

PS2 review

Negative Momentum Compaction lattice options for PS2

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Contributors

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Outline

- Negative (Flexible) Momentum Compaction modules
 - Design principle
 - Example: J-PARC main ring
 - NMC rings
 - With dispersion suppressor
 - Resonant
 - Hybrid
 - Tunability and optics' parameter space scan
 - Chromaticity correction
 - Dynamic aperture
- Comparison and perspectives

Negative Momentum Compaction modules

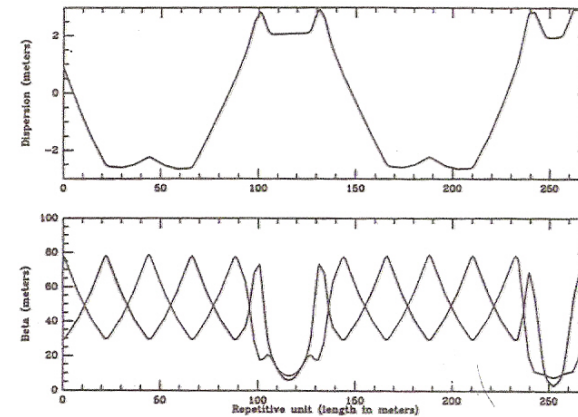
- Avoid transition crossing (beam instabilities and losses)
- Aim at negative momentum compaction

$$a_c = \frac{1}{C} \oint \frac{D(s)}{\rho} ds < 0$$

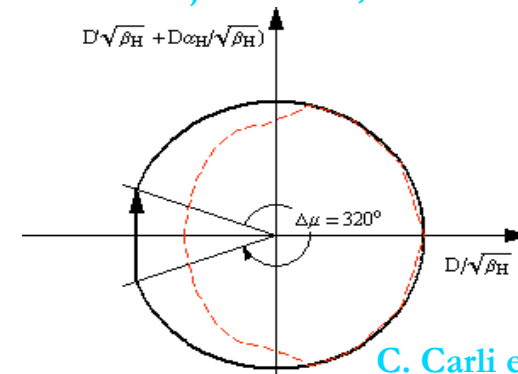
- Modulate dispersion using cells with different bending power
- Normalized coordinates

$$\chi = \frac{D_x}{\sqrt{\beta_x}} \quad \text{and} \quad \xi = D'_x \sqrt{\beta_x} + \frac{\alpha_x D_x}{\sqrt{\beta_x}}$$

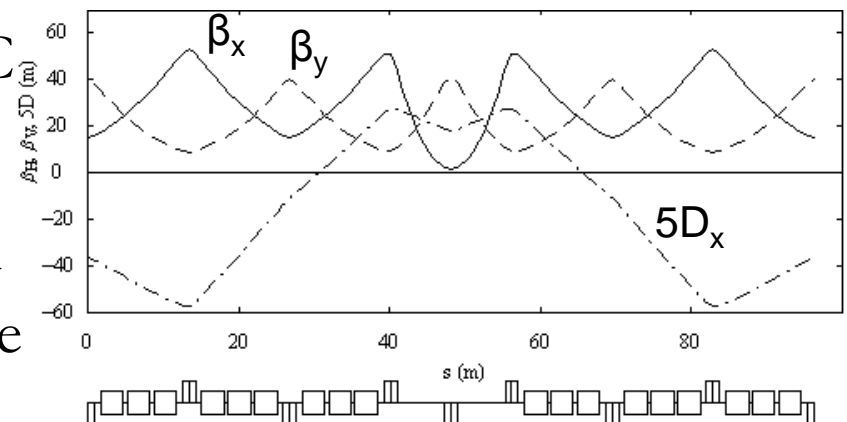
- Dispersion vector (χ, ξ) is invariant outside bends, i.e. vary it with bends in areas of negative dispersion to get NMC
- Similar approach used for J-PARC high energy ring lattices
- **Main difficulty for PS2:** extremely low $\gamma_t \approx 10i$ (high dispersion) in limited space



D. Trbojevic et al, EPAC 90.



C. Carli et al. PAC07

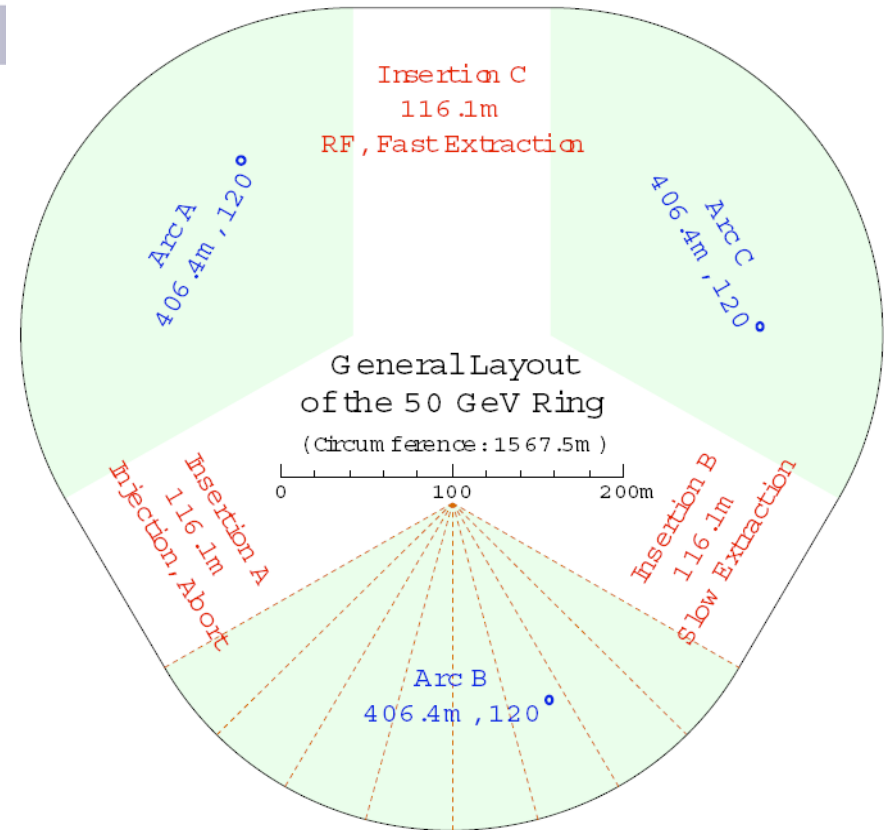


J-Parc Main Ring

- 1567.5m long ring with triangular shape with three 406.4m long arcs and 116.1m long straight sections

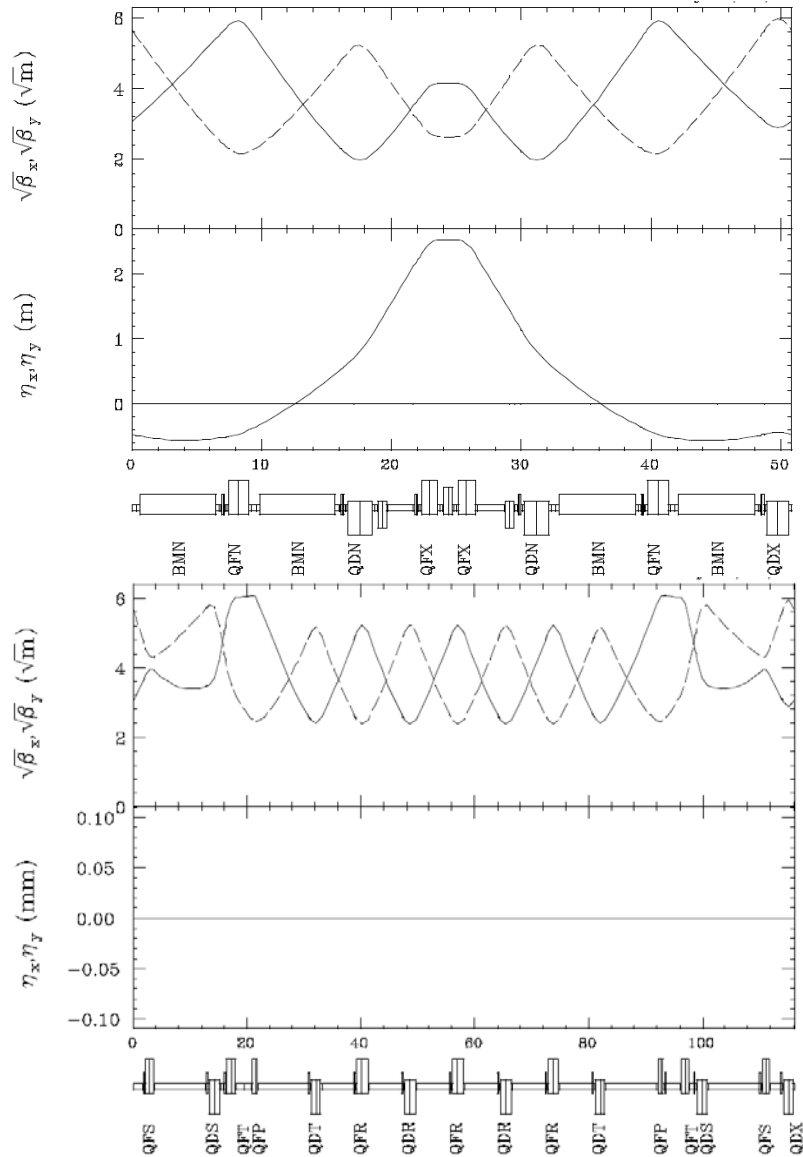
- Optics design criteria

- 3 super-periods (arc + long straight for injection/collimation, extraction and RF)
- Reasonable tuning range for tunes, chromaticity and aim at negative momentum compaction factor (imaginary Y_{\uparrow})



Parameter	J-PARC	PS2
Circumference [m]	1567.5	1346.4
Injection energy [GeV]	3	4
Extraction energy [GeV]	50	50
Particles/pulse [10^{13}]	33	3.2 - 13
Repetition rate [Hz]	0.3	0.21 - 0.42

J-PARC Main Ring lattice



■ Arc with eight **50m**-modules

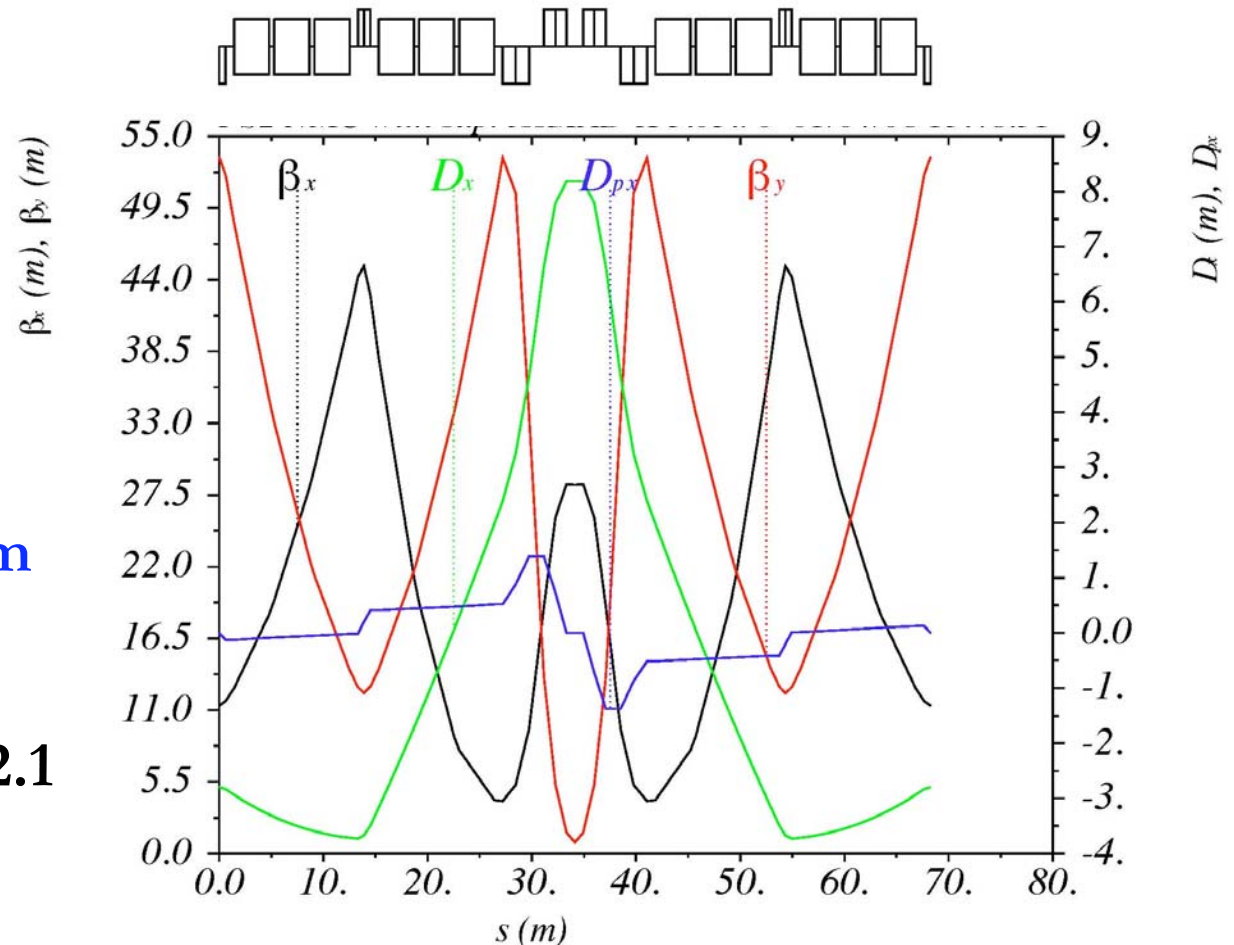
- **32** dipoles (5.85m), 4 families of **57** quadrupoles (1.26-1.86m)
- Module of 3 DOFO cells with central half-cells without bend, with Υ_t of **31.6i**
- Reasonable β and η maxima (35m, 3m)
- Horizontal and vertical phase advance of $3\pi/2$, giving a total of 12π (zero dispersion)
- Vertical phase advance tunable down to 200°

