

**MEASURING FLAVOR MIXING  
WITH  
MINIMAL FLAVOR VIOLATION  
AT THE LHC**

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# Flavor and CP violation within the Standard Model

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quark masses from Yukawa-Higgs coupling

$$\bar{Q}Y_u\langle h^C\rangle U, \quad \bar{Q}Y_d\langle h\rangle D \quad \langle h\rangle \simeq 174 \text{ GeV}$$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 1 & \lambda & \lambda^3 \\ -\lambda & 1 & \lambda^2 \\ -\lambda^3 & -\lambda^2 & 1 \end{pmatrix}; \quad \lambda \simeq 0.22$$

3 generations = 10 parameter in flavor & CP sector: **6 masses, 3 angles and 1 phase in CKM-matrix** unitary, complex, hierarchical

$$|V_{us}| = 0.2257(21), \quad |V_{cb}| = 41.6 \pm 0.6 \cdot 10^{-3}, \quad |V_{ub}| = 4.31 \pm 0.3 \cdot 10^{-3}$$

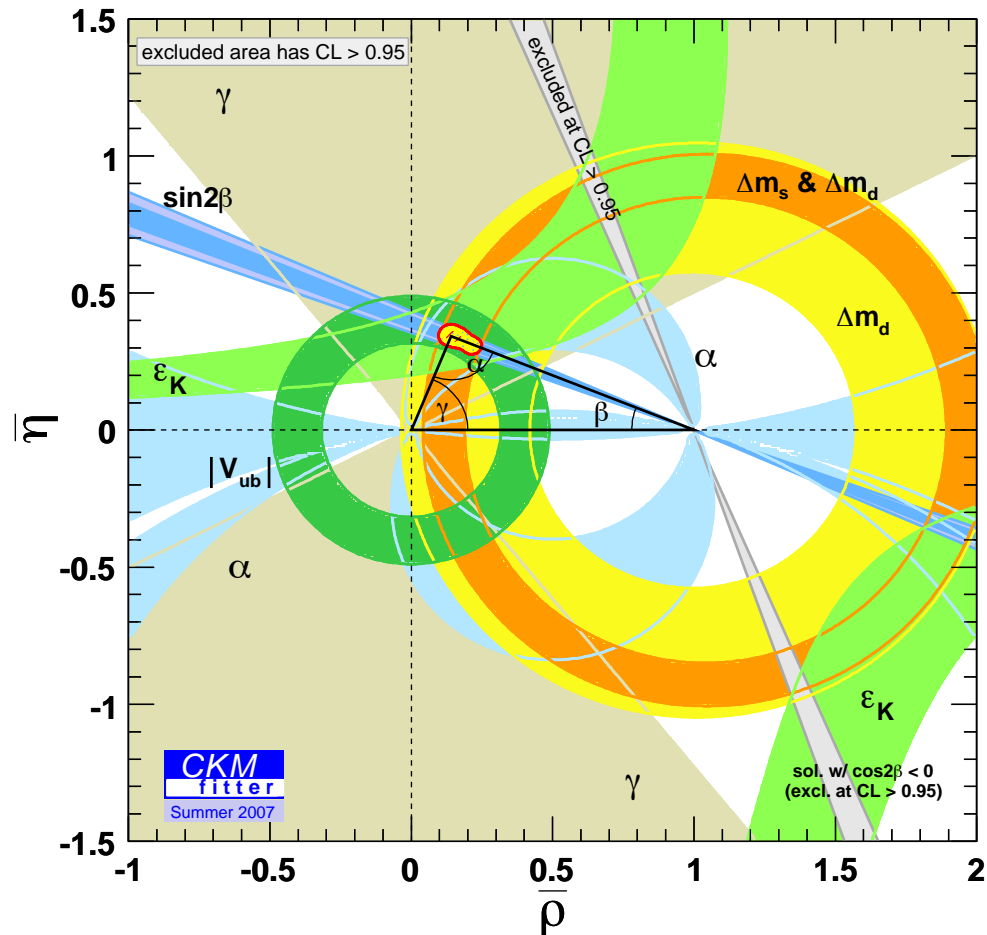
$$\beta(\text{measured}) = (21.23_{-0.99}^{+1.03})^\circ$$

