

Answering CCQE cross-section discrepancy at low energies



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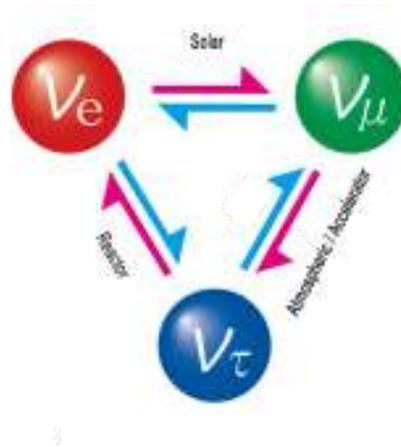
LHEP – AEC, University of BERN.

CHIPP 2014, Fribourg



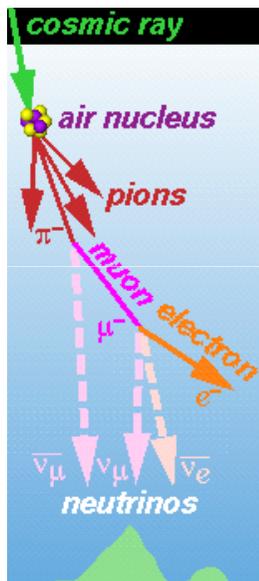
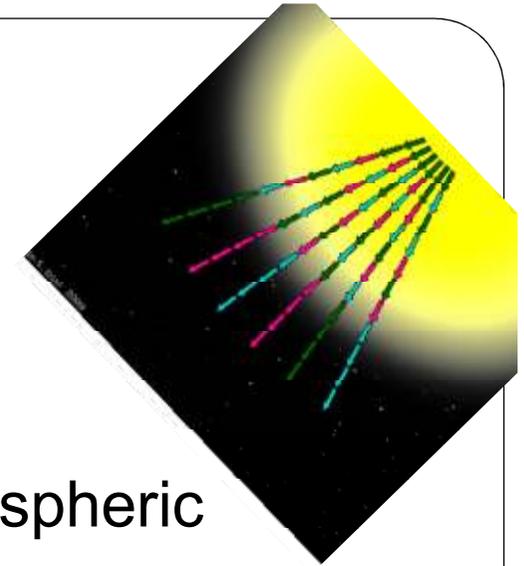
Neutrino

The *weakly* interacting neutral elementary particle



Come in 3 flavor

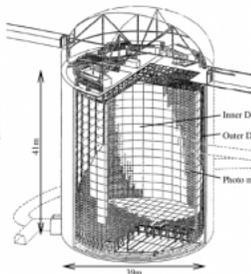
Neutrino puzzle



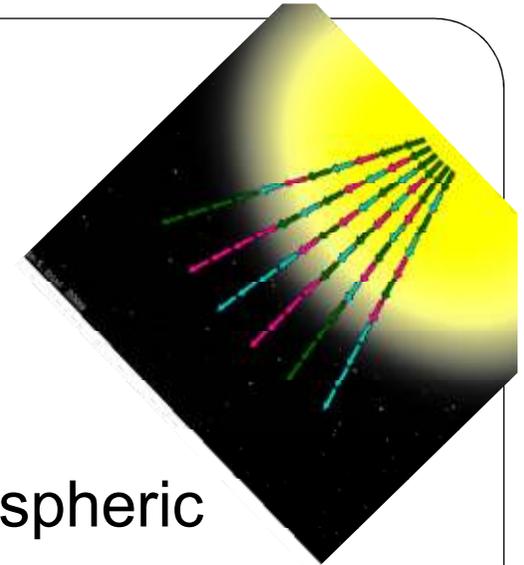
Long standing solar and atmospheric neutrino puzzle

**Measured number of neutrinos,
less than the predicted number!!**

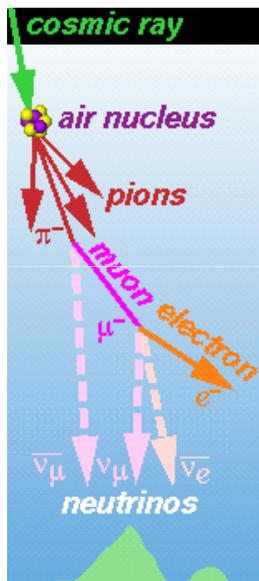
Super-Kamiokande



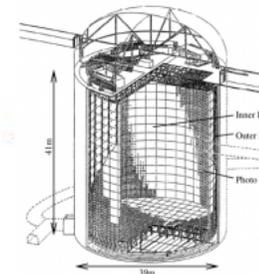
PMNS' matrix



Long standing solar and atmospheric neutrino puzzle, solved



Super-Kamiokande



Flavor States

Note: $c_{ij} = \cos(\theta_{ij})$, $s_{ij} = \sin(\theta_{ij})$

Mass States

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} e^{i\alpha_1}/2 & 0 & 0 \\ 0 & e^{i\alpha_2}/2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



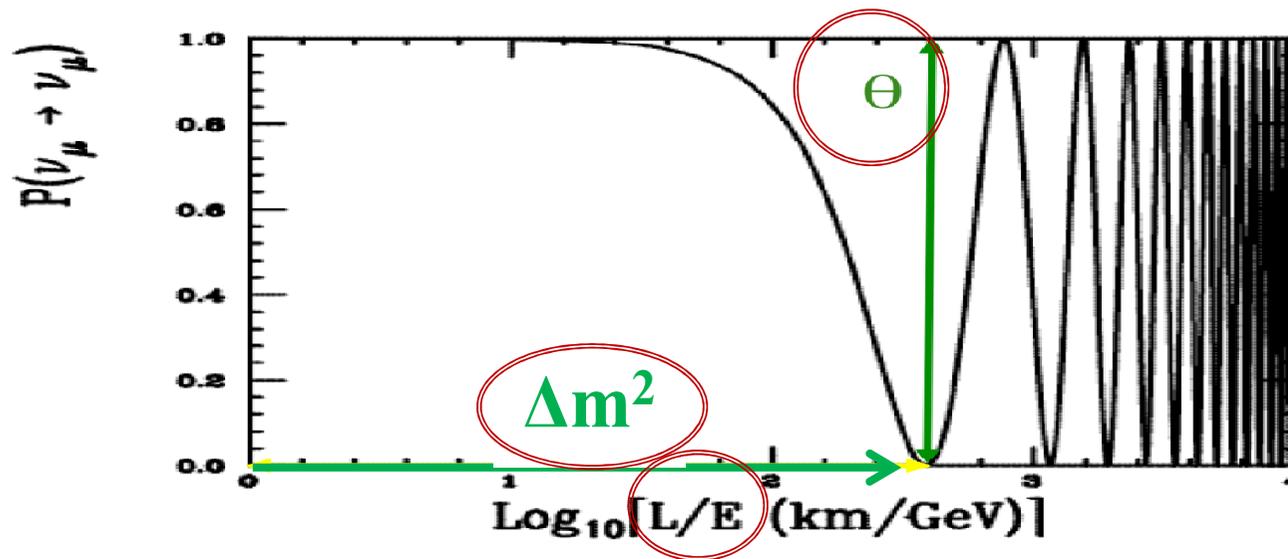
“Atmospheric ν ”
 $\sin^2 2\theta_{23} > 0.95$ (90% C.L.)

