

# Polarization amplitudes and CP asymmetries in $B^0 \rightarrow \Phi K^*(892)^0$ at LHCb

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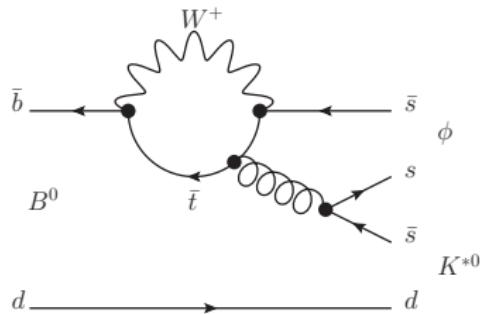
CHIPP PhD Winter School  
Grindelwald, Switzerland 2015

# Overview

- 1 Motivation
- 2 LHCb experiment
- 3 Angular analysis
- 4 Conclusion

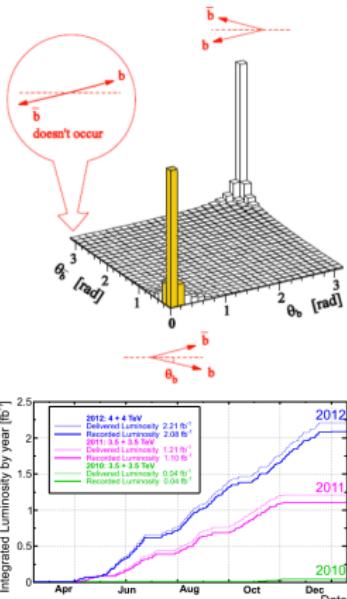
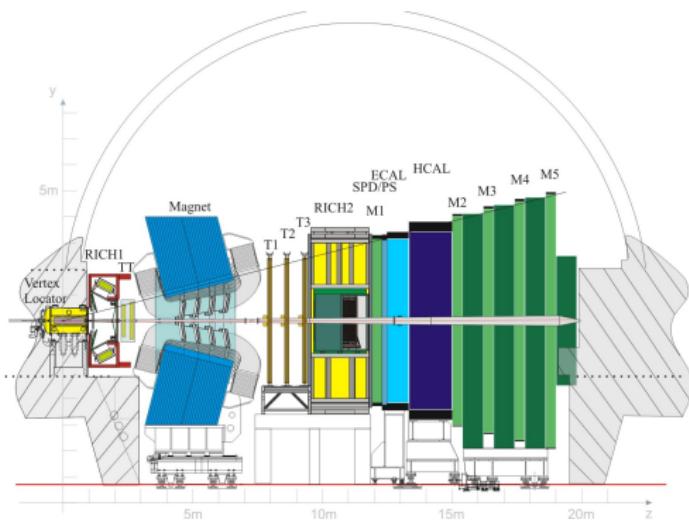
# Motivation

- The first evidence for the decay  $B \rightarrow \phi K^*$  was provided by CLEO (*Phys.Rev.Lett.86,3718 (2001)*) and BABAR (*Phys.Rev.Lett.87, 151801 (2001)*) experiments
- In the SM, the decay  $B_d^0 \rightarrow \phi K^*(892)^0$  proceeds mainly via the gluonic penguin diagram (b → s transition)
- This b → s transition is sensitive to contributions from physics beyond the SM.
- The pseudoscalar to vector-vector decay  $B_d^0 \rightarrow \phi K^*(892)^0$  also allows to study the CP violation in polarization parameters
- In this talk I present the measurements of the polarization amplitudes, phases and CP asymmetries using 2012 data, with an integrated luminosity of  $2.0 \text{ fb}^{-1}$ , collected at a centre-of-mass energy of  $\sqrt{s} = 8 \text{ TeV}$  at the LHCb experiment.



# The LHCb detector

LHCb :dedicated to the study of CP violation and rare decays in b-quark and c-quark sectors  
also indirect search for New Physics



- LHCb is a single-arm forward spectrometer at the LHC
- Optimized for measurements in **heavy-flavour physics**
- Recording pp collisions with  $\sqrt{s} = 7 \text{ TeV}$  (in 2011) and  $8 \text{ TeV}$  (in 2012)
- The experiment has a large forward acceptance of  $2 < \eta < 5$

# Analysis Strategy

- $B^0$  is a pseudoscalar-meson with spin 0;  $\phi$  and  $K^*(892)^0$  are vector-mesons with spin 1 decaying into  $K^+K^-$  and  $K^+\pi^-$  (P-wave) respectively.
- Angular momentum conservation allows three possible helicity configurations with amplitudes denoted  $H_{+1}$ ,  $H_{-1}$  and  $H_0$ .
- In the transversity basis, we can write these in term of a longitudinal polarization,  $A_0$ , and two transverse polarizations,  $A_\perp$  and  $A_\parallel$

$$A_0 = H_0, \quad A_\perp = \frac{H_{+1} - H_{-1}}{\sqrt{2}} \quad \text{and} \quad A_\parallel = \frac{H_{+1} + H_{-1}}{\sqrt{2}}.$$

