

# Low- $x$ QCD with protons and nuclei at the LHC

**1st ECFA-CERN LHeC Workshop**

Divonne les Bains, 1<sup>st</sup> – 3<sup>rd</sup> Sept. 2008

**David d'Enterria**



# Overview

## ■ Introduction:

- Parton structure & evolution at low- $x$ , gluon saturation
- Measurements of low- $x$  PDFs: processes, kinematic domains, ...

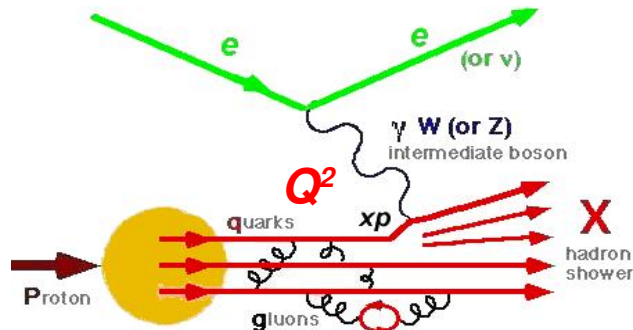
## ■ Experimental tests:

- Saturation hints at HERA (proton)
- Saturation hints at RHIC (nucleus)
- Low- $x$  perspectives at the LHC (proton & nucleus):
  - pp @ 14 TeV: forward (di)jets, QQbar, heavy-Q ...
  - PbPb @ 5.5 TeV:  $dN_{\text{ch}}/d\eta$ ,  $Y$  photo-production

## ■ Summary & Outlook (LHeC).

# Parton densities at low-x

- DIS e-p collisions probe distributions of partons in the proton:



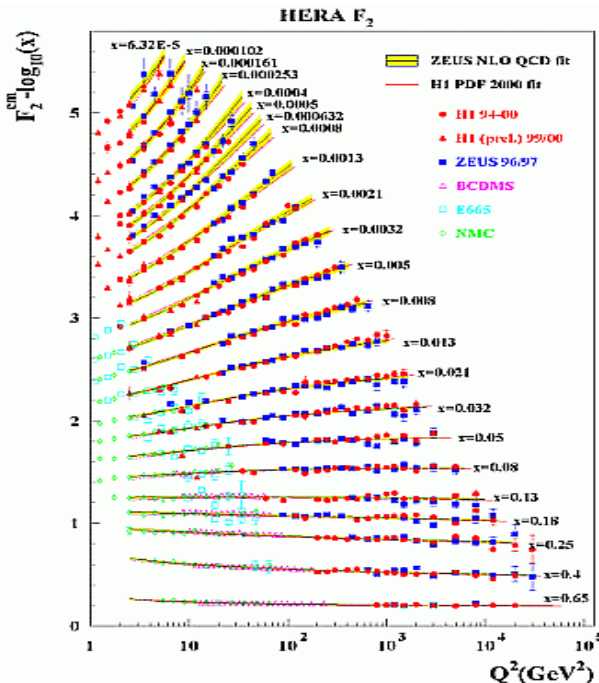
$Q^2$  = “resolving power”

*Bjorken x* = momentum fraction carried by parton

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{x Q^4} [Y_+ \cdot F_2 \mp Y_- \cdot xF_3 - y^2 \cdot FL]$$

$F_2, F_3, F_L$  = proton structure functions, ( $y$  = inelasticity).

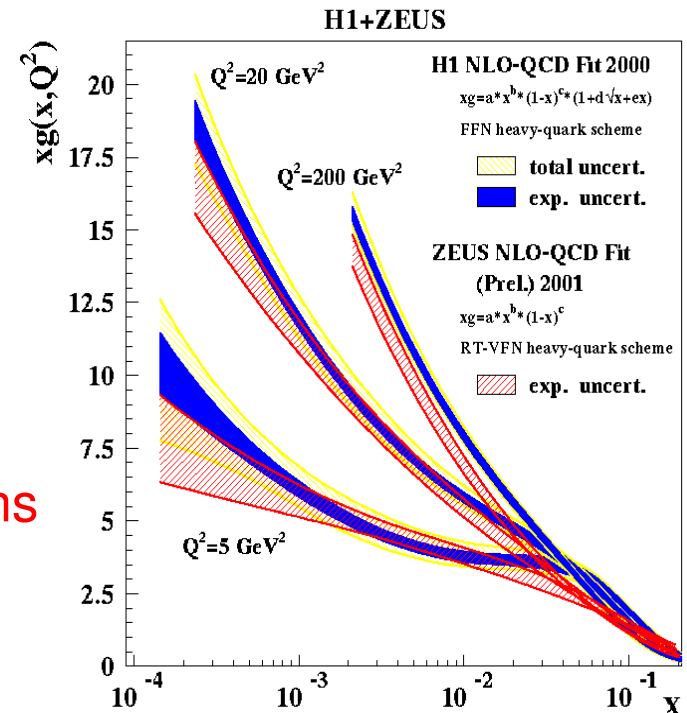
- HERA: strong rise of  $F_2(x, Q^2)$  at low-x:



$\gamma$  couples directly only to (sea) quarks



$$\partial \ln F_2 / \partial \ln Q^2 \propto \text{gluons}$$



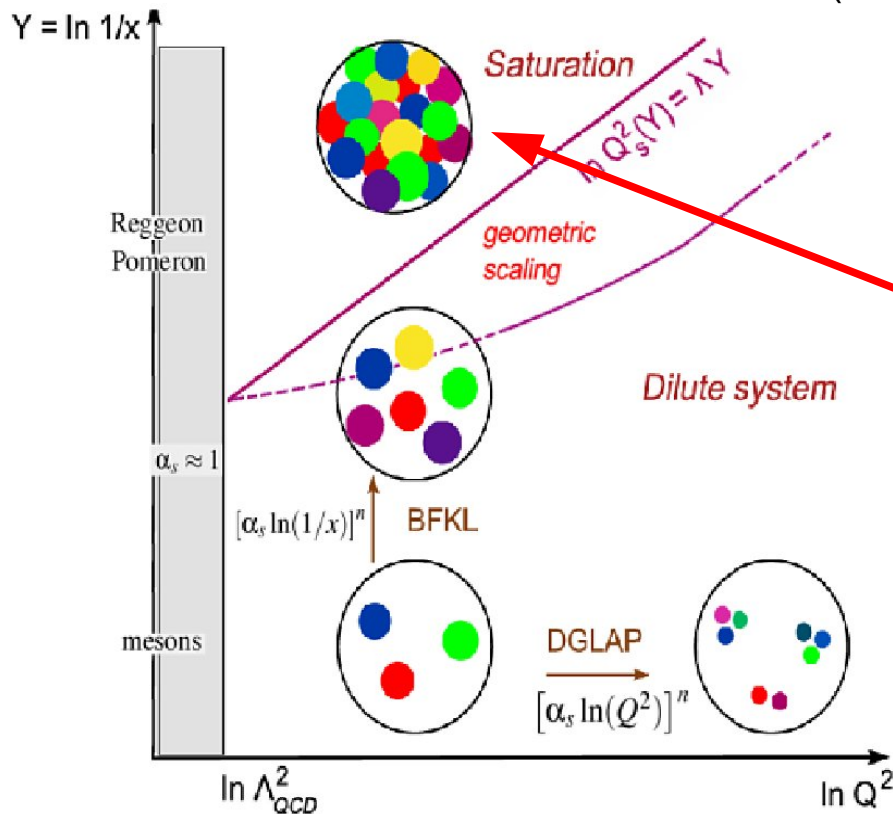
# $(x, Q^2)$ evolution of PDFs

■  **$Q^2$  - DGLAP** ( $k_T$ -order'd emission):  $F_2(Q^2) \sim \alpha_s \ln(Q^2/Q_0^2)^n$ ,  $Q_0^2 \sim 1 \text{ GeV}^2$  [LT, coll.factoriz.]

■  **$x$  - BFKL** ( $p_L$ -ordered emission):  $F_2(x) \sim \alpha_s \ln(1/x)^n$  [uPDFs,  $k_T$ -factoriz.]

■ **Linear equations** – single parton radiation/splitting – cannot work at low- $x$

(even less for multi-parton systems = nuclei):



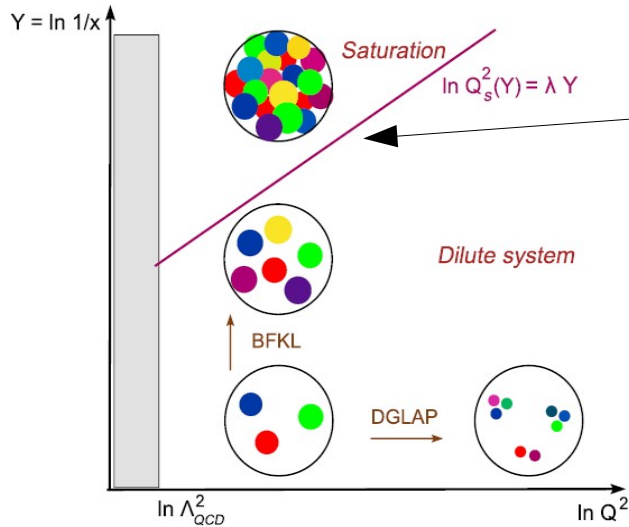
(i) Too high gluon density: **nonlinear gluon-gluon fusion** balances branchings

(ii) pQCD (collinear &  $k_T$ ) **factorization** assumptions invalid (HT, no incoherent parton scatt.)

(iii) **Violation of unitarity** even for  $Q^2 \gg \Lambda^2$  (too large perturbative cross-sections)

# Saturation scale $Q_s$

- **Onset** of non-linear QCD when **gluons** are numerous enough (low-x) & “large” enough (low- $Q^2$ ) to **overlap**:



$$Q_s^2 \sim \alpha_s \frac{x G_A(x, Q_s^2)}{\pi R_A^2}$$

$$\sim A^{1/3} x^{-\lambda} \sim A^{1/3} (\sqrt{s})^\lambda \sim A^{1/3} e^{\lambda y} \quad \lambda \sim 0.3$$

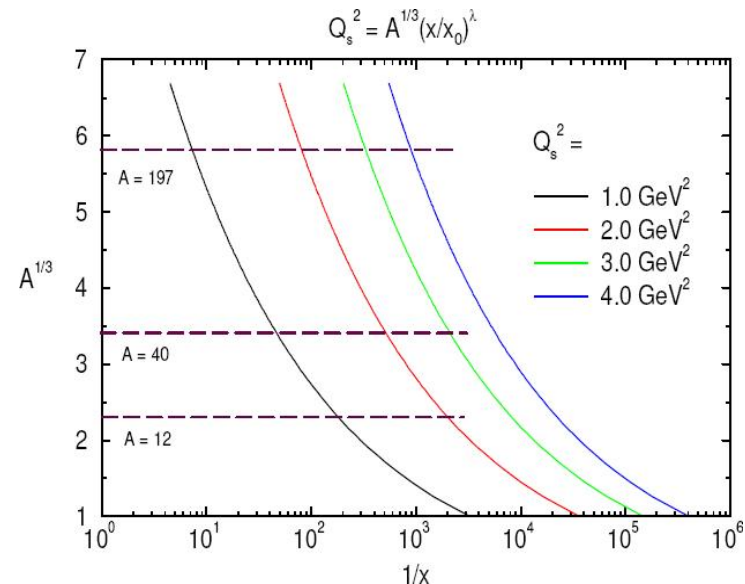
Saturation for: **low x, large s, large y, large A**

- **Nucleus** (larger parton transverse density) **amplifies saturation** effects:

$$Q_s^2 \sim A^{1/3} \sim 6$$

$$Q_s^2 \sim 1 \text{ GeV}^2 \text{ (HERA,p)}$$

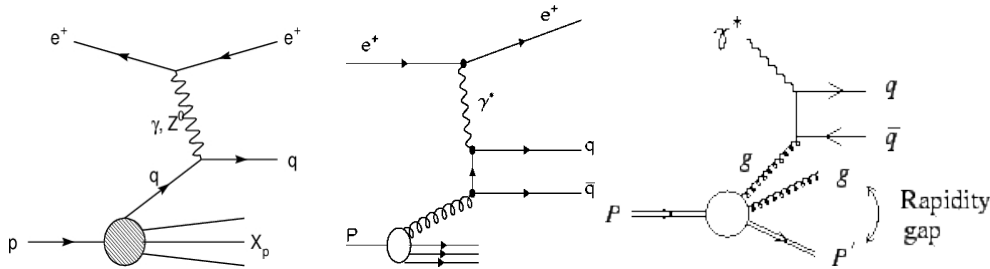
$$Q_s^2 \sim 2 \text{ GeV}^2 \text{ (e)RHIC (Au), } 5 \text{ GeV}^2 \text{ (LHC,Pb)}$$



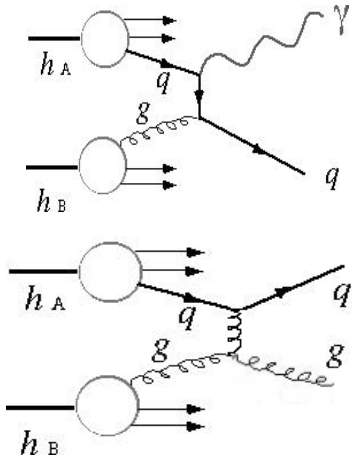
# Experimental access to low-x gluon PDF

## ■ Perturbative processes:

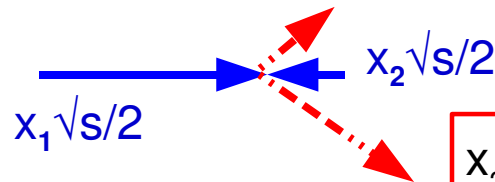
- ▶ e-p:  $\partial \ln F_2 / \partial \ln Q^2$ ,  $F_L$ , heavy- $Q$ , diffractive  $Q\bar{Q}$ :



- ▶ p-p, A-A: prompt  $\gamma$ , (di)jets:

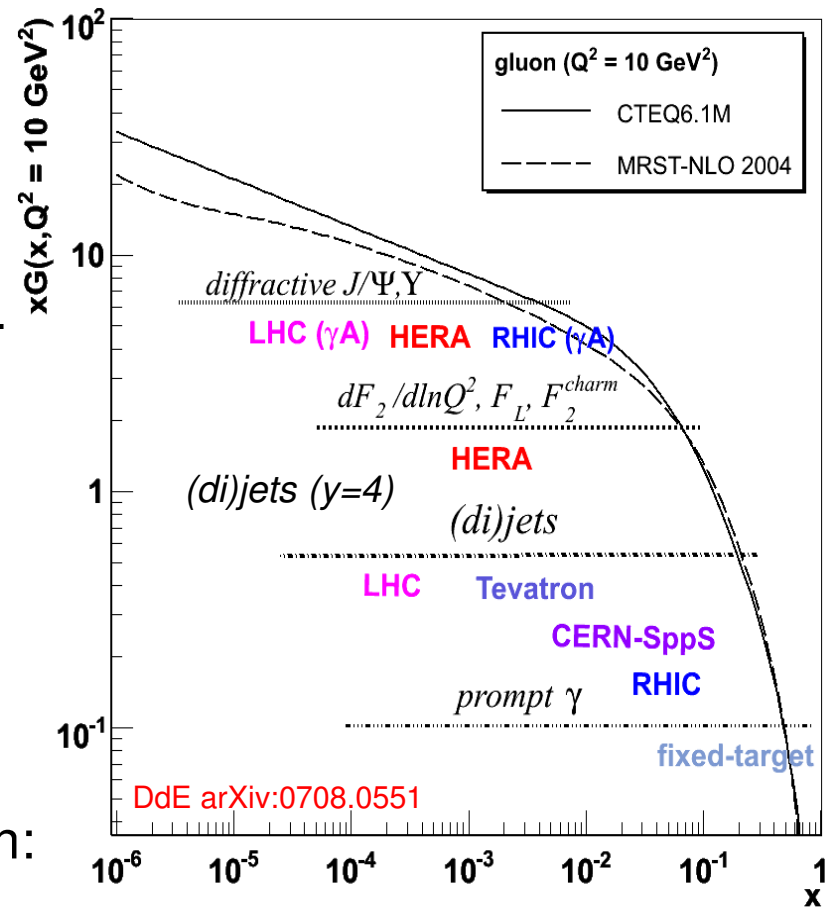


- ▶ Forward production:



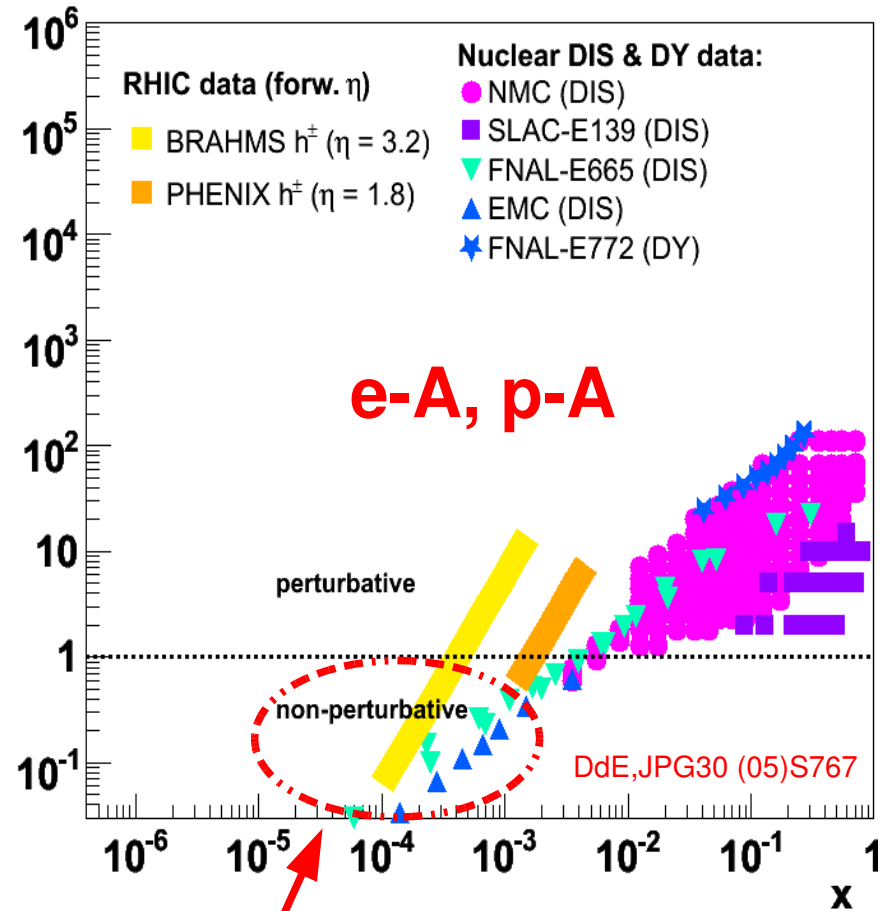
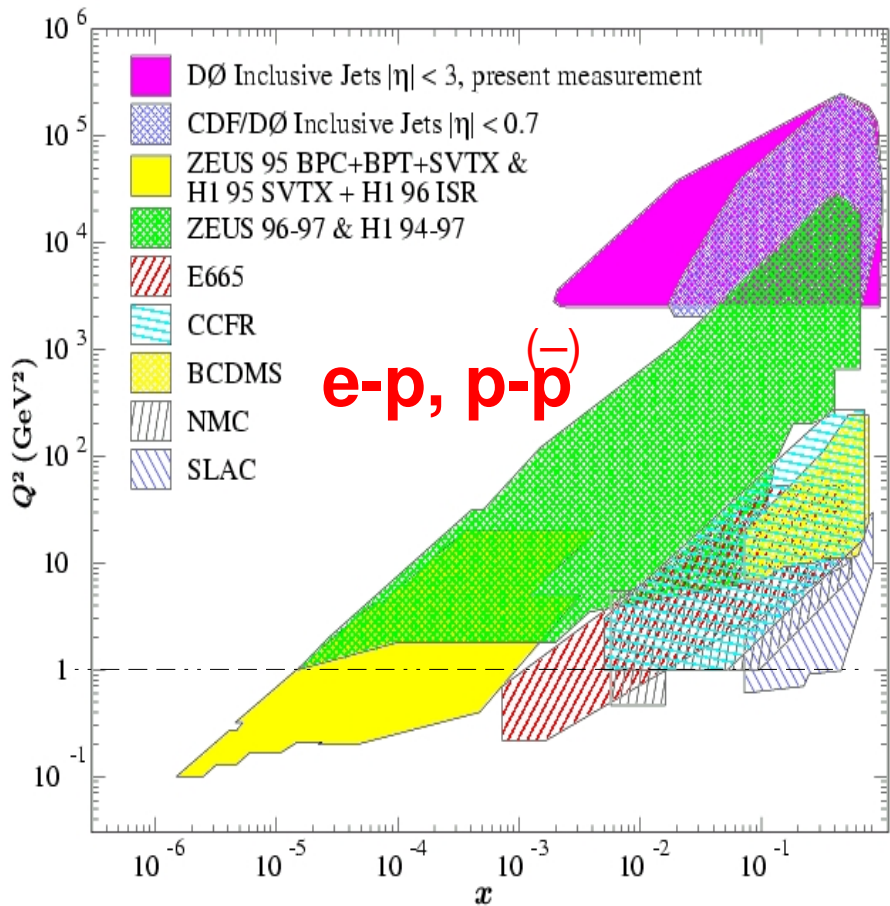
$$x_2^{\min} \sim p_T / \sqrt{s} \cdot e^{-y} = x_T \cdot e^{-y}$$

Every 2-units of  $y$ ,  $x^{\min}$  decreases by  $\sim 10$



# $(x, Q^2)$ experimental domains: proton, nucleus

■ Kinematical  $(x, Q^2)$  domains covered experimentally:



■ Note: most existing **low-x nPDFs** measurements in **non-perturbative** range

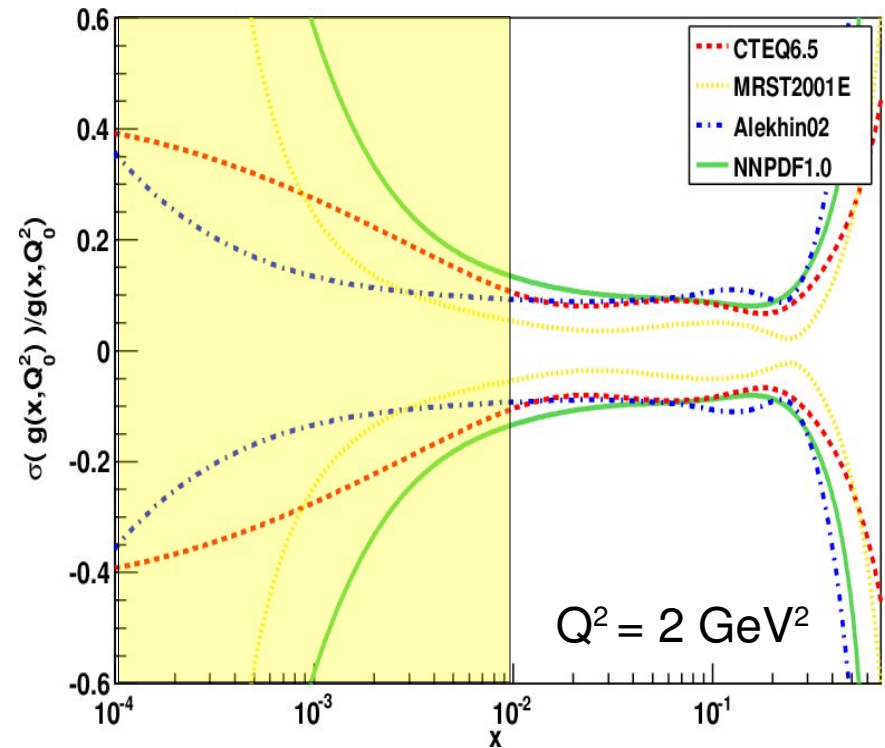
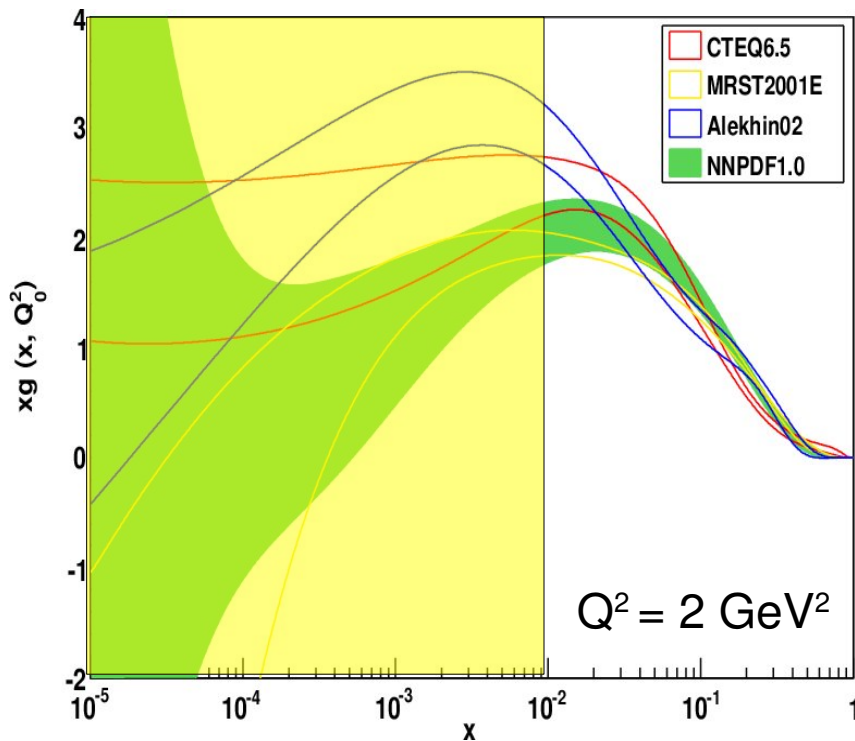
# Low-x gluon PDF (proton)

