

# Flavour Physics & CP Violation

## Lecture 4 of 4

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# Contents

- Part 1
  - What is flavour physics & why is it interesting?
- Part 2
  - What do we know from previous experiments?
- **Part 3**
  - **What do we hope to learn from current experiments?**
- **Part 4**
  - **The future of flavour physics**

# Strong CP?

- I've told you that the CKM matrix is the only source of CP violation in the Standard Model.
- Is this true? What is “the Standard Model”?

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## The SM

Input: Symmetries and fields

- Symmetry: 4d Poincare and

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

- Fields:

- 3 copies of QUDLE fermions

$$\begin{array}{lll} Q_L(3, 2)_{1/6} & U_R(3, 1)_{2/3} & D_R(3, 1)_{-1/3} \\ L_L(1, 2)_{-1/2} & E_R(1, 1)_{-1} & \end{array}$$

- One scalar

$$\phi(1, 2)_{+1/2}$$

## Then Nature is described by

Output: the most general  $\mathcal{L}$

$$\mathcal{L} = \mathcal{L}_{kin} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yukawa}$$

- The model can have SSB

$$\langle \phi \rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix} \Rightarrow SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$$

- This model has a  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$  accidental symmetry
- It has 18 parameters, and we measure them all by now
- We then made many tests and the SM basically passes almost all of them

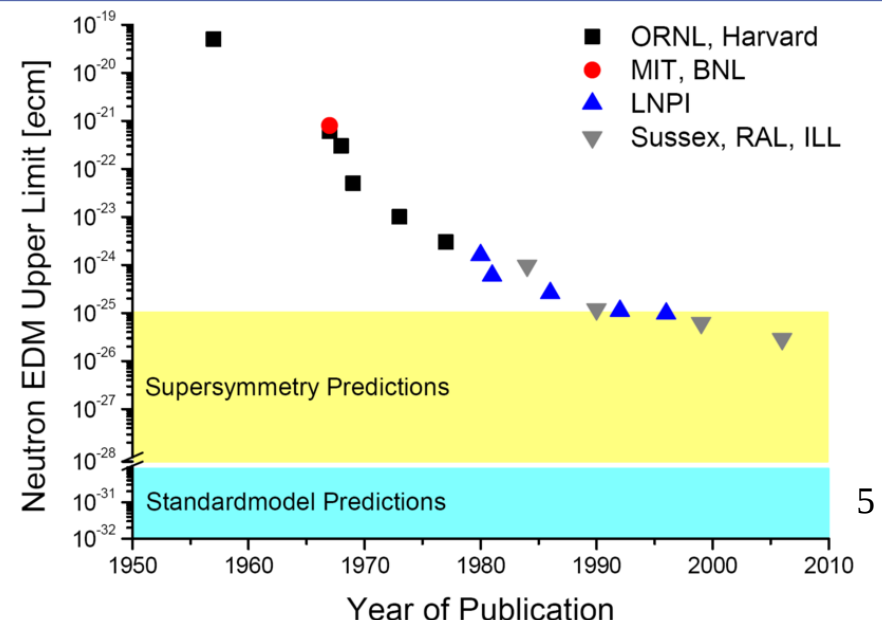
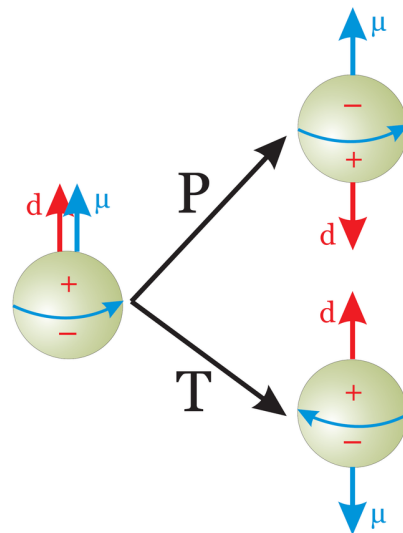
Then

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{n_f g^2 \theta}{32\pi^2} F_{\mu\nu} \tilde{F}^{\mu\nu} + \bar{\psi} (i\gamma^\mu D_\mu - m e^{i\theta' \gamma_5}) \psi$$

# Neutron electric dipole moment

- If the  $\theta_{\text{QCD}}$  parameter is  $\neq 0$ , there is CP violation in the strong interaction
  - observable neutron electric dipole moment
- But:  $|d_n| < 2.9 \times 10^{-26}$  e cm (PRL 97 (2006) 131801)

If neutron were the size of the earth, +/- charges separated by  $< 10$   $\mu\text{m}$

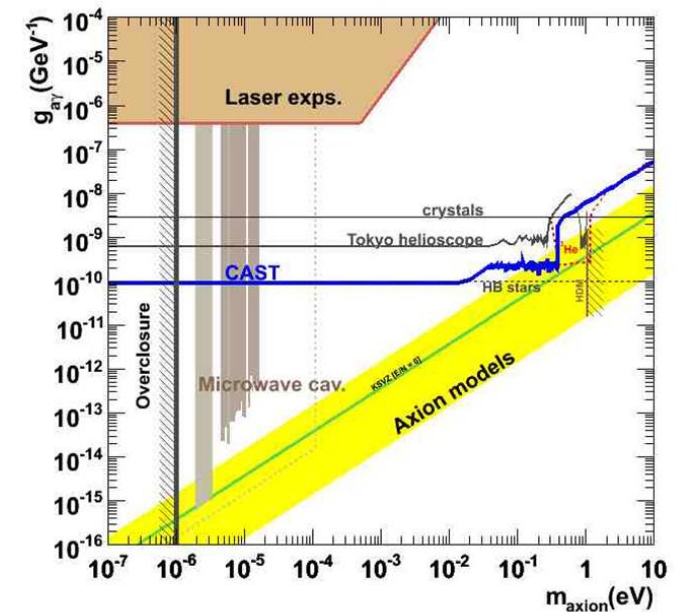


# The strong CP problem

- But:  $|d_n| < 2.9 \times 10^{-26}$  e cm (PRL 97 (2006) 131801)

- Corresponds to  $\theta_{\text{QCD}} < 10^{-9}$

- Why is it so small? Is it zero?
- Does some new symmetry forbid it?
- e.g. Peccei-Quinn theory
  - predicts the **axion**



- various experiments (e.g. CAST, PVLAS, ADMX) search for axions, which are also a potential dark matter candidate

# Precision physics with electric & magnetic moments

- Electric dipole moments are CP violating

- essentially zero in the SM, but can be much larger BSM with sources of flavour-conserving CPV

$$|d_e| < 8.7 \times 10^{-29} \text{ e cm [Science 343 (2014) 6168, 269]}$$

- Magnetic dipole moments are CP conserving

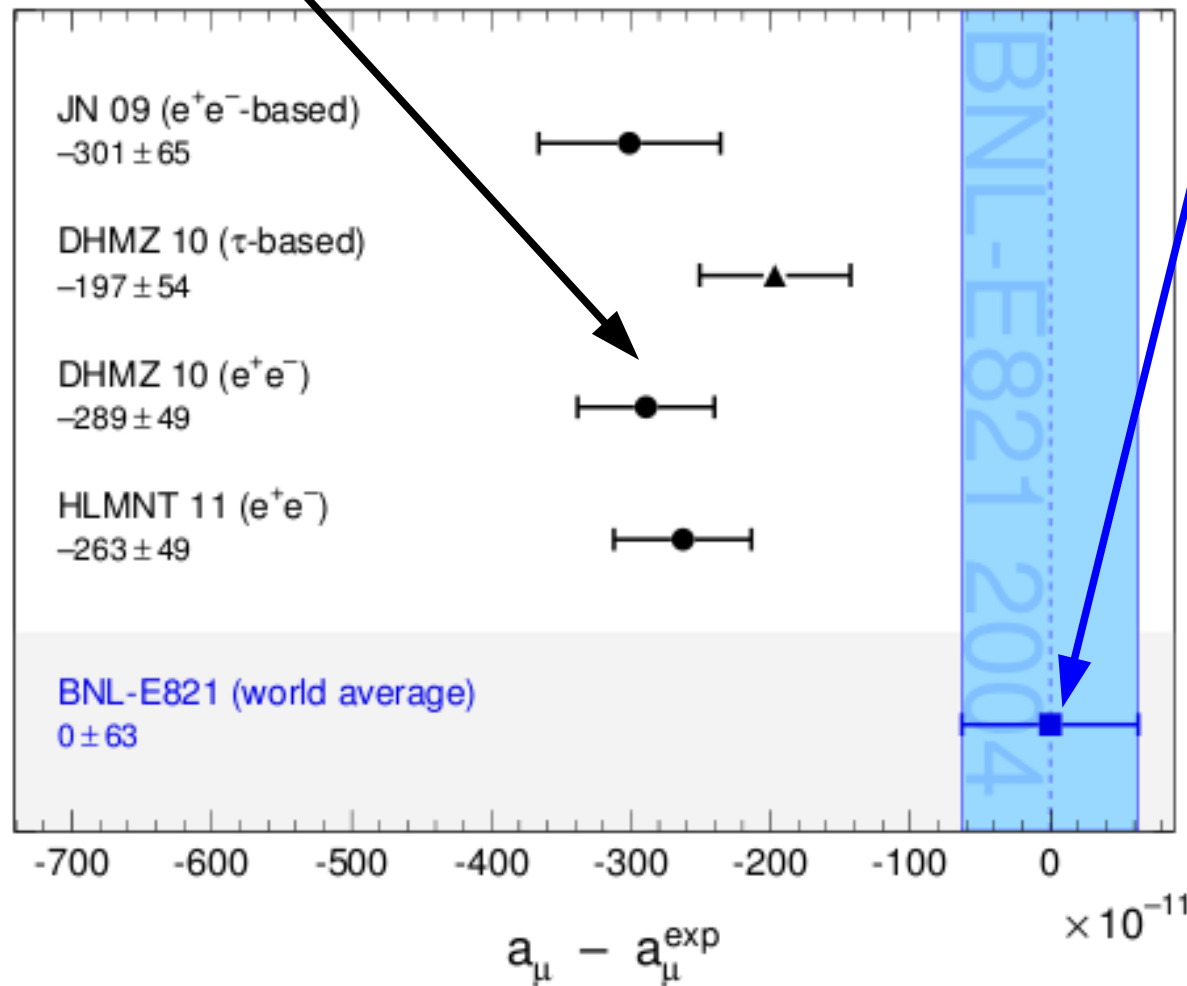
- sensitive to the structure of quantum fields

- Dirac predicted  $g_e = 2$  (RQM)
- Schwinger predicted  $a_e = (g_e - 2)/2 = 0.0011614$  (QED)
- $a_e$  now calculated to 10 loops in QED (PRL 109 (2012) 111807)
  - $a_e = 0.00115965218178$  (77)

$$(g-2)_\mu$$

Theory predictions

Experiment



New experiment at FNAL will reduce uncertainty by factor  $\sim 2$   
Improvements in theory uncertainties also anticipated



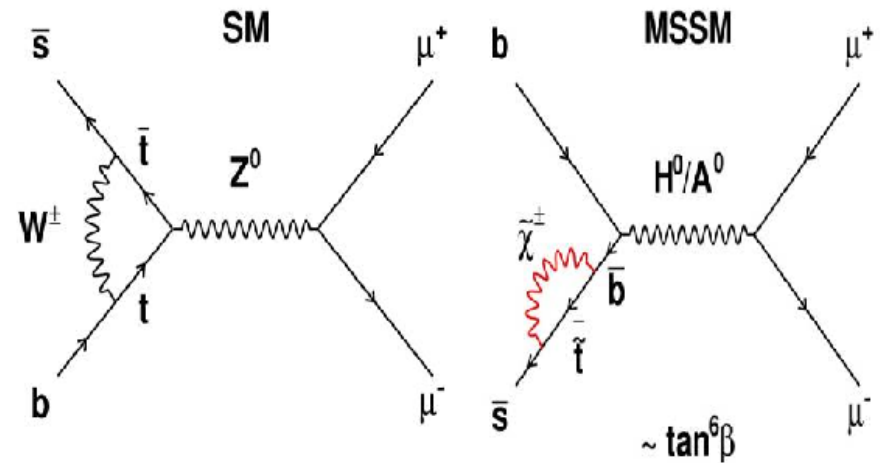
Back to B physics

# Rare Decays

$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

## Killer app. for new physics discovery

- Very small in the SM
  - no tree-level FCNC
  - CKM suppression
  - helicity suppression

