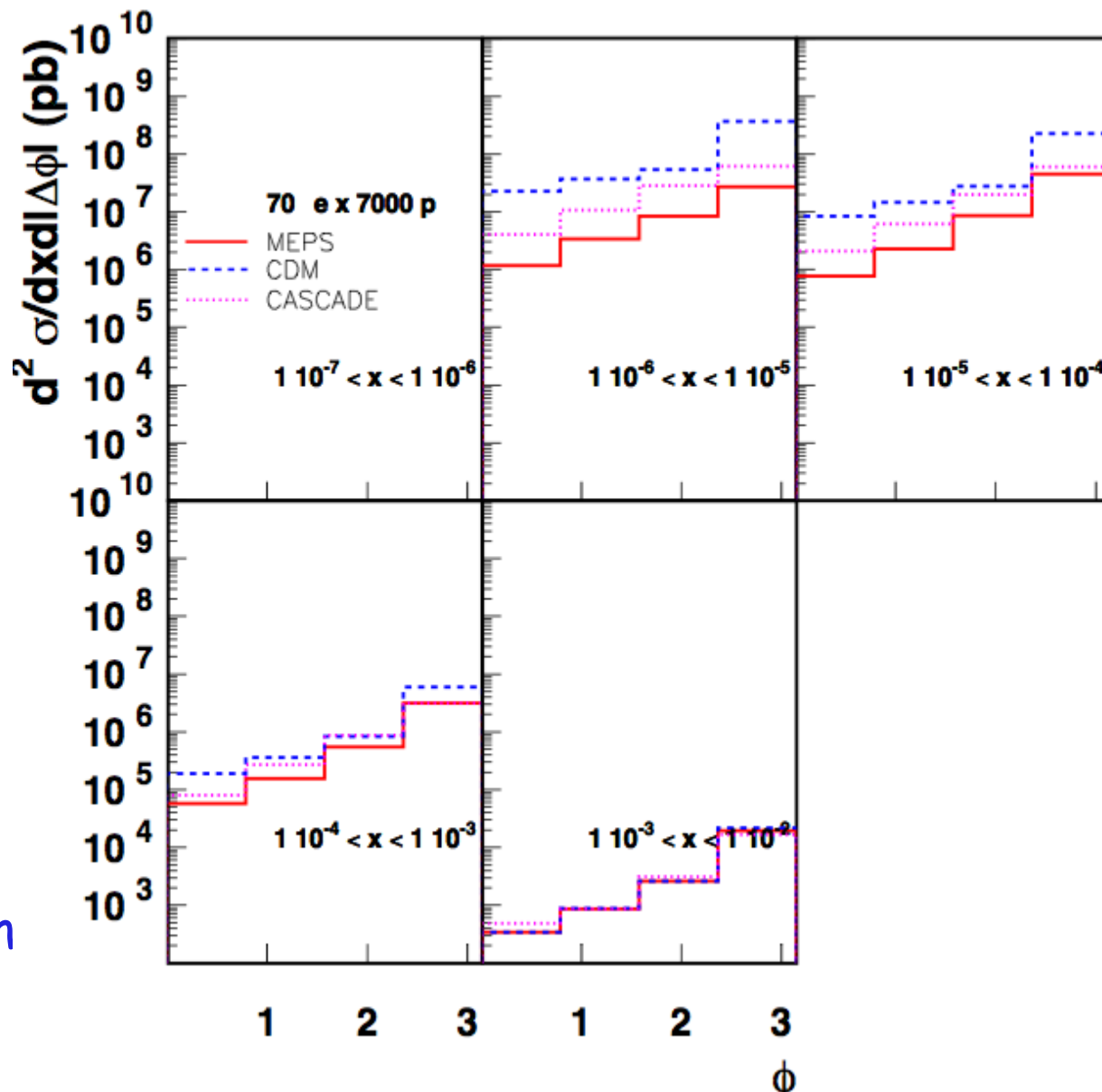




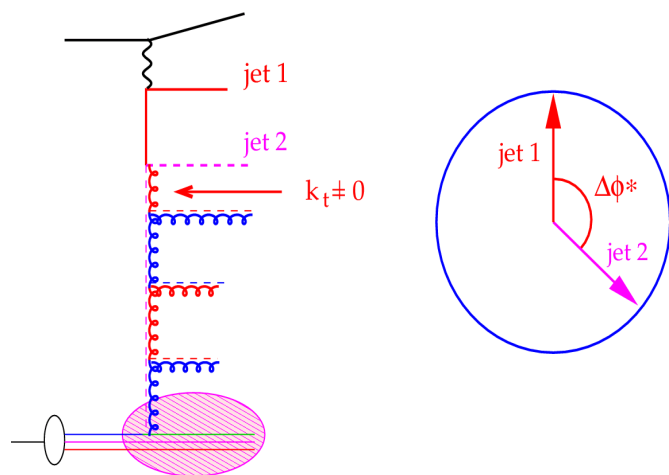
# di-jets: at large energies



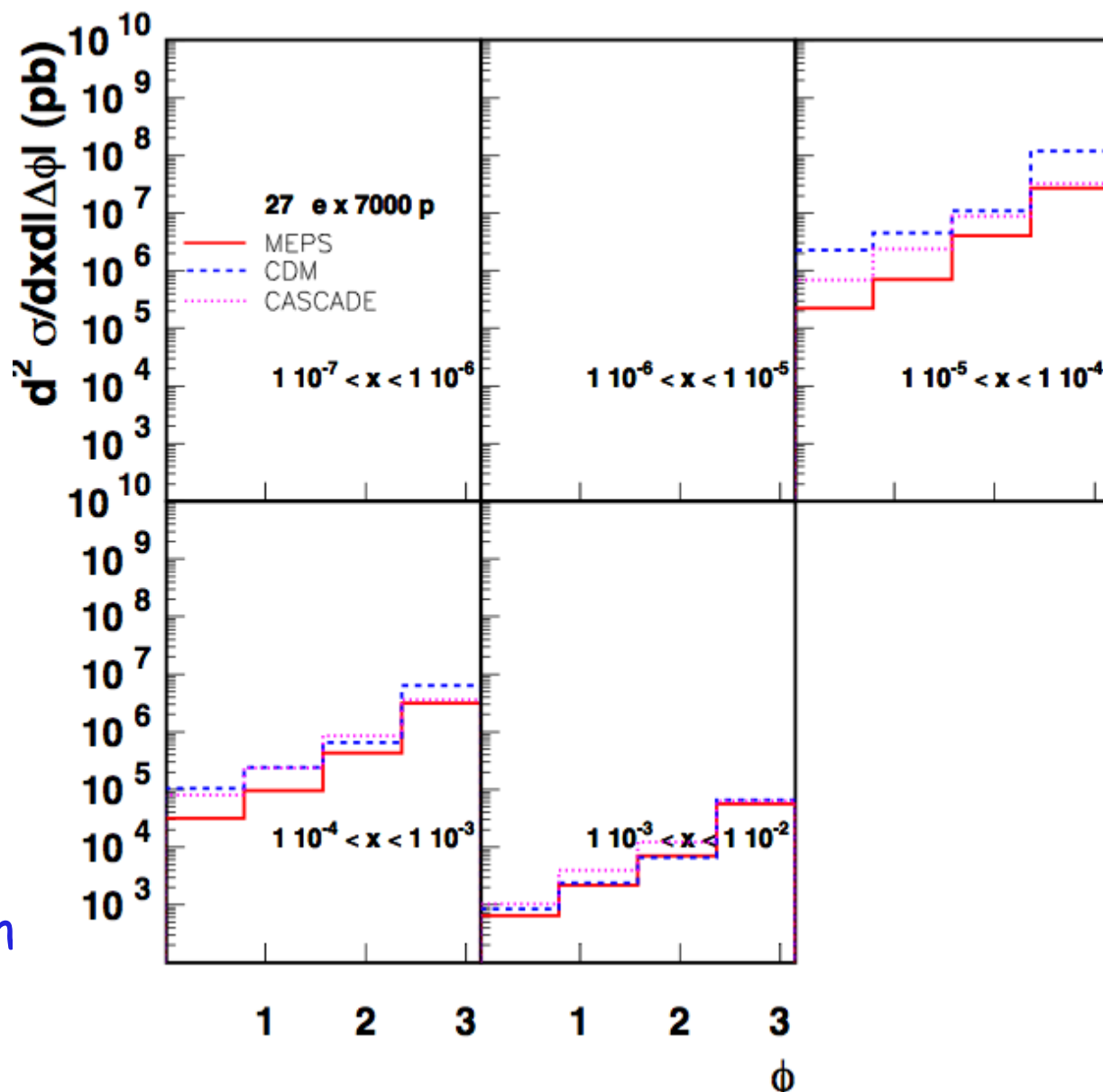
- $5 < Q^2 < 100 \text{ GeV}^2$   
 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$
- small  $k_t \rightarrow \Delta\phi \sim 180$
- large  $k_t$  from evolution



