

# Review of heavy quarkonium production mechanism in $pp$ collisions from low to high $p_t$

Hong-Fei Zhang

Third Military Medical University

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- 2  $J/\psi$  polarization puzzle
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# A good laboratory

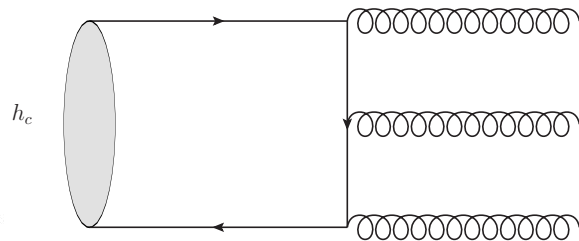
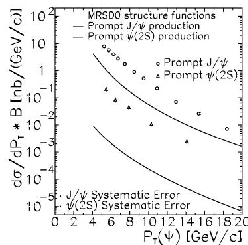
- $J/\psi$  discovery (1974),  $\Upsilon$  discovery (1977).
- good features
  - Heavy enough for perturbative calculations
  - Clear signal
  - Simple structure
- $J/\psi$  suppression as a signature of quark-gluon plasma (QGP)<sup>1</sup>
  - Hot-nuclear-matter (HNM) effects:  $pA$  ( $dA$ ) collisions
  - Cold-nuclear-matter (CNM) effects:  $AA$  collisions

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<sup>1</sup>Matsui, Satz, PLB 178, 416 (1986)

# Colour-singlet Model (CSM)

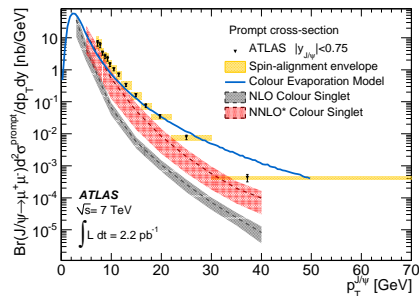
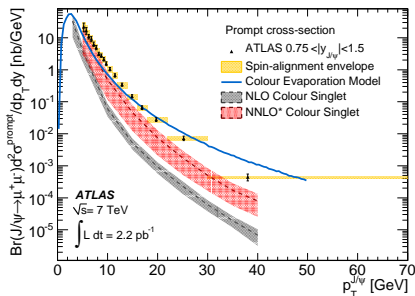
- $\psi'$  ( $J/\psi$ ) surplus<sup>2</sup>
- IR divergence at LO: e.g.  $h_c$  radiative decay



<sup>2</sup>CDF Collaboration, PRL 69, 3704 (1992)

# Colour-evaporation Model (CEM)

- poor agreement with  $p_t$  spectrum of  $\psi$  hadroproduction<sup>3</sup>
- wrong for ratio: e.g.  $\sigma(\chi_{c1}) : \sigma(\chi_{c2}), \sigma(\chi_c) : \sigma(J/\psi)$
- do not apply to polarization



<sup>3</sup>Schuler and Vogt, PLB 387, 181 (1996); ATLAS, NPB 850, 387 (2011)

# Nonrelativistic QCD (NRQCD)<sup>5</sup>

- Separated scales  $m_Q, m_Q v^2$
- $v^2 = 0.3$  for charmonium,  $v^2 = 0.1$  for bottomonium
- Time scales: heavy quark pair fluctuation  $\sim 1/m_Q$ ; hadronization  $\sim 1/(m_Q v^2)$
- NRQCD Factorization (proof up to NNLO<sup>4</sup>)

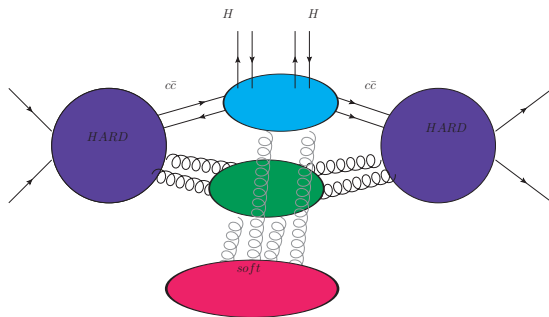
$$d\sigma(H) = \sum_n df_n \langle \mathcal{O}^H(n) \rangle$$