- There are also contributions from S-wave  $K^+K^-$  and S-wave  $K^+\pi^-$  with spin 0. (amplitudes  $A_S^{KK}$  and  $A_S^{K\pi}$ )
- The amplitudes have magnitudes and relative to  $A_0$  phases defined as:

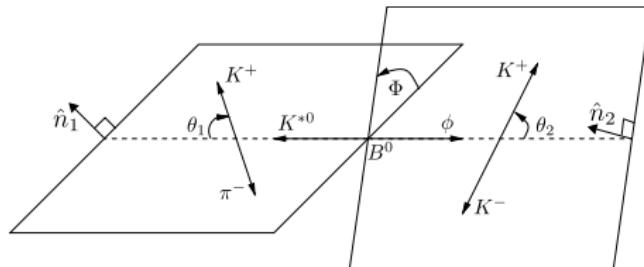
$$A_\parallel = |A_\parallel| e^{i\delta_\parallel}, \quad A_\perp = |A_\perp| e^{i\delta_\perp}, \quad A_S^{K\pi} = |A_S^{K\pi}| e^{i\delta_S^{K\pi}}, \quad A_S^{KK} = |A_S^{KK}| e^{i\delta_S^{KK}}, \quad \delta_0 = 0$$

- To determine these quantities, an analysis of the angular distribution and the invariant masses of the decay products is performed.

# Angular Analysis

- The angular analysis is performed in term of the three helicity angles  $(\theta_1, \theta_2, \Phi)$
- The flavour of the decaying the  $B^0$  meson is determined by the charge of the pion from the  $K^{*0}$  decay
- $B^0$  and  $\bar{B}^0$  decays are analysed separately
- Taking into account both the P- and S-wave contributions and their interference, the differential decay rate is given by:

$$d^5\Gamma \propto |PWave \times M_1(m_1)M_1(m_2) + SWave(K\pi) \times M_0(m_1)M_1(m_2) + SWave(KK) \times M_1(m_1)M_0(m_2)|^2$$



$$\begin{aligned} d^5\Gamma = \frac{9}{8\pi} & |(\mathcal{A}_0 \cos \theta_1 \cos \theta_2 + \frac{\mathcal{A}_{||}}{\sqrt{2}} \sin \theta_1 \sin \theta_2 \cos \varphi + \frac{\mathcal{A}_{\perp}}{\sqrt{2}} \sin \theta_1 \sin \theta_2 \sin \varphi) M_1(m_1) M_1(m_2) \\ & + \frac{\mathcal{A}_S}{\sqrt{3}} \cos \theta_1 M_0(m_1) M_1(m_2) + \frac{\mathcal{A}'_S}{\sqrt{3}} \cos \theta_2 M_1(m_1) M_0(m_2) |^2 d\phi(K, K, \pi) \end{aligned}$$

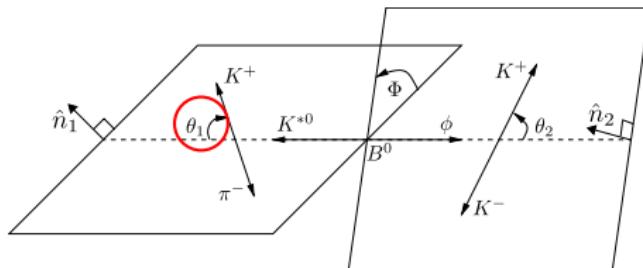
which can be re-written as:

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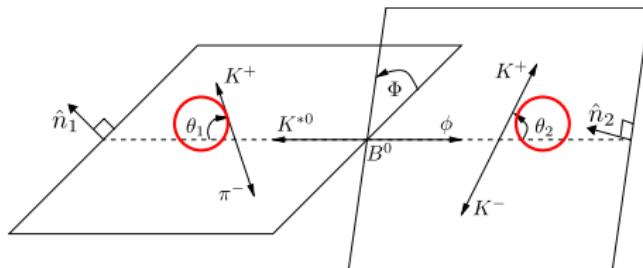
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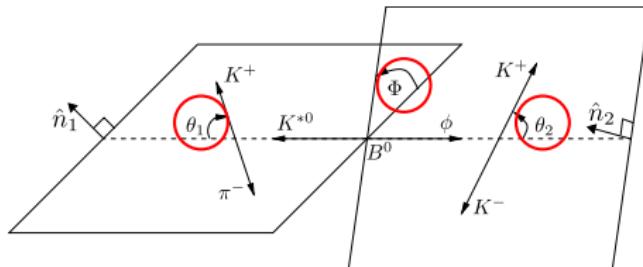
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# Angular Analysis

$$d^5\Gamma = \frac{9}{8\pi} \sum_{i=1}^{15} h_i f_i(\theta_1, \theta_2, \Phi) \mathcal{M}_i(m_{K\pi}, m_{KK}) d\Omega(KKK\pi).$$