- Most of our current knowledge of **low-x gluons** comes **indirectly** from

$$F_2 \text{ scaling violations} : \frac{\partial F_2(x, Q^2)}{\partial \ln(Q^2)} \approx \frac{10\alpha_s(Q^2)}{27\pi} xg(x, Q^2)$$

- Large uncertainties** below  $x \sim 10^{-2}$  at moderate  $Q^2$  :

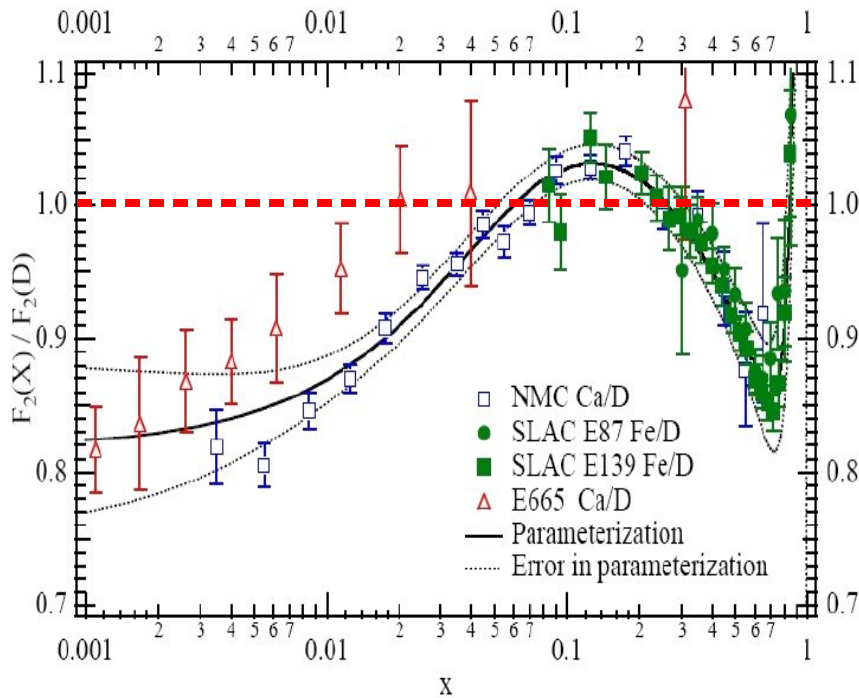
R.D. Ball *et al.* arXiv:0808.1231





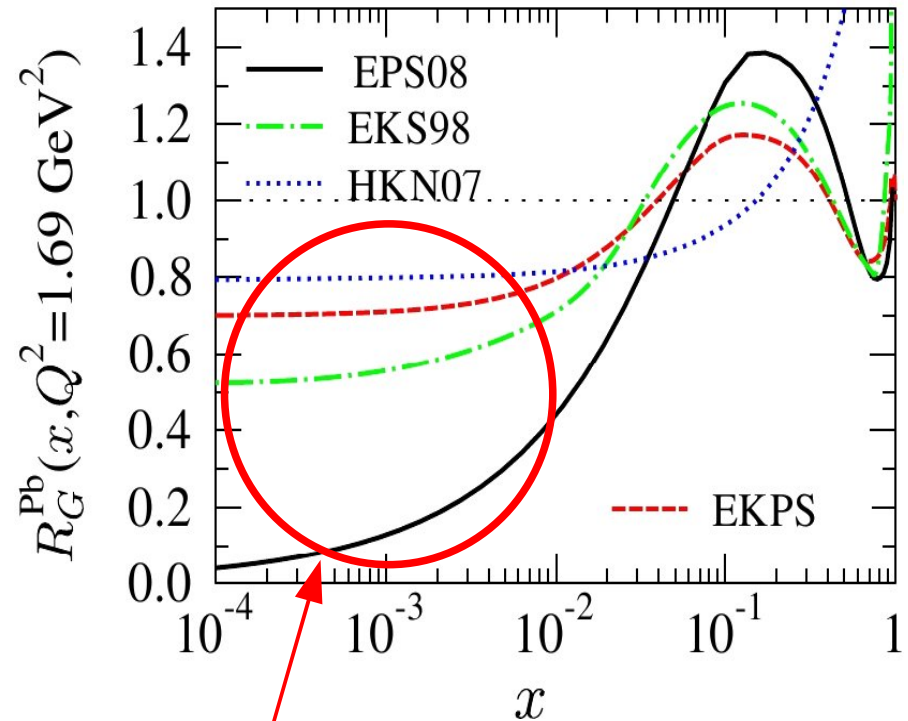
# Low-x gluon PDF (nucleus)

- Current knowledge of **low-x gluons** from:  
nuclear  $F_2$ , nuclear **Drell-Yan** (p-A), **high- $p_T$  hadrons** (d-Au, RHIC).
- Increasing **nuclear shadowing** below  $x \sim 0.1$



See e.g. M.Arneodo  
Phys. Rept. 240 (94) 301

K.Eskola et al. JHEP 0807 (08)102



- Nuclear  $xG(x, Q^2)$  **virtually unknown** below  $x \sim 10^{-3}$  !

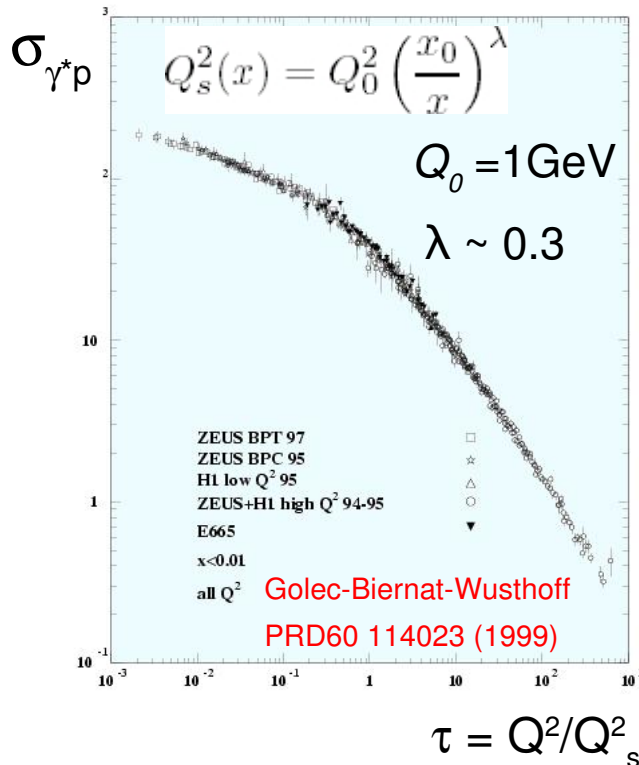
# Saturation hints at HERA: proton

- DGLAP fits most of e-p data. Saturation models explain better a few cases:

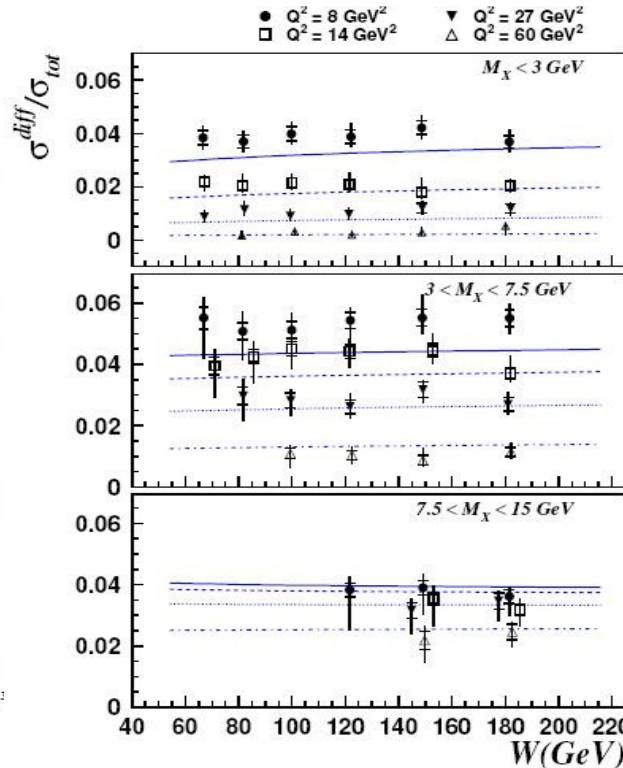
(1) “Geometric scaling”

(2) flat  $\sigma_{\text{diffract}}/\sigma_{\text{tot}}$  vs energy

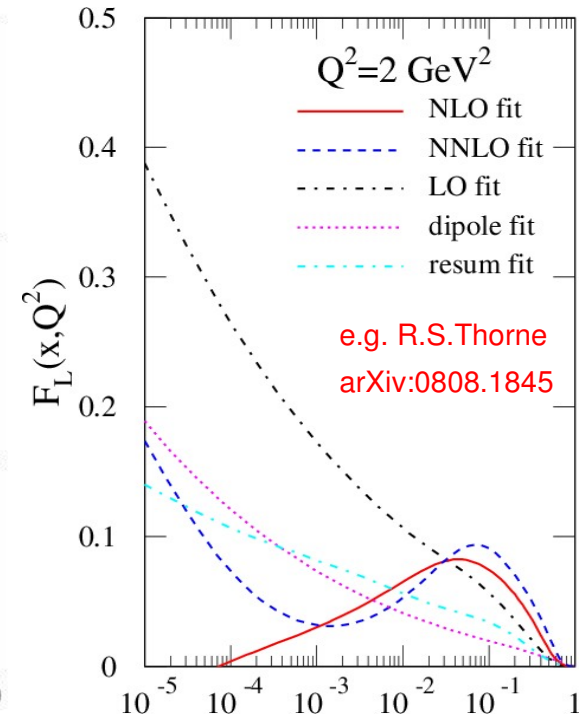
(3) Long. struc. function



Inclusive DIS x-section depends on **single scale**  $Q^2/Q_s^2$  for  $x < 0.01$



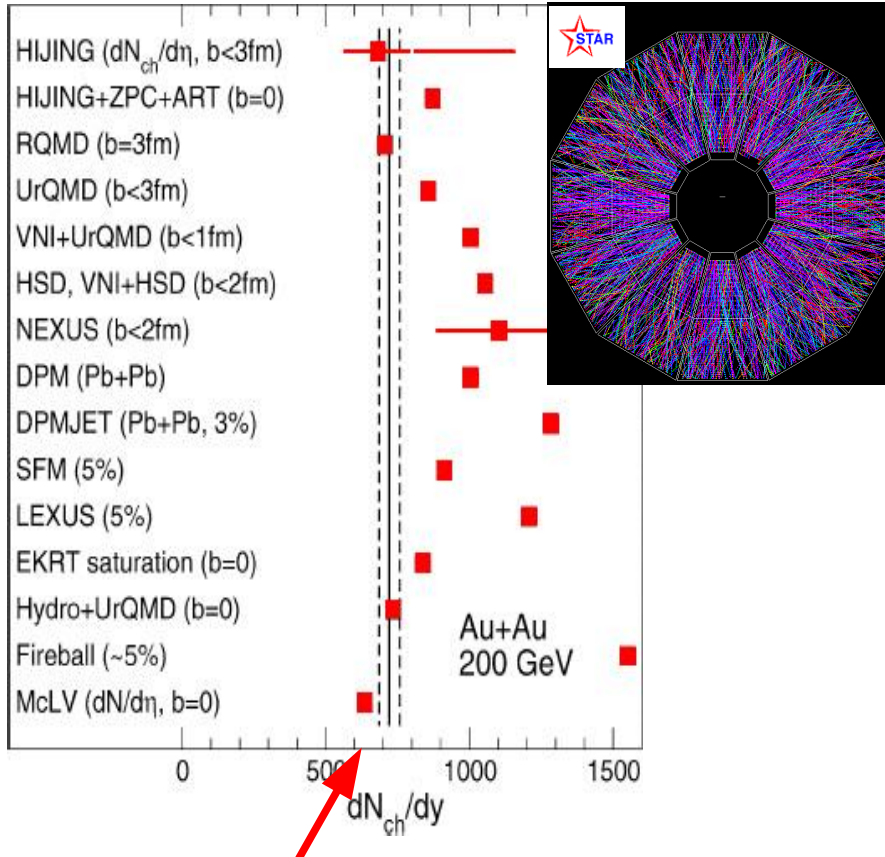
Diffract. & total x-sections similar  $W$  dependence  $\neq$  pQCD:  $\sigma_{\text{tot}} \sim W^{2\lambda} \neq \sigma_{\text{diff}} \sim W^{4\lambda}$



Gluon ( $F_L$ ) at NLO becomes **negative** for  $Q^2 \sim 2 \text{ GeV}^2$  at low- $x$

# Saturation hints at RHIC: nucleus

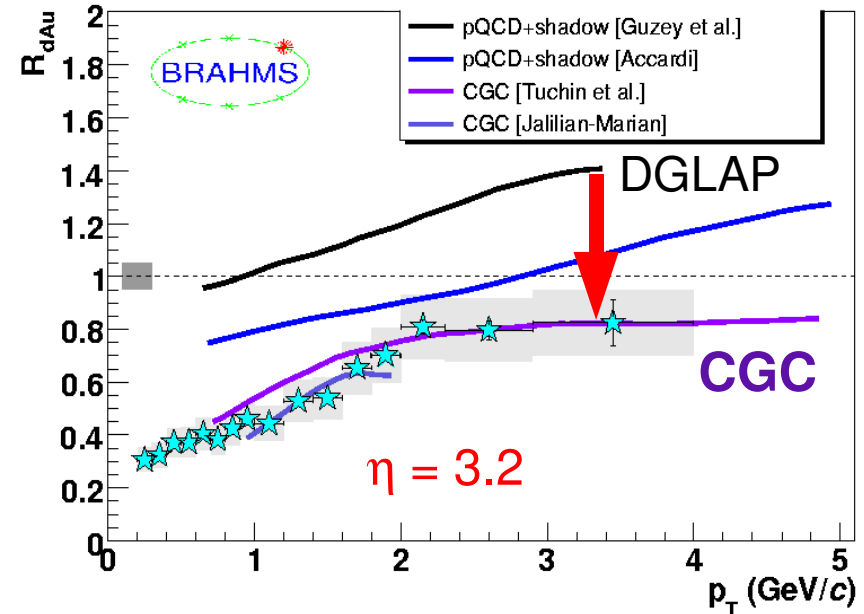
(1) Reduced Au-Au hadron multiplicities:



$dN_{ch}/d\eta \sim 650$  at  $\eta=0$  described by CGC (or models which include reduced incoming parton flux)

(2) Suppressed forward hadrons

( $\eta = 3.2$ ,  $p_T \sim 3 \text{ GeV}/c$ , i.e.  $x \sim 10^{-3}$ ):



$R_{dAu} \sim 0.8$  better described by CGC-models than NLO pQCD: reduced partonic flux in Au at low-x

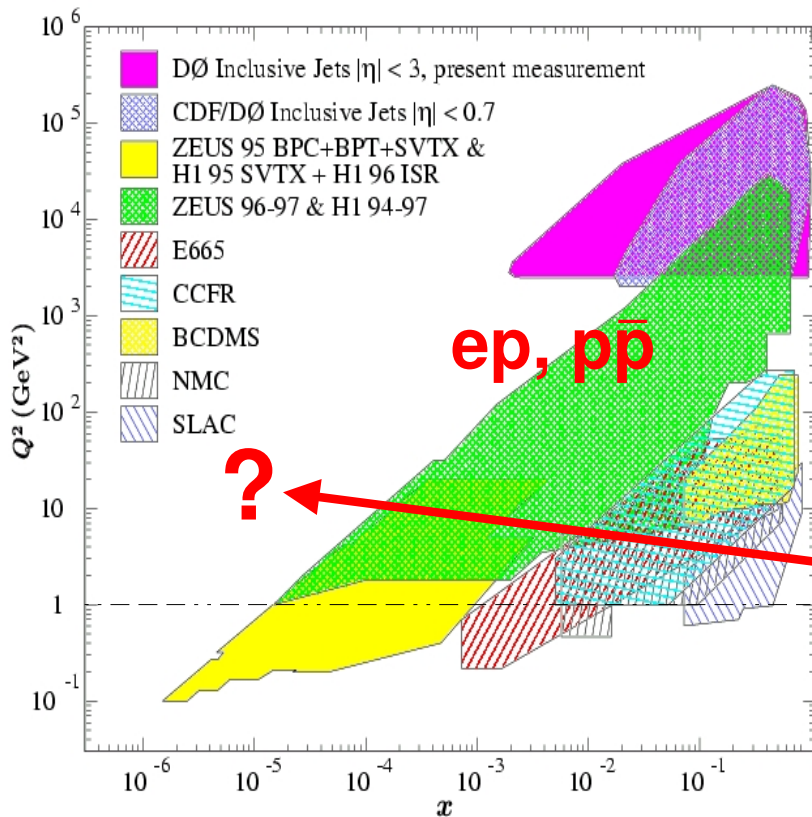
# Low-x studies at the LHC: proton

## ■ p-p @ 14 TeV :

(1) At  $y=0$ ,  $x=2p_T/\sqrt{s} \sim 10^{-3}$  (domain probed at HERA, Tevatron). **Go fwd. for  $x < 10^{-4}$**

(2) Saturation momentum:  $Q_s^2 \sim 1 \text{ GeV}^2$  ( $y=0$ ),  $3 \text{ GeV}^2$  ( $y=5$ )

(3) **Very large perturbative** cross-sections:



$$p(p_1) + p(p_2) \rightarrow \text{jet} + \gamma + X \quad \text{Prompt } \gamma$$

$$p(p_1) + p(p_2) \rightarrow l\bar{l} + X \quad \text{Drell-Yan}$$

$$p(p_1) + p(p_2) \rightarrow \text{jet}_1 + \text{jet}_2 + X \quad \text{Jets}$$

$$p(p_1) + p(p_2) \rightarrow Q + \bar{Q} + X \quad \text{Heavy flavour}$$

$$p(p_1) + p(p_2) \rightarrow W/Z + X \quad \text{W,Z production}$$

LHC **forward** rapidities:

e.g.  $y \sim 6$ ,  $Q \sim 10 \text{ GeV}$

**x down to  $10^{-6}$ !**

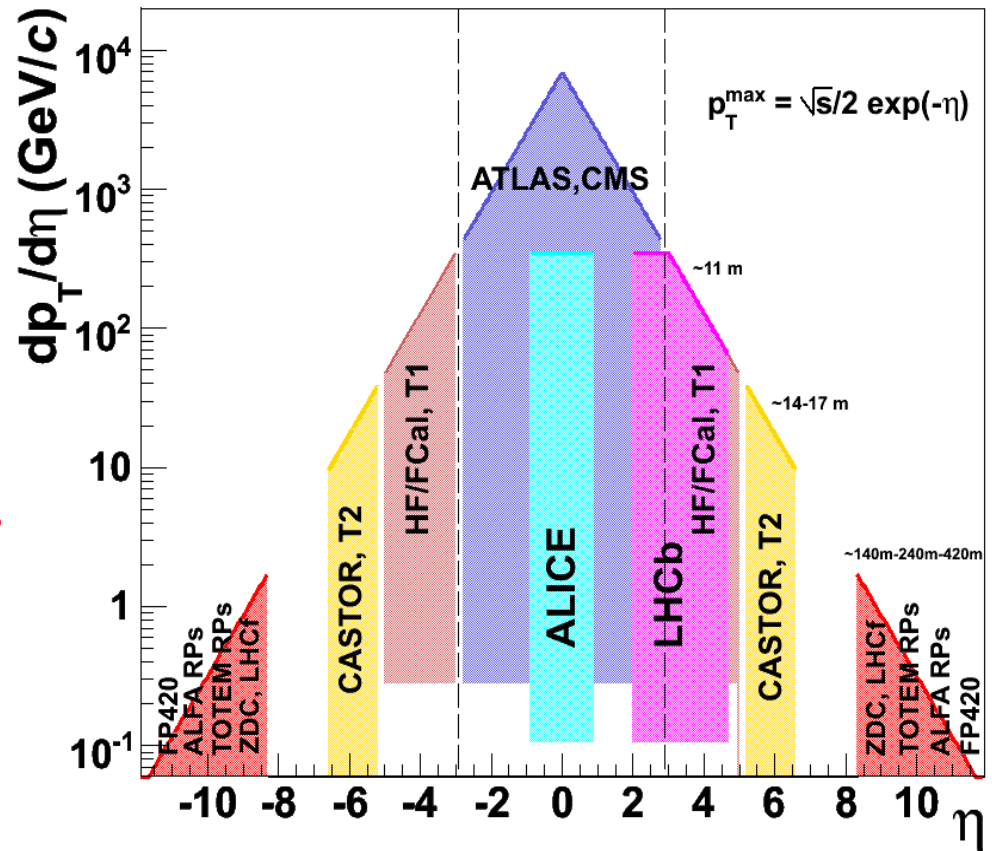
# Forward detectors at the LHC

- Most of phase-space  $\Delta y \sim 2 \times \ln(\sqrt{s})/m_p \sim 20$  covered:

1<sup>st</sup> time in a collider !

