

*Branching Ratios and Polarization
in $B \rightarrow VV, VA, AA$ Decays*

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Introduction

■ We have studied $B \rightarrow S (P,V)$, AP before. It is natural to generalize to AV, AA and revisit VV modes

-- Generalization is highly nontrivial: 3P_1 & 1P_1 axial mesons which have very different decay constants & light cone distribution amplitudes

■ Polarization puzzle in $\bar{B} \rightarrow VV$ decays

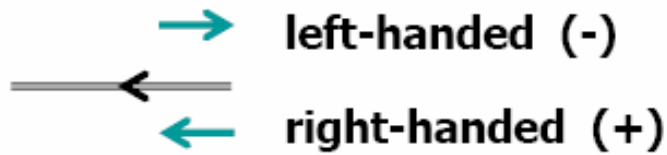
$$\bar{A}_0 : \bar{A}_- : \bar{A}_+ = 1 : \frac{\Lambda}{m_b} : \left(\frac{\Lambda}{m_b} \right)^2$$

In transversity basis $A_\perp = (A^- + A^+) / \sqrt{2}$, $A_\parallel = (A^- - A^+) / \sqrt{2}$

$$f_T \equiv f_\parallel + f_\perp = 1 - f_L = O(m_V^2 / m_B^2), \quad f_\parallel / f_\perp = 1 + O(m_V / m_B)$$

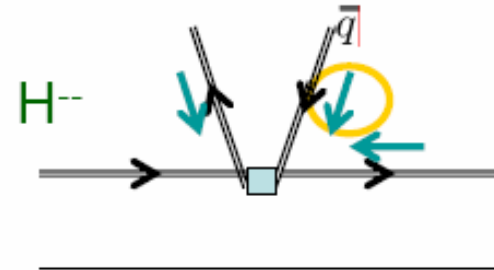
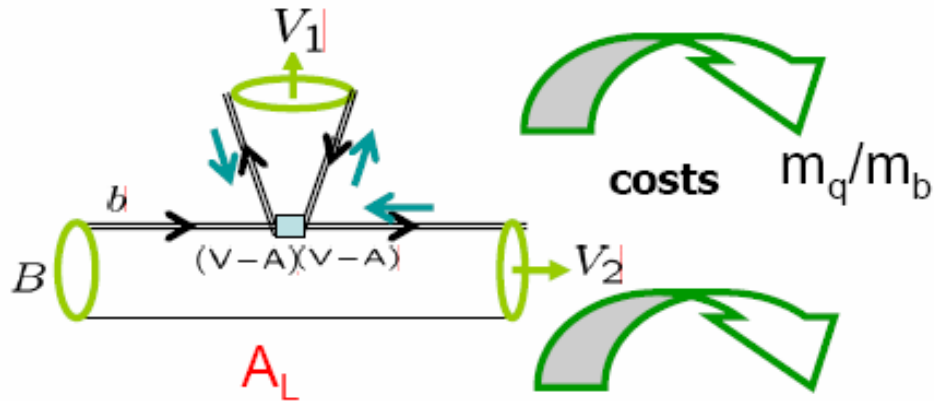
Why is f_T sizable ~ 0.5 in $B \rightarrow K^* \phi$ decays ?

$\bar{B} \rightarrow VV$ polarizations



Transverse

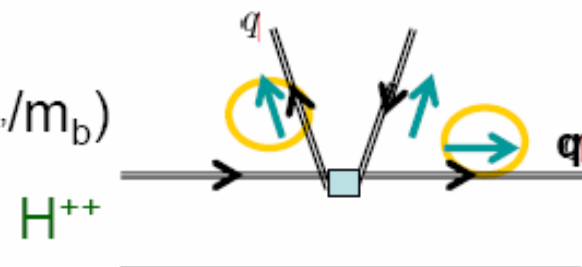
Longitudinal



$$+ \rightarrow A_{\parallel}, - \rightarrow A_{\perp}$$

$$A_L \gg A_{\parallel} \approx A_{\perp}$$

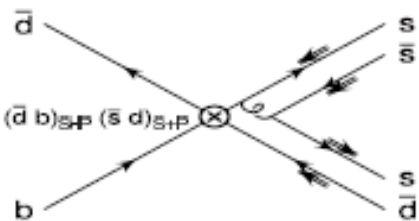
costs $(m_q/m_b)(m_{q'}/m_b)$



The longitudinal component dominates

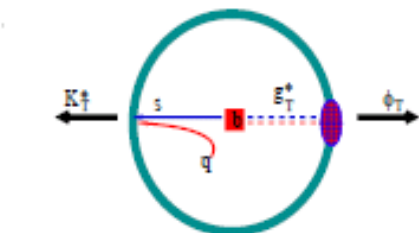
$$A^{00} \gg A^{-} \gg A^{++}$$

Polarization Anomaly: Some Ad hoc Models in SM



- **Annihilation diagram** ([hep-ph/0405134](#)) Kagan

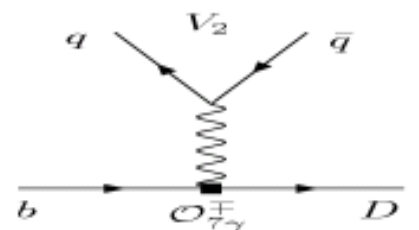
formally suppressed $1/m_b$
not conclusive (vary free parameters)



- **Transverse gluon from $b \rightarrow sg$** ([hep-ph/0408007](#))

analogy with γ from $B \rightarrow K^* \gamma$
seems to be suppressed, not conclusive

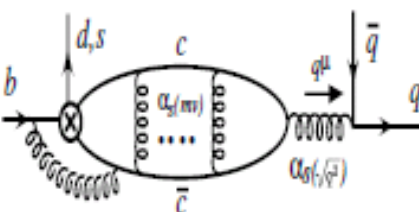
Hou, Nagashima



- **EM penguin** ([hep-ph/0512258](#))

Beneke, Rohrer, Yang

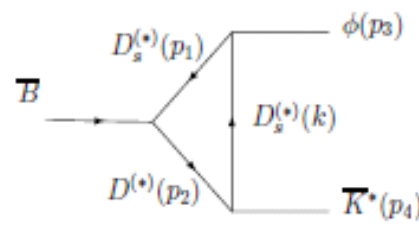
similar polarization to $B \rightarrow K^* \gamma$
appears only for neutral vector mesons



- **Charming penguins** ([hep-ph/0401188](#))

Bauer, Pirjol, Rothstein, Stewart

rely on free parameters, not conclusive

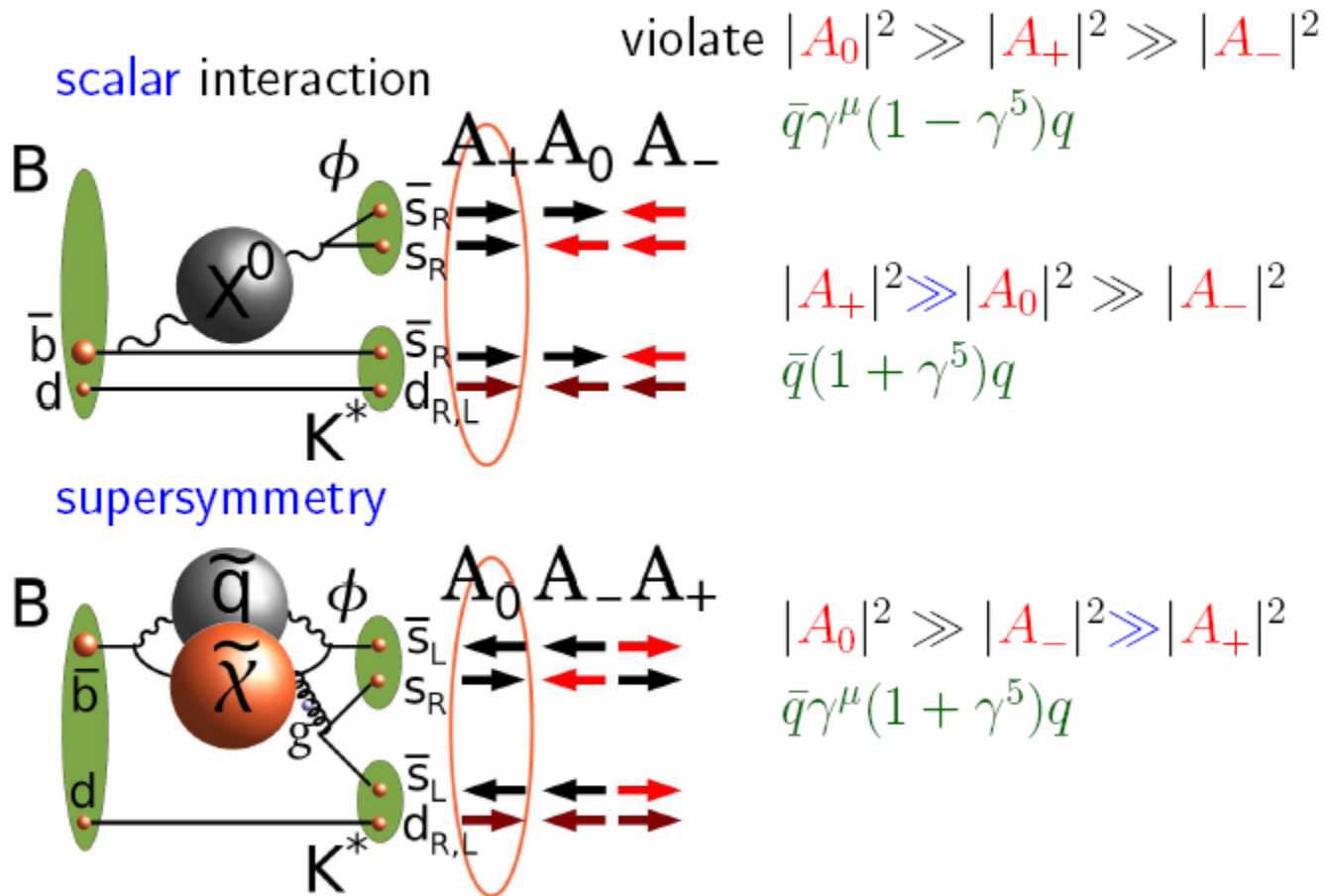


- **Long-distance rescattering** ([hep-ph/0409317](#))

