



# CHIPS improvement of Elastic Scattering in Geant4

Mikhail Kosov, Lisbon, 2006



# Plan

- Neutron-proton elastic scattering
  - Elastic and low energy inelastic np reactions
  - Comparison with **G4LElastic** and **SAID (G4Lnp)**
- Proton-proton elastic scattering
  - Energy dependence of reaction cross-sections
  - Differential cross-sections (+ electromagnetic)
  - Comparison with **G4LElastic** and **SAID (G4Lpp)**
- Proton-nuclear elastic scattering
  - Comparison with **G4LElastic/G4HadronElastic**



# CHIPS improvement of nH elastic

## ■ Importance of nH elastic scattering

- Scintillation detectors in High Energy Physics
- Hydrogen as an element of water for medicine

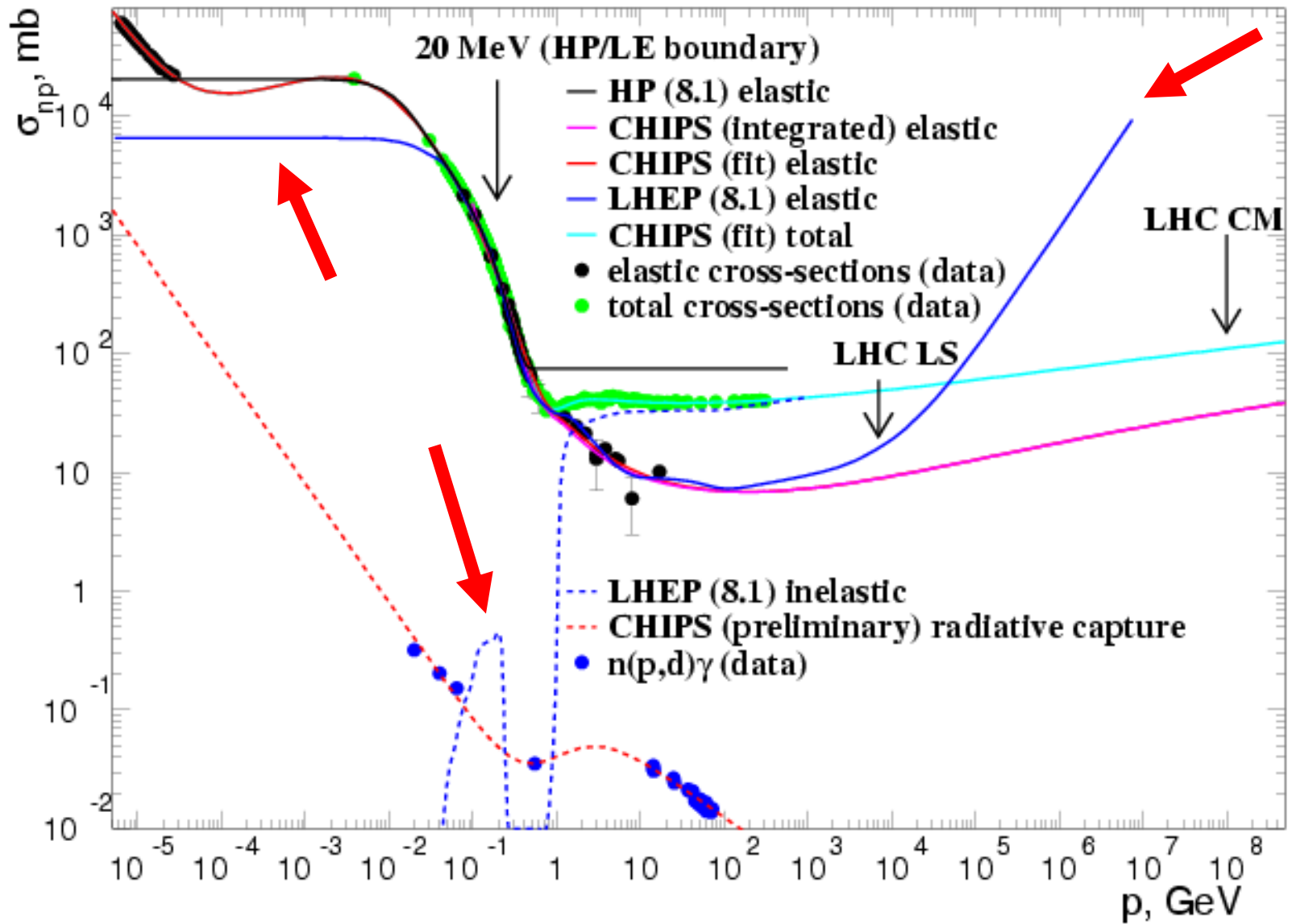
## ■ nH interaction at low energies

- Large elastic scattering with charge exchange
- Binary  $n(p,d)\gamma$  reaction (radiative capture)
- Hard bremsstrahlung of neutrons:  $n(p,np)\gamma$

