

I was asked to give a talk  
"B-Physics Theory Overview".

I was told by somebody,  
who prefers to remain anonymous

-- can you guess? --

this obviously means

"Buras-Physics Overview".

Since it is even more impossible to do that in 30 min.,

I decided to specify the title differently ---

# B Decay Dynamics -- an Overview

Ikaros Bigi, Notre Dame du Lac

First an appeal to LHC experiments:

Try very, very hard to search for

$$\tau \rightarrow 3\mu, \dots$$

desirable range  $\sim 10^{-8} - 10^{-10}$

Will address measurements that

- ❑ can be made at the LHC
- ❑ are **relevant** for LHC studies, even if cannot be done here

# Prologue

## ❖ 3 inter-related aspects of B dynamics

- ❑ indirect probes for New Physics (NP)

observed rate  $\neq$  predicted rate

- ❑ ew SM decay dynamics

SM parameters  $\implies$  accurate SM predictions

{quarks, gluons, ...}  $\longleftrightarrow$  {hadrons, ...}

- ❑ hadronization

- ✍ validate theoret. control over QCD

- ✍ learn (novel ?) lessons on QCD

- ✍ QCD might just be the first of theories realized in nature with essential nonperturb. dynamics

❖ We cannot count on numerically massive impact of TeV scale NP on B decays -- larger than anticipated operational success of B factories suggest typical impact smallish

➔ need reliability & accuracy

☞ sign of hope:  $\bar{\Lambda}/m_b \ll 1$

Heavy Quark Symmetry  $\approx$  Heavy Quark Expans.

$$\sim H_{\text{Pauli}} = -A_0 + (i\partial - \mathbf{A})^2/2m_Q + \boldsymbol{\sigma} \cdot \mathbf{B}/2m_Q \rightarrow -A_0 \quad \text{as } m_Q \rightarrow \infty$$

i.e., infinitely heavy static quark, without spin dynamics, only colour Coulomb potential!

- ❑ classification of  $m_b \rightarrow \infty$  good!
- ❑ understand  $1/m_b$  corrections better!
- ❑ no  $1/m_b$  correct., understand  $1/m_b^2$  correct. best!

❖ Heavy Quark Theory (HQT) mature, robust framework

➔ (quark) model considerations

- ❑ most useful as starting point
- ❑ most helpful to train intuition
- ❑ not satisfactory for final answers
- ❑ should not replace interpretations based on HQT!

❖ We would have seen `generic' SUSY -- but

📖 Nature has shown little taste for `generic' dynam.

📖 the one certain aspect of SUSY -- that it is broken -- is the least understood one

❖ The statement "The data have led us to a world of Minimal Flavour Violation (MFV)" might be visionary -- but it is at least **premature!**