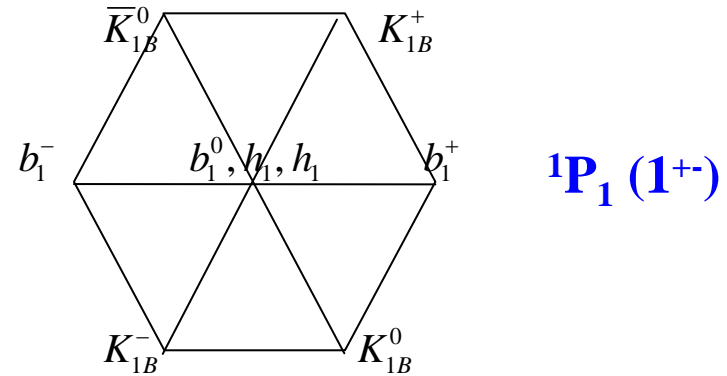
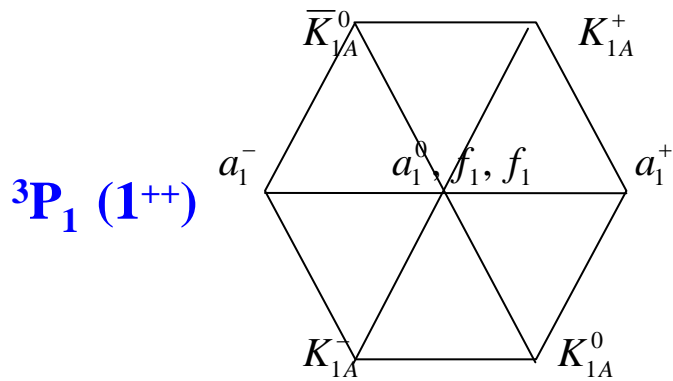
model-dependent, constrained by other data
expect $f_L \sim f_{\parallel} \gg f_{\perp}$ (?)

HYC, Chua, Soni;
Colangelo, De Farzio
Pham

Possible New Physics in Polarization



Axial-vector mesons



For $J^P=1^+$ axial-vector mesons, two nonets have been observed:

■ 3P_1 nonet ($S=1$)

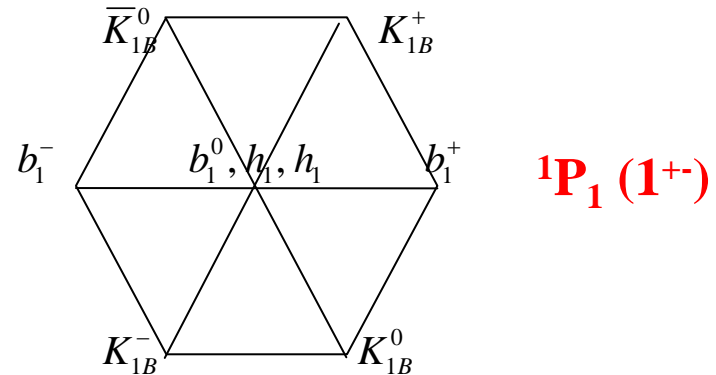
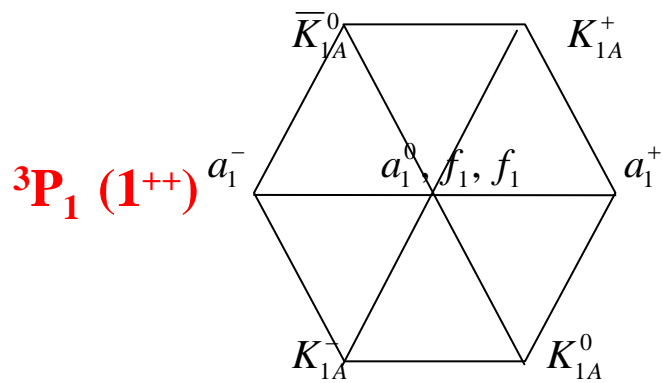
$l=0$: $f_1(1285)$, $f_1(1420)$, $l=1/2$: K_{1A} , $l=1$: $a_1(1260)$,

■ 1P_1 nonet ($S=0$)

$l=0$: $h_1(1170)$, $h_1(1380)$, $l=1/2$: K_{1B} , $l=1$: $b_1(1235)$

K_{1A} , $K_{1B} \rightarrow K_1(1270)$, $K_1(1400)$

Mixing angles



- 3P_1 states $f_1(1285)$ & $f_1(1420)$ have mixing [so are 1P_1 states $h_1(1170)$ & $h_1(1380)$]

$$|f_1(1285)\rangle = |f_1\rangle \cos \theta_{3P_1} + |f_8\rangle \sin \theta_{3P_1}, \quad |f_1(1420)\rangle = -|f_1\rangle \sin \theta_{3P_1} + |f_8\rangle \cos \theta_{3P_1}.$$

$$\cos^2 \theta_{3P_1} = \frac{4m_{K_{1A}}^2 - m_{a_1}^2 - 3m_{f_1(1285)}^2}{3(m_{f_1(1420)}^2 - m_{f_1(1285)}^2)},$$



magnitude of θ

$$\tan \theta_{3P_1} = \frac{4m_{K_{1A}}^2 - m_{a_1}^2 - 3m_{f_1(1420)}^2}{2\sqrt{2}(m_{a_1}^2 - m_{K_{1A}}^2)}.$$



sign of θ

θ_{3P_1} & θ_{1P_1} depend on the K_{1A} - K_{1B} mixing angle

- No a_1 and b_1 mixing due to opposite C or G parities

- In SU(3) limit, K_{1A} & K_{1B} do not get mixed. However, they have admixture due to strange and light quark mass difference

$$\begin{aligned}
 K_1(1270) &= K_{1A} \sin \theta_K + K_{1B} \cos \theta_K & \bar{K}_1(1270) &= -K_{1A} \sin \theta_K + K_{1B} \cos \theta_K \\
 K_1(1400) &= K_{1A} \cos \theta_K - K_{1B} \sin \theta_K & \bar{K}_1(1400) &= K_{1A} \cos \theta_K + K_{1B} \sin \theta_K
 \end{aligned}$$

- PDG $\Rightarrow |\theta_K| \approx 45^\circ$

- Strong decays $K_1(1270), K_1(1400) \rightarrow K\rho, K^*\pi$ and their masses $\Rightarrow \theta_K = \pm 32^\circ, \pm 56^\circ$
(Suzuki, '93)

$$\tau \rightarrow K_1(1270)\nu_\tau, K_1(1400)\nu_\tau \Rightarrow \theta_K = \pm 37^\circ, \pm 58^\circ \quad (\text{HYC, '03})$$

Sign of θ_K depends on the phase convention of states. It

can be inferred from $B \rightarrow K_1\gamma$ decays (HYC, Chua, '05; Yang, Hatanaka, '08)

$$\frac{B(B \rightarrow K_1(1270)\gamma)}{B(B \rightarrow K_1(1400)\gamma)} = \begin{cases} 10.1 \pm 6.2 \quad (280 \pm 200); & \text{for } \theta_{K_1} = -58^\circ \quad (-37^\circ), \\ 0.02 \pm 0.02 \quad (0.05 \pm 0.04); & \text{for } \theta_{K_1} = +58^\circ \quad (+37^\circ). \end{cases}$$

$$Br(B^+ \rightarrow K_1^+(1270)\gamma) = (4.3 \pm 0.9 \pm 0.9) \times 10^{-5}$$

$$Br(B^+ \rightarrow K_1^+(1400)\gamma) < 1.5 \times 10^{-5}$$

Belle measurement favors a negative θ

Decay constants

$$\langle A(p, \varepsilon) | \bar{q} \gamma_\mu \gamma_5 q' | 0 \rangle = i f_A m_A \varepsilon_\mu^*, \quad \langle A(p, \varepsilon) | \bar{q} \sigma_{\mu\nu} \gamma_5 q' | 0 \rangle = -f_A^\perp (\varepsilon_\mu^* p_\nu - \varepsilon_\nu^* p_\mu)$$

↪ scale dependent

- Decay constant of b_1° vanishes due to $C[b_1] = -$ and $CA_\mu C^{-1} = A_\mu$
- Decay constant of charged b_1^\pm vanishes in isospin limit due to $G[b_1] = +$ & $GA_\mu G^{-1} = -A_\mu$. We obtain $f[b_1^+] = 0.6 \pm 0.2$ MeV, $f[b_1^-] = -0.6 \pm 0.2$ MeV
- In SU(3) limit

$$M_a^b(^3P_1) \rightarrow M_b^a(^3P_1), \quad M_a^b(^1P_1) \rightarrow -M_b^a(^1P_1), \quad (a, b = 1, 2, 3).$$

Since $(A_\mu)_a^b \rightarrow (A_\mu)_b^a$ under charge conjugation $\Rightarrow f[^1P_1] = 0$ in SU(3) limit

By the same token, $f^\perp[^3P_1] = 0$ in the same limit

| | | | | |
|-------------------|--------------|--------------|--------------|--------------|
| 3P_1 | $a_1(1260)$ | f_1 | f_8 | K_{1A} |
| $f_{^3P_1}$ | 238 ± 10 | 245 ± 13 | 239 ± 13 | 250 ± 13 |
| 1P_1 | $b_1(1235)$ | h_1 | h_8 | K_{1B} |
| $f_{^1P_1}^\perp$ | 180 ± 8 | 180 ± 12 | 190 ± 10 | 190 ± 10 |

QCDSR by
K.C. Yang

Form factors for $B \rightarrow A$

- ISGW (Isgur-Scora-Grinstein-Wise) non-relativistic quark model ('89,'95)
- Covariant light-front quark model (Chua,Hwang, HYC, '04)
Relativistic effects in B-to-light transitions at $q^2=0$ are important
- Light cone sum rules (K.C. Yang, '07,'08)
- pQCD approach (W. Wang, R.H. Li, C.D. Lu, hep-ph/0711.0432)

| | ISGW2 | CQM | CLF | LQSR | pQCD | expt |
|-----------------|-------|------|------|------|------|-------------|
| $V_0^{Ba_1}(0)$ | 1.01 | 1.20 | 0.13 | 0.30 | 0.34 | ~ 0.31 |

$B \rightarrow a_1$ form factors predicted by ISGW2 & CQM models are too large !