## ■ High Energy: elastic is $\sim 15\%$ of inelastic

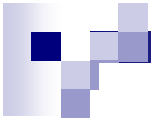
- Weak energy dependence of parameters

### CHIPS improvement of neutron-proton interaction

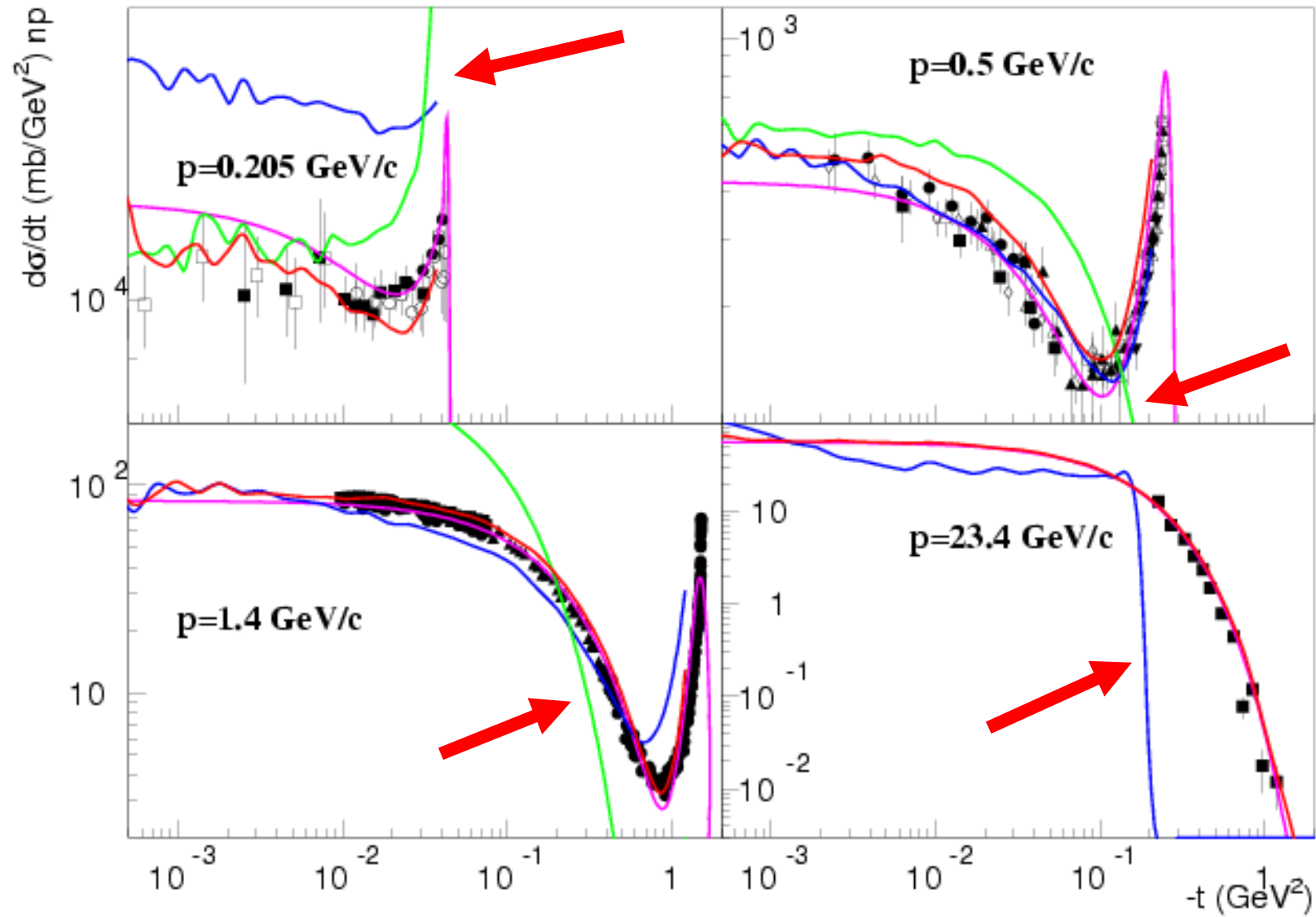


# CHIPS approximation of nH elastic

- Approximation formula for differential cross-section:  $d\sigma/dt = A(p)e^{B(p)t} + C(p)e^{D(p)u}$
- Contributing processes:
  - A(p) includes  $\pi^0$  and Pomeron exchange
  - C(p) includes  $\pi^-$  exchange (small at high E)
- CHIPS (pink lines are approximation, red lines are simulation) compared with
  - G4LElastic (8.1) process (green lines)
  - SAID (PWA) Geant4 version G4Lnp (blue lines)



### CHIPS improvement of np elastic scattering





# CHIPS improvement of pH elastic

## ■ Importance of pH elastic scattering

- Breeding of protons in scintillation detectors (plastic cancer in High Energy Physics)
- Lateral widening of proton's Bragg peak in water

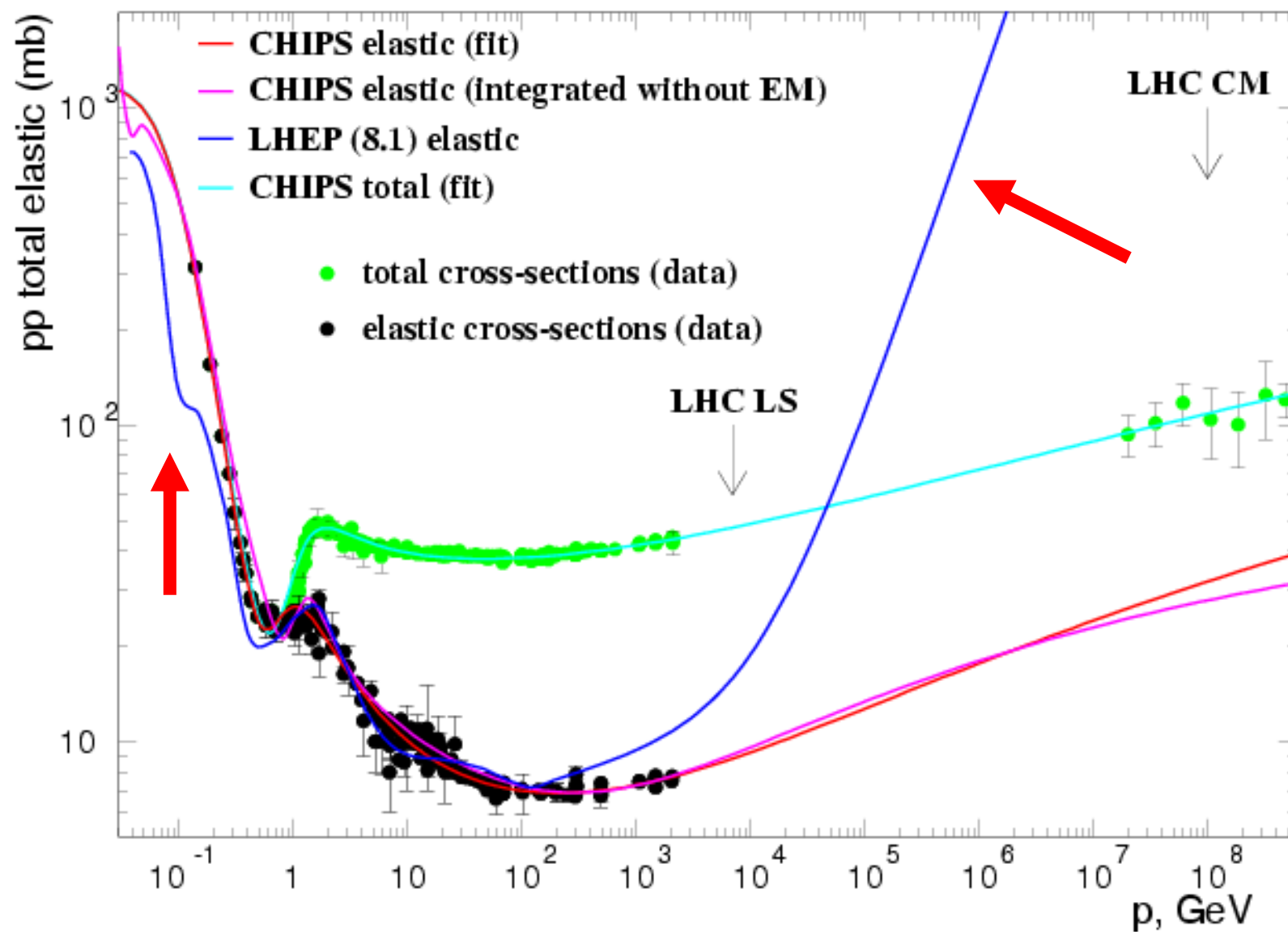
## ■ pH interaction at low energies

- There is no “HP” package for low energy protons
- CHIPS reaction cross section is too big and can make a calculation time problem (continuous?)

## ■ High Energy: elastic is $\sim 15\%$ of inelastic

- Weak energy dependence of parameters

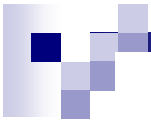
### CHIPS improvement of proton-proton interactions