“Reactor/Acc. ν ”
 $\sin^2 2\theta_{13} = 0.098 \pm 0.013$

“Solar ν ”
 $\sin^2 2\theta_{12} = 0.857 \pm 0.024$

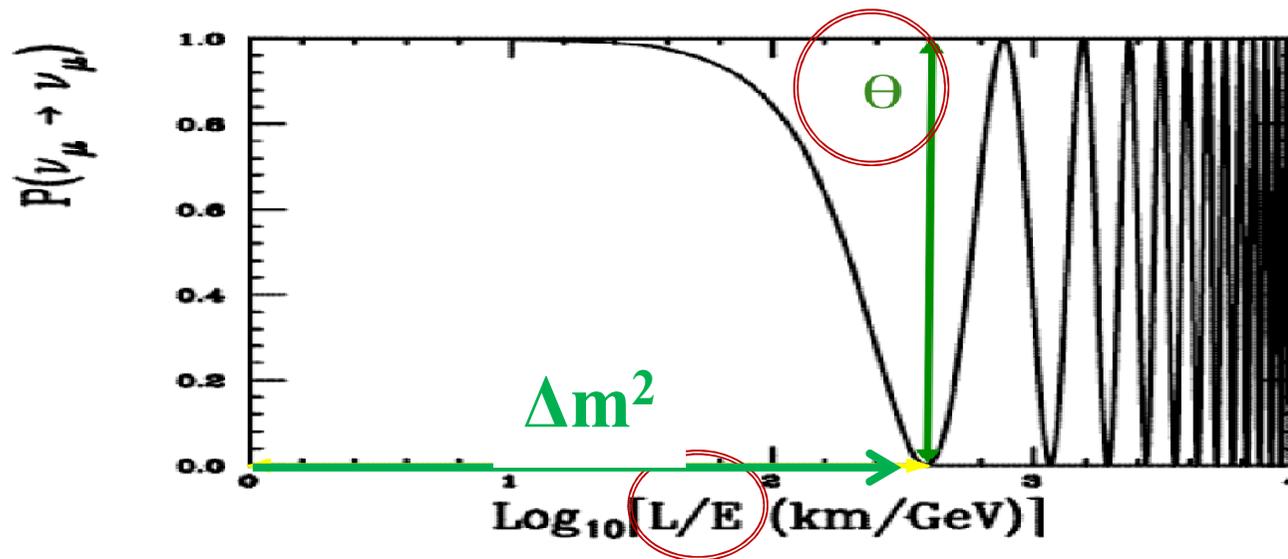
Majorana phases;
Not yet observed

Survival probability

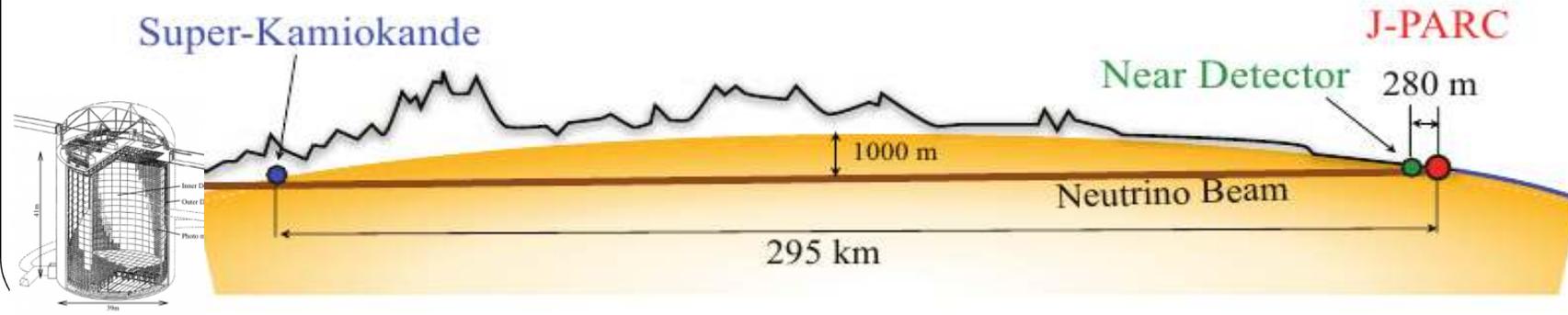


Massive neutrino oscillate from one flavor to another.

Survival probability

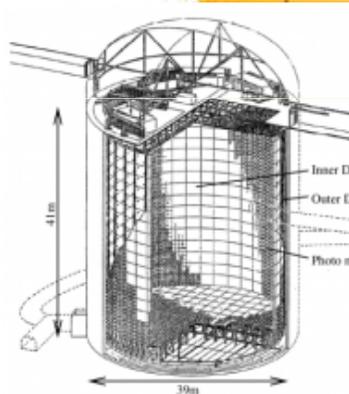
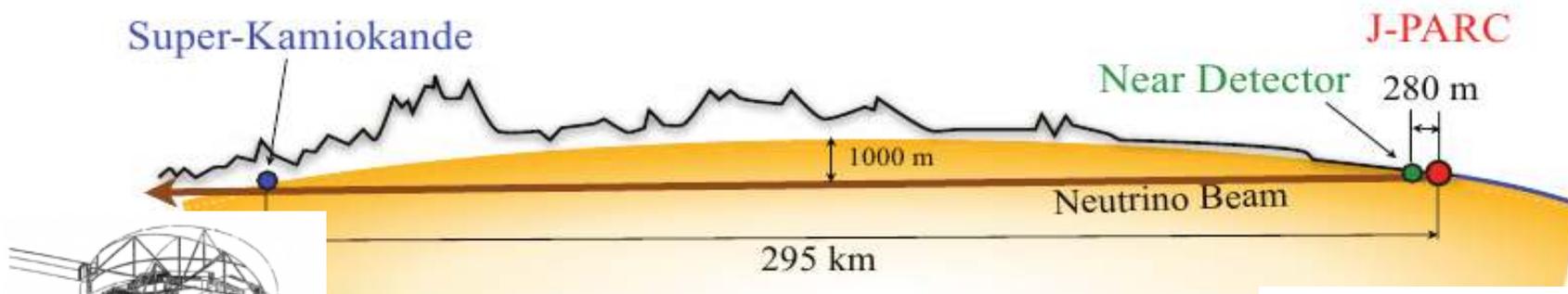


Massive neutrino oscillate from one flavor to another.