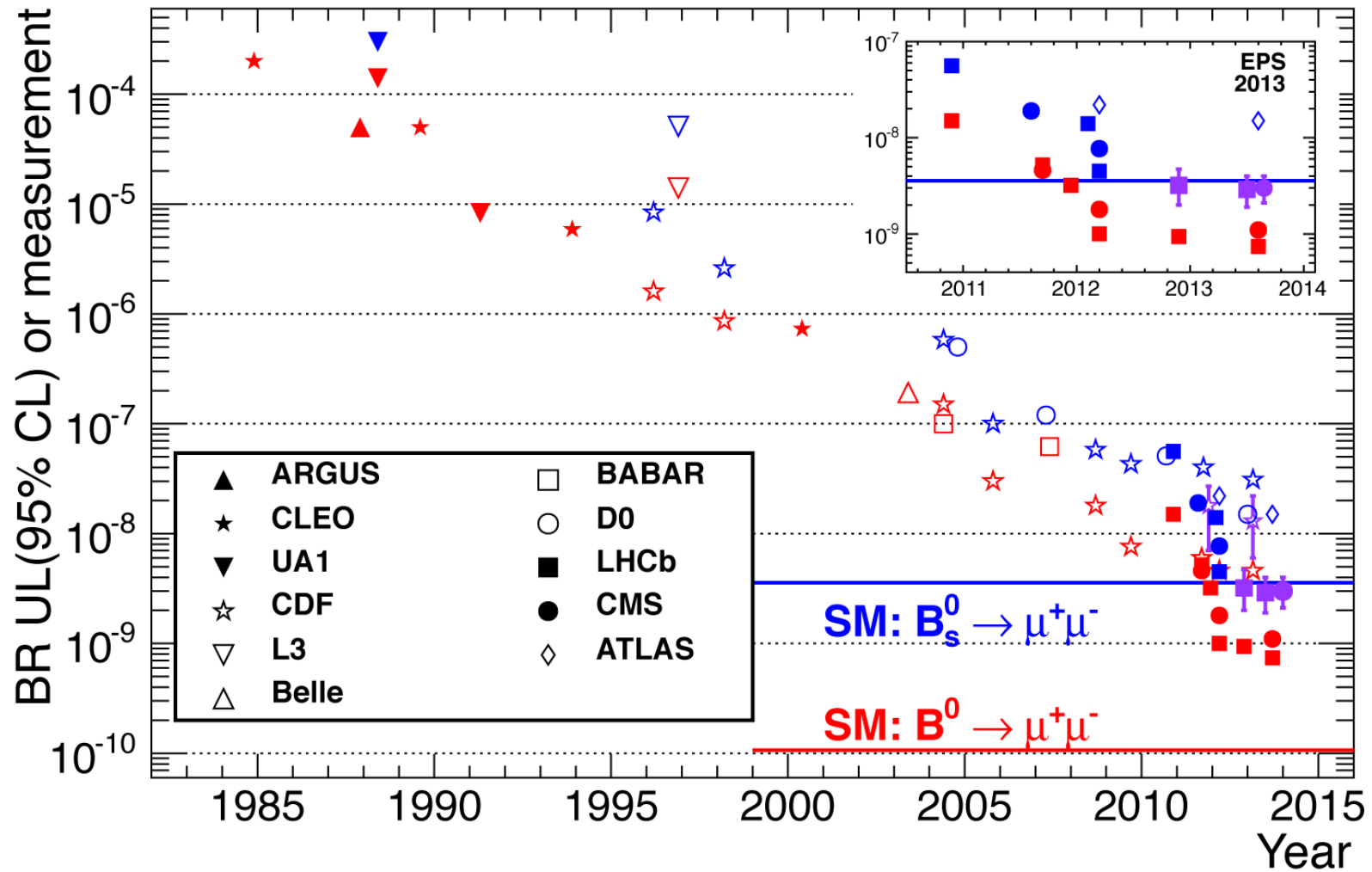


- Huge NP enhancement possible ( $\tan \beta =$  ratio of Higgs vevs)

$$BR(B_s \rightarrow \mu^+ \mu^-)^{SM} = (3.3 \pm 0.3) \times 10^{-9} \quad BR(B_s \rightarrow \mu^+ \mu^-)^{MSSM} \propto \tan^6 \beta / M_{A^0}^4$$

- Clean experimental signature

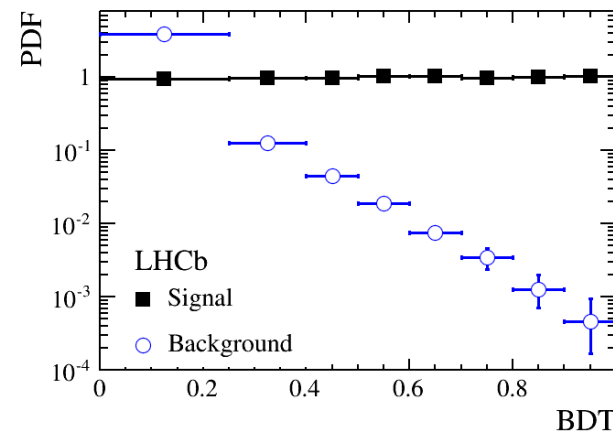
$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$



Searches over 30 years

# $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ – analysis ingredients

- Produce a very large sample of B mesons
- Trigger efficiently on dimuon signatures
- Reject background
  - excellent vertex resolution (identify displaced vertex)
  - excellent mass resolution (identify B peak)
    - also essential to resolve  $B^0$  from  $B_s^0$  decays
  - powerful muon identification (reject background from B decays with misidentified pions)
  - typical to combine various discriminating variables into a multivariate classifier
    - e.g. Boosted Decision Trees algorithm

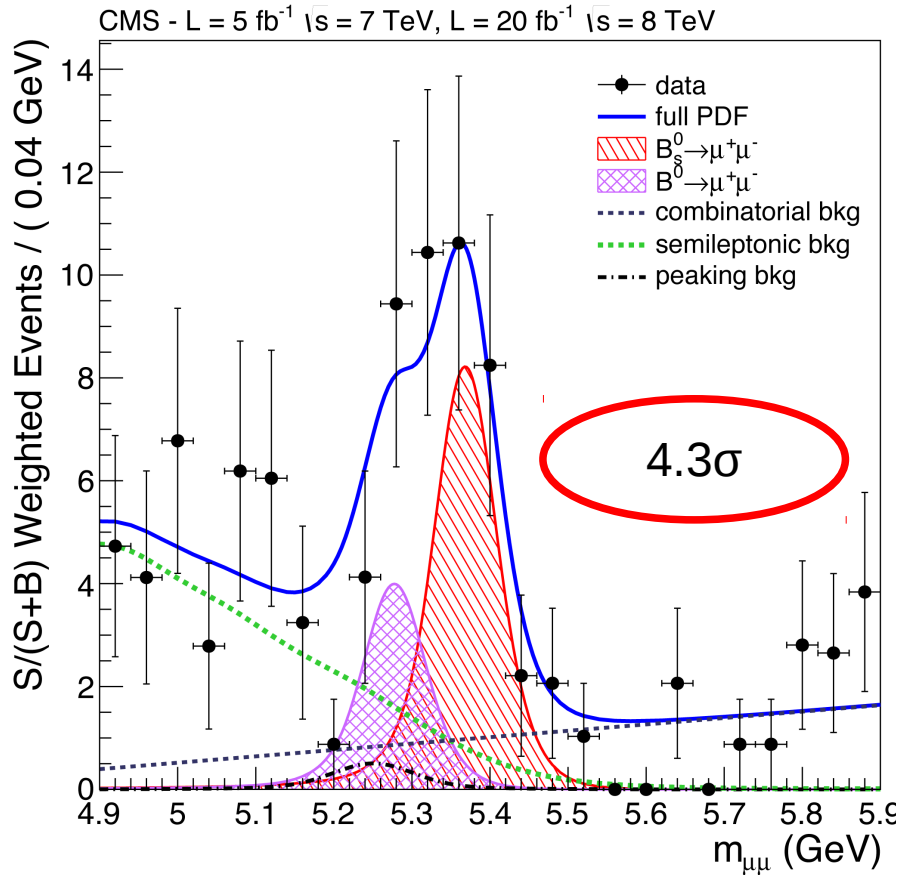


$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

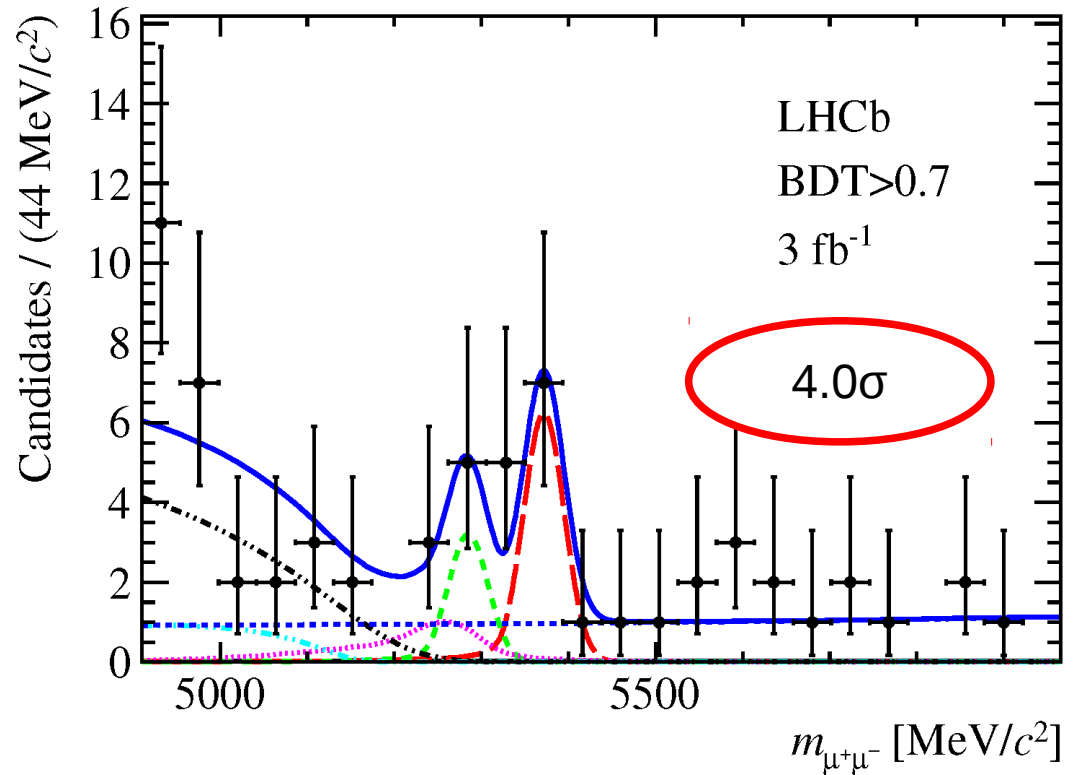
# latest results from CMS & LHCb

CMS PRL 111 (2013) 101804

LHCb PRL 111 (2013) 101805

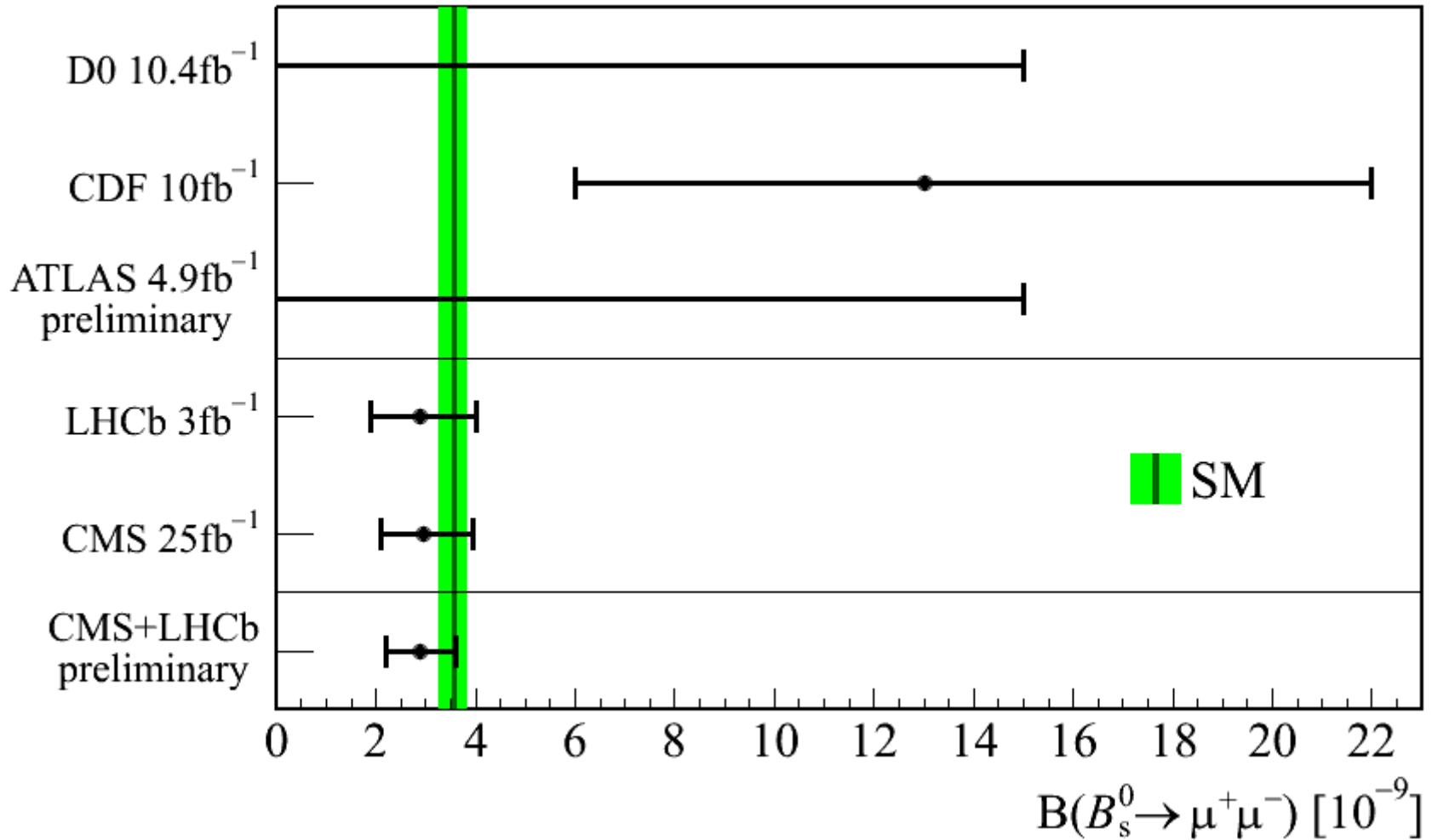


Events weighted by S/(S+B)