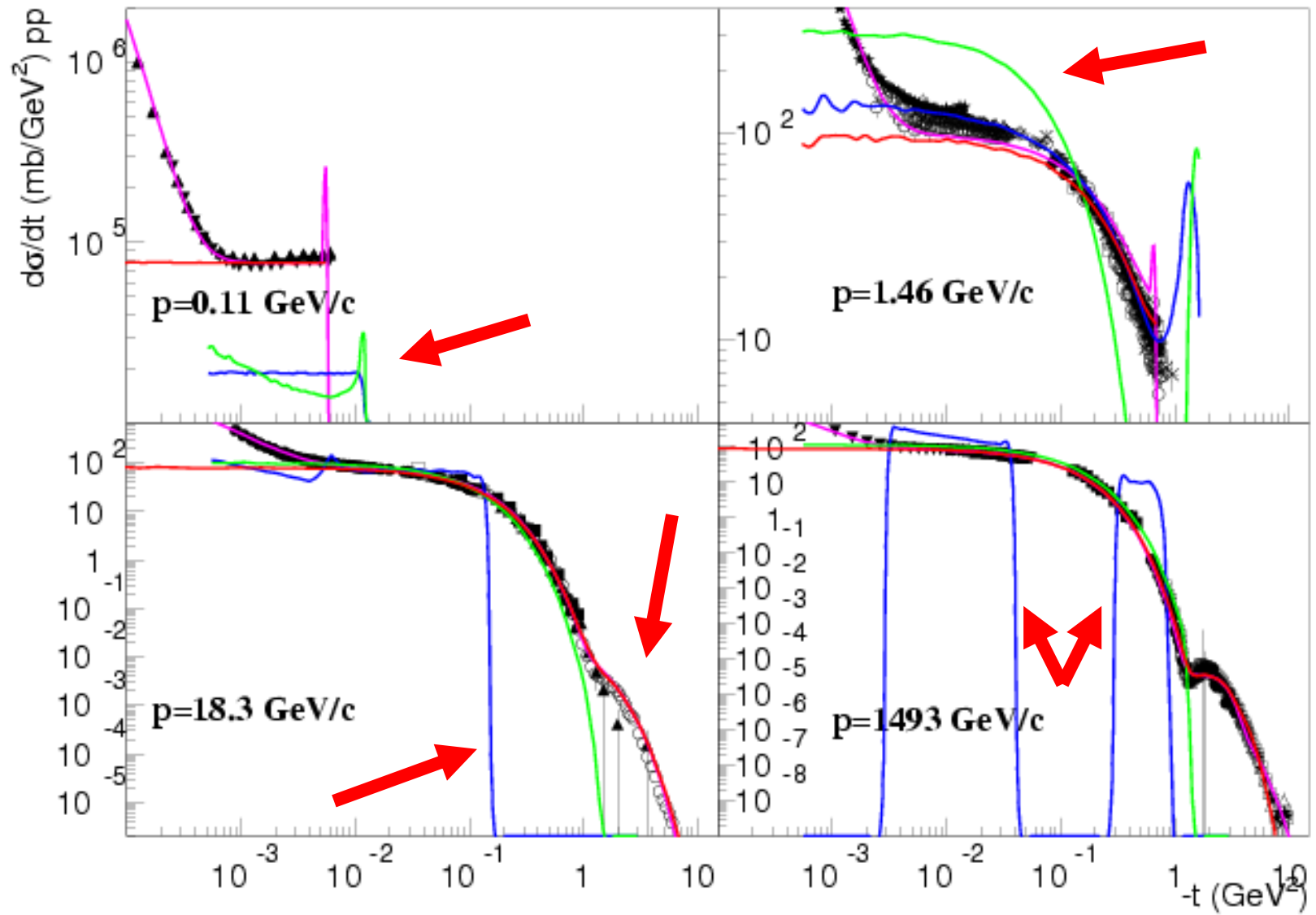


# CHIPS approximation of pH elastic

- Formula for differential cross-section ( $T=|t|^{n-1}$ ):  
$$ds/d|t|=E(p) \cdot e^{-F(p)\sqrt{|t|}} / \sqrt{|t|} + A(p) \cdot e^{B(p) \cdot t} + C(p) \cdot T \cdot e^{D(p) \cdot t \cdot T} + G(p) \cdot e^{H(p) \cdot t}$$
  - $E(p)$  is Electromagnetic pp scattering (EM below)
- Only  $\pi^0$  and Pomeron exchange
  - **Symmetric** in respect to  $90^\circ$  in center of mass
- CHIPS (**pink** lines are approximation, **red** lines are simulation) compared with
  - **G4LElastic** (8.1) process (**green** lines)
  - **SAID (PWA)** Geant4 version **G4Lpp** (**blue** lines)



### CHIPS improvement of pp elastic scattering



# CHIPS approximation of pA elastic

## ■ Formula for differential cross-section ( $T=t^2$ ):

- $A < 7$  (d,  $^3\text{He}$ ,  $^4\text{He}$ ,  $^6\text{Li}$ ) with **nuclear gloria**:

$$ds/d|t| = EM + N \cdot (B + 2C \cdot t) e^{t \cdot (B - C \cdot t)} + D \cdot T \cdot e^{H \cdot t \cdot T} + R \cdot e^{K \cdot t} + G \cdot e^{S \cdot u}$$

- $A > 6$  ( $^7\text{Li}$ , Be, C, Al, Cu, Sn, Pb) ( $V=t^4$ ,  $W=t^6$ )

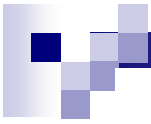
$$ds/d|t| = EM + N \cdot (B + 2C \cdot t) e^{t \cdot (B - C \cdot t)} + D \cdot V \cdot e^{H \cdot t \cdot V} + G \cdot W \cdot e^{S \cdot t \cdot W} + R \cdot e^{K \cdot t}$$

- **N, B, C, D, G, H, K, R, S** are functions of **p** and **A**

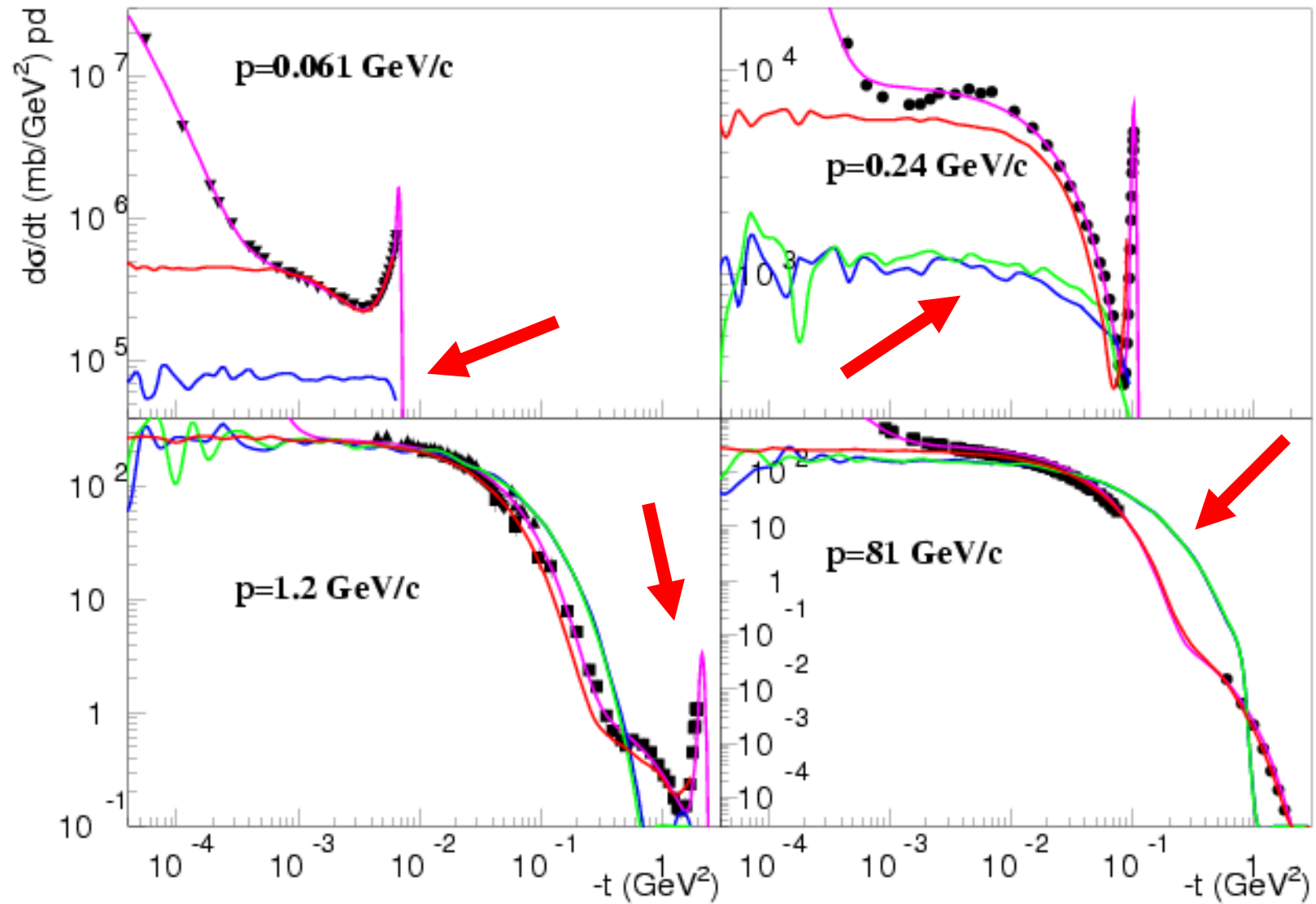
## ■ CHIPS (**pink** lines is approximation, **red** lines is old simulation – **d, $^4\text{He}$** ) compared with

- **G4LElastic** (8.1) process (**green** lines)

- **G4HadronElastic** (8.1-V.Ivanchenko) (**blue** lines)

