



Braking index of Young Neutron Stars

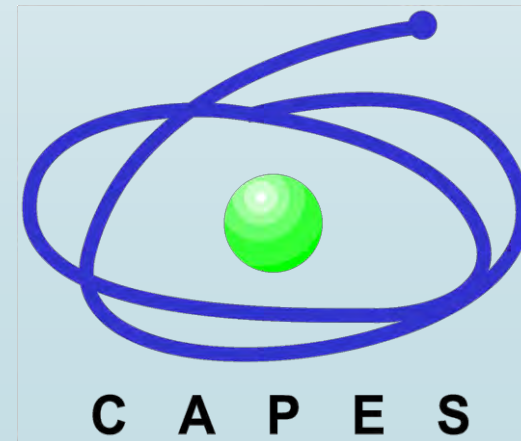
Rodrigo Negreiros – Federal Fluminense University

Cristian Bernal – Federal Fluminense University

Acknowledgements



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C A P E S

Some advertising....



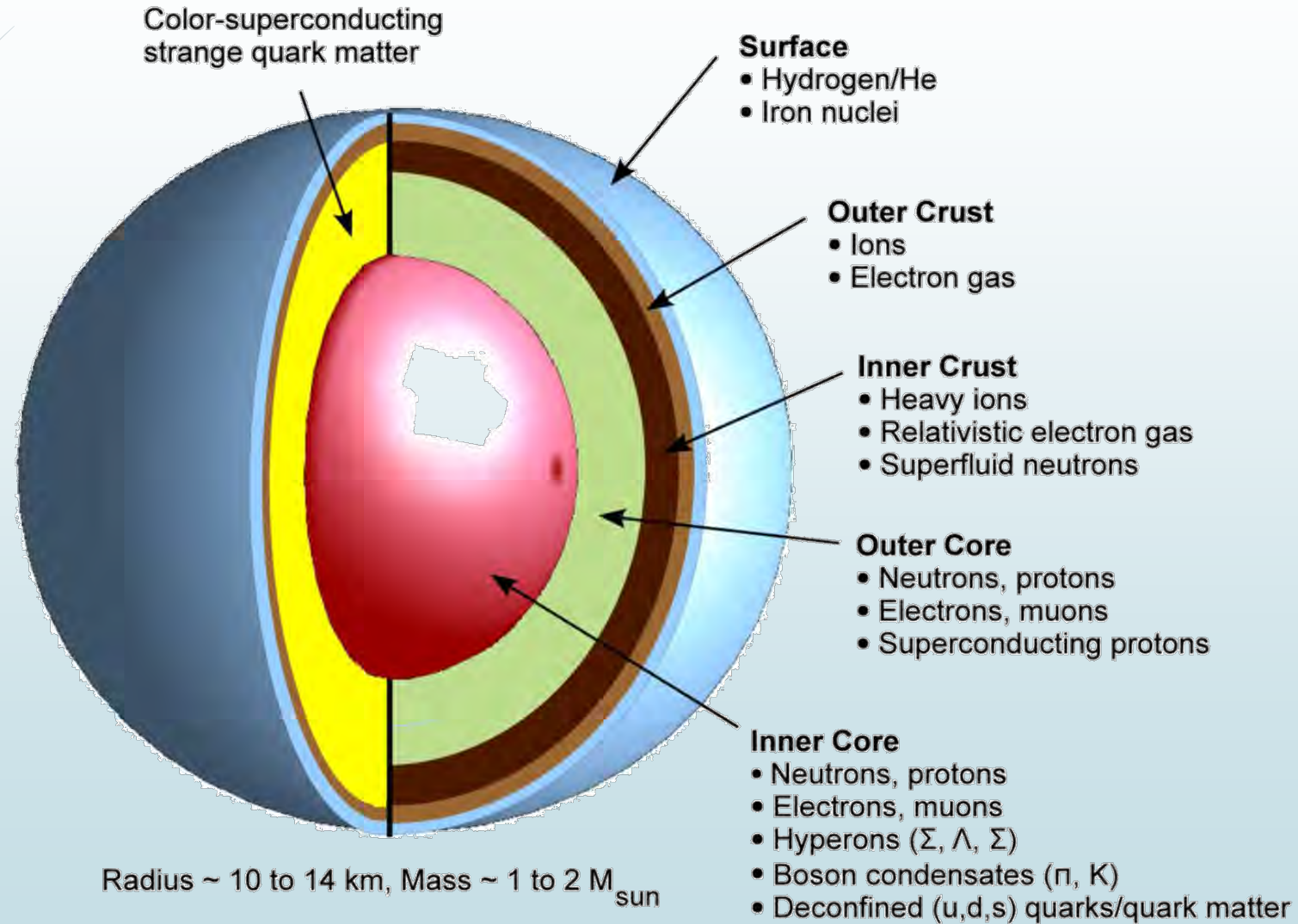
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The microscopic "Zoo"

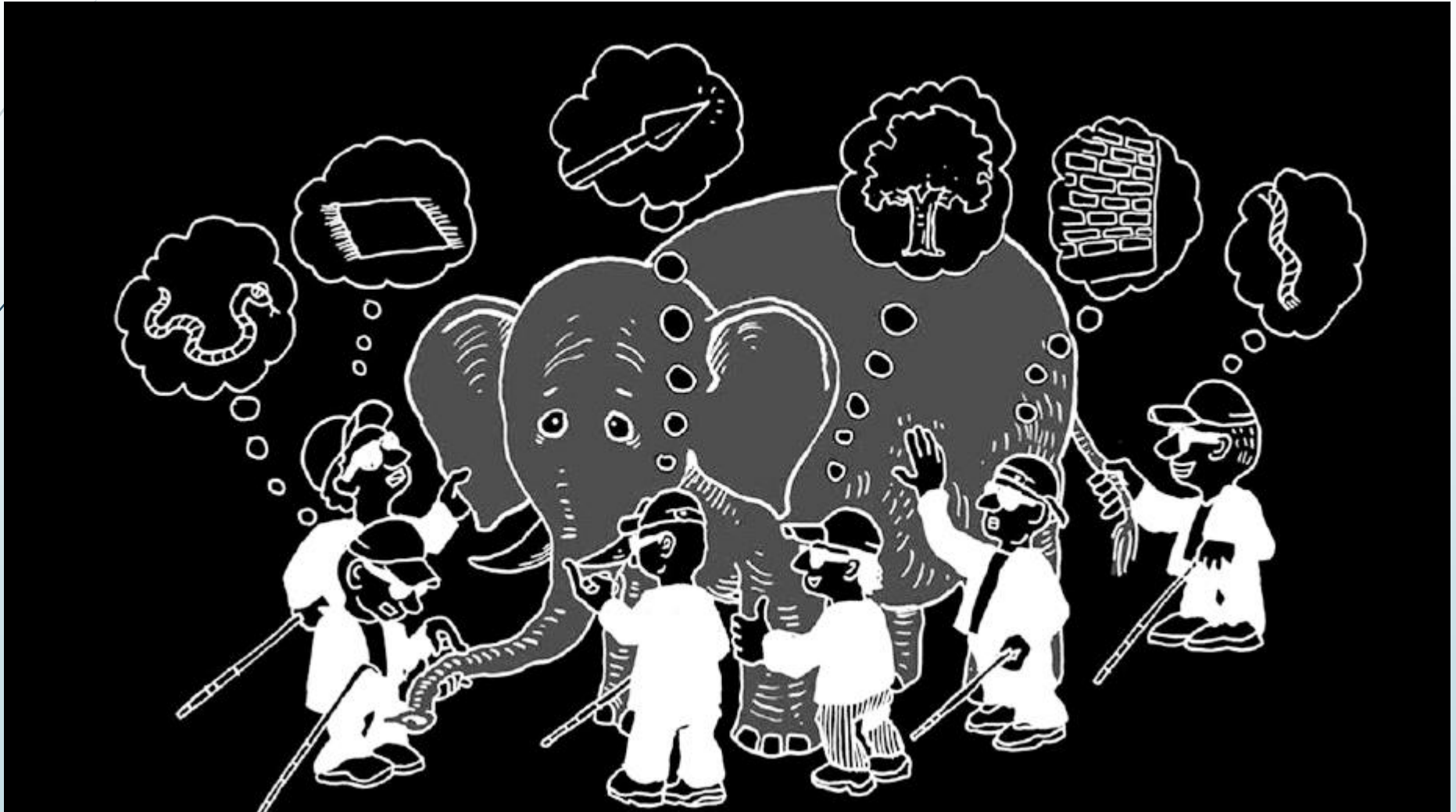


Weber, Hamil, Mimura and Negreiros (2011)