$i$	$h_i$	$f_i(\theta_1, \theta_2, \Phi)$	$\mathcal{M}_i(m_{K\pi}, m_{KK})$
1	$ A_0 ^2$	$\cos \theta_1^2 \cos \theta_2^2$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
2	$ A_\parallel ^2$	$\frac{1}{4} \sin \theta_1^2 \sin \theta_2^2 (1 + \cos(2\Phi))$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
3	$ A_\perp ^2$	$\frac{1}{4} \sin \theta_1^2 \sin \theta_2^2 (1 - \cos(2\Phi))$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
4	$ A_\perp   A_*^*  e^{i(\delta_\perp - \delta_\parallel)}$	$-\frac{1}{2} \sin \theta_1^2 \sin \theta_2^2 \sin(2\Phi)$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
5	$ A_\parallel   A_*^*  e^{i\delta_\parallel}$	$\sqrt{2} \cos \theta_1 \sin \theta_1 \cos \theta_2 \sin \theta_2 \cos \Phi$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
6	$ A_\perp   A_*^*  e^{i\delta_\perp}$	$-\sqrt{2} \cos \theta_1 \sin \theta_1 \cos \theta_2 \sin \theta_2 \sin \Phi$	$ M_1^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
7	$ A_S^{K\pi} ^2$	$\frac{1}{3} \cos \theta_2^2$	$ M_0^{K\pi}(m_{K\pi}) ^2  M_1^{KK}(m_{KK}) ^2$
8	$ A_\parallel   A_S^{K\pi}  e^{i(\delta_\parallel - \delta_S^{K\pi})}$	$\frac{\sqrt{6}}{3} \sin \theta_1 \cos \theta_2 \sin \theta_2 \cos \Phi$	$ M_1^{KK}(m_{KK}) ^2 M_1^{K\pi}(m_{K\pi}) M_0^{*K\pi}(m_{K\pi})$
9	$ A_\perp   A_S^{K\pi}  e^{i(\delta_\perp - \delta_S^{K\pi})}$	$-\frac{\sqrt{6}}{3} \sin \theta_1 \cos \theta_2 \sin \theta_2 \sin \Phi$	$ M_1^{KK}(m_{KK}) ^2 M_1^{K\pi}(m_{K\pi}) M_0^{*K\pi}(m_{K\pi})$
10	$ A_0   A_S^{*K\pi}  e^{-i\delta_S^{K\pi}}$	$\frac{2}{\sqrt{3}} \cos \theta_1 \cos \theta_2^2$	$ M_1^{KK}(m_{KK}) ^2 M_1^{K\pi}(m_{K\pi}) M_0^{*K\pi}(m_{K\pi})$
11	$ A_S^{KK} ^2$	$\frac{1}{3} \cos \theta_1^2$	$ M_0^{KK}(m_{KK}) ^2  M_1^{K\pi}(m_{K\pi}) ^2$
12	$ A_\parallel   A_S^{*KK}  e^{i(\delta_\parallel - \delta_S^{KK})}$	$\frac{\sqrt{6}}{3} \sin \theta_1 \cos \theta_1 \sin \theta_2 \cos \Phi$	$ M_1^{K\pi}(m_{K\pi}) ^2 M_1^{KK}(m_{KK}) M_0^{*KK}(m_{KK})$
13	$ A_\perp   A_S^{*KK}  e^{i(\delta_\perp - \delta_S^{KK})}$	$-\frac{\sqrt{6}}{3} \sin \theta_1 \cos \theta_1 \sin \theta_2 \sin \Phi$	$ M_1^{K\pi}(m_{K\pi}) ^2 M_1^{KK}(m_{KK}) M_0^{*KK}(m_{KK})$
14	$ A_0   A_S^{*KK}  e^{-i\delta_S^{KK}}$	$\frac{2}{\sqrt{3}} \cos \theta_1^2 \cos \theta_2$	$ M_1^{K\pi}(m_{K\pi}) ^2 M_1^{KK}(m_{KK}) M_0^{*KK}(m_{KK})$
15	$ A_S^{K\pi}   A_S^{*KK}  e^{i(\delta_S^{K\pi} - \delta_S^{KK})}$	$\frac{2}{3} \cos \theta_1 \cos \theta_2$	$M_1^{KK}(m_{KK}) M_0^{K\pi}(m_{K\pi}) M_0^{*KK}(m_{KK}) M_1^{*K\pi}(m_{K\pi})$