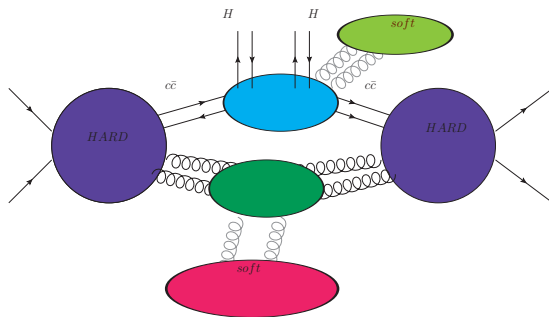
- $f_n$ : Short-distance coefficient (SDC): production of a heavy quark pair, to be calculated perturbatively
- $\langle \mathcal{O}^H(n) \rangle$ : Long-distance matrix element (LDME): hadronization, to be extracted from experiment

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<sup>4</sup>Nayak, Qiu and Sterman, PRD 72, 114012 (2005)

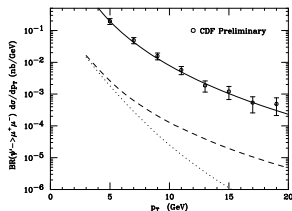
<sup>5</sup>Bodwin, Braaten and Lepage, PRD 51, 1125 (1995)





# NRQCD

- Expansion in  $v$
- $^3S_1^{[1]}$ ,  $^1S_0^{[8]}$ ,  $^3S_1^{[8]}$  and  $^3P_J^{[8]}$  involved in  $\psi$  ( $\Upsilon$ ) production up to  $O(v^4)$
- CSM and CEM are special cases
  - CSM: Colour-octet (CO) channels omitted
  - CEM: higher order in  $v$  involved<sup>6</sup>
- NRQCD tackled the weakness of CSM
  - IR divergences cancelled
  - NRQCD prediction for  $\psi'$  hadroproduction

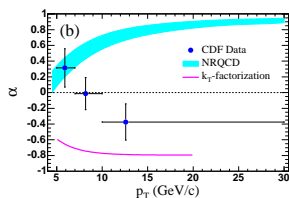
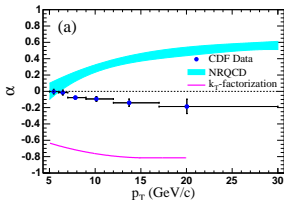


<sup>6</sup>Bodwin, Braaten and Lee, PRD 72, 014004 (2005)

# $J/\psi$ polarization puzzle

- LO NRQCD failed in the description of  $\psi$  polarization<sup>7</sup>

- $\alpha = \frac{\sigma_T - \sigma_L}{\sigma_T + \sigma_L}$



- high  $p_t$  limit

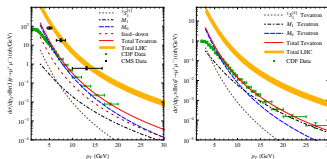
- dominant channel:  $^3S_1^{[8]}$
- dominant mechanism: gluon fragmentation  $\rightarrow$  transversely polarized

<sup>7</sup>Braaten, Kniehl and Lee, PRD 62, 094005 (2000); CDF Collaboration, PRL 99, 132001 (2007)

# NLO era

## NLO for $CS^8$ and $CO^9$

- CS: enhanced by one order, still far below the data
- $^1S_0^{[8]}$ :  $p_t^{-6} \rightarrow$  another small  $p_t^{-4}$  part introduced
- $^3S_1^{[8]}$ : almost unchanged
- $^3P_J^{[8]}$ : positive  $\rightarrow$  minus,  $p_t^{-6} \rightarrow p_t^{-4}$
- $df(^3P_J^{[8]}) = r_0 df(^1S_0^{[8]}) + r_1 df(^3S_1^{[8]})$  (medium and high  $p_t$ , roughly)

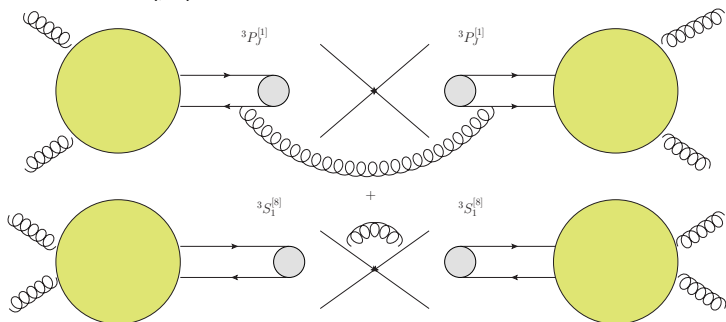


<sup>8</sup>Campbell, Maltoni and Tranmontano, PRL 98, 252002 (2007)