- ATLAS/CMS:  
forward **calorimeters**  
(up to  $|\eta| \sim 6.6$ )
- ALICE/LHCb:  
forward **muon spectrometers**  
(up to  $\eta = 5$ )
- TOTEM:  
forward **trackers**  
(up to  $|\eta| = 6.4$ )

DdE, arXiv:0806.0883



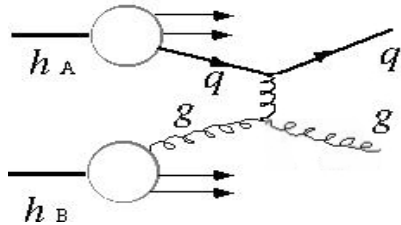
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Every 2-units of  $y$ ,  $x^{\min}$  decreases by  $\sim 10$

# Case-study I: Forward jets in CMS ( $3 < |\eta| < 6.6$ )

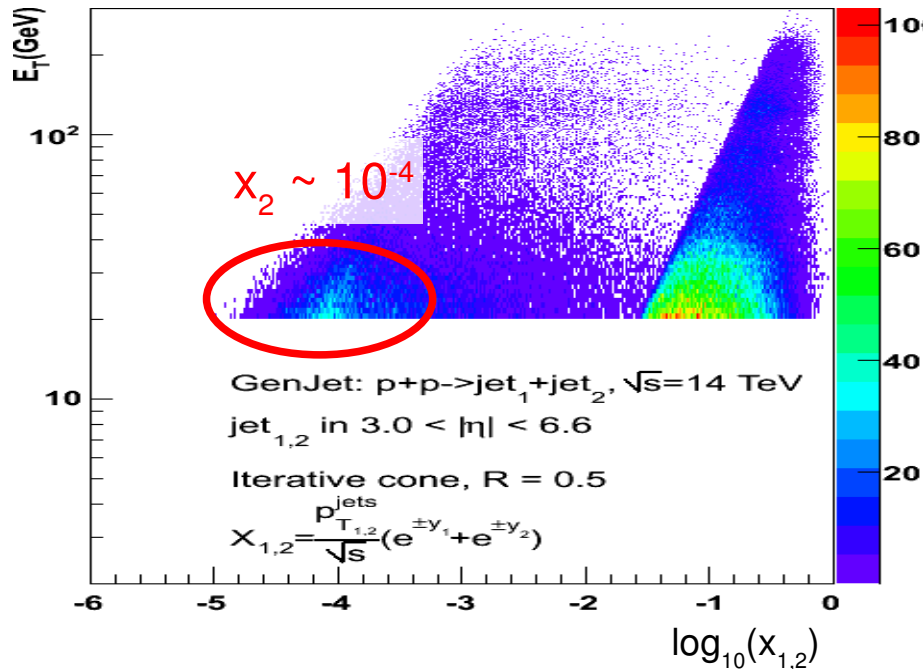
[S.Cerci, D.d'E, CMS]

■ **Forward jets** ( $E_T \sim 20-100$  GeV) sensitive to low-x PDFs:

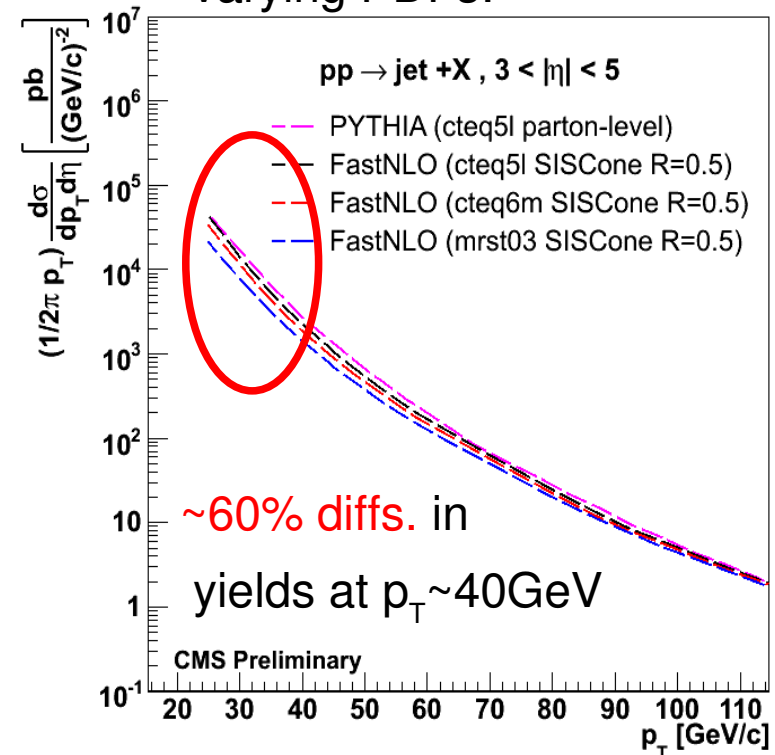


Jets in HF ( $3 < |\eta| < 5$ ) probe:  $x_2 \sim 10^{-4}$

Jets in CASTOR ( $5.1 < |\eta| < 6.6$ ):  $x_2 \sim 10^{-5}$



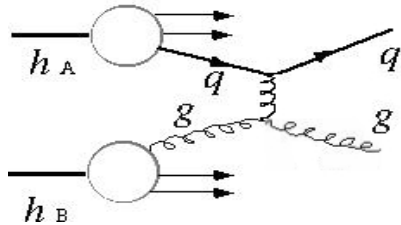
varying PDFs:



# Case-study I: Forward jets in CMS ( $3 < |\eta| < 6.6$ )

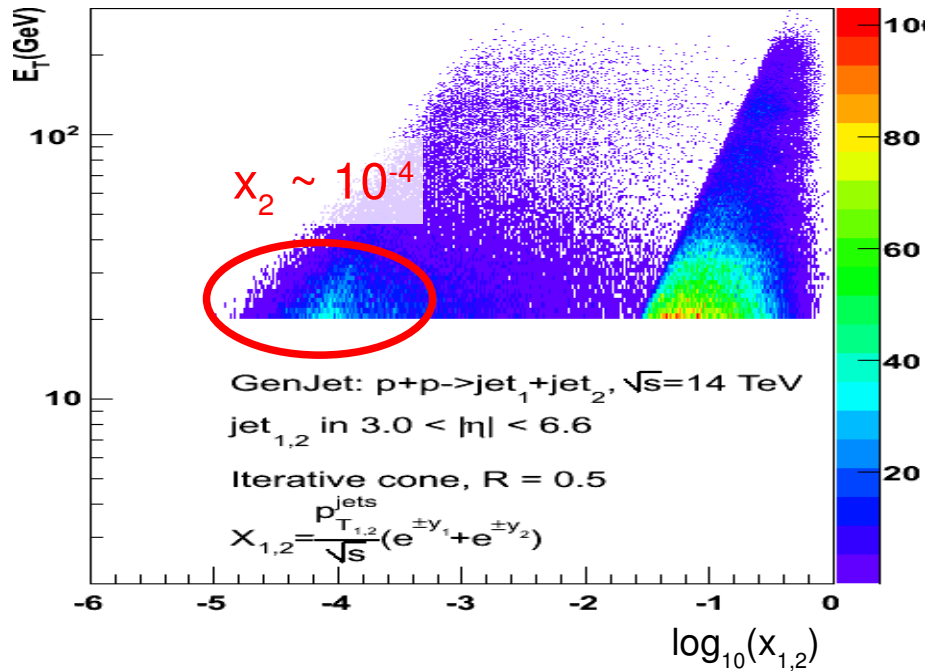
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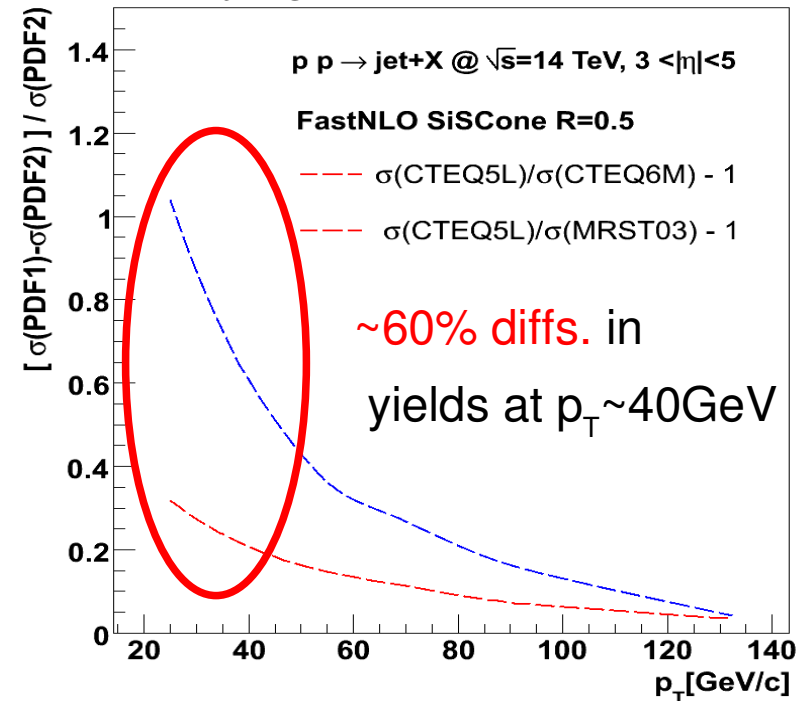


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varying PDFs:



# Case-study II: Mueller-Navelet dijets in CMS ( $\Delta\eta \sim 10$ )

- **Mueller-Navelet dijets** with large  $y$  separation very sensitive to low- $x$  QCD evolution (testing ground for **BFKL**):

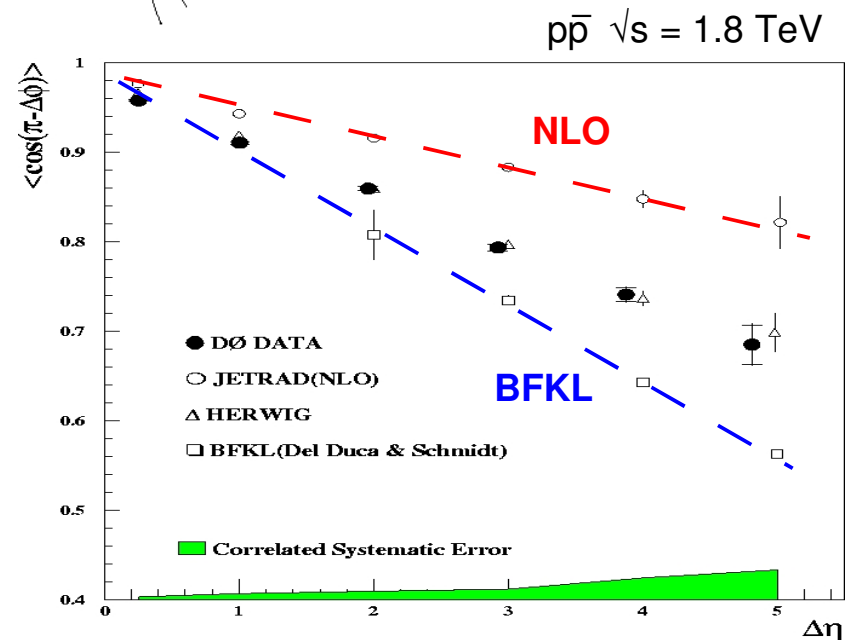
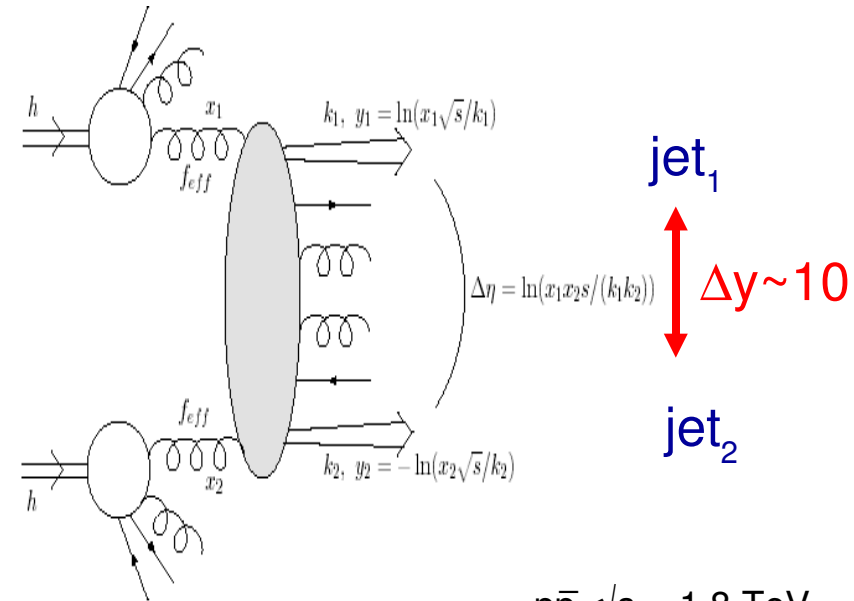
BFKL: **extra radiation** between the 2 jets will smooth out back-to-back topology

A.H.Mueller, H.Navelet, NPB282 (1987)727

(partially **compensated by gluon saturation** ?)

- Increased **azimuthal decorrelation** with increasing  $\Delta y$  (w.r.t. DGLAP collinear-factorization):

[DeDuca, Schmidt], [Orr, Stirling]  
 [A.Sabio-Vera, F.Schwennsen]  
 [C.Marquet, Royon] [E. Iancu et al.]



[D0 Collab, PRL77(97)595]

David d'Enterria (MIT)



# Case-study II: Mueller-Navelet dijets in CMS ( $\Delta\eta \sim 10$ )

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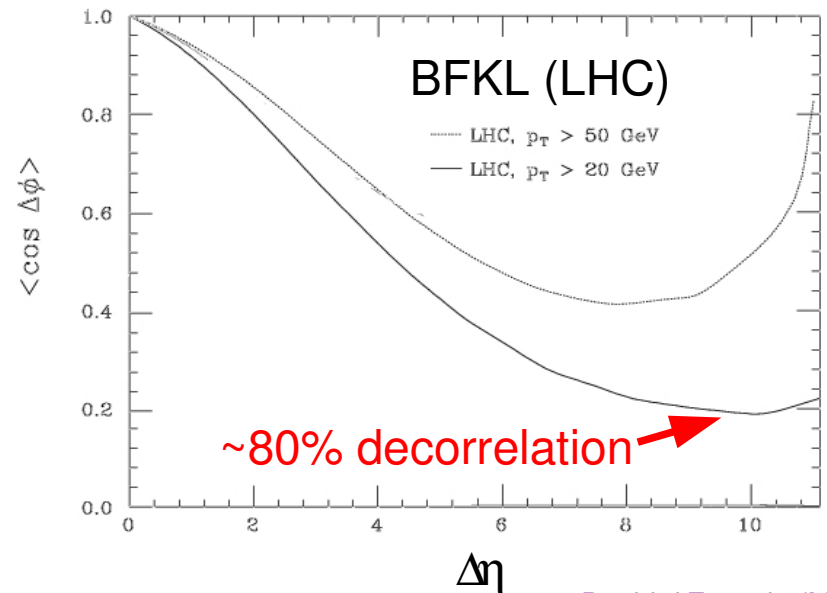
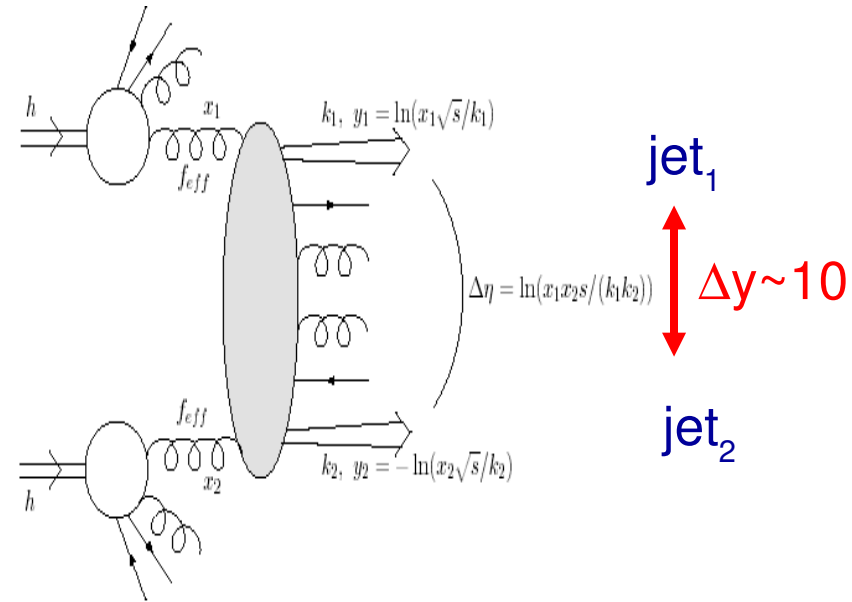
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# Case-study II: Mueller-Navelet dijets in CMS ( $\Delta\eta \sim 10$ )

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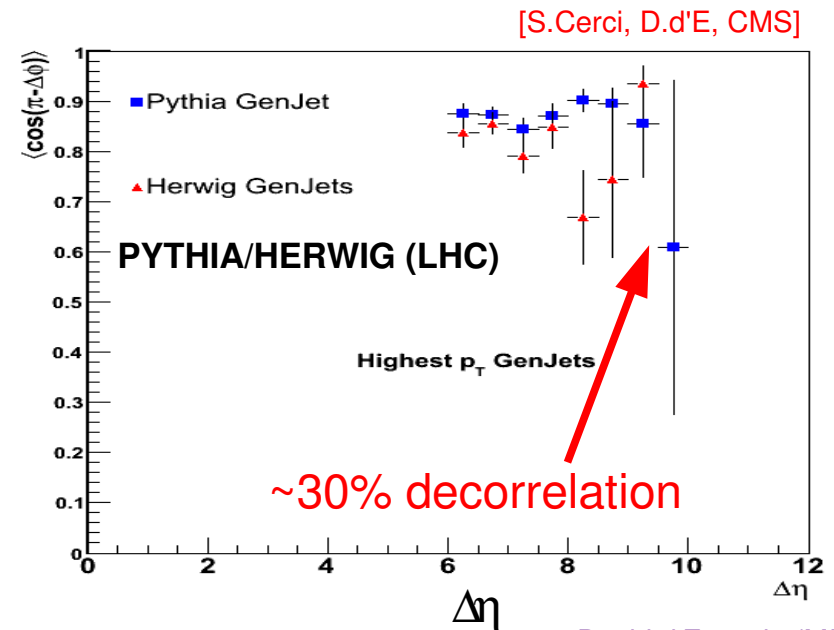
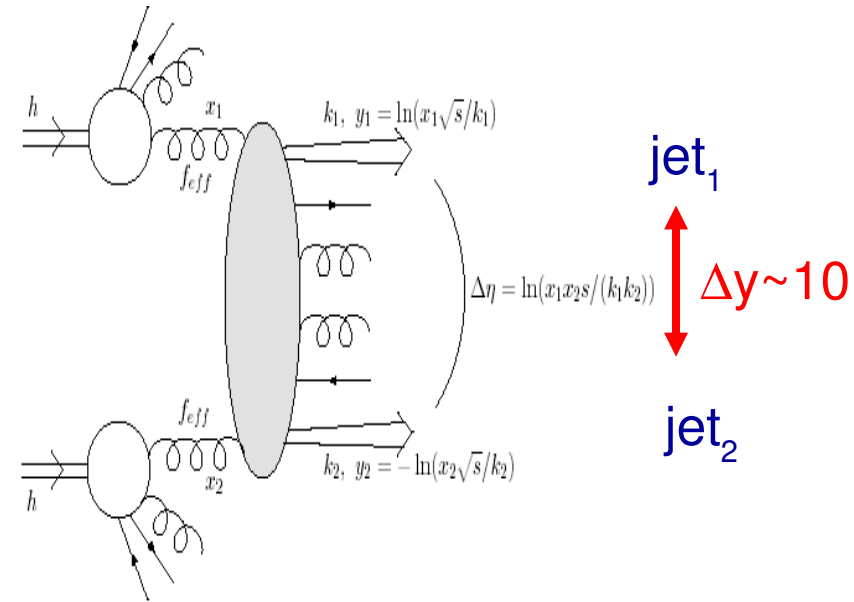
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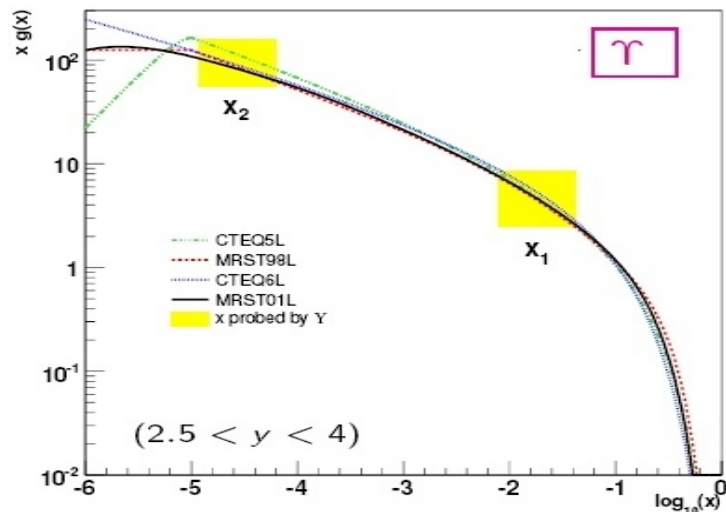
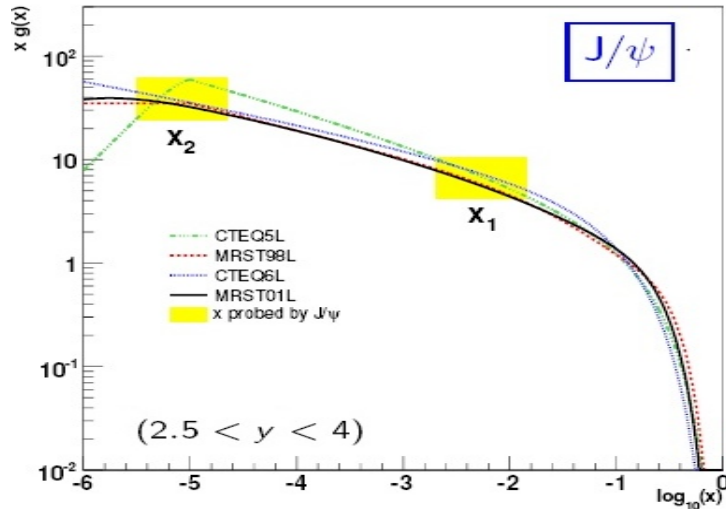
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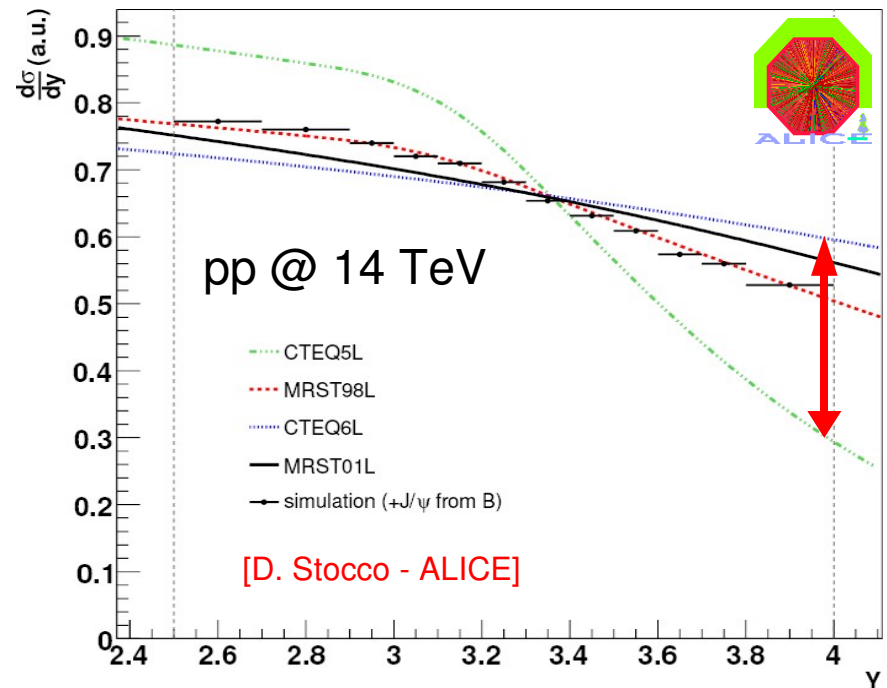


# Case-study III: Forward $Q\bar{Q}$ in ALICE ( $2.5 < |\eta| < 4$ )

- $J/\psi$  measurement in  $\mu$ -spectrometer:  $xg(x)$  in the proton at  $x_2 \sim 10^{-5}$  :



$d\sigma/dy$   $J/\psi$ : NLO CEM w/ varying PDFs



$Q\bar{Q}$ bar: Sensitive to diff. PDFs and  
**DGLAP versus CGC** predictions  
 (Note:  $m_{J/\psi} \sim Q_s$  at the LHC)

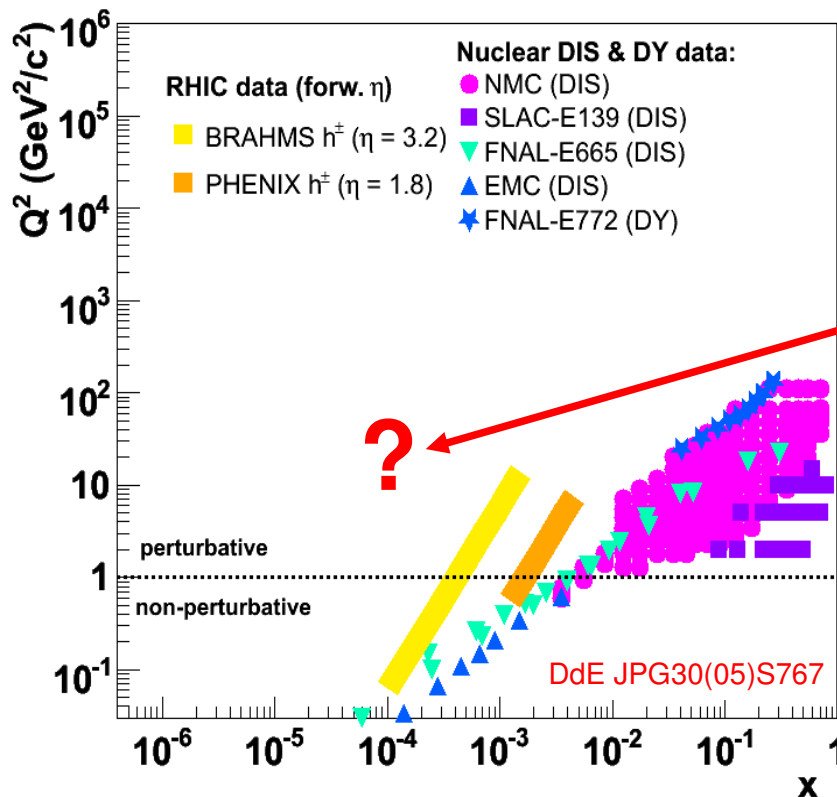
# Low- $x$ studies at the LHC: nucleus

■ Pb-Pb @ 5.5 TeV, p-Pb @ 8.8 TeV:

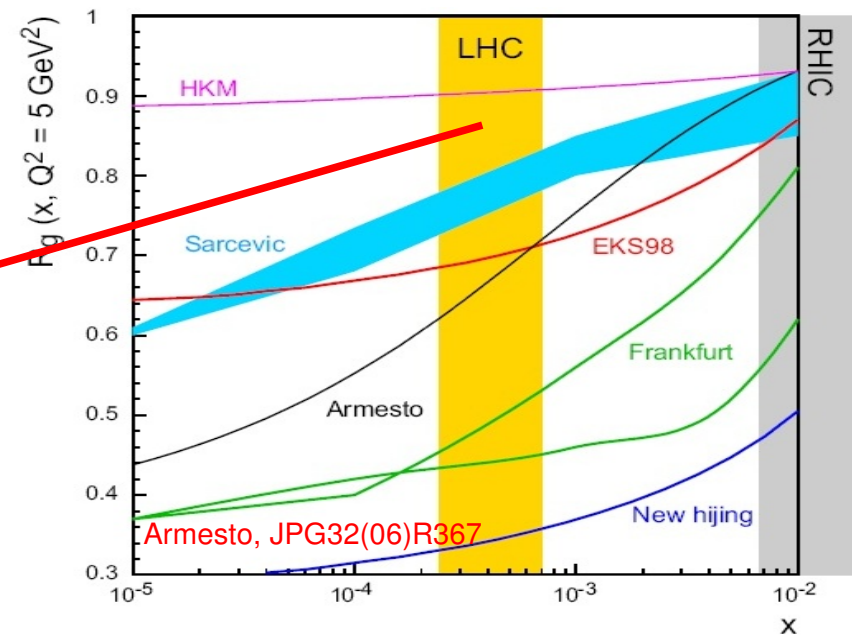
(1) Bjorken  $x=2p_T/\sqrt{s} \sim 30\text{-}45$  times lower than Au-Au, d-Au @ RHIC !