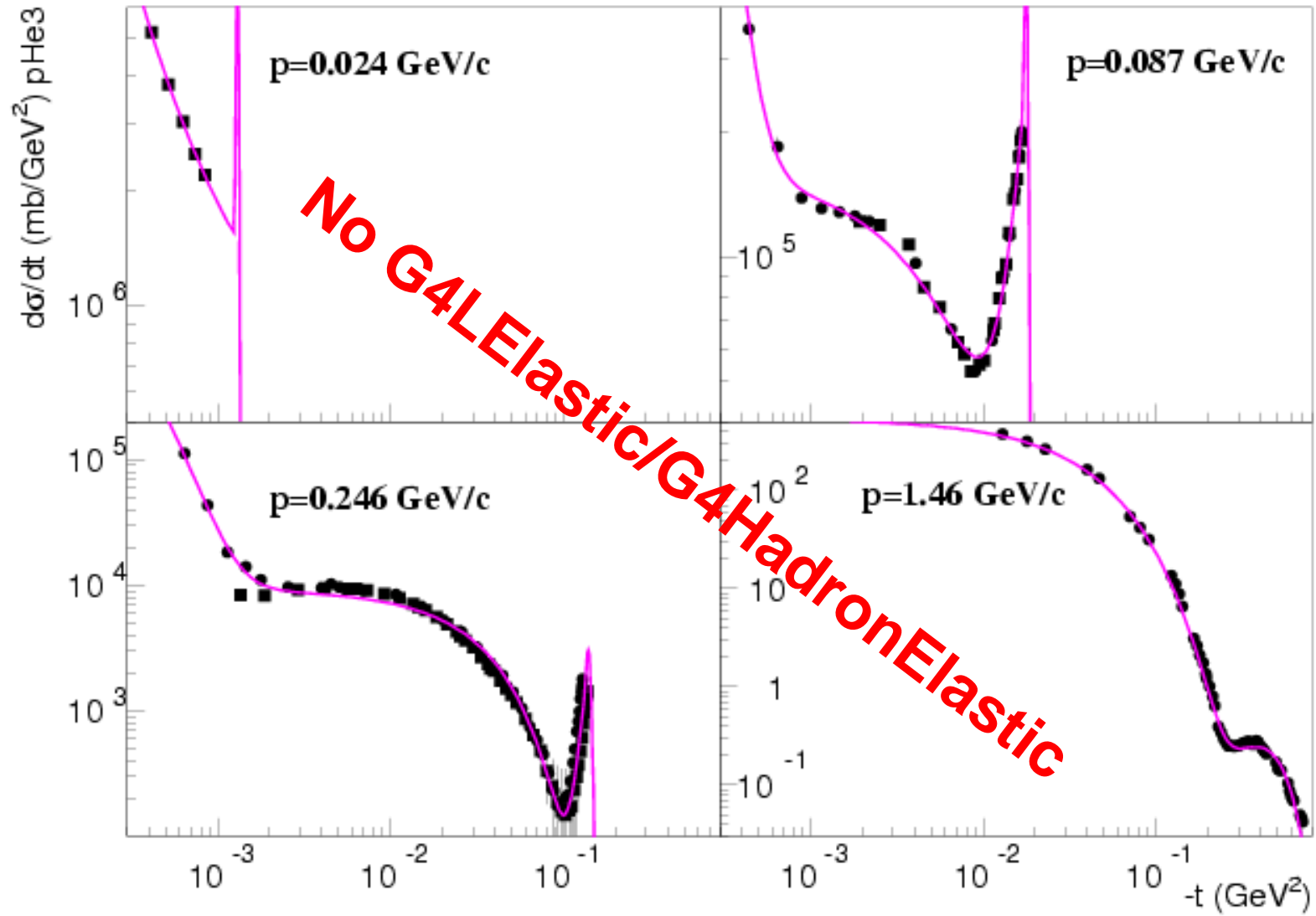


### CHIPS improvement of pd elastic scattering



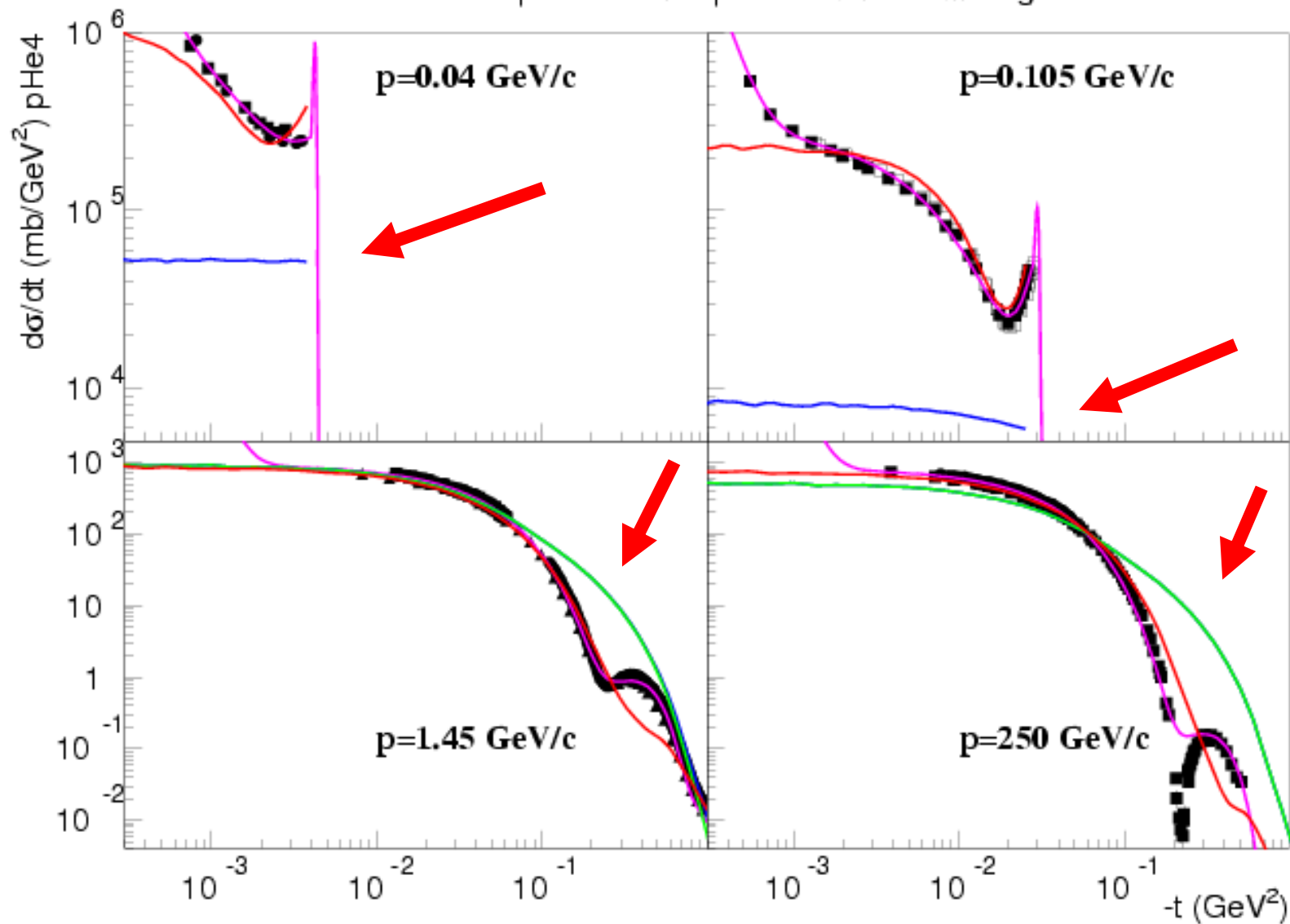


### CHIPS improvement of