Only events with BDT > 0.7

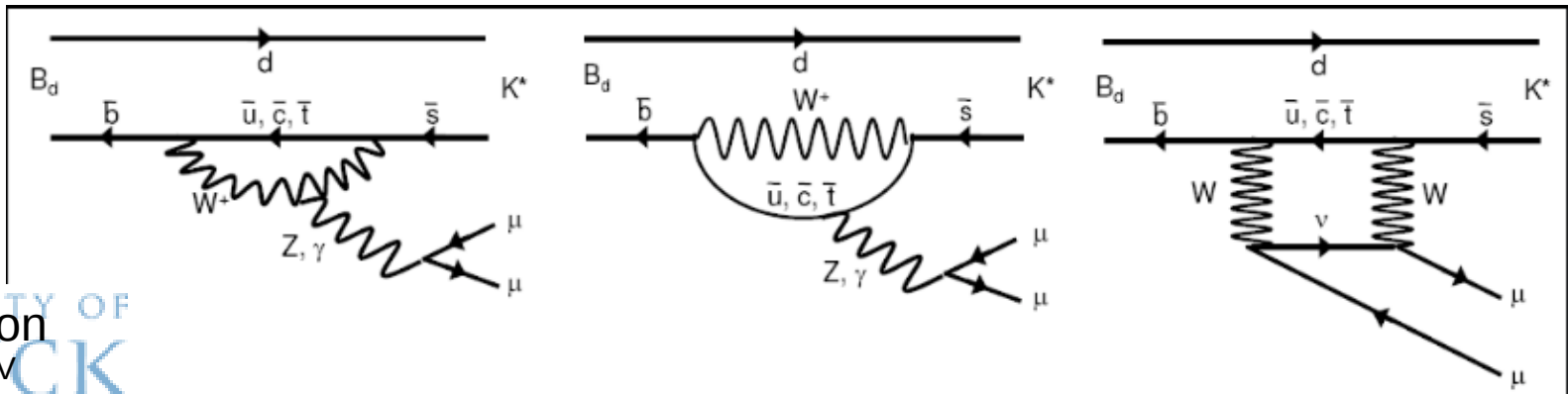
# $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ – combined results



$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7) \times 10^{-9}$$

$$B \rightarrow K^* \mu^+ \mu^-$$

- $b \rightarrow s l^+ l^-$  processes also governed by FCNCs
  - rates and asymmetries of many exclusive processes sensitive to NP
- Queen among them is  $B_d \rightarrow K^{*0} \mu^+ \mu^-$ 
  - superb laboratory for NP tests
  - **experimentally clean signature**
  - many kinematic variables ...
  - ... with clean theoretical predictions (at least at low  $q^2$ )



# Operator Product Expansion

Build an effective theory for b physics

- take the weak part of the SM
- integrate out the heavy fields (W,Z,t)
- (like a modern version of Fermi theory for weak interactions)

$$\mathcal{L}_{(\text{full EW} \times \text{QCD})} \longrightarrow \mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QED} \times \text{QCD}} \left( \begin{array}{l} \text{quarks } \neq t \\ \& \text{ leptons} \end{array} \right) + \sum_n C_n(\mu) Q_n$$

$Q_n$  - local interaction terms (operators),  $C_n$  - coupling constants (Wilson coefficients)

Wilson coefficients

- encode information on the weak scale
- are calculable and known in the SM (at least to leading order)
- are affected by new physics

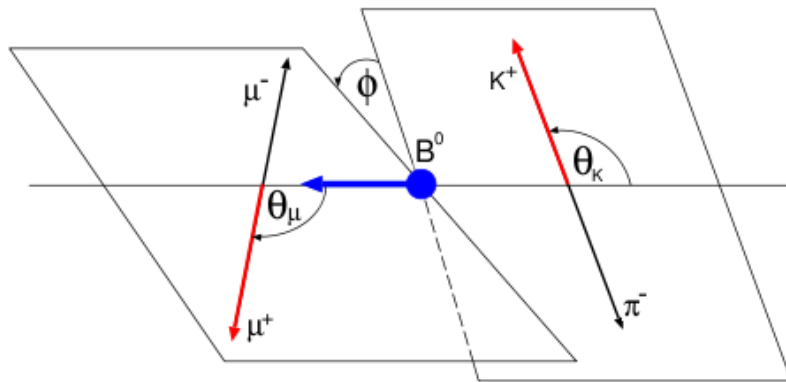
For  $K^* \mu \mu$  we care about  $C_7$  (also affects  $b \rightarrow s \gamma$ ),  $C_9$  and  $C_{10}$



# Theory of $B \rightarrow K^* \mu^+ \mu^-$

- Given for inclusive  $b \rightarrow s \mu^+ \mu^-$  for simplicity
  - physics of exclusive modes  $\approx$  same but equations are more complicated (involving form factors, etc.)
- Differential decay distribution

$$\frac{d^2\Gamma}{dq^2 d \cos \theta_l} = \frac{3}{8} \left[ (1 + \cos^2 \theta_l) H_T(q^2) + 2 \cos \theta_l H_A(q^2) + 2 (1 - \cos^2 \theta_l) H_L(q^2) \right]$$



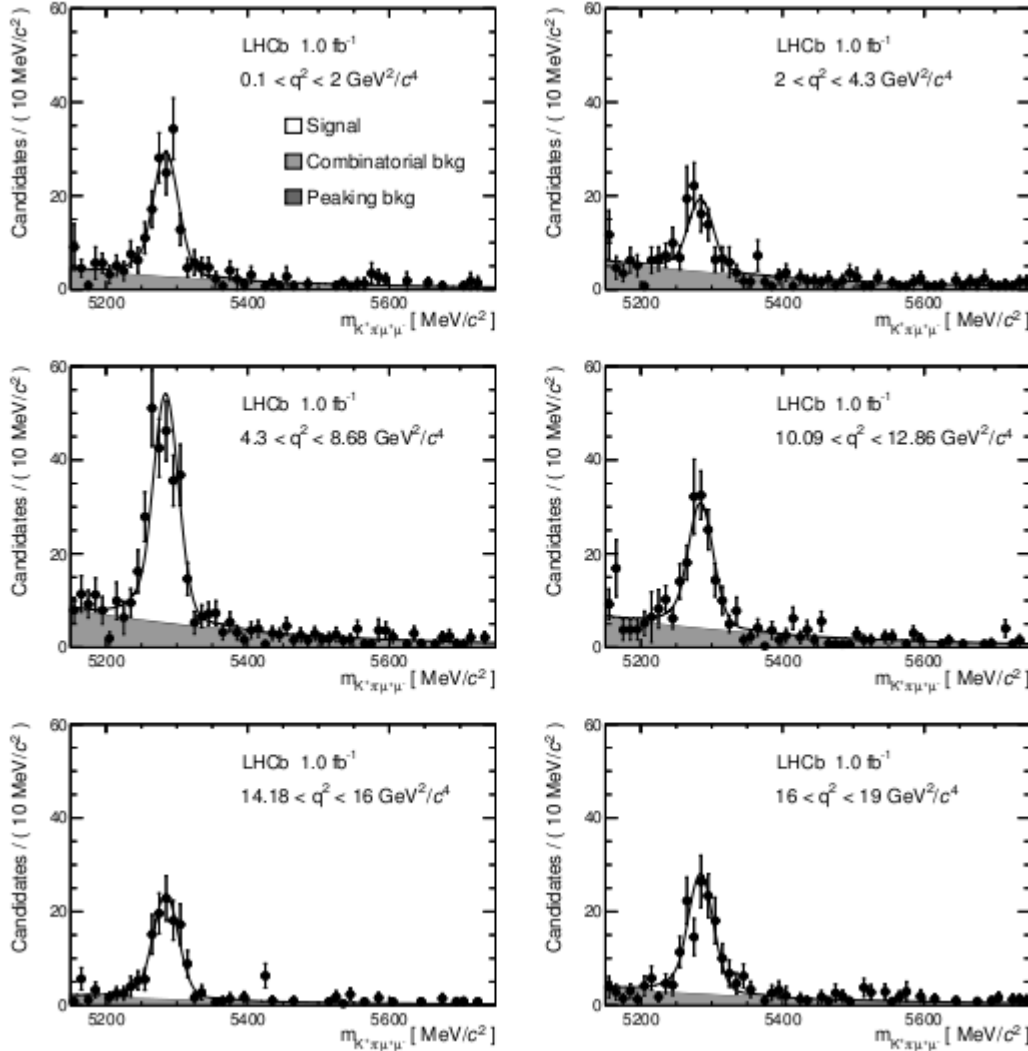
$$H_T(q^2) \propto 2q^2 \left[ \left( C_9 + 2C_7 \frac{m_b^2}{q^2} \right)^2 + C_{10}^2 \right],$$

$$H_A(q^2) \propto -4q^2 C_{10} \left( C_9 + 2C_7 \frac{m_b^2}{q^2} \right),$$

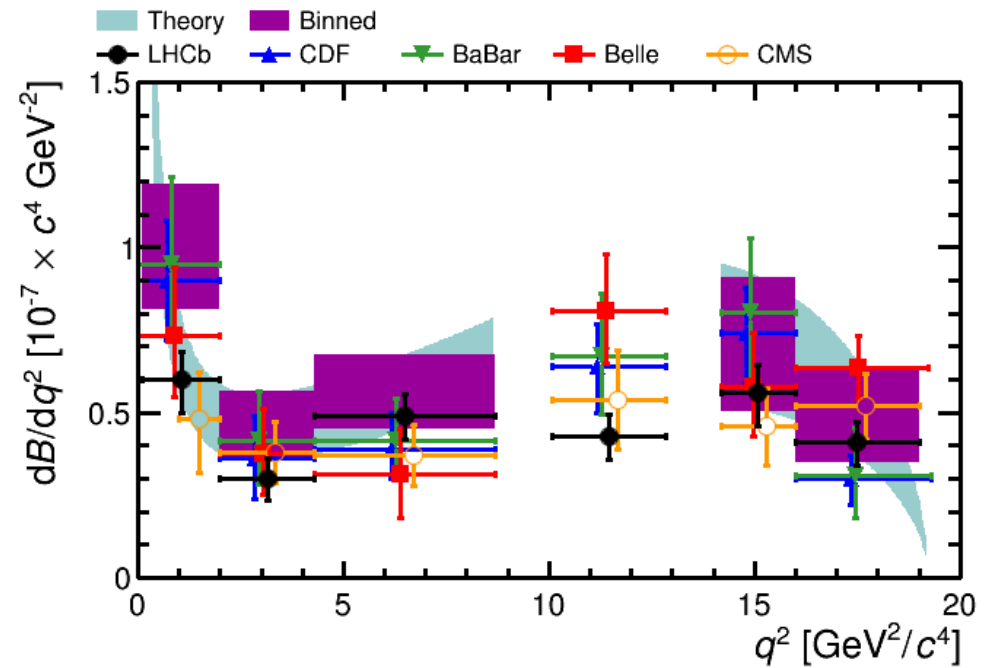
$$H_L(q^2) \propto \left[ (C_9 + 2C_7)^2 + C_{10}^2 \right].$$

This term gives a forward-backward asymmetry

# Angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



LHCb JHEP 08 (2013) 131  
 See also CDF PRL 108 (2012) 081807,  
 BaBar PRD 86 (2012) 032012,  
 Belle PRL 103 (2009) 171801,  
 ATLAS-CONF-2013-038 &  
 CMS PLB 727 (2013) 77

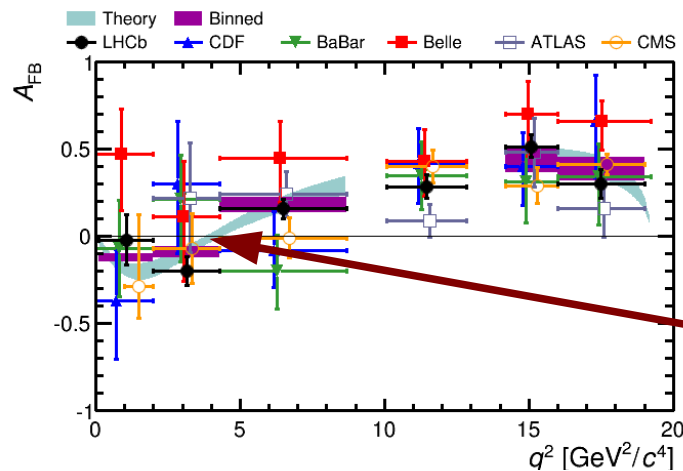
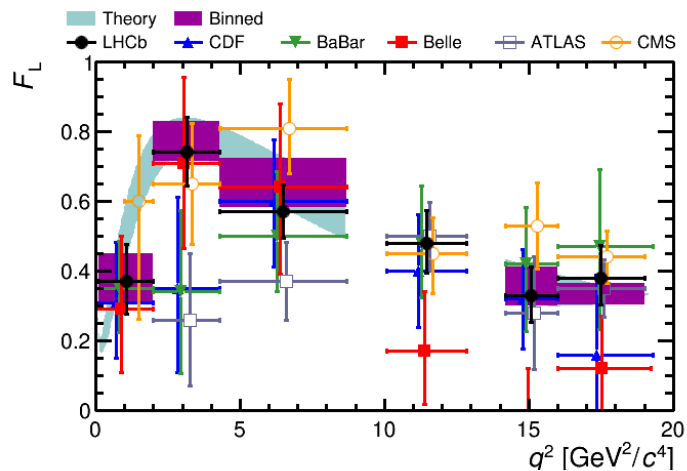


Analysis performed in bins of dimuon  
 invariant mass squared ( $q^2$ )

# Angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

LHCb JHEP 08 (2013) 131

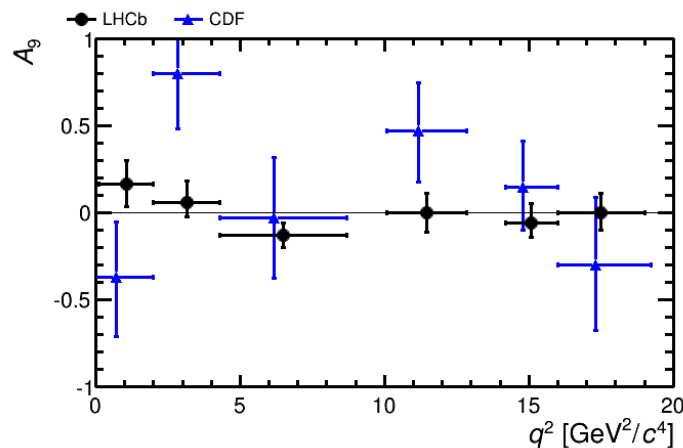
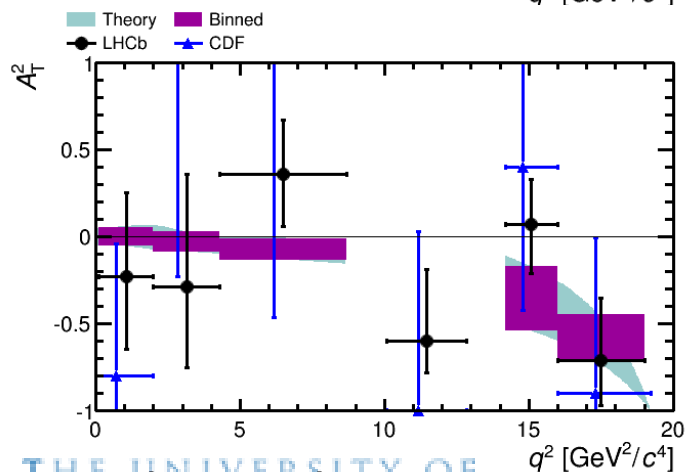
See also CDF PRL 108 (2012) 081807, BaBar PRD 86 (2012) 032012,  
Belle PRL 103 (2009) 171801, ATLAS-CONF-2013-038 & CMS PLB 727 (2013) 77



First measurement of  
zero-crossing point of  $A_{FB}$

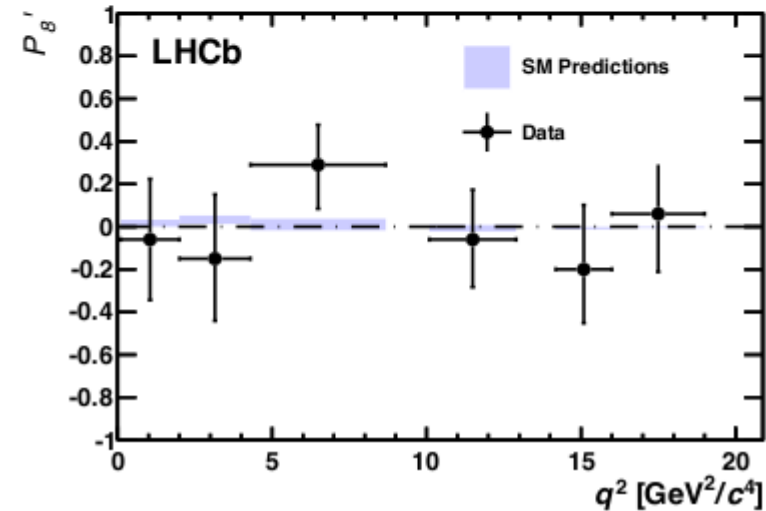
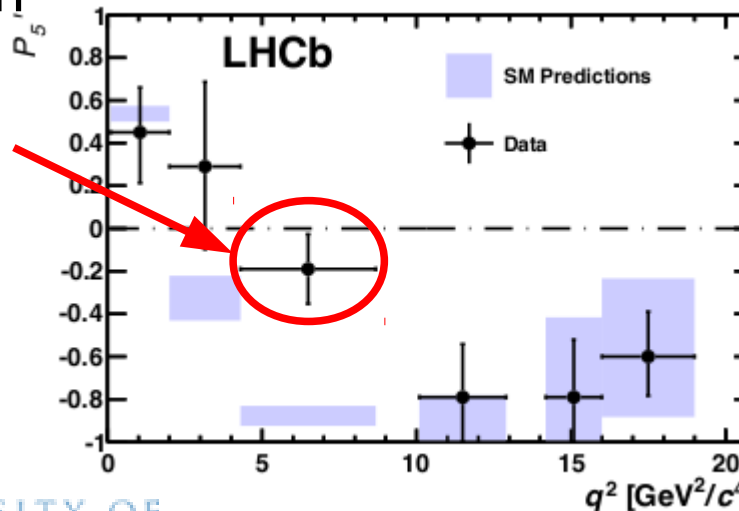
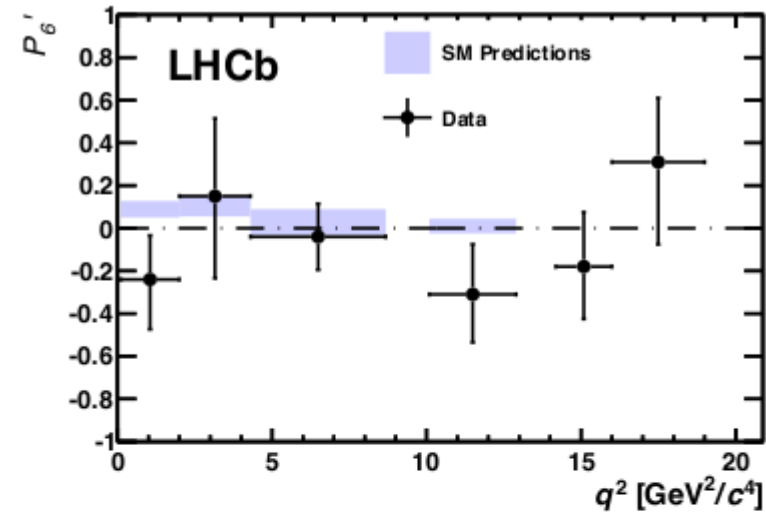
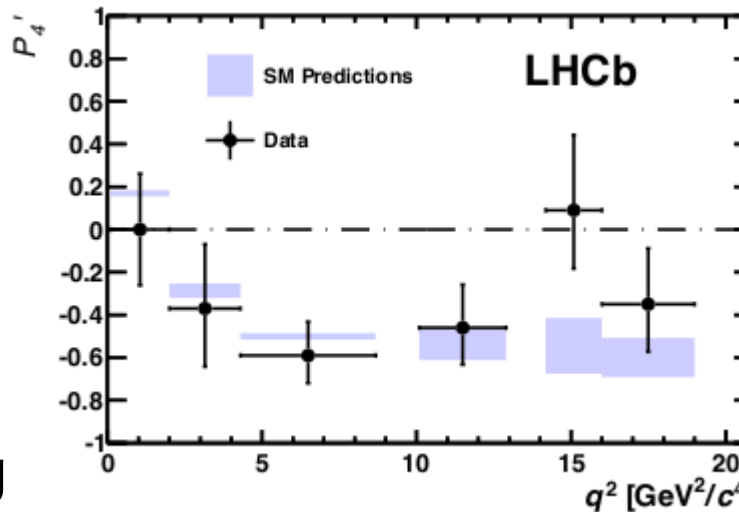
$$q_0^2 = (4.9 \pm 0.9) \text{ GeV}^2/c^4$$

Consistent with SM expectation



# New observables in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

LHCb PRL 111 (2013) 191801



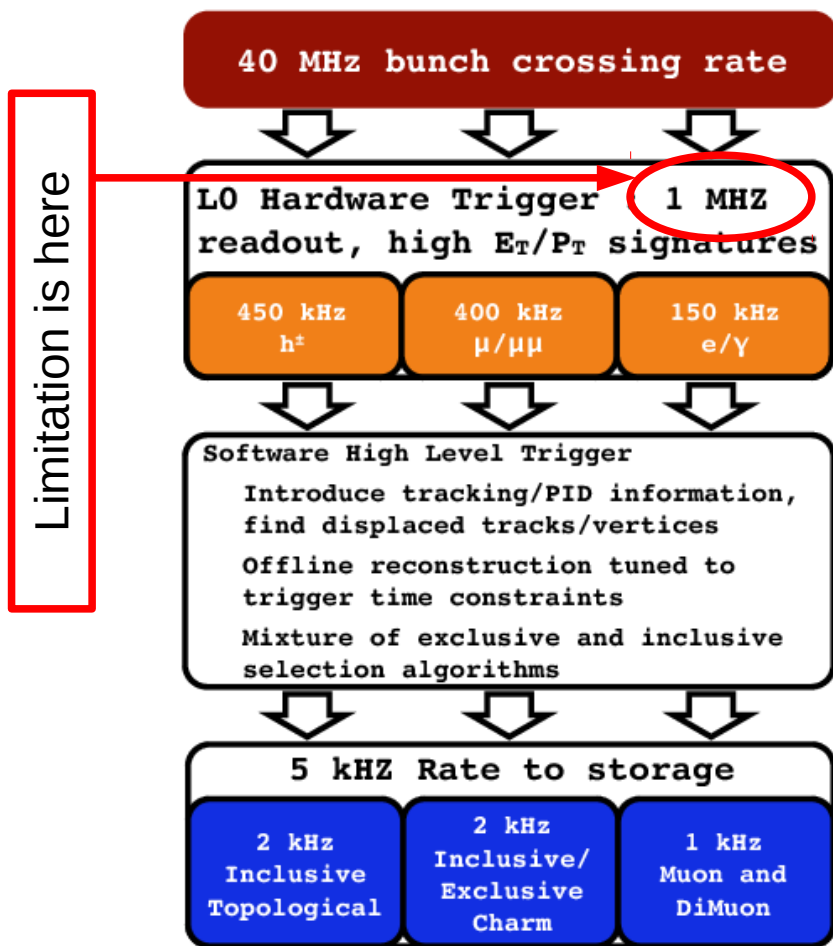
Interesting tension with the SM prediction

# Future flavour physics projects

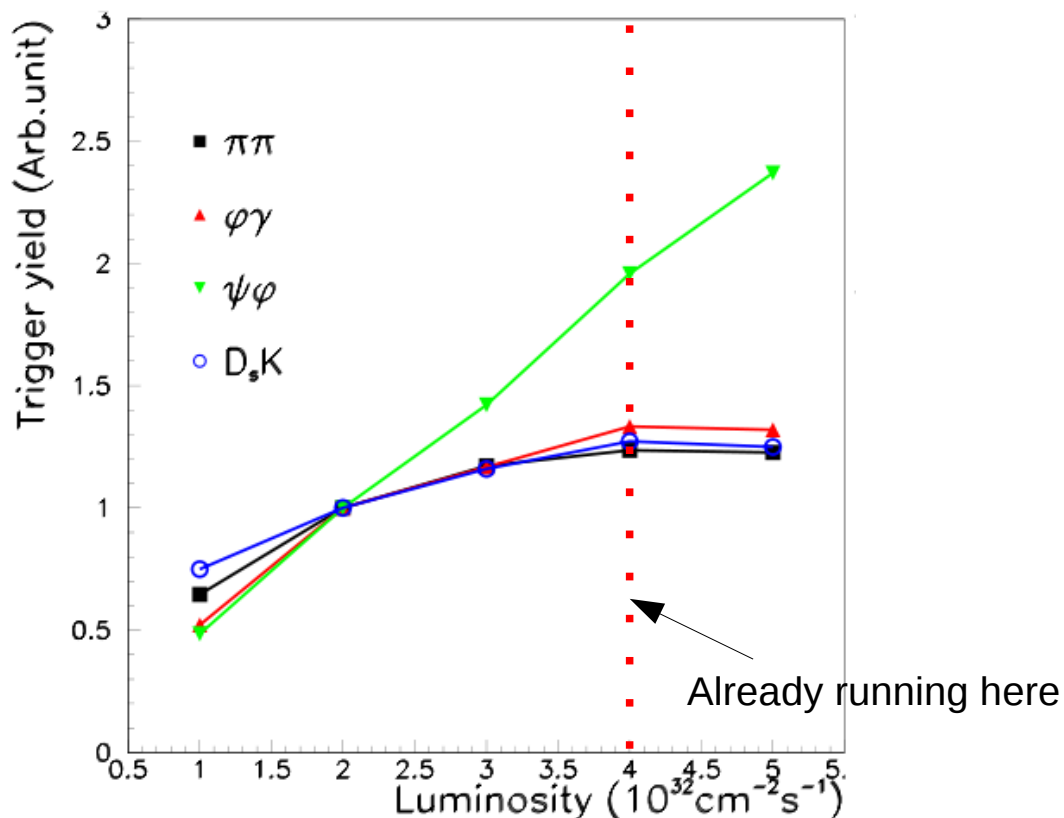
# LHCb upgrade

- To fully exploit LHC potential for heavy flavour physics will require an upgrade to LHCb
  - full readout & trigger at 40 MHz to enable high L running
  - “high L” =  $10^{33}/\text{cm}^2/\text{s}$  (so independent of machine upgrade)
  - planned for 2018 shutdown
- Physics case:
  - “exploration” of 1<sup>st</sup> phase will become “precision studies”
  - new opportunities for exploration open up (e.g. testing consistency of CP violation in tree vs. loop processes)