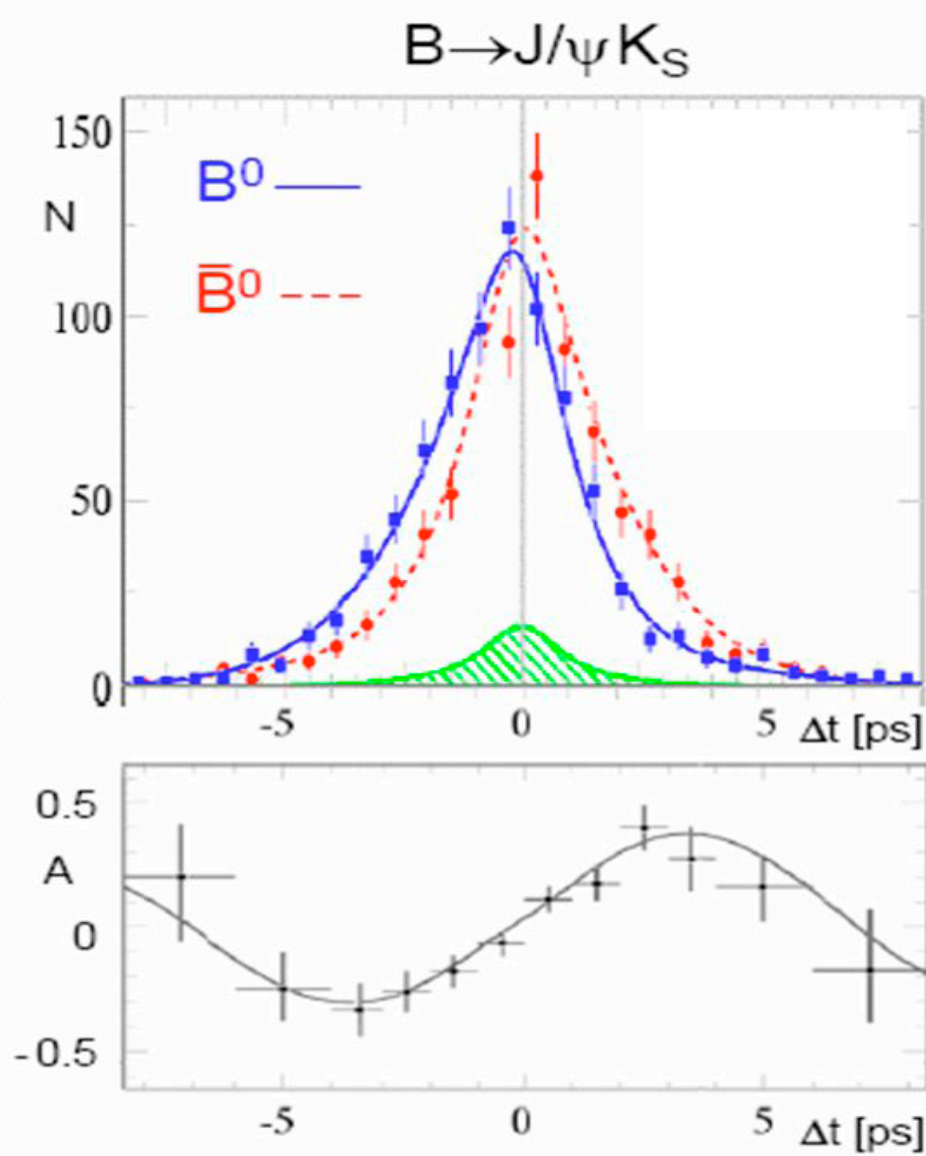
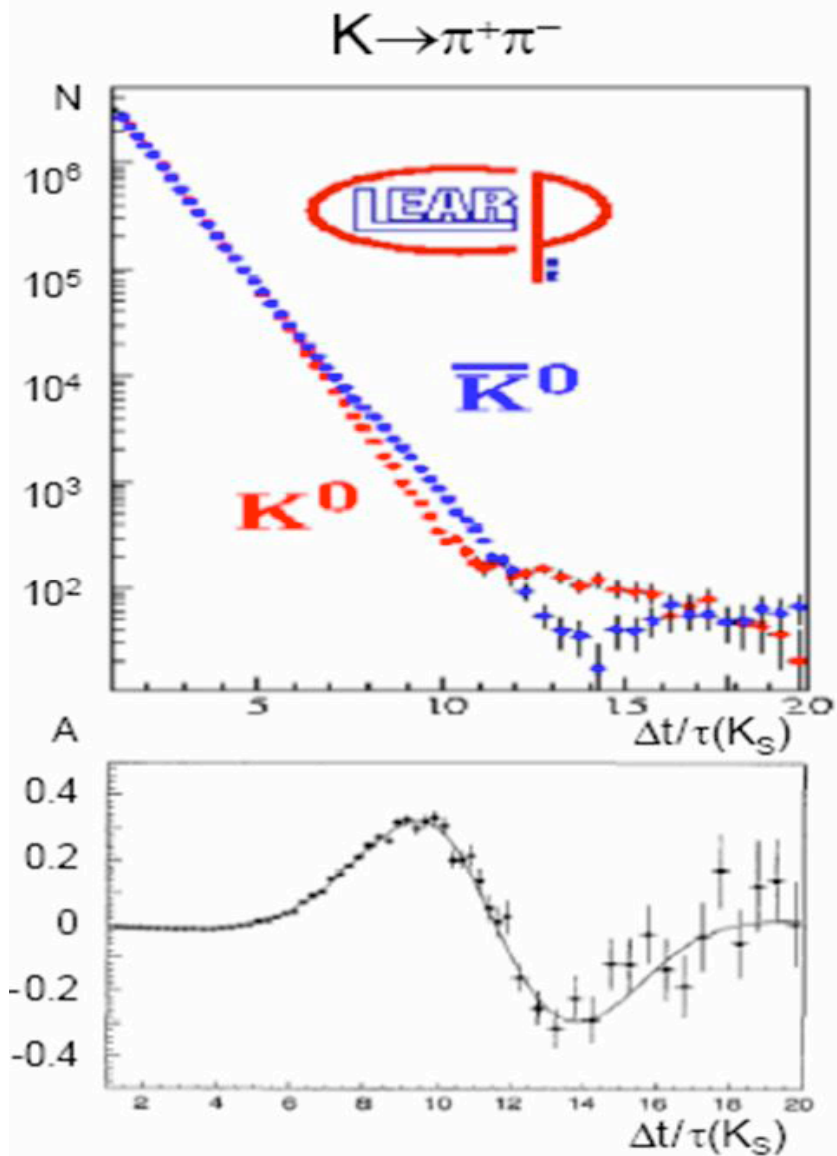
Inferring  $T_{NP} \ll T_{SM}$  from  $T_{NP} < T_{SM}$  needs some act of faith

- it is a **classification** scheme, **not** a model or theory -- analogous to the Superweak Model of ~~CP~~

- one must analyze to which degree a **given** theory implements this scheme **dynamically**:

**absolute** vs. **approximate**; how approximate?

📖 **When & if time dependent ~~CP~~ in  $B_s \rightarrow \psi\phi$  found to be  $< 10\%$ , then I will be more intrigued**