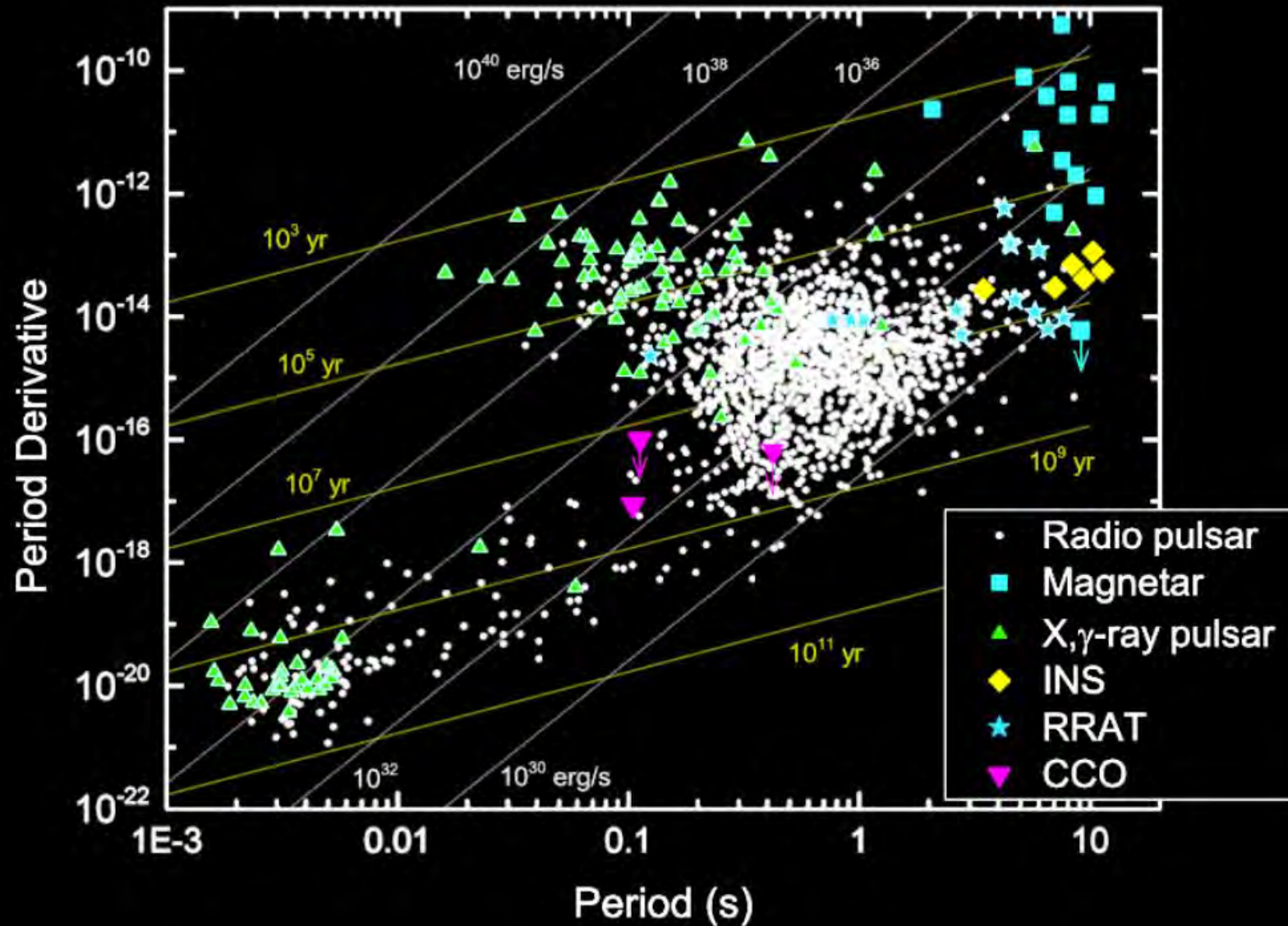
Neutron Stars Zoo



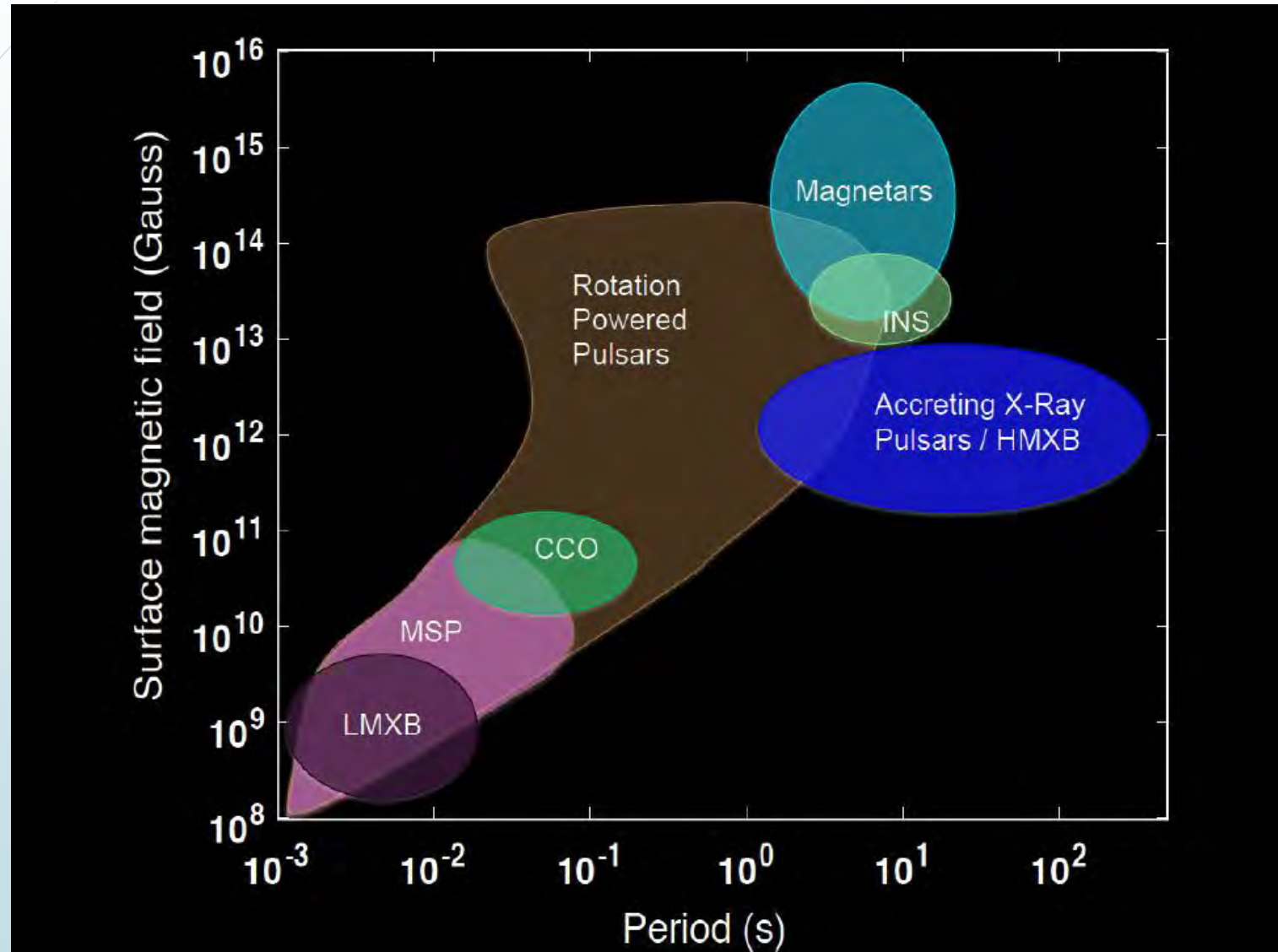
Neutron Star Diversity



Neutron Star Population



Neutron Star Population



Magnetic Braking Model

$$\dot{E} = \frac{d}{dt} \left(\frac{1}{2} I \Omega^2 \right) = -C \Omega^{n+1}$$

- For magnetic dipole radiation ($n=3$)

$$-\frac{dE}{dt} = -\frac{d}{dt} \left(\frac{1}{2} I \Omega^2 \right) = \frac{2}{3} R^6 B^2 \Omega^4 \sin^2 \alpha$$

- Characteristic age

$$\tau = \frac{\Omega}{(n-1)\dot{\Omega}} \left[\left(\frac{\Omega}{\Omega_0} \right)^{n-1} - 1 \right] = \frac{P}{(n-1)\dot{P}} \left[1 - \left(\frac{P_0}{P} \right)^{n-1} \right]$$

Observed Data

Pulsar name	Supernova remnant	Period P (s)	Period derivative \dot{P} (s s ⁻¹)	Characteristic age τ (yr)	Age t (yr)	Braking index n_{obs}	References
B0531+21	Crab	0.0331	4.23×10^{-13}	1240	960	2.51(1)	Lyne et al. 1988
J05376910	N157B	0.0161	5.18×10^{-14}	4930	2000^{+3000}_{-1000}	-1.5(1)	Middleditch et al. 2006
B0540-69	0540-69.3	0.0505	4.79×10^{-13}	1670	1000^{+660}_{-240}	2.140(9)	Nagase et al. 1990
B083345	Vela	0.0893	1.25×10^{-13}	11300	11000^{+5000}_{-5600}	1.4(2)	Lyne et al. 1996
J11196127	G292.2-0.5	0.408	4.02×10^{-12}	1610	7100^{+500}_{-2900}	2.684(2)	Weltevrede et al. 2011
B150958	G320.4-1.2	0.151	1.54×10^{-12}	1550	< 21000	2.839(3)	Kaspi et al. 1994
J18460258	Kesteven 75	0.325	7.08×10^{-12}	729	1000^{+3300}_{-100}	2.65(1)	Livingstone et al. 2007
J17343333	G354.8-0.8	1.17	2.28×10^{-12}	8120	> 1300	0.9(2)	Espinoza et al. 2011



Deviations from the standard oblique rotator model

- ▶ Multipolar electromagnetic radiation ($n \geq 5$)
- ▶ Quadrupolar gravitational radiation ($n = 5$)
- ▶ Decay of the magnetic field, $n > 3$
- ▶ Radial deformation of the magnetic field lines, $1 \leq n \leq 3$,
- ▶ Relativistic winds $n < 3$,
- ▶ Growth of an intense magnetic field submerged on neutron star crust in the hypercritical accretion phase, which re-emerge by ohmic diffusion, $n < 3$ (Muslimov & Page 1996, Bernal et al. 2010, 2013, Pons et al. 2012)
- ▶ Changes in the moment of inertia of the neutron star, $n < 3$ (Glendenning 2003, F. Weber 2010)



Deviations from the standard oblique rotator model

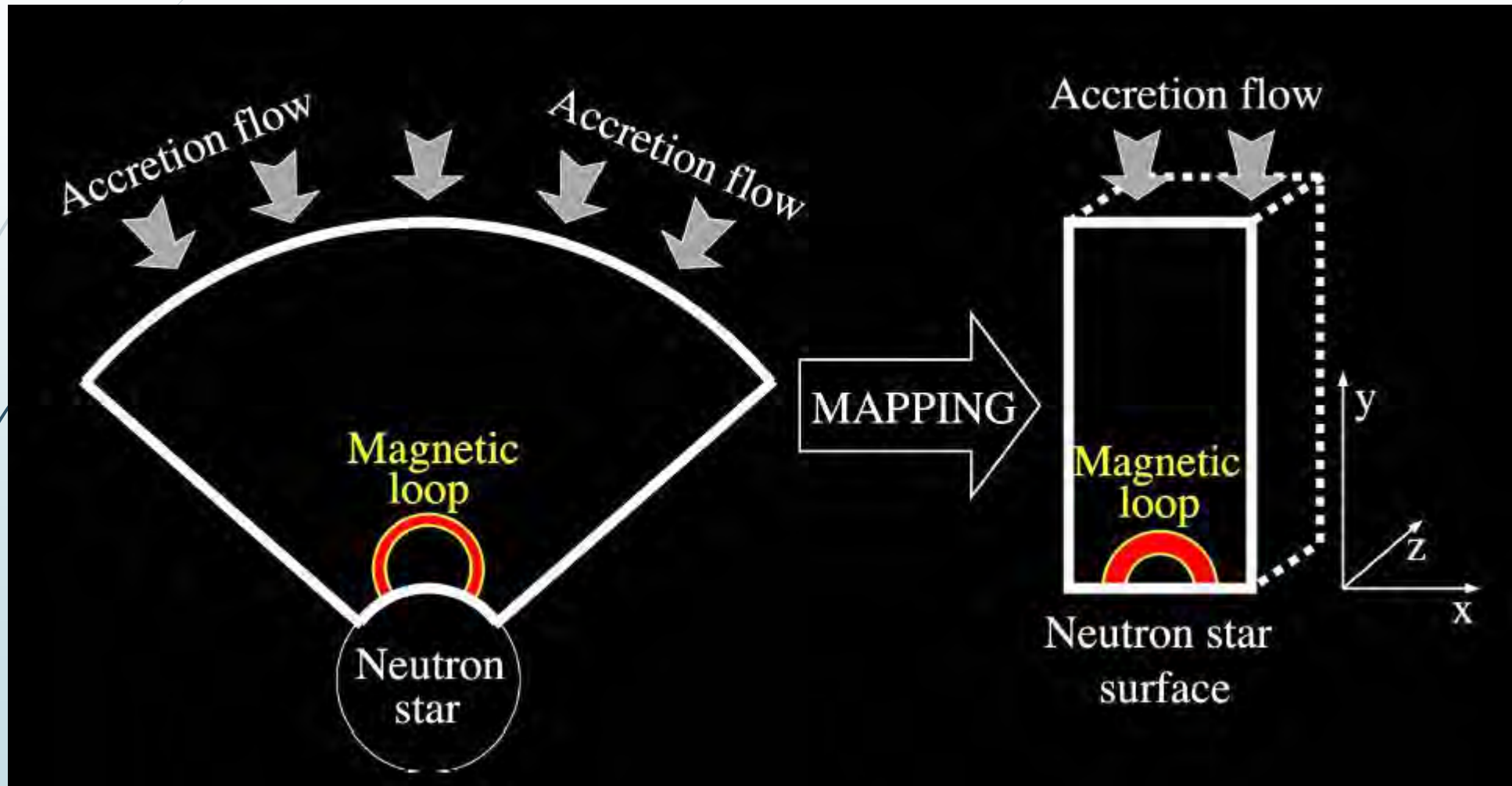
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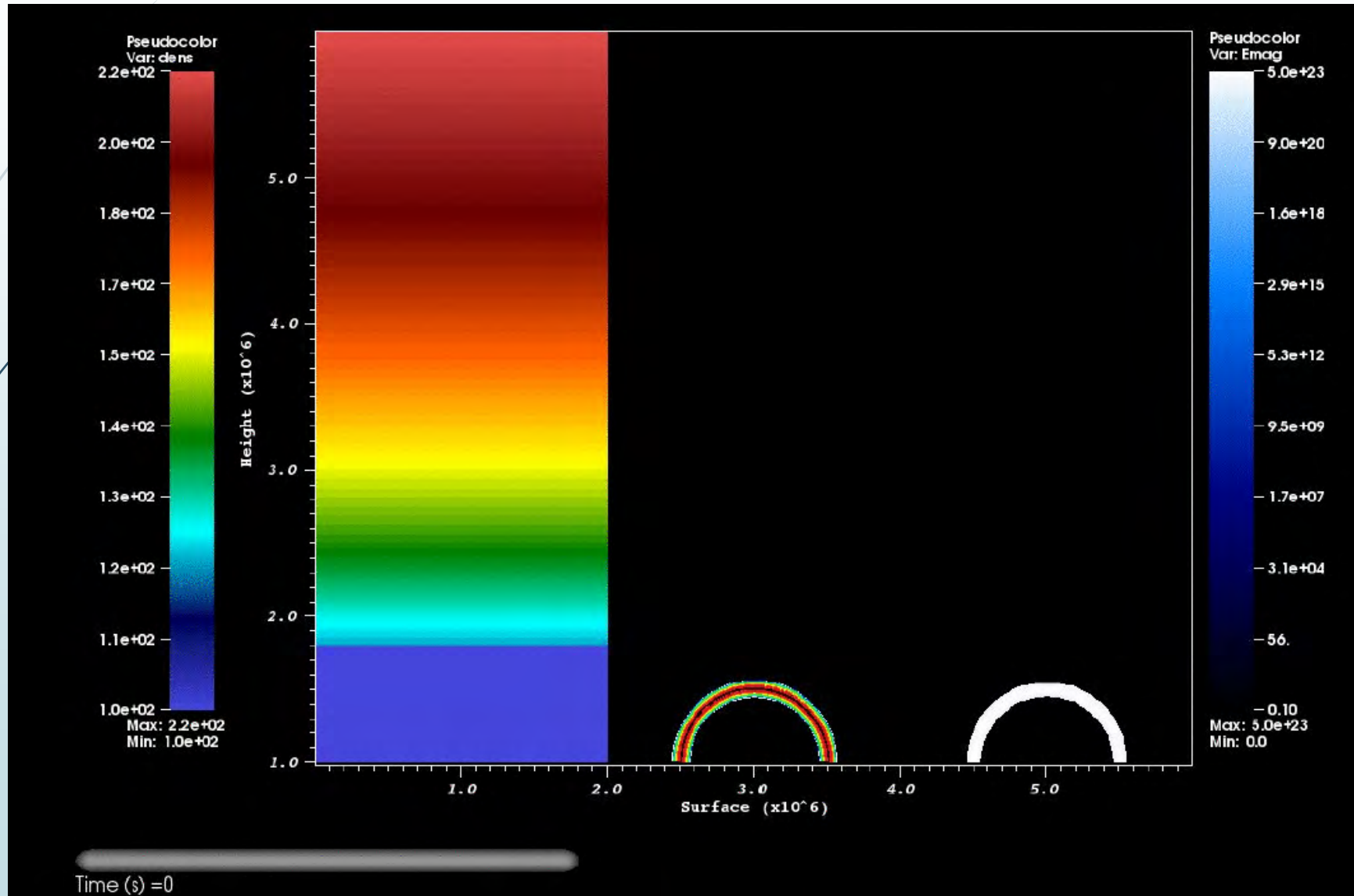
THE GROWTH OF THE MAGNETIC FIELD