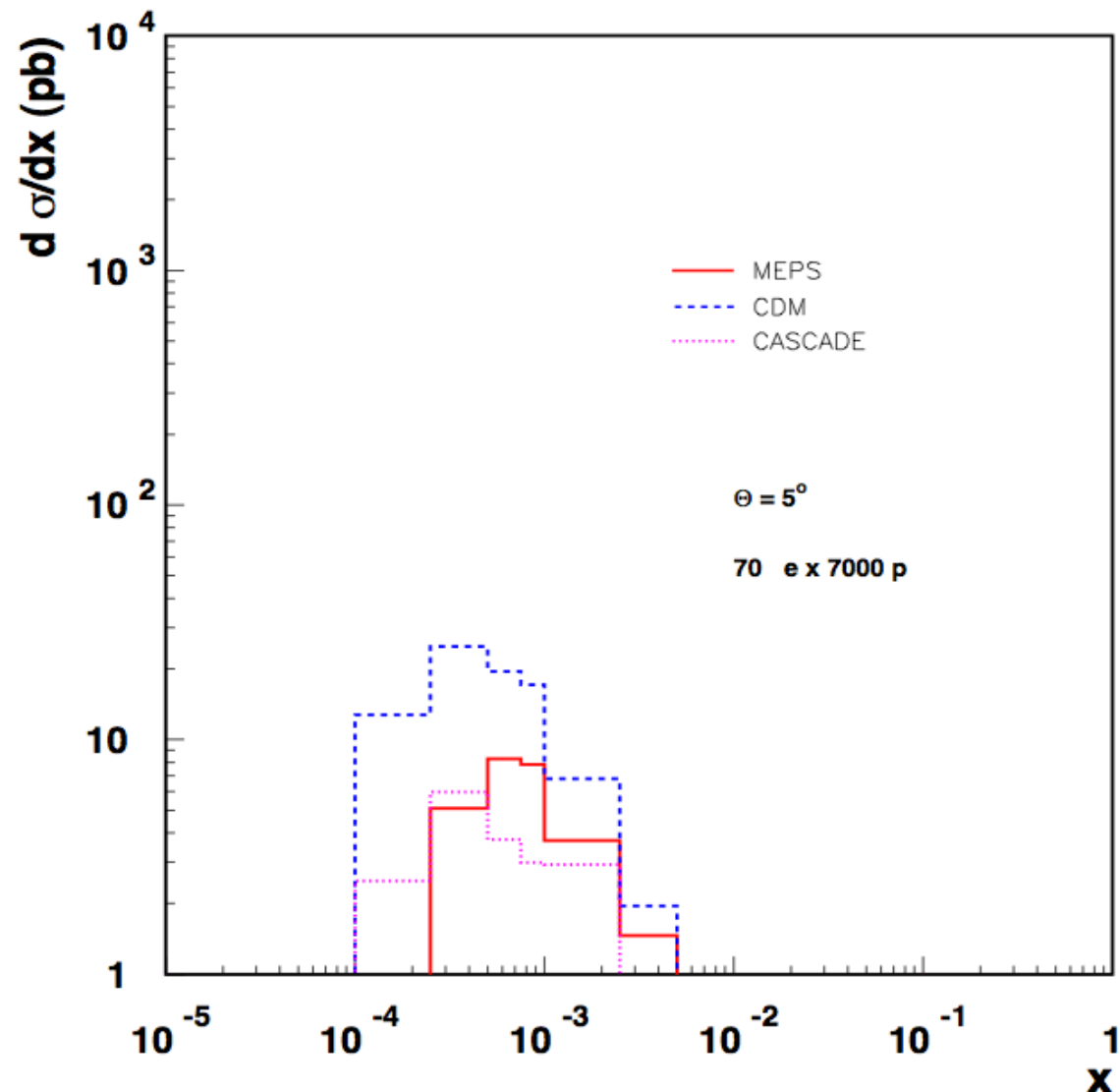
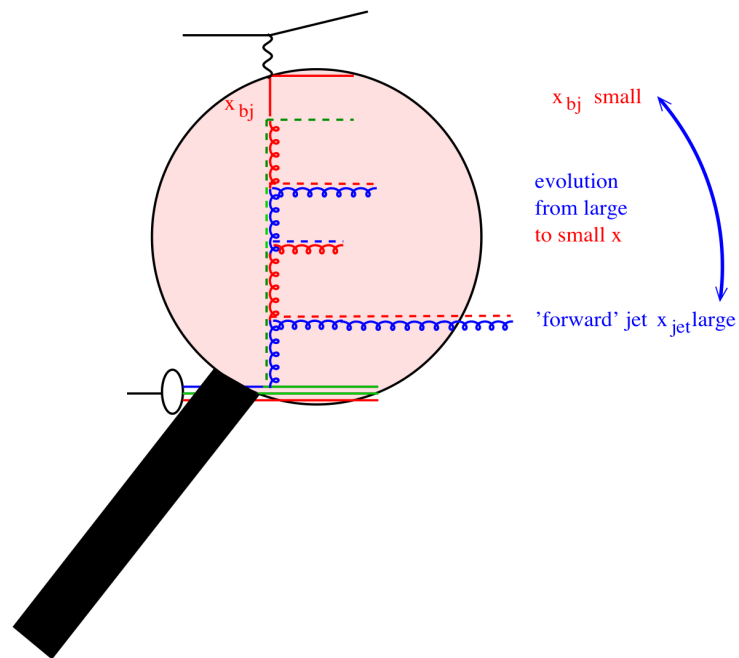
# di-jets: at large energies



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 $-1 < \eta < 2.5$   
 $E_T > 5 \text{ GeV}$
- small  $k_t \rightarrow \Delta\phi \sim 180$
- large  $k_t$  from evolution