# LHC upgrade and the all important trigger

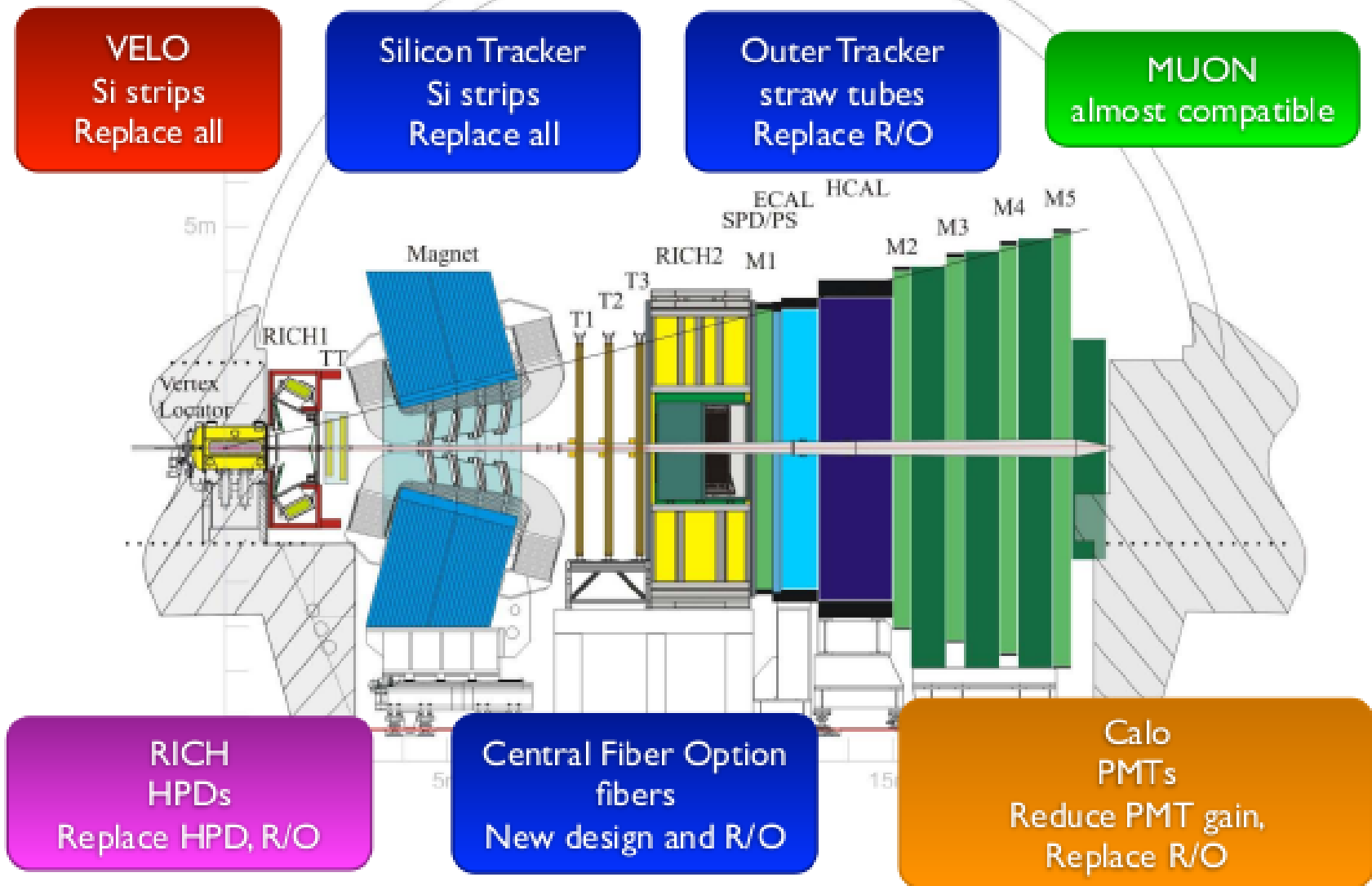


higher luminosity  
 → need to cut harder at L0 to keep rate at 1 MHz  
 → lower efficiency



- readout detector at 40 MHz
- implement trigger fully in software → efficiency gains
- run at  $L_{inst}$  up to  $2 \cdot 10^{33} / \text{cm}^2 / \text{s}$

# LHCb detector upgrade





# LHCb upgrade timeline

- 2011
  - Letter of Intent: [CERN-LHCC-2011-001](#)
- 2012
  - Framework TDR: [CERN-LHCC-2012-007](#)
    - **Endorsed by LHCC and approved by CERN Research Board** ([minutes](#))
    - LHCb upgrade features prominently in draft European Strategy for Particle Physics
  - See also [arXiv:1208.3355](#) for physics discussion
- 2013
  - Sub-detector TDRs ← **now approved**
- 2014-17
  - Final R&D, production and construction
- 2018 (LS2)
  - Installation of upgraded LHCb detector (requires 18 months)

# Upgrade – expected sensitivities

Type	Observable	Current precision	LHCb 2018	Upgrade (50 fb <sup>-1</sup> )	Theory uncertainty
$B_s^0$ mixing	$2\beta_s (B_s^0 \rightarrow J/\psi \phi)$	0.10 [9]	0.025	0.008	$\sim 0.003$
	$2\beta_s (B_s^0 \rightarrow J/\psi f_0(980))$	0.17 [10]	0.045	0.014	$\sim 0.01$
	$A_{fs}(B_s^0)$	$6.4 \times 10^{-3}$ [18]	$0.6 \times 10^{-3}$	$0.2 \times 10^{-3}$	$0.03 \times 10^{-3}$
Gluonic penguin	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\phi)$	–	0.17	0.03	0.02
	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow K^{*0}\bar{K}^{*0})$	–	0.13	0.02	$< 0.02$
	$2\beta_s^{\text{eff}}(B^0 \rightarrow \phi K_S^0)$	0.17 [18]	0.30	0.05	0.02
Right-handed currents	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)$	–	0.09	0.02	$< 0.01$
	$\tau^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)/\tau_{B_s^0}$	–	5 %	1 %	0.2 %
Electroweak penguin	$S_3(B^0 \rightarrow K^{*0}\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.08 [14]	0.025	0.008	0.02
	$s_0 A_{\text{FB}}(B^0 \rightarrow K^{*0}\mu^+\mu^-)$	25 % [14]	6 %	2 %	7 %
	$A_1(K\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.25 [15]	0.08	0.025	$\sim 0.02$
	$\mathcal{B}(B^+ \rightarrow \pi^+\mu^+\mu^-)/\mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-)$	25 % [16]	8 %	2.5 %	$\sim 10\%$
Higgs penguin	$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	$1.5 \times 10^{-9}$ [2]	$0.5 \times 10^{-9}$	$0.15 \times 10^{-9}$	$0.3 \times 10^{-9}$
	$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	–	$\sim 100\%$	$\sim 35\%$	$\sim 5\%$
Unitarity triangle angles	$\gamma (B \rightarrow D^{(*)}K^{(*)})$	$\sim 10\text{--}12^\circ$ [19, 20]	$4^\circ$	$0.9^\circ$	negligible
	$\gamma (B_s^0 \rightarrow D_s K)$	–	$11^\circ$	$2.0^\circ$	negligible
	$\beta (B^0 \rightarrow J/\psi K_S^0)$	$0.8^\circ$ [18]	$0.6^\circ$	$0.2^\circ$	negligible
Charm	$A_\Gamma$	$2.3 \times 10^{-3}$ [18]	$0.40 \times 10^{-3}$	$0.07 \times 10^{-3}$	–
CP violation	$\Delta A_{CP}$	$2.1 \times 10^{-3}$ [5]	$0.65 \times 10^{-3}$	$0.12 \times 10^{-3}$	–

Table 1: Statistical sensitivities of the LHCb upgrade to key observables. For each observable the current sensitivity is compared to that which will be achieved by LHCb before the upgrade, and that which will be achieved with 50 fb<sup>-1</sup> by the upgraded experiment. Systematic uncertainties are expected to be non-negligible for the most precisely measured quantities.

- sample sizes in most exclusive B and D final states far larger than those collected elsewhere
- no serious competition in study of  $B_s$  decays and CP violation

# Other future flavour experiments

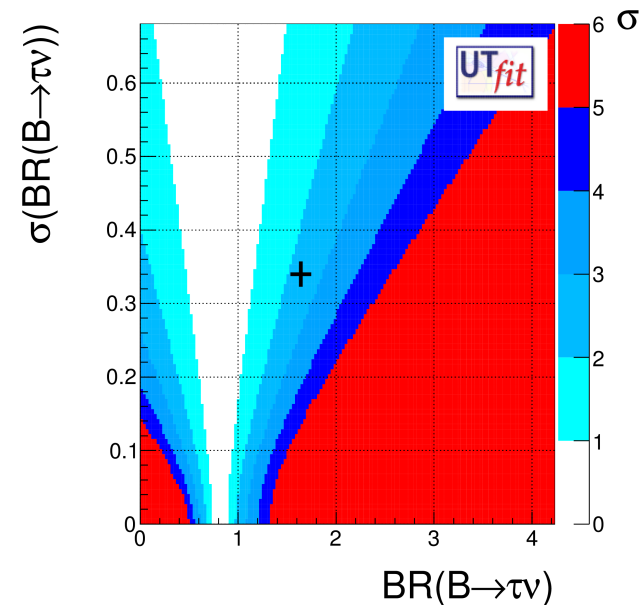
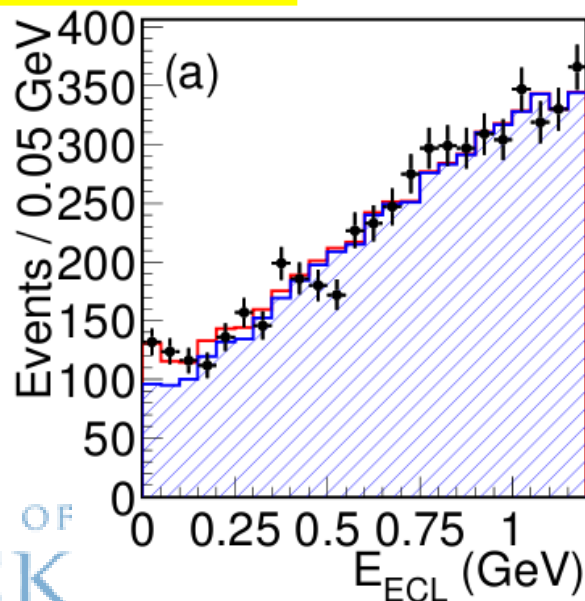
- SuperKEKB/Belle2 & SuperB
  - $B \rightarrow \tau\nu$ , inclusive measurements,  $\tau$  physics, ...
- Rare kaon decays
  - $K^+ \rightarrow \pi^+\nu\nu$  (NA62, CERN);  $K^0 \rightarrow \pi^0\nu\nu$  (KOTO, J-PARC)
- Muon to electron conversion (charged lepton flavour violation)
  - COMET/PRIME (J-PARC); mu2e (FNAL)

# B → τν and charged Higgs limits

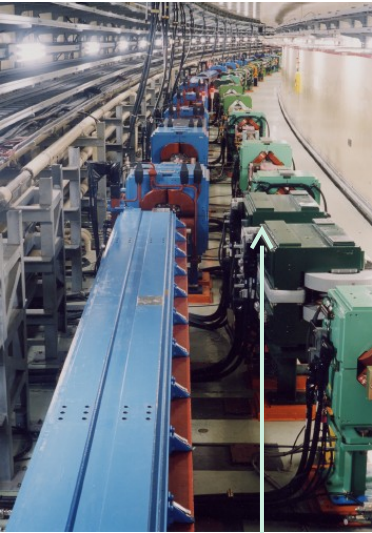
- Pure leptonic decays of charged B mesons very clean
  - clean SM prediction
  - clean effect of charged Higgs boson (2HDM or SUSY)

$$BR(B^+ \rightarrow l^+ \nu)^{SM} = \frac{G_F m_B}{8\pi} m_l^2 \left(1 - \frac{m_l^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B \quad BR(B^+ \rightarrow l^+ \nu)^{NP} = BR(B^+ \rightarrow l^+ \nu)^{SM} \left(1 - \frac{m_B^2}{m_H^2} \tan^2 \beta\right)^2$$