[courtesy of K. Schubert]

→ statement '~~CP~~ in B decays is much larger than in K decays' is an empirically verified fact



## The Menu

I Basics of HQT and HQE

II On Beauty Lifetimes

→ Lenz

III On Extracting  $|V(cb)|$  and  $|V(ub)|$

→ Uraltsev

IV "3/2 vs. 1/2"

V On the Autonomy of  $B_s$  Dynamics

VI On  $B \rightarrow \tau \nu D, \tau \nu X$

→ Uraltsev

VII Outlook

# I Basics of HQT and HQE

One of the most active & most quickly progressing fields of QCD

✍ the goal: to treat **nonperturbative** dynamics **quantitatively**

😊 the hope:  $m_b \gg \Lambda_{\text{QCD}}$

⚡ central tool: Operator Product Expansion (OPE)

⚡ most common application: **inclusive rates**

$$\Gamma(H_Q \rightarrow f) = \sum_i c_i^{(f)}(KM, M_W, m_Q, \alpha_S, \mu) \langle H_Q | O_i | H_Q \rangle_{(\mu)}$$

- short distance dynamics  $\rightarrow$  coeff.  $c_i^{(f)}$
- universal cast of **local** operators  $O_i$
- $\langle H_Q | O_i | H_Q \rangle$  **inferred** from other **observables** or **lattice QCD!**
- expansion parameter

$$1/E_{\text{release}} \sim \begin{cases} 1/(m_b - m_c) & \text{for } b \rightarrow c \\ 1/m_b & \text{for } b \rightarrow u \end{cases}$$

- Wilson: **auxiliary** scale  $\mu$  s.t.

**short** distance  $< \mu^{-1} < \text{long}$  distance

⚡  $c_i \leftrightarrow$  **short** distance dynamics

⚡  $O_i$  **active** fields - **long** distance dynamics

❖ not all OPEs are created equal

caveat:  $\mu_\pi^2 \neq -\lambda_1, \mu_G^2 \neq -\lambda_2$

will use 'kinetic scheme': soft gluon effects lumped into HQP defined at  $\mu \sim 1 \text{ GeV}$

❖ total widths, total SL widths:

❑ no contributions  $\sim O(1/m_b)$  due to complete cancellations between initial and final state corrections

❑ partial cancellations in  $\sim O(1/m_b^2)$

➔ somewhat smaller than 'natural' scale

❑ for  $\Gamma_{SL}(B \rightarrow lvX_c)$  explicit analysis of  $O(1/m_b^4)$

Mannel et al.

❑ can & will be improved with results from IC analysis

Zwicky et al.

## II On Beauty Lifetimes

→ Lenz

	$1/m_b$ predict.	comment	data
$\tau(B^-)/\tau(B_d)$	$1+0.05(f_B/0.2\text{GeV})^2$ '92 $1.06 \pm 0.02$ '98-'03	PI in $\tau(B^-)$ fact. at low scale $\sim 1\text{ GeV}$	$1.076 \pm 0.008$ '05 $1.071 \pm 0.009$ '08
$\langle \tau(B_s) \rangle / \tau(B_d)$	$1 \pm \mathcal{O}(0.01)$ '94		$0.92 \pm 0.03$ '05 $0.961 \pm 0.018$ '08
$\tau(\Lambda_b)/\tau(B_d)$	$\sim 0.9 - 1.0$ '93 $0.88 - 0.97$ '98	quark model ME	$0.806 \pm 0.047$ '05 $0.904 \pm 0.032$ '08
$\tau(B_c)$	$\sim 0.5\text{ psec}$ '94	largest lifetime difference! no $1/m_Q$ crucial	$0.45 \pm 0.12\text{ ps}$ '05 $0.463 \pm 0.071\text{ ps}$ '08
$\Delta\Gamma(B_s)/\Gamma(B_s)$	$0.18(f_B/0.2\text{GeV})^2$ '87 $0.12 \pm 0.04$ '04	less reliable than $\Delta M(B_s)$	$0.07 \pm 0.06$ '08

'93/'94:  $\tau(\Lambda_b)/\tau(B_d) \sim 0.9 - 1.0$  ibiBlokShifUraltVainsh

'94ff:  $\tau(\Lambda_b)/\tau(B_d) \sim 0.806 \pm 0.047$

'98:  $\tau(\Lambda_b)/\tau(B_d) \sim 0.94^{+0.03}_{-0.06}$  [0.88 - 0.97] Uralt ←

if  $\tau(\Lambda_b)/\tau(B_d) < 0.88 \implies$  new paradigm for had. wavefct.