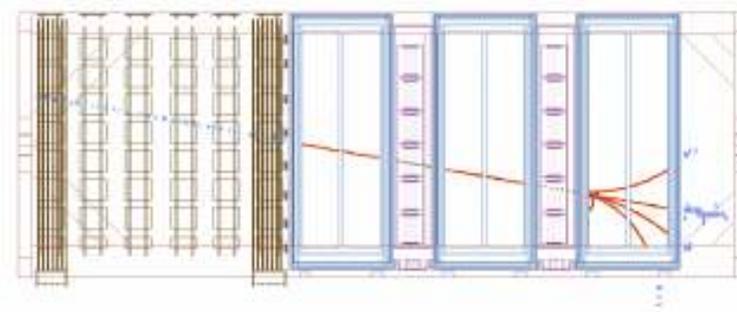
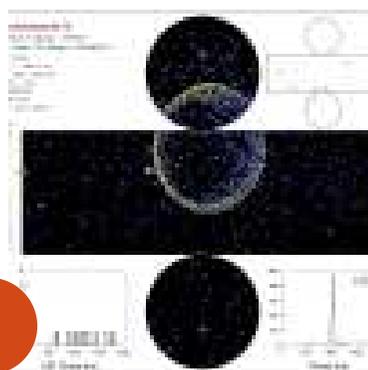
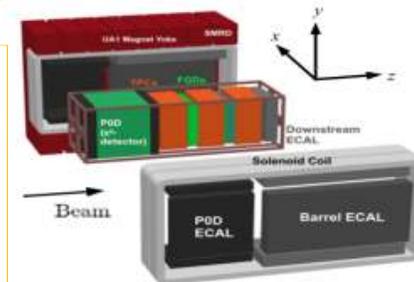




Long baseline accelerator experiment

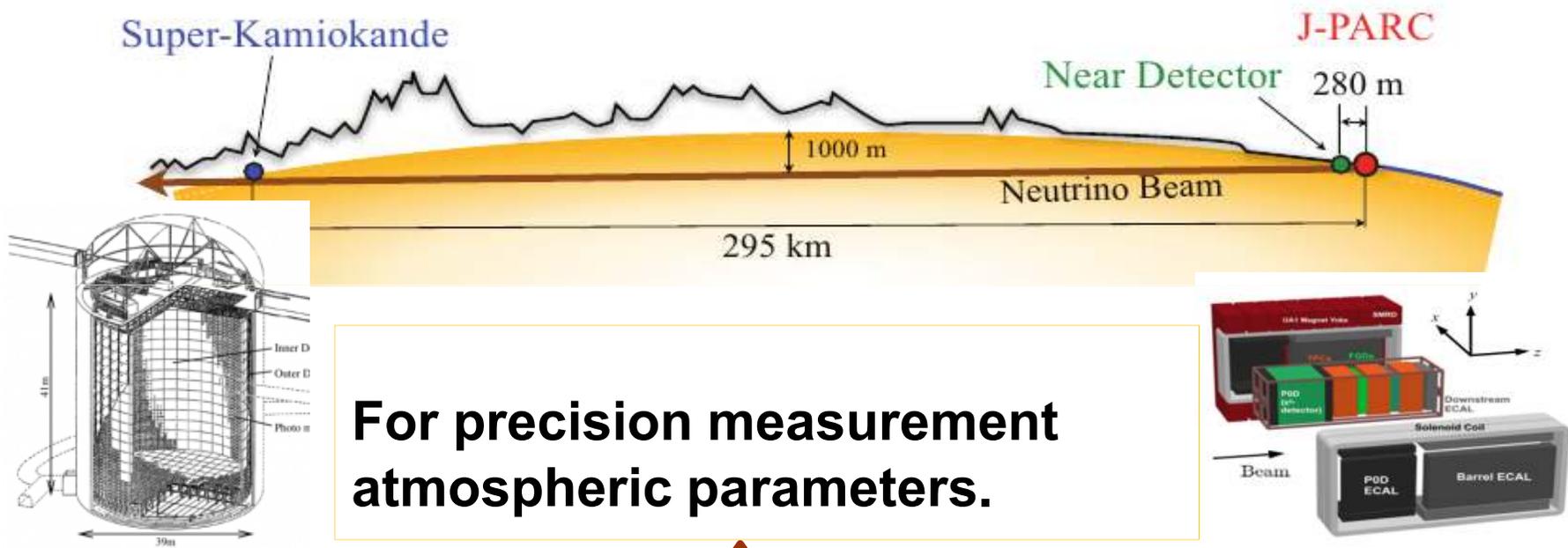


**For precision measurement
atmospheric parameters.**

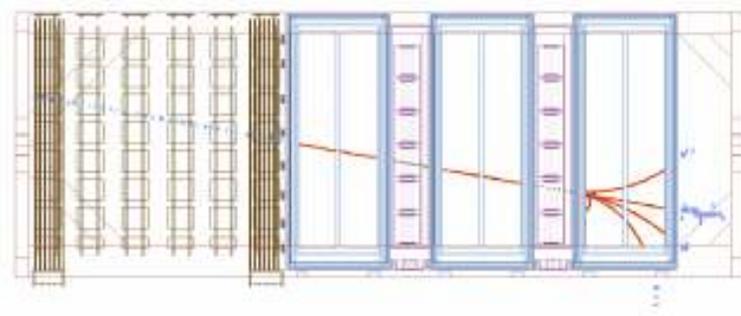
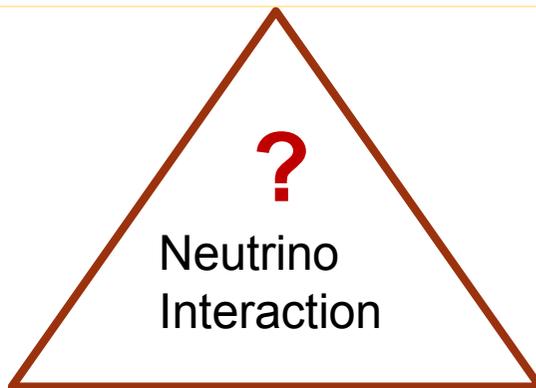




Long baseline accelerator experiment



For precision measurement
atmospheric parameters.



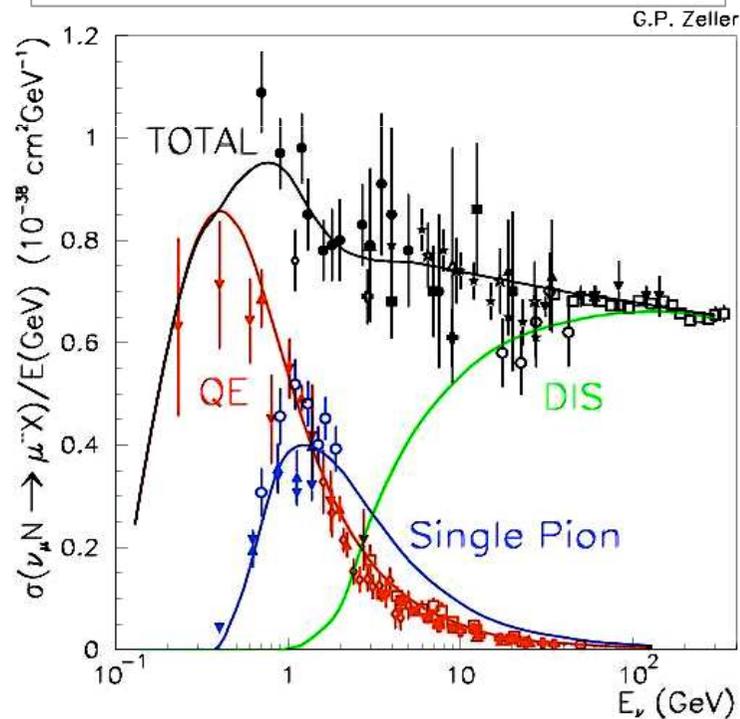
Neutrino Interaction

Charged Current:

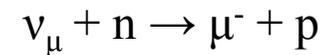
Exchange of W^\pm boson

Neutral Current:

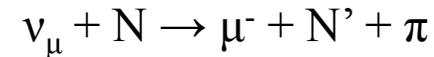
Exchange of Z boson.