(2) Saturation enhanced ( $A^{1/3} \sim 6$ ) :  $Q_s^2 \sim 5 \text{ GeV}^2$

(3) Very large perturbative cross-sections.



Ratio of Pb/p gluon densities:



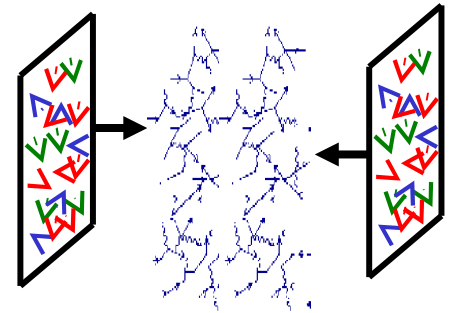
Nuclear  $xG(x, Q^2)$  unknown for  $x < 10^{-3}$  !

# Case-study I: Total Pb-Pb hadron multiplicity

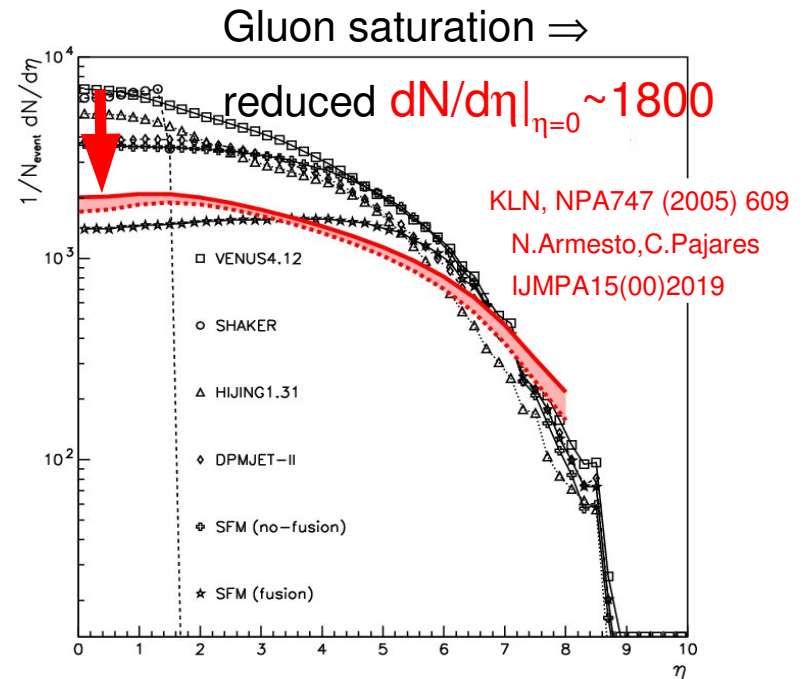
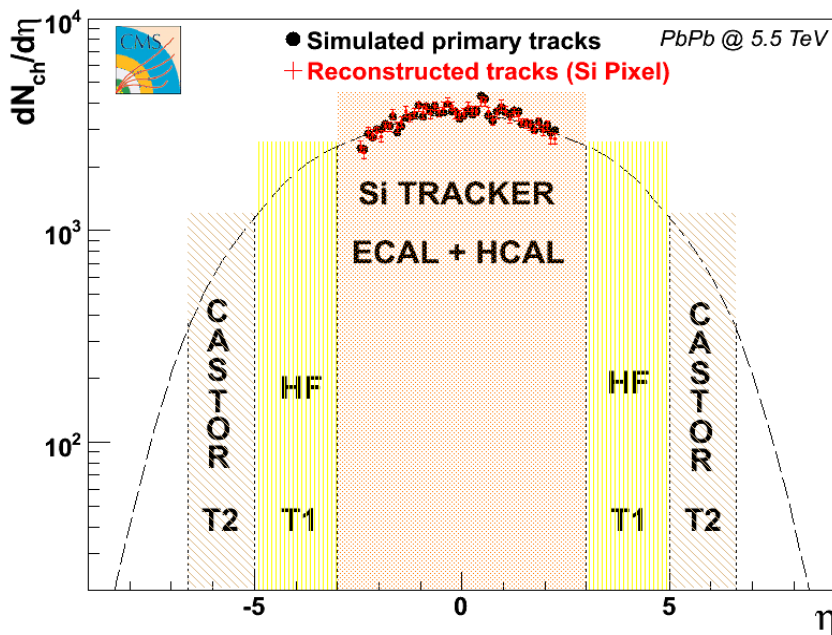
- Final A+A multiplicity  $\propto$  Initial number of released gluons :

CGC: 
$$\frac{dN}{d^2bd\eta} \propto \frac{1}{\alpha_s(Q_s^2)} Q_s^2 \propto xG(x, Q_s^2) \cdot A^{1/3}$$

+ “local parton-hadron duality” (1 gluon = 1 final hadron)



- CMS  $dN_{ch}/d\eta$  ( $|\eta| < 2.5$ ) via hit counting in Si pixel layers:



# Case-study II: $\Upsilon$ photoproduction in UPCs ( $\gamma$ Pb)

[DdE, hep-ex/0703024]

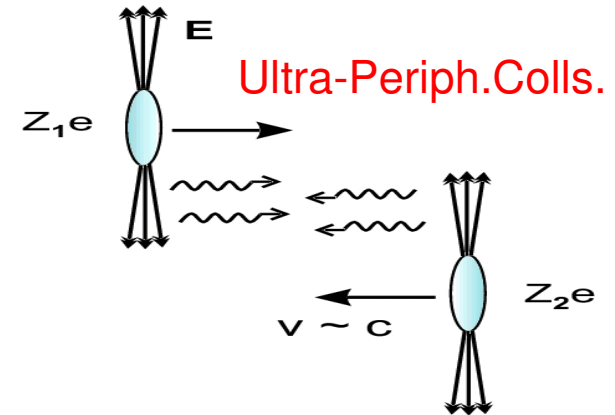
- High-energy heavy-ions produce **strong E.M. fields**

due to coherent action of  $Z_{\text{Pb}} = 82$  protons:

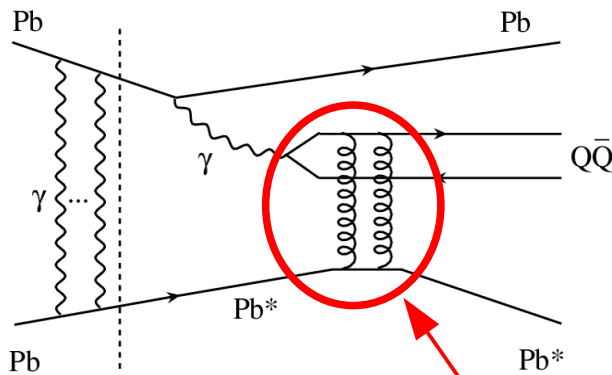
- Equivalent **photon flux**:

$$E_{\gamma}^{\text{max}} \sim 80 \text{ GeV (PbPb-LHC)}$$

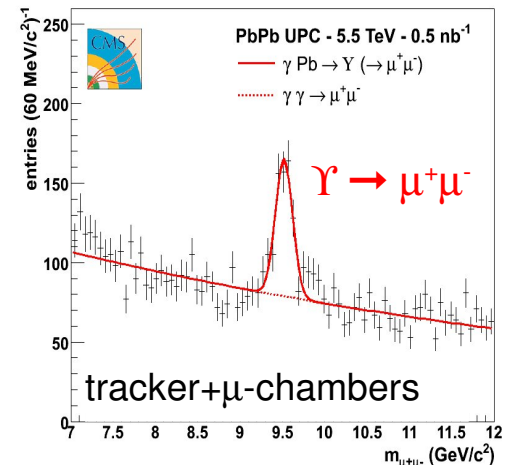
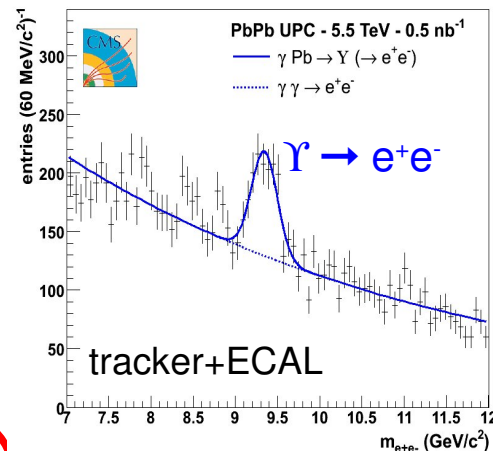
$$\gamma \text{ Pb: max. } \sqrt{s}_{\gamma \text{ Pb}} \approx 1. \text{ TeV} \approx \boxed{3. - 4. \times \sqrt{s}_{\gamma \text{ p}} \text{ (HERA)}}$$



- $Q\bar{Q}$  diffractive photoproduction (ZDC neutron-tagging) sensitive to  $|xG|^2$



$$\left. \frac{d\sigma_{\gamma p, A \rightarrow V p, A}}{dt} \right|_{t=0} = \frac{\alpha_s^2 \Gamma_{ee}}{3\alpha M_V^5} 16\pi^3 \left[ xG(x, Q^2) \right]^2$$



$\sim 500 \Upsilon / 0.5 \text{ nb}^{-1}$  expected in CMS

# Outlook: proposed nuclear DIS facilities

DdE, arXiv:0706.4182

## ■ eRHIC:

(e<sup>-</sup>) 20 GeV – (A) 100 GeV

$\sqrt{s} \sim 60 \text{ GeV}$ ,  $\mathcal{L} \sim 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

## ■ LHeC:

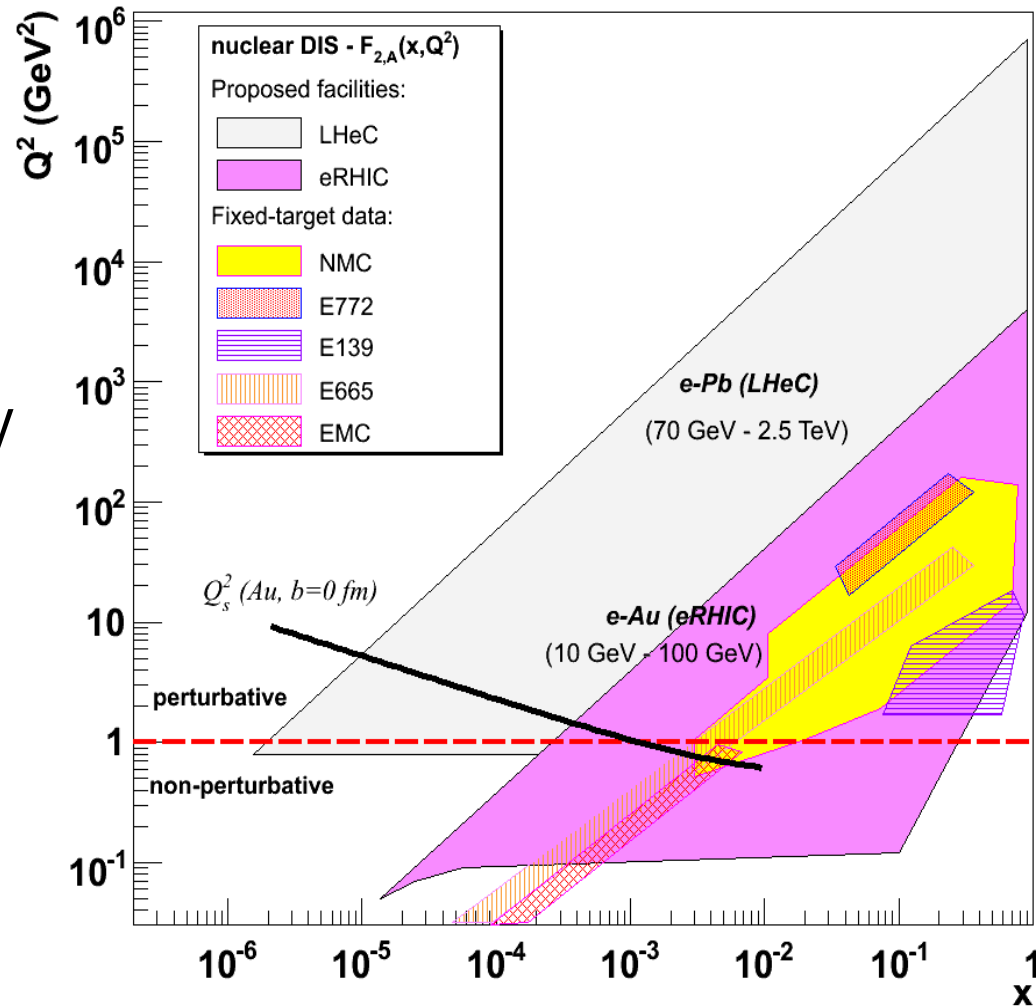
(e<sup>-</sup>) 70 GeV – (p,A) 2.75, 7 TeV

$\sqrt{s} \sim 0.9, 1.4 \text{ TeV}$ ,  $\mathcal{L} \sim 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

Huge increase in nuclear  
(x, Q<sup>2</sup>) kinematical reach !

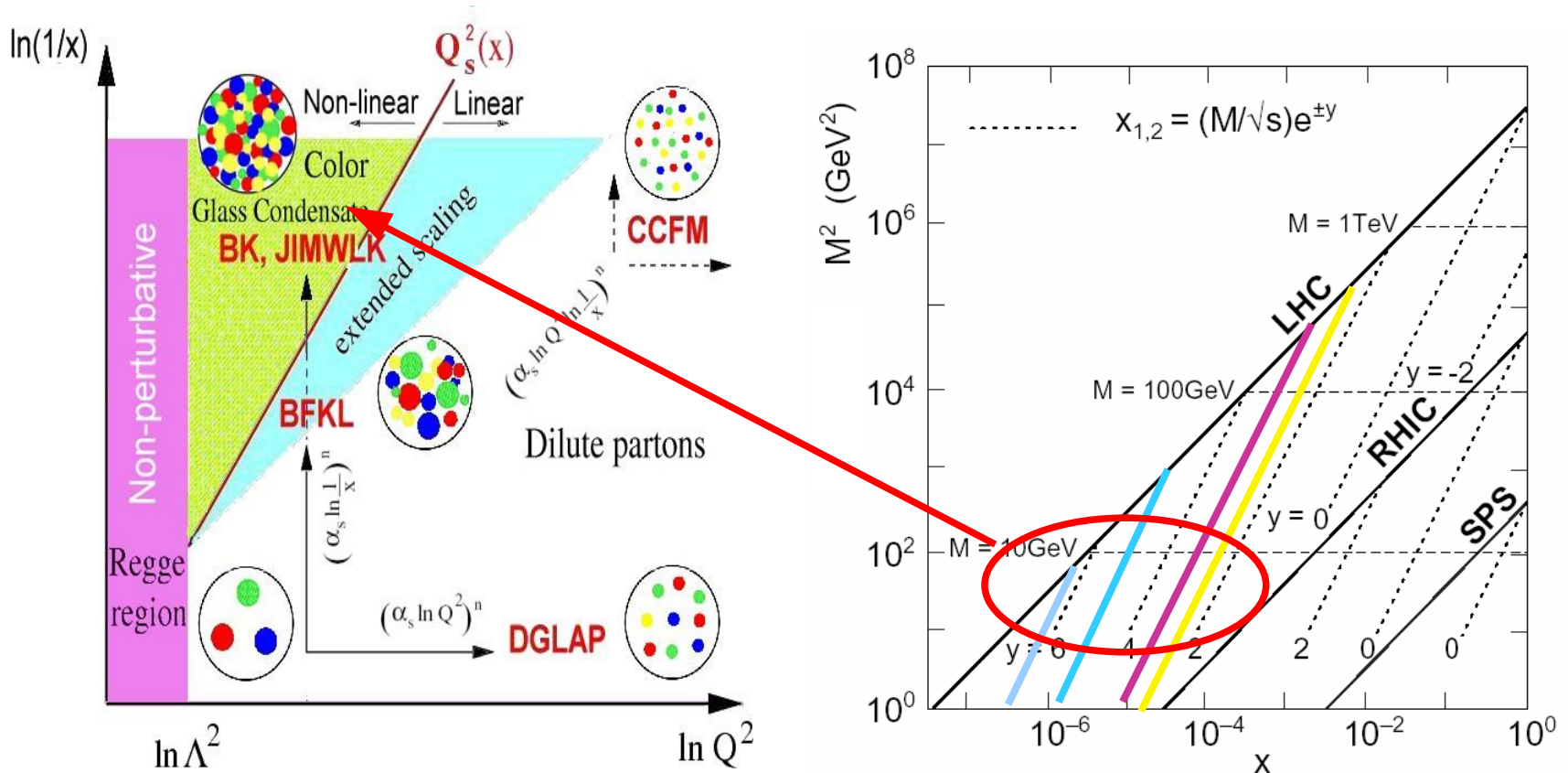
$Q^2 \sim 10^6 \text{ GeV}^2$

$x \sim 10^{-6}$



# Summary

- **Gluon saturation & non-linear evolution** must set-in at (some) low-x in the hadrons → Basic info on **high-energy limit of QCD**
- **Hints** of non-linear QCD dynamics in  $e-p$  (**HERA**) and  $d-A, A-A$  (**RHIC**)
- **LH(e)C = unique lab** to study **high parton density** / evolution in  $p, Pb$  down to  $x \sim 10^{-6}$  using **fwd. detectors** & **perturbative** processes: (di)jets,  $QQbar$ , ...





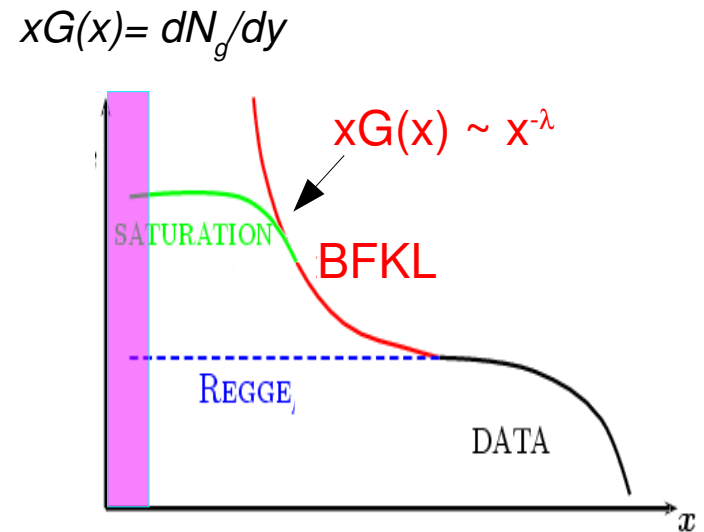
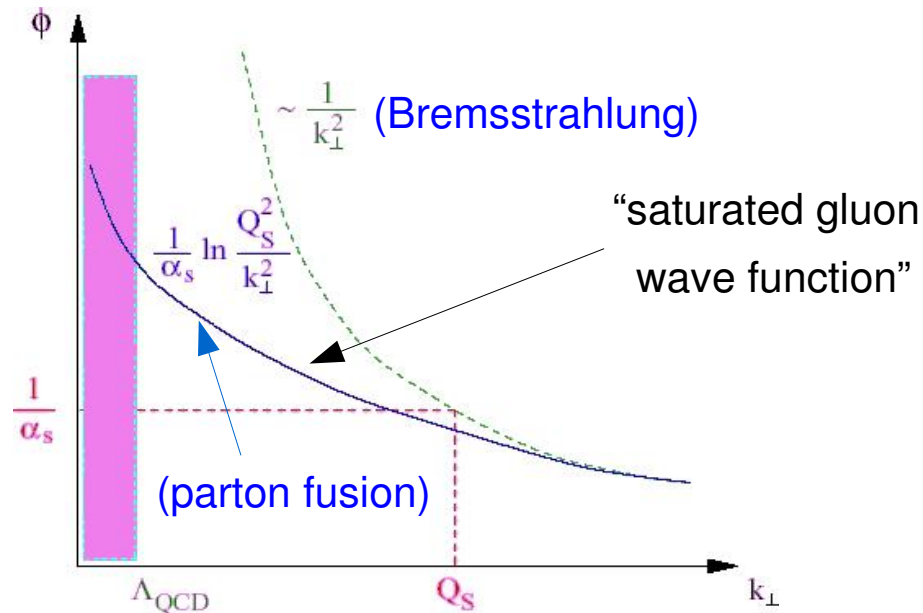
# Backup slides

# Color Glass Condensate (CGC)

[McLerran, Venugopalan, Kharzeev, Levin, Kovchegov, Jalilian-Marian, Mueller, Iancu, Gelis, Tuchin, Iakura, Dumitru, ...]