-third generation is decoupled from the first two

-CP phase is order one

# Testing the Standard Model with Flavor and CP

the unitarity triangle  $V_{ub}V_{ud}^* + V_{cb}V_{cd}^* + V_{tb}V_{td}^* = 0$



-fit consistent; contains tree and loop processes of  $B, K$ -mesons

# New Physics in rare Processes, Where is it ?

$$\Delta m_s^{\text{SM}} \sim (V_{tb}^* V_{ts})^2 \times \frac{g^4}{16\pi^2} \times \frac{(\bar{b}\Gamma_s)(\bar{b}\Gamma'_s)}{m_W^2}$$

$$\Delta m_s^{\text{NP}} \sim \text{flavor} \times \text{loop/tree} \times \frac{(\bar{b}\Gamma_s)(\bar{b}\Gamma'_s)}{\Lambda^2}$$

	New Physics from loops	tree level New Physics
$B_s - \bar{B}_s$	$\Lambda \gtrsim m_W /  V_{ts}  \sim O(2 - 3) \text{ TeV}$	$\Lambda \gtrsim 4\pi m_W /  V_{ts}  \sim O(30) \text{ TeV}$
$B_d - \bar{B}_d$	$\Lambda \gtrsim m_W /  V_{td}  \sim O(10 - 15) \text{ TeV}$	$\Lambda \gtrsim 4\pi m_W /  V_{td}  \sim O(100) \text{ TeV}$
“SM” flavor	$\Lambda \gtrsim m_W \sim O(100) \text{ GeV}$	$\Lambda \gtrsim 4\pi m_W \sim O(1) \text{ TeV}$

Is the absence of NP signals in FCNCs an accident (we haven't looked at the right observables yet) , or is there a symmetry behind?

flavor and CP in SM:  $-\mathcal{L}_Y = \bar{Q}Y_U h^C U + \bar{Q}Y_D h D + \bar{L}Y_E h E + h.c.$

flavor symmetry:  $U(3)^5 \xrightarrow{Y} U(1)_B \times U(1)_L \times U(1)_Y$

non-abelian quark part:  $G_F \equiv SU(3)_Q \times SU(3)_D \times SU(3)_U$

Yukawas are spurions of  $G_F$ :  $Y_D(3, \bar{3}, 1)$ ,  $Y_U(3, 1, \bar{3})$

**Minimal Flavor Violation (MFV) =  $Y_D, Y_U$  are the only spurions of flavor  $G_F$  breaking** Chivukula, Georgi '87; d'Ambrosio et al '02

MFV is property of the Standard Model.

MFV: potential organizing principle for New Physics

non-symmetry based definitions: Ali, London '99; Buras<sup>2</sup> '00

# Solutions to the NP Flavor Puzzle

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unless flavor is "as in the SM":  $\Lambda_{NP} \gg \sqrt{s_{LHC}} \sim \Lambda_{EWKSB}$

model-independent solutions: MFV and variants:

NMFV Agashe et al '05; Feldmann, Mannel '06

hierarchical wave functions Davidson et al '07; previously: Nelson, Strassler "suppressing flavor anarchy" '00

solutions within SUSY:

alignment+flavor symmetry Nir, Seiberg '93

decoupling "effective SUSY" (first 2 generation squarks heavy) Cohen,

Kaplan, Nelson '96

extended R-symmetry ( $A$ -terms and Majorana masses vanish) Kribs,

Poppitz, Weiner '07

# What does MFV imply for SUSY? Simplification !

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superpotential (unbroken R-parity):

$$W_{MSSM} = QY_u H_u U + QY_d H_d D + LY_e H_d E + \mu H_d H_u \quad \text{MFV !}$$