<sup>9</sup>Ma, Wang and Chao, PRL 106, 042002 (2011); Butenschon and Kniehl, PRL 106, 022003 (2011)

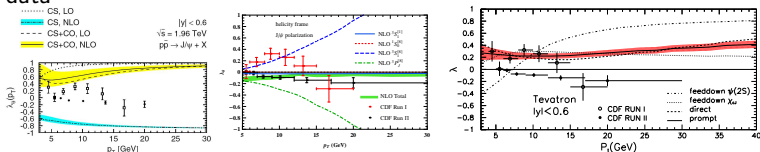
# P-wave states at NLO

- QCD corrections to s-wave LDMEs cancel the singularities in the SDCs
- $\chi_c$  production:  ${}^3P_J^{[1]}$  and  ${}^3S_1^{[8]}$  associated
- $J/\psi$  production:  ${}^3P_J^{[8]}$ ,  ${}^3S_1^{[8]}$  and  ${}^3S_1^{[1]}$  associated
- Only the combination of the associated channels is divergence free and NRQCD scale ( $\mu_\Lambda$ ) independent



# Polarization at NLO

- Left<sup>10</sup>(missing feeddown): Global fit, transversely polarized, bad agreement
- Middle<sup>11</sup>(missing feeddown):  $^1S_0$ <sup>[8]</sup> dominance, agree with CDF Run II data
- Right<sup>12</sup>(complete): agree with CDF Run I data, contradict CDF Run II data



- Different fitting strategy  $\rightarrow$  different LDMEs  $\rightarrow$  different phenomenology
- Three LDMEs to be determined, too many!

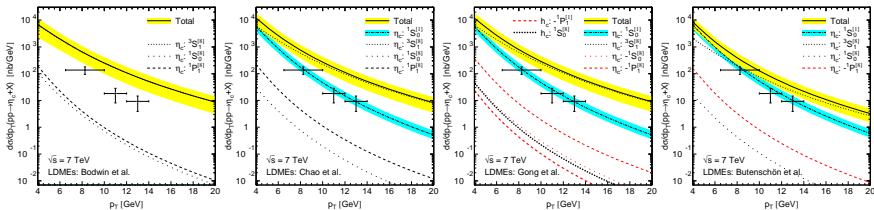
<sup>10</sup>Butenschoen and Kniehl, PRL 108, 172002 (2012)

<sup>11</sup>Chao, Ma, Shao, Wang and Zhang, PRL 108, 242004 (2012)

<sup>12</sup>Gong, Wan, Wang and HFZ, PRL 110, 042002 (2013)

$^1S_0^{[8]}$  dominance picture faces challenge

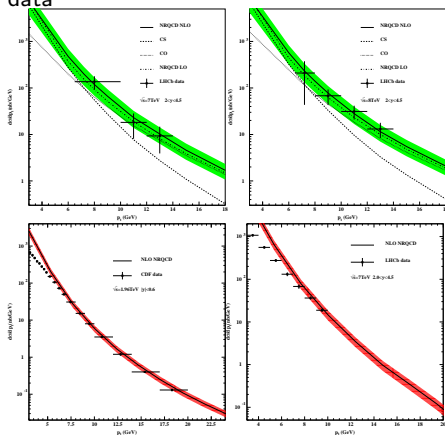
- Why  $^1S_0^{[8]}$  dominance?
  - $p_t$  spectrum: NLO  $^1S_0^{[8]}$  similar to direct  $J/\psi$
  - Polarization:  $^1S_0^{[8]}$  unpolarized
- Challenges
  - Violate velocity scaling rule
  - Violate  $\eta_c$  hadroproduction data<sup>13</sup>



<sup>13</sup>Butenschön, He and Kniehl, PRL 114, 092004 (2015); LHCb, EPJC 75, 311 (2015)

$\eta_c$  and  $J/\psi$  hadroproduction data reconciled

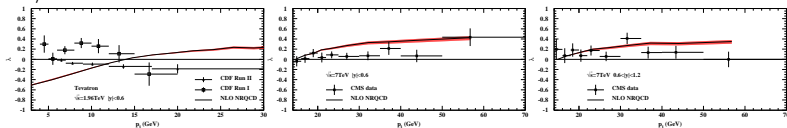
- $\eta_c$  data help to determine LDMEs, consistent with  $J/\psi$  hadroproduction data<sup>14</sup>