## ■ CGC = EFT in high-energy (small-x) QCD limit:

- **C**olor (obvious) **G**lass ( $q \sim$  “frozen” sources) **C**ondensate (high gluon occup.)
- Hadrons = **C**lassical fields below/around  $Q_s$ :



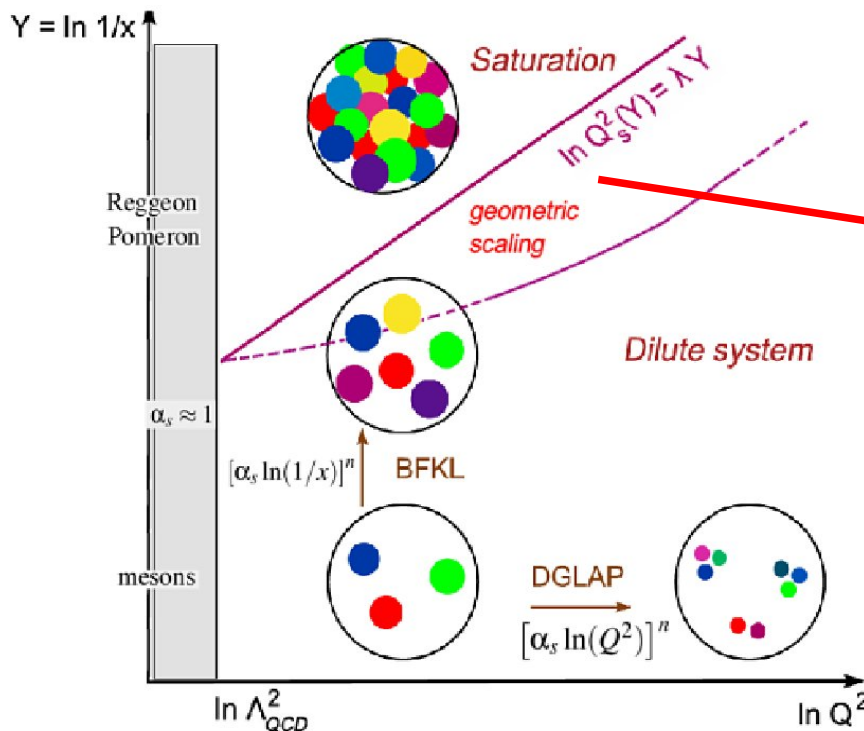
- $Q_s$  hard  $\Rightarrow$  perturbative calculations (strong  $F_{\mu\nu}$ , weak coupling):  $\alpha_s(Q_s^2) \ll 1$
- pA, AA  $\equiv$  collisions of gluon wave function(s) “resum” all multiple scatts.

# Non-linear QCD evolution equations: BK/JIMWLK

- Gluon evolution at low- $x$ : classical stochastic process of splitting & merging governed by **BK-JIMWLK** eqs.

[Balitsky, Kovchegov,  
Jalilian-Marian,  
Iancu, McLerran,  
Kovner, Leonidov,  
Weigert, ...]

- **Non-linear, all-twist** equations in saturation regime
- Generalized Fokker-Planck eq. (wave-function **diffusion**)
- **JIMWLK**  $\rightarrow$  (large  $N_c$  limit)  $\rightarrow$  **BK**  $\rightarrow$  (low-density limit)  $\rightarrow$  **BFKL**



Additional quantum corrections:  
lead to anomalous dimension  
in "extended scaling" region:

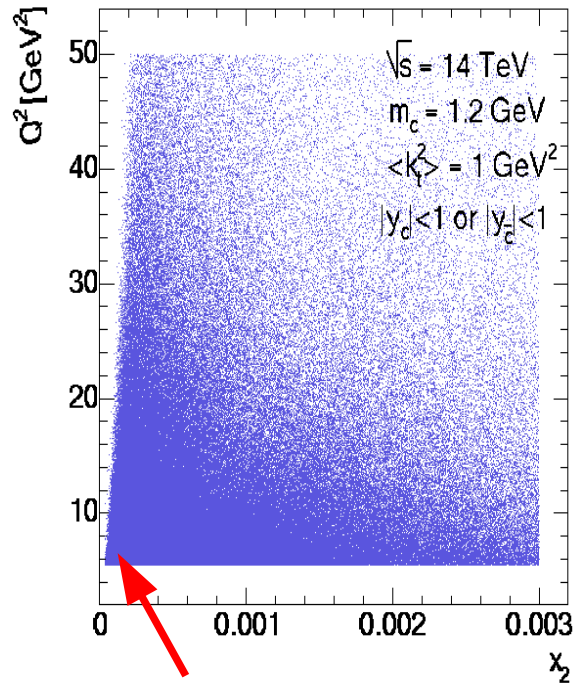
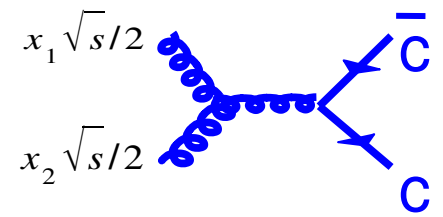
$$\frac{1}{Q^2} \rightarrow \left(\frac{1}{Q^2}\right)^\gamma \quad \gamma \simeq 1/2$$

$$Q_s^2 < Q^2 < Q_s^4/\Lambda^2$$

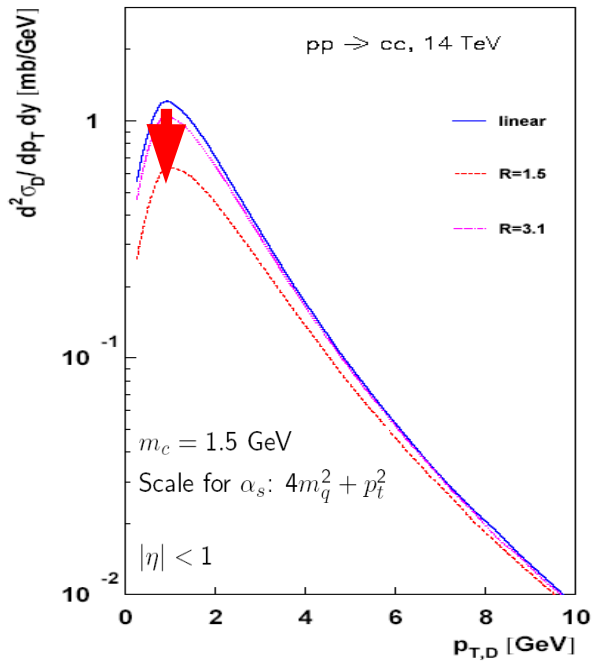
extended window of  
applicability **outside CGC** !

# Case-study IV: Low- $p_T$ charm in ALICE ( $|\eta| < 1$ )

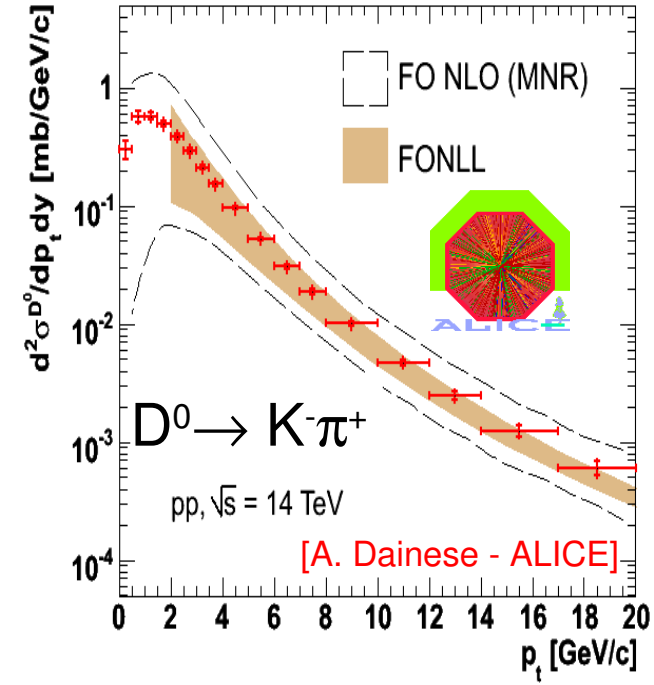
➤ Open charm measurement in TPC+TRD ( $y=0$ ):



$xg(x)$  in the proton  
at  $x_1 \sim x_2 \sim m_c / \sqrt{s} \sim 10^{-4}$



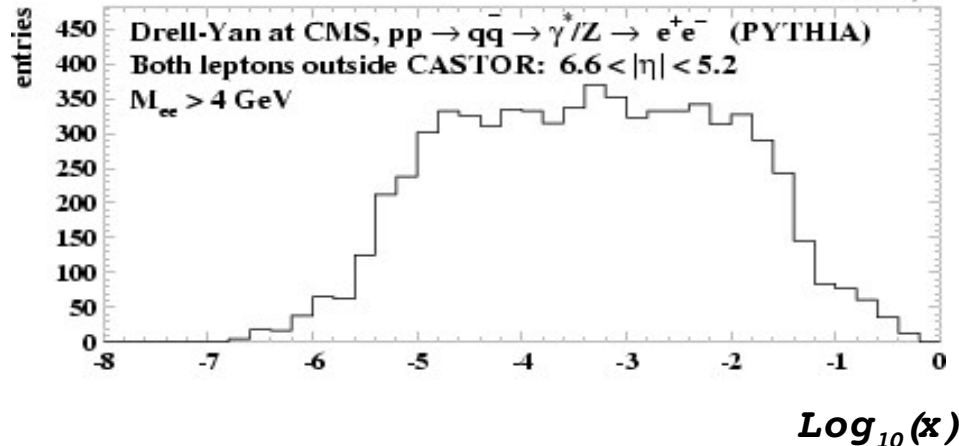
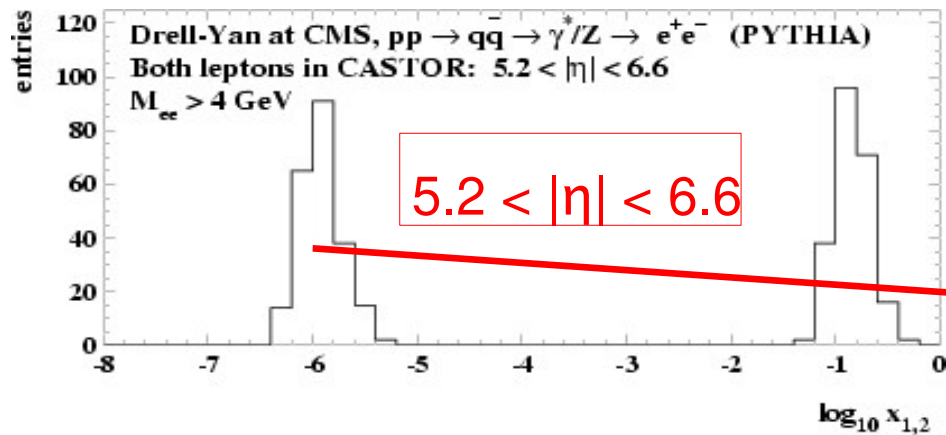
Charm suppression  
due to non-linear QCD  
effects



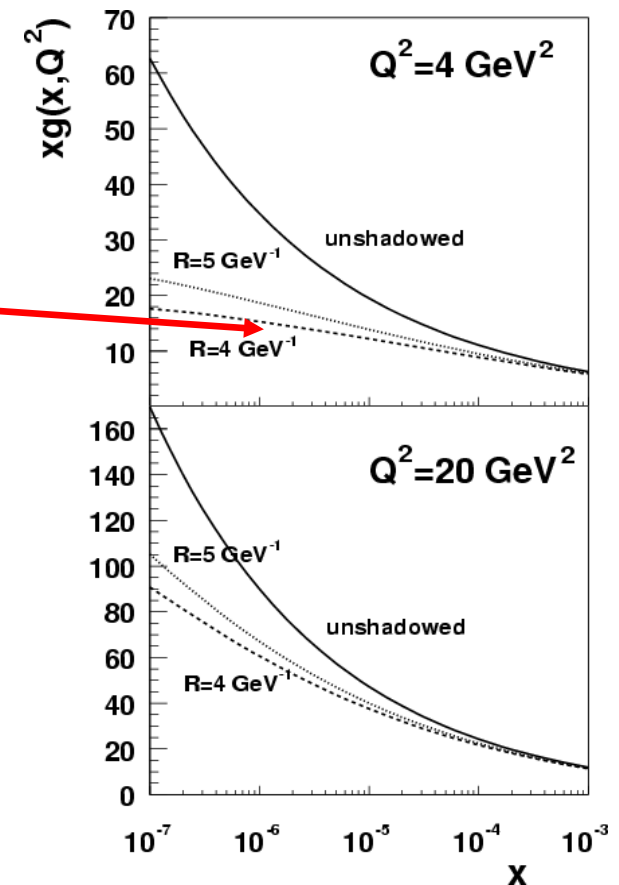
Good reco capabilities  
(displaced vtx. +  $e^\pm$  PID)  
down to  $p_T = 0$  GeV/c

# Case-study VII: DY in CASTOR-T2 ( $5.2 < |\eta| < 6.6$ )

- Drell-Yan **feasibility** studies with CMS (CASTOR) + TOTEM (T2):
- Sensitive to low-x **quark** densities



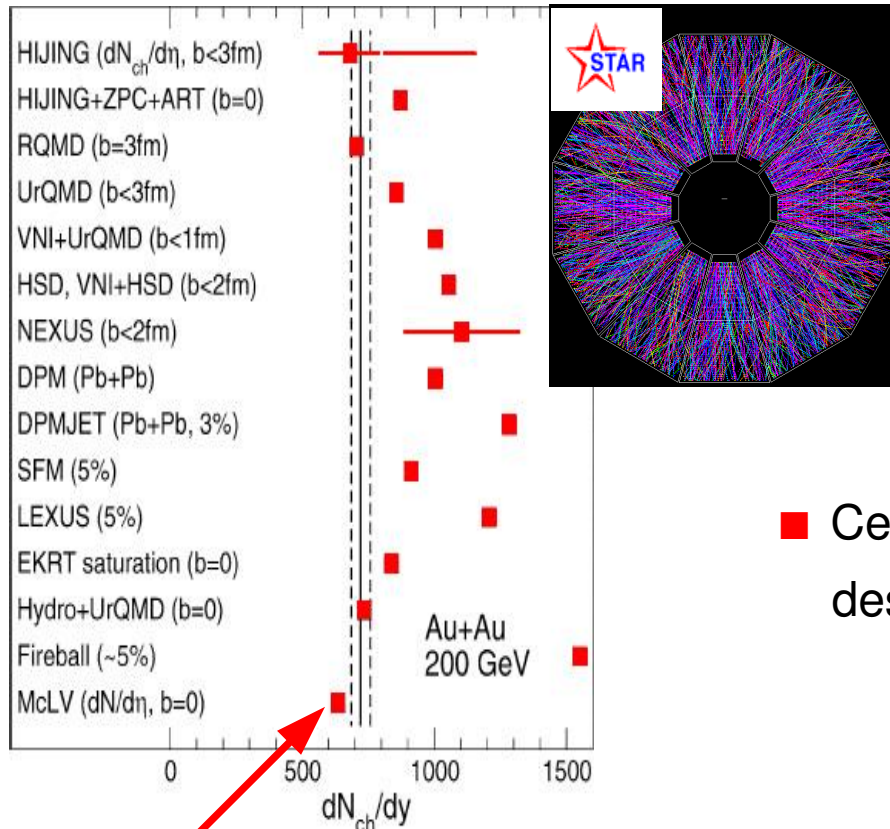
PDF parametrizations



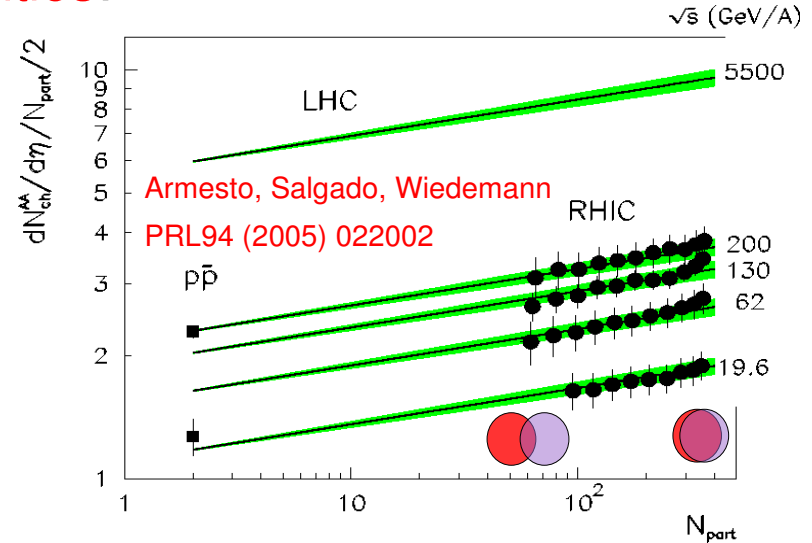
TOTEM T2 tracker+ CASTOR needed to deal w/ **large QCD (& QED) bckgd.**

# Saturation hints at RHIC ? (AuAu @ 200 GeV)

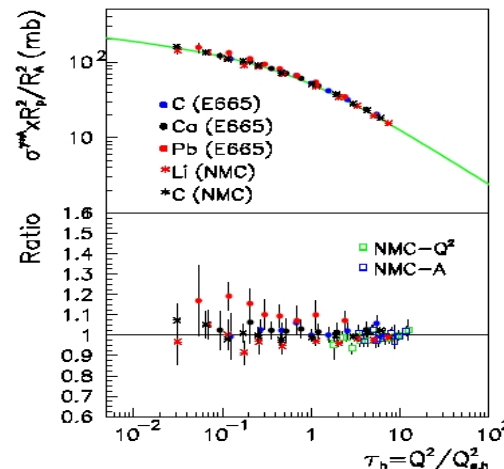
- “Reduced” total AuAu hadron multiplicities:



$dN_{ch}/d\eta \sim 650$  at  $\eta=0$  described by CGC  
 (or models which include reduced incoming parton flux)



- Centrality & sqrt(s) dependence of  $dN/d\eta$  described by geometric-scaling models.

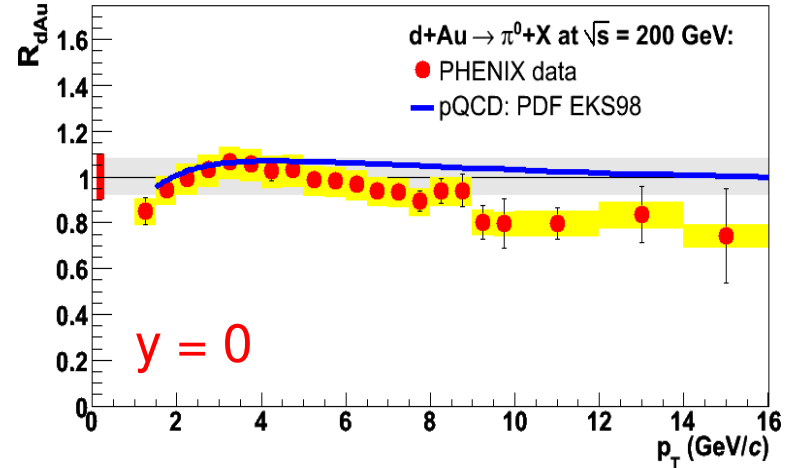
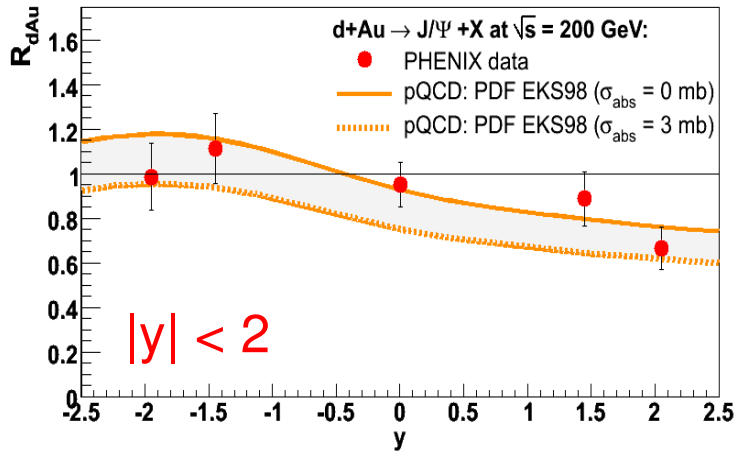


Confirms approx:

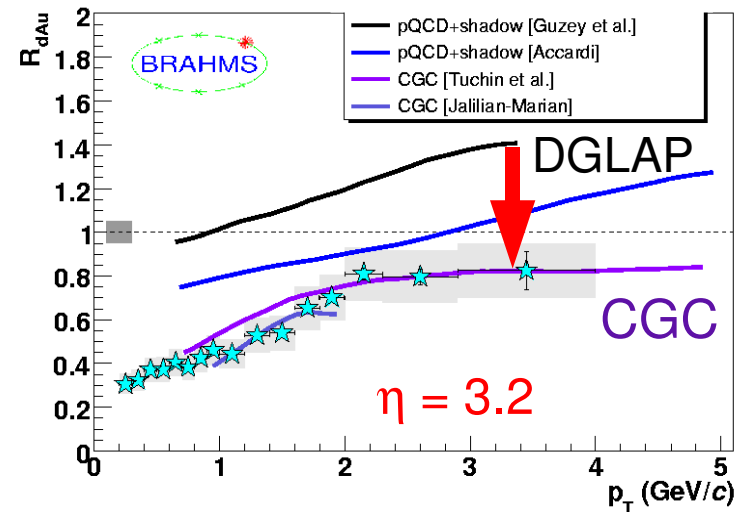
$$Q_s^2 \sim A^{1/3}$$

# Saturation hints at RHIC ? (dAu @ 200 GeV)

- $y \sim 0$  ( $x \sim 10^{-2}$ ): **Hard** hadroprod. described by **NLO pQCD** (+mild LT shadowing):



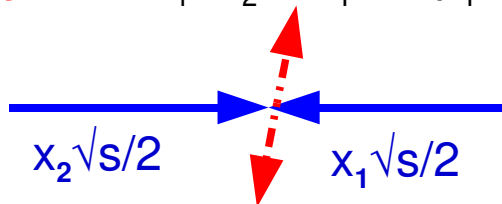
- $\eta = 3.2$  ( $x \sim 10^{-3}$ ): **Suppressed hadron production** ( $p_T \sim 2 - 4$  GeV/c) better described by **CGC** than NLO pQCD: reduced partonic flux in Au at low-x



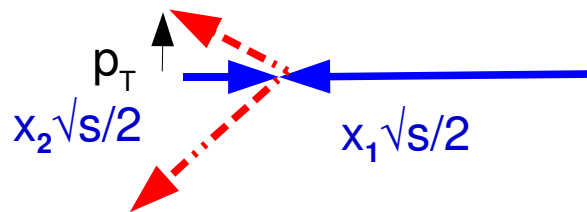
# Small- $x \rightarrow$ Forward rapidities

## ■ $2 \rightarrow 2$ parton kinematics:

$y = 0$ :  $x_1 \sim x_2 \sim x_T = 2p_T/\sqrt{s}$



$$x_{1,2}^{2 \rightarrow 2} = \frac{p_T}{\sqrt{s}} (e^{\pm y} + e^{\pm y'}) \Rightarrow x_2^{\min} = \frac{x_T e^{-\eta}}{2 - x_T e^{\eta}}$$



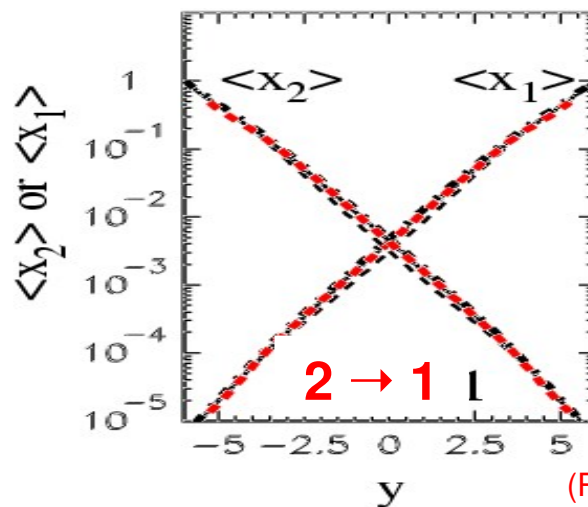
e.g. LHC,  $p_T = 10 \text{ GeV}/c$   
 $x_T \sim 10^{-3}$  ( $\eta \sim 6$ ):  $x_{\min} \sim 10^{-6}$

## ■ $2 \rightarrow 1$ (gluon fusion) CGC kinematics: much lower $x$ reached ( $x_2 = x_2^{\min}$ )

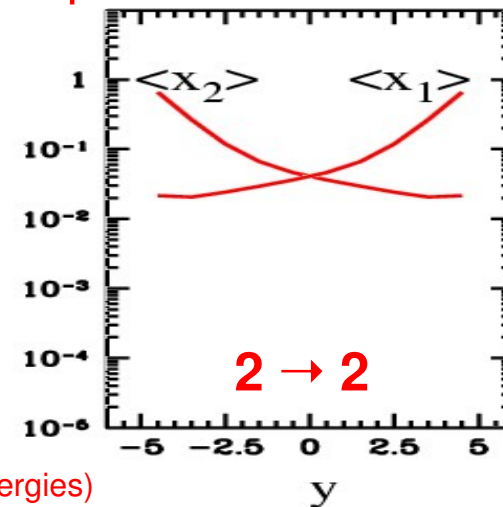
$$x_{1,2}^{2 \rightarrow 1} = \frac{p_T}{\sqrt{s}} (e^{\pm y})$$