ISGW2, QCDSR: $f [^1P_1]$, $f [^3P_1]$ of the same sign

$B \rightarrow ^1P_1$ and $B \rightarrow ^3P_1$ form factors are opposite in sign

θ_K is negative

CLFQM, pQCD: $f [^1P_1]$, $f [^3P_1]$ have opposite signs

$B \rightarrow ^1P_1$ and $B \rightarrow ^3P_1$ form factors of same sign

θ_K is positive

Light-cone distribution amplitudes (LCDAs)

chiral-even

$$\langle A(P, \lambda) | \bar{q}_1(y) \gamma_\mu \gamma_5 q_2(x) | 0 \rangle = i m_A \int_0^1 du e^{i(u py + \bar{u} px)} \left\{ p_\mu \frac{\epsilon^{(\lambda)*} z}{pz} \Phi_{\parallel}(u) + \epsilon_{\perp\mu}^{(\lambda)*} g_{\perp}^{(a)}(u) \right\}$$

$$\langle A(P, \lambda) | \bar{q}_1(y) \gamma_\mu q_2(x) | 0 \rangle = -i m_A \epsilon_{\mu\nu\rho\sigma} \epsilon_{(\lambda)}^{*\nu} p^\rho z^\sigma \int_0^1 du e^{i(u py + \bar{u} px)} \frac{g_{\perp}^{(v)}(u)}{4}$$

chiral-odd

$$\langle A(P, \lambda) | \bar{q}_1(y) \sigma_{\mu\nu} \gamma_5 q_2(x) | 0 \rangle = \int_0^1 du e^{i(u py + \bar{u} px)} \left\{ (\epsilon_{\perp\mu}^{(\lambda)*} p_\nu - \epsilon_{\perp\nu}^{(\lambda)*} p_\mu) \Phi_{\perp}(u) \right. \\ \left. + \frac{m_A^2 \epsilon^{(\lambda)*} z}{(pz)^2} (p_\mu z_\nu - p_\nu z_\mu) h_{\parallel}^{(t)}(u) \right\},$$

$$\langle A(P, \lambda) | \bar{q}_1(y) \gamma_5 q_2(x) | 0 \rangle = m_A^2 \epsilon^{(\lambda)*} z \int_0^1 du e^{i(u py + \bar{u} px)} \frac{h_{\parallel}^{(p)}(u)}{2}.$$

twist-2: $\Phi_{\parallel}, \Phi_{\perp}$

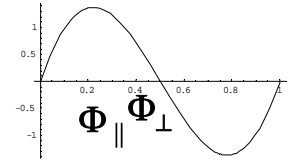
twist-3: $g_{\perp}^{(v)}, g_{\perp}^{(a)}, h_{\perp}^{(t)}, h_{\parallel}^{(p)}$ related to twist-2 ones via Wandzura-Wilczek relations (neglecting 3-parton distributions)

$$\Phi_{\parallel}^A(u) = 6u\bar{u} f_A \left[a_0^{\parallel, A} + \sum_{i=1}^{\infty} a_i^{\parallel, A} C_i^{3/2}(2u-1) \right] \quad C_i^{3/2}: \text{ Gegenbauer polynomial}$$

Since $f[b_1^{\circ}] = 0$, how to construct LCDA Φ_{\parallel} for neutral b_1 ?

1P_1 meson

Due to even G-parity, Φ_{\perp} , $h_{\parallel}^{(t)}$, $h_{\parallel}^{(p)}$ are symmetric under $u \rightarrow 1-u$, while Φ_{\parallel} , $g_{\perp}^{(v)}$, $g_{\perp}^{(a)}$ are antisymmetric with the replacement $u \rightarrow 1-u$ in SU(3) limit



$$\Phi_{\perp}^{1P_1}(u) = f_{1P_1}^{\perp} 6u\bar{u} \left\{ 1 + 3a_1^{\perp, 1P_1} (2u-1) + a_2^{\perp, 1P_1} \frac{3}{2} [5(2u-1)^2 - 1] \right\} \quad \int_0^1 du \Phi_{\perp}^{1P_1}(u) = f_{1P_1}^{\perp}$$

$$(1) \quad \Phi_{\parallel}^{1P_1}(u) = f_{1P_1}^{\perp} 6u\bar{u} \left\{ a_0^{\parallel, 1P_1} + 3a_1^{\parallel, 1P_1} (2u-1) + a_2^{\parallel, 1P_1} \frac{3}{2} [5(2u-1)^2 - 1] \right\}$$

$$\int_0^1 du \Phi_{\parallel}^{1P_1}(u) = f_{1P_1}^{\perp} \Rightarrow \boxed{f_{1P_1} = f_{1P_1}^{\perp}(\mu) a_0^{\parallel, 1P_1}(\mu)}$$

LCDA $\Phi_{\parallel}^{1P_1}$ can be recast to the form

$$(2) \quad \Phi_{\parallel}^{1P_1}(u) = f_{1P_1} 6u\bar{u} \left\{ 1 + \mu_{1P_1} \sum_{i=1}^2 a_i^{\parallel, 1P_1} C_i^{3/2}(2u-1) \right\} \quad \text{with} \quad \mu_{1P_1} = 1/a_0^{\parallel, 1P_1}$$

- For neutral b_1 , $f_{b_1} = 0$, but $f_{b_1} \mu_{b_1} = f_{b_1}^{\perp}$ is finite !
- This is very similar to the scalar meson case where $f [f_0, a_0^0, \sigma] = 0$, but decay constant defined by $\langle S | \bar{q}_1 q_2 | 0 \rangle = m_S \bar{f}_S$ is not vanishing. LCDA (1) and (2) are equivalent for describing Φ_{\parallel} for 1P_1 meson

3P_1 meson

Due to odd G-parity, Φ_{\perp} , $h_{\parallel}^{(t)}$, $h_{\parallel}^{(p)}$ are anti-symmetric under $u \rightarrow 1-u$, while Φ_{\parallel} , $g_{\perp}^{(v)}$, $g_{\perp}^{(a)}$ are symmetric with the replacement $u \rightarrow 1-u$ in SU(3) limit

$$\begin{aligned} \Phi_{\parallel}^{3P_1}(u) &= f_{3P_1} 6u\bar{u} \left\{ 1 + 3a_{1\parallel}^{3P_1}(2u-1) + a_{2\parallel}^{3P_1} \frac{3}{2} [5(2u-1)^2 - 1] \right\}, \\ (1) \quad \Phi_{\perp}^{3P_1}(u) &= f_{3P_1} 6u\bar{u} \left\{ a_0^{\perp, 3P_1} + 3a_1^{\perp, 3P_1}(2u-1) + a_2^{\perp, 3P_1} \frac{3}{2} [5(2u-1)^2 - 1] \right\} \end{aligned}$$

$$\int_0^1 du \Phi_{\parallel}^{3P_1}(u) = f_{3P_1}, \quad \int_0^1 du \Phi_{\perp}^{3P_1}(u) = f_{3P_1}^{\perp} \quad \Rightarrow \quad f_{3P_1}^{\perp}(\mu) = f_{3P_1} a_0^{\perp, 3P_1}(\mu).$$

LCDA $\Phi_{\perp}^{3P_1}$ can be recast to the form

$$(2) \quad \Phi_{\perp}^{3P_1}(u) = f_{3P_1}^{\perp} 6u\bar{u} \left\{ 1 + \mu_{3P_1} \sum_{i=1}^2 a_i^{\perp, 3P_1} C_i^{3/2}(2u-1) \right\} \quad \text{with} \quad \mu_{3P_1} = 1/a_0^{\perp, 3P_1}$$

One can use LCDA (1) or (2) to describe Φ_{\perp} for 3P_1 meson

Gegenbauer moments

K.C. Yang, Nucl. Phys. B776, 187 (2007)