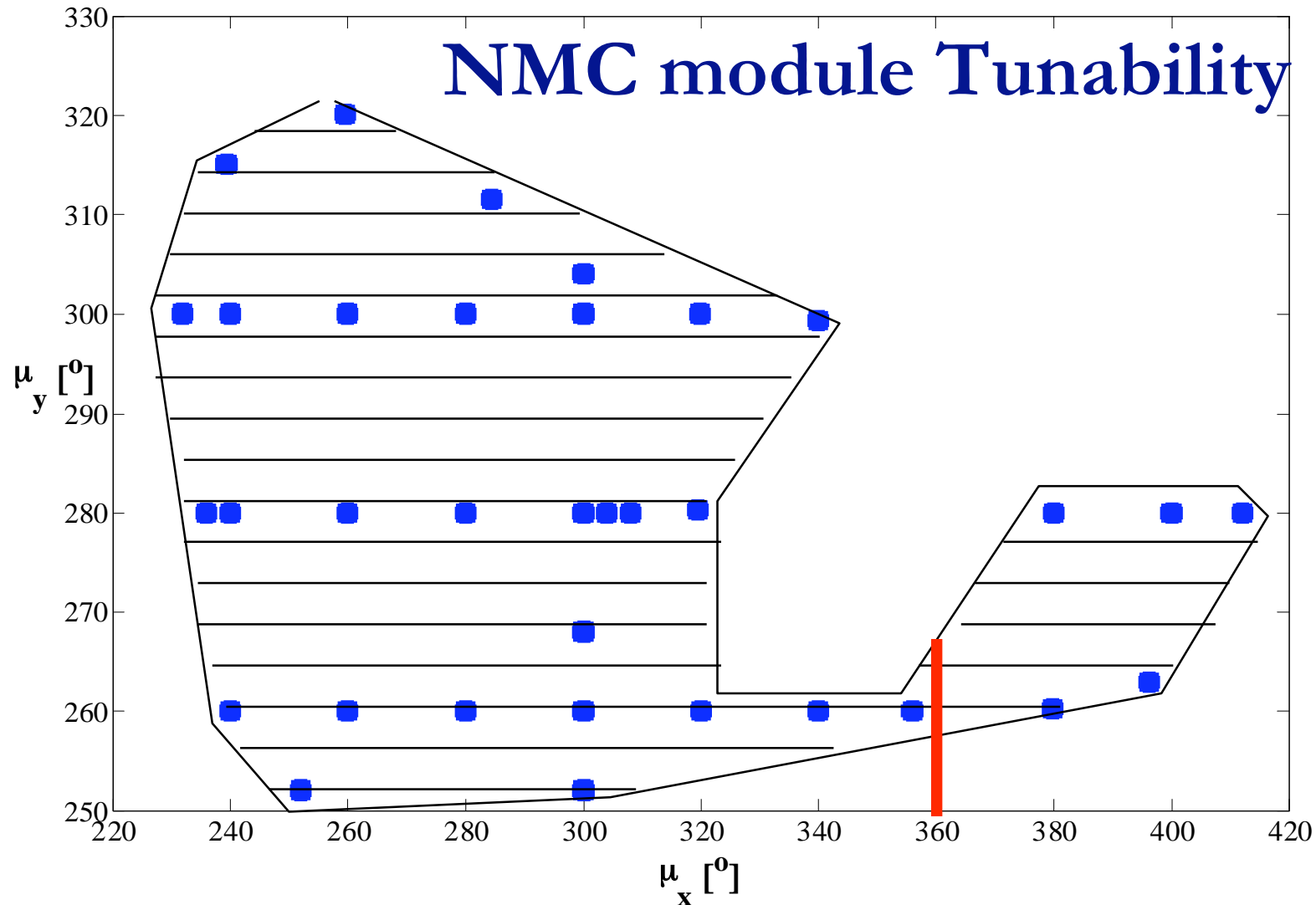
■ Long straight with 3 central DOFOs and doublet matching in either side

- 7 families of **15** quadrupoles (0.9-1.76m)
- FODO cells used for adjusting phase advance (collimation) long half-cell for injection, beam dump and fast extraction, short half-cell for slow extraction (electrostatic septum)

The “short” NMC module

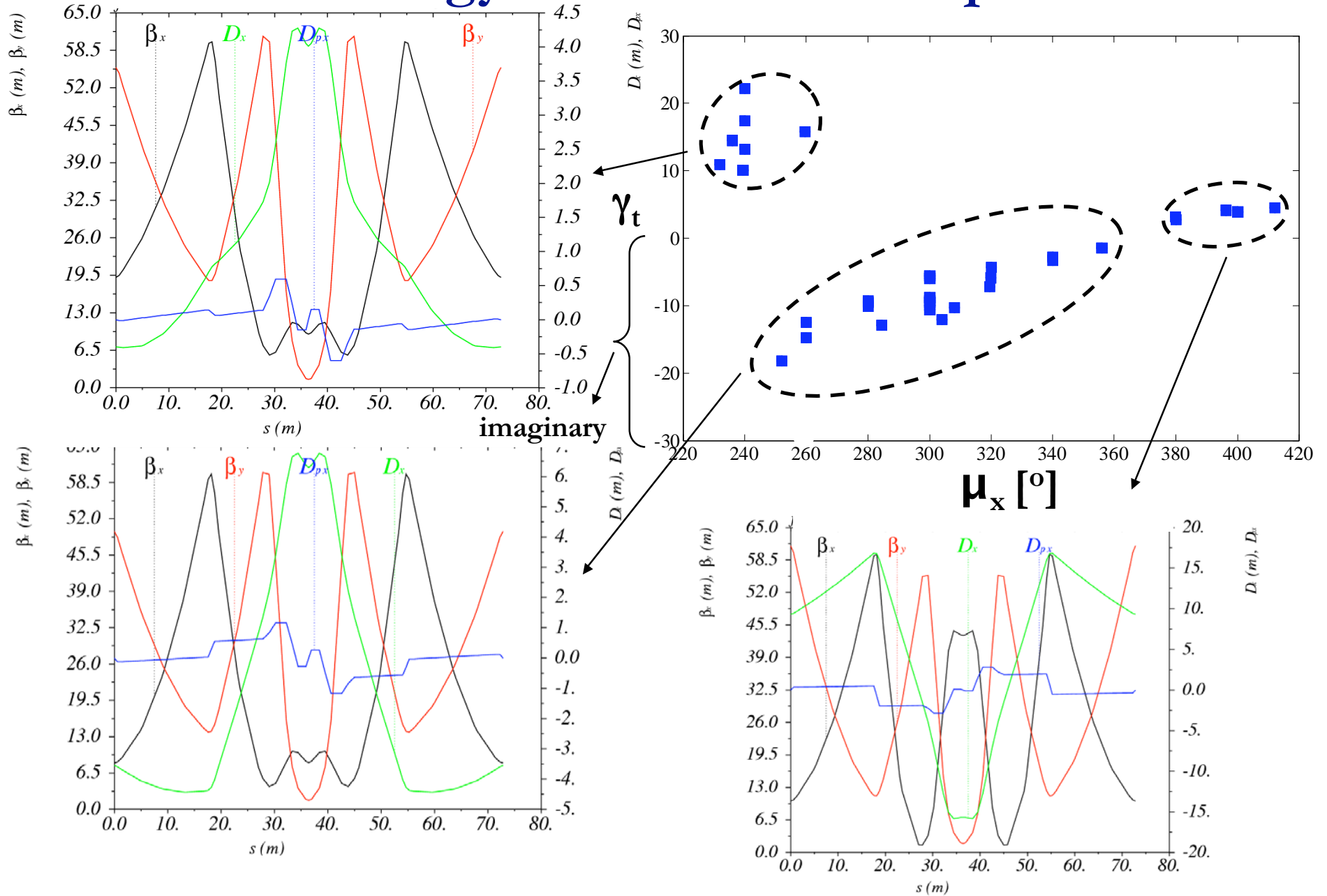
- 1 DOFO cell with 3 + 3 bends and a low-beta doublet
- γ_t of **8.1i**
- Phase advances of **306°** and **288°** per module
- Four families of quads, with max. strength of **0.1m⁻²**
- Max. beta of **44** and **53m**
- Min. dispersion of **-4m** and maximum of **8m**
- Chromaticities of **-1.3, -2.1**
- Total length of **68.25m**
- Magnet-to-magnet drift space requirements satisfied



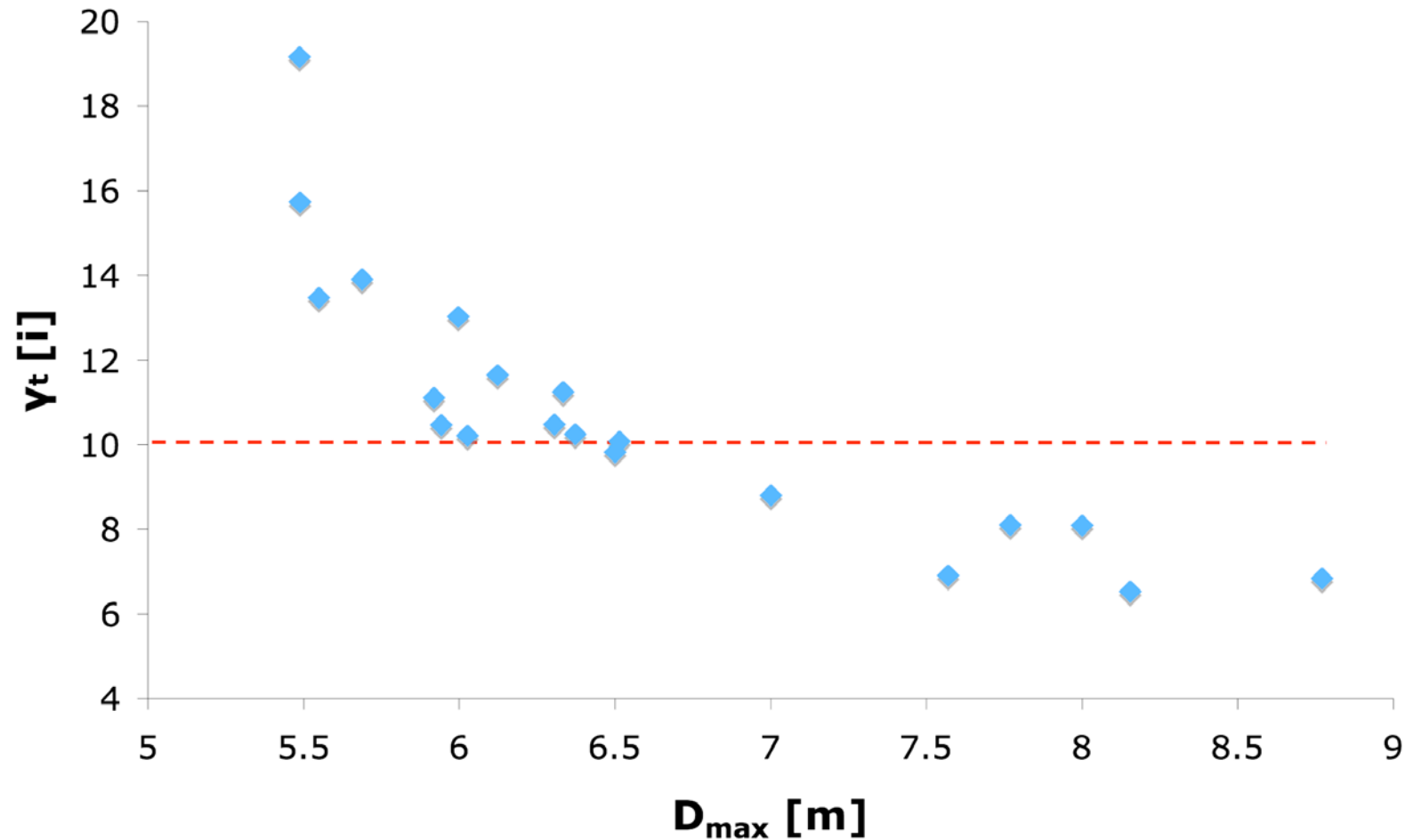


- Phase advance tunable between 240° and 420° in the horizontal and between 250° and 320° in the vertical plane