SUSY-breaking constrained by MFV:

$$\tilde{Q}^\dagger \tilde{m}_Q^2 \tilde{Q} + \tilde{U}^\dagger \tilde{m}_U^2 \tilde{U} + \tilde{D}^\dagger \tilde{m}_D^2 \tilde{D} + (A_u \tilde{Q} H_u \tilde{U}^* + A_d \tilde{Q} H_d \tilde{D}^* + h.c.)$$

$$\tilde{m}_Q^2 = \tilde{m}^2 (a_1 \mathbf{1} + b_1 Y_u Y_u^\dagger + b_2 Y_d Y_d^\dagger)$$

$$\tilde{m}_U^2 = \tilde{m}^2 (a_2 \mathbf{1} + b_5 Y_u^\dagger Y_u + c_1 Y_u^\dagger Y_d Y_d^\dagger Y_u)$$

$$A_u = A (a_4 \mathbf{1} + b_7 Y_d Y_d^\dagger) Y_u \quad \text{etc} \quad \text{D'Ambrosio et al '02}$$

predictions:

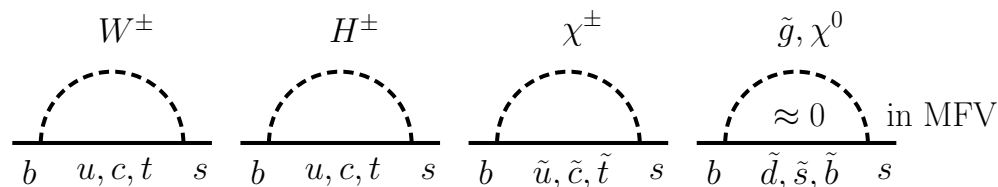
- 3rd generation decoupled (via  $V_{CKM}$ )
- highly degenerate squarks of 1st and 2nd generation:

$$\Delta m / m_0 \sim \lambda_c^2 / 2; \quad \Delta m < 1 \text{ GeV} \quad \text{GH, Schmaltz '01}$$

-squark spectrum is 10+2 (8+4 for large  $\tan \beta$ )

# Testing Minimal Flavor Violation: 1. loops

FCNC quantum loops:



$O_{10} \sim \bar{s}_L \gamma_\mu b_L \leftrightarrow \bar{s}_L z b_L$   
  
 $\sim V_{tb} V_{cs}^* \frac{m_t}{\tan\beta} (\delta_{23}^u)_{LR}$   
*no tanβ enhancement*

**constraints from K,D,B-physics “penguins”, meson-mixing**

potentially huge effects if flavor is not minimally broken.

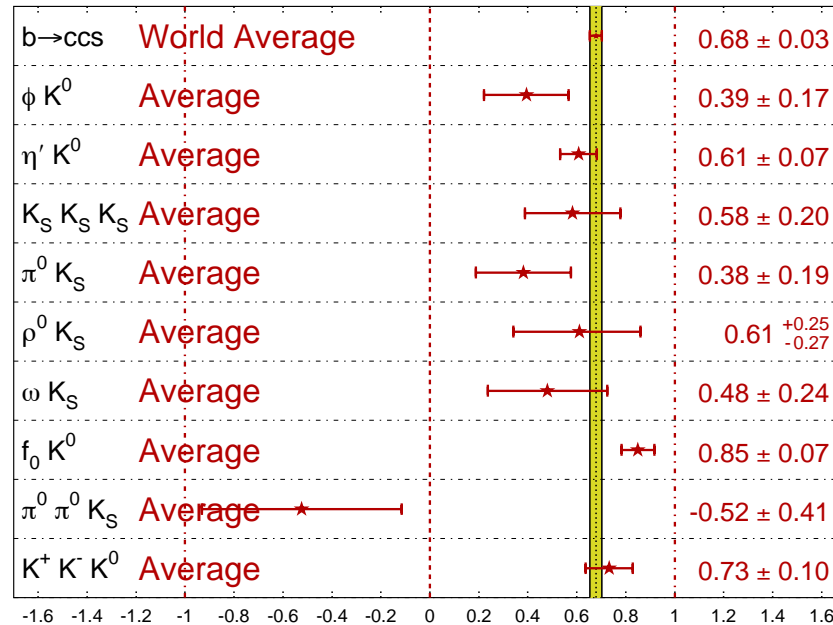
ongoing tests at B-factories and Tevatron; extended searches at LHC