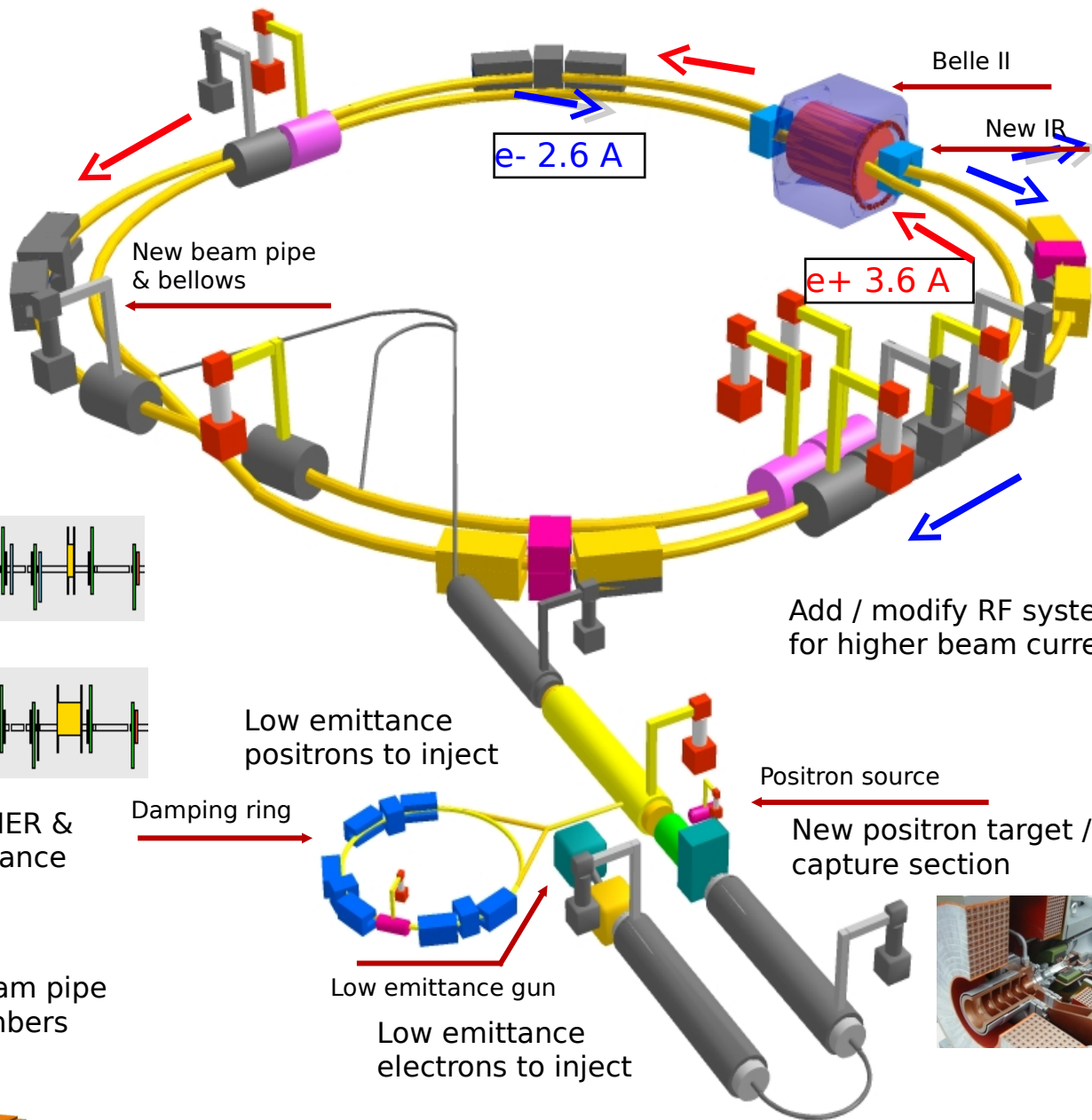
Belle PRD 82 (2010) 071101



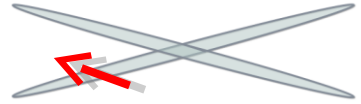
# KEKB to SuperKEKB



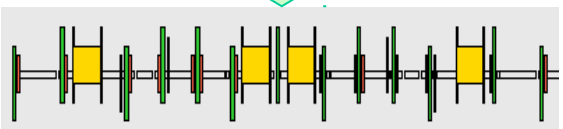
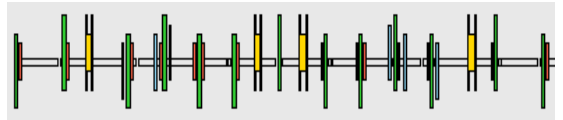
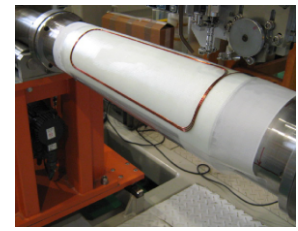
Replace short dipoles with longer ones (LER)



Colliding bunches

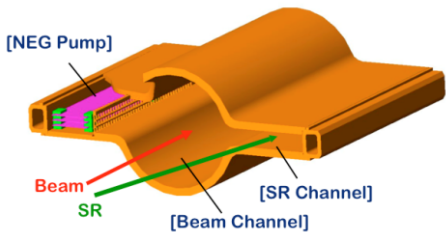


New superconducting / permanent final focusing quads near the IP



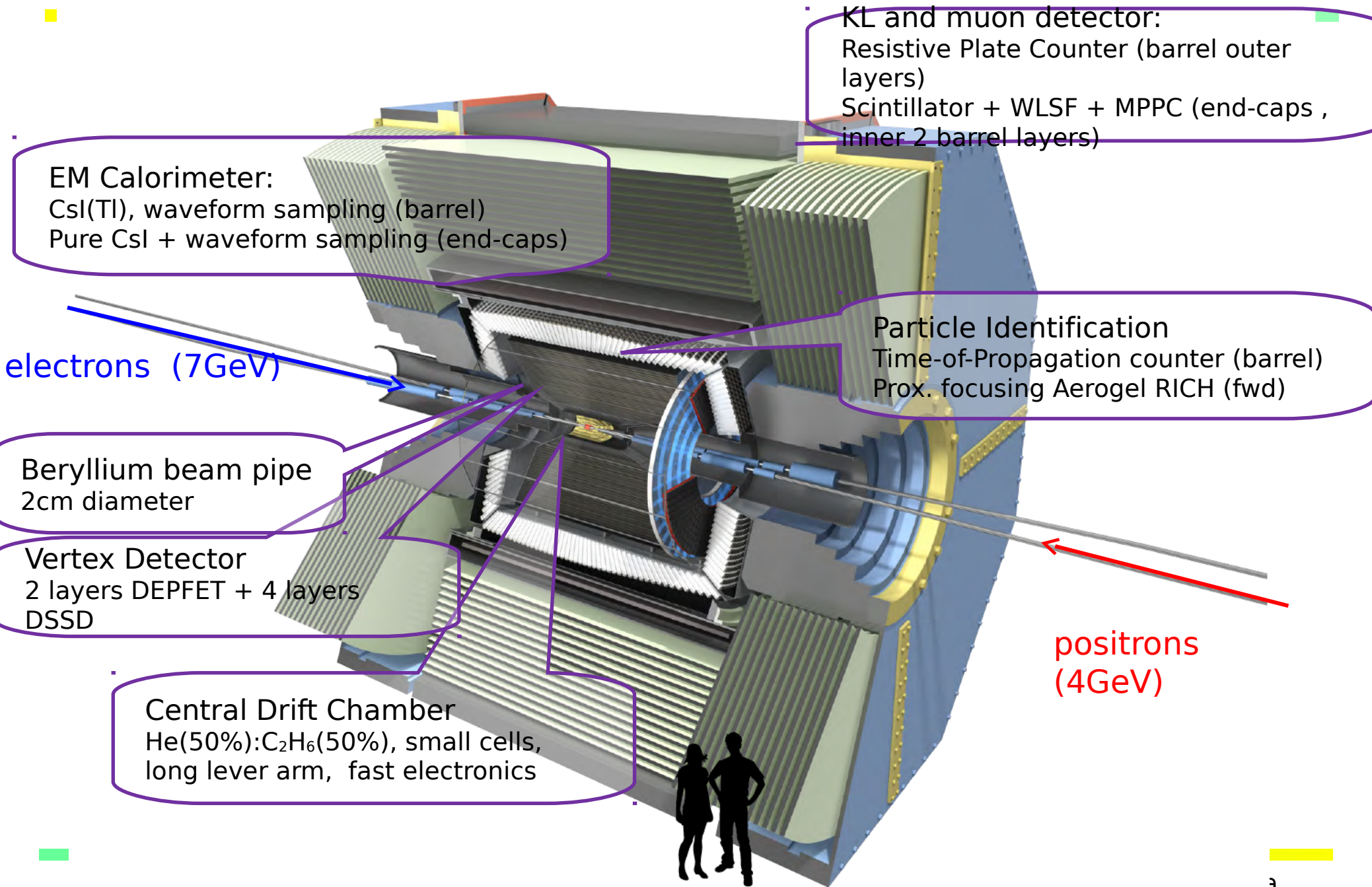
Redesign the lattices of HER & LER to squeeze the emittance

TiN-coated beam pipe with antechambers



**To obtain x40 higher luminosity**

# Belle II Detector



EM Calorimeter:  
CsI(Tl), waveform sampling (barrel)  
Pure CsI + waveform sampling (end-caps)

KL and muon detector:  
Resistive Plate Counter (barrel outer layers)  
Scintillator + WLSF + MPPC (end-caps , inner 2 barrel layers)

electrons (7GeV)

Particle Identification  
Time-of-Propagation counter (barrel)  
Prox. focusing Aerogel RICH (fwd)

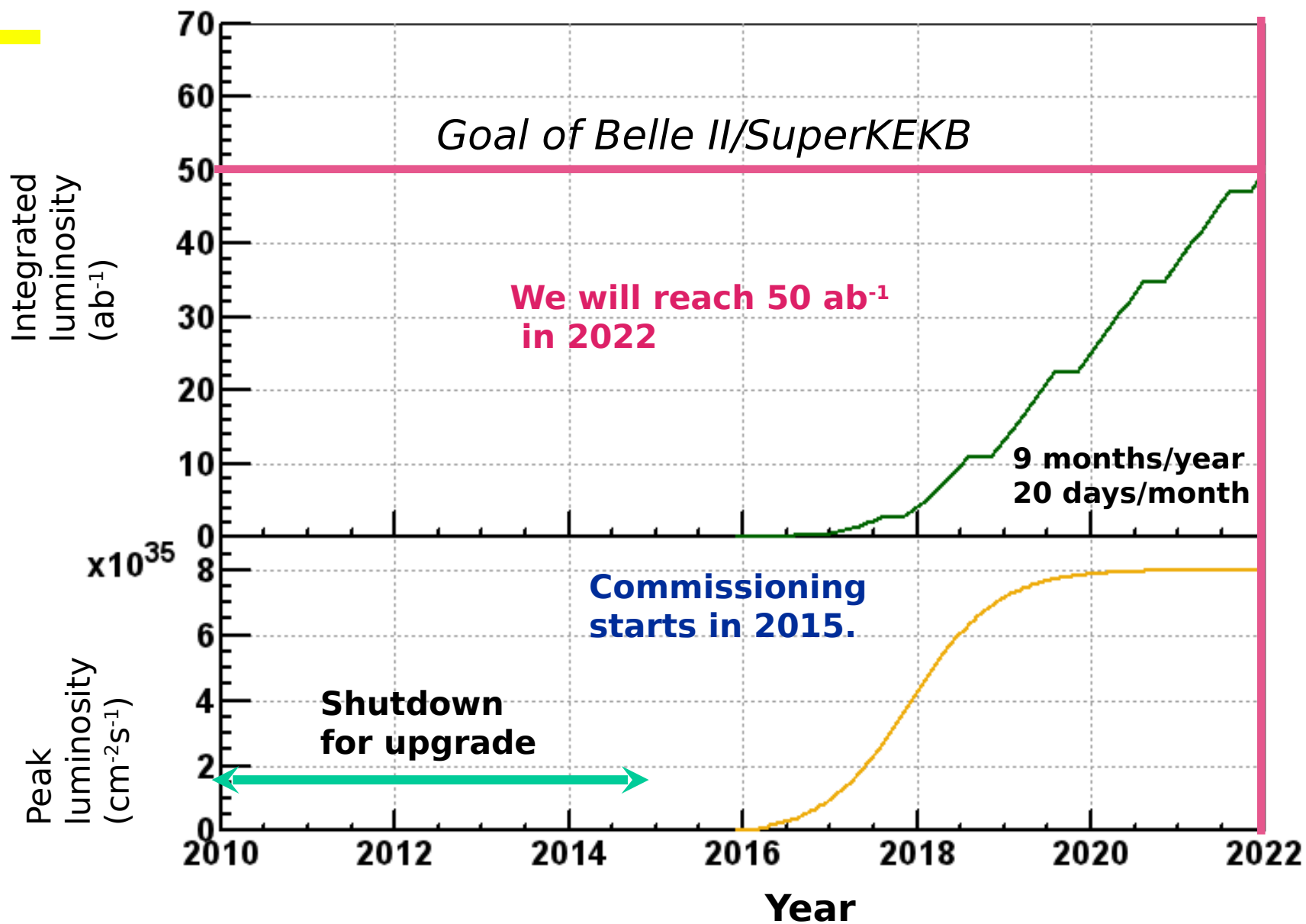
Beryllium beam pipe  
2cm diameter

Vertex Detector  
2 layers DEPFET + 4 layers DSSD

positrons (4GeV)

Central Drift Chamber  
He(50%):C<sub>2</sub>H<sub>6</sub>(50%), small cells,  
long lever arm, fast electronics

# Schedule



# The holy grail of kaon physics: $K \rightarrow \pi \nu \nu$

Highest CKM suppression  
of the  $s \rightarrow d$  coupling:

$$A \sim (m_t/m_W)^2 |V_{ts}^* V_{td}| \sim \lambda^5$$

## SM branching ratios

(Brod, Gorbahn, Stamou; PRD83 (2011) 034030)

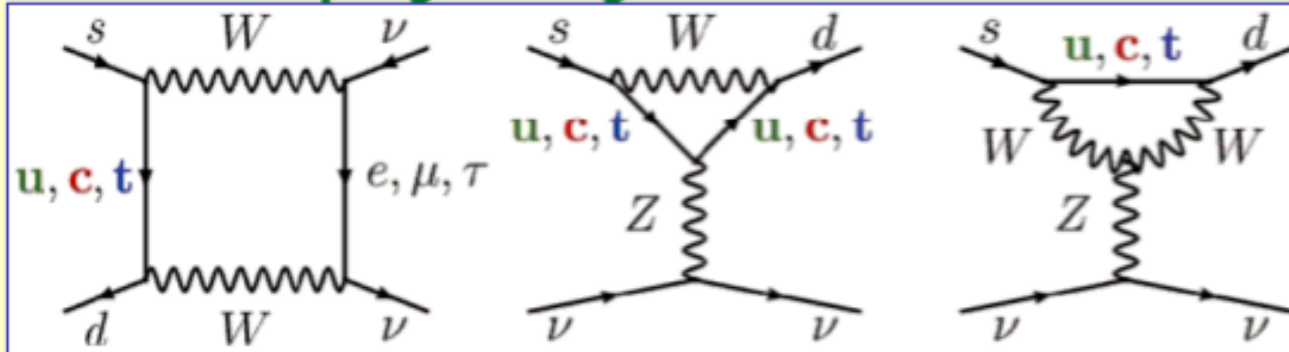
Mode	$BR_{SM} \times 10^{11}$
$K^+ \rightarrow \pi^+ \nu \bar{\nu} (\gamma)$	$7.81 \pm 0.75 \pm 0.29$
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$2.43 \pm 0.39 \pm 0.06$