Transition energy versus horizontal phase advance

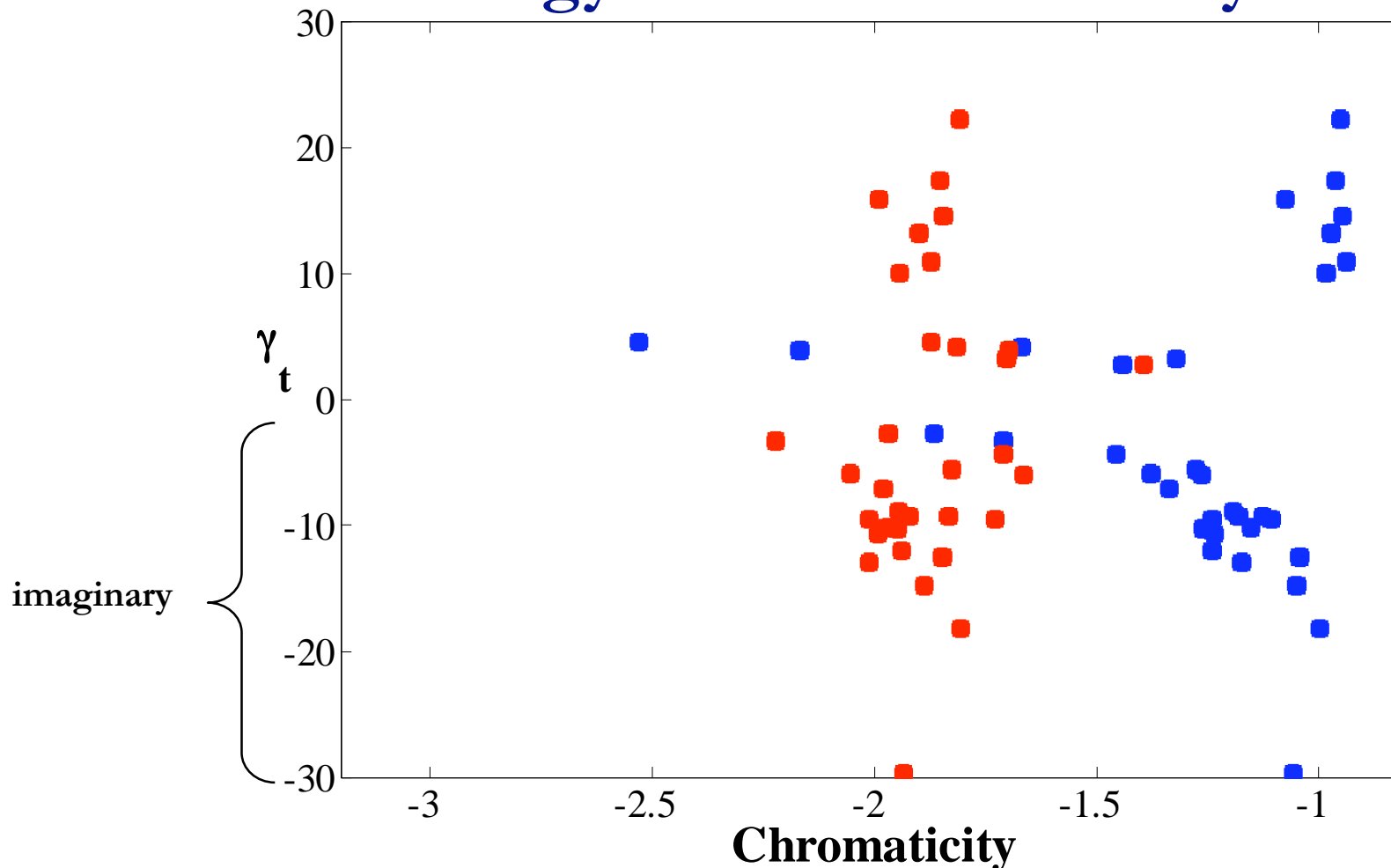


Dispersion versus transition energy



- Almost linear dependence of momentum compaction with dispersion max values
- Higher dispersion variation for Y_t closer to 0
- Smaller dispersion variation for higher Y_t

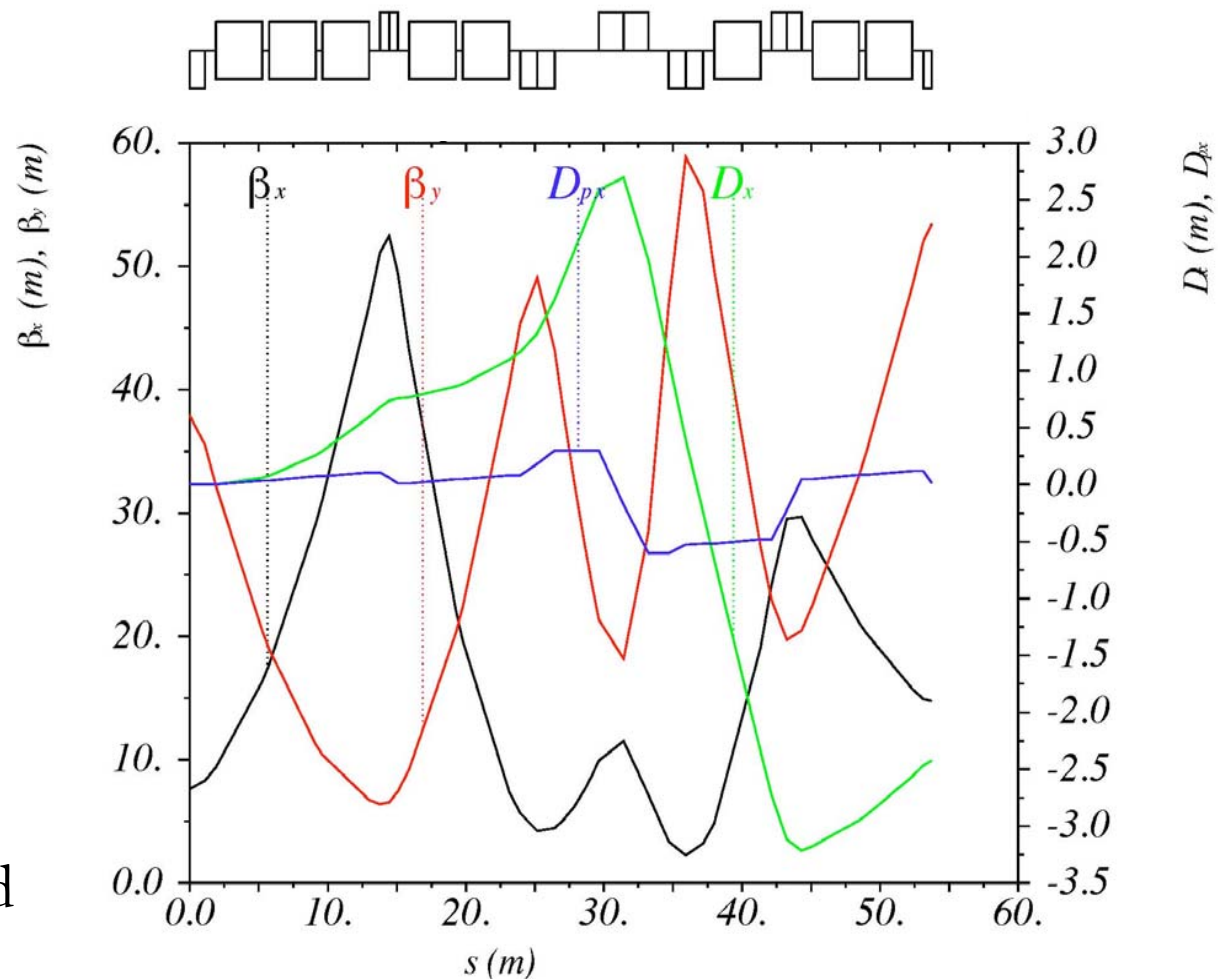
Transition energy versus chromaticity



- Higher in absolute **horizontal** chromaticities for smaller transition energies
- **Vertical** chromaticities between -1.8 and -2 (depending on vertical phase advance)
- Main challenge: design of dispersion suppressor and matching to straights

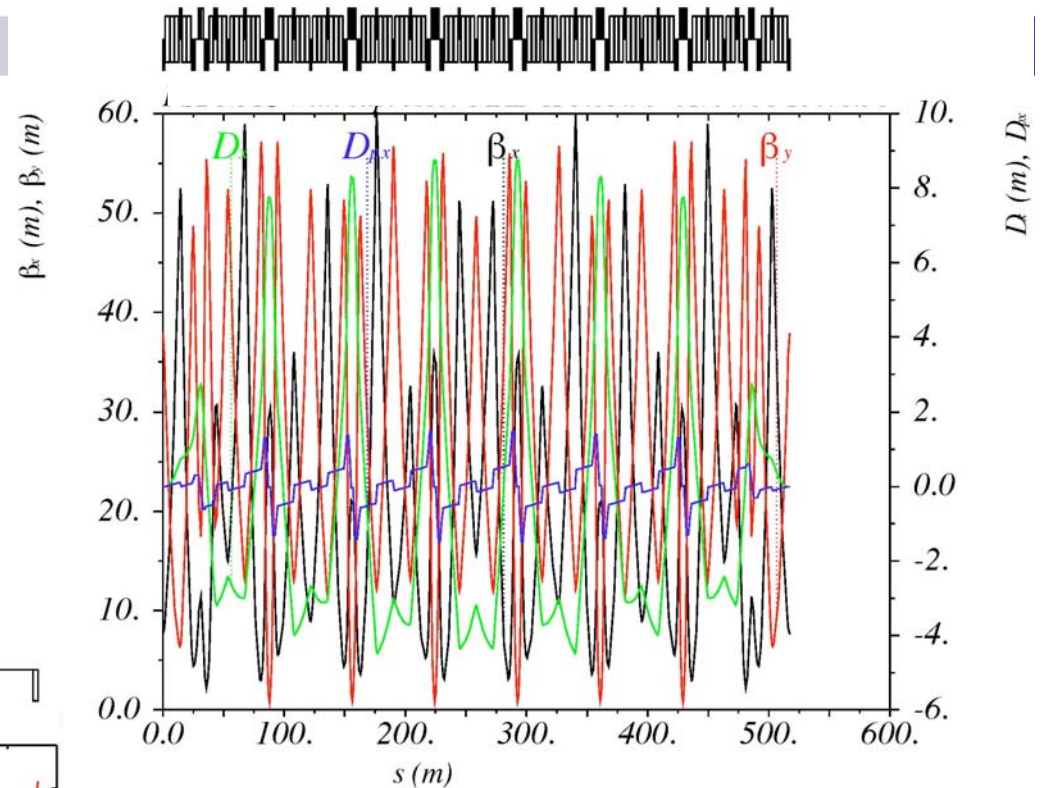
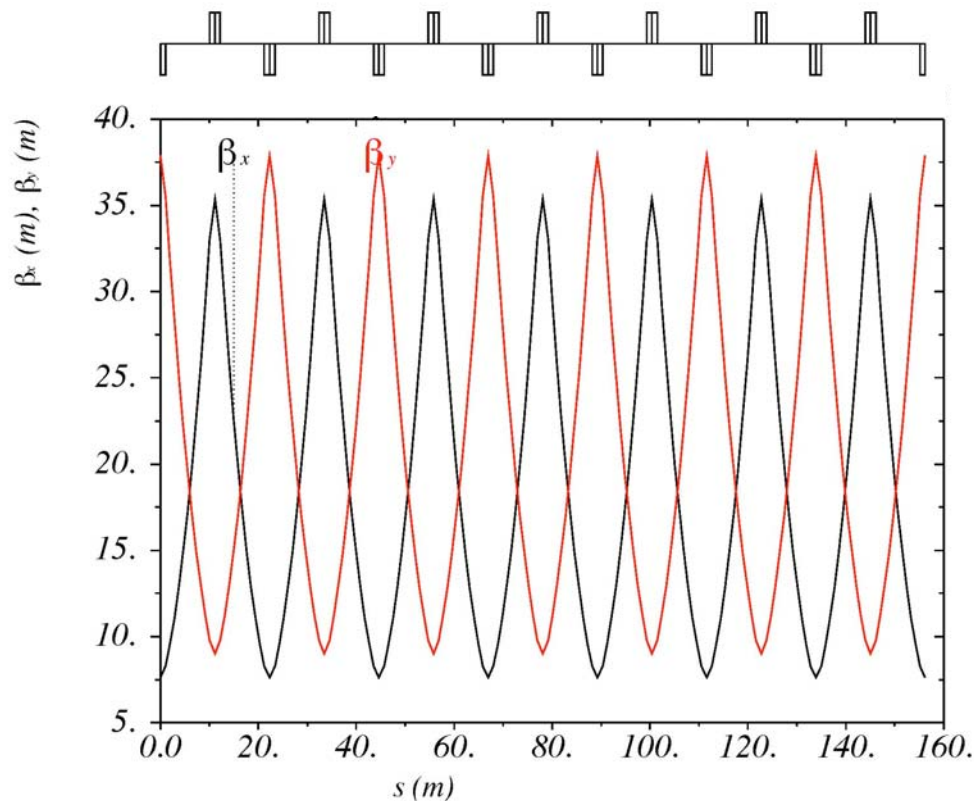
Dispersion suppressor and matching cell

- Similar half module as for the NMC with **3+2** dipoles for suppressing dispersion and matching cell with **1+2** dipoles
- Using **5** families of quads with strengths within the imposed limits (sharing two half quads with the straight section and arc module)
- Maximum beta of **53** and **60m**
- Total length of **53.75m**



Arc and long straight section

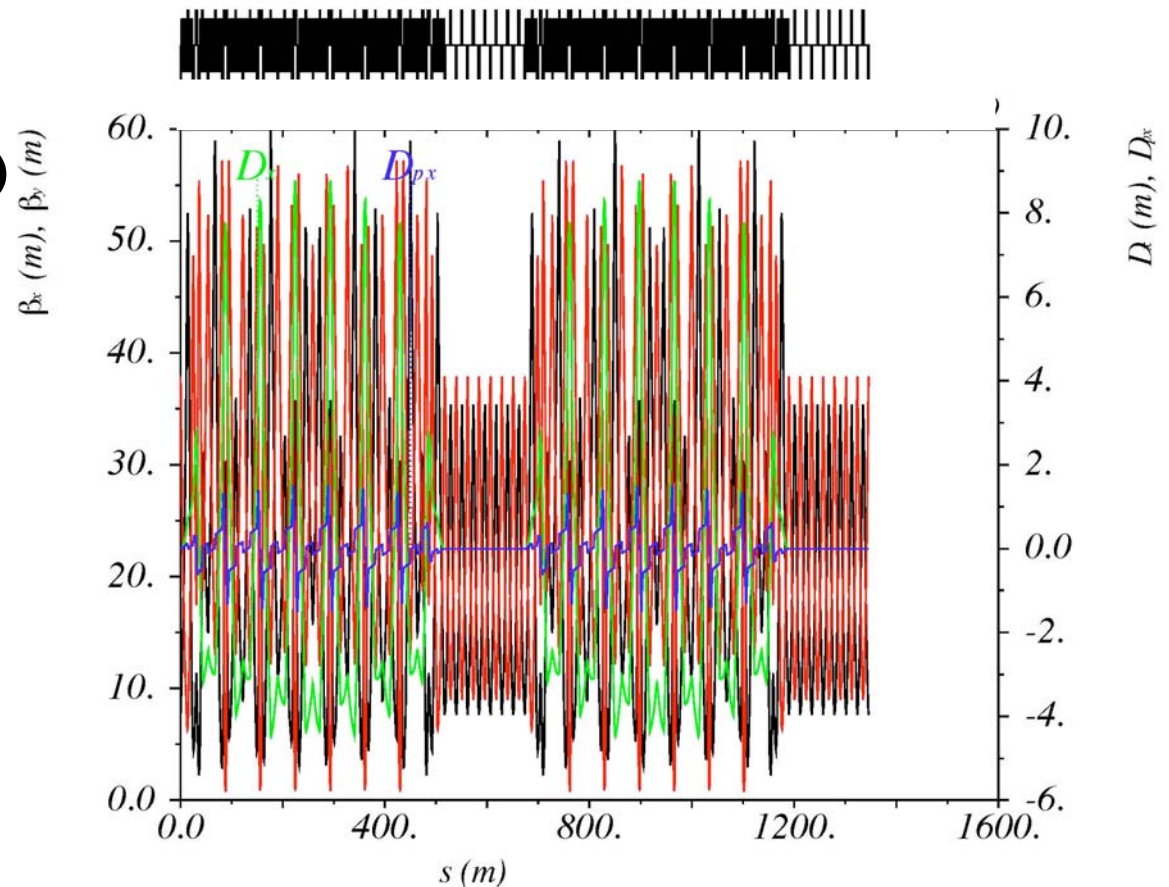
- Arc composed of six NMC modules and two dispersion suppressors with matching cells
- Total length of **517m**