# Challenges for Minimal Flavor Violation

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFAG  
LP 2007  
PRELIMINARY



$$\eta_{CP} \sin 2\beta(\underbrace{(\bar{s}s)K_S}_{FCNC}) = \sin 2\beta(\underbrace{(\bar{c}c)K_S}_{tree}) + \underbrace{\left| \frac{V_{ub}V_{us}^*}{V_{tb}V_{ts}^*} \right|}_{0.02} \cdot \#(hadronic)$$

non-CKM CP-phases, right-handed currents, CKM-links broken,

e.g.,  $\mathcal{B}(B_d \rightarrow \mu\mu)/\mathcal{B}(B_s \rightarrow \mu\mu) \neq |f_{B_d}V_{td}|^2/|f_{B_s}V_{ts}|^2$ ;

$B \rightarrow K^{(*)}ll$  CP observables in angular analysis [Bobeth,GH,Piranishvili 0805.2525](#)

# Some (further) Standard Model tests with $b$ -physics

	experiment	SM	comments
$a_{CP}(b \rightarrow s\gamma)$	$0.4 \pm 3.6 \%$	$0.42 \pm 0.17 \%$ <small>hep-ph/0312260</small>	CPX in $bs\gamma, g$
$a_{CP}(b \rightarrow d/s\gamma)$	$-0.110 \pm 0.116$ <small>BaBar'05</small>	$10^{-9}$ <small>hep-ph/0312260</small>	MFV test
$S_{K_S\pi^0\gamma}$	$0.00 \pm 0.28$ <small>Belle/BaBar'05</small>	$-2m_s/m_b$	V+A FCNCs
spin $\Lambda_b \rightarrow \Lambda\gamma$	—	$\sim m_s/m_b$ <small>GH,Kagan '00; '07</small>	V+A FCNCs
$\mathcal{B}(B \rightarrow X_s g)$	$< 9\%$ <small>CLEO'97</small>	$5.0 \pm 1.0 \cdot 10^{-3}$	NP in $bsg$
<b>TDCPA</b> $b \rightarrow s\bar{s}s$	$S_{avg} = 0.53 \pm 0.05$	$\sin 2\beta + \Delta S$	CPX
$\mathcal{B}(B \rightarrow X_s \bar{\mu}\mu)$	$4.3 \pm 1.2 \cdot 10^{-6}$	$4.3 \pm 0.7 \cdot 10^{-6}$	$q^2$ -spectra
$a_{CP}(B \rightarrow X_s \bar{\ell}\ell)$	$-0.22 \pm 0.26$	$-0.2 \pm 0.2 \%$ <small>hep-ph/9812267</small>	CPX
$A_{FB}^{CP}(B \rightarrow K^* \bar{\ell}\ell)$	—	$\lesssim 10^{-3}$ <small>Buchalla, GH, Isidori'00</small>	CPX in $bsZ$
$R_K \mu\mu$ vs. $ee$	$1.06 \pm 0.48$ <small>BaBar'05</small>	$1 + \mathcal{O}(m_\mu^2/m_b^2)$ <small>GH, Krüger 03</small>	non-SM Higgs
$\mathcal{B}(B \rightarrow K\nu\bar{\nu})$	$< 3.6 \cdot 10^{-5}$ <small>Belle'05</small>	$3.8_{-0.6}^{+1.2} \cdot 10^{-6}$	$O(10)$ from SM
$\mathcal{B}(B_s \rightarrow \mu^+\mu^-)$	$< 4.7 \cdot 10^{-8}$ <small>CDF'07</small>	$3.2 \pm 1.5 \cdot 10^{-9}$	$O(15)$ from SM
$\mathcal{B}(B_s \rightarrow \tau^+\tau^-)$	$< \mathcal{O}(5\%)$	$7.2 \pm 1.1 \cdot 10^{-7}$	$O(10^5)$ from SM
$\mathcal{B}(B_d \rightarrow \tau^+\tau^-)$	$< 3.4 \cdot 10^{-3}$ <small>BaBar'05</small>	$2.1 \pm 0.3 \cdot 10^{-8}$	$O(10^5)$ from SM
$R_{\ell\ell}$ (Bd vs. Bs)	—	$ V_{td}/V_{ts} f_{Bd}/f_{Bs} ^2$	LHC-MFV test
ang $aB \rightarrow K\ell\bar{\ell}$	$O(1)$ <small>BaBar, Belle</small>	$\%$ <small>Bobeth, GH, Piranishvili 07</small>	new Higgses