Every 2-units of  $y$ ,  
 $x_2$  decreases by  $\sim 10$

CGC:  $x(y=4) \sim 10^{-4}$



pQCD:  $x(y=4) \sim 10^{-2}$



(RHIC energies)

[Accardi,nucl-th/0405046]



# Forward Detectors in CMS & ATLAS

## ➤ CMS + TOTEM:



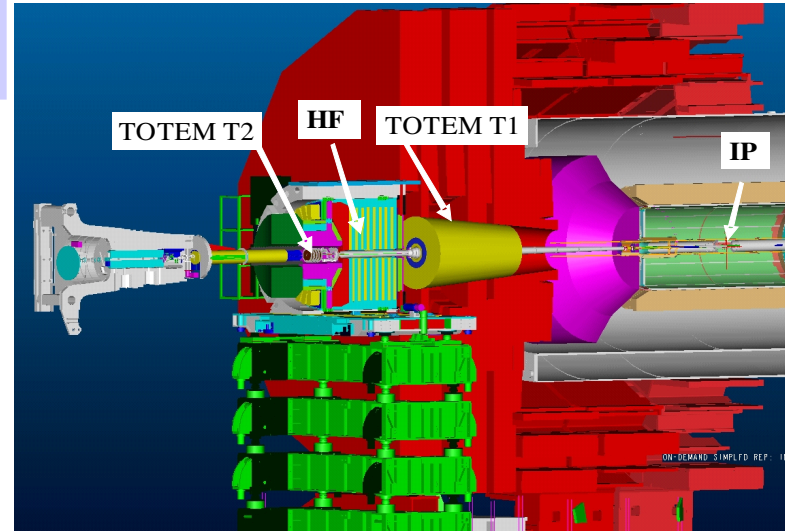
**HF** (Iron-Q-fiber calo):  $3 < \eta < 5$

**TOTEM-T1** (CSC telescope):  $3.1 < \eta < 4.7$

**TOTEM-T2** (GEM telescope):  $5.3 < \eta < 6.7$

**CASTOR** (W/-Q-fiber calo):  $5.3 < \eta < 6.5$

**ZDC** (W/Q-fiber calo):  $\eta > 8.3$  (neutral)



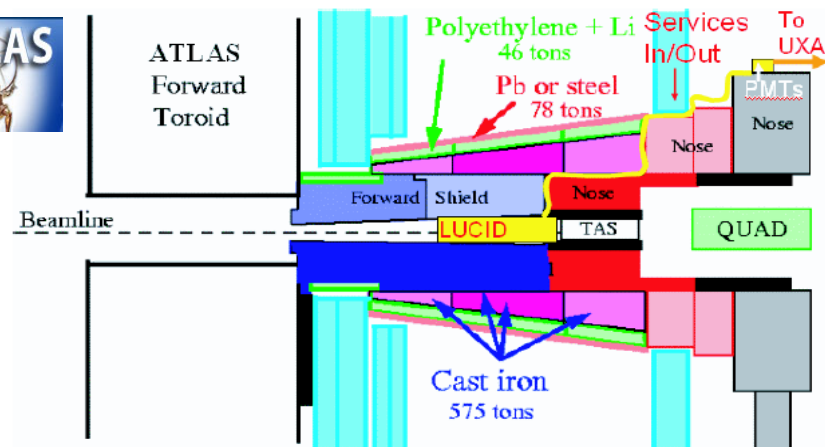
## ➤ ATLAS:



**FCal.**:  $3 < \eta < 5$

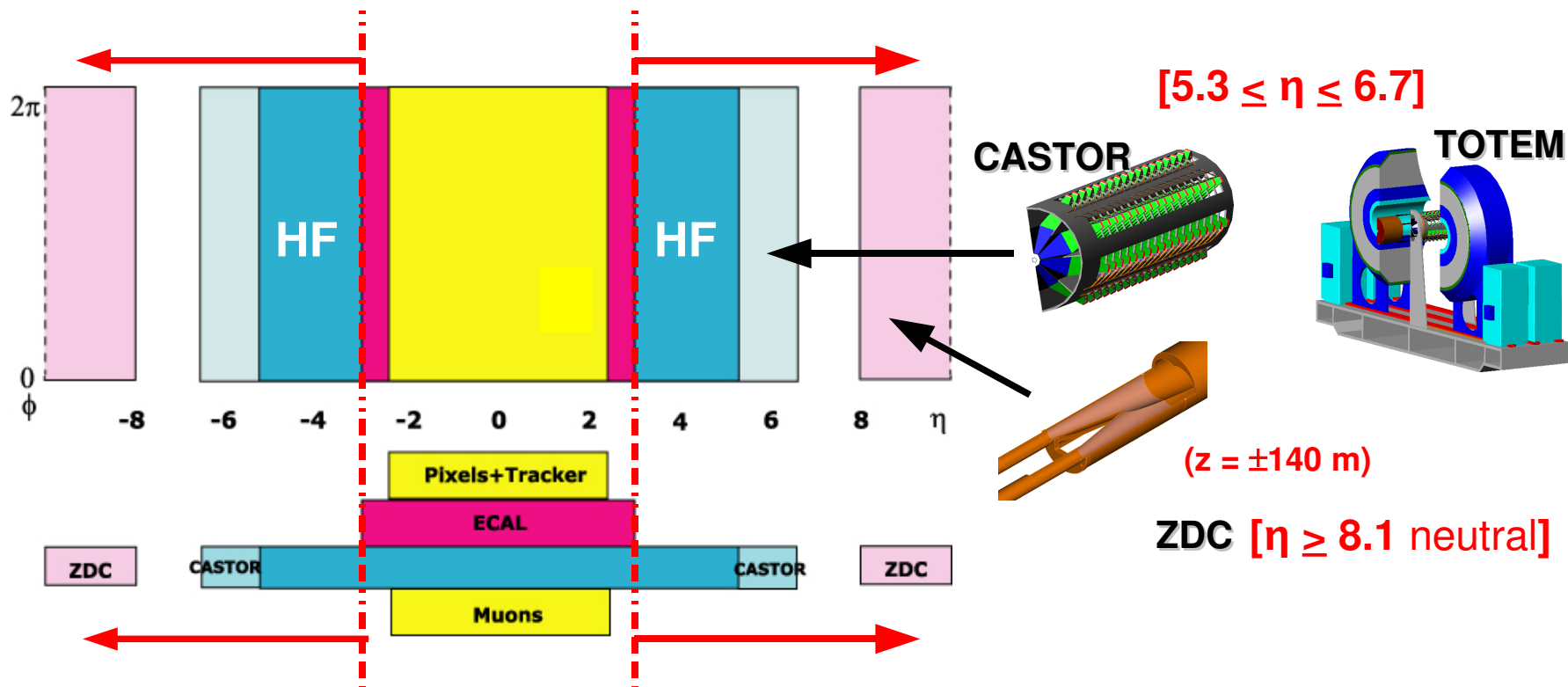
**LUCID** (Cerenkov Counter):  $5.4 < \eta < 6.1$

**ZDC** (W/Q-fiber calo):  $\eta > 8.3$  (neutral)



# CMS/TOTEM at the LHC

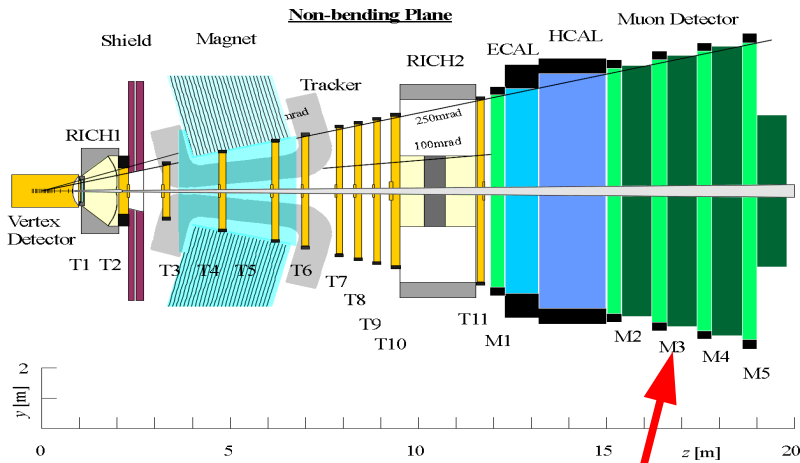
- HF, CASTOR, ZDC + TOTEM: Quasi-full acceptance at LHC:



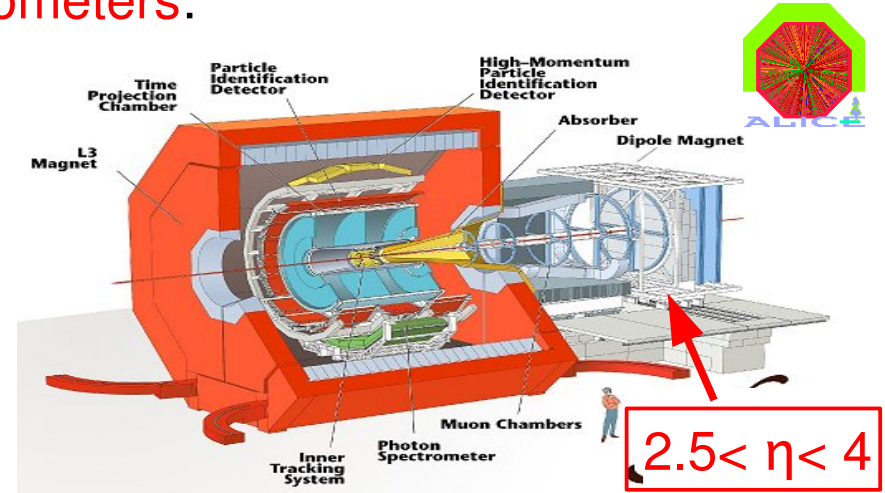
- Detection capabilities within  $\eta \leq 6.7$  (and  $\eta \geq 8.1$ , neutral).
- Hard scattering measurements (jets, high- $p_T$  hadrons, DY) possible down to  $x \sim 10^{-6}$  in pp, pA, AA at LHC.

# Forward Detectors in ALICE & LHCb

➤ ALICE, LHCb forward muon spectrometers:

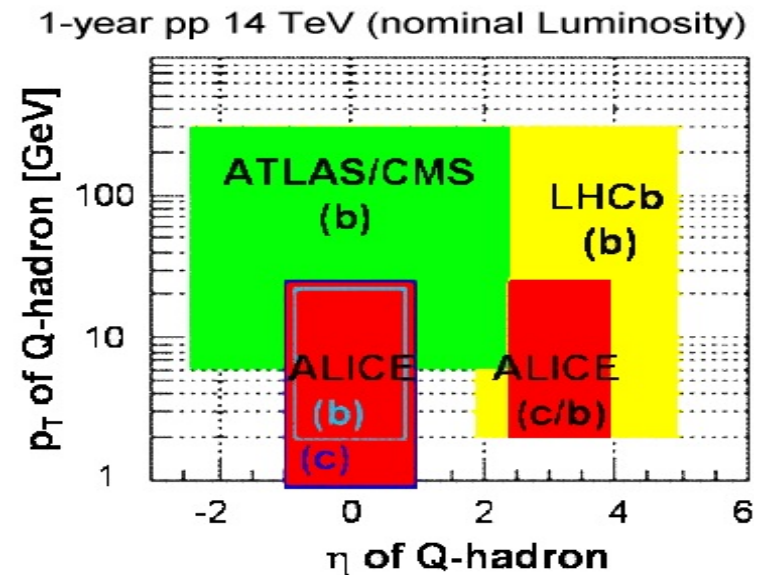


$2 < \eta < 5$



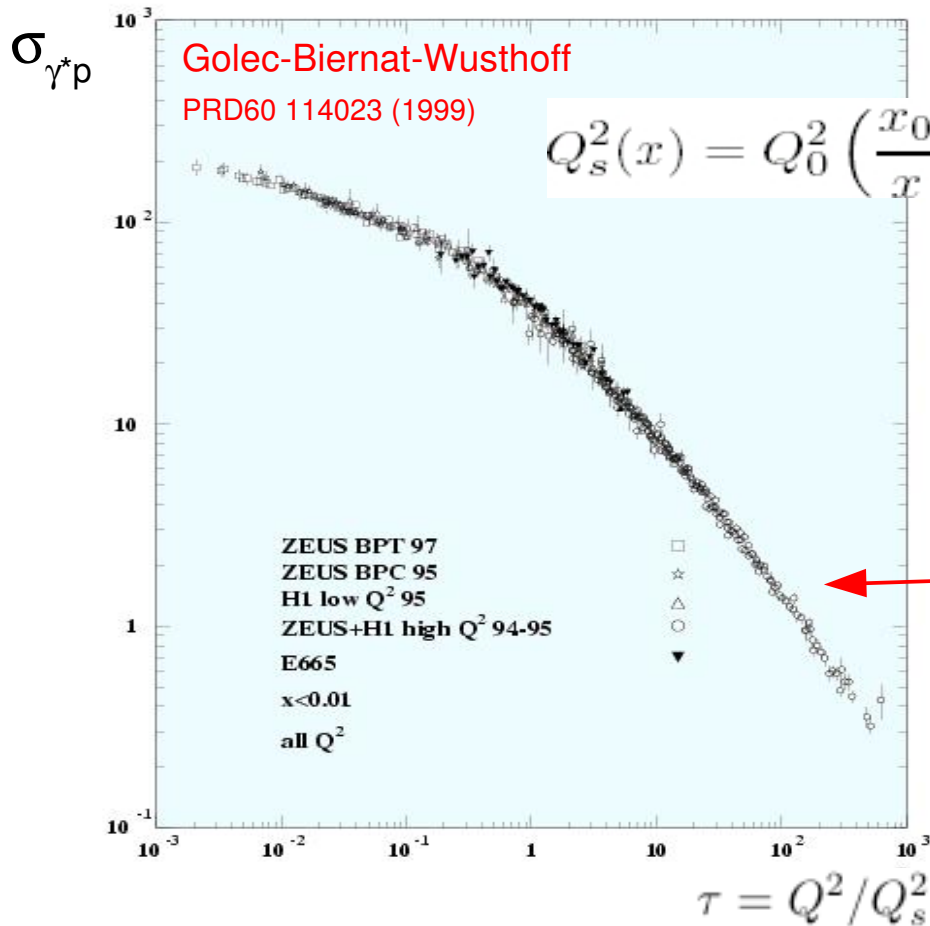
$2.5 < \eta < 4$

➤ Excellent capabilities for heavy-Q, QQbar fwd. measurements at low-x:



# Saturation hints at HERA (I): “Geometric scaling”

- Saturation predicts **low-x** structure **dependence on single scale  $Q_s^2(x)$**
- Inclusive  $\sigma_{\gamma^*p}$  seen to scale with  $Q^2/Q_s^2$  for  **$x < 0.01$** :



$\sigma_{\gamma^*p}$  described by **dipole model**:  
 particular realization of CGC  
 where  $\sigma_{\text{dipole-p}} \sim f(G(x)) \sim f(Q_s)$

Scaling valid up to large  $Q^2$   
 (“**extended scaling**” region):

$$Q_s^2 < Q^2 < Q_s^4/\Lambda^2$$

[Note: DGLAP also shows this property but much more sensitive to  $xG(Q^2)$  fit chosen]

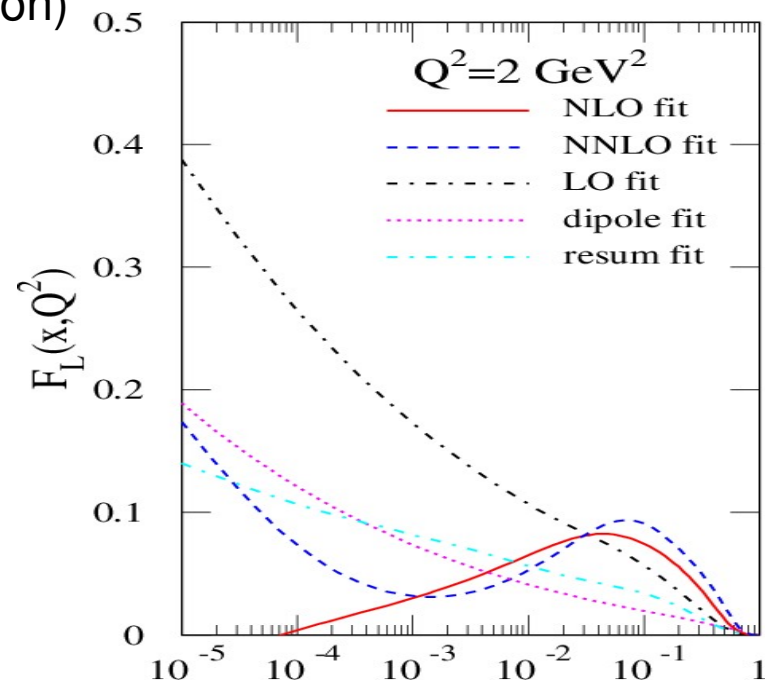
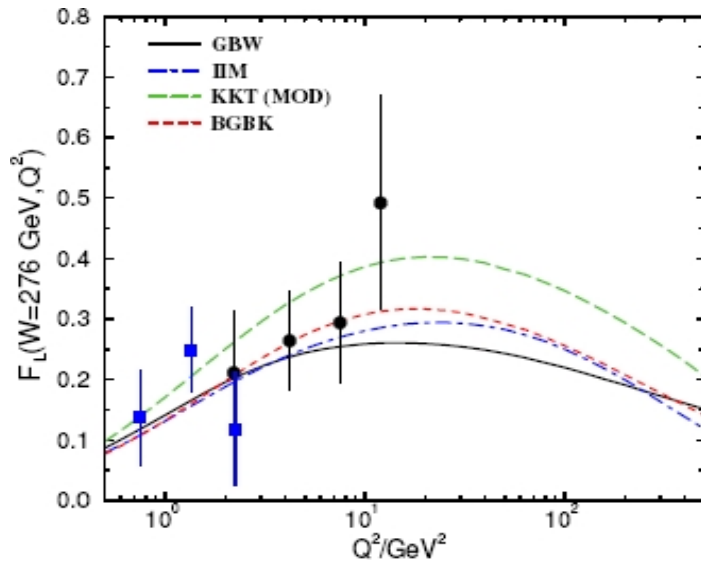
# Saturation hints at HERA (II): $F_L$ at low- $x$

- $F_L$  directly depends on gluon PDF:  $F_L \propto \alpha_s xg$

but  $F_L$  is a small correction to  $\sigma_{\gamma p}$ :  $\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} [Y_+ \cdot F_2 \mp Y_- \cdot xF_3 - y^2 \cdot F_L]$

- $F_L$  derived from NLO DGLAP analysis, is negative for  $Q^2 \sim 2 \text{ GeV}^2$  !?

(indicates “tension” with std. DGLAP evolution)



- Direct measurement of  $F_L$  carried out at HERA in Jun'07: e-p at lower  $\sqrt{s}$

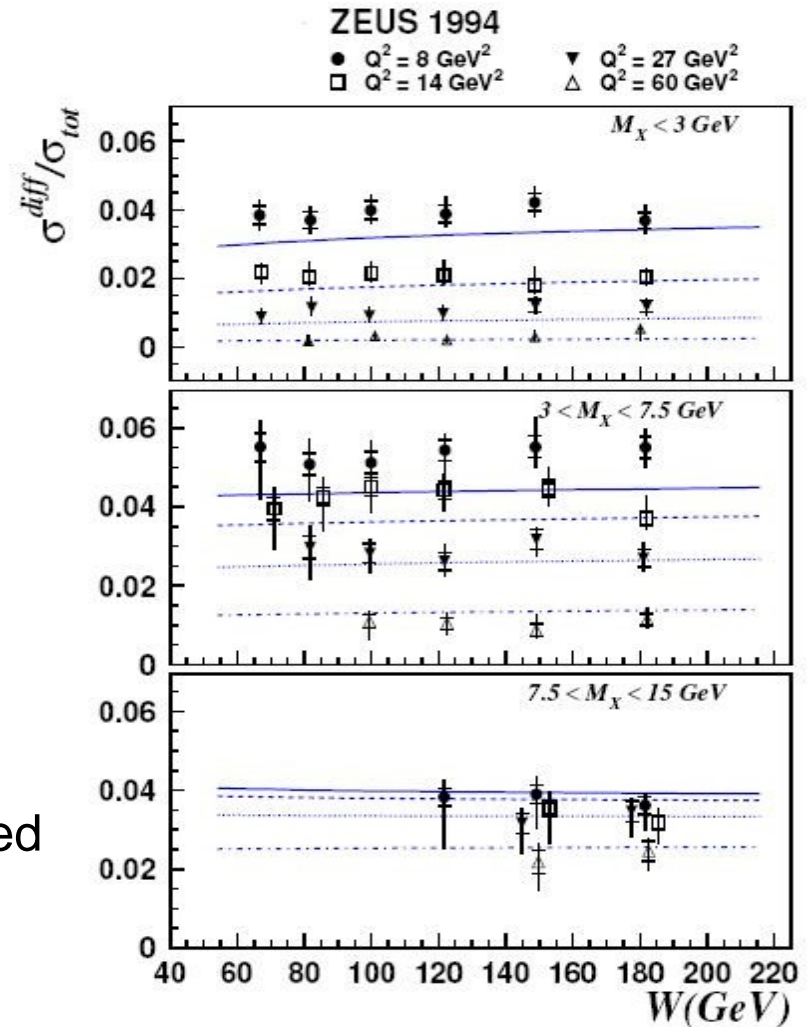
# Saturation hints at HERA (III): $\sigma_{\text{diffract}}/\sigma_{\text{tot}}$ ratio

- **Hard diffraction x-sections** & total x-sections observed to have similar energy dependence.

- **Flat  $\sigma_{\text{diffract}}/\sigma_{\text{tot}}$  vs energy** is at variance with expected rise behaviour in standard **pQCD**:

$$\sigma_{\text{diff}}/\sigma_{\text{tot}} \propto |xg(x, Q^2)|^2/xg(x, Q^2) \\ \sim W^{4\lambda}/W^{2\lambda} \sim W^{2\lambda}$$

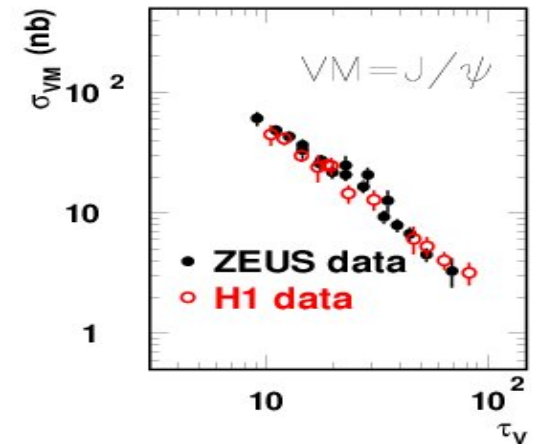
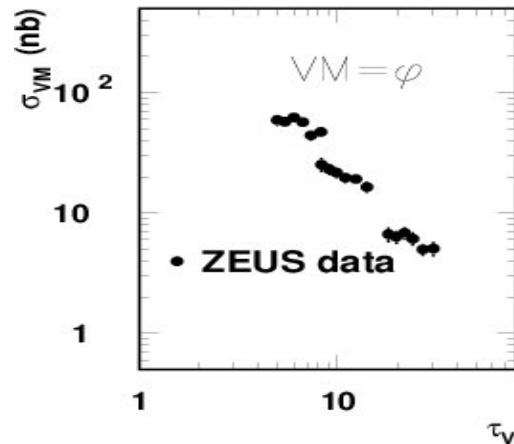
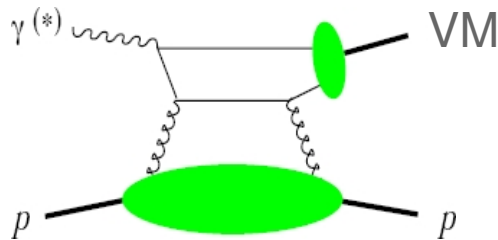
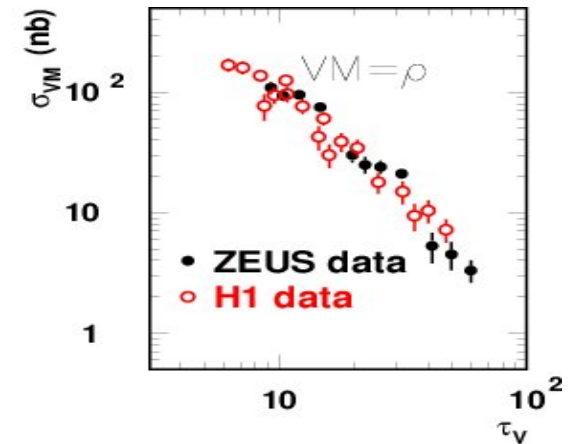
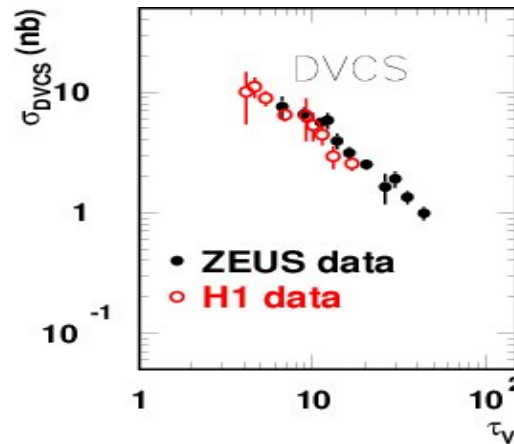
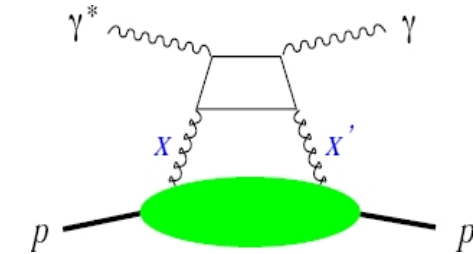
... constant dependence naturally described by saturation models.