- Straight section with 7 FODO cells with horizontal phase advance of **85.25°** and vertical of **74°**
- Straight section drift of **9m**
- Only two families of quadrupoles are used
- Extra two families can be added for internal phase adjustments
- Total length of **156.2m**

- γ_t of **10.9i**
- Tunes of **16.75** and **14.2**
- **176** dipoles, **3.4m** long (**1.8T** field)
- **134** quadrupoles in **11(+ 2)** families of 6 types (lengths and apertures), with max. strength of **0.1m^{-2}**
- Max. beta of **60m** in horizontal and **57m** in the vertical plane
- Dispersion min. of **-4m** and max. of **8.8m**
- Chromaticities of **-24** and **-32**
- Total length of **1346.4m**

The NMC with dispersion suppressor ring I

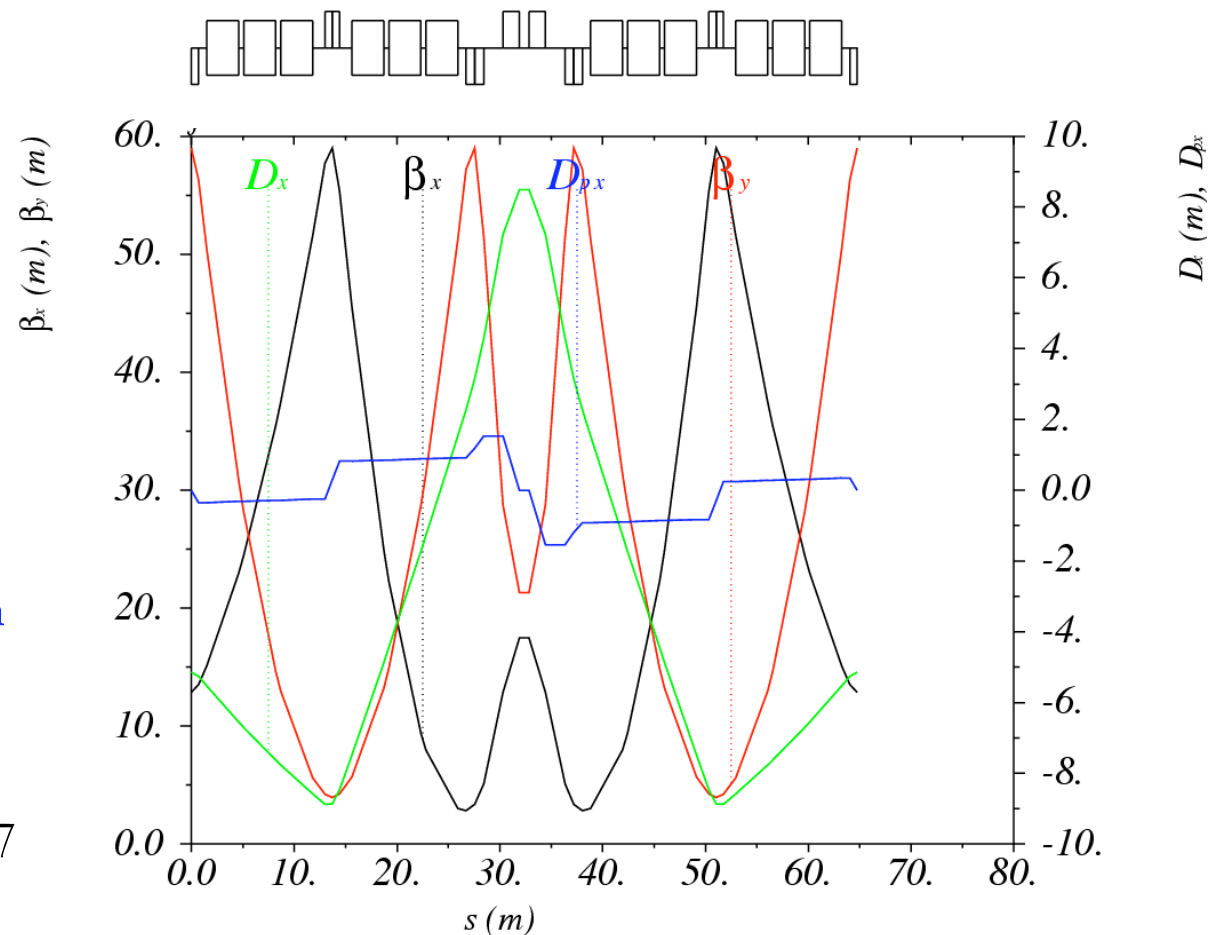


The resonant NMC module

e.g. Y. Senichev BEAM'07

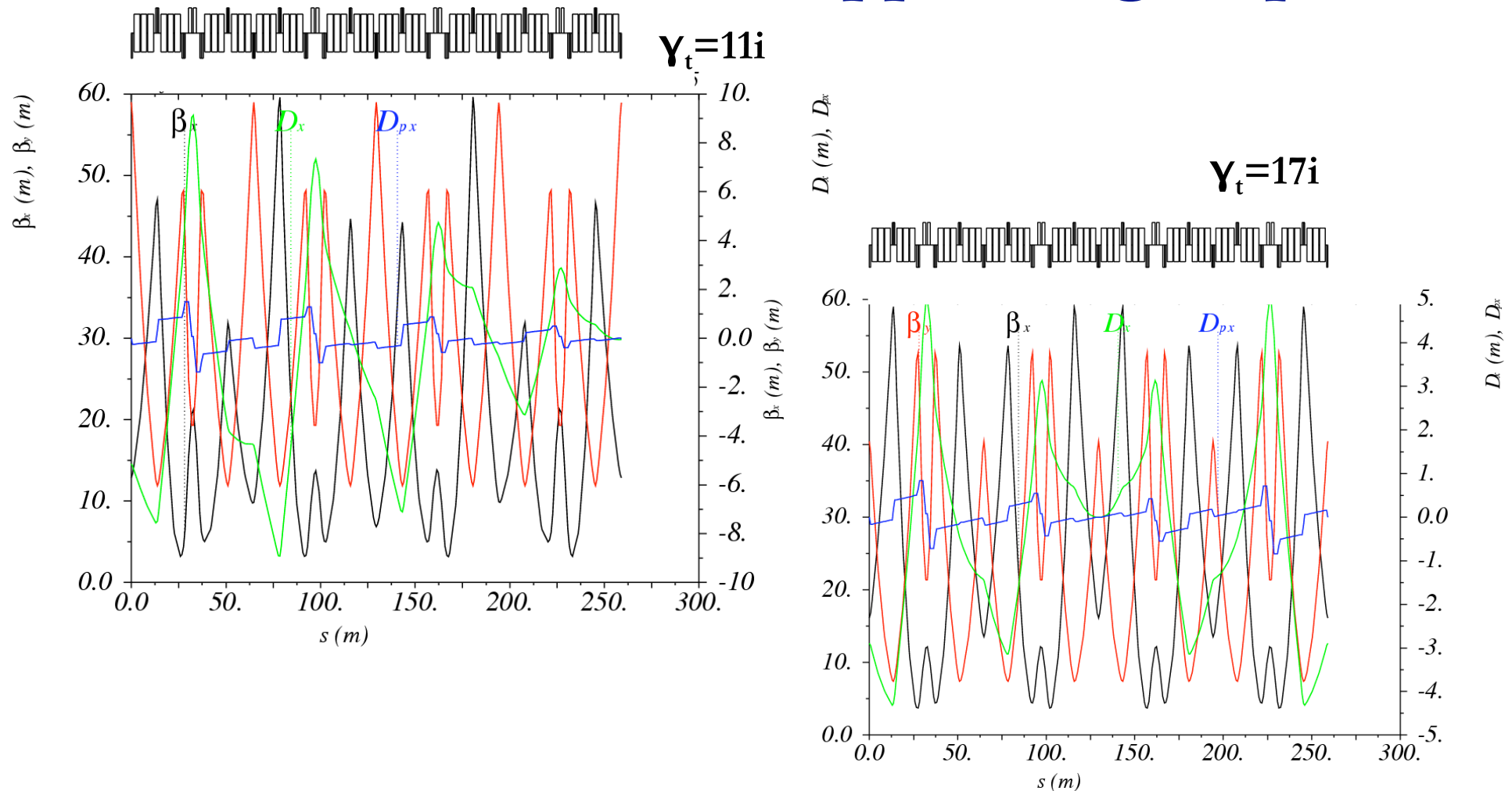
- 1 symmetric FODO cell with 3 + 3 bends and a low-beta doublet

- Phase advances of $315^\circ, 270^\circ$ per module
 - $8 \times 315^\circ \rightarrow 7 \times 2\pi$
 - $8 \times 270^\circ \rightarrow 6 \times 2\pi$
- Υ_t of **5.7i!!!**
- **Four** families of quads, with max. strength of 0.1m^{-2}
- Max. beta of around **59m** in both planes
- Min. and max. dispersion of **-8.5m** and **8.9m**
- Chromaticities of -1.5, -1.7
- Length of **1.2m** between QF and D
- Total length of **64.8m**





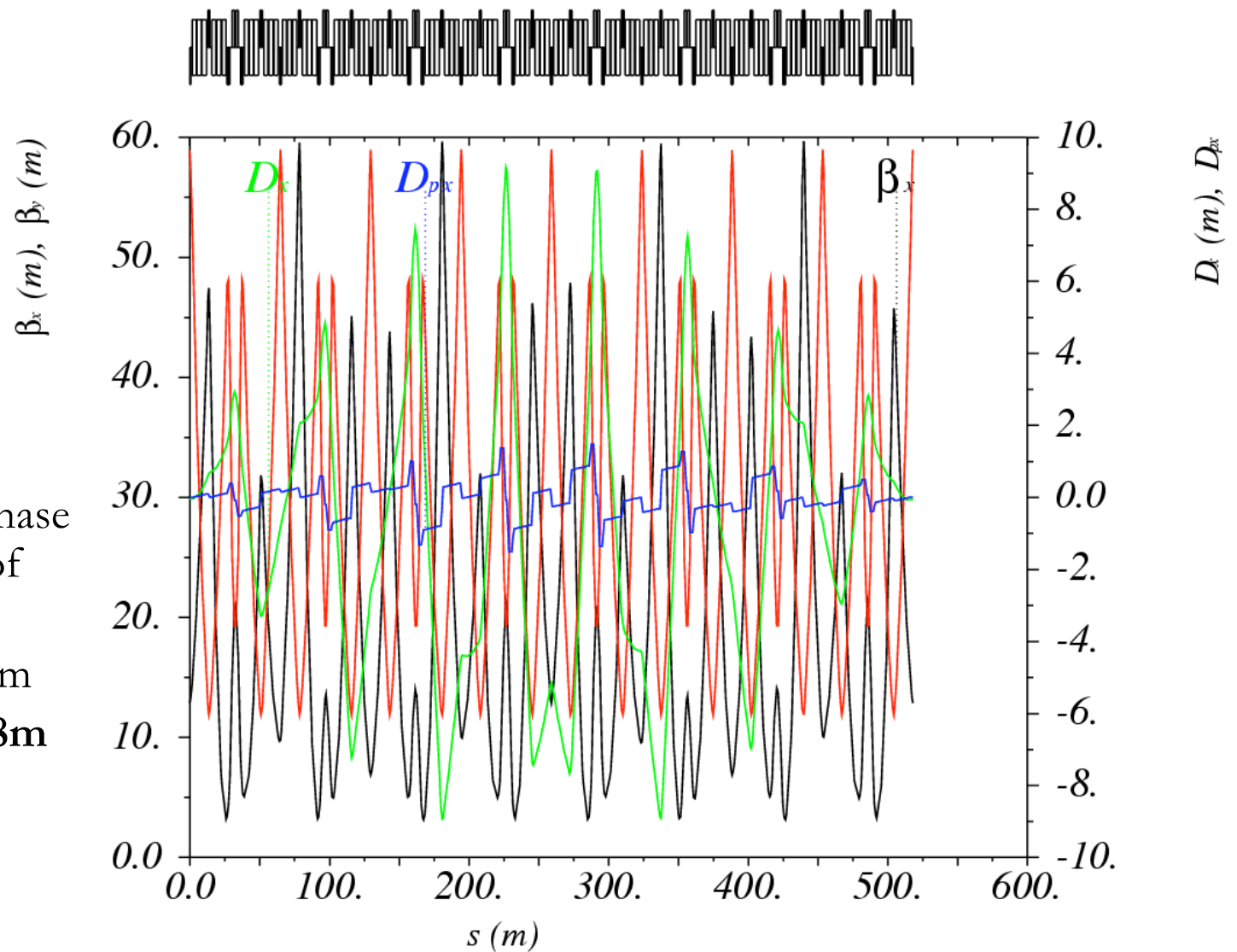
Suppressing dispersion



- Dispersion is suppressed by fixing horizontal phase advance to multiple of 2π
- Solution with **odd** number of 2π multiples preferable for getting **lower imaginary** Y_t