| | | | | | | |
|---------|------------------------------|-------------------------------|-------------------------------|---------------------------|---------------------------|---------------------------|
| μ | $a_2^{\parallel, a_1(1260)}$ | $a_2^{\parallel, f_1^{3P_1}}$ | $a_2^{\parallel, f_8^{3P_1}}$ | $a_2^{\parallel, K_{1A}}$ | $a_1^{\parallel, K_{1A}}$ | |
| 1 GeV | -0.02 ± 0.02 | -0.04 ± 0.03 | -0.07 ± 0.04 | -0.05 ± 0.03 | $-0.30^{+0.26}_{-0.00}$ | |
| 2.2 GeV | -0.01 ± 0.01 | -0.03 ± 0.02 | -0.05 ± 0.03 | -0.04 ± 0.02 | $-0.24^{+0.21}_{-0.00}$ | |
| μ | $a_1^{\perp, a_1(1260)}$ | $a_1^{\perp, f_1^{3P_1}}$ | $a_1^{\perp, f_8^{3P_1}}$ | $a_1^{\perp, K_{1A}}$ | $a_0^{\perp, K_{1A}}$ | $a_2^{\perp, K_{1A}}$ |
| 1 GeV | -1.04 ± 0.34 | -1.06 ± 0.36 | -1.11 ± 0.31 | -1.08 ± 0.48 | $0.26^{+0.03}_{-0.22}$ | 0.02 ± 0.21 |
| 2.2 GeV | -0.81 ± 0.26 | -0.82 ± 0.28 | -0.86 ± 0.24 | -0.84 ± 0.37 | $0.24^{+0.03}_{-0.21}$ | 0.01 ± 0.15 |
| μ | $a_1^{\parallel, b_1(1235)}$ | $a_1^{\parallel, h_1^{1P_1}}$ | $a_1^{\parallel, h_8^{1P_1}}$ | $a_1^{\parallel, K_{1B}}$ | $a_0^{\parallel, K_{1B}}$ | $a_2^{\parallel, K_{1B}}$ |
| 1 GeV | -1.95 ± 0.35 | -2.00 ± 0.35 | -1.95 ± 0.35 | -1.95 ± 0.45 | -0.15 ± 0.15 | $0.09^{+0.16}_{-0.18}$ |
| 2.2 GeV | -1.56 ± 0.28 | -1.60 ± 0.28 | -1.56 ± 0.28 | -1.56 ± 0.36 | -0.15 ± 0.15 | $0.06^{+0.11}_{-0.13}$ |
| μ | $a_2^{\perp, b_1(1235)}$ | $a_2^{\perp, h_1^{1P_1}}$ | $a_2^{\perp, h_8^{1P_1}}$ | $a_2^{\perp, K_{1B}}$ | $a_1^{\perp, K_{1B}}$ | |
| 1 GeV | 0.03 ± 0.19 | 0.18 ± 0.22 | 0.14 ± 0.22 | -0.02 ± 0.22 | $0.30^{+0.00}_{-0.31}$ | |
| 2.2 GeV | 0.02 ± 0.14 | 0.14 ± 0.17 | 0.11 ± 0.17 | -0.02 ± 0.17 | $0.25^{+0.00}_{-0.26}$ | |

$B \rightarrow VV$ in QCDF

HYC, K.C. Yang, 2001

Li, Lu, Y.D. Yang, 2003, 2005

Kagan, 2004 (penguin annihilation)

Zou, Xiao, 2005

Y.D. Yang, Wang, Lu, 2005

Das, K.C. Yang, 2005

Huang, Ko, Wu, Y.D. Yang, 2006

Beneke, Rohrer, D.S. Yang, 2007

Most of early results do not agree with each other due mainly to incorrect projection on polarization states (except Das & Yang); all have errors (except Kagan) and none complete.

Beneke et al. obtained complete NLO corrections to a_i^h & computed LO weak annihilation.

B → VV, VA, AA in QCDF

Apply QCD factorization to B → VV, VA, AA (Beneke, Buchalla, Neubert, Sachrajda)

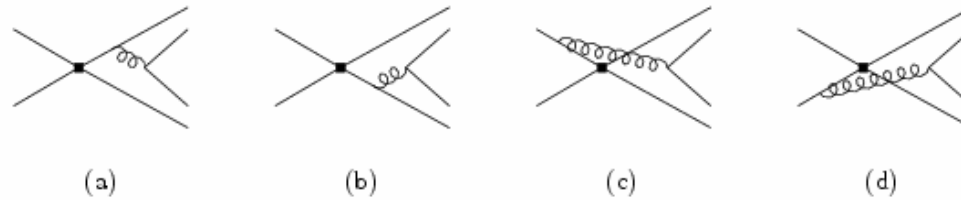
vertex & penguin



hard spectator int.



annihilation



$$a_i^{p,h}(M_1 M_2) = \left(c_i + \frac{c_{i\pm 1}}{N_c} \right) N_i^h(M_2) \boxed{} + \frac{c_{i\pm 1}}{N_c} \frac{C_F \alpha_s}{4\pi} \left[V_i^h(M_2) + \frac{4\pi^2}{N_c} H_i^h(M_1 M_2) \right] + P_i^{h,p}(M_2),$$

$$N_i(M_2) = \begin{cases} 0, & i = 6, 8, \\ 1, & \text{else.} \end{cases} = \begin{cases} 1 & \text{for } {}^3P_1 \\ a_0^{\parallel, 1P_1} & \text{for } {}^1P_1, \text{ vanishes in SU(3) limit} \end{cases}$$

$$M_{\parallel}^V = -i \frac{f_V}{4} \frac{m_V(\epsilon_{(\lambda)}^* n_+)}{2} \not{k}_- \Phi_{\parallel}(u) - i \frac{f_V^{\perp} m_V}{4} \frac{m_V(\epsilon_{(\lambda)}^* n_+)}{2E} \left\{ -\frac{i}{2} \sigma_{\mu\nu} n_-^{\mu} n_+^{\nu} h_{\parallel}^{(t)}(u) \right. \\ \left. - iE \int_0^u dv (\Phi_{\perp}(v) - h_{\parallel}^{(t)}(v)) \sigma_{\mu\nu} n_-^{\mu} \frac{\partial}{\partial k_{\perp\nu}} + \frac{h_{\parallel}^{(s)}(u)}{2} \right\} \Big|_{k=uv} + \mathcal{O}\left[\left(\frac{m_V}{E}\right)^2\right],$$

$$M_{\perp}^V = -i \frac{f_V^{\perp}}{4} E \not{\epsilon}_{\perp}^{*(\lambda)} \not{k}_- \Phi_{\perp}(u) \\ - i \frac{f_V m_V}{4} \left\{ \not{\epsilon}_{\perp}^{*(\lambda)} g_{\perp}^{(v)}(u) - E \int_0^u dv (\Phi_{\parallel}(v) - g_{\perp}^{(v)}(v)) \not{k}_- \epsilon_{\perp\mu}^{*(\lambda)} \frac{\partial}{\partial k_{\perp\mu}} \right. \\ \left. + i \epsilon_{\mu\nu\rho\sigma} \gamma^{\mu} \epsilon_{\perp}^{*(\lambda)\nu} n_-^{\rho} \gamma_5 \left[n_+^{\sigma} \frac{g_{\perp}^{(a)}(u)}{8} - E \frac{g_{\perp}^{(a)}(u)}{4} \frac{\partial}{\partial k_{\perp\sigma}} \right] \right\} \Big|_{k=up} + \mathcal{O}\left[\left(\frac{m_V}{E}\right)^2\right],$$

$$M_{\parallel}^A = -i \frac{f_A}{4} \frac{m_A(\epsilon_{(\lambda)}^* n_+)}{2} \not{k}_- \gamma_5 \Phi_{\parallel}(u) + i \frac{f_A^{\perp} m_A}{4} \frac{m_A(\epsilon_{(\lambda)}^* n_+)}{2E} \left\{ -\frac{i}{2} \sigma_{\mu\nu} \gamma_5 n_-^{\mu} n_+^{\nu} h_{\parallel}^{(t)}(u) \right. \\ \left. - iE \int_0^u dv (\Phi_{\perp}(v) - h_{\parallel}^{(t)}(v)) \sigma_{\mu\nu} \gamma_5 n_-^{\mu} \frac{\partial}{\partial k_{\perp\nu}} + \gamma_5 \frac{h_{\parallel}^{(p)}(u)}{2} \right\} \Big|_{k=un} + \mathcal{O}\left[\left(\frac{m_A}{E}\right)^2\right]$$

$$M_{\perp}^A = i \frac{f_A^{\perp}}{4} E \not{\epsilon}_{\perp}^{*(\lambda)} \not{k}_- \gamma_5 \Phi_{\perp}(u) \\ - i \frac{f_A m_A}{4} \left\{ \not{\epsilon}_{\perp}^{*(\lambda)} \gamma_5 g_{\perp}^{(a)}(u) - E \int_0^u dv (\Phi_{\parallel}(v) - g_{\perp}^{(a)}(v)) \not{k}_- \gamma_5 \epsilon_{\perp\mu}^{*(\lambda)} \frac{\partial}{\partial k_{\perp\mu}} \right. \\ \left. + i \epsilon_{\mu\nu\rho\sigma} \gamma^{\mu} \epsilon_{\perp}^{*(\lambda)\nu} n_-^{\rho} \left[n_+^{\sigma} \frac{g_{\perp}^{(v)}(u)}{8} - E \frac{g_{\perp}^{(v)}(u)}{4} \frac{\partial}{\partial k_{\perp\sigma}} \right] \right\} \Big|_{k=up} + \mathcal{O}\left[\left(\frac{m_A}{E}\right)^2\right]$$

Transverse momentum derivative terms should be included before taking collinear approximation

- Factorization breaks down for transverse polarization amplitudes even at leading power [HYC, Yang,...; Beneke et al.]

Hard spectator scattering:

$H^{-1,5}$ have log div., H^{+1} has log and linear div

$$\int_0^1 \frac{dx}{x} \equiv X \rightarrow \ln\left(\frac{m_B}{\Lambda_h}\right) (1 + \rho e^{i\phi})$$

- Nonfactorization \Rightarrow transverse polarization amplitudes are on much less solid footing than longitudinal ones

B → K* φ

$$\mathcal{A}_{\bar{B} \rightarrow \bar{K}^* \phi}^h \approx V_c (\alpha_3^h + \alpha_4^{c,h} + \beta_3^h - \frac{1}{2} \alpha_{3,EW}^h) X_{\bar{K}^* \phi}^h.$$

$$\alpha_3 = \mathbf{a}_3 + \mathbf{a}_5, \quad \alpha_4 = \mathbf{a}_4 - r_\chi \phi \mathbf{a}_6, \quad \alpha_{3,EW} = \mathbf{a}_9 + \mathbf{a}_7, \quad \beta_3 = \text{penguin ann}$$

$$X_{\bar{K}^* \phi}^h = \langle \phi | J_\mu | 0 \rangle \langle \bar{K}^* | J^\mu | B \rangle, \quad |X_{\bar{K}^* \phi}^0| : |X_{\bar{K}^* \phi}^-| : |X_{\bar{K}^* \phi}^+| = 1 : 0.35 : 0.007$$

| | h=0 | | h=- | | | h=0 | | h=- | |
|------------------------|---------------|----------|---------------|----------|---------------------------|---------------|----------|---------------|----------|
| $\alpha_3(K^* \phi)$ | <u>0.005</u> | - 0.001i | <u>-0.004</u> | - 0.001i | $\alpha_{3,EW}(K^* \phi)$ | <u>-0.009</u> | - 0.000i | <u>0.002</u> | - 0.000i |
| $\alpha_4^u(K^* \phi)$ | <u>-0.022</u> | - 0.014i | <u>-0.047</u> | - 0.016i | $\alpha_4^c(K^* \phi)$ | <u>-0.027</u> | - 0.014i | <u>-0.049</u> | - 0.006i |

Coefficients are helicity dependent !