'04:  $\tau(\Lambda_b)/\tau(B_d) \sim 0.86 \pm 0.05$  GOP

'05:  $\tau(\Lambda_b)/\tau(B_d) \sim 0.87 \pm 0.17 \pm 0.03$  D0

$\tau(\Lambda_b)/\tau(B_d) \sim 0.944 \pm 0.086$  CDF

'06:  $\tau(\Lambda_b)/\tau(B_d) \sim 1.037 \pm 0.058$  CDF

❖ highly desirable to measure  $\tau(\Xi_b^0)$  &  $\tau(\Xi_b^-)$   
to diagnose failure or confirm success

'93/'94:  $\bar{\tau}(B_s)/\tau(B_d) = 1 \pm O(1\%)$  ibiUralt

'08:  $\bar{\tau}(B_s)/\tau(B_d) = 0.961 \pm 0.018$

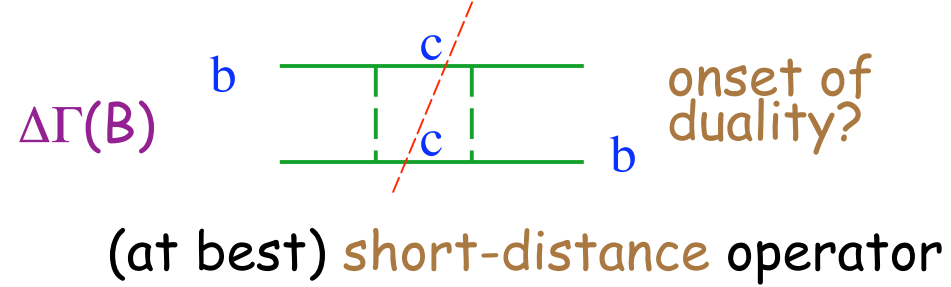
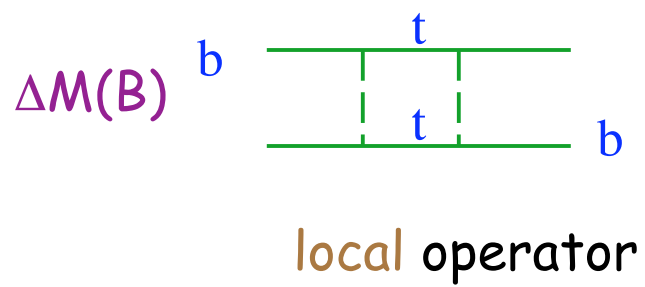
$$\Delta\Gamma_s$$

theoret. predict.  
based on quark  
box diagram

$$\Delta\Gamma(B_s)/\Gamma(B_s)$$

$0.18(f_B/0.2\text{GeV})^2$  '87  
 $0.12\pm 0.04$  '04

my heart wishes  $\Delta\Gamma(B_s)/\Gamma(B_s) \sim 0.5$   
yet my head tells me  $\Delta\Gamma(B_s)/\Gamma(B_s) > 0.25$  very unlikely



- ☞ quark box diagram less reliable for  $\Delta\Gamma(B)$  than for  $\Delta M(B)$
- ➔ theoretical uncertainties might be sizable in  $\Delta\Gamma(B)/\Delta M(B)$  even with the bag factor dropping out!

### III On Extracting $|V(cb)|$ and $|V(ub)|$

→Uraltsev

(3.1)  $|V(cb)|$

$B \rightarrow l\nu X_c$

total width & normalized moments for  $B \rightarrow l\nu X_c/\gamma X$

$$\rightarrow |V(cb)|_{incl} = (42.04 \pm 0.34|_{fit} \pm 0.59|_{\Gamma_{SL}}) \times 10^{-3}$$