# Forward jets at LHeC

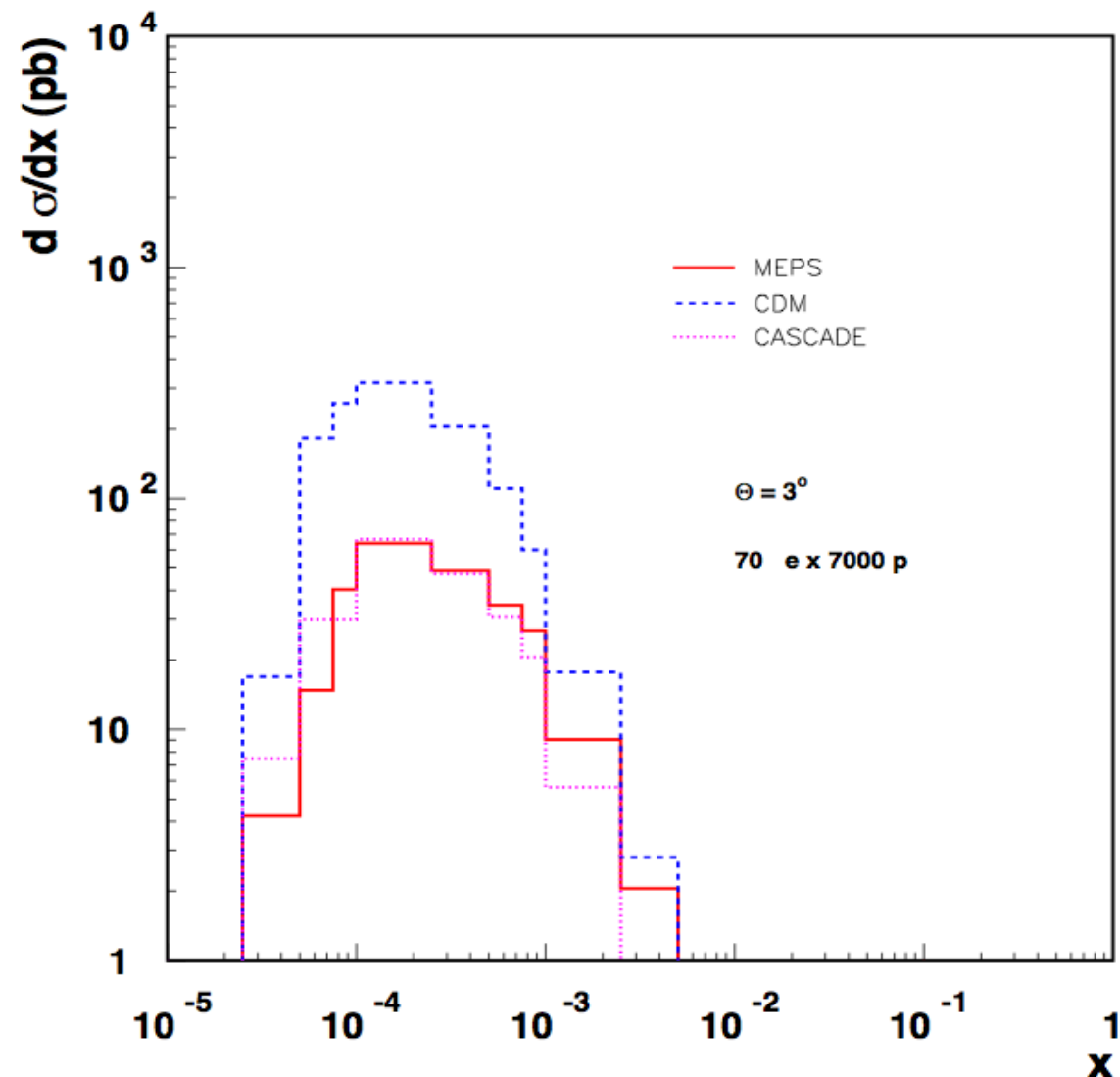
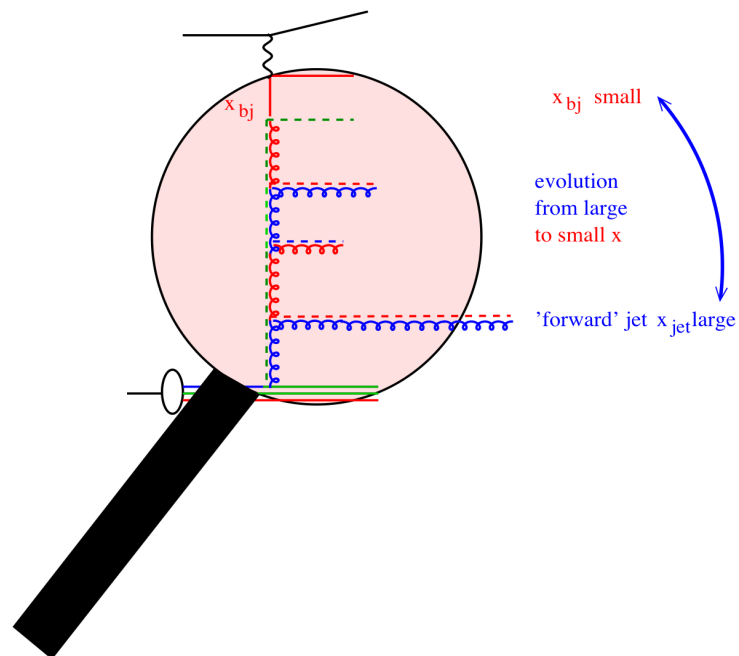


- DIS and forward jet:

$$x_{jet} > 0.03$$

$$0.5 < \frac{p_{t,jet}^2}{Q^2} < 2$$

# Forward jets at LHeC

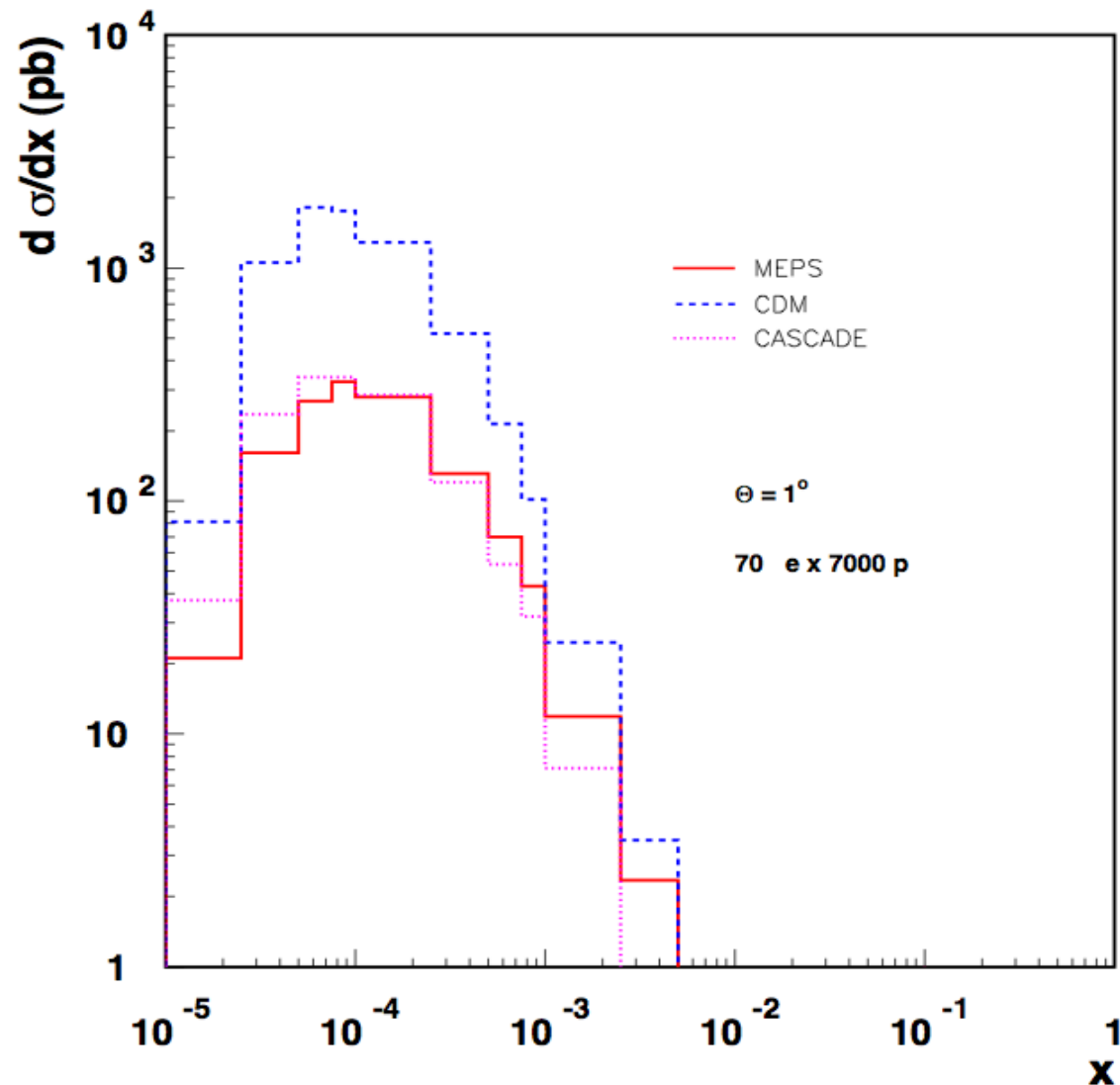
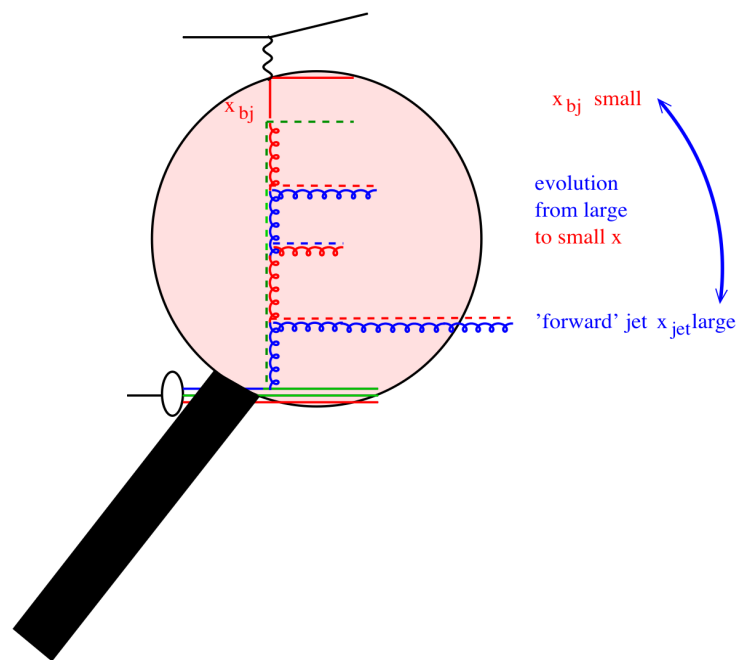