# HERA (diffract. DIS): “Geometric scaling” of $\sigma_{VM}$ , $\sigma_{DVCS}$

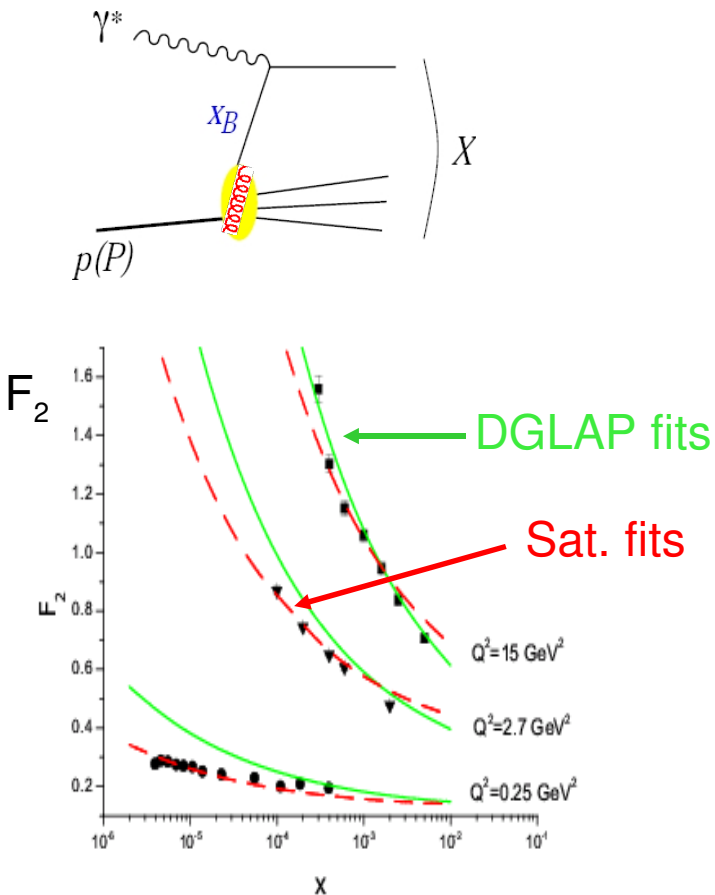
- Geometric scaling also observed in diffractive observables (DVCS, exclusive vector-meson production):

C.Marquet, L. Schoeffel  
hep-ph/0606079

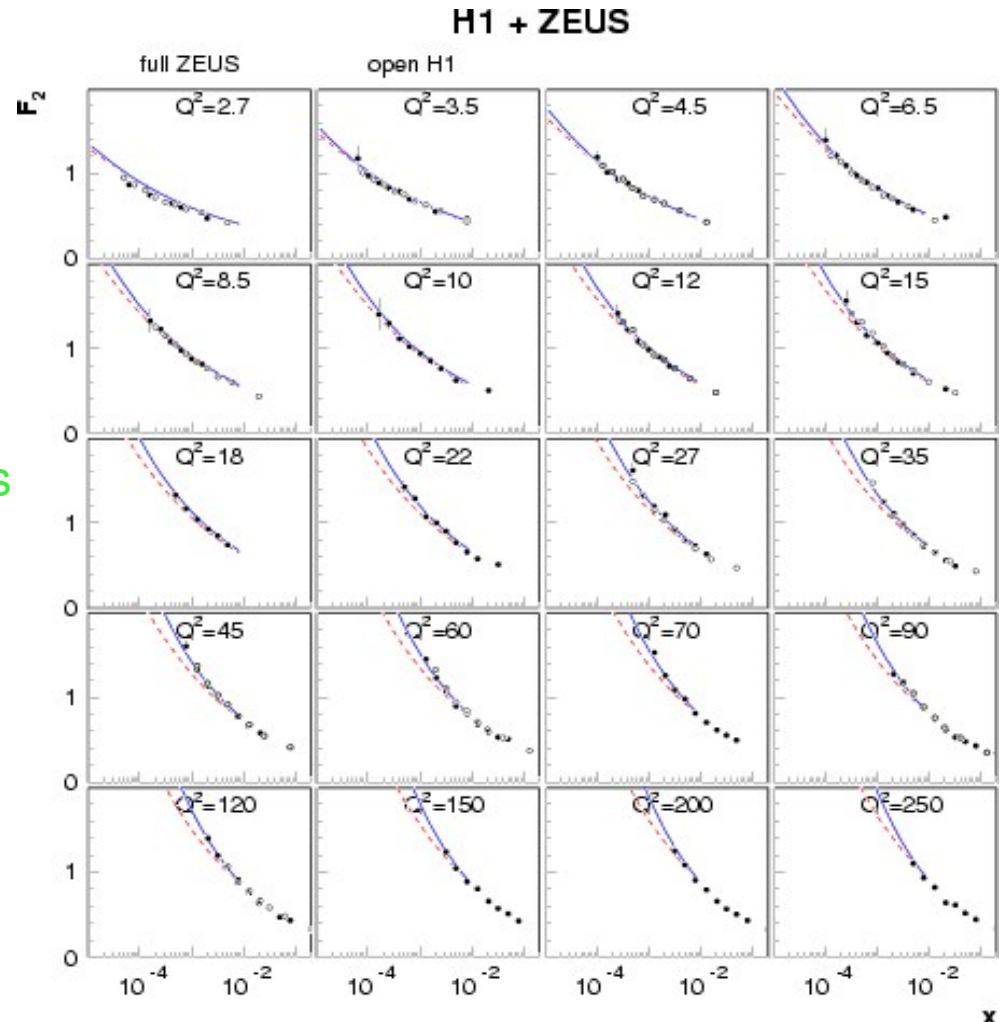


# HERA data vs. saturation models: $F_2(x, Q^2)$

- Saturation models describe well  $F_2(x, Q^2)$  in “transition region” of moderate/low  $Q^2$  (Note: also DGLAP, though at limit of applicability)



[Forshaw, Shaw, hep-ph/0411337]



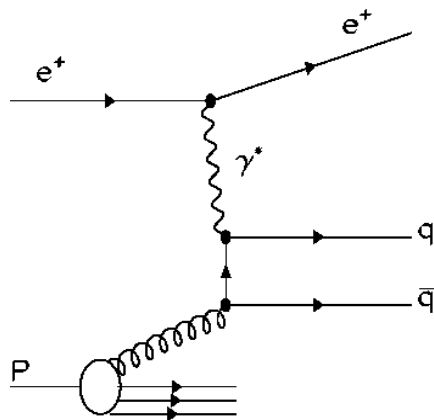
x



# HERA data vs. saturation models: $F_2^{\text{charm}}(x, Q^2)$

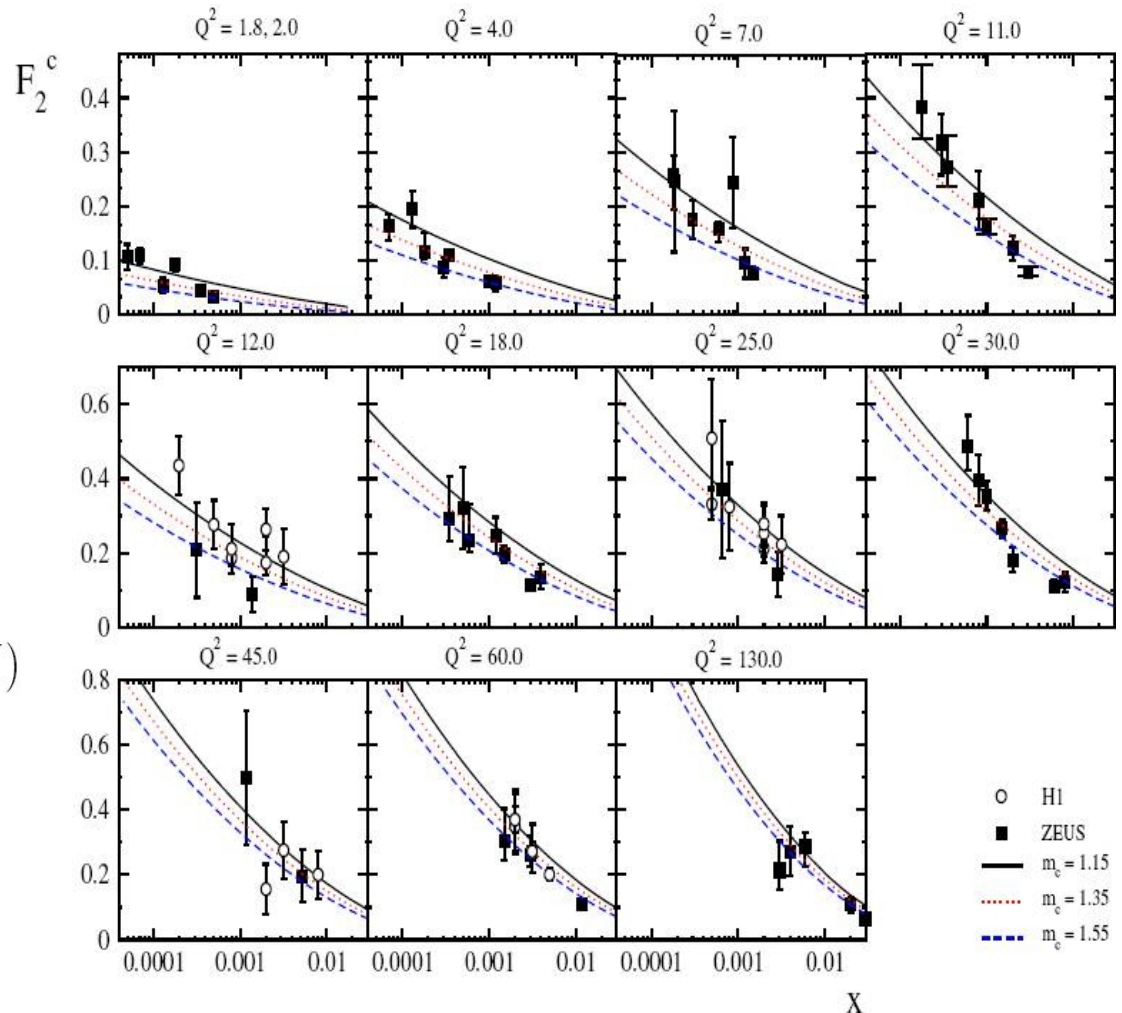
- Saturation models describe well  $F_2$  for charm:

(Note: also DGLAP models)



$$F_2^{c\bar{c}}(x, Q^2) = \frac{Q^2}{4\pi\alpha} \sigma_{\text{tot}}(\gamma p \rightarrow c\bar{c}X)$$

[Machado-Goncalves, EPJC 30 (2003)]

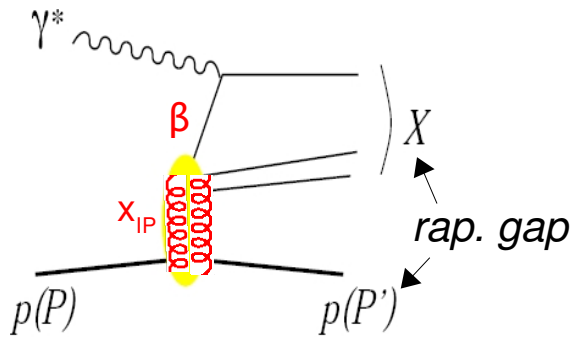


○ H1  
 ■ ZEUS  
 —  $m_c = 1.15$   
 .....  $m_c = 1.35$   
 - - -  $m_c = 1.55$

X

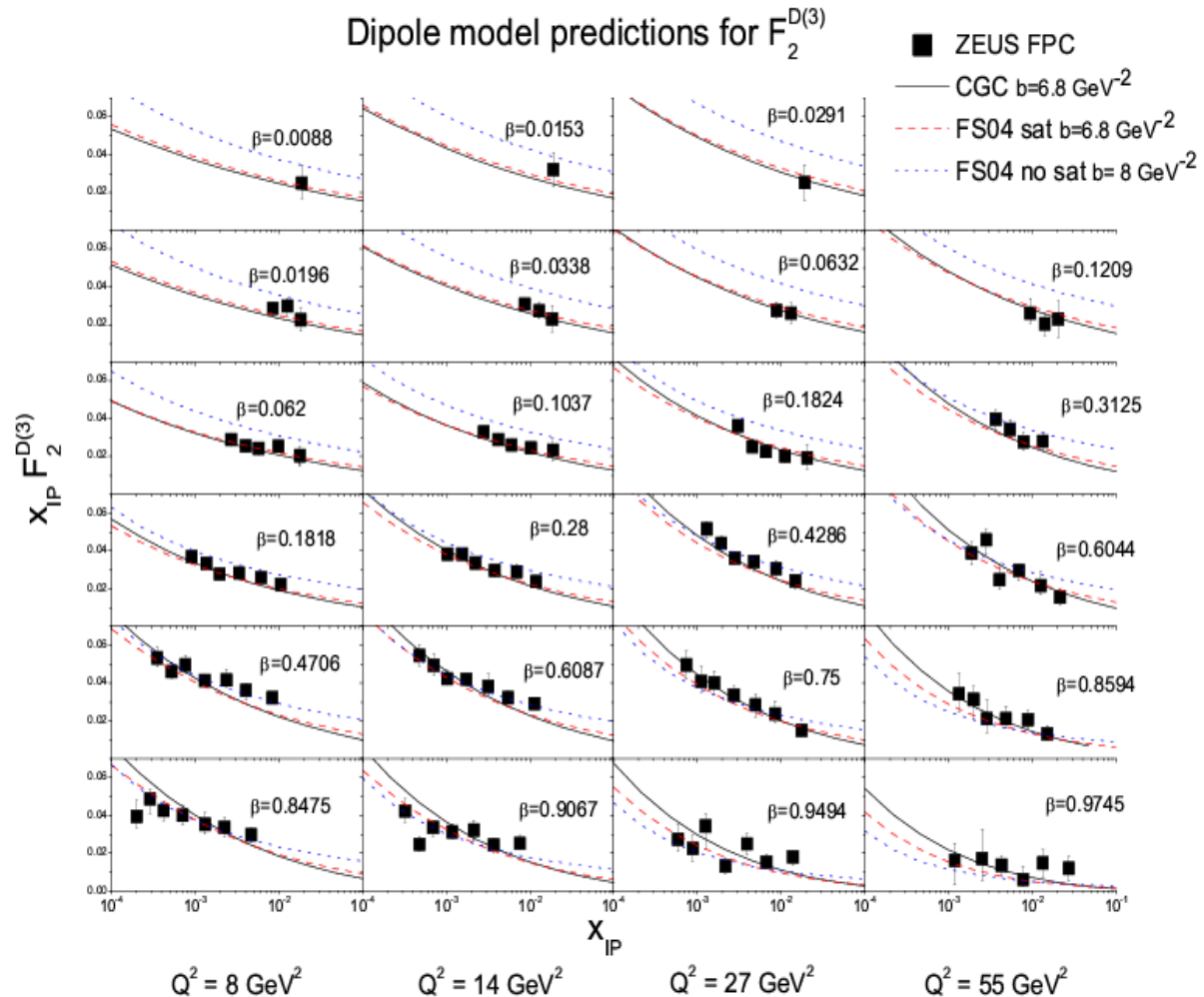
# HERA (diffractive DIS): $F_2^D(x,\beta)$ described

- Saturation models provides framework to describe consistently total  $\gamma^*p$  x-section ( $F_2$ ) and **DDIS** ( $x_{IP}F_2^{D(3)}$ , Pomeron) & **DVCS** forward amplitudes:



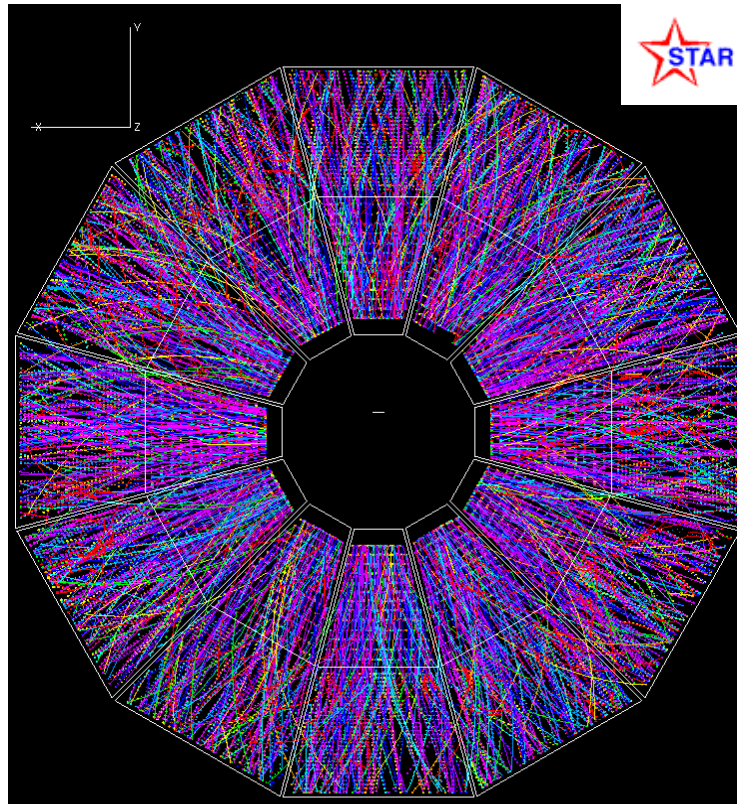
$x_{IP}$  = fraction of p momentum carried by Pomeron  
 $\beta$  = fraction of IP momentum carried by struck parton

Forshaw, Shaw  
 hep-ph/0411337

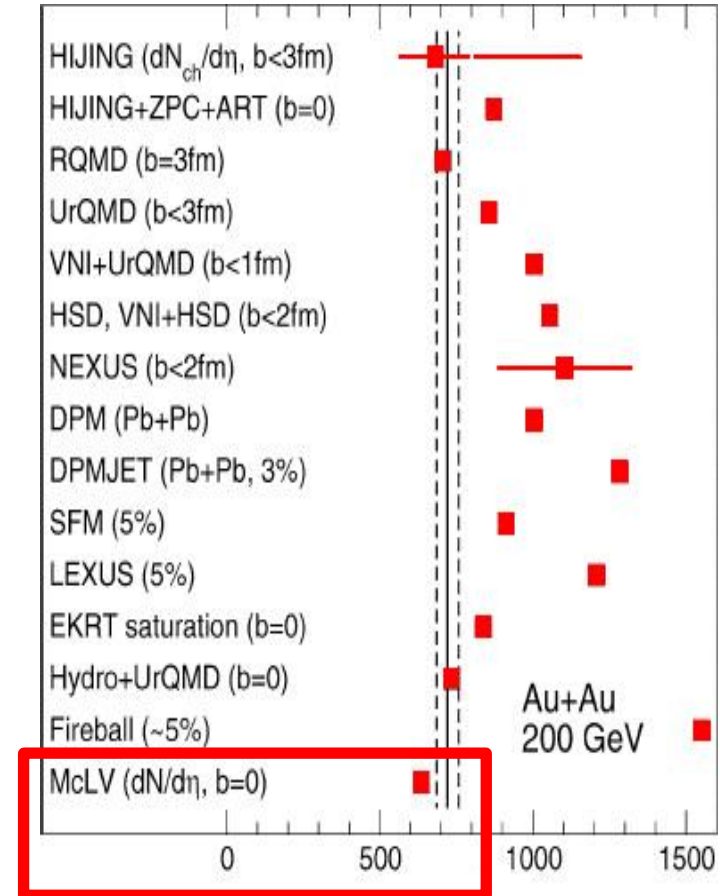


# Saturation hints at RHIC (I): hadron multiplicity

- AuAu (200 GeV) 0-5% most central colls.: Predicted multiplicites:



$dN_{ch}/d\eta \sim 650$  charged particles at  $y=0$



$dN_{ch}/d\eta$

- **Reduced multiplicity** predicted by saturation models: **gluon recombination** reduces incoming parton flux.