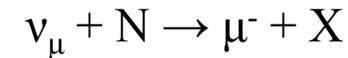
- **quasi-elastic scattering (QE)**
(nucleon)



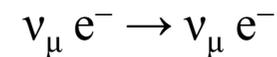
- **single π production** (excitation of nucleus)



- **deep inelastic scattering (DIS)**
(quark)



- **elastic ν -electron scattering**



(μ could be any lepton)

CCQE model

- Scattering cross-section of neutrinos off the nucleon is given by the Llewellyn-Smith formula / Smith-Moniz

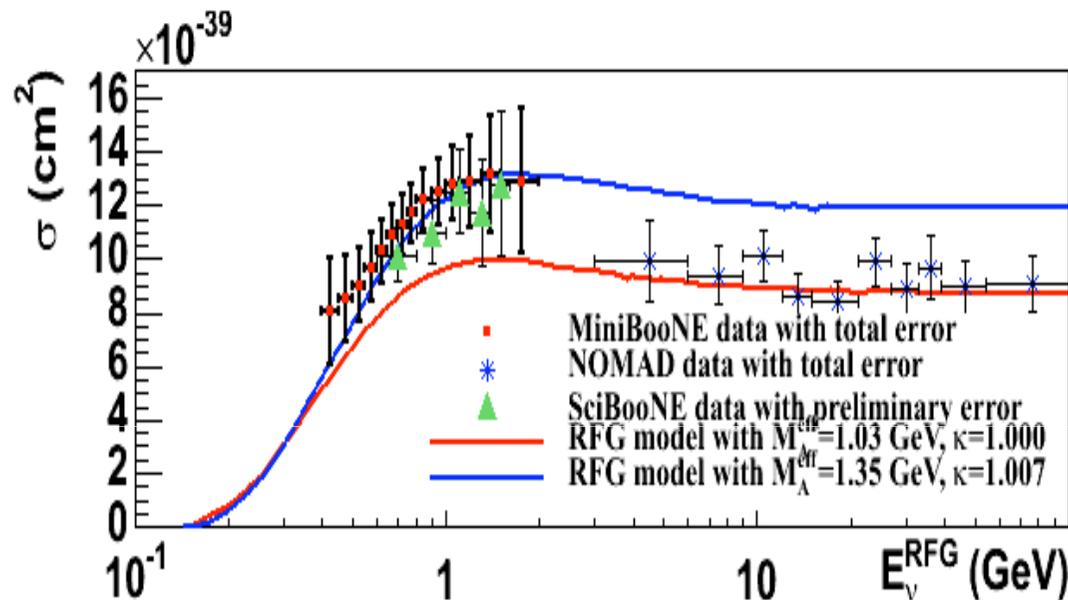
$$\frac{\partial \sigma}{\partial Q^2} = \frac{M^2 G_F^2 \cos \Theta}{8E_\nu^2} \left(A(Q^2) \pm \frac{B(Q^2)(s-u)}{M^2} + \frac{C(Q^2)(s-u)^2}{M^4} \right)$$

- A, B, C are function of Q^2 , with coefficients called form-factor.
- Form factor parameterize hadronic information and are measured experimentally.

$$F_A^{dipole} = \frac{F_A(0)}{\left(1 - \frac{q^2}{M_A^2}\right)^2}$$

World average value of $M_A = 1.01$

Cross-section discrepancy



World average (D2)	1.020±0.03
--------------------	------------

K2K SciFi (O)	1.200±0.12
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K2K SciBar (C)	1.140±0.10
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MiniBooNE (C)	1.350±0.17
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MINOS (Fe)	1.190±0.17
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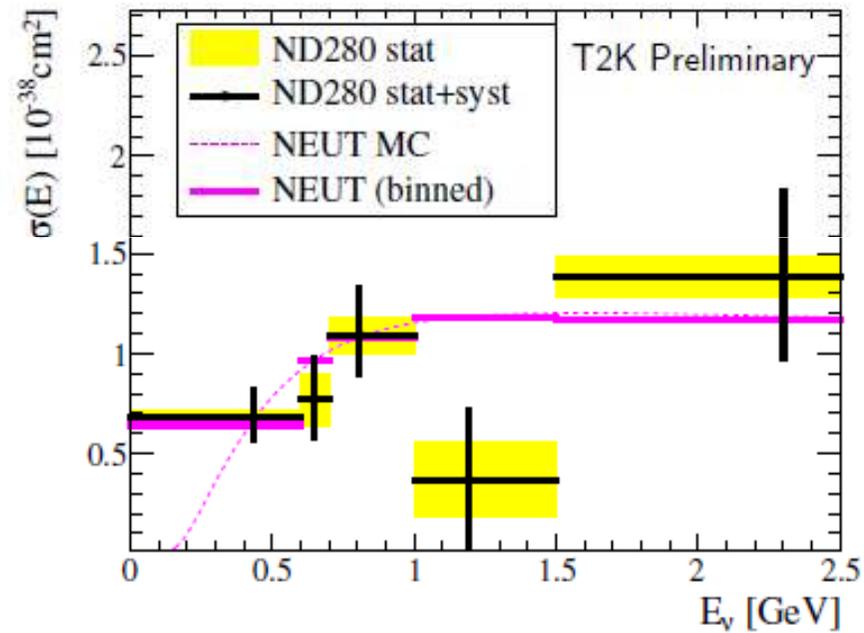
NOMAD (C)	1.050±0.06
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MiniBooNE QE data was fitted with higher M_A value 1.35

Also its QE sample has different muon kinematics.

Difference in cross-section along Q^2 reflects incompleteness of cross-section model.