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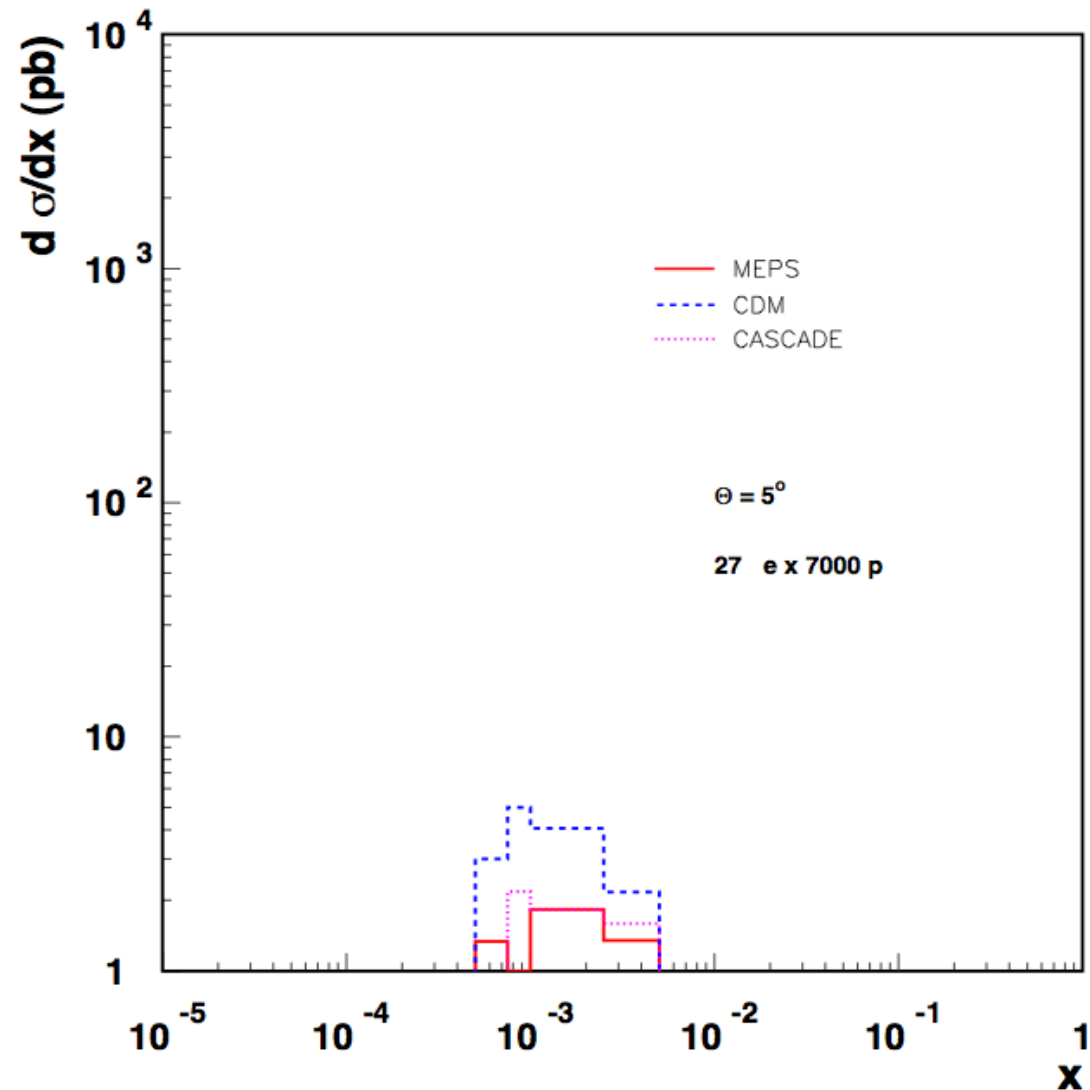
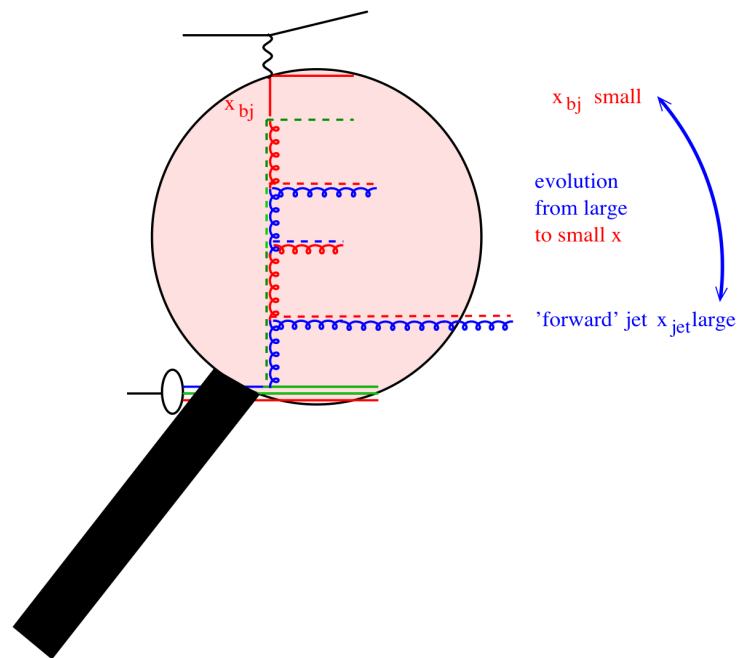