pHe3 elastic scattering

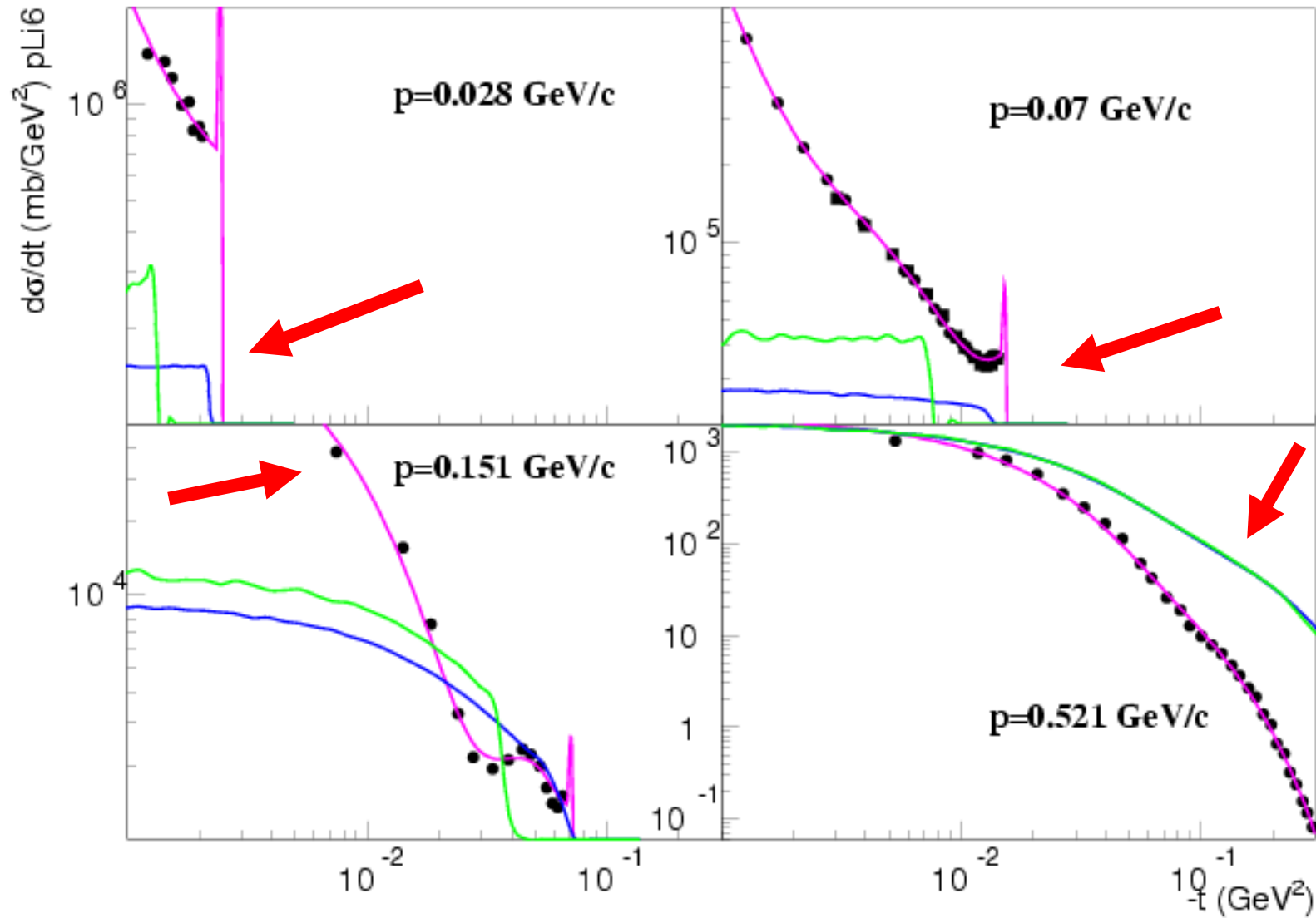




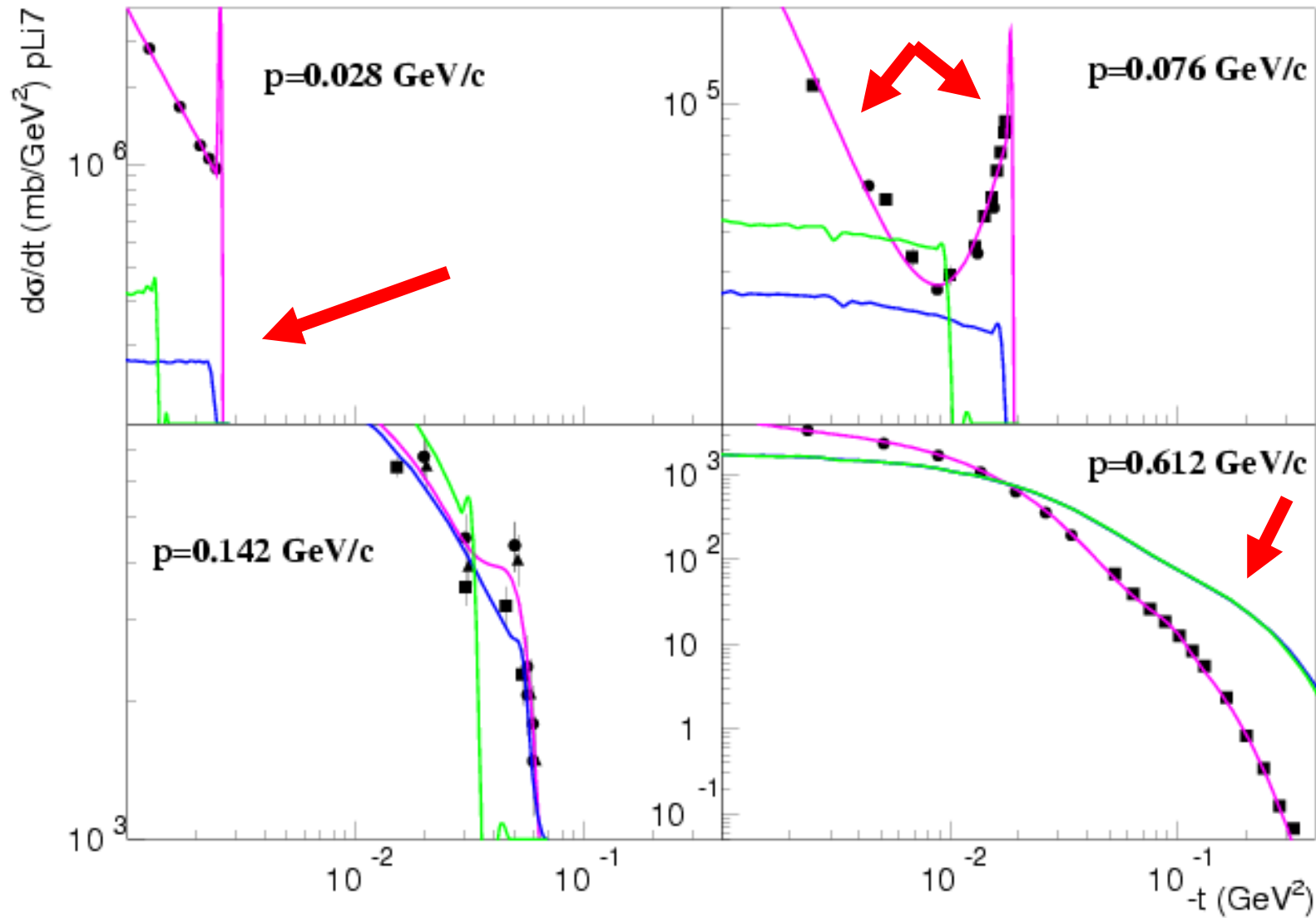
### CHIPS improvement of pHe4 elastic scattering