- ▶ A newborn neutron star may be exposed to a hyper accretion phase few moments after the supernova explosion that originated it.
- ▶ In the core-collapse scenario, the shock wave sweeps the outer layers of the progenitor until it encounters a discontinuity in density. At this point, a reverse shock is generated leading to a fallback episode which allows to deposit large amounts of material on the stellar surface.
- ▶ The magnetic field can be submerged on the new crust of the neutron star during such phase.
- ▶ Following these ideas it is possible to study the growth of the magnetic field, when it re-emerge from the neutron star crust, and to follow its consequences on the pulsar spindown

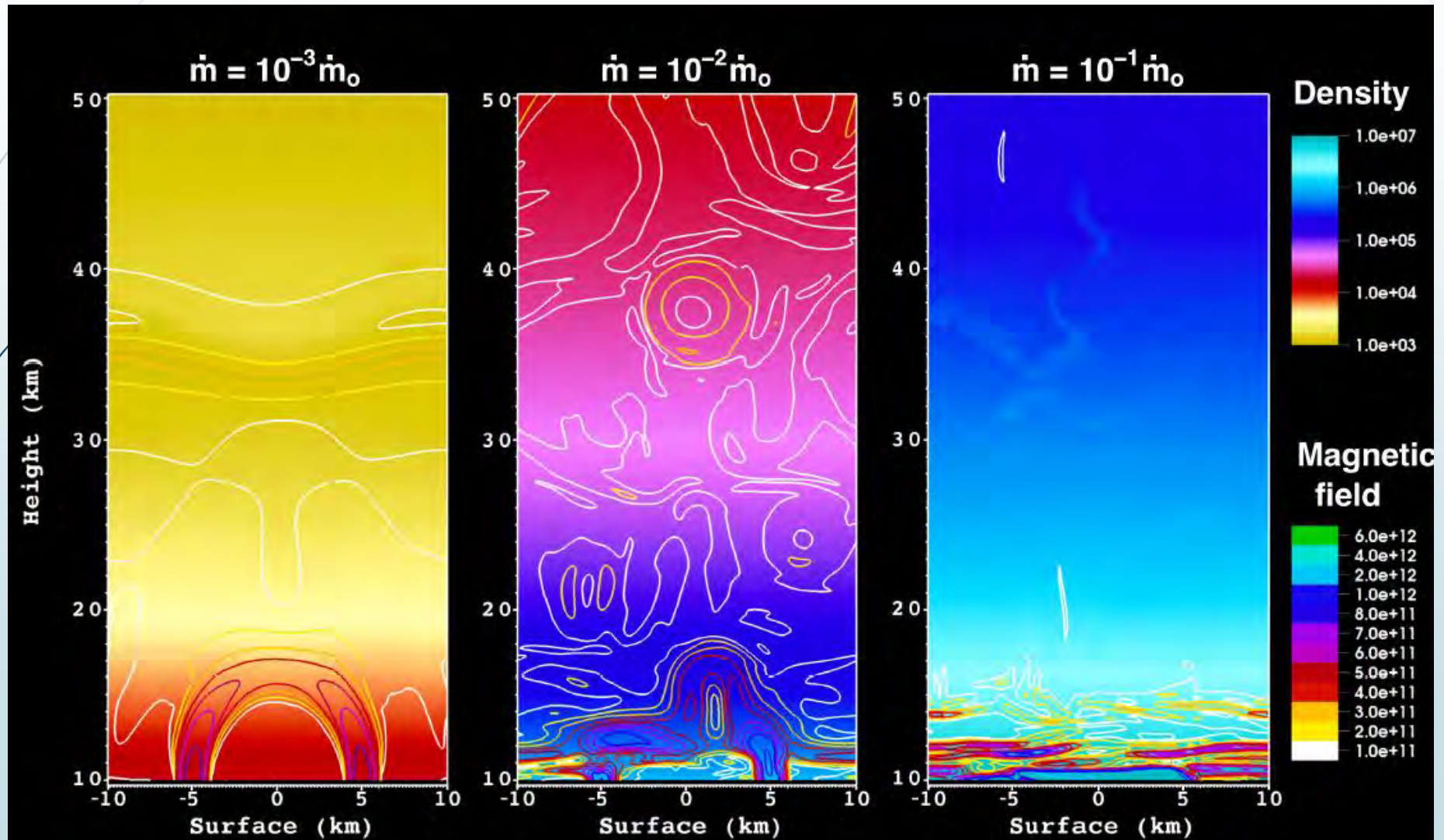
Hyper-Accretion Simulations



Hyper-Accretion Simulations



Hyper-Accretion Simulations



THE GROWTH OF THE MAGNETIC FIELD

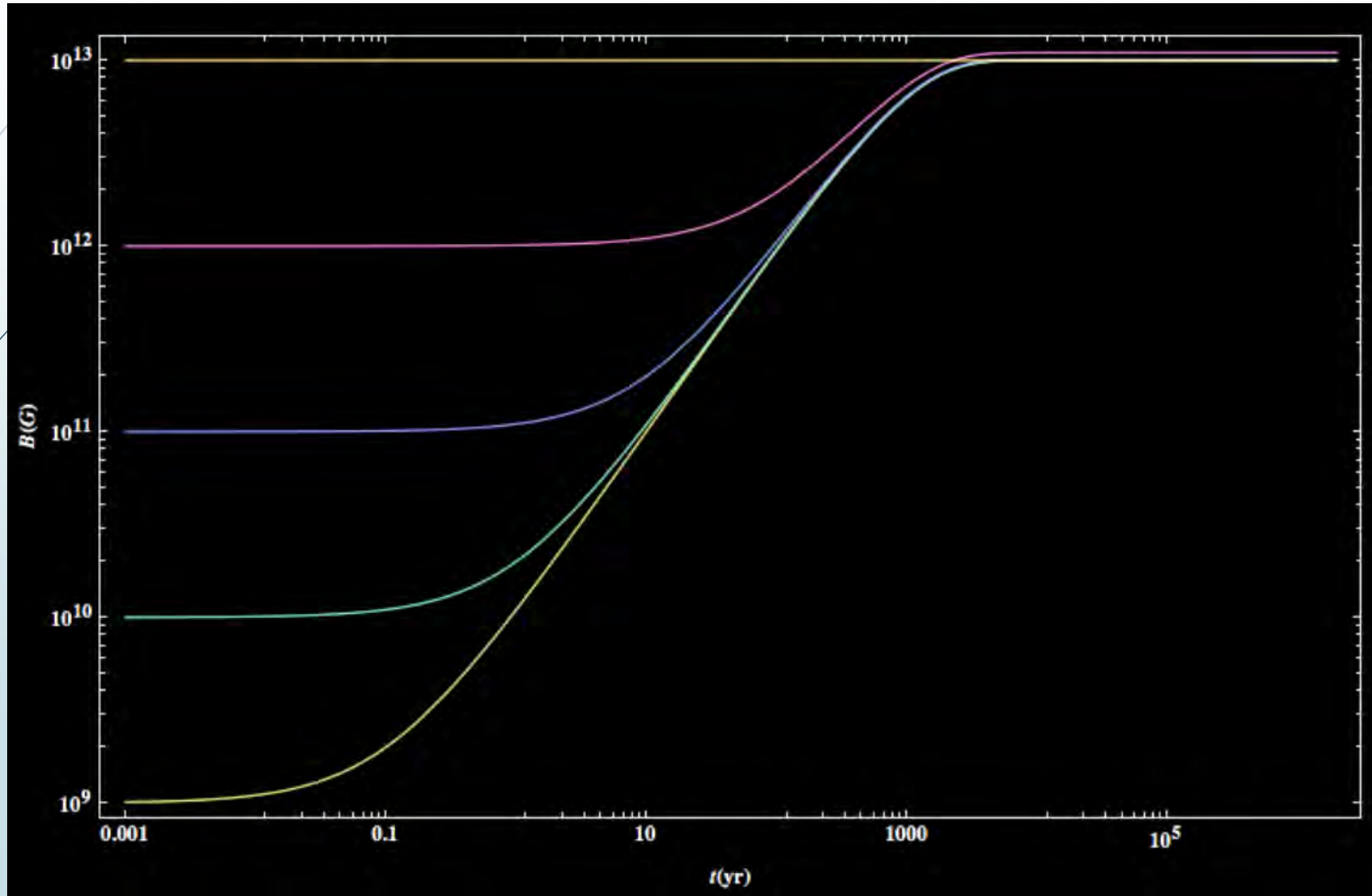
$$\dot{\Omega} = -k(t)\Omega^n, \quad k(t) = kf(t)$$