<sup>14</sup>Han, Ma, Meng, Shao and Chao, PRL 114, 092005 (2015); HFZ, Sun, Sang and Li, PRL 114, 092006 (2015)

# $J/\psi$ polarization puzzle remains

- Bad agreement with  $J/\psi$  polarization in midrapidity region
- $\sigma_T/\sigma_L$ : 2.3 vs. 1.2



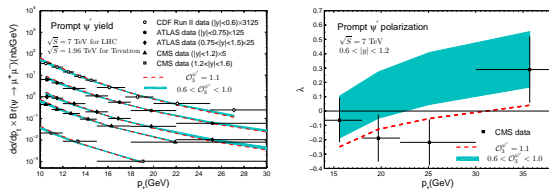
# Charmonia hadroproduction and polarization data reconciled<sup>15</sup>

- New discovery in phenomenology 1)

- The unique key parameter to govern the polarization:

$$R_{J/\psi} \equiv \langle O^{J/\psi}(^3S_1^{[8]}) \rangle / \langle O^{J/\psi}(^3P_0^{[8]}) \rangle$$

- Equation to govern the yield:  $\langle O^{\psi}(^3S_1^{[8]}) \rangle = k_{\psi} \langle O^{\psi}(^3P_0^{[8]}) \rangle + b_{\psi}$
- $k_{J/\psi} = 0.367$ ,  $b_{J/\psi} = 0.00348 \pm 0.00011 \text{ GeV}^3$ ,  $R_{J/\psi} = 0.546 \pm 0.006$
- The polarization is extremely sensitive to  $R_{J/\psi}$
- narrow yield band  $\rightarrow$  huge polarization band



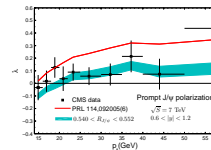
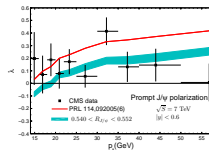
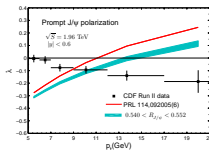
- Conclusion

- Minimizing  $\chi^2$  in the fit to yield data is not reasonable!
- Yield data does not provide information for polarization!

# Charmonia hadroproduction and polarization data reconciled

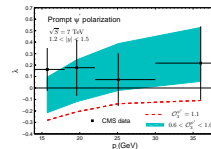
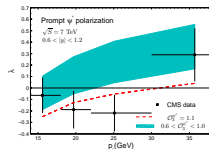
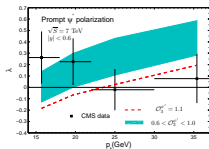
- New discovery in phenomenology 2)

- $J/\psi$  polarization understood



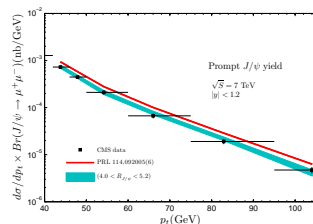
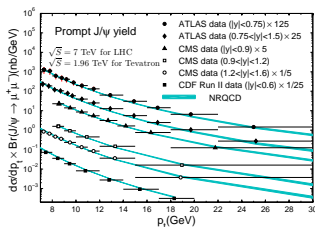
- Relativistic corrections will improve CDF predictions

- $\psi(2s)$  polarization can also be understood



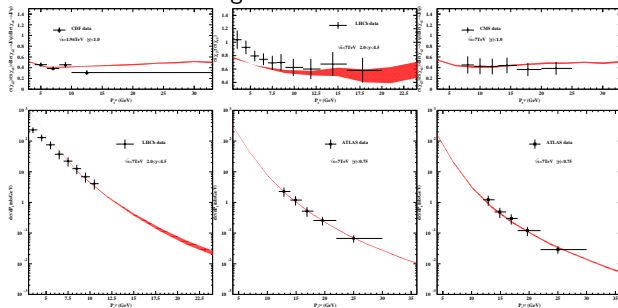
# Charmonia hadroproduction and polarization data reconciled

- $J/\psi$  yield data can also be described



$\chi_C$ , the best laboratory to test NRQCD

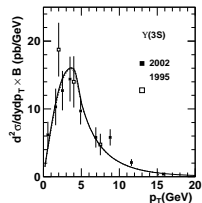
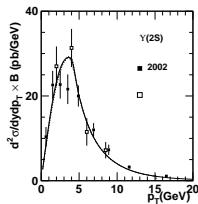
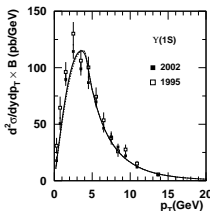
- Only one free parameter
- Good agreement with all the existing data<sup>16</sup>