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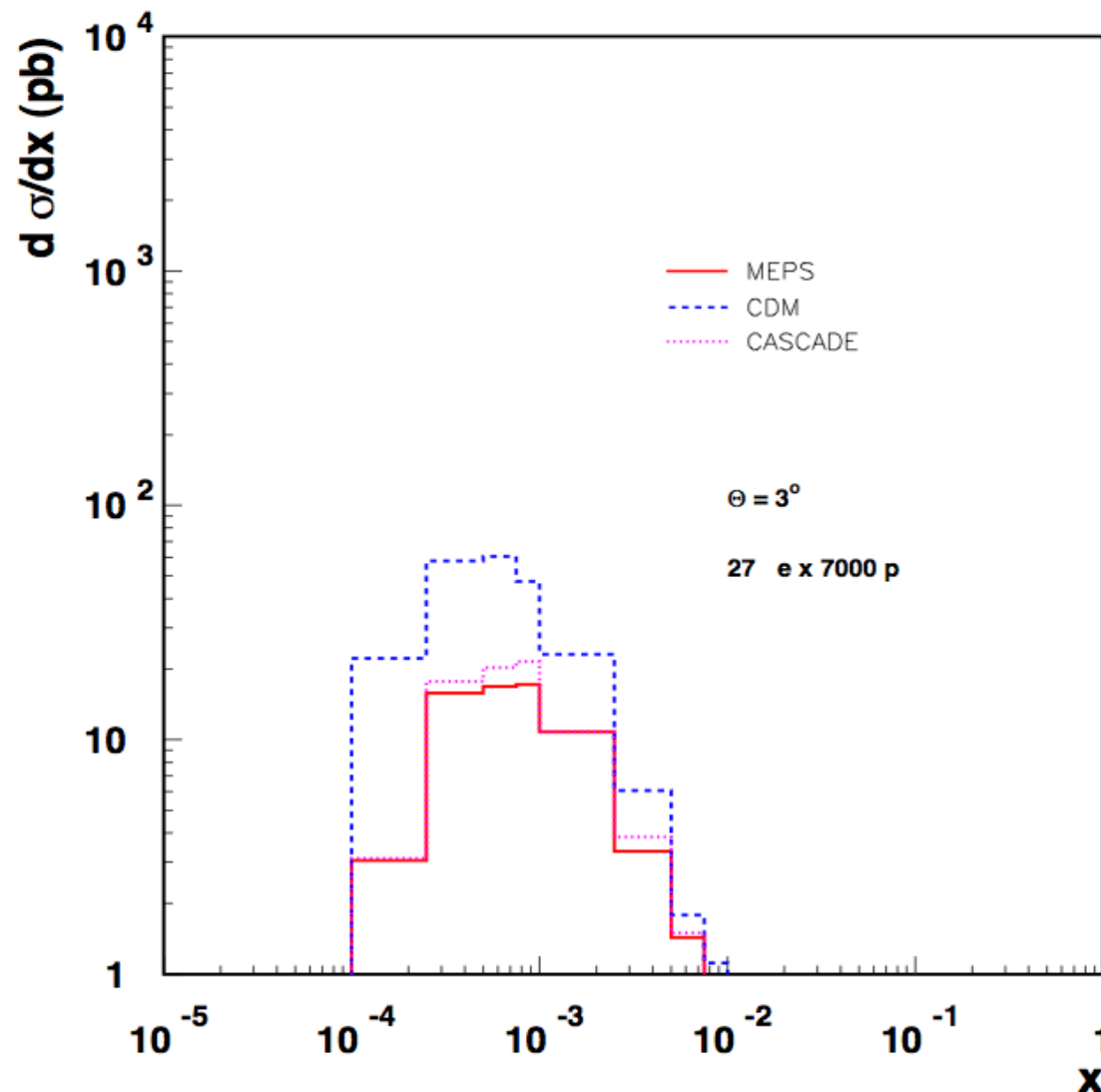
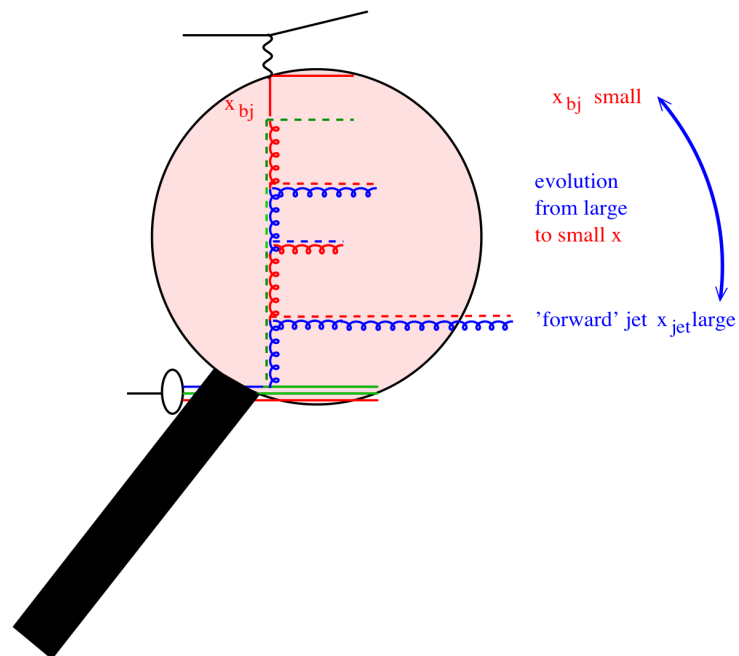


