

1. Introduction 2. Requirements from Beam Delivery 3. Resonant Slow Extraction 4. Development of RF-KO 5. Summary Contents

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Study on Spill Ripple in RF-KO Method

In order to improve the time structure of the extracted beam for the fast 3D scanning, the ripple source was studied.

- 1. Time Structure for one FM period
- 2. Dual FM method
- 3. Separate function Method
- 4. Robust RF-KO method against Q-field ripple
- 5. Global Spill-Structure Control

1.4. Spill-Structure Control by Chromaticity

Simulation Result:

With increasing the chromaticity, both peak (a) and (b) are widened.

It is considered as follows:

Peak (A): the extraction region is increased with increasing the chromaticity.

Peak (B): The average distance from the particles in the extraction region to the boundary is to be long with incasing the extraction region. Further, the particles move obliquely toward the boundary due to amplitude beat through the RF-KO and due to momentum growth through the synchrotron oscillation. For a large

chromaticity, thus, it takes the long time to reach to the boundary, compared with for a small chromaticity.

3rd Integer Resonant Slow Extraction
\n- Analysis -
\n
$$
\frac{d^2x}{ds^2} + K(s)x = g(x, s)
$$
\n
$$
\frac{dr}{d\theta} = -Q\beta^2rg(X, \theta)sin\phi
$$
\n
$$
\frac{d^2X}{d\theta^2} + Q^2X = Q^2\beta^2g(X, \theta)
$$
\n
$$
X = \frac{x}{\sqrt{\beta(s)}}, \theta = \int \frac{ds}{QB}
$$
\n
$$
g(x, s) = \sum_{j} S_jx^2\delta(s - s_j)
$$
\n
$$
X = r \cdot cos(Q\theta + \phi) \equiv r \cdot cos\phi
$$
\n
$$
X' = r \cdot sin(Q\theta + \phi) \equiv r \cdot sin\phi
$$
\n
$$
r = \sqrt{X^2 + X'^2}
$$
\n
$$
\frac{d\phi}{d\theta} = -\frac{r^3}{4\pi} \sum_{j} S_j \beta^3 \sin(3\Psi + p\theta_j)
$$
\n
$$
r = \sqrt{X^2 + X'^2}
$$
\n
$$
\frac{d\phi}{d\theta} = q - \frac{r}{8\pi} \sum_{j} S_j \beta^3/2 \cos(3\Psi + p\theta_j)
$$
\n
$$
\left(\frac{X}{X'}\right) = \frac{1}{\sqrt{\beta}} \left(\frac{1}{\alpha} \frac{0}{\beta}\right) \left(\frac{x}{x'}\right)
$$
\n
$$
\psi = \phi - \frac{p}{3}\theta = \left(Q - \frac{p}{3}\right)\theta + \phi = q\theta + \phi
$$

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