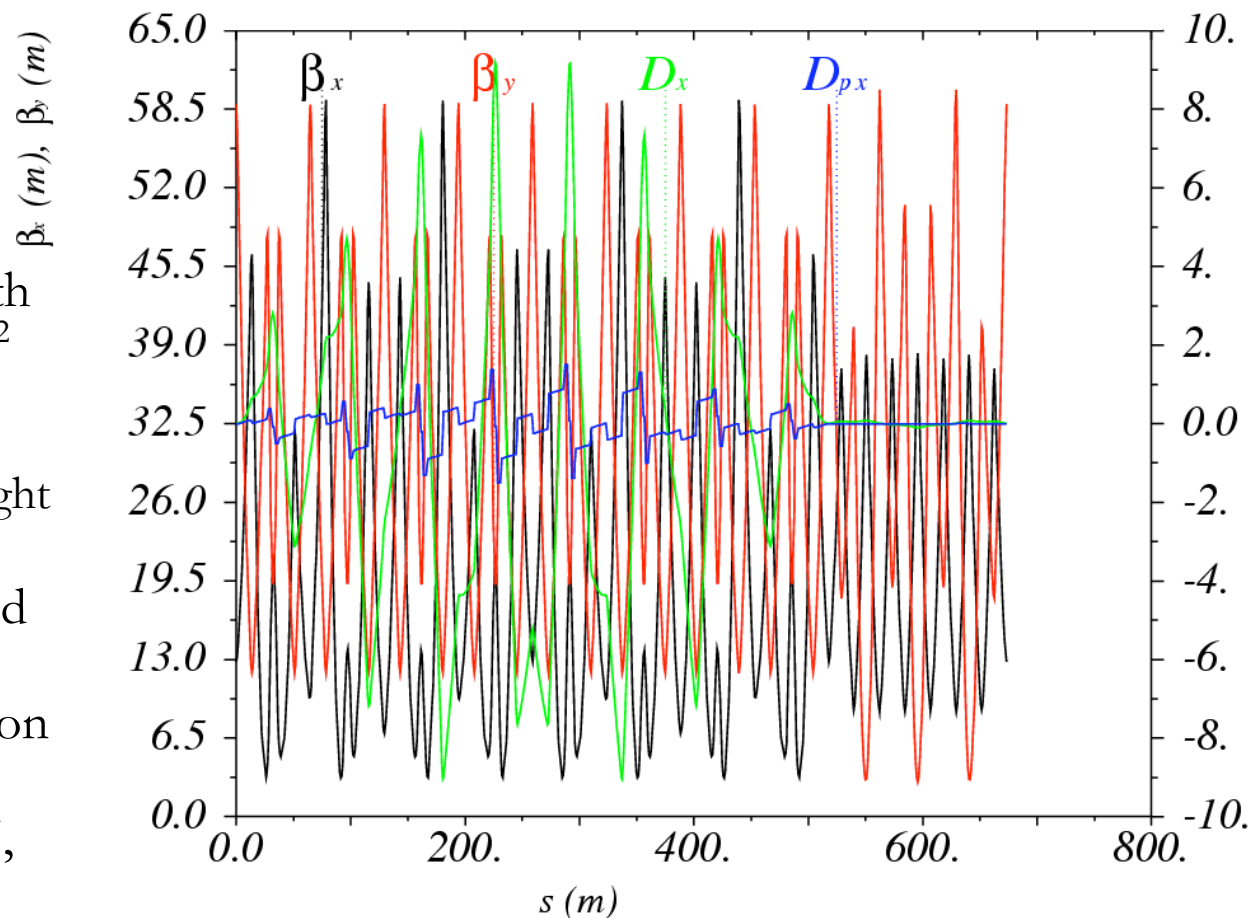
The “resonant” NMC arc

- 8 NMC modules
- Total horizontal phase advance multiple of 2π
- Maximum β of 59m
- Total length of **518m**



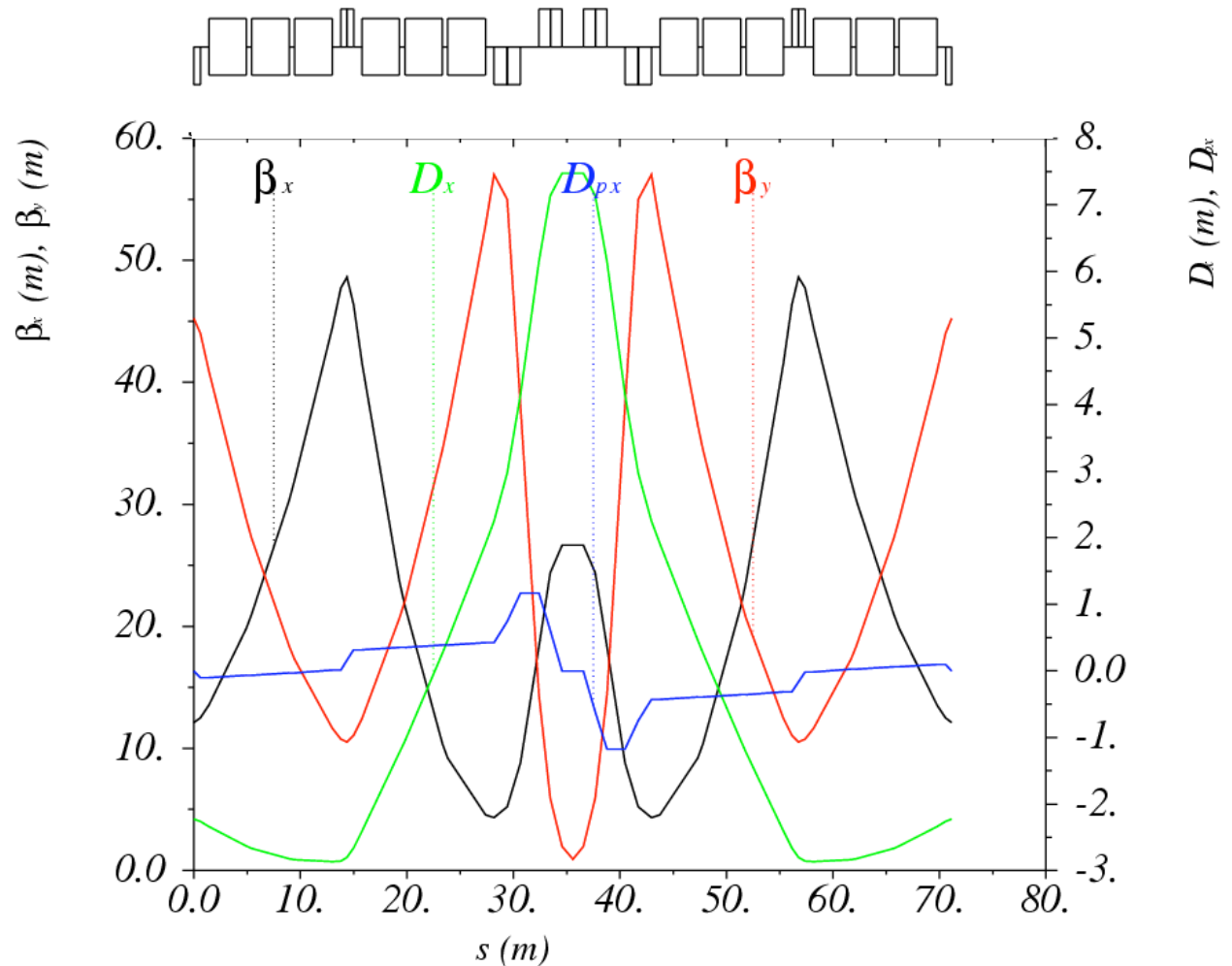
The “resonant” NMC ring II

- Adding a straight section with 7 FODO cells, using 2 matching quadrupoles
 - Straight drift of **9.4m**
 - Tunes of (16.8,9.8)
 - Υ_t of **10.7i**
 - 8 families of quads, with max. strength of 0.1m^{-2}
 - Extra families for phase advance flexibility in the straight
 - Max beta of around **60.5m** in horizontal and vertical plane
 - Min. and max. dispersion of **-8.5m** and **8.9m**
 - Chromaticities of -21.7, -19.8
 - Total length of **1346.4m**



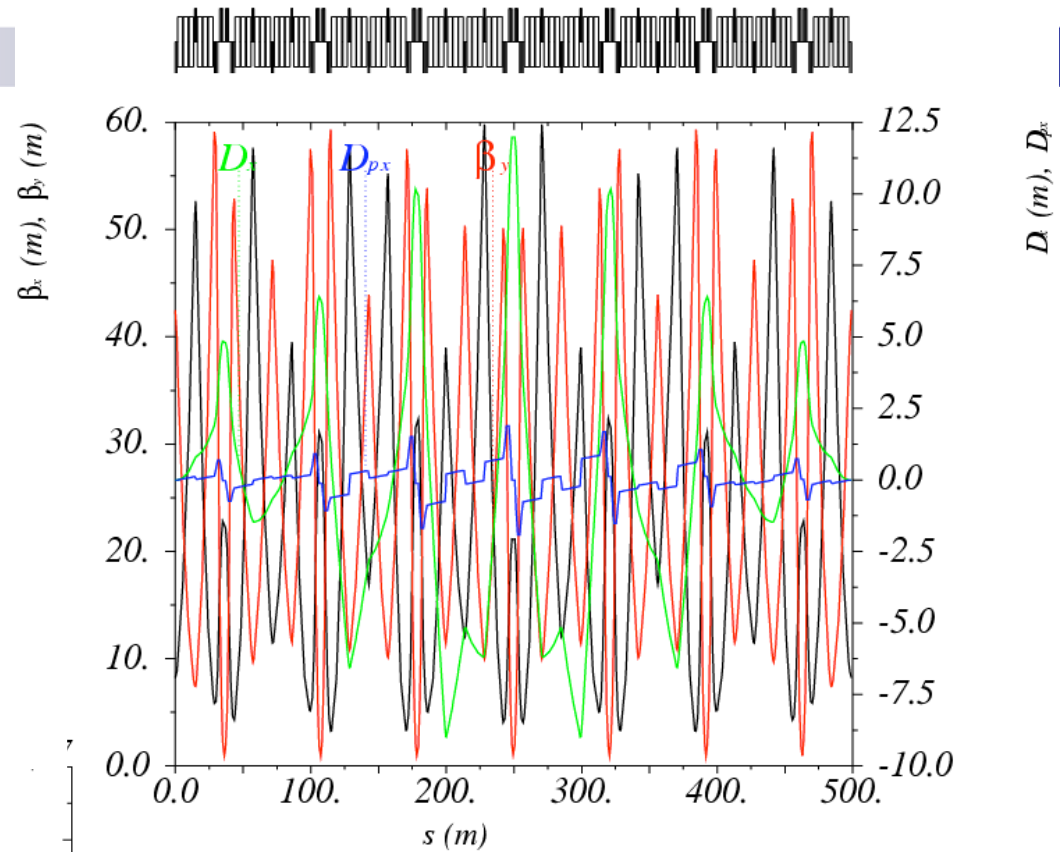
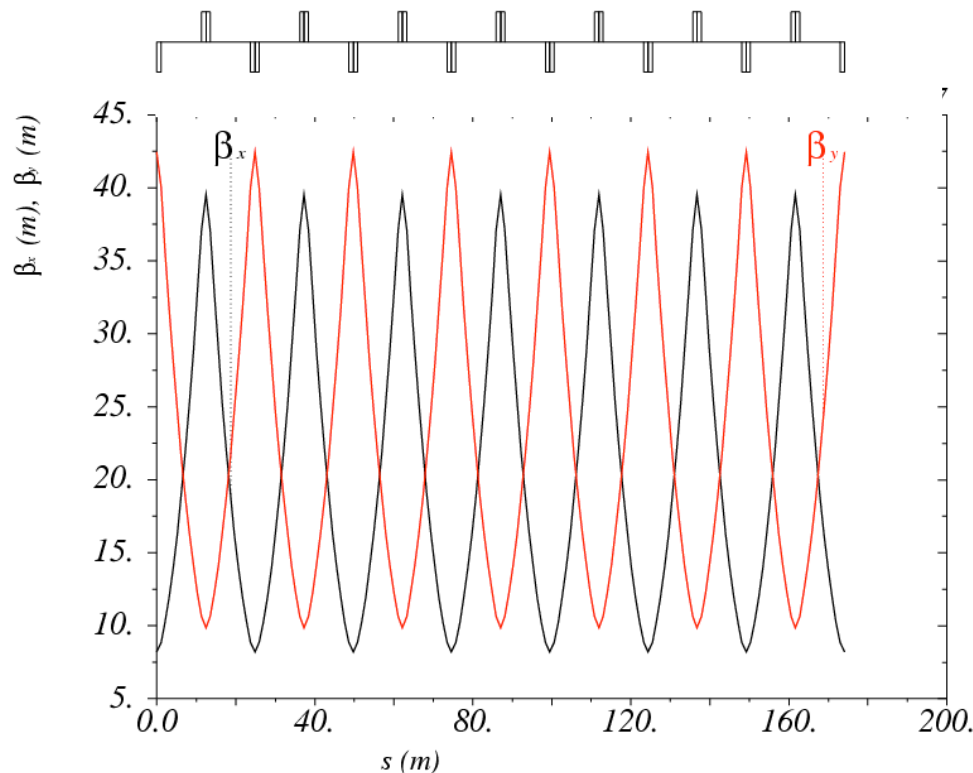
Yet...another NMC arc module

- 1 symmetric FODO cell with 3 + 3 bends and a low-beta doublet
 - Phase advances of $294^\circ, 310^\circ$ per module
 - Υ_t of **10.2i**
 - 4 families of quads, with max. strength of 0.1m^{-2}
 - Max. beta of **49m** and **57m**
 - Min. dispersion of -2.9m and maximum of **7.5m**



Arc and straight section

- Dispersion suppression with 2 extra quad families in the last arc modules
- Last arc quad. shared between arc and straight



- Straight section with horizontal phase advance of 87.5°
- Straight section drift of 10.2m
- Only two families of quadrupoles are used
- Extra two families can be added for extra internal phase adjustments
- Perfectly matched to the arc

- Three types of 8 (+2) quadrupole families (max. strength of 0.1m^{-2}) for a length of **1346.4m**