# Modelling the $K\pi$ P-wave and S-wave

- The  $K\pi$  P-wave amplitude (the resonant mass) is parameterised with a relativistic Breit-Wigner spin-1

$$M_1^{K\pi}(m_{K\pi}) = N_1 \frac{m_{K\pi}}{q} \frac{m_0^{K^*} \Gamma_1^{K\pi}(m_{K\pi})}{(m_0^{K^*})^2 - m_{K\pi}^2 - im_0^{K\pi} \Gamma_1^{K\pi}(m_{K\pi})}$$

The mass-dependent width is given by

$$\Gamma_1^{K\pi}(m_{K\pi}) = \Gamma_0^{K^*} \frac{m_0^{K^*}}{m_{K\pi}} \frac{1+r^2 q_0^2}{1+r^2 q^2} \left(\frac{q}{q_0}\right)^3$$

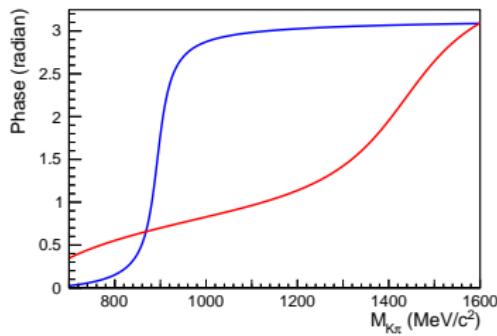
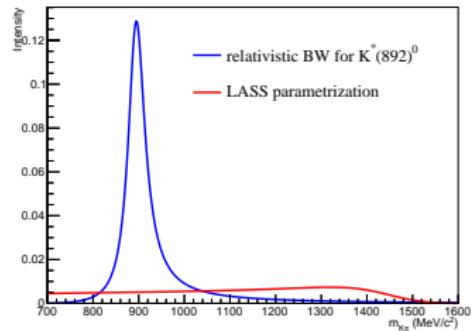
- The LASS parameterisation is used to describe the  $K\pi$  S-wave (addition of a rel. BreitWigner spin-0  $K_0^*(1430)$  and a nonresonant amplitude):

$$M_0^{K\pi}(m_{K\pi}) = N_2 \frac{m_{K\pi}}{q} \left[ \frac{1}{\cot \delta_\beta - i} + e^{2i\delta_\beta} \frac{1}{\cot \delta_\alpha(m_{K\pi}) - i} \right]$$

Resonance:  $\cot \delta_\alpha(m_{K\pi}) = \frac{(m_0^{K^*})^2 - m_{K\pi}^2}{m_0^{K^*} \Gamma_0(m_{K\pi})}$

Non-resonance:  $\cot \delta_\beta = \frac{1}{aq} + \frac{1}{2} bq$

a is the scattering length; b is the effective range



# Modelling the $KK$ P-wave and S-wave

- For the decay  $\phi \rightarrow K^+K^-$  (a vector meson decays in two pseudoscalars with equal masses), the P-wave can be parametrized with a rel. Breit-Wigner spin-1, given by:

$$M_1^{KK}(m_{KK}) = N_3 \sqrt{\frac{m_{KK}}{q}} \frac{\sqrt{m_{KK} \Gamma_1^{KK}(m_{KK})}}{(m_0^\phi)^2 - m_{KK}^2 - im_0^\phi \Gamma_1^{KK}(m_{KK})}$$

where,  $\Gamma_1^{KK}(m_{KK}) = \Gamma_0^\phi \frac{m_0^\phi}{m_{KK}} \frac{1+r^2 q_0^2}{1+r^2 q^2} \left(\frac{q}{q_0}\right)^3$

- The  $K^+K^-$  S-wave is described by a coupled-channel Breit-Wigner (Flatté parameterization) describing the  $f_0(980)$  meson close to  $K^+K^-$  threshold

$$M_0^{KK}(m_{KK}) = N_4 \frac{1}{m_{f_0}^2 - m_{KK}^2 - im_{f_0}(g_{\pi\pi}\rho_{\pi\pi} + g_{KK}\rho_{KK})},$$