$$m_b^{kin} = (4.597 \pm 0.034|_{fit}) \text{ GeV}$$

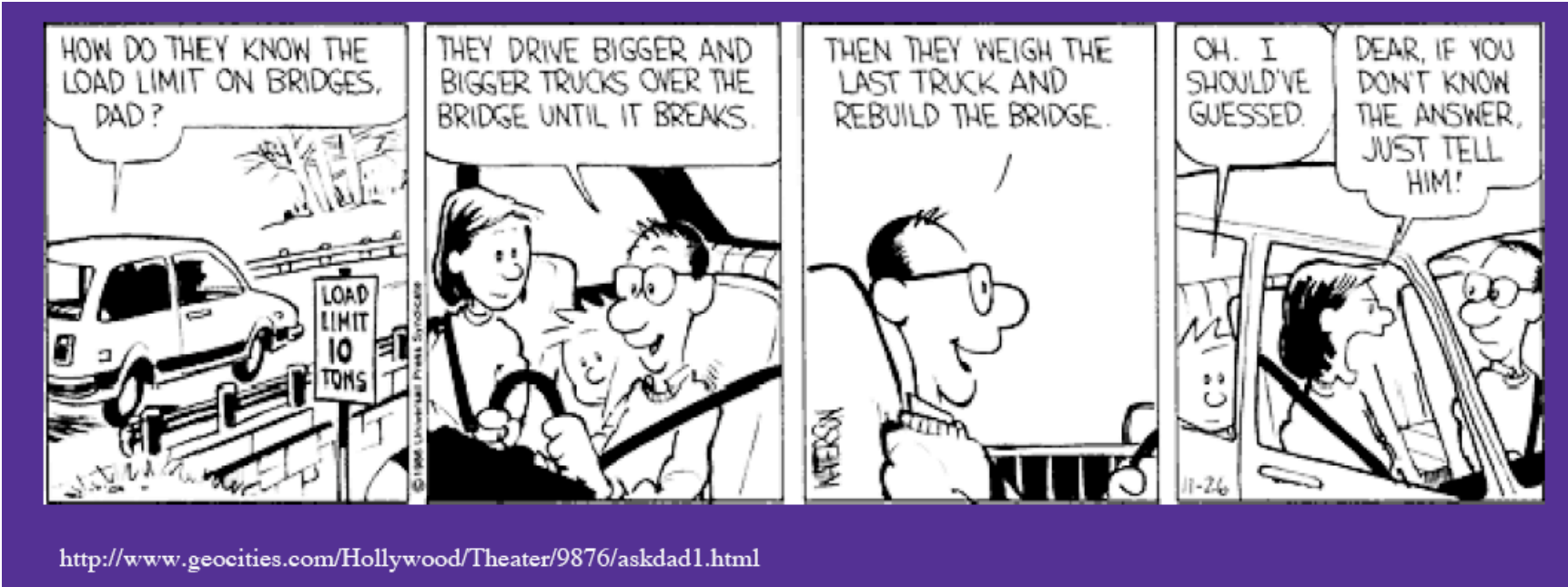
$$m_c = (1.163 \pm 0.051|_{fit}) \text{ GeV}$$

$$\mu_\pi^2 = (0.434 \pm 0.033|_{fit}) \text{ GeV}^2$$

$$\rho_D^3 = (0.213 \pm 0.033|_{fit}) \text{ GeV}^3$$

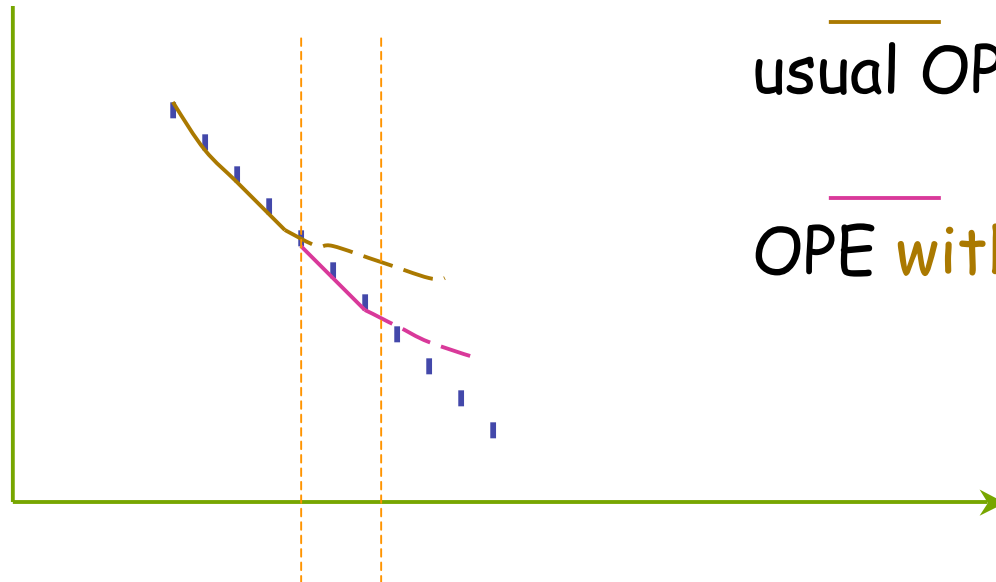
 theoretical error budget defensible since

- 4 HQP provide consistent fit to several moments with different cuts  $\implies$  high degree of overconstraints
- $m_b^{kin}$  from weak  $B \rightarrow l\nu X_c = m_b^{kin}$  from em&str.  $\Upsilon(4S) \rightarrow bb$
- fit values satisfy relations without them being imposed



'defensible' ? --

'moment'



usual OPE expression

OPE with bias correc.

'E<sub>cut</sub>'  
16



$$B \rightarrow l\nu D^*$$

Extract  $|F(1)||V(cb)|_{\text{excl}} = (36.2 \pm 0.6) \times 10^{-3}$

↻ LQCD:  $|F(1)| = 0.924 \pm 0.023$

➔  $|V(cb)|_{\text{excl}} = (39.2 \pm 0.6 \pm 1.0) \times 10^{-3}$

↻  $F(1) = 0.89 \pm 0.04 + \mathcal{O}(1/m_Q^3)$  Uraltsev '94

□  $F(1) < 0.89$  Uraltsev '07

↻ caveat concerning  $F(1)$

□ leading expansion term  $1/m_c$

to consider when comparing

$$|V(cb)|_{\text{incl}} = (42.04 \pm 0.34|_{\text{fit}} \pm 0.59|_{\Gamma_{\text{SL}}}) \times 10^{-3}$$

vs.