$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{\bar{B} \rightarrow \bar{K}^* \phi} \approx \left(\frac{\alpha_3^- + \alpha_4^{c,-} - \frac{1}{2} \alpha_{3,EW}^-}{\alpha_3^0 + \alpha_4^{c,0} - \frac{1}{2} \alpha_{3,EW}^0} \right) \left(\frac{X_{\bar{K}^* \phi}^-}{X_{\bar{K}^* \phi}^0} \right) \quad \text{with } \beta_3=0$$

constructive (destructive) interference in A⁻ (A⁰) ⇒ f_L ≈ 0.58

Any serious model for solving polarization enigma should consider NLO corrections

Although f_{\perp} is reduced to 60% level, polarization puzzle is not resolved as the predicted rate, $BR \sim 4.3 \times 10^{-6}$, is too small compared to the data, $\sim 10 \times 10^{-6}$ for $B \rightarrow K^* \phi$

$$P^c = \underbrace{[a_4^c + r_{\chi} a_6^c]_{SD} + [a_4^c + r_{\chi} a_6^c]_{LD}}_{\text{charming penguin, FSI}} + \underbrace{\beta_3^c}_{\text{penguin annihilation}} + \dots$$

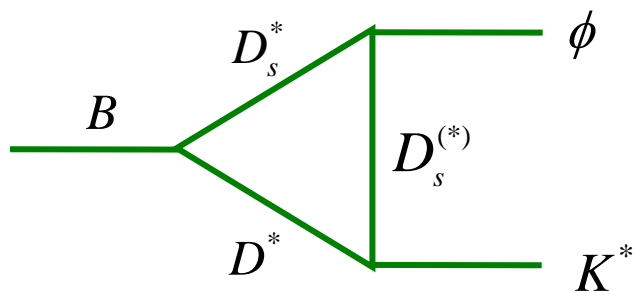
■ Br & f_{\perp} are fit by adjusting $X_A = \ln\left(\frac{m_B}{\Lambda_h}\right)(1 + \rho_A e^{i\phi_A})$ Kagan ('04)
 $\Rightarrow \rho_A = 0.60, \phi_A = -50^\circ$

| Decay | \mathcal{B} | | f_L | | f_{\perp} | |
|---|-------------------------------|----------------|------------------------|-------------------|------------------------|-------------------|
| | Theory | Expt | Theory | Expt | Theory | Expt |
| $B^- \rightarrow K^{*-} \phi^c$ | $10.0^{+1.3+14.1}_{-1.1-6.3}$ | 10.0 ± 1.1 | $0.49^{+0.51}_{-0.38}$ | 0.50 ± 0.05 | $0.25^{+0.20}_{-0.25}$ | 0.20 ± 0.05 |
| $\bar{B}^0 \rightarrow \bar{K}^{*0} \phi$ | $9.5^{+1.2+13.5}_{-1.1-6.1}$ | 9.5 ± 0.8 | $0.50^{+0.50}_{-0.38}$ | 0.484 ± 0.034 | $0.25^{+0.19}_{-0.25}$ | 0.256 ± 0.032 |

$$f_{\parallel} \approx f_{\perp} \sim 0.25$$

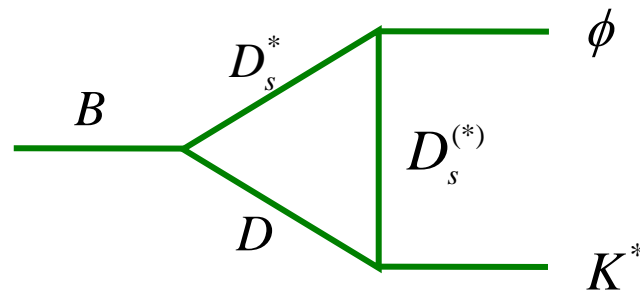
We use ρ_A & ϕ_A to *accommodate* the data of Br & f_{\perp} rather than to *predict* them

- Get large transverse polarization from $B \rightarrow D_s^* D^*$ and then convey it to ϕK^* via FSI (or charming penguin) [HYC, Chua, Soni; Colangelo, De Farzio, Pham]



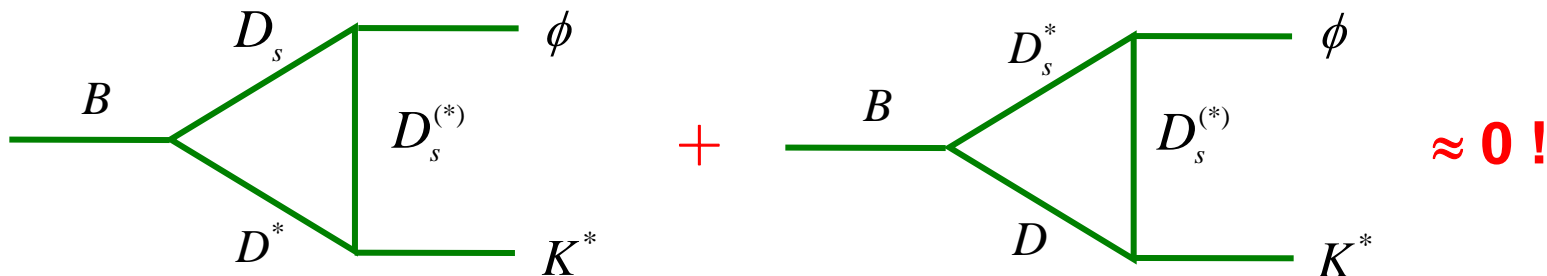
$$f_L(D_s^* D^*) \sim 0.51$$

$$f_{\parallel} \sim 0.41, f_{\perp} \sim 0.08$$



contributes to f_{\perp} only

Large cancellation occurs in $B \rightarrow \{D_s^* D, D_s D^*\} \rightarrow \phi K^*$ processes. This can be understood as CP & SU(3) symmetry

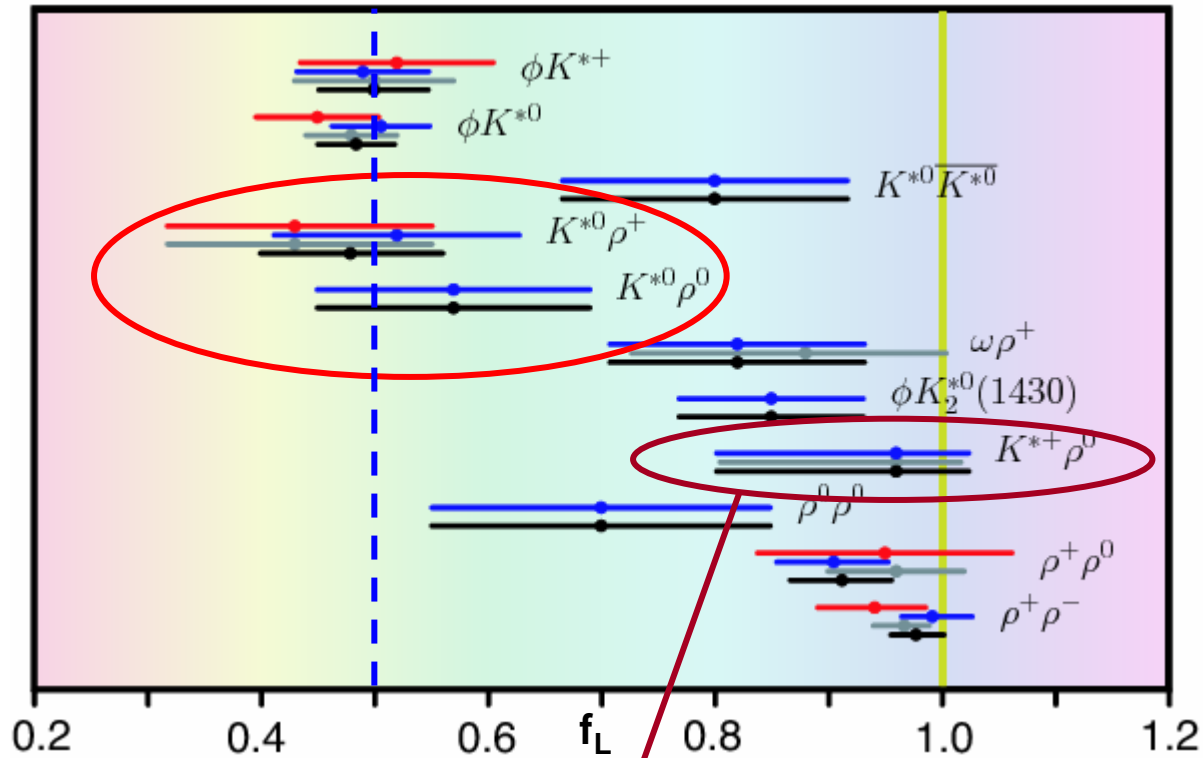


\Rightarrow very small perpendicular polarization, $f_{\perp} \sim 2\%$, in sharp contrast to $f_{\perp} \sim 15\%$ obtained by Colangelo et al.

While $f_T \approx 0.50$ is achieved, why is f_\perp not so small ?