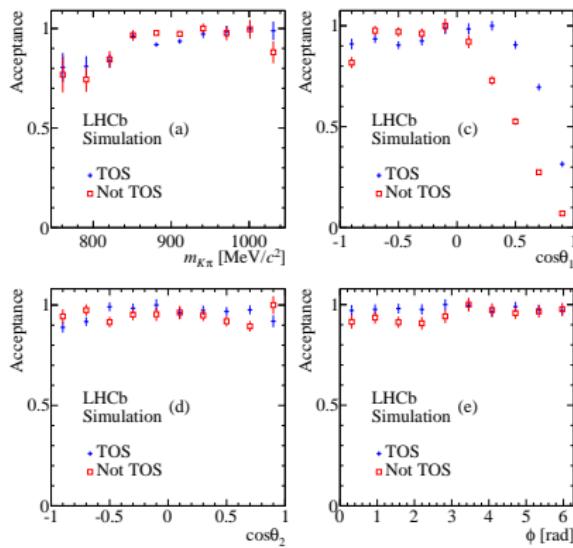
$g_{KK,\pi\pi}$  are partial decay widths and the  $\rho_{KK,\pi\pi}$  are phase-space factors.

$$\rho_{KK} = \begin{cases} (1 - 4m_K^2/m^2)^{1/2} & \text{above } KK \text{ threshold} \\ i(4m_K^2/m^2 - 1)^{1/2} & \text{below } KK \text{ threshold} \end{cases}$$

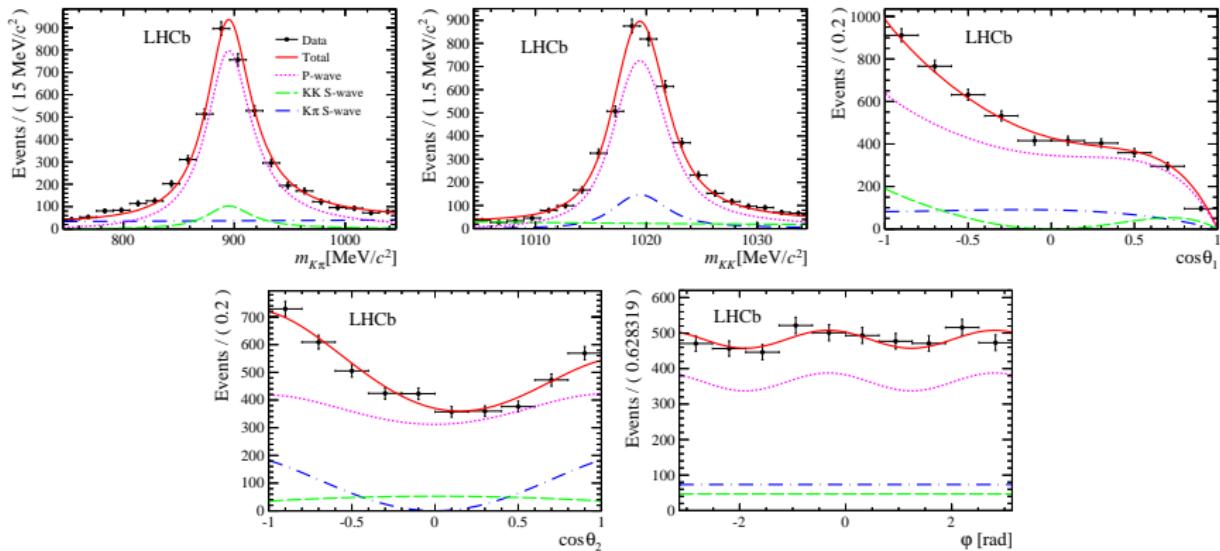
# Angular Acceptance

- Due to detector geometry and kinematic cuts, the acceptance of the detector is not uniform as a function of the decay angles and invariant mass. We have to correct for it.

- TOS (Trigger On Signal)
- TIS (Trigger Independent of Signal)
- 17% overlap between TOS and TIS are treated as TOS.  
The remaining TIS are labelled "Not TOS"



# Angular analysis results



- Data are separated in four categories, depending on the flavour of the B meson and the trigger category TOS and TIS.
- A simultaneous fit is performed to the four subsets

+	- - - - -	+	- - - - -	+
	{TOS;B0}		1163	
	{TIS;B0}		1247	
	{TOS;B0bar}		1175	
	{TIS;B0bar}		1239	
+	- - - - -	+	- - - - -	+

# Systematic uncertainties

- Various sources of systematic uncertainty are studied
  - Uncertainty on acceptance correction
  - Difference in kinematic variables between Data and MC
  - The  $K^+K^-K^+\pi^-$  mass model used to determine the signal weights for the angular analysis.
  - The models of the S-wave in the  $K^+K^-$  and  $K^+\pi^-$  system.