$$\tau = \frac{1}{f(t)} \left[\tau_0 + \int_0^t f(t) dt \right]$$

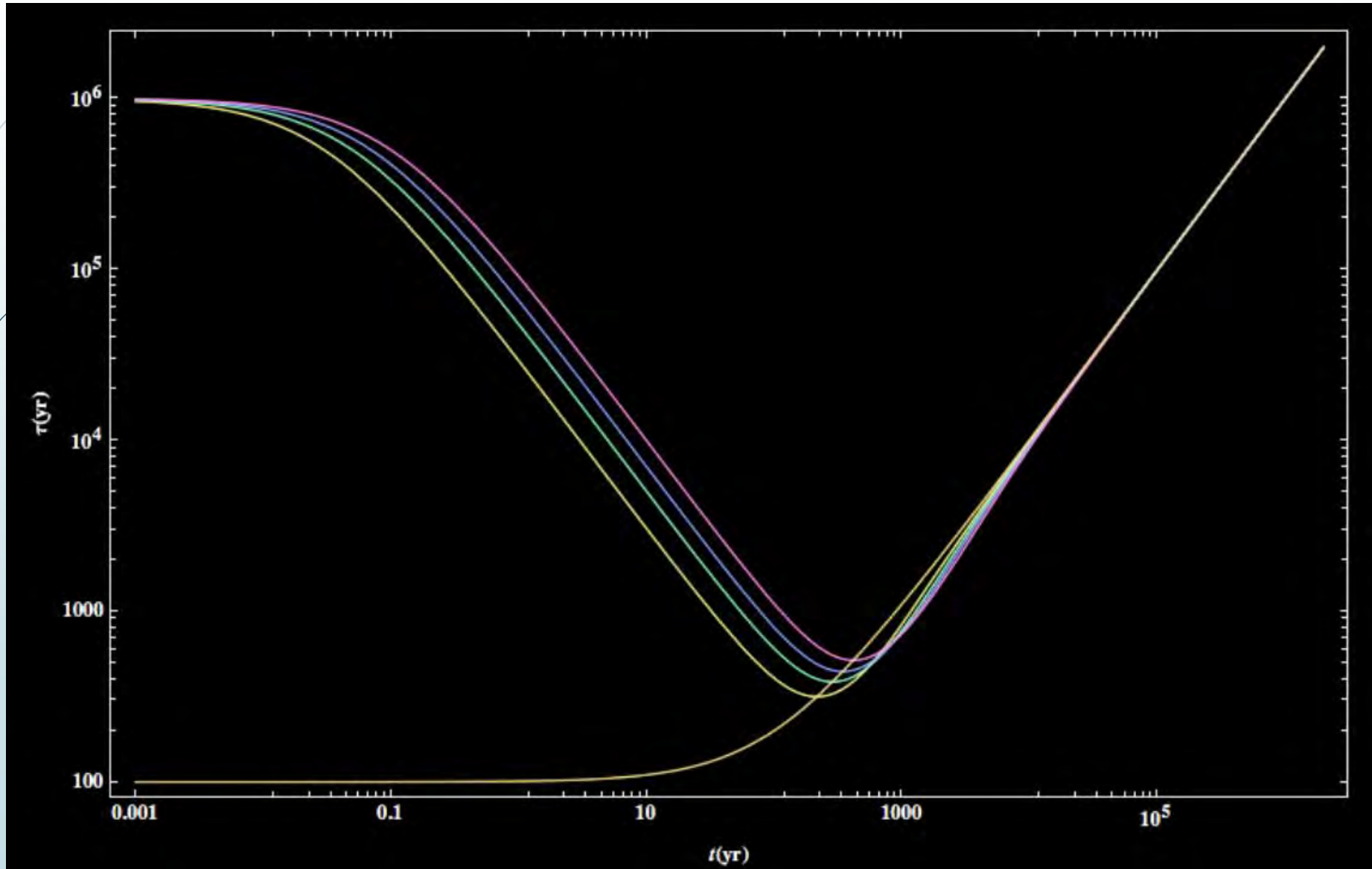
$$n = n_* + \frac{\dot{f}(t) \Omega}{f(t) \dot{\Omega}} = n_* - \frac{\dot{f}(t) P}{f(t) \dot{P}}$$

$$f(t) = \epsilon + \left[1 - \exp \left(-\frac{t}{\tau_B} \right) \right]$$

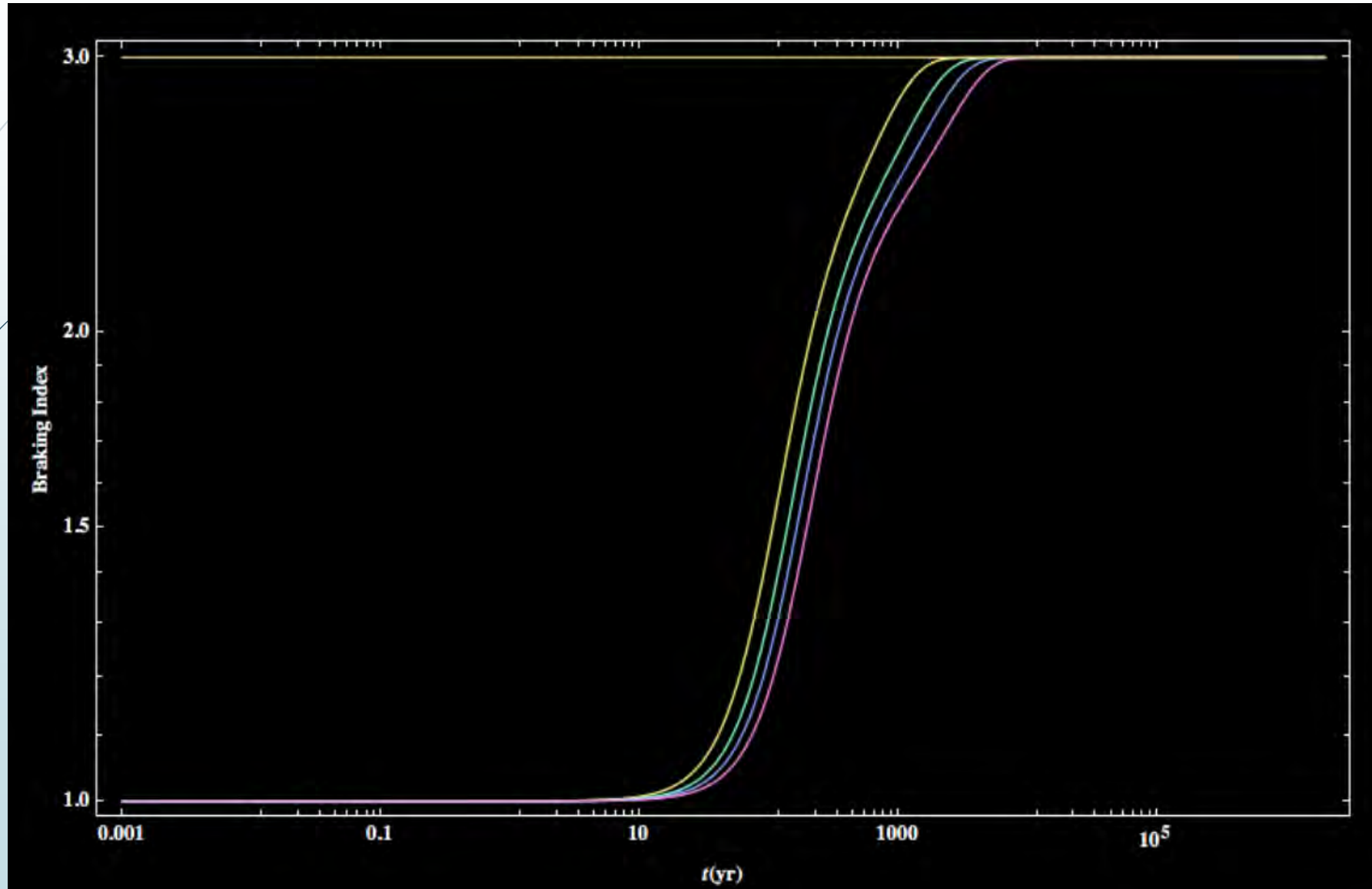
THE GROWTH OF THE MAGNETIC FIELD



THE GROWTH OF THE MAGNETIC FIELD



Braking Index



Changes in the Moment of Inertia

► Superfluid Decoupling*

$$\frac{d}{dt}(I\Omega) = -\beta\Omega^3 - N_{\text{pin}} - N_{\text{mf}}$$
$$\frac{d}{dt}(I_{\text{sf}}\Omega_{\text{sf}}) = N_{\text{pin}} + N_{\text{mf}},$$

* Ho and Anderson, 2012

Changes in the Moment of Inertia

► Superfluid Decoupling*

$$\begin{aligned} \frac{d}{dt}(I\Omega) &= -\beta\Omega^3 - N_{\text{pin}} - N_{\text{mf}} \\ \frac{d}{dt}(I_{\text{sf}}\Omega_{\text{sf}}) &= N_{\text{pin}} + N_{\text{mf}}, \end{aligned}$$

Mutual friction
Vortex Pinning

* Ho and Anderson, 2012

Changes in the Moment of Inertia

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Annotations for the equations above:

- From N_{mf} in the first equation to "Mutual friction" (top right)
- From N_{pin} in the first equation to "Vortex Pinning" (middle right)
- From I in the first equation to "Moment of Inertia of unpaired matter" (middle left)
- From I_{sf} in the second equation to "Moment of Inertia of SF matter" (bottom left)

* Ho and Anderson, 2012

Changes in the Moment of Inertia

- Superfluid Decoupling*

$$\frac{d}{dt}(I\Omega) = -\beta\Omega^3 - N_{\text{pin}} - N_{\text{mf}}$$

Mutual friction
 Vortex Pinning

$$\frac{d}{dt}(I_{\text{sf}}\Omega_{\text{sf}}) = N_{\text{pin}} + N_{\text{mf}}$$

Moment of Inertia of unpaired matter
 Moment of Inertia of SF matter

- Considering the case in which pinning leads to: $\Omega_{\text{sf}} = 0$ *

$$\frac{d\Omega}{dt} = (\Omega_{\text{sf}} - \Omega) \frac{1}{I} \frac{dI}{dt} - \beta \frac{\Omega^3}{I}$$

* Ho and Anderson, 2012

Changes in the Moment of Inertia

- To keep track of the moment of inertia changes, one need to investigate the thermal evolution.

$$\frac{\partial(Le^{2\phi})}{\partial m} = -\frac{1}{\epsilon\sqrt{1-2m/r}} \left(\epsilon_\nu e^{2\phi} + c_\nu \frac{\partial(Te^\phi)}{\partial t} \right)$$
$$\frac{\partial(Te^\phi)}{\partial m} = -\frac{(le^{-\phi})}{16\pi^2 r^4 \kappa \epsilon \sqrt{1-2m/r}},$$

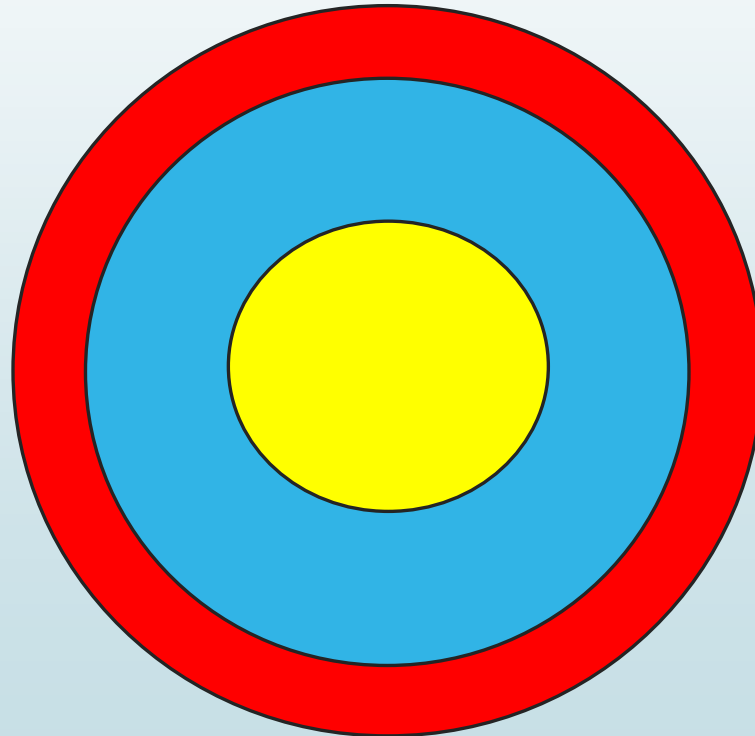


Changes in the Moment of Inertia

- ▶ While in their work, Ho and Anderson only considered neutron ($3P_2$) pairing on a npe neutron star, we consider a more complex scenario.
- 