T2K cross-section measurement



Fit to T2K data also agrees on higher value of $M_a = 1.21$

QE signal

MiniBooNE : only muon (1 track) no pion

- may include, multiple nucleon (not CCQE)

NOMAD: only muon (1 track) or muon+proton (2 track)

- Pure-QE Sample

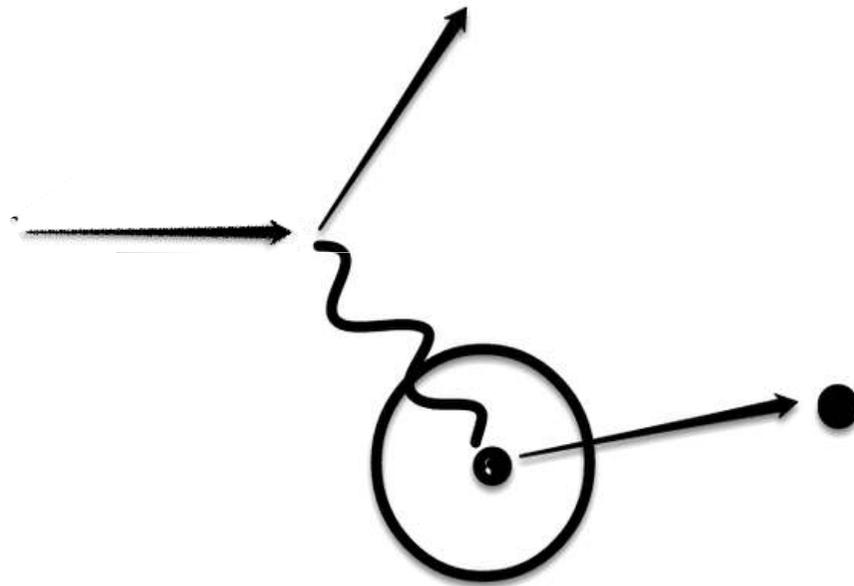
MinibooNE selected QE-like events which may includes additional interaction not foreseen before.

Possible reasons for the excess

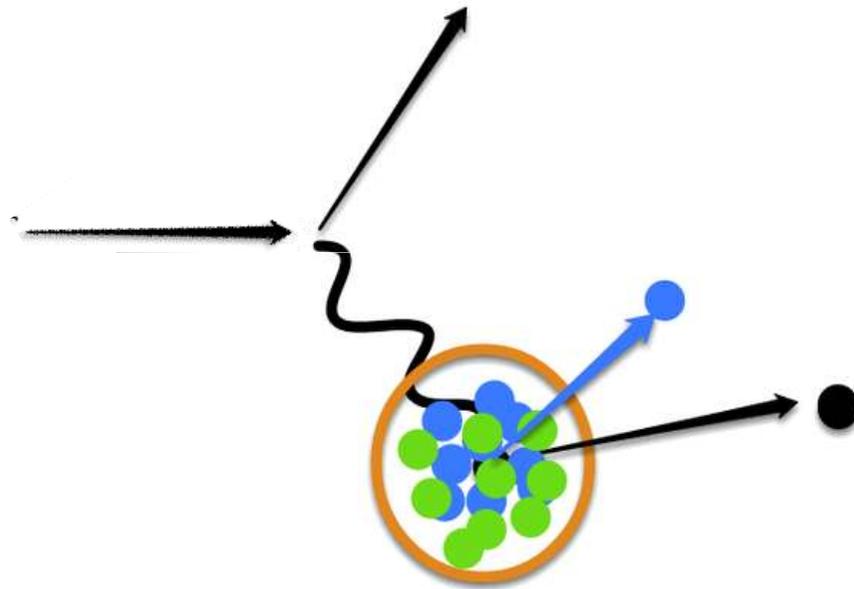
- Could there be some mode of interaction we failed to observe before?
 - Nuclear medium can alter QE free nucleon scattering prediction .
- Why didn't we see it before?
 - Bubble chamber experiments typically employed light targets (H₂ or D₂)
 - Required the detection of both ,the final state muon and single nucleon.
- If the data fits with $M_a=1.35$, good enough. Why not use that?
 - Muon kinematics altered => mis-reconstruction of the neutrino energy.

Need a model to explain this effect.

QE with Impulse Approximation



Nuclear correlation

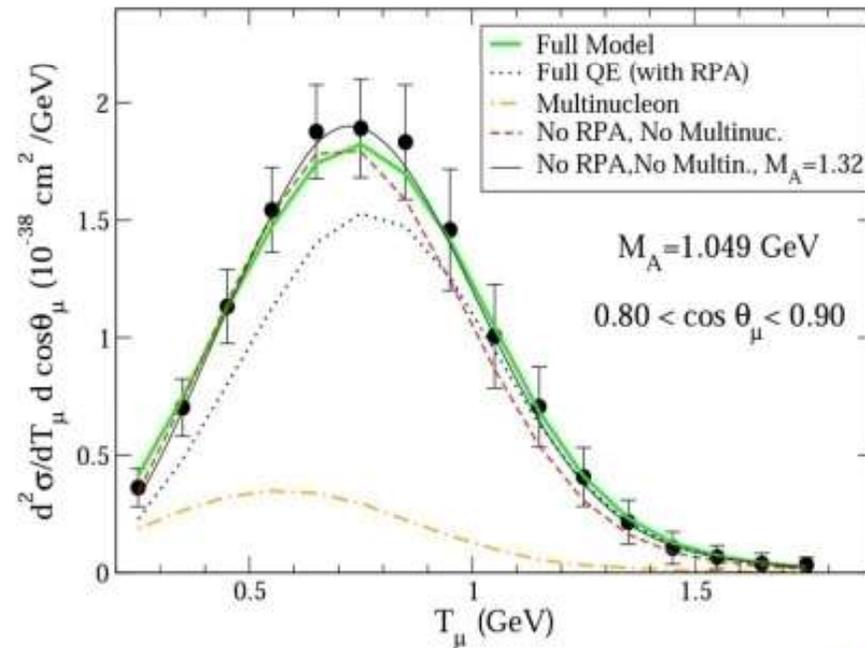


Nuclear correlation

Multinucleon ejection model +

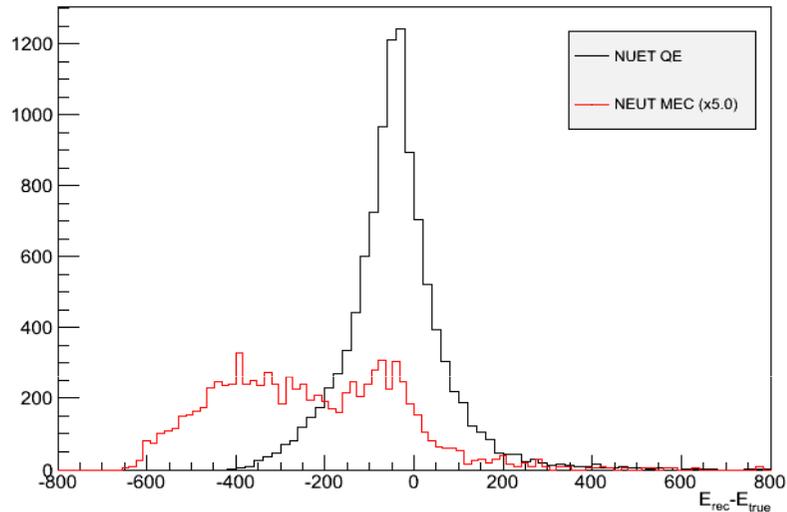
Random phase approximation

Nieves multinucleon + QE with RPA fits MiniBooNE data.