$$|V(cb)|_{\text{excl}} = (39.2 \pm 0.6 \pm 1.0) \times 10^{-3}$$

(3.2)  $|V(ub)|$

$B \rightarrow l\nu X_u$

no need to 're-invent the wheel':

• for  $B \rightarrow l\nu X_u$  use same values of the HQP as determined in  $B \rightarrow l\nu X_c$

• yet given enough data can check it anyway

□ in principle  $\Gamma(B \rightarrow l\nu X_u)$  under better theoretical control than  $\Gamma(B \rightarrow l\nu X_c)$

Lepton energy endpoint spectrum ?

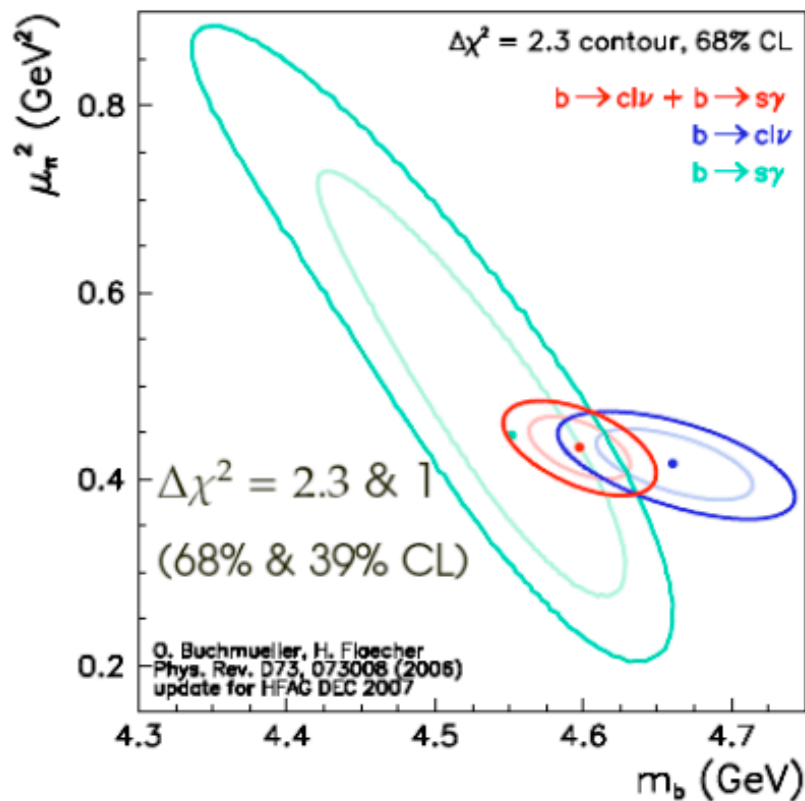
- ☹ model dependent!
- ☹ can get heavy quark distribution function from  $B \rightarrow \gamma X$ 
  - ☹ but only to leading order in  $1/m_b$
- ☹ endpoint spectrum different for  $SL B_u$  and  $B_d$  decays (WA)

Hadronic recoil mass spectrum !

$$B \rightarrow l\nu X_u$$

$$M_X < M_D \text{ vs. } E_l > [\sim] (M_B^2 - M_D^2)/2M_B \text{ vs. } q^2 > (M_B - M_D)^2$$

- ✂ cuts destroy straightforward applicability of OPE
- ✂ sensitivity to precise value of  $m_b$



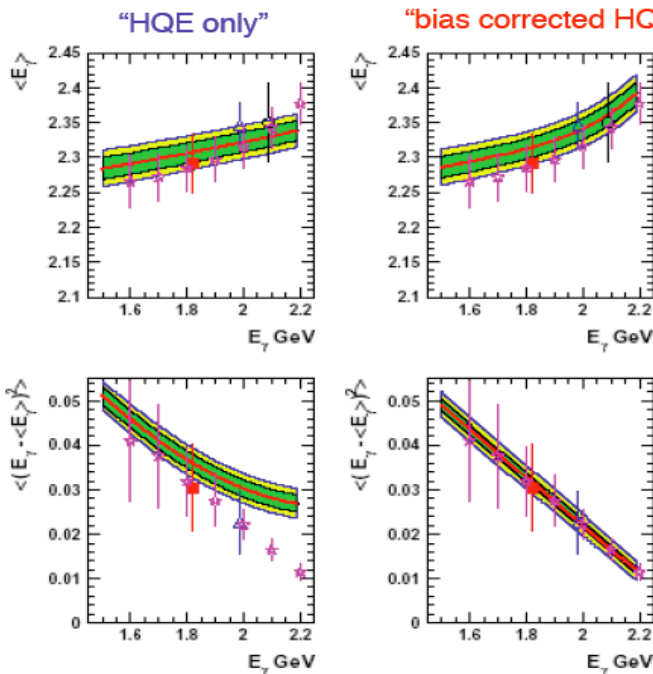
Should we 'toss out'  $B \rightarrow \gamma X$  moments due to severe cuts on  $E_\gamma$ ?