Measurement	Acceptance	Data/MC	Mass model	S-wave	Total
$f_L$	0.004	0.021	0.002	0.002	0.022
$f_\perp$	0.003	0.009	0.001	0.002	0.010
$f_S(K\pi)$	0.007	0.005	0.001	0.002	0.009
$f_S(KK)$	0.003	0.004	0.002	0.004	0.007
$\delta_\perp$	0.015	0.002	0.006	0.008	0.018
$\delta_\parallel$	0.015	0.004	0.004	0.006	0.017
$\delta_S(K\pi)$	0.011	0.020	0.004	0.055	0.060
$\delta_S(KK)$	0.013	0.002	0.004	0.018	0.023
$A_0^{CP}$	-	0.001	0.002	0.006	0.006
$A_\perp^{CP}$	-	0.005	0.006	0.004	0.009
$A_S(K\pi)^{CP}$	-	0.001	0.005	0.018	0.019
$A_S(KK)^{CP}$	-	0.006	0.009	0.046	0.047
$\delta_\perp^{CP}$	-	0.004	0.001	0.003	0.005
$\delta_\parallel^{CP}$	-	0.008	0.002	0.004	0.009
$\delta_S(K\pi)^{CP}$	-	0.002	0.003	0.027	0.027
$\delta_S(KK)^{CP}$	-	0.002	0.002	0.014	0.014

# Angular analysis results

- Parameters measured in the angular analysis. The first and second uncertainties are statistical and systematic, respectively.

Parameter	Definition	Fitted value
$f_L$	$0.5( A_0 ^2/F_P +  \bar{A}_0 ^2/\bar{F}_P)$	$0.503 \pm 0.011 \pm 0.022$
$f_\perp$	$0.5( A_\perp ^2/F_P +  \bar{A}_\perp ^2/\bar{F}_P)$	$0.221 \pm 0.009 \pm 0.010$
$f_S(K\pi)$	$0.5( A_S^{K\pi} ^2 +  \bar{A}_S^{K\pi} ^2)$	$0.152 \pm 0.007 \pm 0.009$
$f_S(KK)$	$0.5( A_S^{KK} ^2 +  \bar{A}_S^{KK} ^2)$	$0.097 \pm 0.007 \pm 0.007$
$\delta_\perp$	$0.5(\arg A_\perp + \arg \bar{A}_\perp)$	$2.610 \pm 0.038 \pm 0.018$
$\delta_\parallel$	$0.5(\arg A_\parallel + \arg \bar{A}_\parallel)$	$2.524 \pm 0.038 \pm 0.017$
$\delta_S(K\pi)$	$0.5(\arg A_S^{K\pi} + \arg \bar{A}_S^{K\pi})$	$2.200 \pm 0.033 \pm 0.060$
$\delta_S(KK)$	$0.5(\arg A_S^{KK} + \arg \bar{A}_S^{KK})$	$2.536 \pm 0.045 \pm 0.023$

$$F_P = |A_0|^2 + |A_\parallel|^2 + |A_\perp|^2, F_S = |A_S^{K\pi}|^2 + |A_S^{KK}|^2, F_P + F_S = 1$$

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$$F_P = |A_0|^2 + |A_\parallel|^2 + |A_\perp|^2, F_S = |A_S^{K\pi}|^2 + |A_S^{KK}|^2, F_P + F_S = 1$$

- The value of  $f_L$  is close to 0.5, indicating that the longitudinal and transverse polarizations have similar size

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$\delta_\perp$	$0.5(\arg A_\perp + \arg \bar{A}_\perp)$	$2.610 \pm 0.038 \pm 0.018$
$\delta_\parallel$	$0.5(\arg A_\parallel + \arg \bar{A}_\parallel)$	$2.524 \pm 0.038 \pm 0.017$
$\delta_S(K\pi)$	$0.5(\arg A_S^{K\pi} + \arg \bar{A}_S^{K\pi})$	$2.200 \pm 0.033 \pm 0.060$
$\delta_S(KK)$	$0.5(\arg A_S^{KK} + \arg \bar{A}_S^{KK})$	$2.536 \pm 0.045 \pm 0.023$

$$F_P = |A_0|^2 + |A_\parallel|^2 + |A_\perp|^2, F_S = |A_S^{K\pi}|^2 + |A_S^{KK}|^2, F_P + F_S = 1$$

- The value of  $f_L$  is close to 0.5, indicating that the longitudinal and transverse polarizations have similar size
- Significant S-wave contributions are found in both the  $K^+K^-$  and  $K^+\pi^-$  systems