CKM parametric  
(mainly  $|V_{ts}|$ )

Intrinsic

## SM: box and penguin diagrams

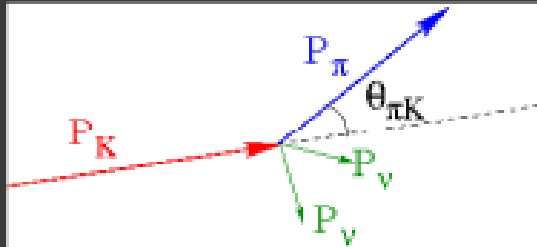


Next generation experiments should  
measure these decays for the 1<sup>st</sup> time

- $K^+ \rightarrow \pi^+ \nu \nu$  (NA62, CERN)
- $K^0 \rightarrow \pi^0 \nu \nu$  (KOTO, J-PARC)
- Proposals also at FNAL

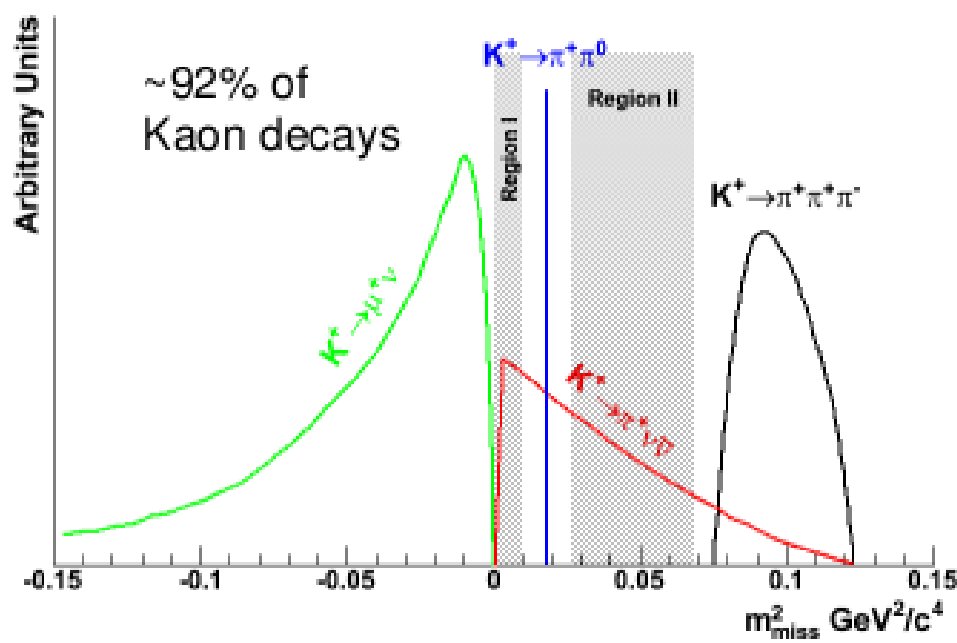


# NA62 Technique: Decay in Flight

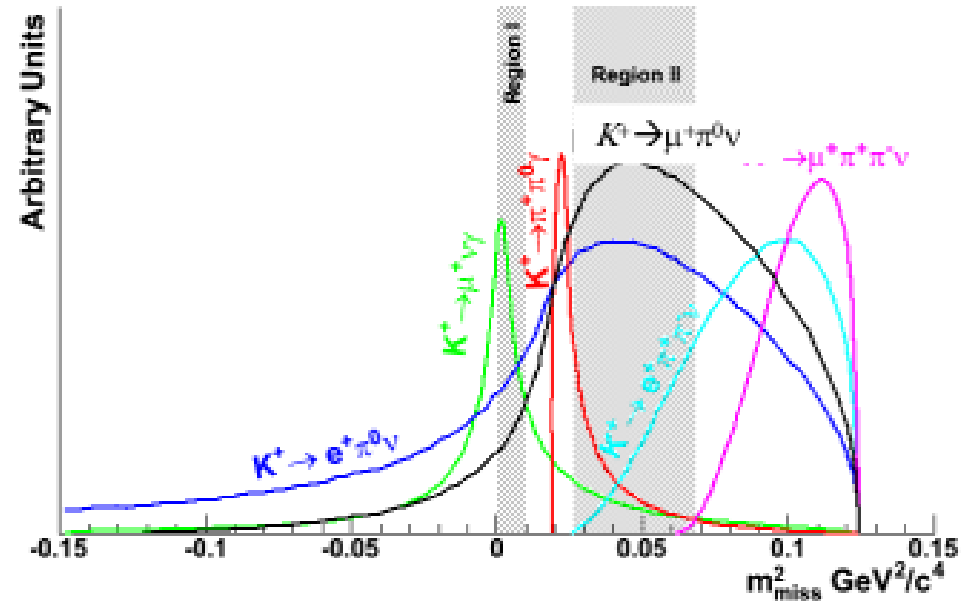


$$m_{miss}^2 = (\tilde{p}_K - \tilde{p}_\pi)^2$$

## Kinematically Constraint Decays

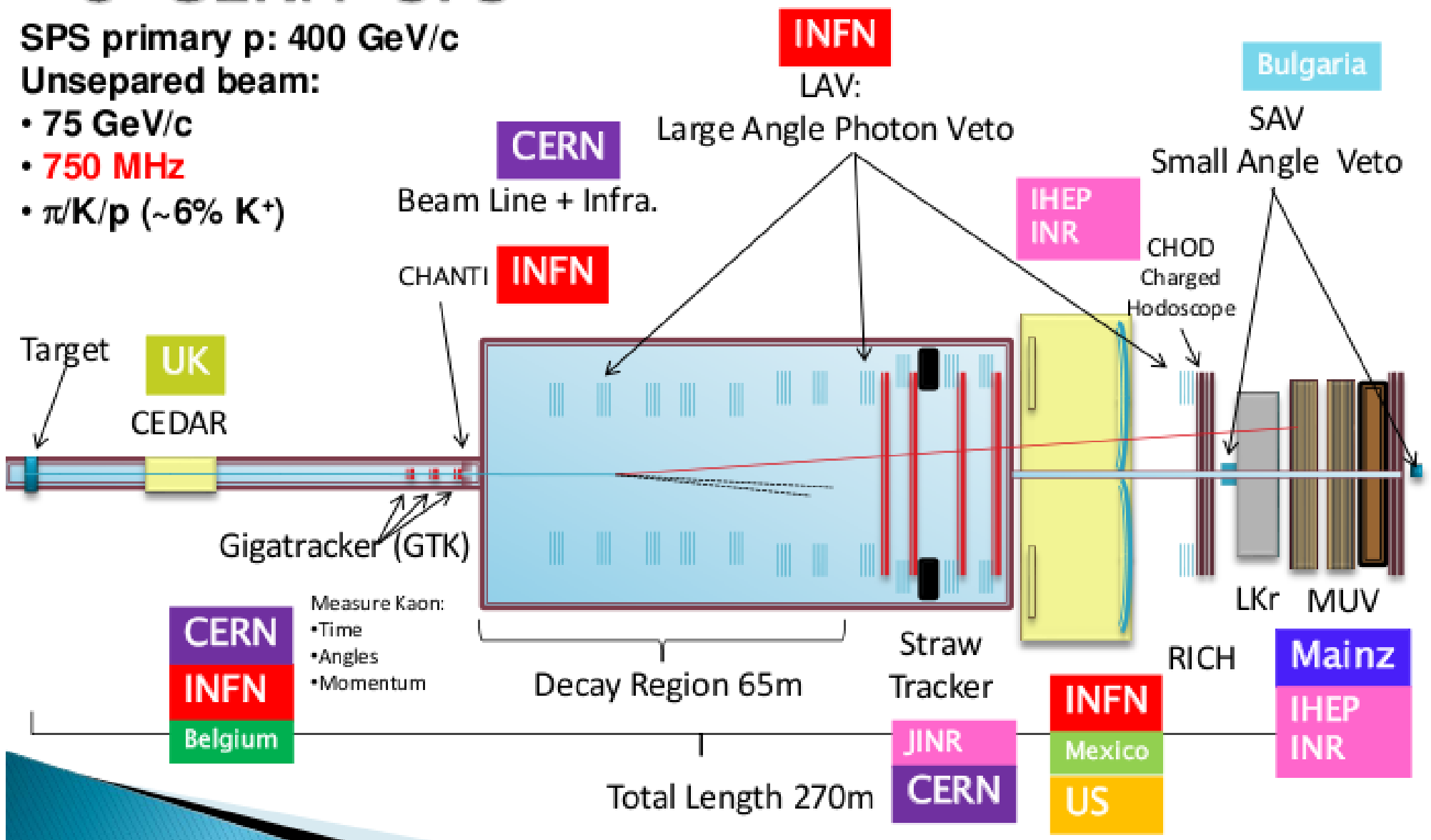


## Unconstraint Decays

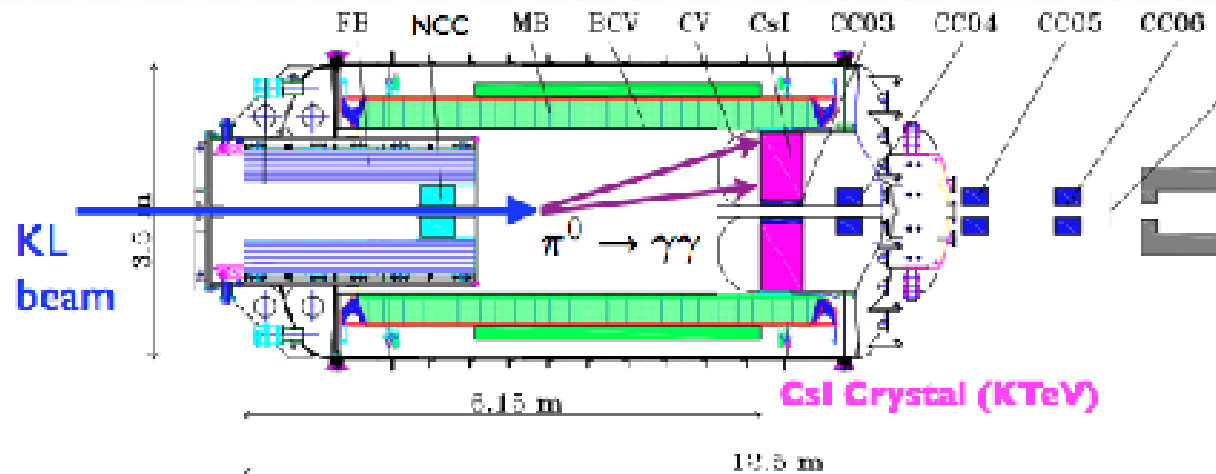
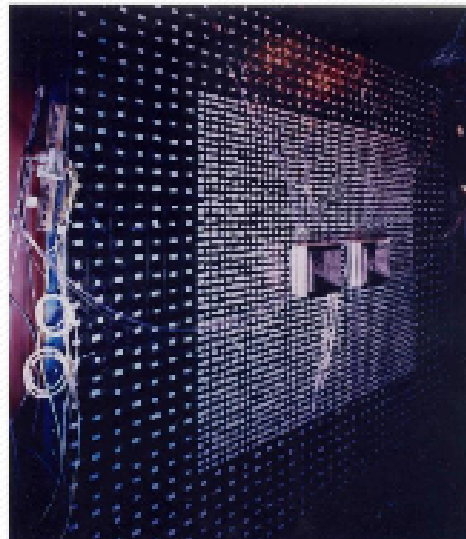
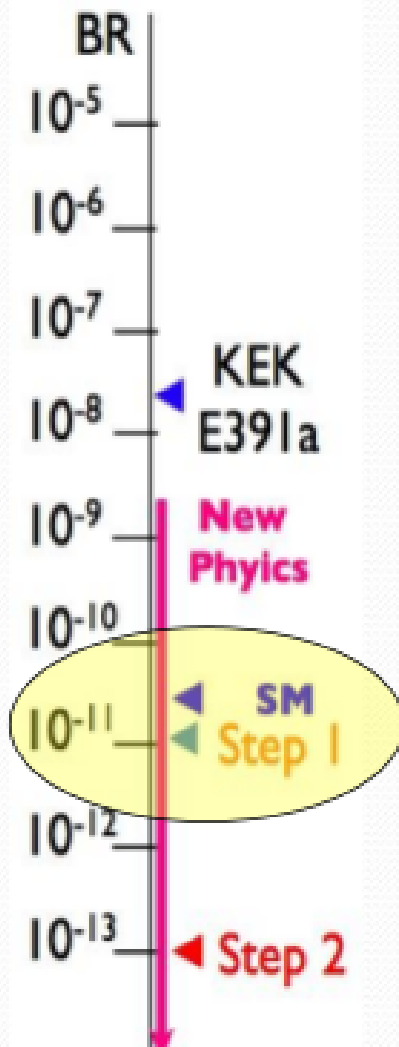