- Υ_t of **11i**

- Tunes matched to **(14.8,15.2)**

- Max. β 's of around **60m** both planes

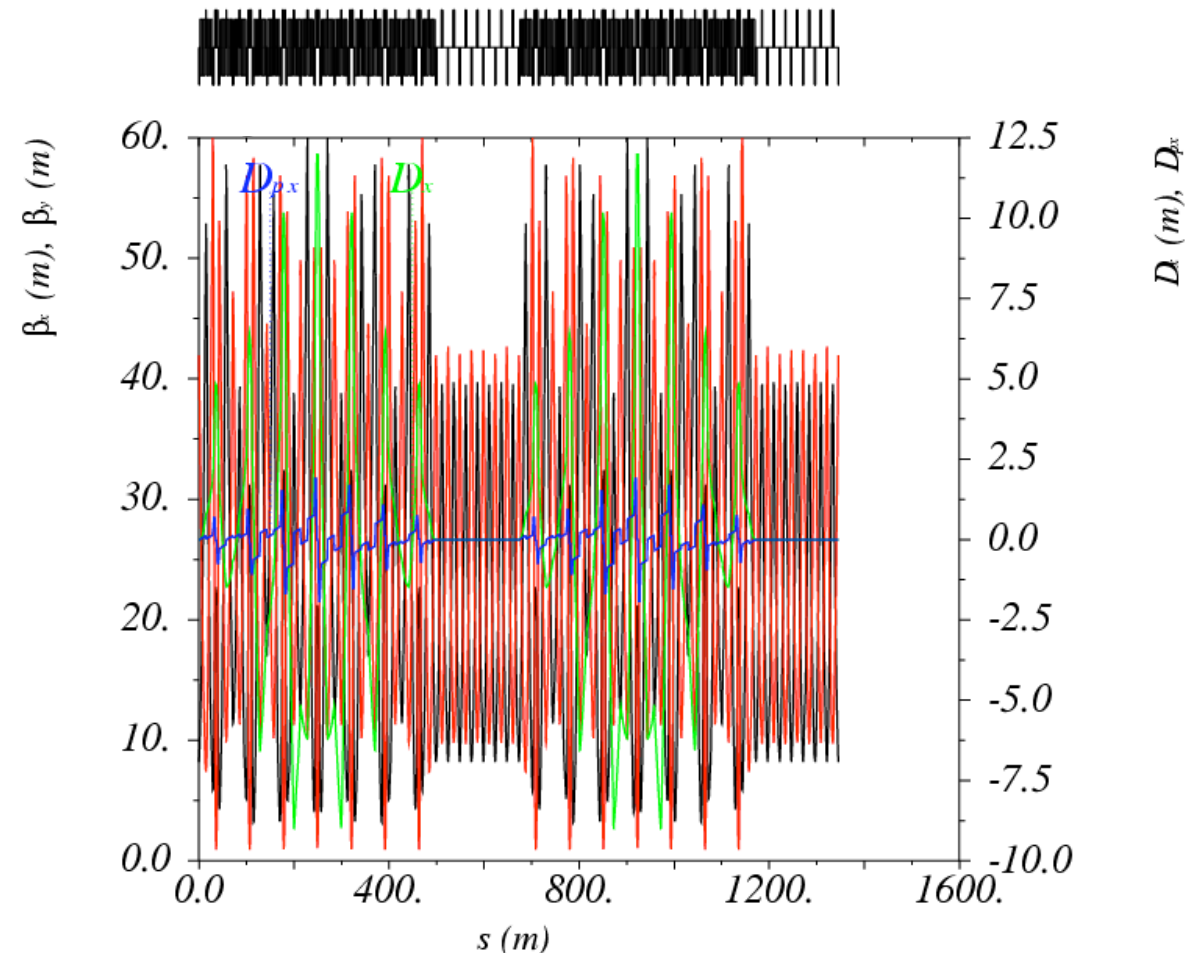
- Dispersion of **-9m** and maximum of **12m**

- Tunability between **14** and **16** in both planes but penalty on the beta function maxima

- Chromaticities of -21.5, -32.2

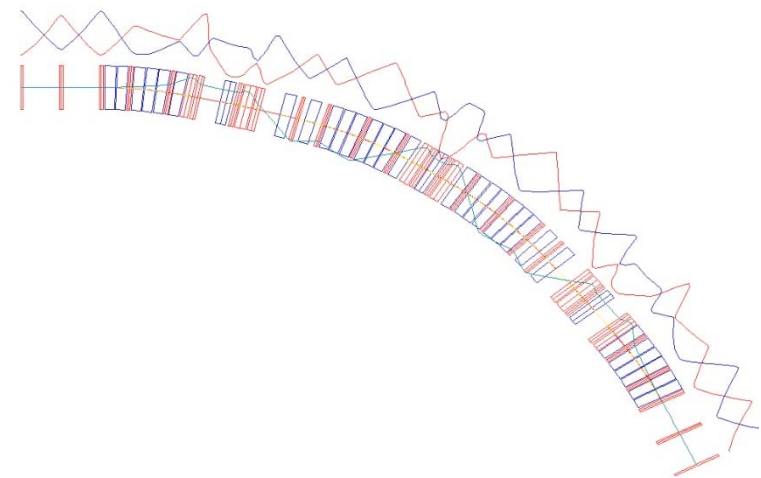
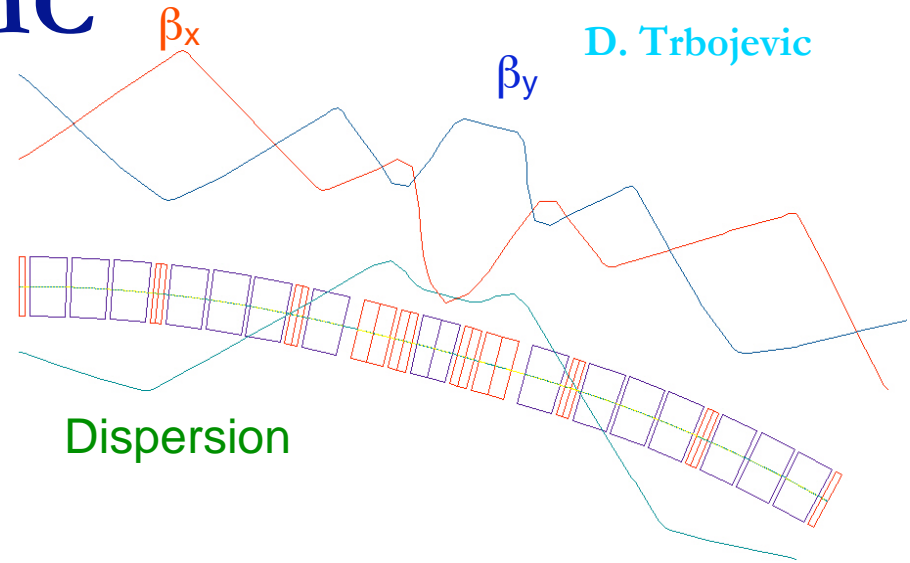
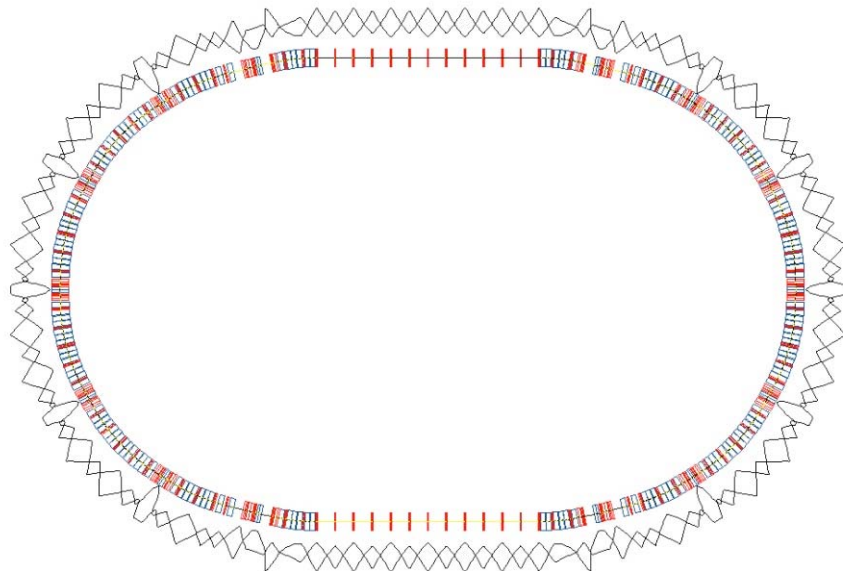
29/05/08

The “hybrid” NMC ring III



High filling factor NMC

- High filling factor module with additional dipoles in between the low beta doublets
- Υ_t of **8.66i** for the module and **11.6i** for the ring
- Max. horizontal beta of **53m** and vertical of **46m**
- Min. dispersion of **-4.3** and maximum of **3.3 m**
- Maximum quadrupole gradient of **0.11m⁻²**
- Total length of **75.9 m**
- Chromaticities of **-20.2** and **-17.4**

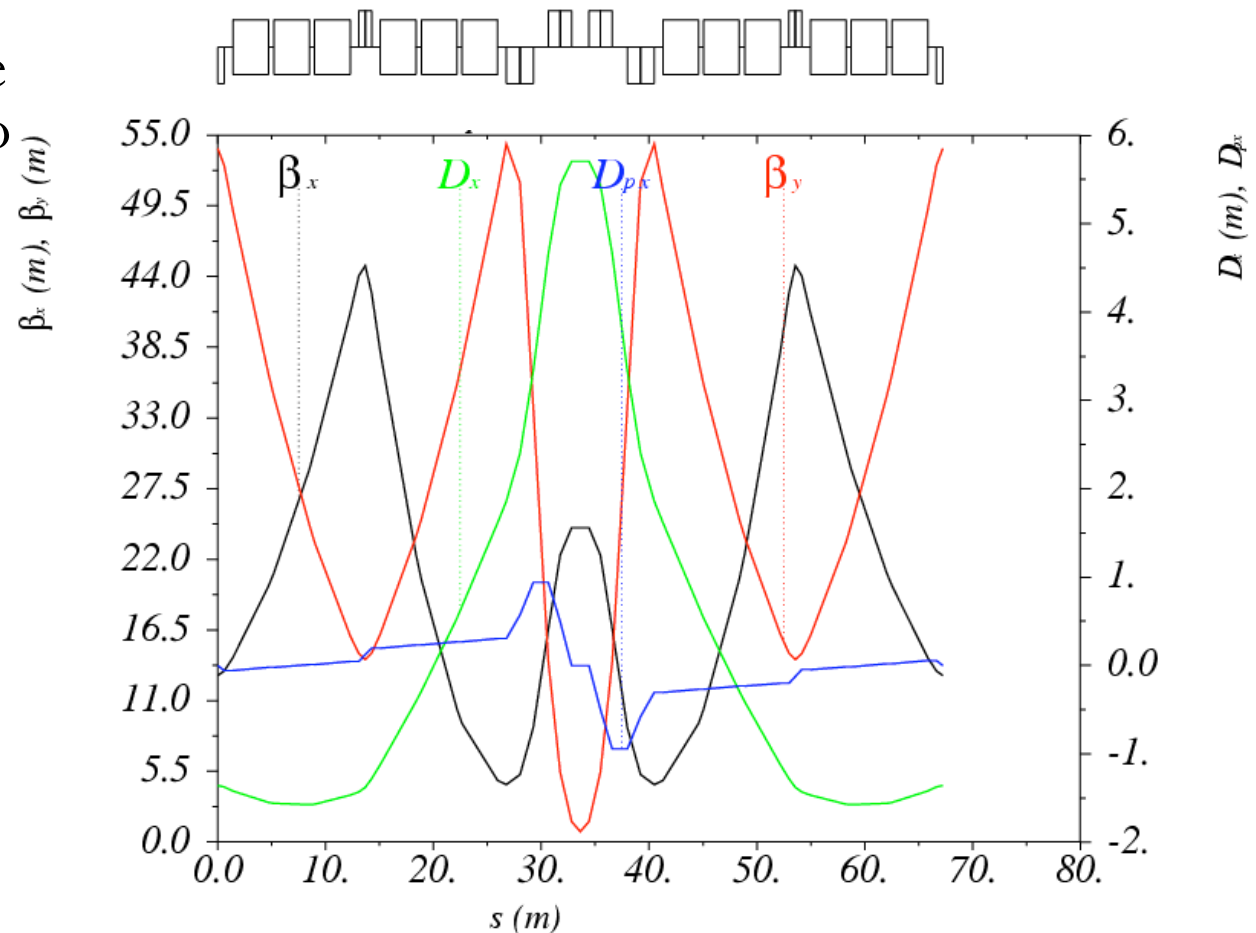


- Main disadvantage is the long arc: only **6** cells available for long straight sections