- ◆ Cancellation in $B \rightarrow \{VP, PV\} \rightarrow \phi K^*$ can be circumvented in $B \rightarrow \{SA, AS\} \rightarrow \phi K^*$. For $S, A = D^{**}, D_s^{**} \Rightarrow f_\perp \sim 0.22$
- ◆ It is easy to explain the rate deficit & $f_L \approx 0.50$ via FSI, but it takes some efforts to accommodate $f_\perp \sim f_\parallel$
- ◆ Ways of distinguishing penguin annihilation from rescattering have been proposed by London et al. [arXiv:0802.0897]

B → K* ρ



| Decay | Expt | |
|---|---------------|------------------------|
| | B | f _L |
| $B^- \rightarrow \bar{K}^{*0} \rho^-$ | 9.2 ± 1.5 | 0.48 ± 0.08 |
| $B^- \rightarrow K^{*-} \rho^0$ | < 6.1 | $0.96^{+0.06}_{-0.16}$ |
| $\bar{B}^0 \rightarrow K^{*-} \rho^+$ | < 12 | — |
| $\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0$ | 5.6 ± 1.6 | 0.57 ± 0.12 |

While $f_L(K^{*0} \rho^-, K^{*0} \rho^0) \sim 1/2$, $K^{*-} \rho^0$ is dominated by longitudinal polarization

even more puzzling !

| Parameter | $h = 0$ | $h = -$ | Parameter | $h = 0$ | $h = -$ |
|------------------------|-------------------|-------------------|---------------------------|-------------------|-------------------|
| $\alpha_1(\rho K^*)$ | $0.96 + 0.02i$ | $1.11 + 0.03i$ | $\alpha_{3,EW}(K^* \rho)$ | $-0.009 - 0.000i$ | $0.005 - 0.000i$ |
| $\alpha_2(K^* \rho)$ | $0.28 - 0.08i$ | $-0.17 - 0.17i$ | $\alpha_{4,EW}(K^* \rho)$ | $-0.002 + 0.001i$ | $0.001 + 0.001i$ |
| $\alpha_4^u(\rho K^*)$ | $-0.022 - 0.014i$ | $-0.048 - 0.016i$ | $\beta_3(\rho K^*)$ | $0.015 - 0.020i$ | $-0.012 + 0.016i$ |
| $\alpha_4^c(\rho K^*)$ | $-0.026 - 0.014i$ | $-0.050 - 0.006i$ | | | |

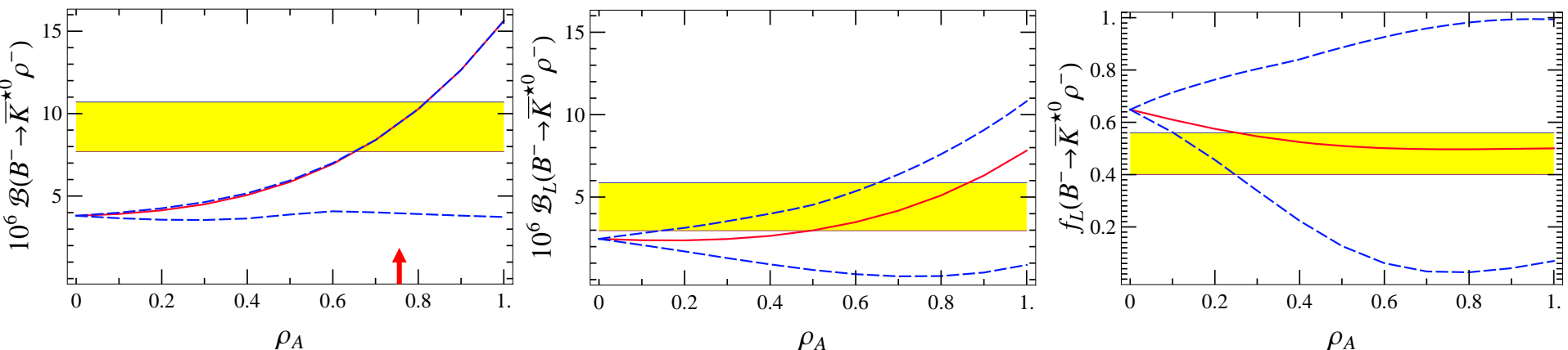
$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0} \approx \begin{pmatrix} \alpha_4^{c,-} - \frac{3}{2} \alpha_{3,EW}^- \\ \alpha_4^{c,0} - \frac{3}{2} \alpha_{3,EW}^0 \end{pmatrix} \begin{pmatrix} X_{\bar{K}^* \rho}^- \\ X_{\bar{K}^* \rho}^0 \end{pmatrix} \quad \begin{array}{l} \text{constructive} \\ \text{destructive} \end{array} \quad \text{with } \beta_3=0$$

$$\frac{\mathcal{A}^-}{\mathcal{A}^0} \Big|_{B^- \rightarrow K^{*-} \rho^0} \approx \begin{pmatrix} \alpha_4^{c,-} + \frac{3}{2} \alpha_{3,EW}^- \\ \alpha_4^{c,0} + \frac{3}{2} \alpha_{3,EW}^0 \end{pmatrix} \begin{pmatrix} X_{\bar{K}^* \rho}^- \\ X_{\bar{K}^* \rho}^0 \end{pmatrix} \quad \begin{array}{l} \text{destructive} \\ \text{constructive} \end{array}$$

$\Rightarrow f_L(K^{*-} \rho^0) = 0.96, \quad f_L(\bar{K}^{*0} \rho^0) = 0.47 \quad (=0.91 \text{ if } a_i^h \text{ are helicity indep})$

| Decay | Expt | | (i) | |
|---|---------------------------------|--|---------------|-------------|
| | \mathcal{B} | f_L | \mathcal{B} | f_L |
| $B^- \rightarrow \bar{K}^{*0} \rho^-$ | <u>9.2 ± 1.5</u> | 0.48 ± 0.08 | <u>3.8</u> | 0.78 |
| $B^- \rightarrow K^{*-} \rho^0$ | < 6.1 | <u>$0.96^{+0.06}_{-0.16}$</u> | 3.6 | <u>0.96</u> |
| $\bar{B}^0 \rightarrow K^{*-} \rho^+$ | < 12 | — | 3.6 | 0.84 |
| $\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0$ | <u>5.6 ± 1.6</u> | <u>0.57 ± 0.12</u> | <u>1.1</u> | <u>0.47</u> |

But, the predicted rates for $K^{*-} \rho^0$ & $\bar{K}^{*0} \rho^0$ are too small !



Choose $K^*0\rho^-$ as an input, a fit to BR and f_L yields $\rho_A=0.75$, $\phi_A=-42^\circ$, slightly different from the ones $\rho_A=0.60$, $\phi_A=-50^\circ$ inferred from $B\rightarrow K^*\phi$

| Decay | \mathcal{B} | | f_L | | f_\perp | |
|---|---|---------------------------------|--|-------------------------------------|------------------------|------|
| | Theory | Expt | Theory | Expt | Theory | Expt |
| $B^- \rightarrow \bar{K}^{*0}\rho^-$ ^a | $9.3^{+1.2+4.5}_{-1.1-5.6}$ | 9.2 ± 1.5 | $0.50^{+0.50}_{-0.38}$ | 0.48 ± 0.08 | $0.25^{+0.19}_{-0.25}$ | |
| $B^- \rightarrow K^{*-}\rho^0$ | $5.4^{+0.6+0.9}_{-0.5-2.4}$ | < 6.1 | $0.69^{+0.29}_{-0.47}$ | $0.96^{+0.06}_{-0.16}$ ^b | $0.15^{+0.23}_{-0.14}$ | |
| $\bar{B}^0 \rightarrow K^{*-}\rho^+$ | $9.0^{+1.1+4.8}_{-1.0-5.5}$ | < 12 | $0.55^{+0.42}_{-0.31}$ | | $0.22^{+0.16}_{-0.21}$ | |
| $\bar{B}^0 \rightarrow \bar{K}^{*0}\rho^0$ | $4.7^{+0.6+4.0}_{-0.5-3.7}$ | 5.6 ± 1.6 | $0.43^{+0.56}_{-0.29}$ | 0.57 ± 0.12 | $0.29^{+0.15}_{-0.28}$ | |

$K^{*}\rho^0$ was contaminated by $K^*f_0(980)$ in previous 2003 measurement of $f_L(K^{*}\rho^0)$. New BaBar measurement of $f_L=0.9 \pm 0.2$ has only 2.5 significance

$$f_L(K^{*}\rho^0) > f_L(K^{*}\rho^+) > f_L(\bar{K}^{*0}\rho^-) > f_L(\bar{K}^{*0}\rho^0)$$

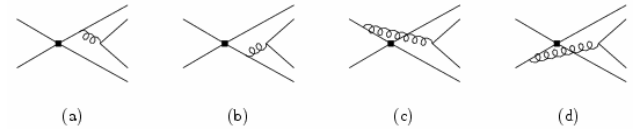
Comparison with Beneke, Rohrer, Yang

- sign difference in annihilation terms $A_3^{f,0}$ $A_3^{i,0}$

$$A_3^{f,0}(V_1 V_2) \approx -18\pi\alpha_s \left(r_\chi^{V_1} - r_\chi^{V_2} \right) (X_A^0 - 2)(2X_A^0 - 1),$$

$$A_3^{i,0}(V_1 V_2) \approx 18\pi\alpha_s \left(-r_\chi^{V_1} - r_\chi^{V_2} \right) \left(X_A^{0^2} - 2X_A^0 + 4 - \frac{\pi^2}{3} \right)$$

$$r_\chi^V(\mu) = \frac{2m_V}{m_b(\mu)} \frac{f_V^\perp(\mu)}{f_V}$$



BRY got a negative sign for $r_\chi^{V_2}$. Recall that annihilation in A_0 is governed by $A_3^{f,0}$ or β_3^0