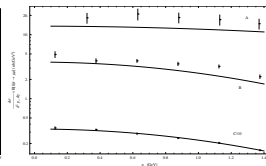
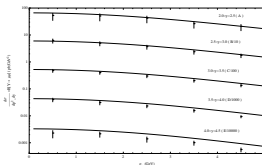
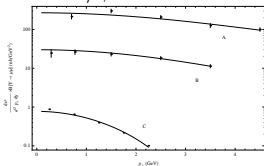
<sup>16</sup>Ma, Wang and Chao, PRD 83, 111503(R) (2011); Shao, Ma, Wang and Chao, PRL 112, 182003 (2014); HFZ, Yu, Zhang and Jia, 1410.4032 (2014)

## Collins-Soper-Sterman (CSS) resummation

- $\Upsilon$ : CSS+CEM<sup>17</sup>



- $\Upsilon$  and  $J/\psi$ : CSS+NRQCD<sup>18</sup>

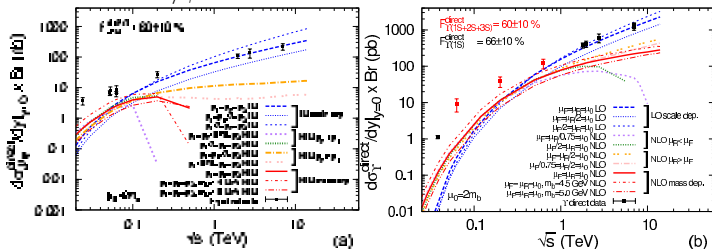


<sup>17</sup>Berger, Qiu and Wang, PRD 71, 034007 (2005)

<sup>18</sup>Sun, Yuan and Yuan, PRD 88, 054008 (2013)

$\log(x)$  resummation is important for  $J/\psi$ 

- Colour-singlet cross sections as a function of c.m. energy<sup>19</sup>
- $d\sigma/dy$  is free of  $\log^2(p_t/m_c)$ , still negative cross sections
- The only large log:  $\log(x)$
- $\Upsilon$  better than  $J/\psi$

<sup>19</sup>Feng, Lansberg and Wang, EPJC 75, 313 (2015)

## Colour Glass Condensate (CGC)<sup>20</sup>

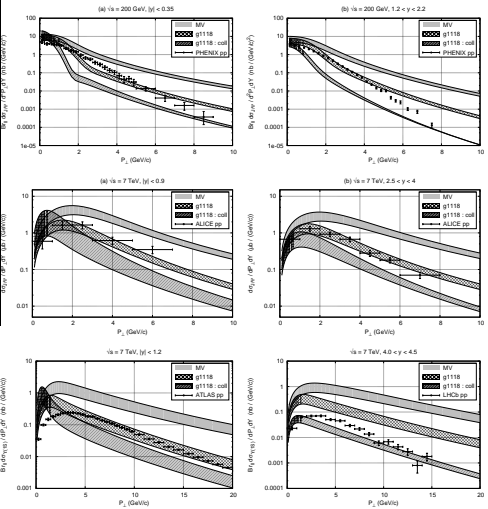
- Dilute-dense approximation
- $x > x_0$ : dilute;  $x < x_0$ : dense
- Resum  $\log(x)$
- JIMWLK evolution

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<sup>20</sup>Mclerran and Venugopalan, PRD 49, 2233; 49, 3352; 50, 2225 (1994)

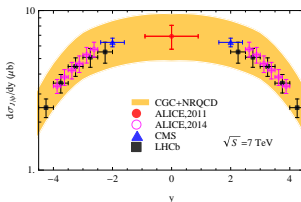
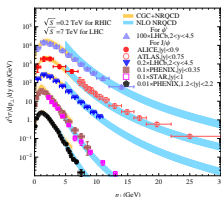
# CGC+CEM<sup>21</sup>

● Bad agreement

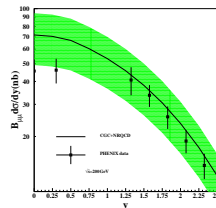
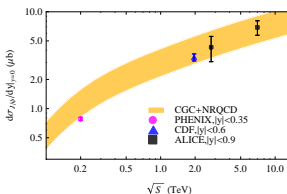