D. Trbojevic

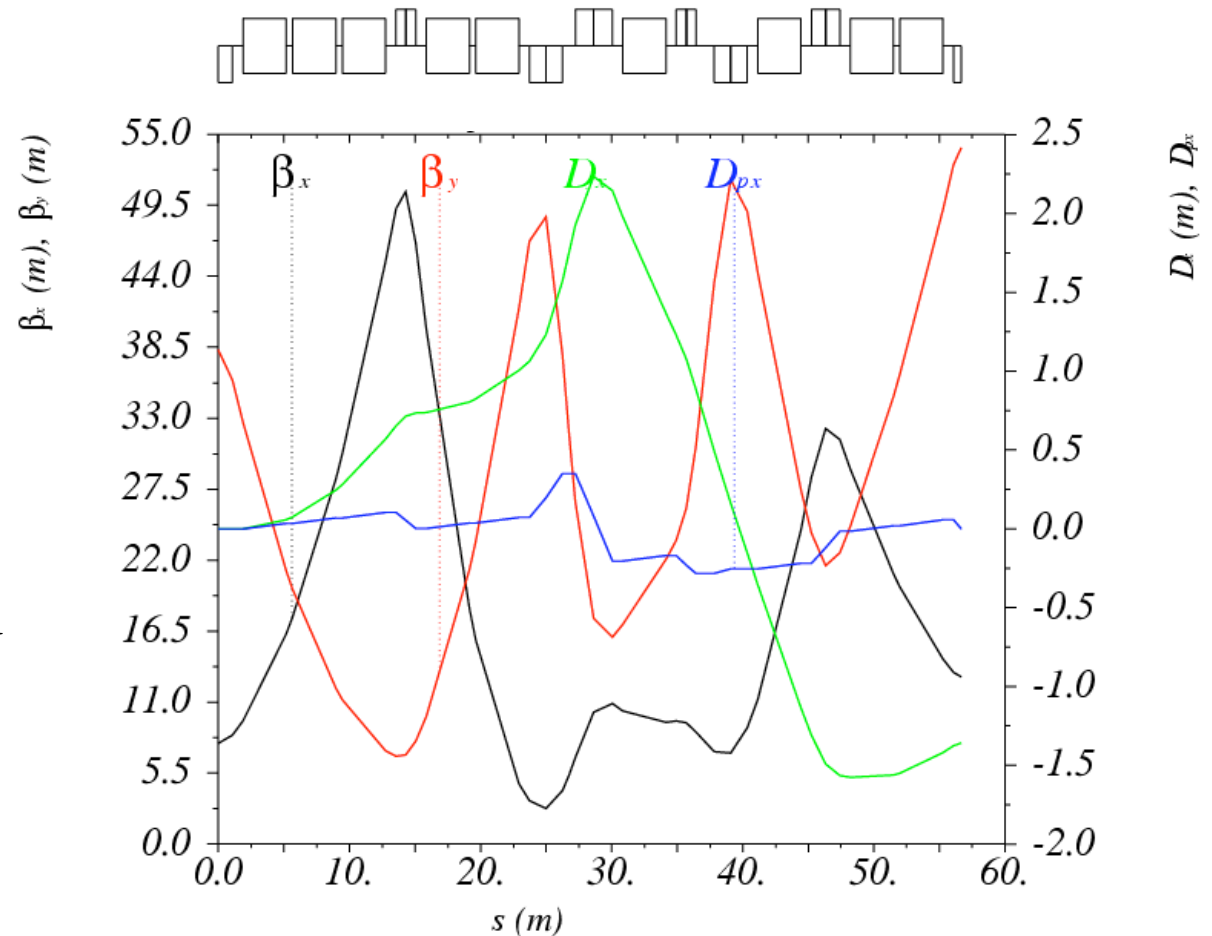
“Short” NMC module with high imaginary γ_t

- Raising the γ_t to **15.3i** by decreasing the phase advances per module to **280°** and **275°** (from **306°** and **288°**)
- Max. beta of **44** and **53m** (as before)
- Min. dispersion of **-1.5m** (from **-4m**) and max. of **5.7m** (from **8m**)
- Chromaticities of **-1.1** and **-2** from (**-1.3** and **-2.1**)
- Total length of **67.25m** (from 68.25)



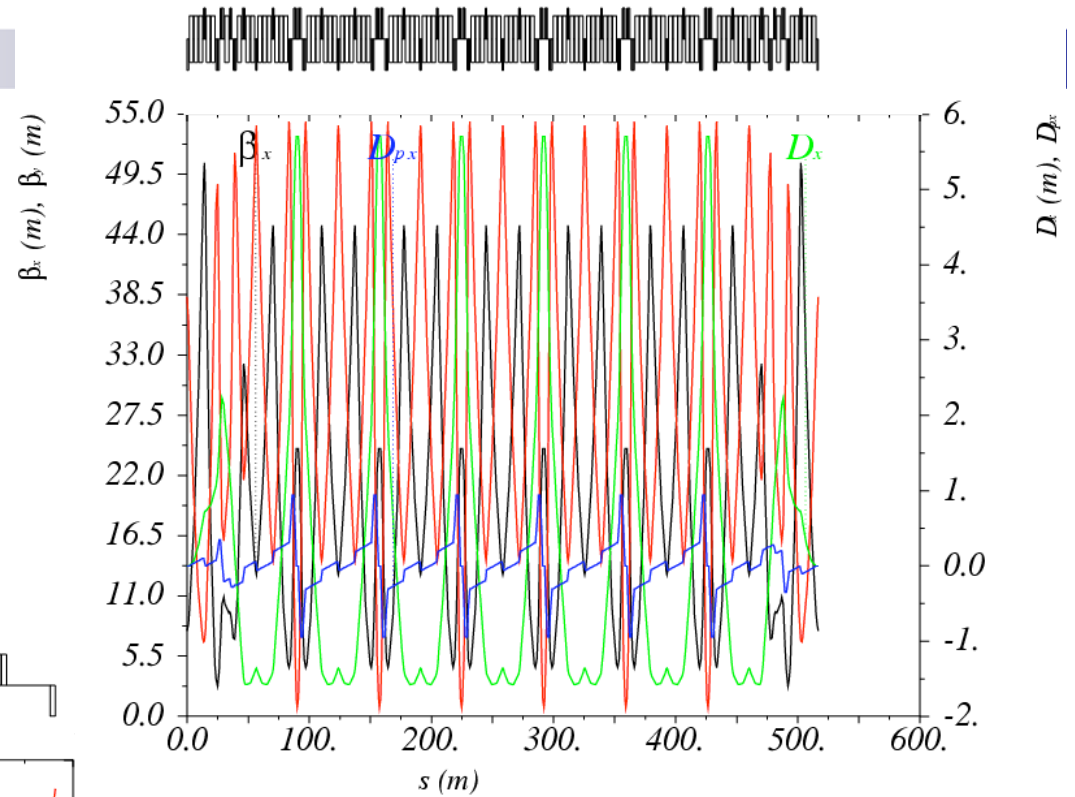
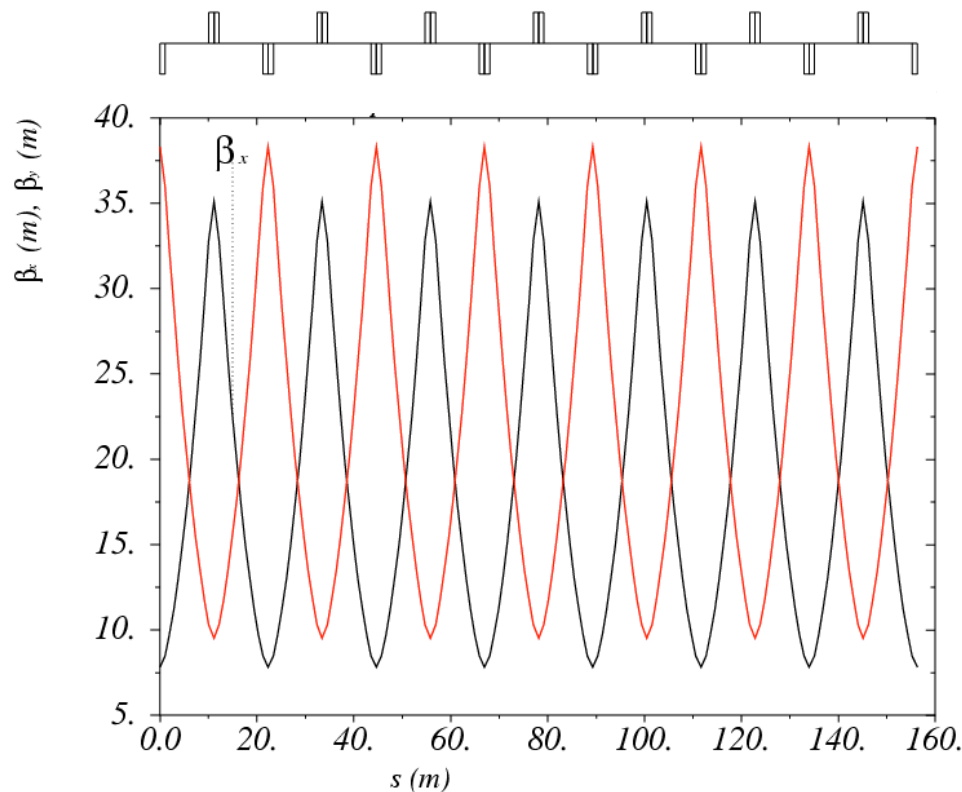
Dispersion suppressor and matching cell

- Similar half module as for the NMC with **3+2** dipoles for suppressing dispersion and matching cell with **1+1+2** dipoles (from 1+2)
- Using **6** (instead of **5**) for better matching
- Maximum beta of **50** and **54m** (from 53 and 60m)
- Total length of 56.7m (from 53.8m)



Arc and long straight section

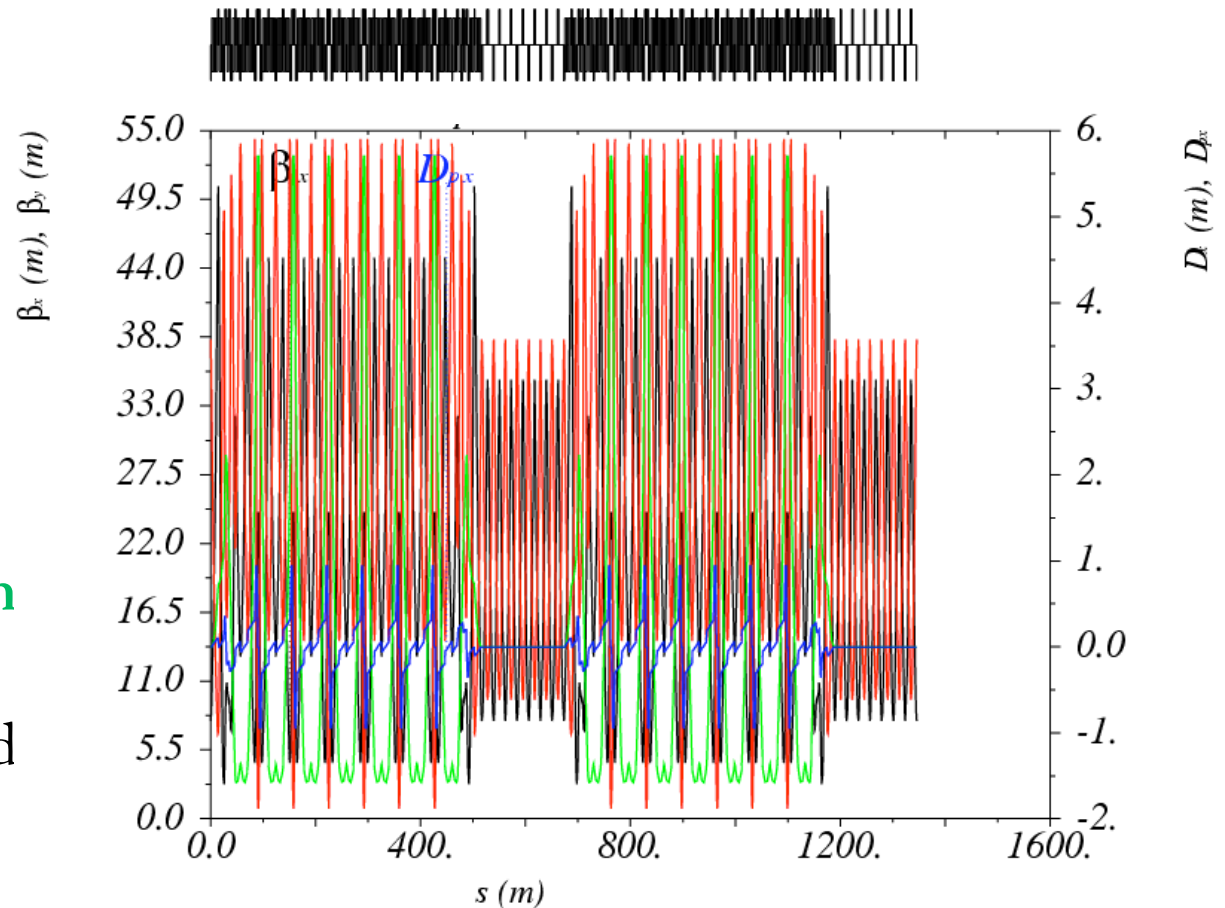
- Arc composed of six NMC modules and two dispersion suppressors with matching cells
- Total length of **517m** (as before)



- Straight section with 7 FODO cells with horizontal phase advance of **84.35°** and vertical of **71.7°**
- Straight section drift of **9m** (as before)
- Total length of **156.3m**