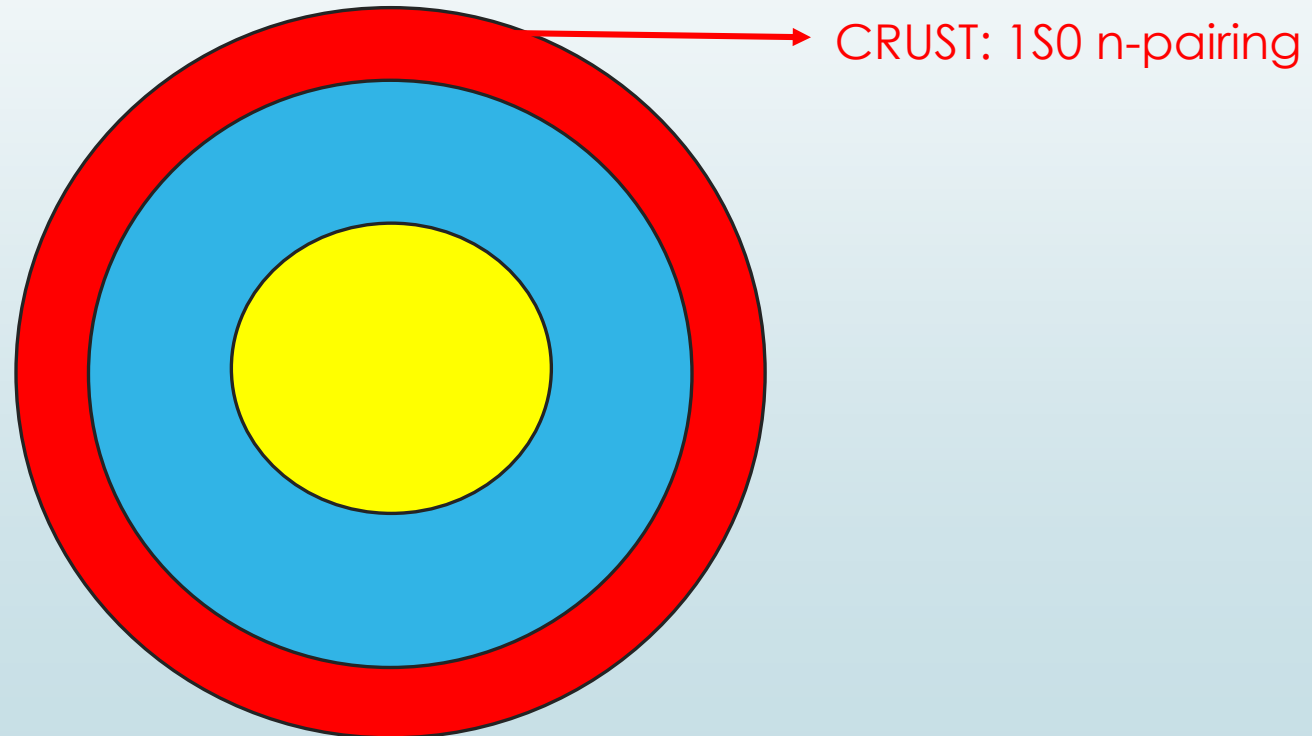
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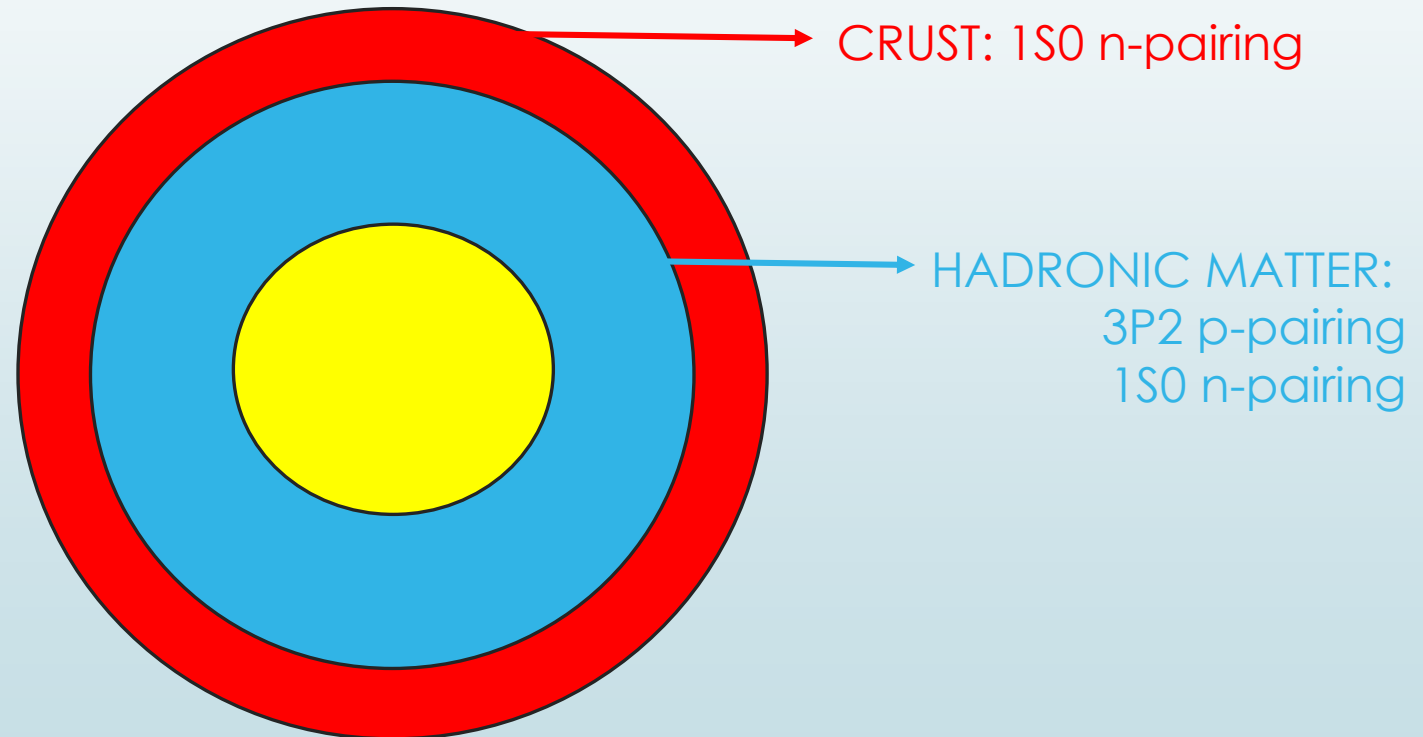
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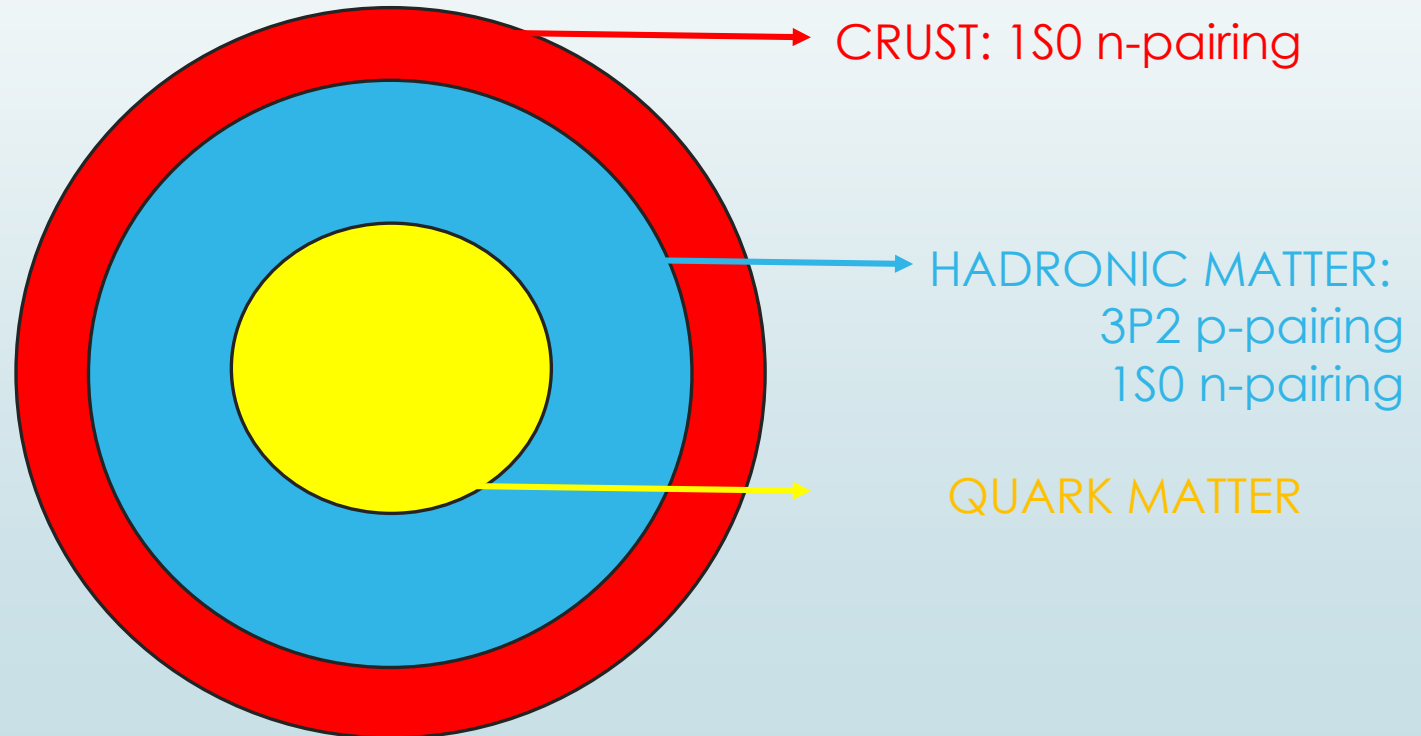
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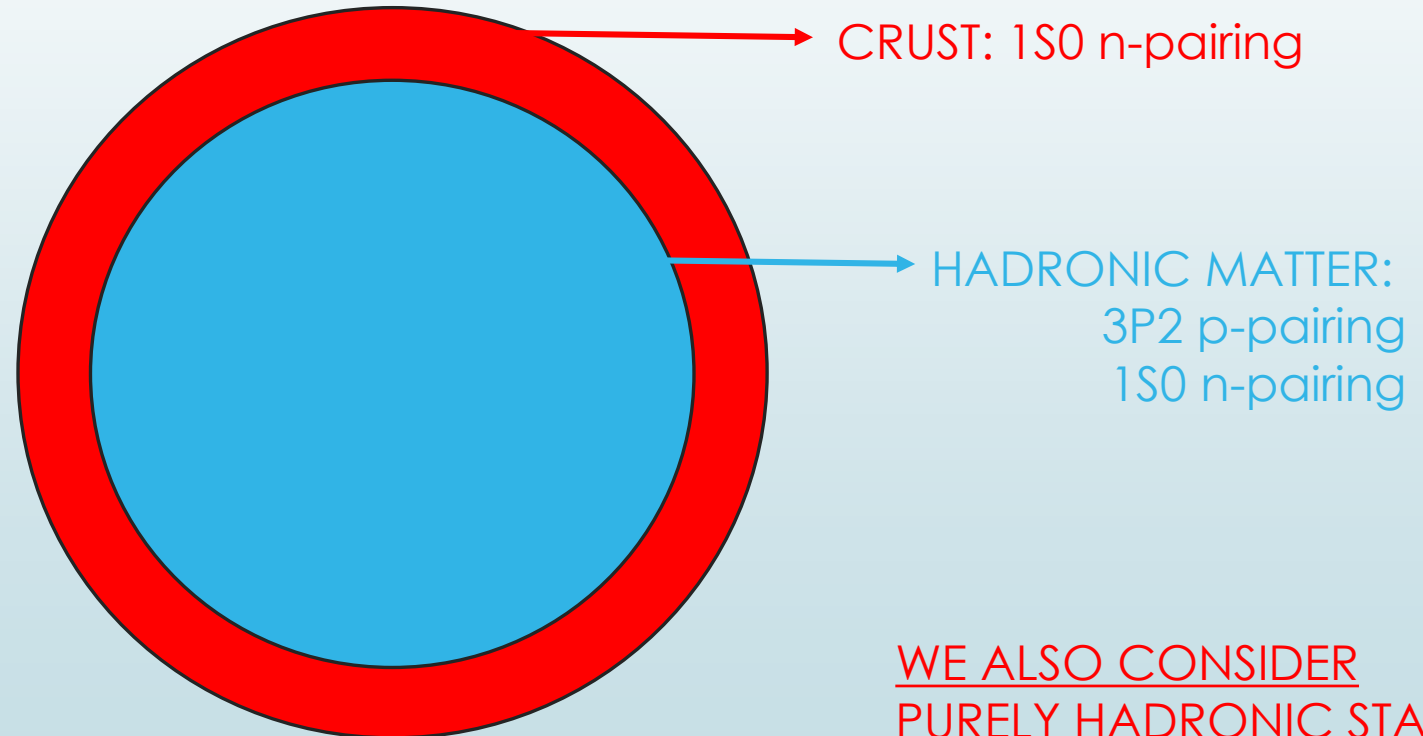
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Changes in the Moment of Inertia