CGC+NRQCD<sup>22</sup>

## ● Good agreement



## ● Not good in midrapidity region at low energy where dilute-dense approximation is ruined (HFZ)

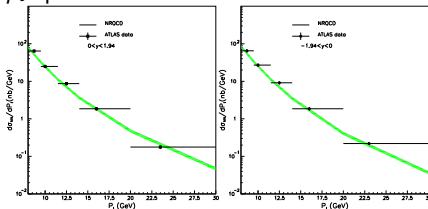


<sup>22</sup>Kang, Ma and Venugopalan, JHEP 1401, 056 (2013); Ma and Venugopalan, PRL 113, 192301 (2014)

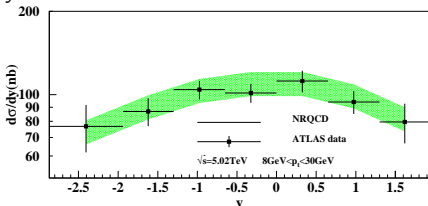
# $J/\psi$ production in $pA$ collisions at high $p_t$ <sup>24</sup>

- EPS09 employed<sup>23</sup>

- $p_t$  spectrum



- $y$  distribution



<sup>23</sup>Eskola, Paukkunen and Salgado, JHEP 0904, 065 (2009)

<sup>24</sup>HFZ and etc., in preparation

# $J/\psi$ production in $pA$ collisions<sup>25</sup>

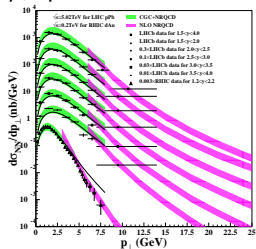
- Two free parameters:  $Q_{s0,A}$  and  $R_A$
- $Q_{s0,A}^2 = N \times Q_{s0,p}^2$ 
  - $N \approx 3$  for  $\gamma = 1.113$ ;  $N \approx 1.5$  for  $\gamma = 1$
  - We set  $\gamma = 1$ ,  $N = 2$  as a tentative choice
- $R_{pA} \equiv \frac{d\sigma_{pA}}{A \times d\sigma_{pp}}$ 
  - $R_{pA} \rightarrow \frac{R_A^2}{AR_p^2} \frac{Q_{s0,A}^2}{Q_{s0,p}^2}$  (high  $p_t$ )
  - $R_{pA} \rightarrow 1$  at high  $p_t$ , a natural assumption to determine  $R_A$

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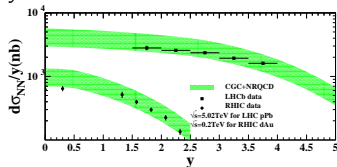
<sup>25</sup>Ma, Venugopalan and HFZ, 1503.07772 (2015)

# $J/\psi$ production in $pA$ collisions

## $p_t$ spectrum

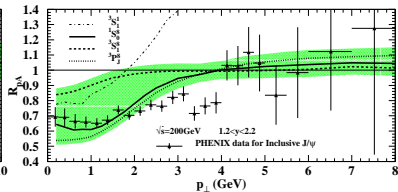
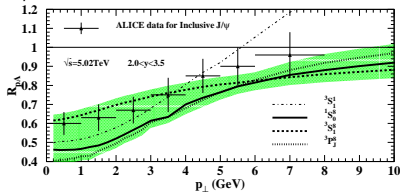


## $y$ distribution

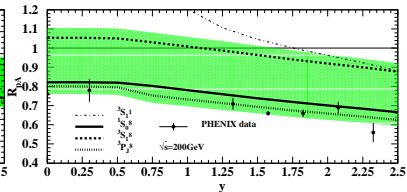
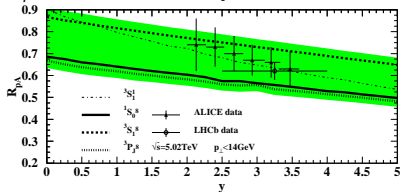


$J/\psi$  suppression

- $R_{pA}$  as a function of  $p_t$



- $R_{pA}$  as a function of  $y$



# Summary

- NRQCD can describe both  $\psi$  production and polarization
- Minimizing  $\chi^2$  is not appropriate in the determination of the LDMEs
- Small- $x$  resummation is required in small  $p_t$  region
- CGC+NRQCD provide good description of both  $pp$  and  $pA$  data
- pQCD+NRQCD can describe the high- $p_t$   $J/\psi$  production data in  $pA$  collision

# Thanks!