# NA62: $K^+ \rightarrow \pi^+ \nu \nu$ in-flight @ CERN-SPS

- SPS primary p: 400 GeV/c  
Unseparated beam:
- 75 GeV/c
  - 750 MHz
  - $\pi/K/p$  (~6%  $K^+$ )



# KOTO at JPARC



# The need for more precision

- “Imagine if Fitch and Cronin had stopped at the 1% level, how much physics would have been missed”

– A.Soni

- “A special search at Dubna was carried out by Okonov and his group. They did not find a single  $K_L^0 \rightarrow \pi^+\pi^-$  event among **600 decays** into charged particles (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the lab. **The group was unlucky.**”

– L.Okun

(remember:  $B(K_L^0 \rightarrow \pi^+\pi^-) \sim 2 \cdot 10^{-3}$ )

# Summary

- We still don't know:
  - why there are so many fermions in the SM
  - what causes the baryon asymmetry of the Universe
  - where exactly the new physics is ...
  - ... and what its flavour structure is
- Prospects are good for progress in the next few years
- We need a continuing programme of flavour physics into the 2020s
  - complementary to the high- $p_T$  programme of the LHC

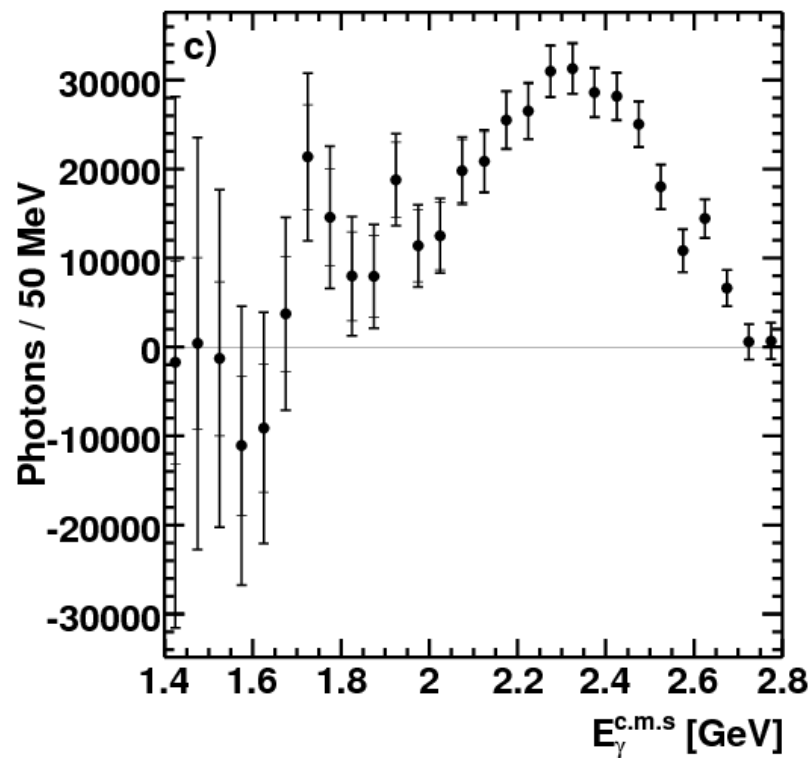
# References and background reading

- Reviews by the Particle Data Group
  - <http://pdg.lbl.gov/>
- Heavy Flavour Averaging Group (HFAG)
  - <http://www.slac.stanford.edu/xorg/hfag/>
- CKMfitter & UTfit
  - <http://ckmfitter.in2p3.fr/> & <http://www.utfit.org/>
- Review journals (e.g. Ann. Rev. Nucl. Part. Phys.)
  - <http://nucl.annualreviews.org>
- Proceedings of CKM workshops
  - Phys.Rept. 494 (2010) 197, eConf C100906
- Books
  - CP violation, I.I.Bigi and A.I.Sanda (CUP)
  - CP violation, G.C.Branco, L.Lavoura & J.P.Silva (OUP)

# Back up

# $b \rightarrow s\gamma$ rate and photon energy spectrum

Archetypal FCNC probe for new physics



Belle PRL 103 (2009) 241801

$$B(B \rightarrow X_s \gamma)_{E_\gamma > 1.7 \text{ GeV}} = (3.45 \pm 0.15 \pm 0.40) \times 10^{-4}$$

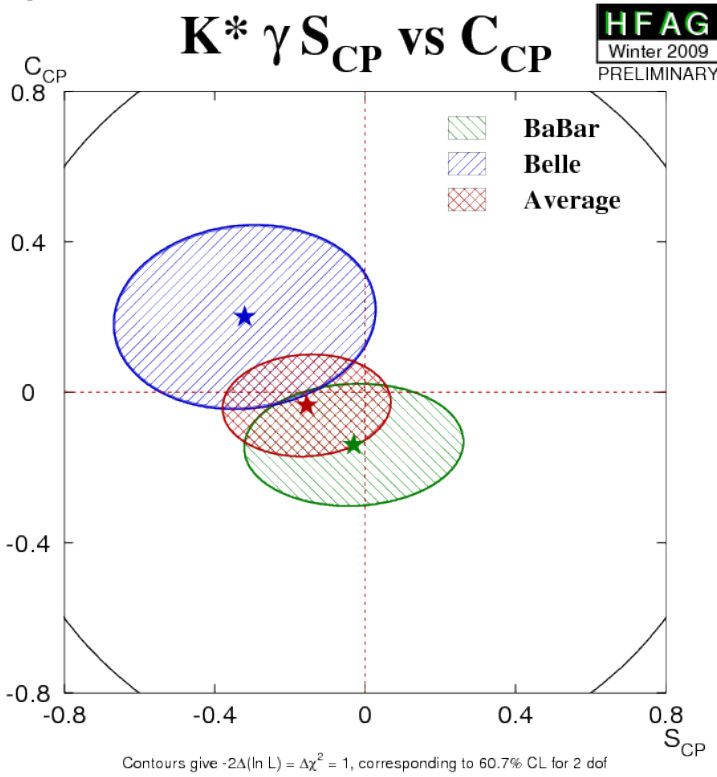
consistent with the SM prediction

... but SM also predicts that the photon is polarised



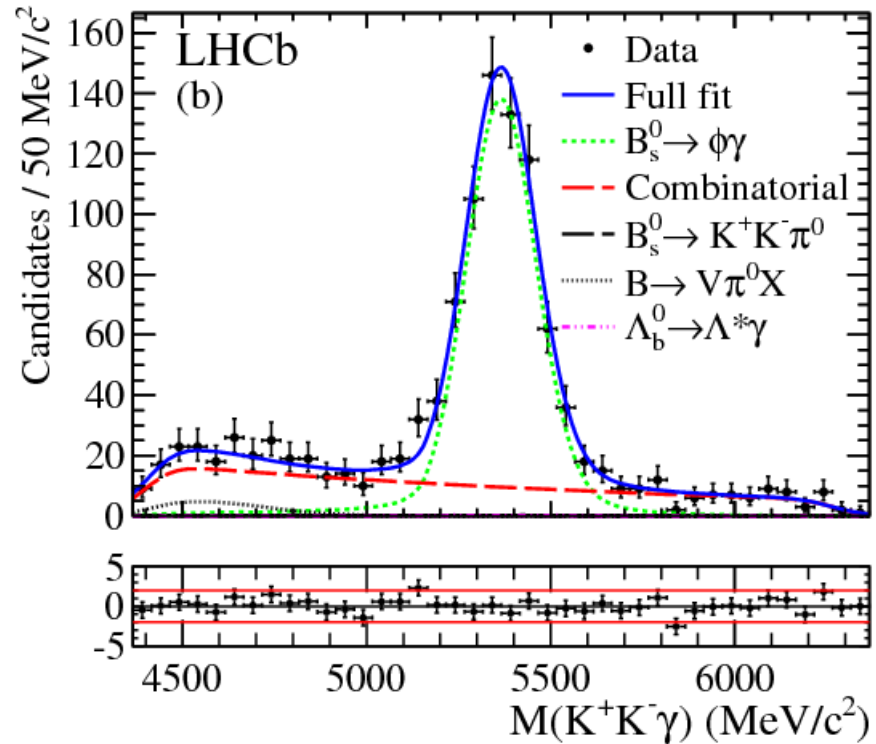
# $b \rightarrow s\gamma$ photon polarisation measurement

- Search for time-dependent asymmetry
  - Observable effect requires NP: left-handed current & new CP phase



Excellent prospects for LHCb with  $B_s \rightarrow \phi\gamma$

NPB 867 (2013) 1



# First measurement of photon polarisation in $b \rightarrow s\gamma$ transitions

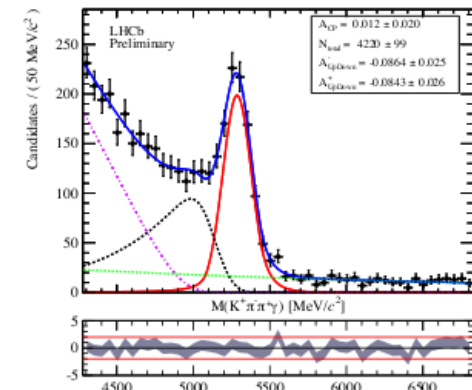
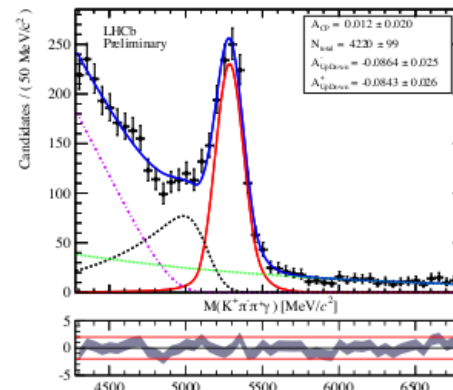
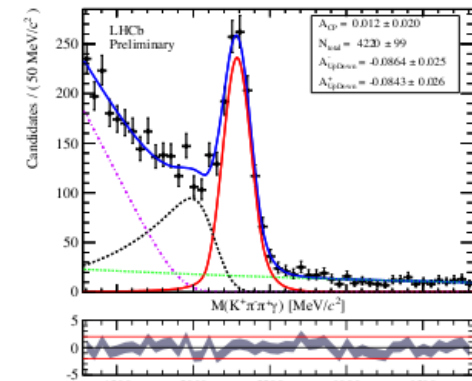
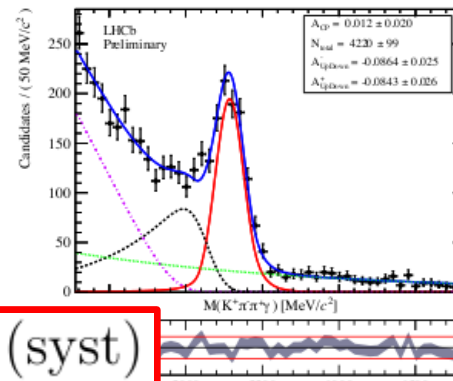
- New LHCb measurement

LHCb-CONF-2013-009

- uses  $B^+ \rightarrow K^+\pi\pi\gamma$  decays
- compare  $\gamma$  direction relative to  $K^+\pi\pi$  plane

$$A_{ud} = -0.085 \pm 0.019 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

$A_{ud}$  proportional to polarisation  
(unfortunately, constant of proportionality has large uncertainty)



# Effective operators

$$\mathcal{H}_W^{\Delta B=1, \Delta C=0, \Delta S=-1} = 4 \frac{G_F}{\sqrt{2}} \left( \lambda_c^s (C_1(\mu) Q_1^c(\mu) + C_2(\mu) Q_2^c(\mu)) \right. \\ \left. + \lambda_u^s (C_1(\mu) Q_1^u(\mu) + C_2(\mu) Q_2^u(\mu)) - \lambda_t^s \sum_{i=3}^{10} C_i(\mu) Q_i(\mu) \right)$$

where the  $\lambda_q^s = V_{qb}^* V_{qs}$  and the operator basis is given by

$$\begin{aligned} Q_1^q &= \bar{b}_L^\alpha \gamma^\mu q_L^\alpha \bar{q}_L^\beta \gamma_\mu s_L^\beta & Q_2^q &= \bar{b}_L^\alpha \gamma^\mu q_L^\beta \bar{q}_L^\beta \gamma_\mu s_L^\alpha \\ Q_3 &= \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q \bar{q}_L^\beta \gamma_\mu q_L^\beta & Q_4 &= \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q \bar{q}_L^\beta \gamma_\mu q_L^\alpha \\ Q_5 &= \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q \bar{q}_R^\beta \gamma_\mu q_R^\beta & Q_6 &= \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q \bar{q}_R^\beta \gamma_\mu q_R^\alpha \\ Q_7 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q e_q \bar{q}_R^\beta \gamma_\mu q_R^\beta & Q_8 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q e_q \bar{q}_R^\beta \gamma_\mu q_R^\alpha \\ Q_9 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q e_q \bar{q}_L^\beta \gamma_\mu q_L^\beta & Q_{10} &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q e_q \bar{q}_L^\beta \gamma_\mu q_L^\alpha \end{aligned}$$

Four-fermion operators (except  $Q_{7\gamma}$  &  $Q_{8g}$ ) – dimension 6

$$Q_{7\gamma} = \frac{e}{16\pi^2} m_b \bar{b}_L^\alpha \sigma^{\mu\nu} F_{\mu\nu} s_L^\alpha$$

$$Q_{8g} = \frac{g_s}{16\pi^2} m_b \bar{b}_L^\alpha \sigma^{\mu\nu} G_{\mu\nu}^A T^A s_L^\alpha$$

$$Q_{9V} = \frac{1}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \bar{l} \gamma_\mu l$$

$$Q_{10A} = \frac{1}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \bar{l} \gamma_\mu \gamma_5 l$$

# Future projects