SUSY FCNC rates can be sizeable  $\mathcal{O}(10\%)$  Hurth, Porod '03

$$\mathcal{B}(\tilde{t}_{1,2} \rightarrow \tilde{\chi}^+ b) \sim 50\% \text{ and } \mathcal{B}(\tilde{u} \rightarrow \tilde{\chi}^+ b) \sim 13\%$$

Problem for squark mass determination from edges in cascades (such analyses assume implicitly MFV, i.e.,  $\tilde{m}_1^2 = \tilde{m}_2^2 \neq \tilde{m}_3^2$  and FCNC= 0).

Flavored di-squark-production  $pp \rightarrow \tilde{q}\tilde{q}' X$  Klasen et al '05, '07, Rainwater '05

Study with 2 down-quark singlets show that there is discriminating power between MFV or not Grossmann, Nir, Thaler, Volansky, Zupan '07

Charged-Higgs-production with or without flavor  $pp \rightarrow H^+ X,$

$$pp \rightarrow H^+ + jet + X$$
 Diaz-Cruz, He, Yuan; Dittmaier, GH, Plehn, Spannowsky '07

slepton mass splitting Nomura et al'07; Feng et al '07 secondary vertex from  $\tilde{t}$  GH, Nir'08

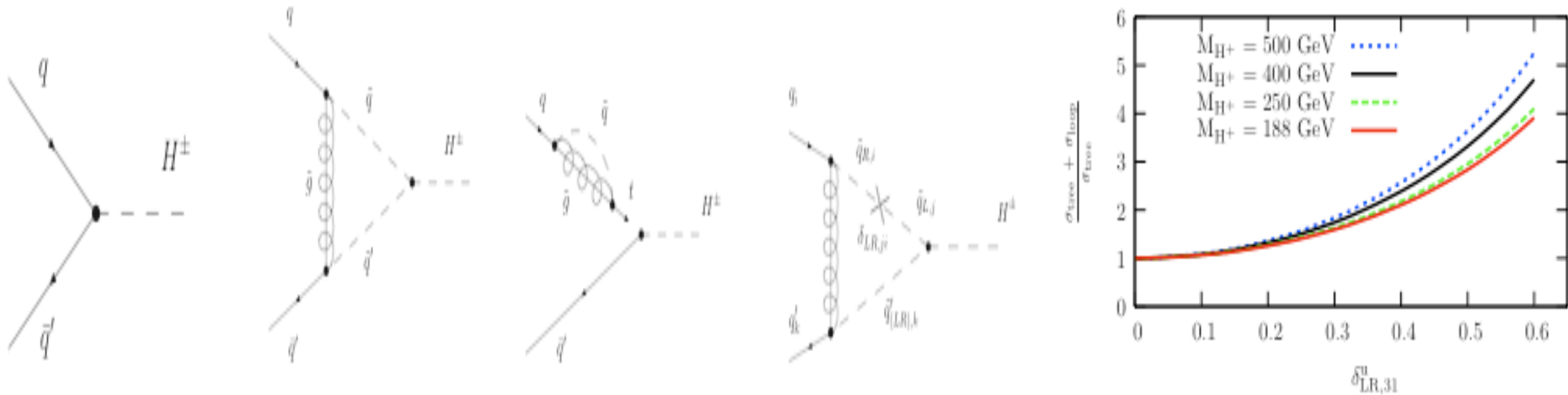
# Testing Minimal Flavor Violation: 2. direct at the LHC

potentially huge effects if flavor is not minimally broken.