No!

- 👉 'Do not let the excellent be the enemy of the very good!'
- 👉 We have demonstrated that the cut dependence is under sufficient control -- the 'bias corrections'

### Consistency between $b \rightarrow s\gamma$ and $b \rightarrow c\ell\nu$

Use extracted HQE parameters from the  $c\ell\nu$  moment fit to predict the moments of the photon energy spectrum.



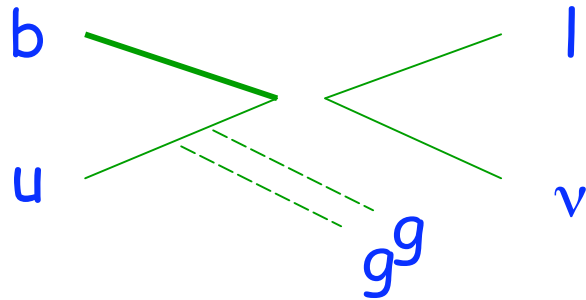
Moment measurements agree well with HQE prediction obtained from the  $c\ell\nu$  moment fit.  
Evidence that bias correction is needed for moments above  $E_\gamma > 1.8$  GeV

But we can do more ...  
→ Use the shape function parameter that fit the BELLE spectrum to obtain the moments as a function of the cut.  
(Test: agrees nicely at  $E_\gamma = 1.8$  GeV with the direct measurement from BELLE)

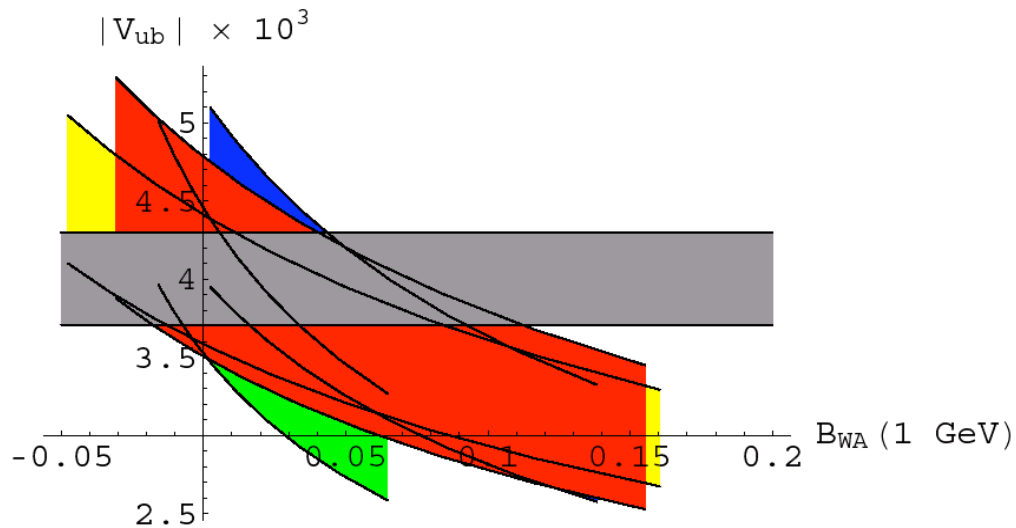
**Remarkable agreement with HQE prediction**  
Strong evidence, especially from the second moment, that bias corrections are needed above  $E_\gamma > 1.8$  GeV.

from O. Buchmueller

## Important concern: Weak Annihilation (WA)



- dominant contribution at high  $q^2$
- unambiguous signature: difference in  $B_d$  &  $B_u$  endpoint spectrum
- yet can have also sizable isoscalar contribution
  - ➔ need careful modeling



Preliminary Babar analysis of the  $q^2$  spectrum seems to suggest a Small WA contribution and  $V_{ub} \sim 0.0040$

P. Gambino, Valencia Super-B

From P. Gambino's FPCP talk

Kinetic scheme -- Gambino, Giordano, Ossola, Uraltsev --

$$|V(ub)|_{incl} = (3.94 \pm 0.15 |_{exp}^{+0.20} |_{th}^{-0.23}) \times 10^{-3}$$

-- BLNP --

$$|V(ub)|_{incl} = (3.99 \pm 0.14 |_{exp}^{+0.32} |_{th}^{-0.27}) \times 10^{-3}$$

[if same input values used in BLNP,  $|V(ub)|_{incl} \sim 4.1 \times 10^{-3}$ ]

vs.

$$|V(ub)|_{excl} = (3.5 \pm 0.4 \pm 0.1) \times 10^{-3}$$

$$|V(ub)|_{excl} = (3.5 \pm 0.4 |_{th} \pm 0.2 |_{sh} \pm 0.1 |_{exp}) \times 10^{-3}$$

→ no clear discrepancy between  $|V(ub)|_{incl}$  &  $|V(ub)|_{excl}$

↔ some tension with  $|V(ub)|_{CKMfit} = (3.57 \pm 0.17) \times 10^{-3}$

## My conclusions

- Theory error estimates for  $|V(ub)|_{incl}$  have not reached same level of maturity as for  $|V(cb)|_{incl}$
- ~ 5 % within reach in next few years
- need better understanding of  $WA$
- need higher accuracy on  $m_b$
- we are encountering a Calvinist scenario:  
many paths to heaven -- only success reveals Heaven's blessing
- ~ 2 % conceivable with data set from Super-B factory!