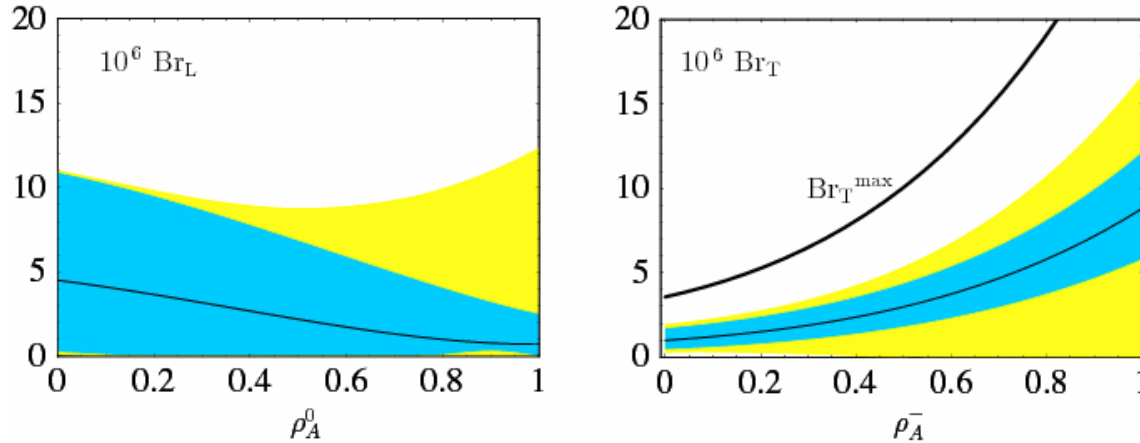
- different c quark mass, $m_c(m_b)=1.3\pm 0.2$ GeV (we use 0.91 GeV)
- BRY use the same ρ_A & ϕ_A parameters for $B \rightarrow K^* \rho$ & $K^* \phi$

| Decay | Expt | | BRY | | Beneke new f_L |
|---|---------------------------------|------------------------|---------------------------------------|------------------------|------------------------|
| | \mathcal{B} | f_L | \mathcal{B} | f_L | |
| $B^- \rightarrow \bar{K}^{*0} \rho^-$ | <u>9.2 ± 1.5</u> | 0.48 ± 0.08 | <u>$5.9_{-3.7}^{+6.6}$</u> | $0.56_{-0.30}^{+0.48}$ | $0.44_{-0.40}^{+0.59}$ |
| $B^- \rightarrow K^{*-} \rho^0$ | < 6.1 | $0.96_{-0.16}^{+0.06}$ | $4.5_{-1.9}^{+3.4}$ | $0.84_{-0.25}^{+0.16}$ | $0.61_{-0.44}^{+0.44}$ |
| $\bar{B}^0 \rightarrow K^{*-} \rho^+$ | < 12 | — | $5.5_{-3.3}^{+6.0}$ | $0.61_{-0.29}^{+0.38}$ | $0.41_{-0.20}^{+0.55}$ |
| $\bar{B}^0 \rightarrow \bar{K}^{*0} \rho^0$ | <u>5.6 ± 1.6</u> | 0.57 ± 0.12 | <u>$2.4_{-2.0}^{+3.5}$</u> | $0.22_{-0.14}^{+0.53}$ | $0.33_{-0.18}^{+0.66}$ |

Kagan ('04)

In absence of penguin ann, $f_L \approx 0.90$ (≈ 0.67 by BRY, ≈ 0.58 by us)
as Kagan didn't consider vertex and spectator corrections

Have to rely heavily on penguin ann to bring up f_T



In our case, we use penguin ann mainly to accommodate rate deficit rather than to enhance f_T

pQCD (Li, Mishima)

$$\text{Br}(B \rightarrow K^* \phi) \sim 15 \times 10^{-6}, \quad f_L \sim 0.75 \quad (A_0 = 0.40 \text{ for } B \rightarrow K^* \text{ transition})$$

$$\begin{aligned} A_L &\propto 2r_2 \epsilon_2^*(L) \cdot \epsilon_3^*(L) A_0, \\ A_{\parallel} &\propto -\sqrt{2}(1+r_2) A_1, \\ A_{\perp} &\propto -\frac{2r_2 r_3}{1+r_2} \sqrt{2[(v_2 \cdot v_3)^2 - 1]} V \end{aligned}$$

Li proposed to use $A_0 \sim 0.28$ to get

$$\text{Br}(B \rightarrow K^* \phi) \sim 10 \times 10^{-6}, \quad f_L \sim 0.59$$

➤ too small A_0 ? (many people use $A_0 \sim 0.37$)

not welcome for $B^0 \rightarrow K^{*0} \underline{K}^{*0}$ (see next)

➤ NLO corrections need to be considered (in progress)

Other VV modes

| Decay | \mathcal{B} | | f_L | | f_\perp | |
|---|------------------------------|------------------------|------------------------|---------------------------|------------------------|------|
| | Theory | Expt | Theory | Expt | Theory | Expt |
| $B^- \rightarrow \rho^- \rho^0$ | $20.1^{+4.0+2.0}_{-1.9-0.9}$ | 18.2 ± 3.0 | $0.96^{+0.02}_{-0.02}$ | $0.912^{+0.044}_{-0.045}$ | 0.02 ± 0.01 | |
| $\bar{B}^0 \rightarrow \rho^+ \rho^-$ | $25.3^{+1.5+2.4}_{-2.6-1.5}$ | $24.2^{+3.1}_{-3.2}$ | $0.92^{+0.01}_{-0.02}$ | $0.978^{+0.025}_{-0.022}$ | $0.04^{+0.01}_{-0.00}$ | |
| $\bar{B}^0 \rightarrow \rho^0 \rho^0$ | $0.9^{+1.5+1.1}_{-0.4-0.2}$ | 0.68 ± 0.27 | $0.92^{+0.06}_{-0.36}$ | 0.70 ± 0.15 | $0.04^{+0.14}_{-0.03}$ | |
| $B^- \rightarrow \rho^- \omega$ | $19.1^{+3.3+1.7}_{-1.6-1.0}$ | $10.6^{+2.6}_{-2.3}$ | $0.96^{+0.02}_{-0.02}$ | 0.82 ± 0.11 | 0.02 ± 0.01 | |
| $\bar{B}^0 \rightarrow \rho^0 \omega$ | $0.1^{+0.1+0.4}_{-0.1-0.0}$ | < 1.5 | $0.55^{+0.47}_{-0.29}$ | | $0.22^{+0.16}_{-0.23}$ | |
| $B^- \rightarrow K^{*-} \omega$ | $3.5^{+0.4+3.5}_{-0.4-1.8}$ | < 3.4 | $0.67^{+0.32}_{-0.36}$ | | $0.16^{+0.18}_{-0.16}$ | |
| $\bar{B}^0 \rightarrow \bar{K}^{*0} \omega$ | $3.0^{+0.5+3.4}_{-0.4-1.8}$ | < 2.7 | $0.57^{+0.44}_{-0.41}$ | | 0.21 ± 0.22 | |
| $B^- \rightarrow K^{*0} K^{*-}$ | $0.6^{+0.1+0.3}_{-0.1-0.3}$ | < 71 | $0.48^{+0.51}_{-0.38}$ | | $0.26^{+0.19}_{-0.26}$ | |
| $\bar{B}^0 \rightarrow K^{*-} K^{*+}$ | $0.1^{+0.0+0.1}_{-0.0-0.1}$ | < 141 | 1 | | 0 | |
| $\bar{B}^0 \rightarrow K^{*0} \bar{K}^{*0}$ | $0.6^{+0.1+0.2}_{-0.1-0.3}$ | $1.28^{+0.37}_{-0.32}$ | $0.52^{+0.48}_{-0.47}$ | $0.80^{+0.12}_{-0.13}$ | $0.24^{+0.23}_{-0.24}$ | |

tree

penguin

- Longitudinal amplitude dominates tree-dominated decays except for $\rho^0 \omega$
- $B \rightarrow \omega$ form factors are slightly smaller than what expected from light-cone sum rules

B → VA (A = a₁, b₁, K₁, f₁, h₁)