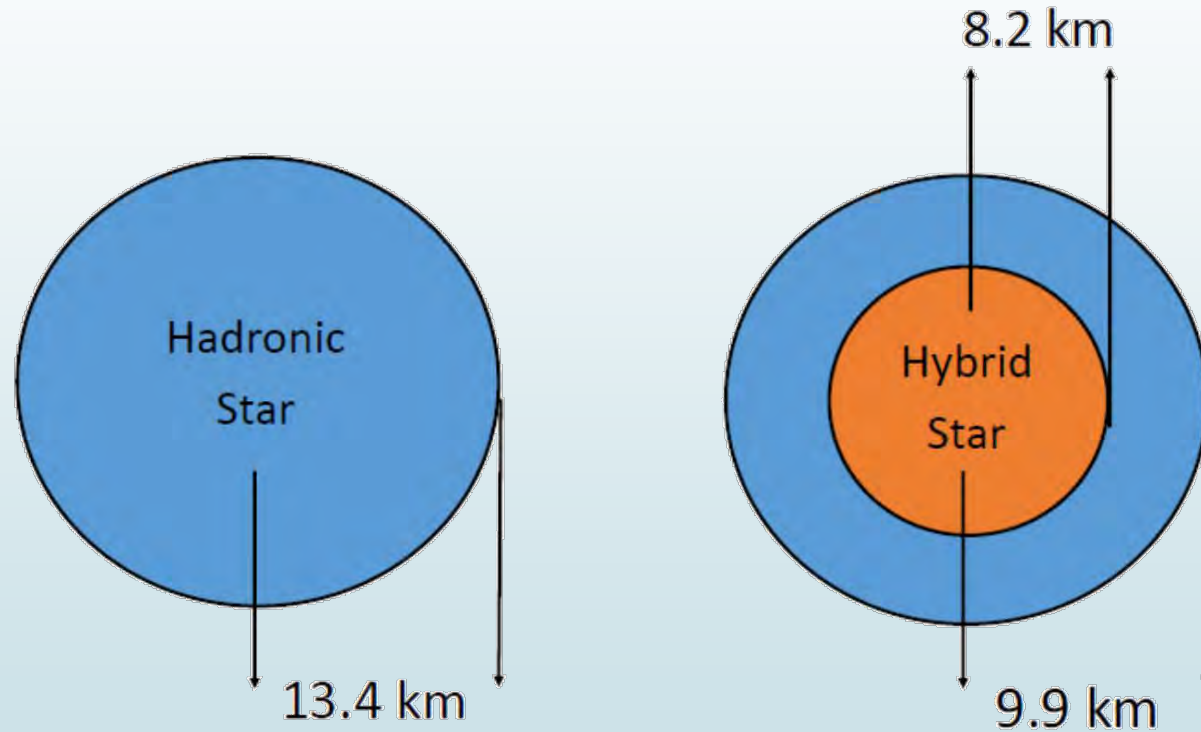
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WE ALSO CONSIDER
PURELY HADRONS STARS !