MFV-null test: if we see signal in particular reaction, MFV (or MSSM) must be broken:

Charged-Higgs-production with or without flavor  $pp \rightarrow H^+ X$ ,

$pp \rightarrow H^+ + jet + X$  Diaz-Cruz,He,Yuan; Dittmaier,GH,Plehn,Spannowsky '07



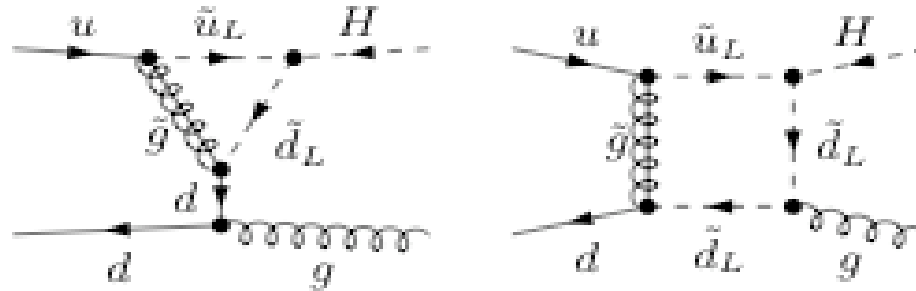
sensitive to flavor mixing essentially unconstrained by K,D,B-physics

# Charged-Higgs plus jet $qg \rightarrow q' H^+$

idea: avoid chiral suppression by extra gauge boson, e.g.,

$$\bar{Q} \gamma_\mu Q H_u D^\mu H_u^C.$$

D-term contribution from  $H^+ \tilde{q} \tilde{q}'$  finite in chiral limit and MFV.



$\sigma_{pp \rightarrow H^+ j}$	2HDM	MFV D-term only	MFV with $m_q \neq 0$	beyond MFV
$\tan \beta = 3$	$2.5 \cdot 10^{-1} fb$	$6.7 \cdot 10^{-4} fb$	$\simeq \sigma_{2HDM}$	$14.3 fb$

**O(30) enhancement over MFV (small/moderate  $\tan \beta$ )**

In MFV, mixing between third and other generations is suppressed:

$$\tilde{m}_Q^2 = \tilde{m}^2(a_1 \mathbf{1} + b_1 Y_u Y_u^\dagger + b_2 Y_d Y_d^\dagger) \quad (\tilde{m}_Q^2)_{23} = \tilde{m}^2 b_2 \lambda_b^2 V_{cb} V_{tb}^*$$

There is an opportunity to measure the mixing because it is so small: measure lifetime instead of branching ratio GH, Nir '08

This is a counterexample to the lore that colliders determine only masses and mixing are measured in low energy experiments

requirement:  $\tilde{t} \rightarrow c\chi^0$  dominant decay & sufficiently suppressed rate

stop lifetime  $\tau_{\tilde{t}} \sim \text{ps} \left( \frac{m_{\tilde{t}}}{100 \text{ GeV}} \right) \left( \frac{0.03}{\Delta m / m_{\tilde{t}}} \right)^2 \left( \frac{10^{-5}}{Y} \right)^2$  is long