# Angular analysis results

Parameter	Definition	Fitted value
$f_L$	$0.5( A_0 ^2/F_P +  \bar{A}_0 ^2/\bar{F}_P)$	$0.503 \pm 0.011 \pm 0.022$
$f_\perp$	$0.5( A_\perp ^2/F_P +  \bar{A}_\perp ^2/\bar{F}_P)$	$0.221 \pm 0.009 \pm 0.010$
$f_S(K\pi)$	$0.5( A_S^{K\pi} ^2 +  \bar{A}_S^{K\pi} ^2)$	$0.152 \pm 0.007 \pm 0.009$
$f_S(KK)$	$0.5( A_S^{KK} ^2 +  \bar{A}_S^{KK} ^2)$	$0.097 \pm 0.007 \pm 0.007$
$\delta_\perp$	$0.5(\arg A_\perp + \arg \bar{A}_\perp)$	$2.610 \pm 0.038 \pm 0.018$
$\delta_\parallel$	$0.5(\arg A_\parallel + \arg \bar{A}_\parallel)$	$2.524 \pm 0.038 \pm 0.017$
$\delta_S(K\pi)$	$0.5(\arg A_S^{K\pi} + \arg \bar{A}_S^{K\pi})$	$2.200 \pm 0.033 \pm 0.060$
$\delta_S(KK)$	$0.5(\arg A_S^{KK} + \arg \bar{A}_S^{KK})$	$2.536 \pm 0.045 \pm 0.023$
$A_0^{CP}$	$( A_0 ^2/F_P -  \bar{A}_0 ^2/\bar{F}_P)/( A_0 ^2/F_P +  \bar{A}_0 ^2/\bar{F}_P)$	$-0.020 \pm 0.022 \pm 0.006$
$A_\perp^{CP}$	$( A_\perp ^2/F_P -  \bar{A}_\perp ^2/\bar{F}_P)/( A_\perp ^2/F_P +  \bar{A}_\perp ^2/\bar{F}_P)$	$-0.035 \pm 0.042 \pm 0.009$
$\delta_\perp^{CP}$	$0.5(\arg A_\perp - \arg \bar{A}_\perp)$	$+0.031 \pm 0.038 \pm 0.005$
$\delta_\parallel^{CP}$	$0.5(\arg A_\parallel - \arg \bar{A}_\parallel)$	$+0.020 \pm 0.038 \pm 0.009$
$A_S(K\pi)^{CP}$	$( A_S^{K\pi} ^2 -  \bar{A}_S^{K\pi} ^2)/( A_S^{K\pi} ^2 +  \bar{A}_S^{K\pi} ^2)$	$+0.119 \pm 0.049 \pm 0.019$
$A_S(KK)^{CP}$	$( A_S^{KK} ^2 -  \bar{A}_S^{KK} ^2)/( A_S^{KK} ^2 +  \bar{A}_S^{KK} ^2)$	$+0.002 \pm 0.072 \pm 0.047$
$\delta_S(K\pi)^{CP}$	$0.5(\arg A_S^{K\pi} - \arg \bar{A}_S^{K\pi})$	$+0.027 \pm 0.033 \pm 0.027$
$\delta_S(KK)^{CP}$	$0.5(\arg A_S^{KK} - \arg \bar{A}_S^{KK})$	$+0.085 \pm 0.045 \pm 0.014$

# Angular analysis results

Parameter	Definition	Fitted value
$f_L$	$0.5( A_0 ^2/F_P +  \bar{A}_0 ^2/\bar{F}_P)$	$0.503 \pm 0.011 \pm 0.022$
$f_\perp$	$0.5( A_\perp ^2/F_P +  \bar{A}_\perp ^2/\bar{F}_P)$	$0.221 \pm 0.009 \pm 0.010$
$f_S(K\pi)$	$0.5( A_S^{K\pi} ^2 +  \bar{A}_S^{K\pi} ^2)$	$0.152 \pm 0.007 \pm 0.009$
$f_S(KK)$	$0.5( A_S^{KK} ^2 +  \bar{A}_S^{KK} ^2)$	$0.097 \pm 0.007 \pm 0.007$
$\delta_\perp$	$0.5(\arg A_\perp + \arg \bar{A}_\perp)$	$2.610 \pm 0.038 \pm 0.018$
$\delta_\parallel$	$0.5(\arg A_\parallel + \arg \bar{A}_\parallel)$	$2.524 \pm 0.038 \pm 0.017$
$\delta_S(K\pi)$	$0.5(\arg A_S^{K\pi} + \arg \bar{A}_S^{K\pi})$	$2.200 \pm 0.033 \pm 0.060$
$\delta_S(KK)$	$0.5(\arg A_S^{KK} + \arg \bar{A}_S^{KK})$	$2.536 \pm 0.045 \pm 0.023$
$A_0^{CP}$	$( A_0 ^2/F_P -  \bar{A}_0 ^2/\bar{F}_P)/( A_0 ^2/F_P +  \bar{A}_0 ^2/\bar{F}_P)$	$-0.020 \pm 0.022 \pm 0.006$
$A_\perp^{CP}$	$( A_\perp ^2/F_P -  \bar{A}_\perp ^2/\bar{F}_P)/( A_\perp ^2/F_P +  \bar{A}_\perp ^2/\bar{F}_P)$	$-0.035 \pm 0.042 \pm 0.009$
$\delta_\perp^{CP}$	$0.5(\arg A_\perp - \arg \bar{A}_\perp)$	$+0.031 \pm 0.038 \pm 0.005$
$\delta_\parallel^{CP}$	$0.5(\arg A_\parallel - \arg \bar{A}_\parallel)$	$+0.020 \pm 0.038 \pm 0.009$
$A_S(K\pi)^{CP}$	$( A_S^{K\pi} ^2 -  \bar{A}_S^{K\pi} ^2)/( A_S^{K\pi} ^2 +  \bar{A}_S^{K\pi} ^2)$	$+0.119 \pm 0.049 \pm 0.019$
$A_S(KK)^{CP}$	$( A_S^{KK} ^2 -  \bar{A}_S^{KK} ^2)/( A_S^{KK} ^2 +  \bar{A}_S^{KK} ^2)$	$+0.002 \pm 0.072 \pm 0.047$
$\delta_S(K\pi)^{CP}$	$0.5(\arg A_S^{K\pi} - \arg \bar{A}_S^{K\pi})$	$+0.027 \pm 0.033 \pm 0.027$
$\delta_S(KK)^{CP}$	$0.5(\arg A_S^{KK} - \arg \bar{A}_S^{KK})$	$+0.085 \pm 0.045 \pm 0.014$