Changes in the Moment of Inertia

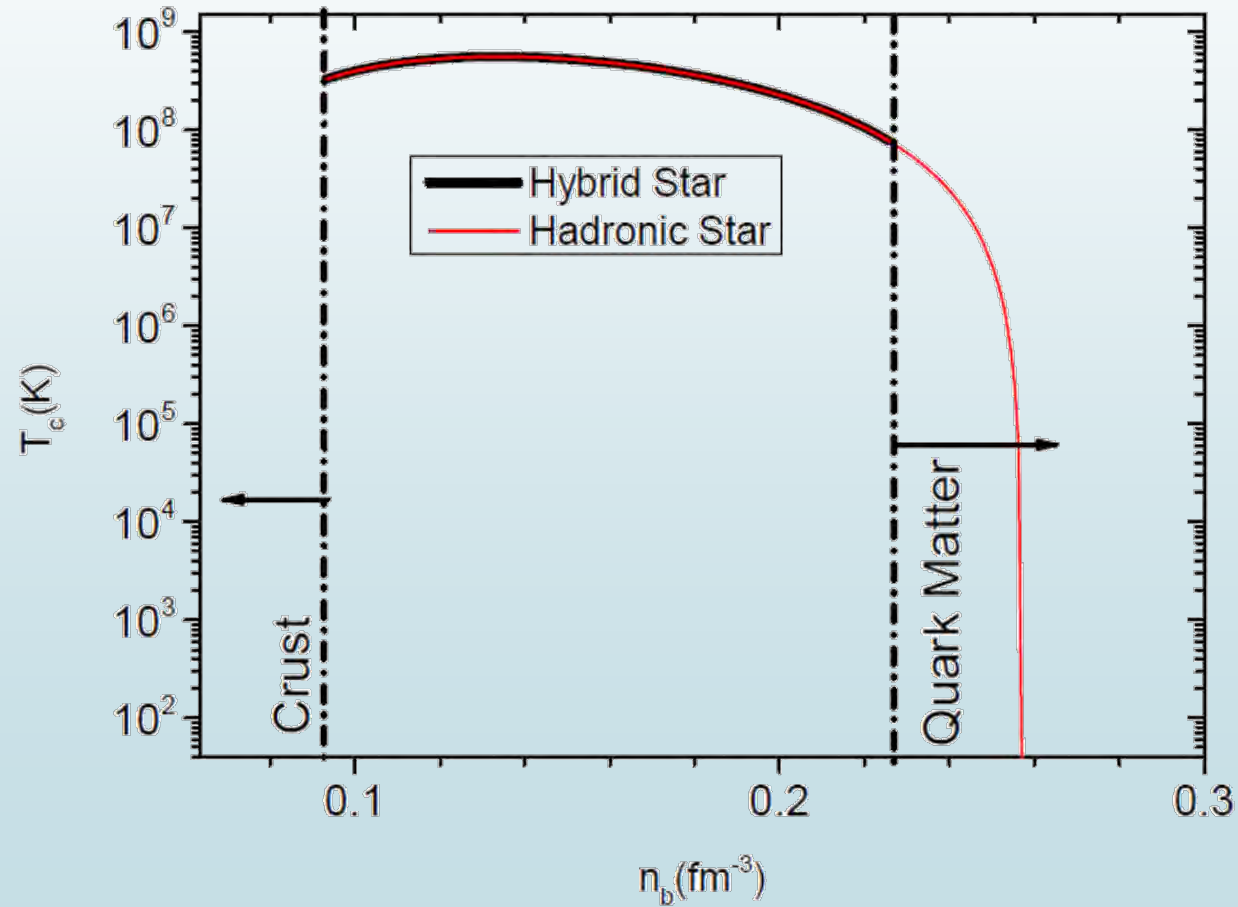
- Two neutron star models studied



Mass = $1.55 M_{\text{sun}}$

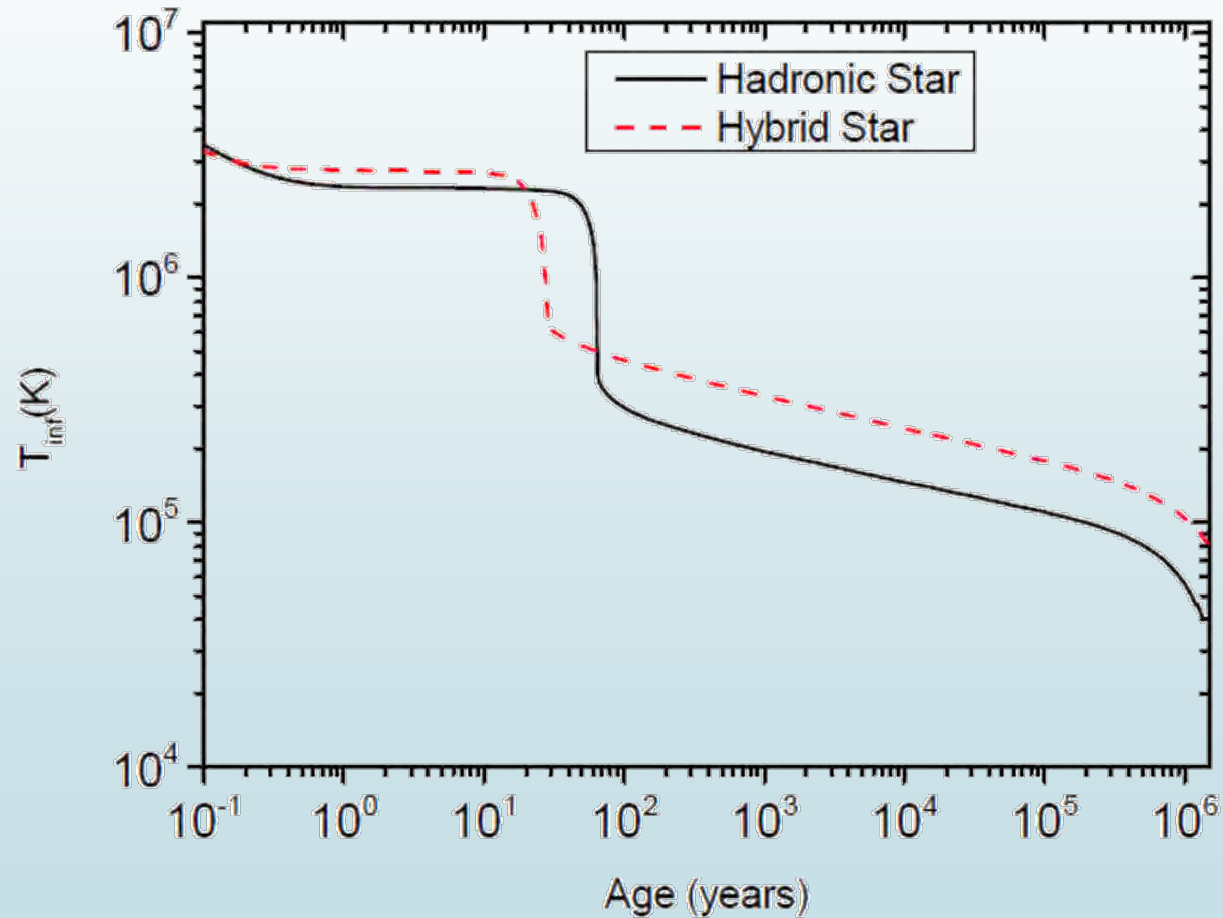
Superfluidity model

- Superfluidity model adopted



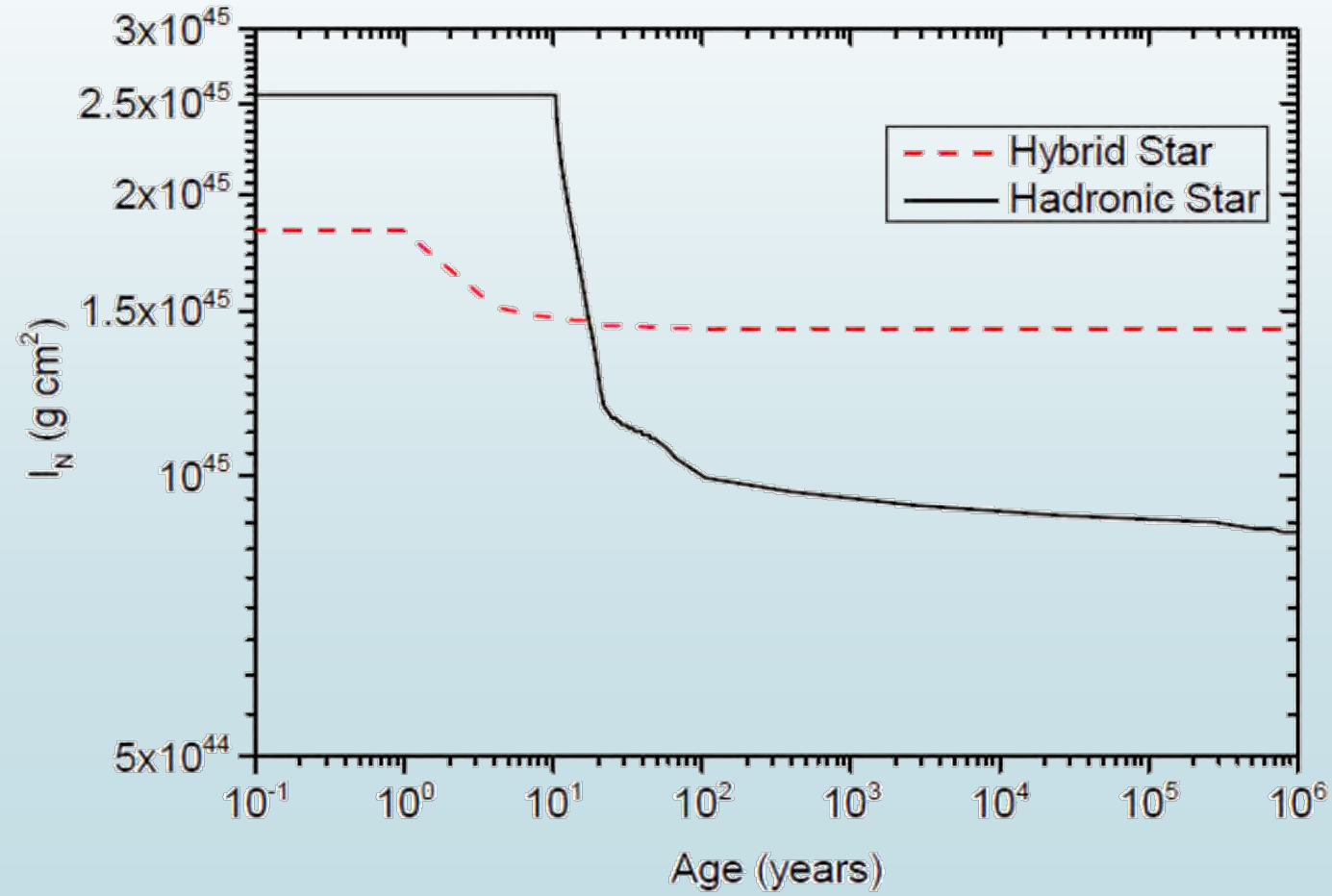
Thermal Evolution

- Collins of the studied stars under current superfluidity model



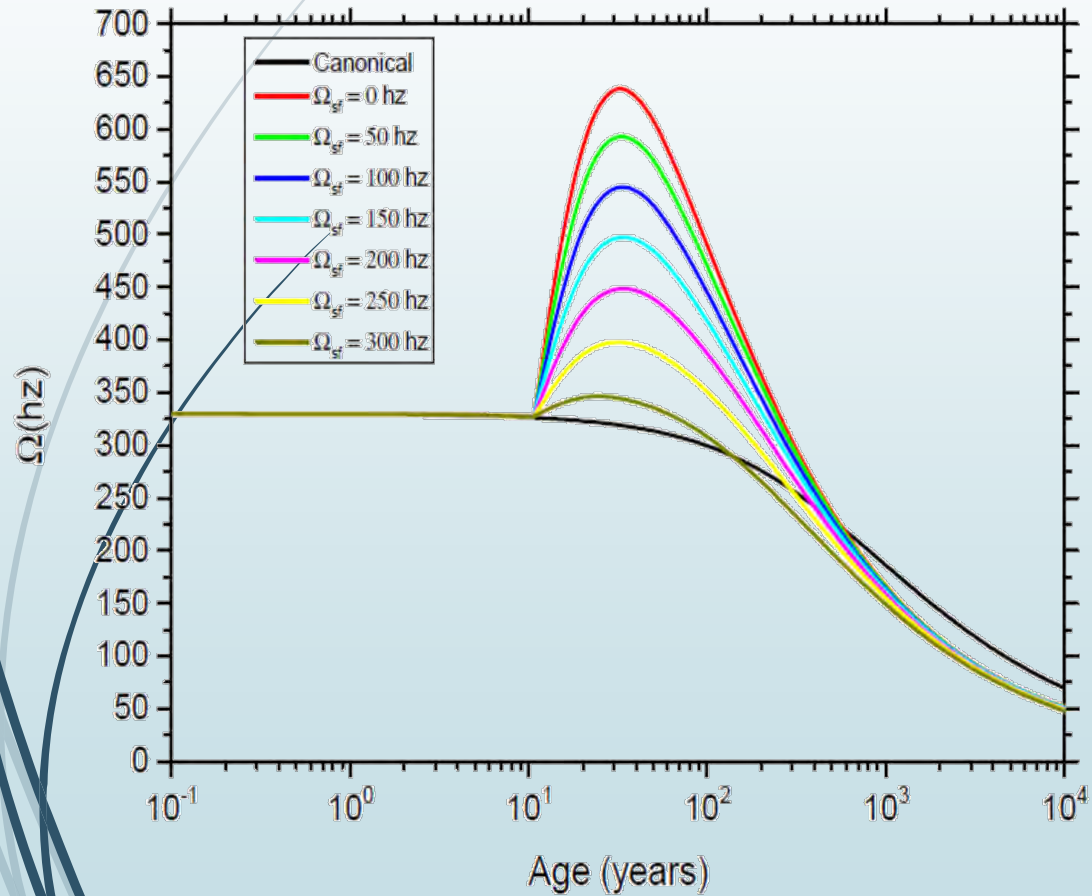
Moment of Inertia Evolution

- Coupled momen inertia evolution

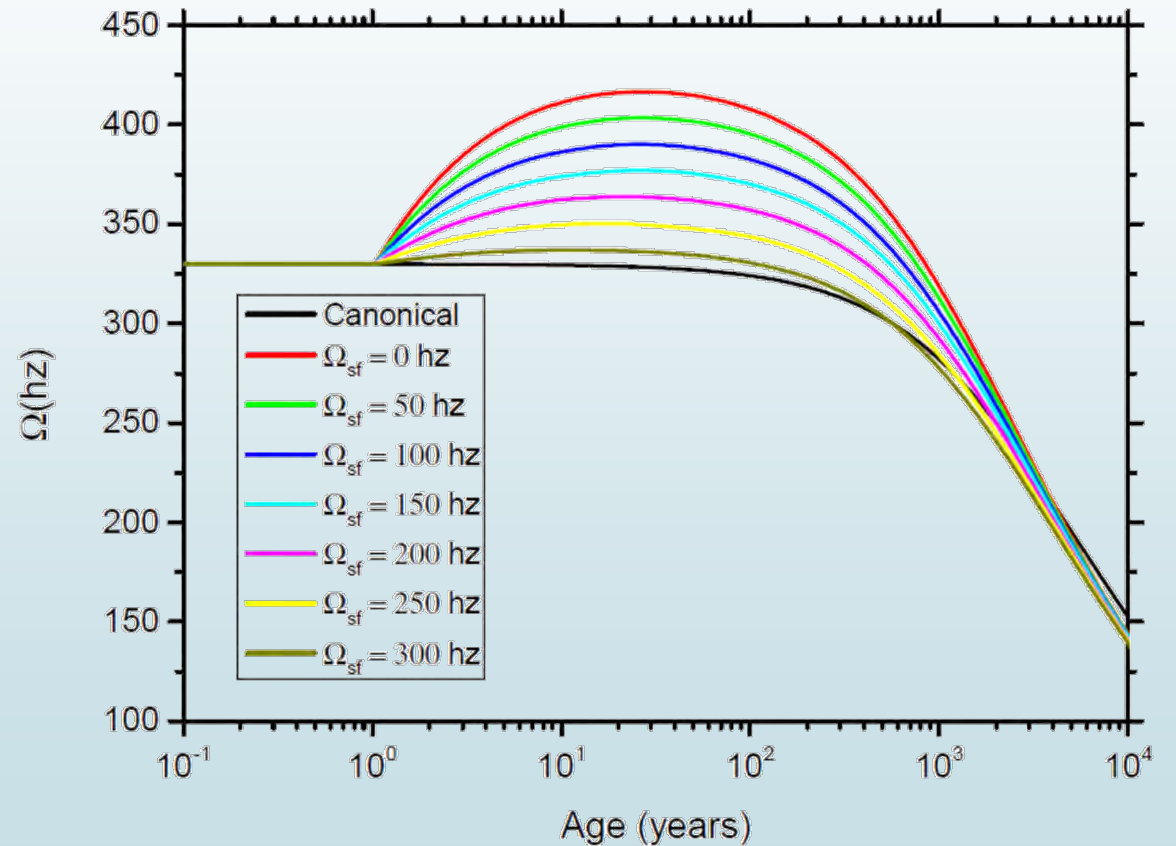


Spin Evolution

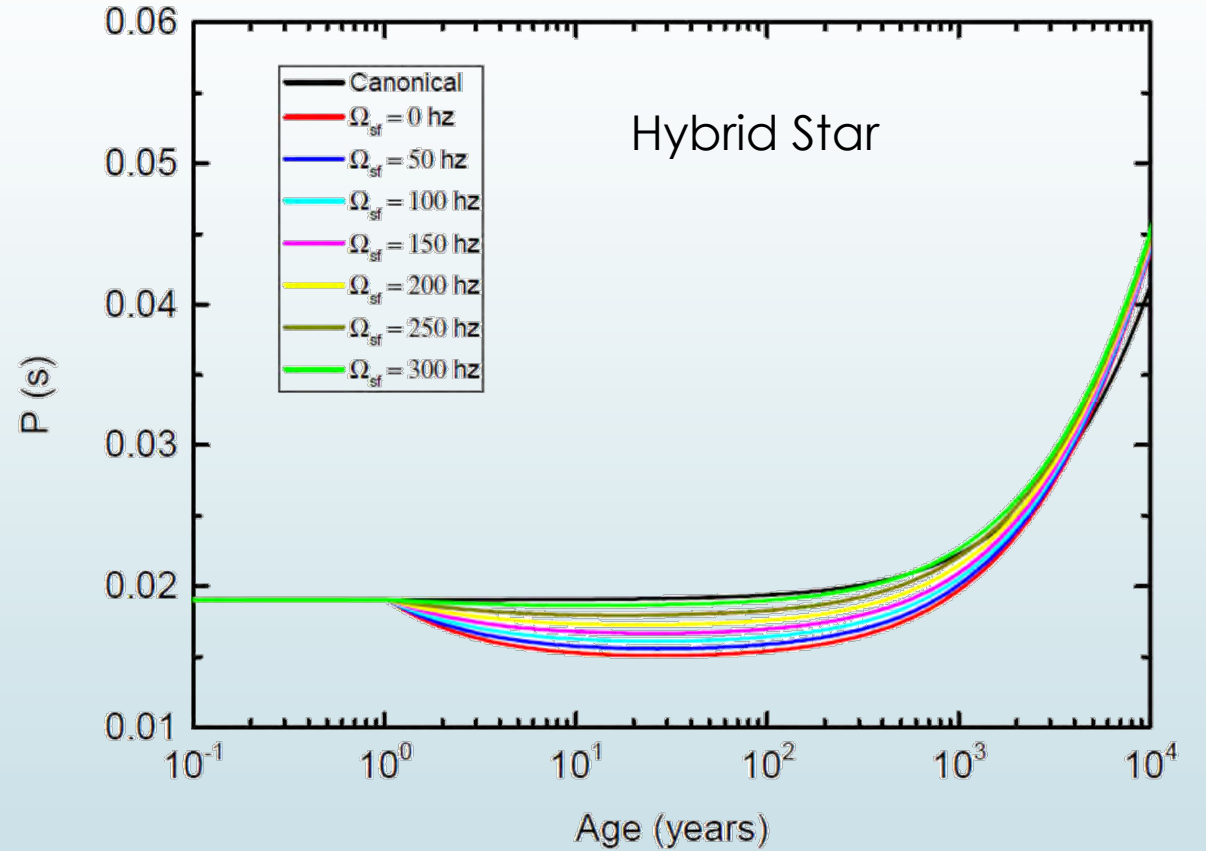
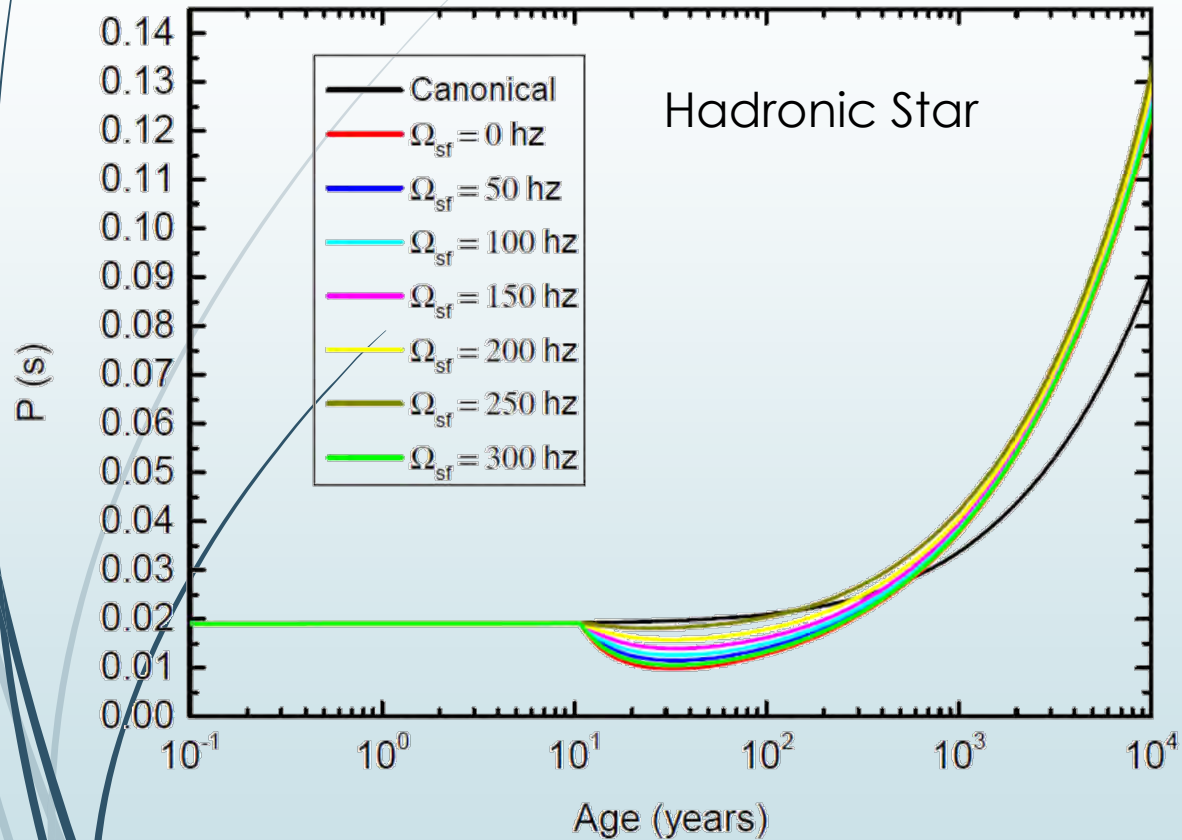
Hadronic Star