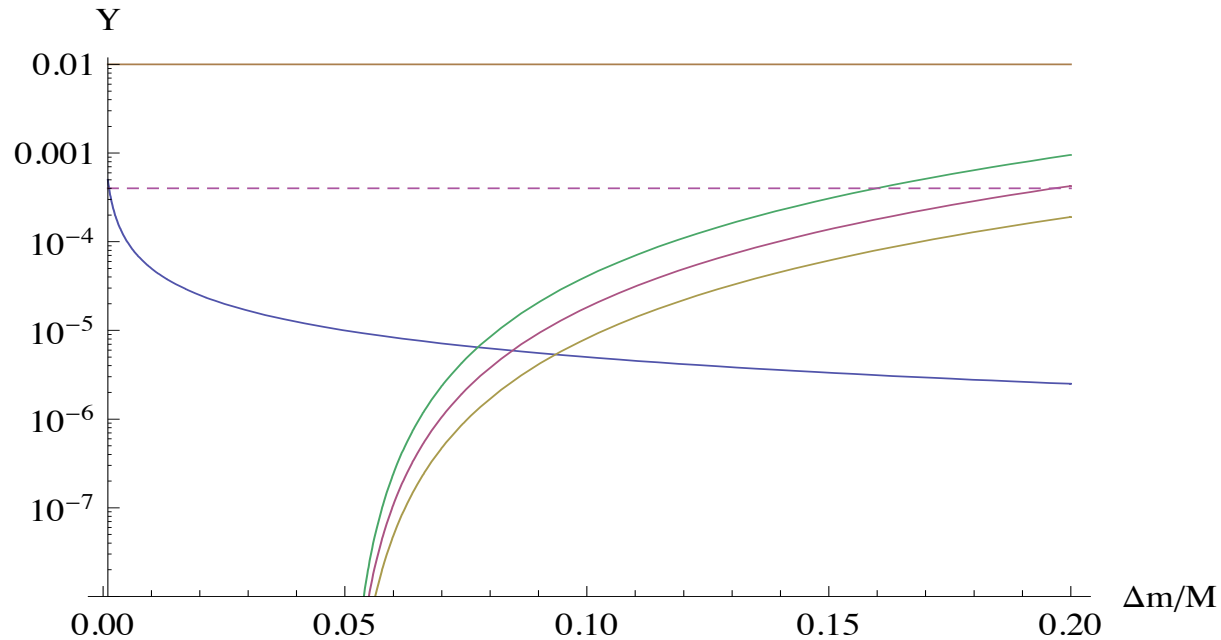
$\Delta m = m_{\tilde{t}} - m_{\chi^0}$ ; macroscopic decay length (small  $Y \sim \lambda_b^2 V_{cb}$ )

unique to MFV

$\Delta m > m_b$  opens up tree level 4-body decays  $\tilde{t} \rightarrow b\chi^0 l\nu$ .

$$\frac{\Gamma(\tilde{t} \rightarrow b\chi^0 l\nu)}{\Gamma(\tilde{t} \rightarrow c\chi^0)} \approx \frac{g^6 |V_{tb}|^2}{2} \frac{(\Delta m - m_b)^7}{[Y(\Delta m/M)]^2 M m_W^4 m_{\chi^+}^2}$$

solid curve:  $\beta\gamma\tau_{\tilde{t}} > 0.1mm$ ; dashed:  $Y_{min}$  alignment; horizontal solid line  $Y \simeq \lambda_c$  anarchy + extended R-symm. GH, Nir '08



light stop ingredient of EWK baryogenesis; supports coannihilation of relic density; stop NLSP in hypercharged anomaly mediation

Dermisek etal'07

- The flavor structure of the SM is very specific, hence, very predictive. (CKM, CP-violation)
- This flavor breaking could be also realized by symmetry in physics beyond-the-SM “Minimal Flavor Violation “.
- If MFV, this implies certain form of quark-partners spectrum and mixing.
- The LHC can answer these and many other questions; complementary (direct/indirect; quarks & leptons)
- The possibility of a stop decay length measurement shows that ATLAS/CMS could have much more to say about flavor and mixing than usually thought.



back up slides

# Charged-Higgs plus Jet $qg \rightarrow q' H^+$

discovery of charged-Higgs prod. would signal breakdown of SM and non-standard flavor/Higgssector, including breakdown of MFV.

works for small  $\tan \beta$  !

Dittmaier,GH,Plehn,Spanowsky '07