## IV "3/2 vs. 1/2"

Heavy Quark Symmetry  $\approx$  Heavy Quark Expans.

$$\sim H_{\text{Pauli}} = -A_0 + (i\partial - \mathbf{A})^2/2m_Q + \boldsymbol{\sigma} \cdot \mathbf{B}/2m_Q \rightarrow -A_0 \quad \text{as } m_Q \rightarrow \infty$$

i.e.,

infinitely heavy static quark, without spin dynamics,  
only colour Coulomb potential!

→ hadrons  $H_Q$  labeled by total spin  $S$  and by  $j_q = l_q + s_q$ :

□ ground states:  $[S | l_q | j_q] = [0, 1 | 0 | 1/2]$ :

PS -- B or D -- & V -- B\* or D\*

□ 1st excit. states:  $[0, 1 | 1 | 1/2]$  &  $[1, 2 | 1 | 3/2]$

4 P wave states: 2  $j_q = 3/2$  narrow states  
2  $j_q = 1/2$  broad states



2/3 - 3/4 of  $B \rightarrow l\nu X_c$  given by  $D/D^*$

→ charm can act as a heavy flavour

👉 what is the rest of  $X_c$  made up from?

👉 P wave states

HQ SR: narrow `3/2' have to dominate over broad `1/2'

QM, LQCD: same prediction to different numerical degrees

Data: somewhat ambiguous findings

- ❑ agree with expectations on narrow states
- ❑ ~ 15 - 20 % of final states of different nature
- 👉 non-resonant  $D/D^*\pi$ 's forming ~15% a priori not surpris.
- ❑ no obvious non-resonant contribution in data
- ❑ if observed broad structures `1/2', then ~~`3/2' → `1/2'!~~

?? Novel lesson on QCD ??

Can LHCb contribute?

## V On the Autonomy of $B_s$ Dynamics

original paradigm: need  $B_d$  &  $B_s$  to determine all 3 angles

$\phi_2/\alpha, \phi_1/\beta$  from  $B_d$  vs.  $\phi_3/\gamma$  from  $B_s$

new paradigm: can get all angles from  $B_d$

Furthermore NP in general will not obey SM relations between

$B$  and  $B_s$  decays

→  $B_s$  decays a priori independent chapter in nature's book  
on fundamental dynamics

$B_s(t) \rightarrow \psi\phi, \psi\eta, \phi\phi$  not a repetition of lessons from  
 $B_d$  &  $B_u$  decays!

## VI On $B \rightarrow \tau\nu D, \tau\nu X$

$B \rightarrow \tau\nu D$  could be affected by  $H^\pm-X$

• hadronization effects do not drop out from

$\Gamma(B \rightarrow \tau\nu D)/\Gamma(B \rightarrow \mu\nu D)$  at finite quark masses

[1 FF for  $B \rightarrow \mu\nu D$ , 2 FFs for  $B \rightarrow \tau\nu D$ ]

• Uraltsev's BPS approximation can help:

□ validate it in  $B \rightarrow \mu\nu D$

□ apply it to  $B \rightarrow \tau\nu D$

$B \rightarrow \tau\nu X_c$  could be affected by  $H^\pm-X$

its SM size been evaluated in '94 (Neubert et al.)

• now we can do it much better: ingredients there to

predict  $\Gamma(B \rightarrow \tau\nu X)|_{SM}$  to within very few %

• even if no NP found there, novel lessons on onset of duality!

## VII Outlook

We have come a long way in the last 15 years

- in B decay dynamics have established theoretical control over non-pert. dynamics on the very few % level with
    - detailed theoretical error budgets
    - that can be defended
  - Basis for this progress two-fold
    - robust theoretical framework
    - challenged & complemented by detailed high quality data
  - emerging synergies between diff. theoret. technologies
  - further progress likely[possible]:  $\delta V_{cb} \sim 1\%$ ,  $\delta V_{ub} \sim 5\%$  [2%]
  - LHCb will be highly successful --
- $B_s$  = indep. chapter in nature's book on fundamental dynamics  
-- but not complete the agenda of heavy flavour dynamics

A final thought:

Models with extra dimensions have several ad-hoc features

...

yet are sufficiently radical/crazy to push our thinking out of the comfort zone of a possible dead end into new fruitful directions --

i.e. are a most helpful `imagination stretcher'!