# CHIPS improvement of pLi6 elastic scattering

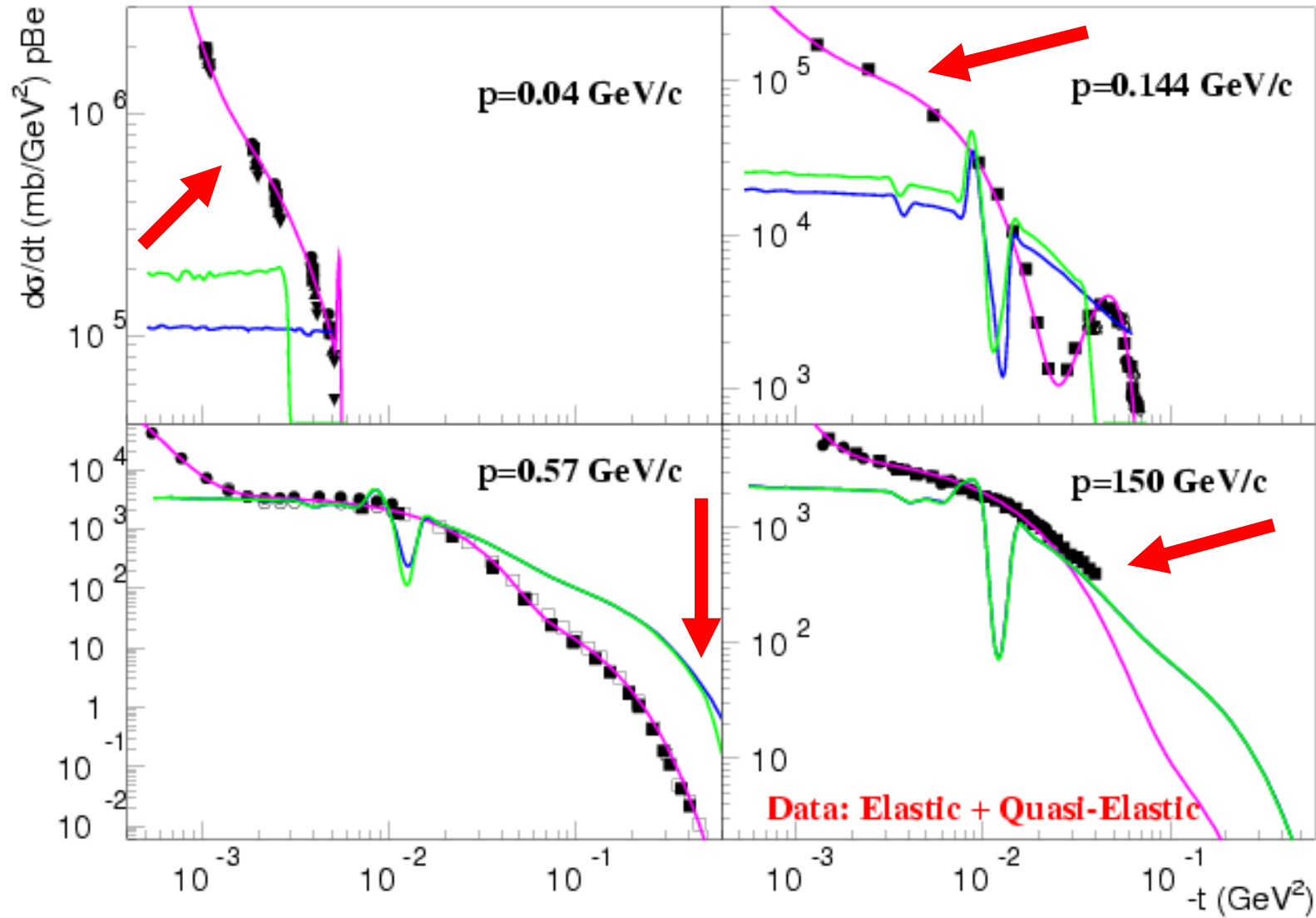


# CHIPS improvement of pLi7 elastic scattering

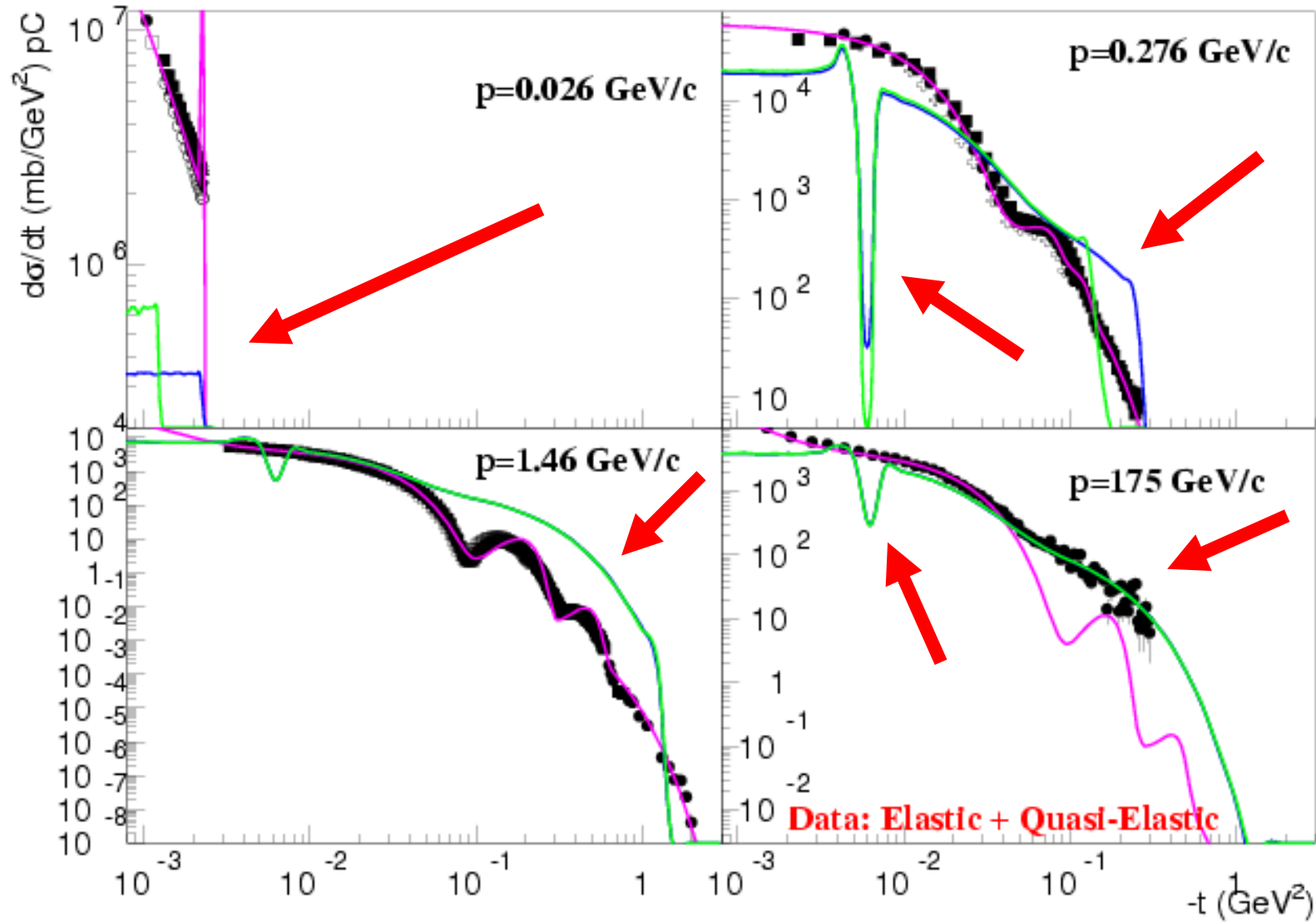




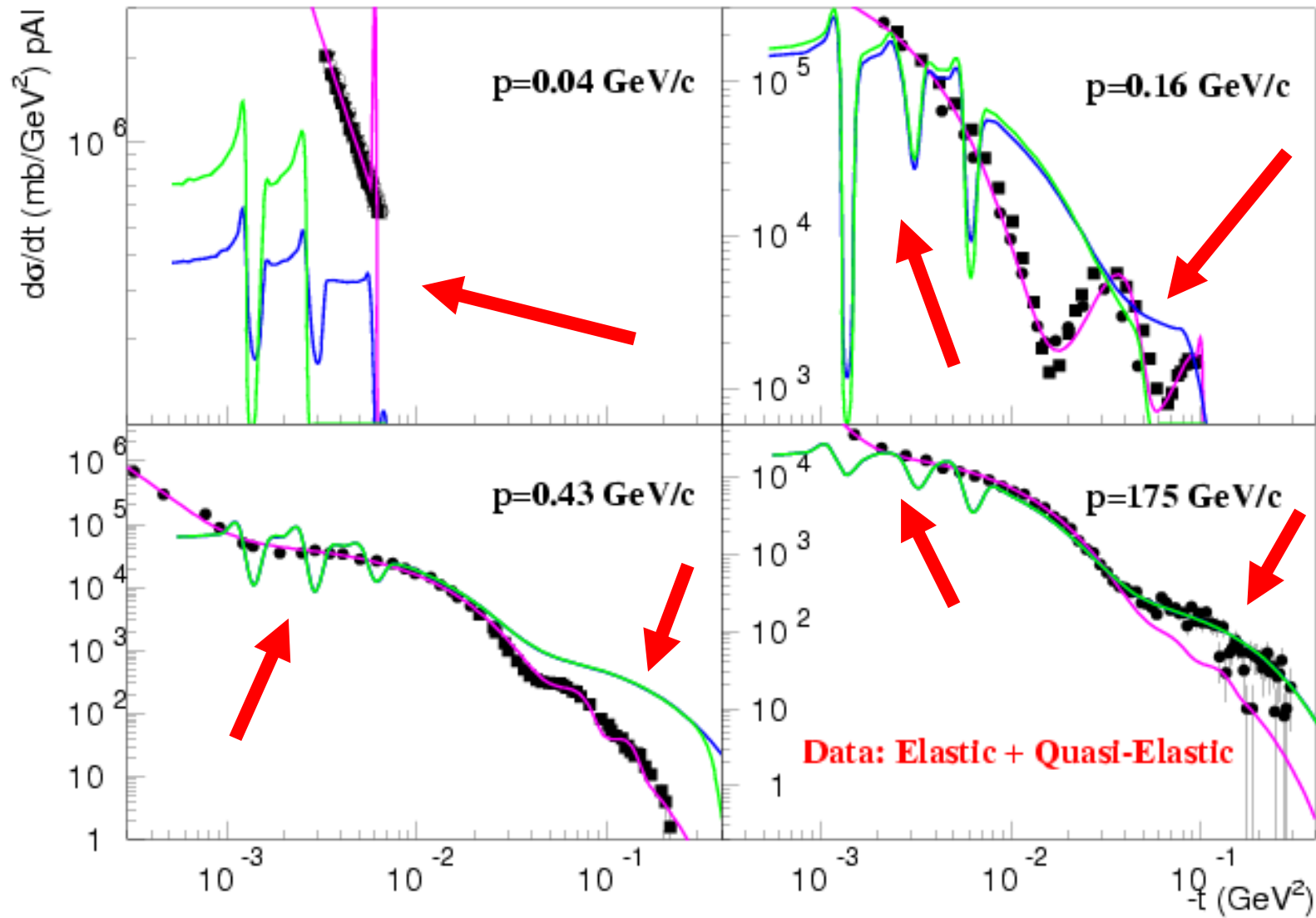
# CHIPS improvement of pBe elastic scattering