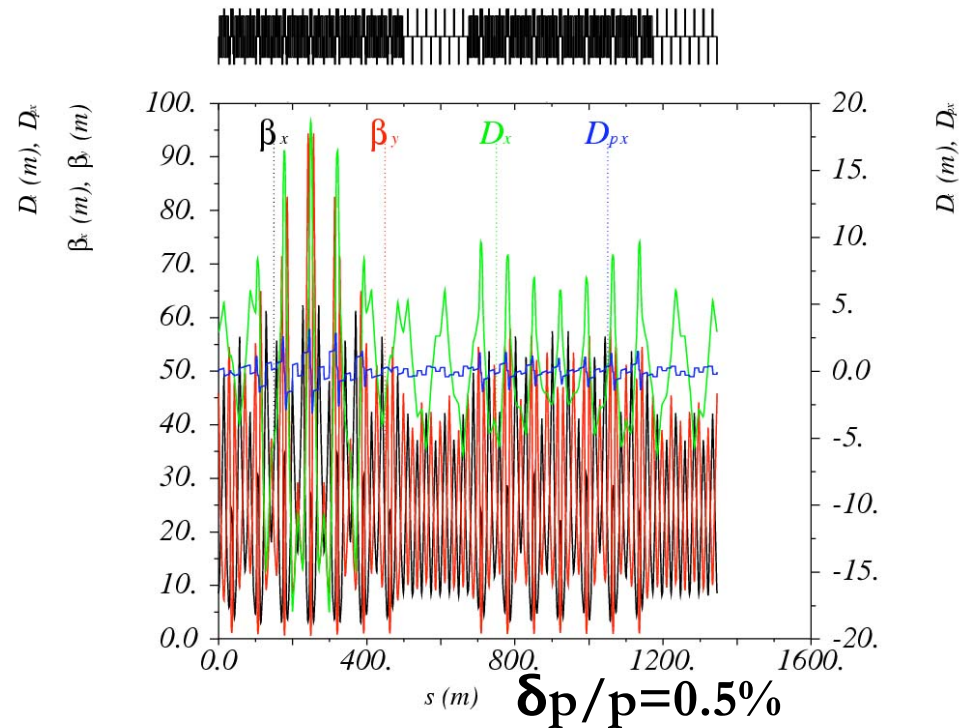
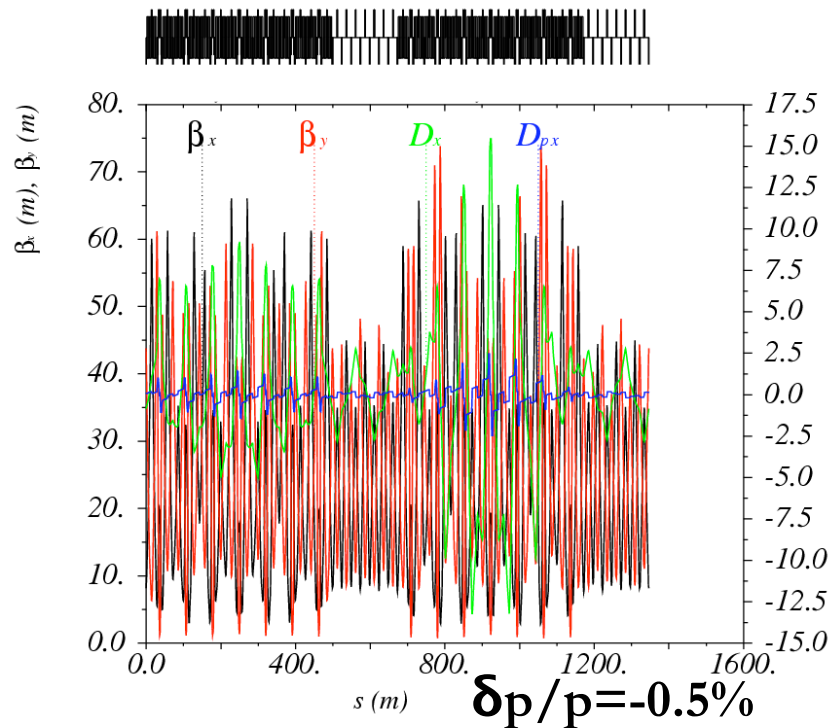
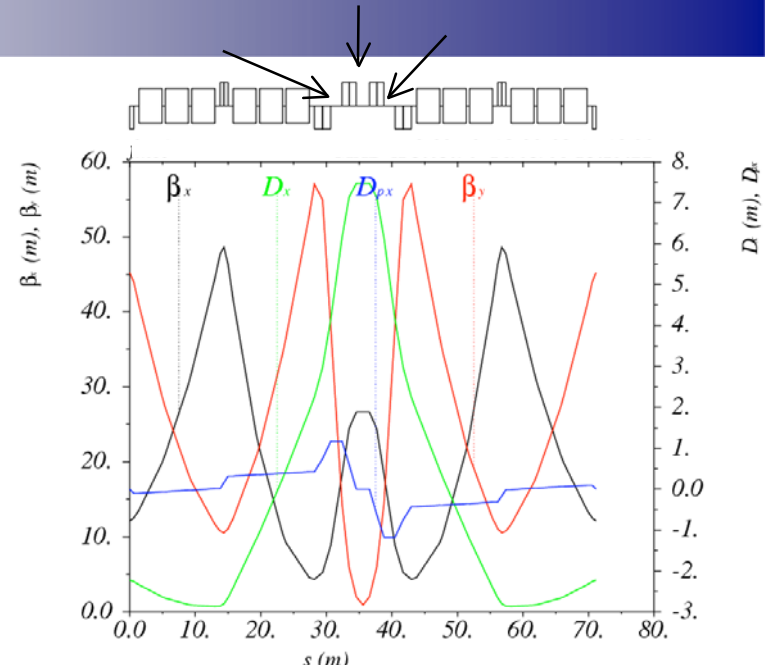
- γ_t of **19.8i**
- Tunes of **15.75** and **13.75**
- **180** dipoles, **3.3m** long
- **134** quadrupoles in **12** (+ **2**) families of **5** types with max. strength of **0.1m^{-2}**
- Max. beta of **51m** in horizontal and **54m** in the vertical plane
- Dispersion min. of **-1.5m** and max. of **5.7m**
- Chromaticities of **-21** and **-31**
- Total length of **1346.4m**

The NMC with dispersion suppressor ring Ib



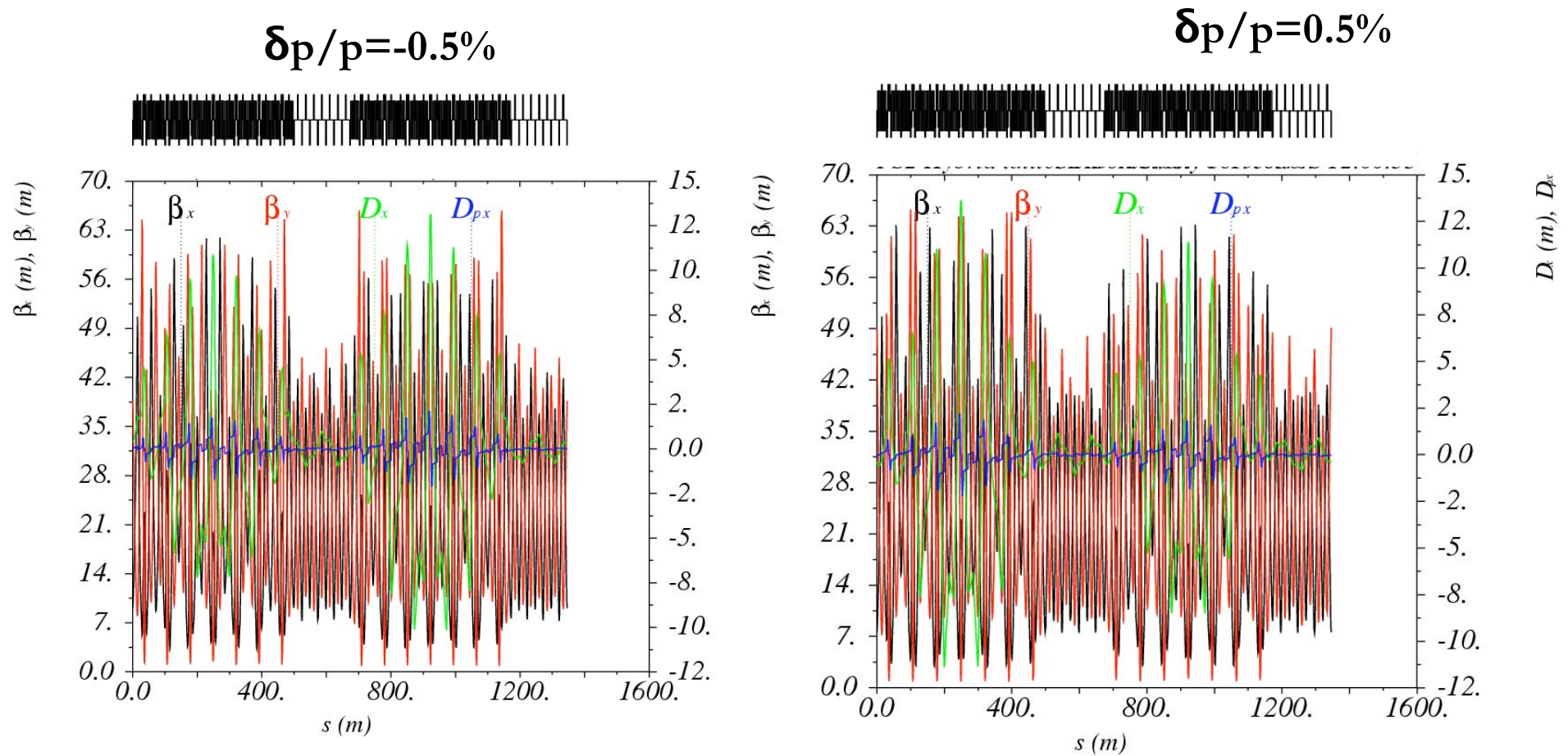
Chromaticity correction

- Same approach for all three lattice types
- Sextupoles of 0.4m long placed in the low beta doublet
- In principle 2 families needed for chromaticity correction
- Second-order chromaticity and off-momentum β -beating not corrected



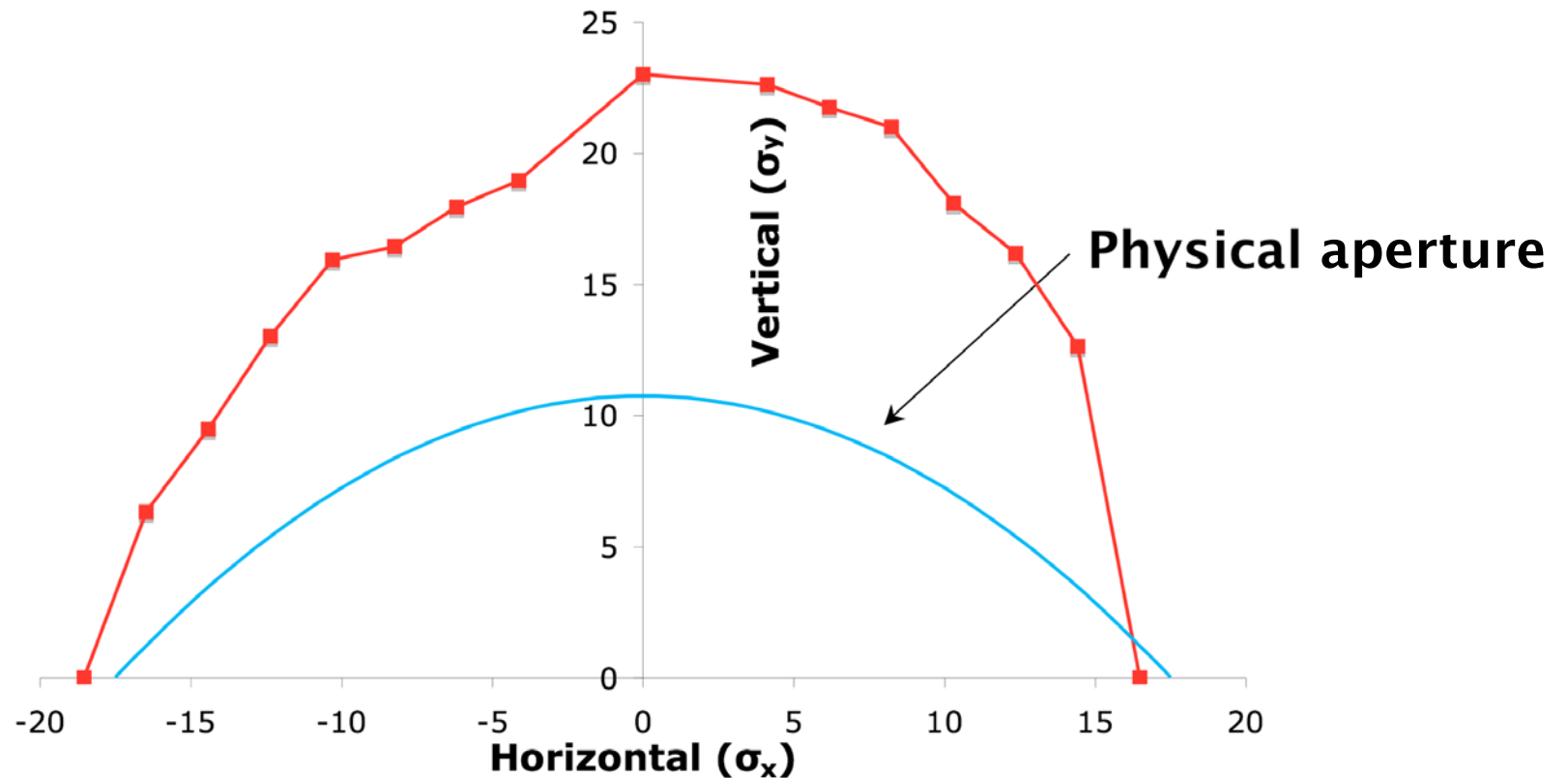
Chromaticity correction

- Using 8 sextupole families to minimize 2nd order chromaticity and off-momentum beta variation in both planes



Dynamic aperture (preliminary)

- On momentum tracking using SIXTRACK for the hybrid lattice
- Only non-linearity included: chromaticity sextupoles
- Large vertical and slightly smaller horizontal DA
- Tune optimization necessary



Comparison

Parameters	NMC with DS RING Ia	NMC with DS RING Ib	NMC resonant RING II	NMC hybrid RING III
Transition energy	10.9i	19.8i	10.7i	11i
Number of dipoles	176	180	192	168
Dipole length [m]	3.4	3.3	3.1	3.5
Arc module length [m]	68.3	67.3	64.8	71.2
Number of arc modules	6+2	6+2	8	7
Arc length [m]	517	517	518	500
Straight section drift length [m]	9	9	9.4	10.2
Quadrupole families	11	12	6	8
Arc phase advance [2π]	6.7/5.7	6.2/5.5	7/6	5.7/6.1
Max. beta functions [m]	60/57	51/54	61/61	60/60
Max. dispersion function [m]	8.8	5.7	8.9	12
Tunes	16.75/14.2	15.75/13.75	16.8/9.8	14.8/15.2
Chromaticity	-24.1/-32.1	-20.6/-30.9	-21.7/-19.8	-21.6/-32.2



Conclusions

- Thorough optics design of several NMC modules with low imaginary transition energy
 - NMC with dispersion suppressor is my **preferred** solution
 - NMC hybrid ring a good **alternative**
 - NMC resonant ring has **limited tunability**
- Relaxing the transition energy constraint (to around **20i**) is an advantage:
 - Reduces the optics functions maxima (less chromaticity, more aperture)
 - Leaves margin for tuning and operational flexibility
 - For example, the J-PARC high energy ring lattice is tuned for a transition energy of **30i**
- Lattice choice based on detailed comparison of performance with respect to beam losses
 - Collimation system, non-linear dynamics, collective effects