Concern for Oscillation Analysis

Energy misreconstruction $E > 740$ & $E < 760$



Black: only QE sample. Red : npnh events reconstructed as QE using formula given below

$$E_v^{QE} = \frac{m_p^2 - (m_n - E_b)^2 - m_\mu^2 + 2(m_n - E_b)E_\mu}{2(m_n - E_b - E_\mu + p_\mu \cos \theta_\mu)}$$

- Multi-nucleons interaction (npnh) have different lepton kinematics than CCQE.
- If tagged as CCQE leads to **misreconstruction of neutrino energy**.
- Consequently affects oscillation analysis
- Of concern at higher statistics as the statistical errors are reduced.

Updating Monte Carlo neutrino generator, **NEUT**

(official generator of T2K)

Multinucleon ejection:

- Nieves based on many body formalism, for the energy regions of QE and Δ excitation and the dip between the two.
- Additional correlated pair of nucleons

Random Phase Approximation:

- Effect of change in strength of electroweak coupling of nucleon in a nucleus due to presence of strongly interacting nucleons.
- Accounts for medium polarization effect in 1p1h.
- Improves prediction at low Q^2

Outlook

Next, I will test these models against T2K data.
A model dependent cross-section fit with new models in generator and more statistics.

Thank you.

Cross-section measurement

$$N_{\nu} = \Phi(E) \times \sigma(E) \times T$$

$\Phi(E)$ = Neutrinos Flux

$\sigma(E)$ = interaction Cross-section

T = number of nucleons. (Target, Size of the detector)

N_{ν} = *Observed neutrino event*

To increase the number of observed events

- **Increase the flux**
- Increase the energy ($\sigma_{\nu} \propto E$). But fixed by oscillation parameter.
- **Increase the density of nucleon by changing the target to heavy element.**

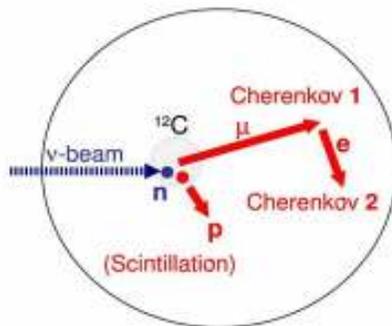
Higher statistics is achieved by increasing flux and changing over to heavy nucleus target.

Understanding the difference MiniBoone

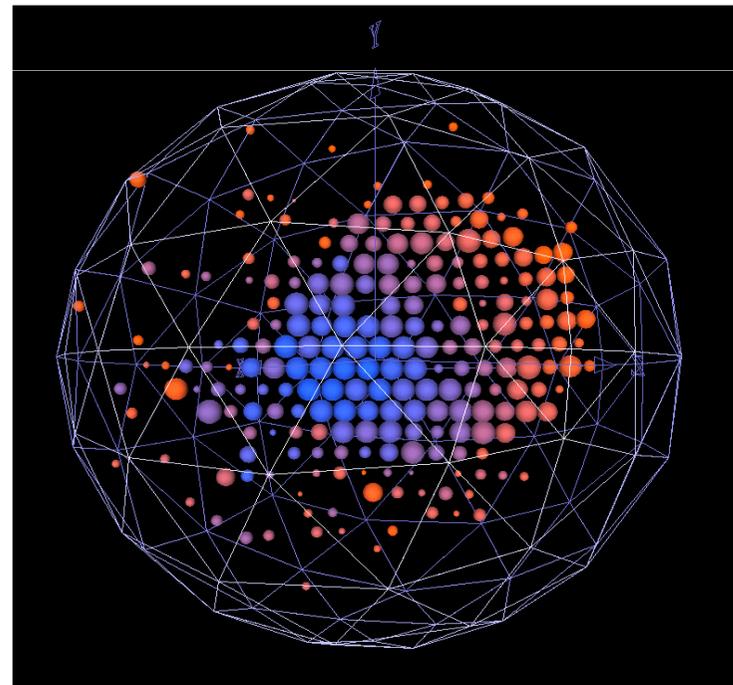
- 800t Cherenkov detector, filled with mineral oil (C) Energy ~ 700 MeV

QE Selection:

- muon identified with decay electron, no direct selection on proton
- CC1 π background are constrained based on CC1 π selected event



First experiment to make double differential cross-section plots possible because of high statistics it had. (model independent.)

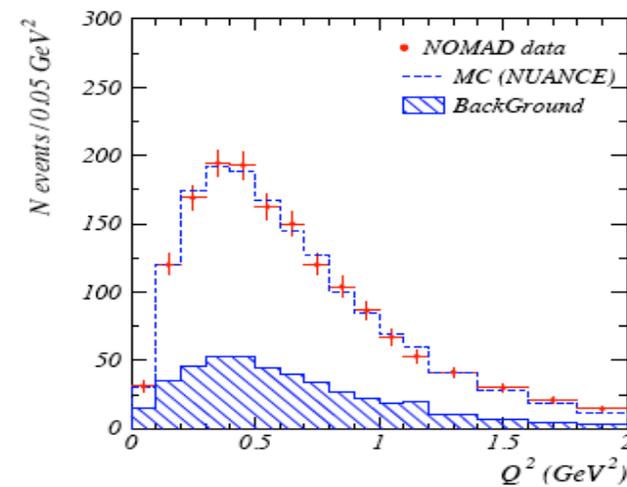
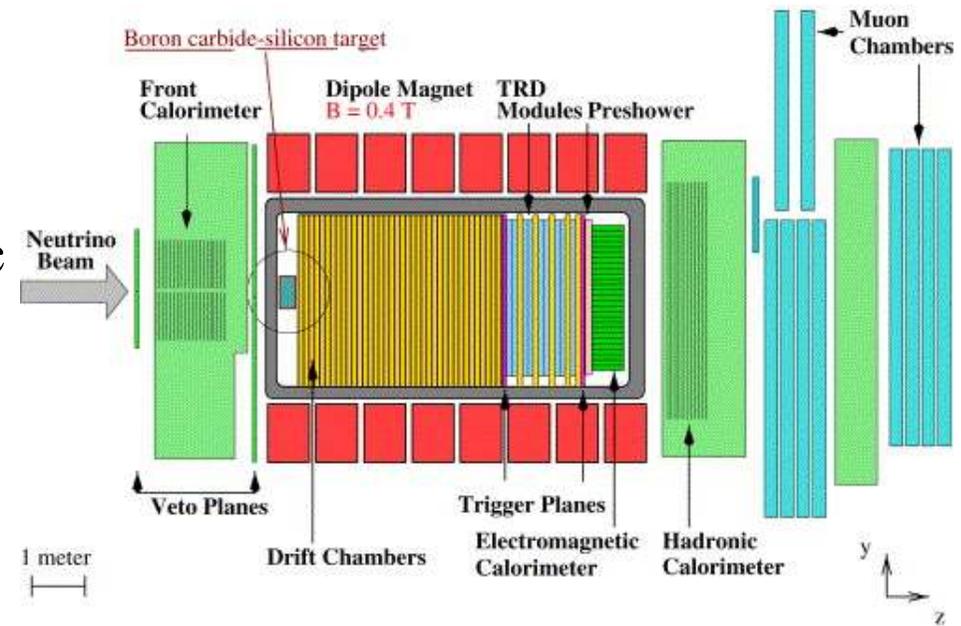