CHIPS improvement of pC elastic scattering

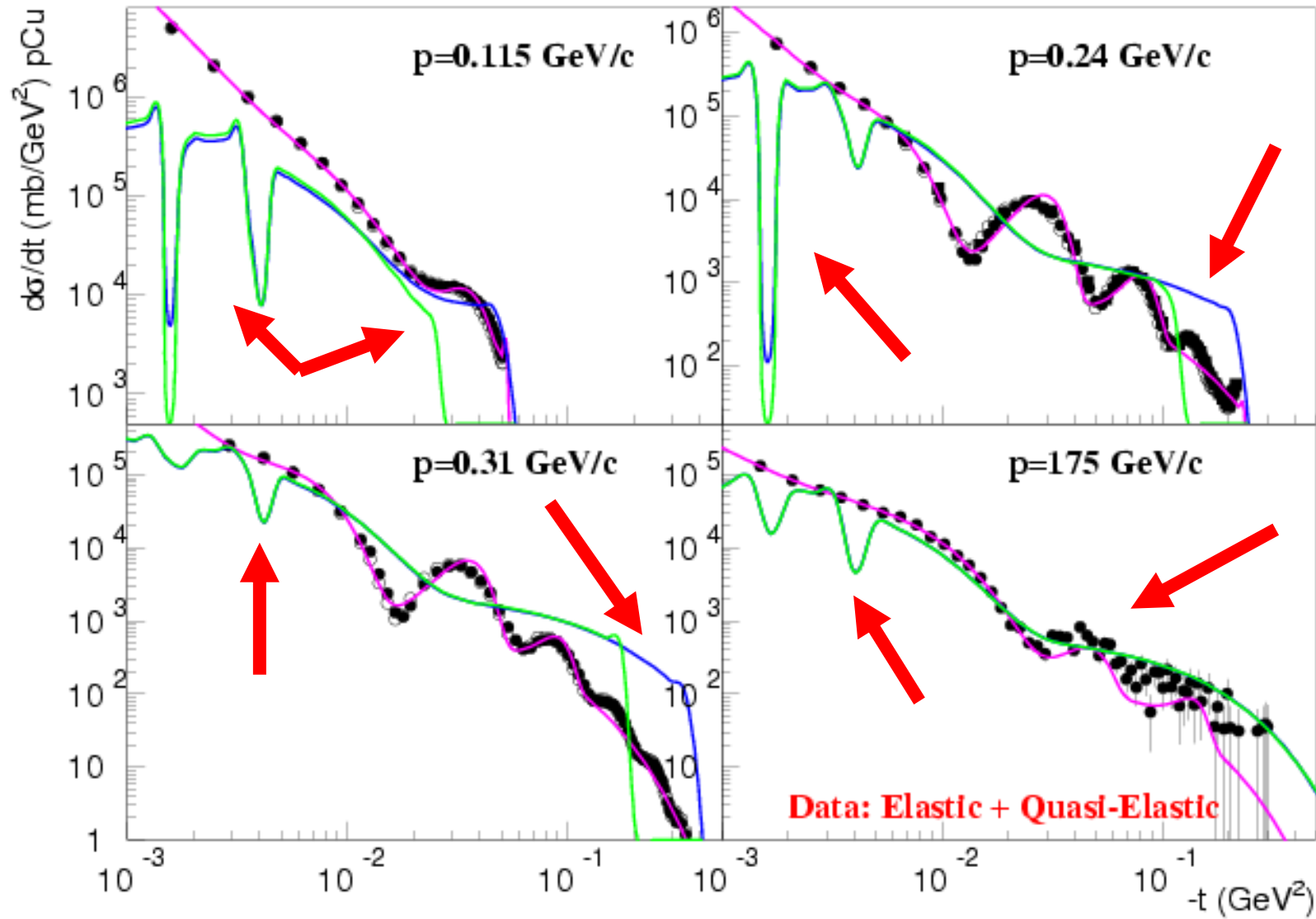


# CHIPS improvement of pAl elastic scattering

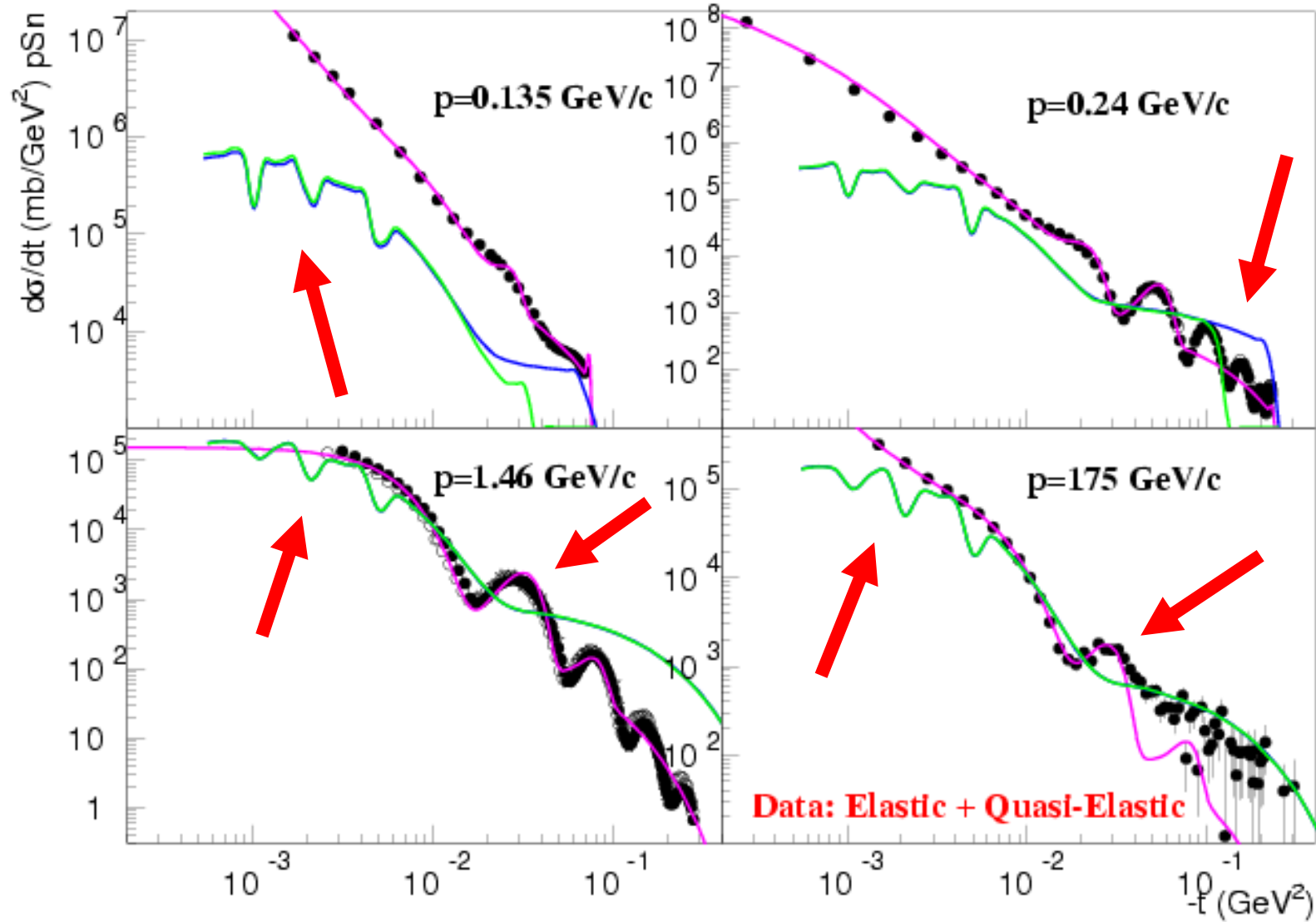




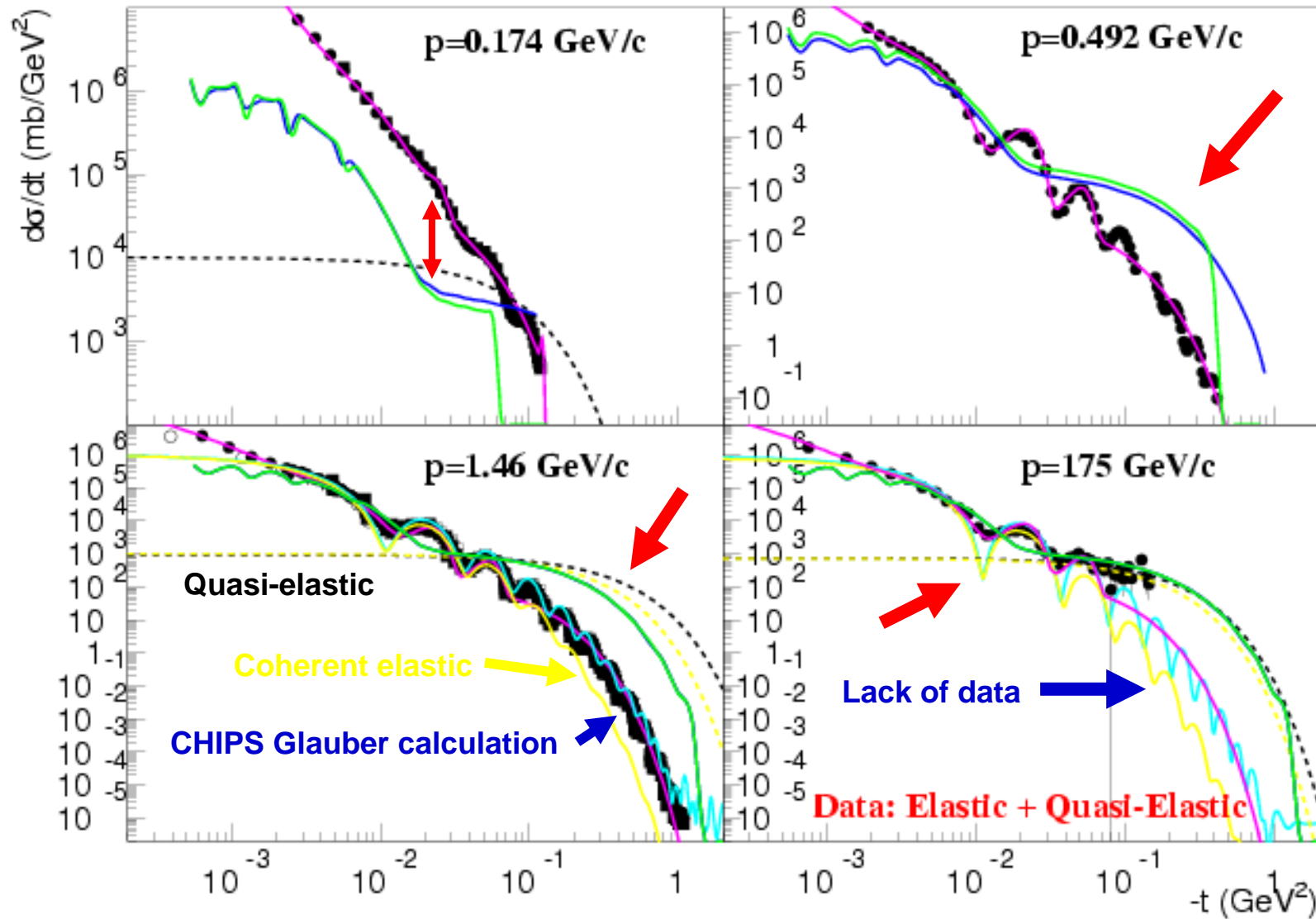
### CHIPS improvement of pCu elastic scattering



### CHIPS improvement of pSn elastic scattering



### CHIPS improvement of pPb elastic scattering



# Conclusion

## ■ Review of existing Geant4 elastic models

- **G4LElastic(8.1)** is used in LHEP (stops at  $90^\circ$  c.m. – nothing above)
  - bad at low energies ( $E < 30$  MeV) – bad reaction cross-sections
  - **double counting of quasi-elastic scattering at high energies**
  - no isotope dependency (**independent internal isotope choice**)
  - frequently 1 particles in final state, **no energy/momentum conservation**
- **G4HadronElastic(8.1)** (**G4QElastic** for np and pp) is used in QGSP
  - the same bad at low energies with arbitrary extrapolation to  $180^\circ$  c.m.
  - **redouble the double counting of quasi-elastic** (extend from  $90^\circ$  to  $180^\circ$ )
  - lets to make the isotope choice, but **does not have e.g.  $^3\text{He}$**  isotope
  - **produces 2 particles in final state and conserves energy/momentum**
- **G4np/G4pp (SAID)** **is not used in physics lists (only inside Binary)**
  - The same bad at low energies (because of the wrong reaction XS)
  - **Not applicable above 3 GeV** (drops down at  $|t| > 0.1$  GeV<sup>2</sup> etc.)
- **G4QElastic (CHIPS)** – good, but made only for np, pp, and pA now
- **G4ElasticHadrNucleusHE/G4ElasticCascadeInterface** don't work