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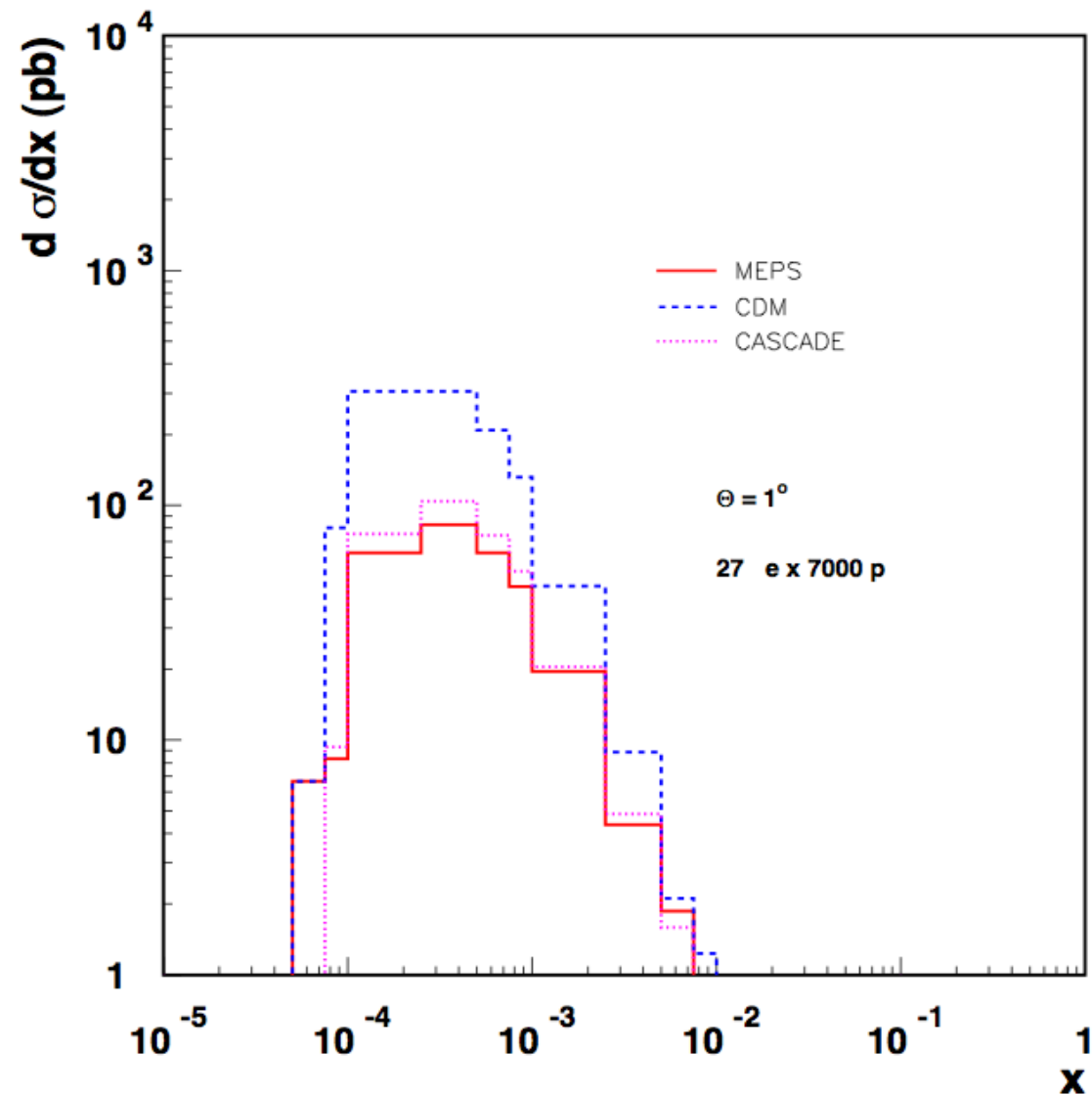
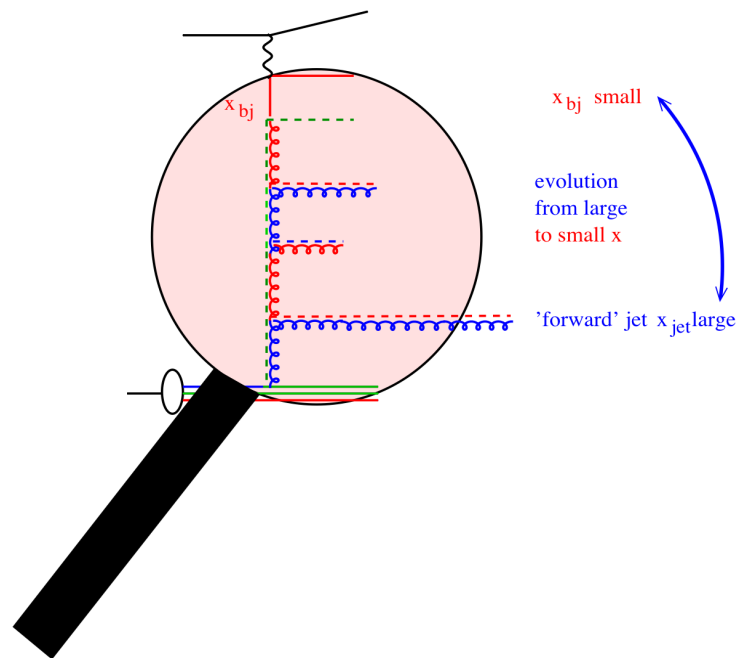


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- DIS and forward jet:

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# Evolution of uPDFs and x-section

- unintegrated PDFs (uPDFs): keep full  $k_T$  dependence during perturbative evolution

→ using **D**<sub>okshitzer</sub> **G**<sub>ribov</sub> **L**<sub>ipatov</sub> **A**<sub>ltarelli</sub> **P**<sub>arisi</sub>, **B**<sub>alitski</sub> **F**<sub>adin</sub> **K**<sub>uraev</sub> **L**<sub>ipatov</sub> or

**C**<sub>iafaloni</sub> **C**<sub>atani</sub> **F**<sub>iorani</sub> **M**<sub>archesini</sub> / **L**<sub>iinked</sub> **D**<sub>ipole</sub> **C**<sub>hain</sub> evolution equations

- **CCFM/LDC** treats explicitly real gluon emissions
  - according to color coherence ... angular ordering
  - angular ordering includes **DGLAP** and **BFKL** as limits...

- cross section (in  $k_T$  factorization) :

$$\frac{d\sigma^{jets}}{dE_T d\eta} = \sum \int \int \int dx_g dQ^2 d \dots [dk_{\perp}^2 x_g \mathcal{A}_i(x_g, k_{\perp}^2, \bar{q})] \hat{\sigma}_i(x_g, k_{\perp}^2)$$

- can be reduced to the collinear limit:

$$\frac{d\sigma^{jets}}{dE_T d\eta} = \sum \int \int \int dx dQ^2 d \dots x f_i(x, Q^2) \hat{\sigma}_i(x, Q^2, \dots)$$