- The  $CP$  asymmetries in both amplitudes and phases are consistent with zero

# Angular analysis results

- Comparison with previous LHCb result using 2011 data (JHEP 1405 (2014) 069)

Parameter	2011 data	2012 data (not yet approved)
	$1.0 \text{ fb}^{-1} \text{ at } \sqrt{s} = 7 \text{ TeV}$	$2.0 \text{ fb}^{-1} \text{ at } \sqrt{s} = 8 \text{ TeV}$
$f_L$	$0.497 \pm 0.019 \pm 0.015$	$0.503 \pm 0.011 \pm 0.022$
$f_\perp$	$0.221 \pm 0.016 \pm 0.013$	$0.221 \pm 0.009 \pm 0.010$
$f_S(K\pi)$	$0.143 \pm 0.013 \pm 0.012$	$0.152 \pm 0.007 \pm 0.009$
$f_S(KK)$	$0.122 \pm 0.013 \pm 0.008$	$0.097 \pm 0.007 \pm 0.007$
$\delta_\perp$	$2.633 \pm 0.062 \pm 0.037$	$2.610 \pm 0.038 \pm 0.018$
$\delta_\parallel$	$2.562 \pm 0.069 \pm 0.040$	$2.524 \pm 0.038 \pm 0.017$
$\delta_S(K\pi)$	$2.222 \pm 0.063 \pm 0.081$	$2.200 \pm 0.033 \pm 0.060$
$\delta_S(KK)$	$2.481 \pm 0.072 \pm 0.048$	$2.536 \pm 0.045 \pm 0.023$
$A_0^{CP}$	$-0.003 \pm 0.038 \pm 0.005$	$-0.020 \pm 0.022 \pm 0.006$
$A_\perp^{CP}$	$+0.047 \pm 0.074 \pm 0.009$	$-0.035 \pm 0.042 \pm 0.009$
$A_S(K\pi)^{CP}$	$+0.073 \pm 0.091 \pm 0.035$	$+0.119 \pm 0.049 \pm 0.019$
$A_S(KK)^{CP}$	$-0.209 \pm 0.105 \pm 0.012$	$+0.002 \pm 0.072 \pm 0.047$
$\delta_\perp^{CP}$	$+0.062 \pm 0.062 \pm 0.005$	$+0.031 \pm 0.038 \pm 0.005$
$\delta_\parallel^{CP}$	$+0.045 \pm 0.069 \pm 0.015$	$+0.020 \pm 0.038 \pm 0.009$
$\delta_S(K\pi)^{CP}$	$+0.062 \pm 0.062 \pm 0.022$	$+0.027 \pm 0.033 \pm 0.027$
$\delta_S(KK)^{CP}$	$+0.022 \pm 0.072 \pm 0.004$	$+0.085 \pm 0.045 \pm 0.014$

- The results with 2012 data are consistent with and more precise than the results with 2011 data.

# Conclusion

- We have studied the decay  $B^0 \rightarrow \phi K^{*0}$  with the S-wave included in the  $K\pi$  and  $KK$  decays.
- We have obtained:
  - The polarization amplitudes and strong phase differences in the decay mode  $B^0 \rightarrow \phi K^{*0}$ .
  - The results are consistent with, but more precise than previous measurements
  - The  $CP$  asymmetries which are consistent with no direct  $CP$  violation.

Thank you for your attention !

# Backup