Understanding the difference NOMAD

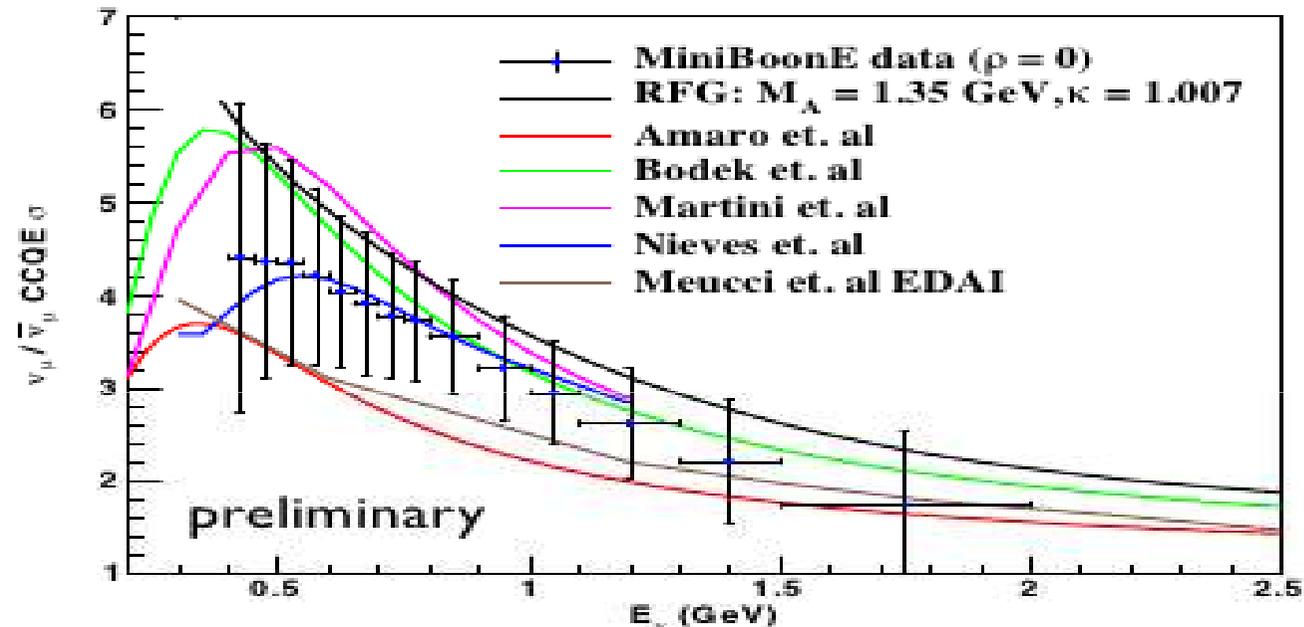
- Drift chambers with hadronic calorimeters and muon detectors situated in magnetic field ($E_\nu \sim 24$ GeV, carbon target)

QE Selection:

- “1 track” + “2 track” (muon, proton, ~ 3.5 k) samples



Theory rescue, Multi-nucleon ejection models



- Multi-nucleon ejection model (Nieves' et al) which best fit the data below 1.5 GeV. (now extended to higher energies within limit $q_3 < 1.2$)
- Transverse enhancement model (TEM, Bodek et. al.), in the region where Nieves' model fails.

Nieves multi-nucleon ejection model.

- Successfully tested electron-nucleus measurements.
- Extended many body formalism developed for computation of inclusive electron-nucleus cross section in the energy regions of QE and Δ excitation and the dip between the two.
- This formalism systematically incorporates different gauge boson absorption terms which will contribute to multi-nucleon ejection.
- Nuclear effects like Random Phase approximation (phase polarization) are taken into account.

Recipes for W-boson absorption.