| | Mode | Br | f _L | | Mode | Br | f _L |
|---------|--|---------------------------------------|--------------------------|--|--|----------------------------------|--------------------------|
| tree | $\bar{B}^0 \rightarrow a_1^+ \rho^-$ | $23.8^{+10.5+3.2}_{-9.2-0.4}$ | $(0.82^{+0.05}_{-0.13})$ | | $\bar{B}^0 \rightarrow b_1^+ \rho^-$ | $32.1^{+16.5+12.0}_{-14.7-4.7}$ | $(0.96^{+0.01}_{-0.02})$ |
| | $\bar{B}^0 \rightarrow a_1^- \rho^+$ | $35.8^{+3.4+2.6}_{-3.8-0.4}$ | $(0.84^{+0.02}_{-0.06})$ | | $\bar{B}^0 \rightarrow b_1^- \rho^+$ | $0.6^{+0.6+1.8}_{-0.3-0.2}$ | $(0.98^{+0.00}_{-0.32})$ |
| | $\bar{B}^0 \rightarrow a_1^0 \rho^0$ | $1.2^{+2.0+5.2}_{-0.6-0.2}$ | $(0.83^{+0.06}_{-0.88})$ | | $\bar{B}^0 \rightarrow b_1^0 \rho^0$ | $0.4^{+0.4+21.3}_{-0.2-0}$ | $(0.82^{+0.16}_{-0.51})$ |
| | $B^- \rightarrow a_1^0 \rho^-$ | $17.9^{+10.2+1.0}_{-6.4-0.2}$ | $(0.91^{+0.05}_{-0.03})$ | | $B^- \rightarrow b_1^0 \rho^-$ | $29.0^{+16.2+5.4}_{-10.6-5.8}$ | $(0.96^{+0.01}_{-0.06})$ |
| | $B^- \rightarrow a_1^- \rho^0$ | $23.1^{+3.6+4.0}_{-2.9-0.1}$ | $(0.89^{+0.11}_{-0.16})$ | | $B^- \rightarrow b_1^- \rho^0$ | $0.9^{+1.7+2.6}_{-0.6-0.5}$ | $(0.90^{+0.06}_{-0.33})$ |
| | $\bar{B}^0 \rightarrow a_1^0 \omega$ | $0.2^{+0.1+0.8}_{-0.1-0}$ | $(0.82^{+0.05}_{-0.89})$ | | $\bar{B}^0 \rightarrow b_1^0 \omega$ | $0.1^{+0.2+1.4}_{-0.0-0.0}$ | $(0.10^{+1.04}_{-0.01})$ |
| | $B^- \rightarrow a_1^- \omega$ | $22.4^{+3.3+3.2}_{-2.7-0.4}$ | $(0.88^{+0.10}_{-0.15})$ | | $B^- \rightarrow b_1^- \omega$ | $0.9^{+1.4+2.7}_{-0.5-0.3}$ | $(0.91^{+0.07}_{-0.33})$ |
| penguin | $\bar{B}^0 \rightarrow a_1^0 \phi$ | $0.002^{+0.016+0.043}_{-0.007-0.009}$ | $(0.94^{+0.01}_{-0.69})$ | | $\bar{B}^0 \rightarrow b_1^0 \phi$ | $0.01^{+0.01+0.01}_{-0.00-0.00}$ | $(0.98^{+0.01}_{-0.33})$ |
| | $B^- \rightarrow a_1^- \phi$ | $0.01^{+0.01+0.04}_{-0.00-0.00}$ | $(0.94^{+0.01}_{-0.69})$ | | $B^- \rightarrow b_1^- \phi$ | $0.02^{+0.02+0.03}_{-0.01-0.00}$ | $(0.98^{+0.01}_{-0.33})$ |
| | $\bar{B}^0 \rightarrow a_1^+ K^{*-}$ | $7.0^{+4.5+25.2}_{-3.0-7.1}$ | $(0.19^{+0.09}_{-0.15})$ | | $\bar{B}^0 \rightarrow b_1^+ K^{*-}$ | $7.6^{+3.3+40.7}_{-2.4-7.1}$ | $(0.71^{+0.17}_{-0.66})$ |
| | $\bar{B}^0 \rightarrow a_1^0 \bar{K}^{*0}$ | $1.7^{+1.1+8.6}_{-0.7-1.6}$ | $(0.20^{+0.51}_{-0.14})$ | | $\bar{B}^0 \rightarrow b_1^0 \bar{K}^{*0}$ | $3.0^{+1.1+4.6}_{-0.7-2.1}$ | $(0.80^{+0.20}_{-0.70})$ |
| | $B^- \rightarrow a_1^- \bar{K}^{*0}$ | $9.7^{+4.9+32.9}_{-3.5-2.4}$ | $(0.38^{+0.51}_{-0.40})$ | | $B^- \rightarrow b_1^- \bar{K}^{*0}$ | $12.1^{+4.4+21.2}_{-3.2-2.7}$ | $(0.80^{+0.20}_{-0.70})$ |
| | $B^- \rightarrow a_1^0 K^{*-}$ | $7.1^{+2.6+16.8}_{-2.0-3.4}$ | $(0.55^{+0.40}_{-0.46})$ | | $B^- \rightarrow b_1^0 K^{*-}$ | $6.8^{+2.4+12.5}_{-1.8-4.4}$ | $(0.84^{+0.15}_{-0.29})$ |

■ $\Gamma(B^0 \rightarrow b_1^+ \rho^-) \gg \Gamma(B^0 \rightarrow b_1^- \rho^+)$

■ BaBar: $\text{Br}(B^0 \rightarrow a_1^\pm \rho^\mp) < 61 \times 10^{-6}$; $\text{Br}(B^0 \rightarrow b_1^\pm \rho^\mp) < 1.7 \times 10^{-6}$ (FPCP2008)

Naively, it is expected that $b_1^+ \rho^- \sim 3 b_1^+ \pi^- \sim 30 \times 10^{-6}$

■ $a_1 K^*$ modes are dominated by transverse amplitudes

B → AA

| Decay | $\theta_{K_1} = -37^\circ$ | | $\theta_{K_1} = -58^\circ$ | |
|--|-----------------------------------|------------------------|-----------------------------------|------------------------|
| | \mathcal{B} | f_L | \mathcal{B} | f_L |
| $\bar{B}^0 \rightarrow K_1^-(1270)a_1^+$ | $32.0^{+43.2+174.8}_{-20.5-30.5}$ | $0.21^{+0.18}_{-0.07}$ | $36.4^{+46.8+184.0}_{-23.2-33.5}$ | $0.14^{+0.31}_{-0.06}$ |
| $\bar{B}^0 \rightarrow \bar{K}_1^0(1270)a_1^0$ | $16.0^{+22.0+85.9}_{-10.4-15.5}$ | $0.21^{+0.71}_{-0.13}$ | $17.4^{+23.7+92.4}_{-11.7-17.0}$ | $0.11^{+0.27}_{-0.03}$ |
| $B^- \rightarrow \bar{K}_1^0(1270)a_1^-$ | $33.4^{+45.1+175.8}_{-21.5-32.2}$ | $0.19^{+0.22}_{-0.16}$ | $38.1^{+48.5+183.5}_{-24.1-36.0}$ | $0.13^{+0.31}_{-0.13}$ |
| $B^- \rightarrow K_1^-(1270)a_1^0$ | $18.8^{+22.4+89.6}_{-10.8-1.9}$ | $0.26^{+0.41}_{-0.15}$ | $21.4^{+24.2+91.3}_{-12.1-17.7}$ | $0.21^{+0.44}_{-0.13}$ |
| $\bar{B}^0 \rightarrow K_1^-(1400)a_1^+$ | $10.1^{+8.7+12.8}_{-4.8-6.7}$ | $0.31^{+0.33}_{-0.27}$ | $5.0^{+4.5+20.6}_{-1.8-3.9}$ | $0.92^{+0.04}_{-0.53}$ |
| $\bar{B}^0 \rightarrow \bar{K}_1^0(1400)a_1^0$ | $5.5^{+4.4+7.7}_{-2.5-3.7}$ | $0.39^{+0.51}_{-0.37}$ | $3.8^{+2.7+11.9}_{-1.4-2.9}$ | $0.96^{+0.15}_{-0.44}$ |
| $B^- \rightarrow \bar{K}_1^0(1400)a_1^-$ | $11.4^{+9.2+17.7}_{-5.2-8.5}$ | $0.37^{+0.63}_{-0.37}$ | $5.9^{+5.1+22.3}_{-2.2-5.0}$ | $0.95^{+0.08}_{-0.54}$ |
| $B^- \rightarrow K_1^-(1400)a_1^0$ | $5.1^{+4.3+7.3}_{-2.3-0.9}$ | $0.28^{+0.35}_{-0.24}$ | $2.1^{+2.2+9.5}_{-0.8-1.6}$ | $0.88^{+0.08}_{-0.72}$ |
| $\bar{B}^0 \rightarrow K_1^-(1270)b_1^+$ | $12.9^{+9.7+66.5}_{-5.8-11.5}$ | $0.37^{+0.47}_{-0.18}$ | $11.8^{+10.7+67.2}_{-4.8-8.3}$ | $0.20^{+0.65}_{-0.24}$ |
| $\bar{B}^0 \rightarrow \bar{K}_1^0(1270)b_1^0$ | $6.5^{+4.8+33.4}_{-2.8-5.7}$ | $0.37^{+0.46}_{-0.30}$ | $6.0^{+5.1+36.0}_{-2.2-3.9}$ | $0.20^{+0.65}_{-0.25}$ |
| $B^- \rightarrow \bar{K}_1^0(1270)b_1^-$ | $13.5^{+10.4+73.2}_{-6.0-12.7}$ | $0.39^{+0.39}_{-0.27}$ | $11.1^{+10.2+73.5}_{-4.2-8.2}$ | $0.13^{+0.62}_{-0.12}$ |
| $B^- \rightarrow K_1^-(1270)b_1^0$ | $7.9^{+6.5+36.6}_{-3.7-0.9}$ | $0.47^{+0.41}_{-0.25}$ | $6.9^{+6.5+34.3}_{-2.9-4.4}$ | $0.30^{+0.57}_{-0.30}$ |
| $\bar{B}^0 \rightarrow K_1^-(1400)b_1^+$ | $20.2^{+21.4+199.7}_{-8.8-18.1}$ | $0.91^{+0.03}_{-0.31}$ | $21.7^{+20.3+199.7}_{-10.1-19.7}$ | $0.98^{+0.02}_{-0.37}$ |
| $\bar{B}^0 \rightarrow \bar{K}_1^0(1400)b_1^0$ | $10.8^{+10.6+106.9}_{-4.5-10.2}$ | $0.90^{+0.06}_{-0.80}$ | $11.5^{+10.4+104.5}_{-5.3-10.8}$ | $0.98^{+0.02}_{-0.71}$ |
| $B^- \rightarrow \bar{K}_1^0(1400)b_1^-$ | $22.9^{+22.8+224.5}_{-9.7-21.7}$ | $0.90^{+0.05}_{-0.82}$ | $25.7^{+23.3+225.0}_{-12.0-24.5}$ | $0.98^{+0.02}_{-0.84}$ |
| $B^- \rightarrow K_1^-(1400)b_1^0$ | $10.7^{+11.4+104.8}_{-4.7-0.2}$ | $0.91^{+0.01}_{-0.33}$ | $12.0^{+11.3+107.6}_{-5.7-11.2}$ | $0.98^{+0.02}_{-0.50}$ |

Penguin-dominated $K_1 A$ modes (except for $K_1 b_1$) have sizable transverse polarization; see arXiv:0805.0329 for details

Conclusions

- NLO corrections to a_{i^h} can render A^- comparable to A^0 in some VV modes and hence will bring up transverse polarization; no indication for new physics.
- Decay rates should be produced correctly before making a sensible prediction for polarization fractions
- Rate deficit puzzle is more serious than polarization one