# Saturation hints at RHIC (II): $dN_{ch}/d\eta$ vs. centrality

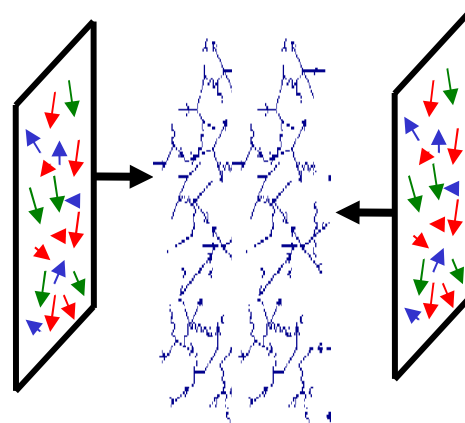
- **CGC**: Final hadron multiplicity  $\propto$  Initial number of released gluons  $\propto Q_s^2$

$$\frac{dN}{d^2bd\eta} \propto \frac{1}{\alpha_s(Q_s^2)} Q_s^2 \propto xG(x, Q_s^2) \cdot A^{1/3}$$

+ “local **parton-hadron duality**” (1 gluon = 1 final hadron)

- **Centrality &  $\sqrt{s}$  dependence well described:**

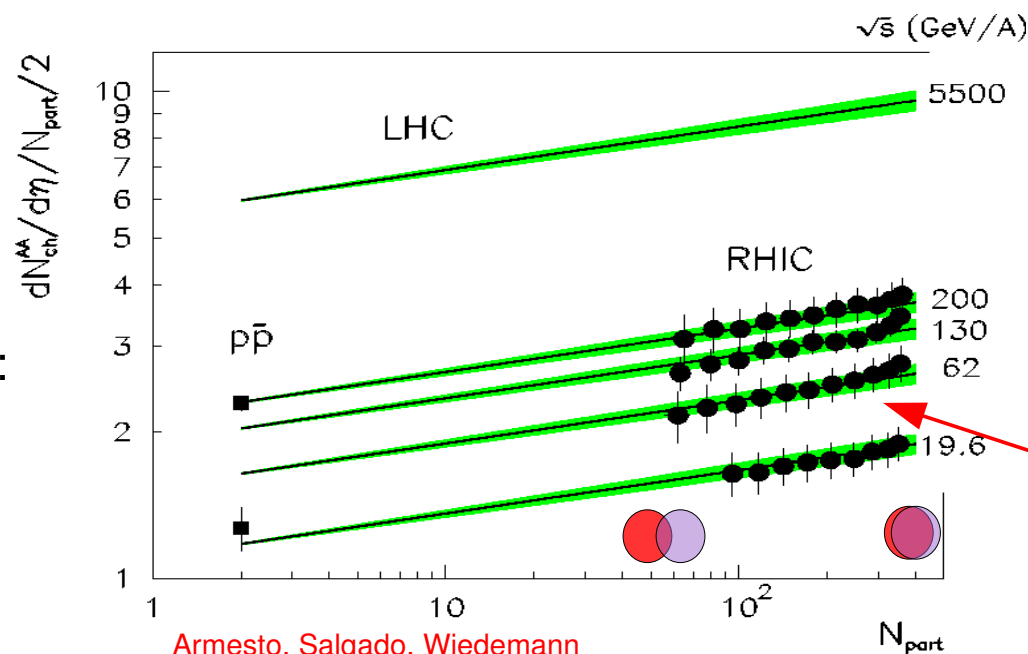
Collision of 2 classical (saturated) fields



$Q_s$  dependence on transv. area

$$\sim \frac{1}{\alpha_s(Q_s^2)}$$

Kharzeev-Levin-Nardi, PLB507 (2001) 121

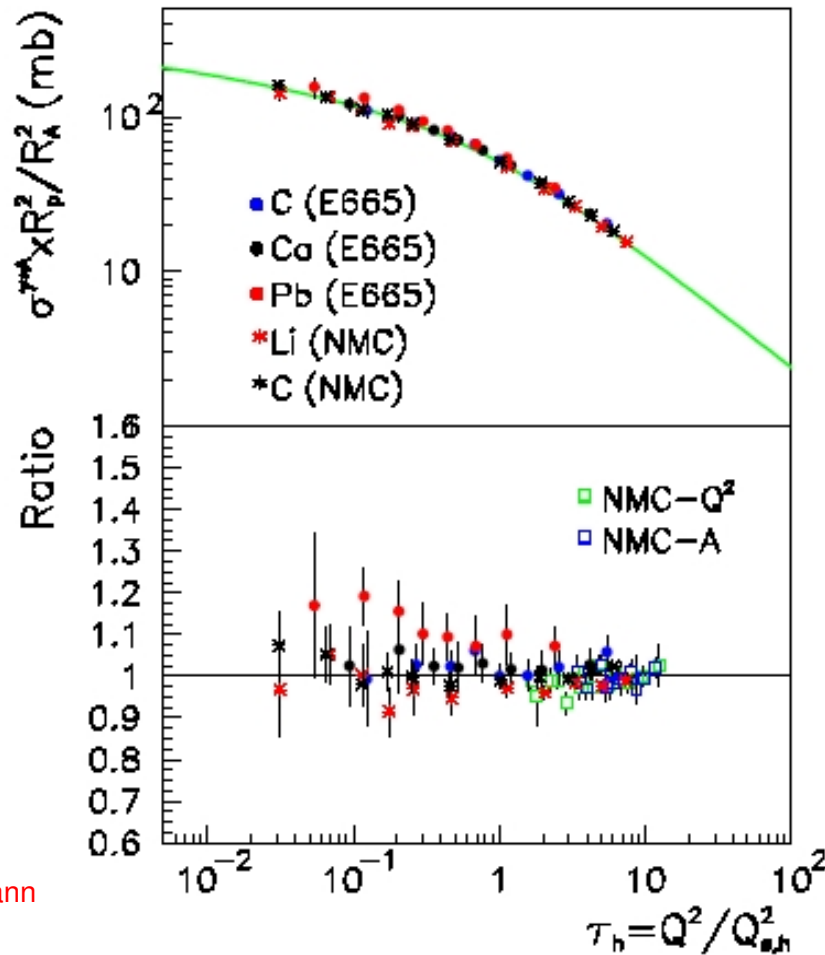


Armesto, Salgado, Wiedemann

PRL94 (2005) 022002

# nuclear DIS: “Geometric scaling” at low-x

- Geometric scaling also in nuclear DIS  $\sigma_{\gamma A}$  data (E665, NMC) for  $x < 0.01$



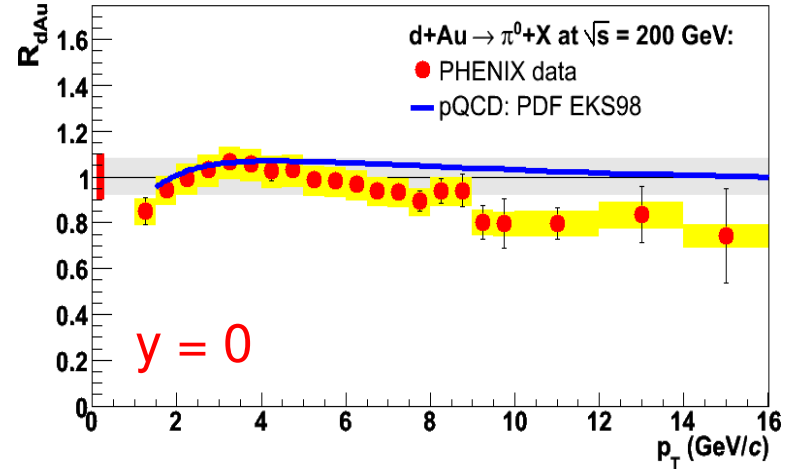
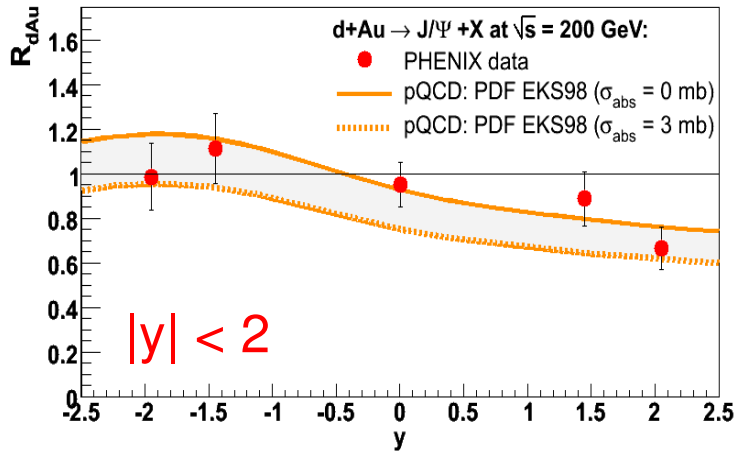
Confirms approx:

$$Q_s^2 \sim A^{1/3}$$

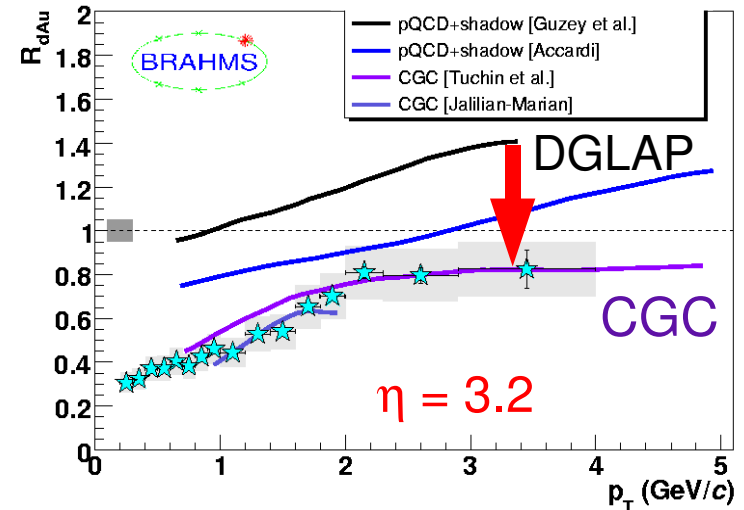
Armesto, Salgado, Wiedemann  
 PRL94 (2005) 022002

# Saturation hints at RHIC (III): fwd. hadron suppression

■  $y \sim 0$  ( $x \sim 10^{-2}$ ): **Hard** hadroprod. described by **NLO pQCD** (+mild LT shadowing):



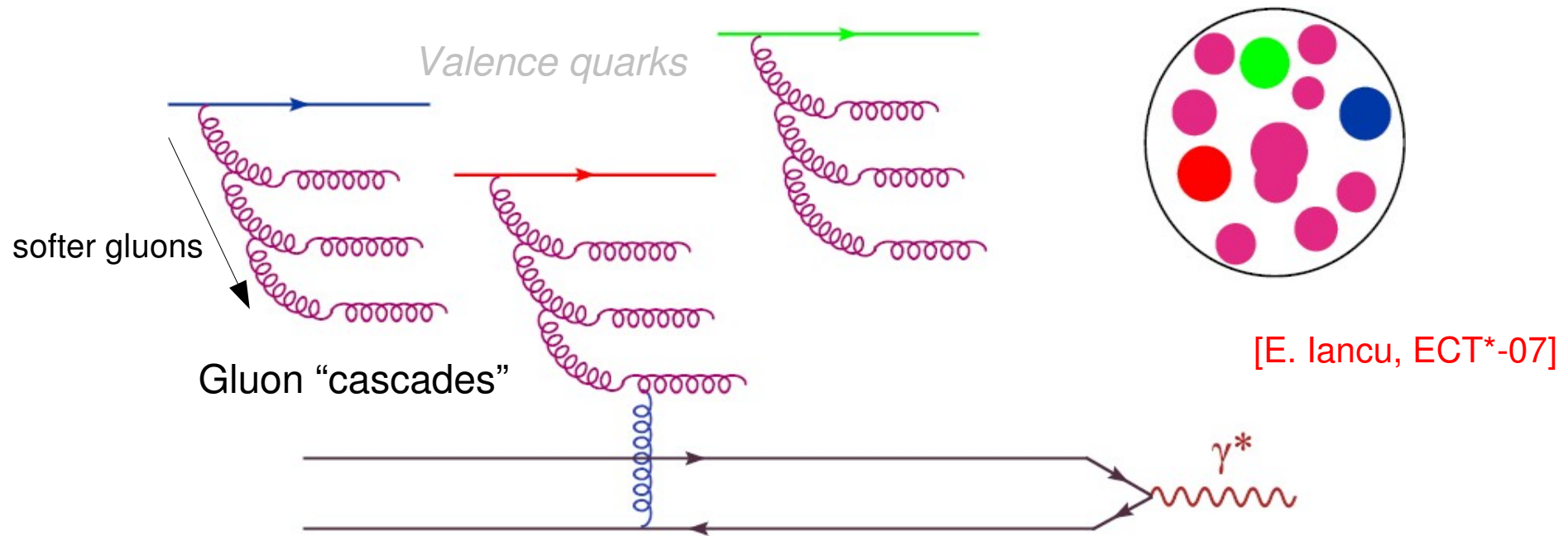
■  $\eta = 3.2$  ( $x \sim 10^{-3}$ ): **Suppressed hadron production** ( $p_T \sim 2 - 4$  GeV/c) better described by **CGC** than NLO pQCD: reduced partonic flux in Au at low-x



# BFKL linear evolution equations

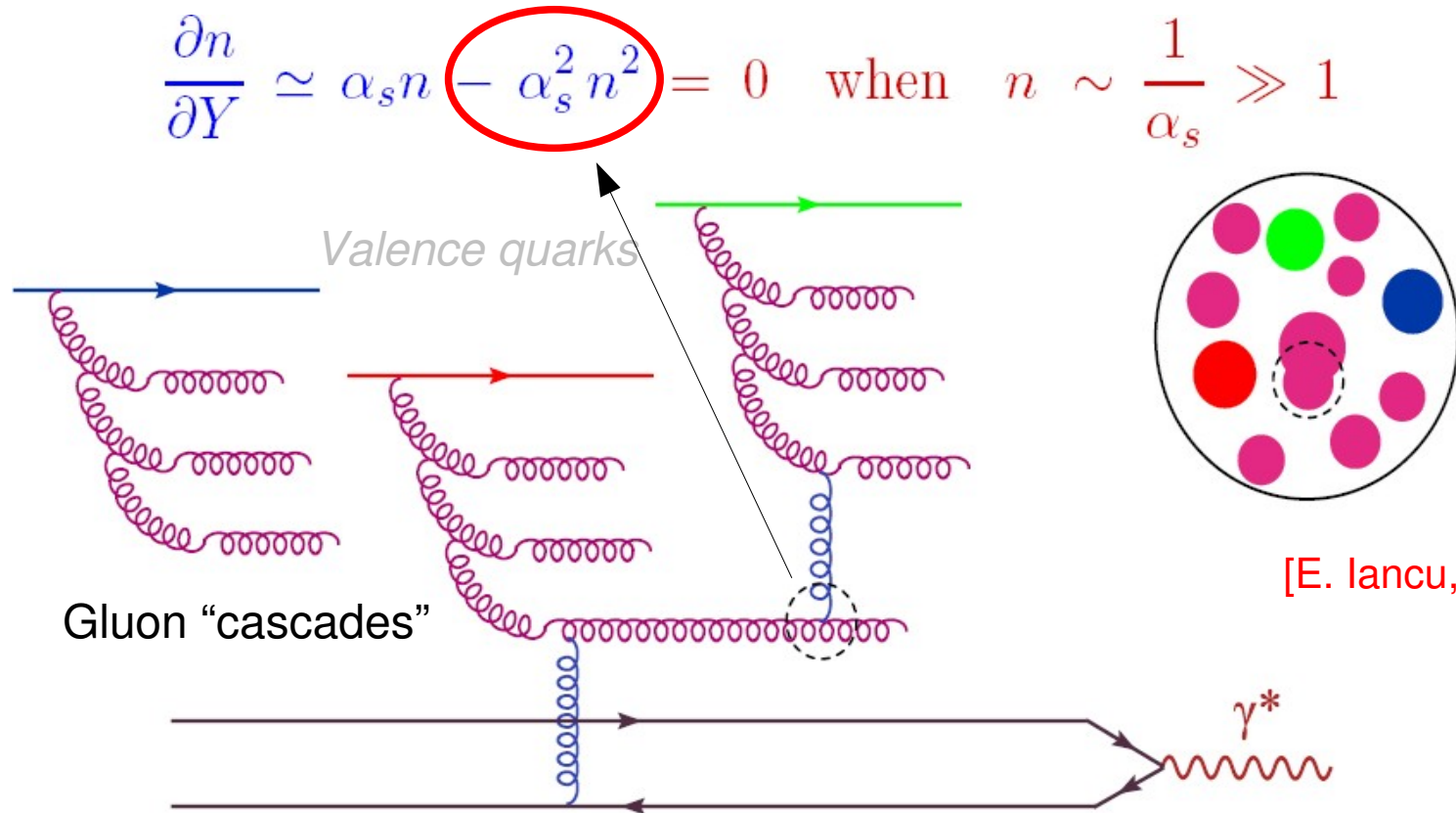
- **Malthusian growth** of gluon density ( $n$ ) w/ increasing- $Y$  (decreasing- $x$ ):

$$\frac{\partial n}{\partial Y} \simeq \alpha_s n \quad \Rightarrow \quad n(Y) \propto e^{\omega \alpha_s Y}, \quad Y = \ln(1/x)$$



# Non-linear QCD evolution equations

- Growth of gluon density ( $n$ ) compensated by **gluon fusion** ( $-n^2$ ):

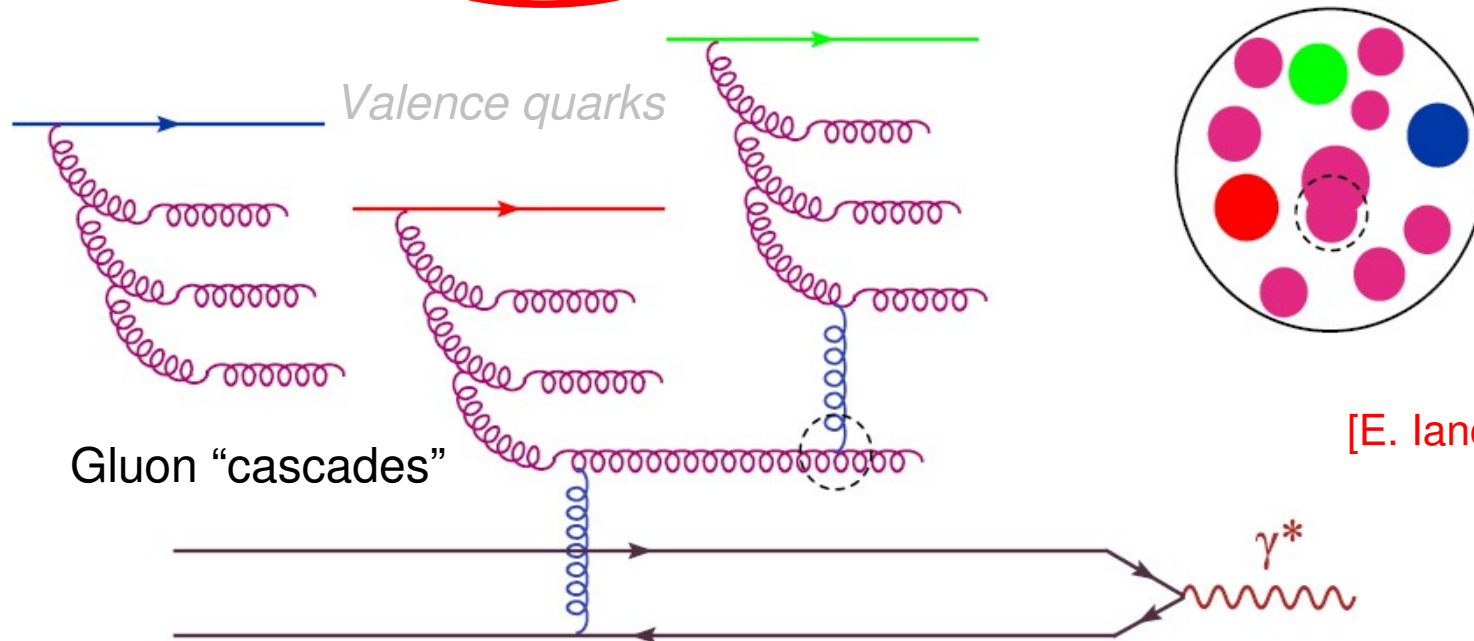




# BK-JIMWLK non-linear QCD equations

- Full evolution (non-locality) requires additional **diffusion term**: saturation “spills out” into the dilute regime **above  $Q_s$**  (“geometric scaling”)

$$\partial_Y n(\rho, Y) = \alpha_s \partial_\rho^2 n(\rho, Y) + \alpha_s n(\rho, Y) - \alpha_s^2 n^2(\rho, Y)$$

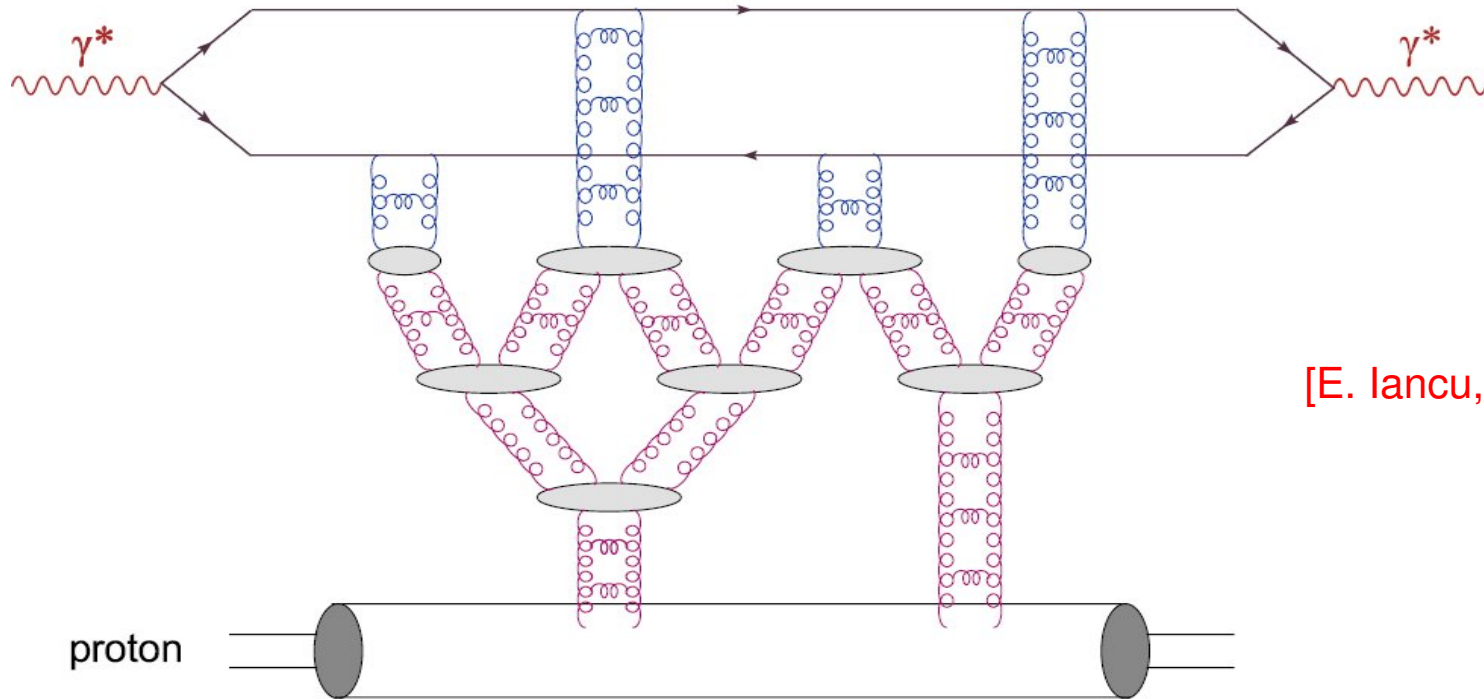


- Same class as **FKPP eq.** (stat. phys.): **diffusion+growth+recombination**

# BK-JIMWLK + “Pomeron loops”

- Full non-linear evolution needs to take into account also **gluon-number fluctuations** (“hot spots” inside hadron):

$$\frac{\partial n}{\partial Y} = \alpha_s \partial_\rho^2 n + \alpha_s n - \alpha_s^2 n^2 + \sqrt{\alpha_s^2 n} \nu \quad \langle \nu(Y_1) \nu(Y_2) \rangle = \delta(Y_1 - Y_2)$$

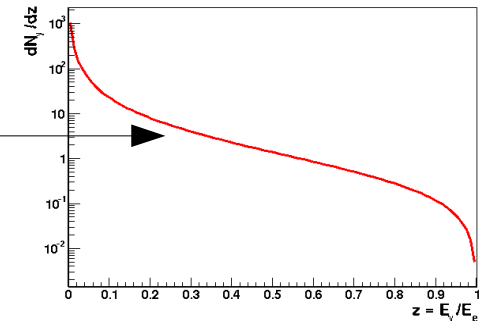
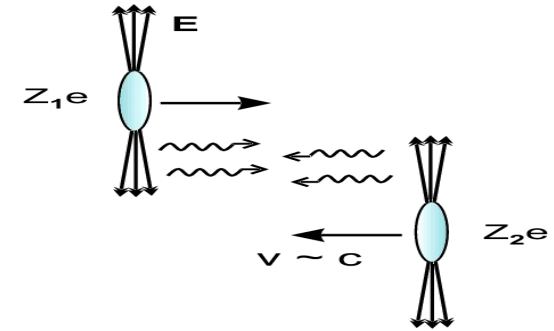


[E. Iancu, ECT\*-07]

- **Stochastic FKKP** equation: full reaction-diffusion process in stat. phys.

# Photoproduction ( $\gamma A$ ) in UPC AA collisions

- Heavy-ions (charge  $Z$ ) produce **strong EM fields** (coherent action of all protons):
- Equivalent **flux of photons** in electromagnetic (aka. Ultra-Peripheral,  $b_{\min} \sim 2R_A$ ) A+A :



$$\frac{dN_\gamma}{dE}(b > b_{\min}) \propto \frac{\alpha_{em} Z^2}{\pi} \frac{1}{E} \quad (\text{soft bremsstrahlung } \gamma \text{ spectrum})$$

- Photon beams:

- **Flux  $\sim Z^2$**  ( $\sim 7 \cdot 10^3$  for Pb).

- **“Coherence condition”** :  $\gamma$  wavelength  $>$  nucleus size

Maximum  $\gamma$  energy:  $\omega < \omega_{\max} \approx \left(\frac{\gamma}{R}\right) \sim 80 - 160 \text{ GeV (Pb,Ca)}$

- Center of mass-energies (LHC):  $\sqrt{s}_{\gamma A} \approx 0.7 - 2. \text{ TeV} \approx (3 - 10) \times \sqrt{s}_{\gamma p}(\text{HERA})$

- Bjorken  $x$  range in nucleus:  $(y=0): x(J/\Psi) \sim 3 \cdot 10^{-3}, x(\Upsilon) \sim 10^{-2}$   
 $(y=3): x(J/\Psi) \sim 2 \cdot 10^{-5}, x(\Upsilon) \sim 10^{-4}$

- Forward **neutron-tagging (ZDC)**:  $\sim 50\%$  UPC colls. lead to nuclear breakup.