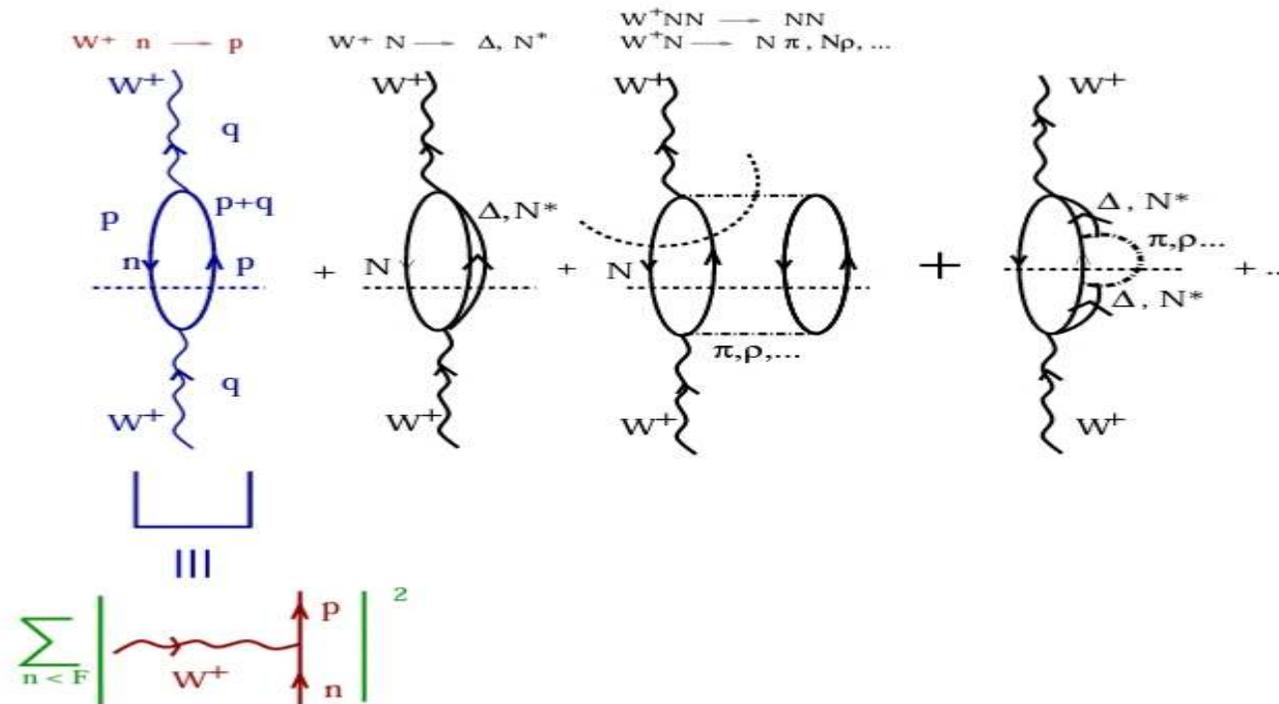
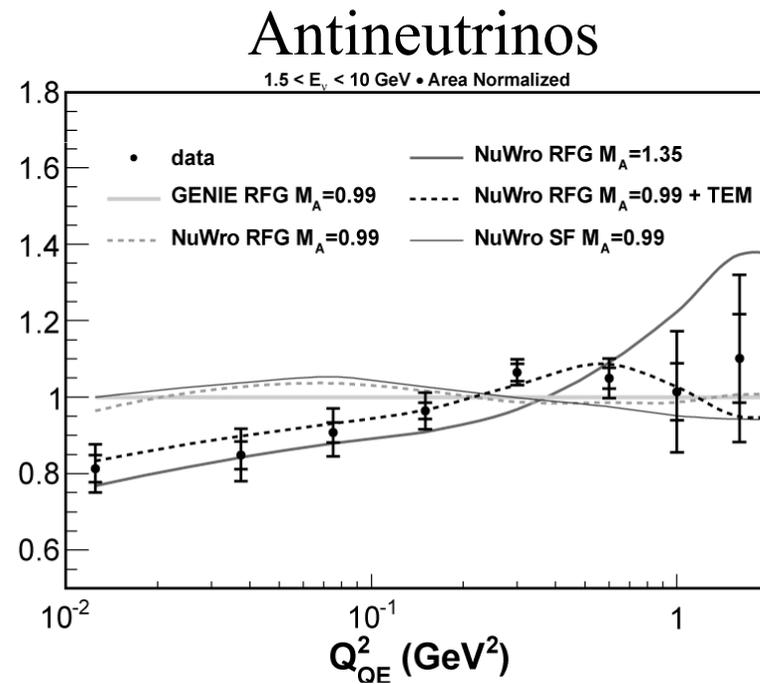
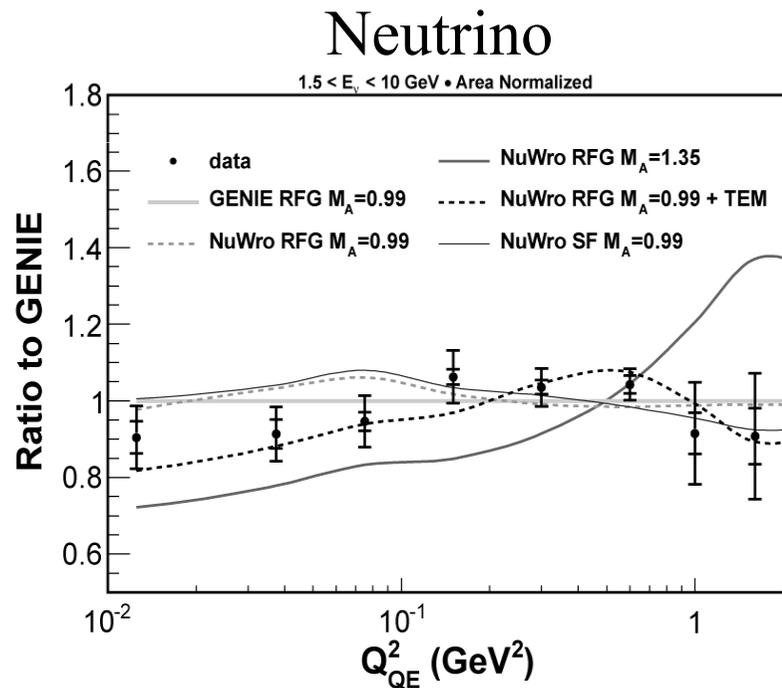


Figure 2.3: Diagrammatic representation of some mechanisms contributing to the W^+ -selfenergy

- absorption by one nucleon.
- absorption by pair of nucleon or more.
- Real or virtual meson production
- Excitation of Δ isobars and higher resonances dof

Validation by Minerva

- Uses finely segmented scintillator detector at Fermilab to measure ν_μ & $\bar{\nu}_\mu$ QE interactions on nuclear targets.
- At energies between 1.5 and 10 GeV .



Llewellyn-Smith formula for QE scattering

- Scattering cross-section of neutrinos off the nucleon is given by the Llewellyn-Smith formula / Smith-Moniz (RFG)
 - Impulse Approximation : gauge boson is absorbed by just one nucleon .
 - Use Fermi Gas model , i.e. $P(\text{nucleon}) < P_f \text{ max}$ ($P_f \text{ max}$ is function of #nucleons.)

$$\frac{\partial \sigma}{\partial Q^2} = \frac{M^2 G_F^2 \cos^2 \Theta}{8E_\nu^2} \left(A(Q^2) \pm \frac{B(Q^2)(s-u)}{M^2} + \frac{C(Q^2)(s-u)^2}{M^4} \right)$$

G_F is the Fermi constant, | M is the average nucleon mass, | θ_C is the Cabbibo angle; | E is the neutrino energy | s and u are Mandelstam variables

Form Factor

- A, B, C are function of Q^2 , with coefficients called form-factor.
- Form factor parameterize hadronic information and are measured experimentally.
 - Two vector form factor are know from electron scattering experiments.
 - Pseudo-scalar form factor contribution is negligible.
 - Only unknown Axial mass form factor, is measured using neutrino scattering.
 - Axial form factor in the dipole form is dependent on two parameters.
 - F_A is precisely known from beta decay experiment.
 - **So the only parameter left was M_A**

$$F_A^{dipole} = \frac{F_A(0)}{\left(1 - \frac{q^2}{M_A^2}\right)^2}$$

World average value of M_A 1.01

Sterile neutrino global Fit results

arXiv:1311.1335v1

	3+1 LOW	3+1 HIG	3+1 noMB	3+1 noLSND	3+2 LOW	3+2 HIG	3+1+1 LOW	3+1+1 HIG
χ_{\min}^2	291.7	261.8	236.1	278.4	284.4	256.4	289.8	259.0
NDF	256	250	218	252	252	246	253	247
GoF	6%	29%	19%	12%	8%	31%	6%	29%
$(\chi_{\min}^2)_{\text{APP}}$	99.3	77.0	50.9	91.8	87.7	69.8	94.8	75.5
$(\chi_{\min}^2)_{\text{DIS}}$	180.1	180.1	180.1	180.1	179.1	179.1	180.1	180.1
$\Delta\chi_{\text{PG}}^2$	12.7	4.8	5.1	6.4	17.7	7.5	14.9	3.4
NDF_{PG}	2	2	2	2	4	4	3	3
GoF_{PG}	0.2%	9%	8%	4%	0.1%	11%	0.2%	34%
$\Delta\chi_{\text{NO}}^2$	47.5	46.2	47.1	8.3	54.8	51.6	49.4	49.1
NDF_{NO}	3	3	3	3	7	7	6	6
$n\sigma_{\text{NO}}$	6.3σ	6.2σ	6.3σ	2.1σ	6.0σ	5.8σ	5.8σ	5.8σ