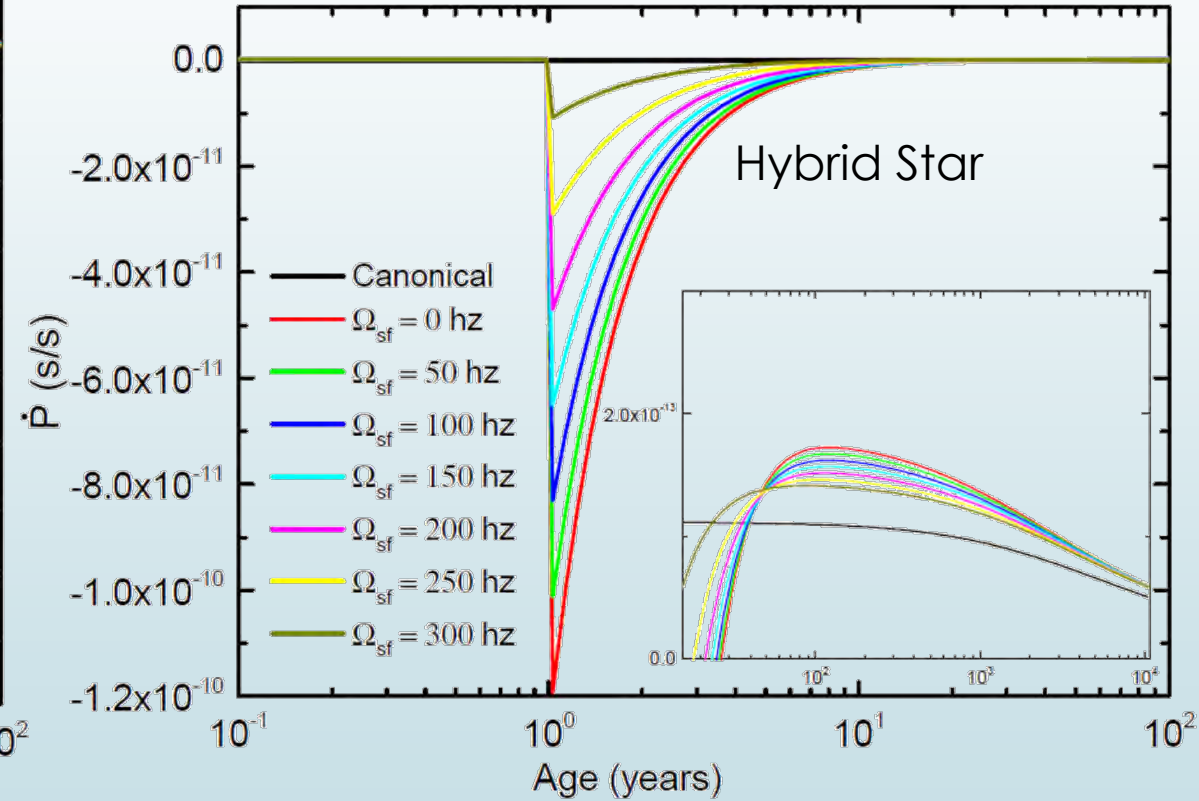
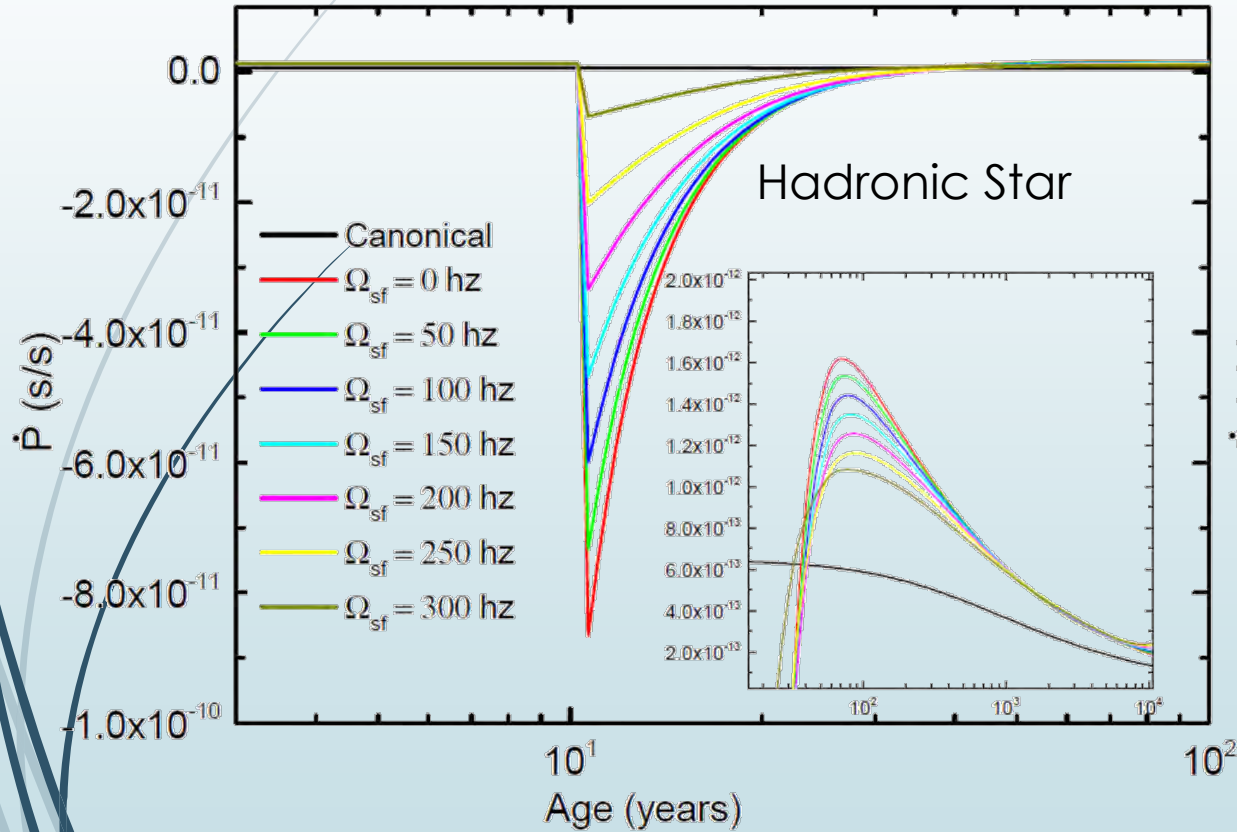
Hybrid Star



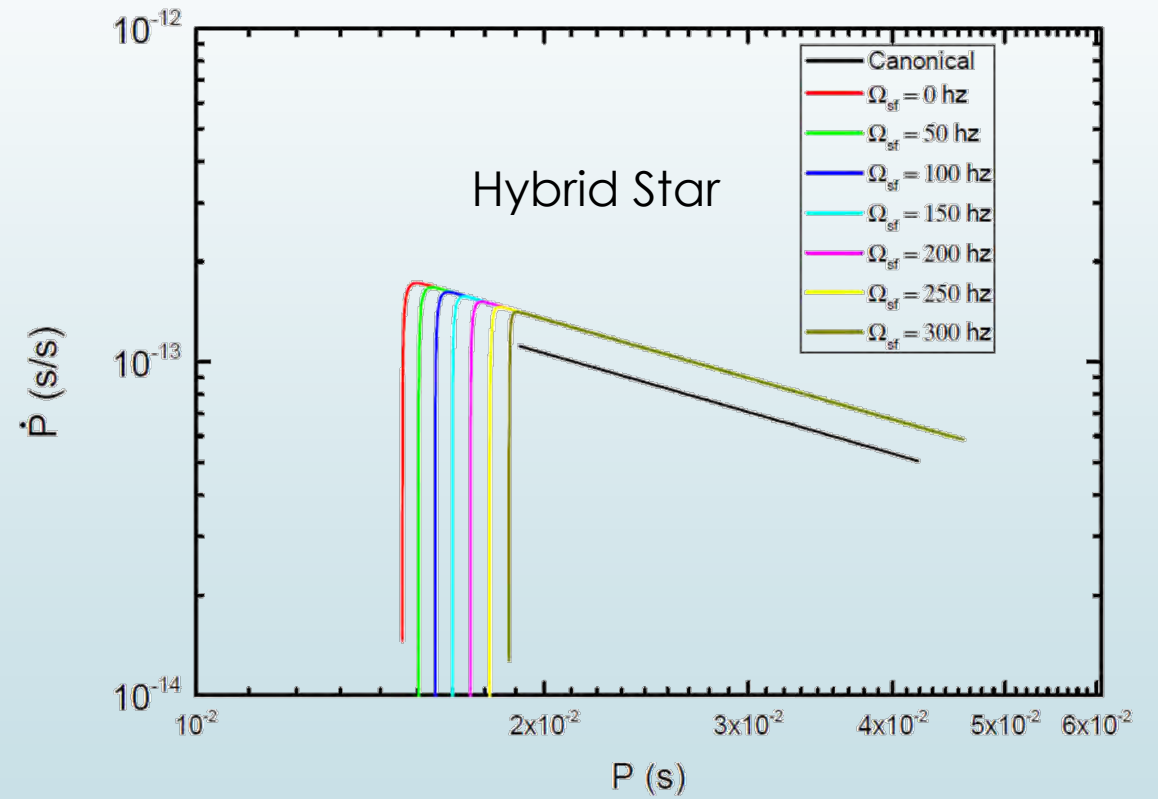
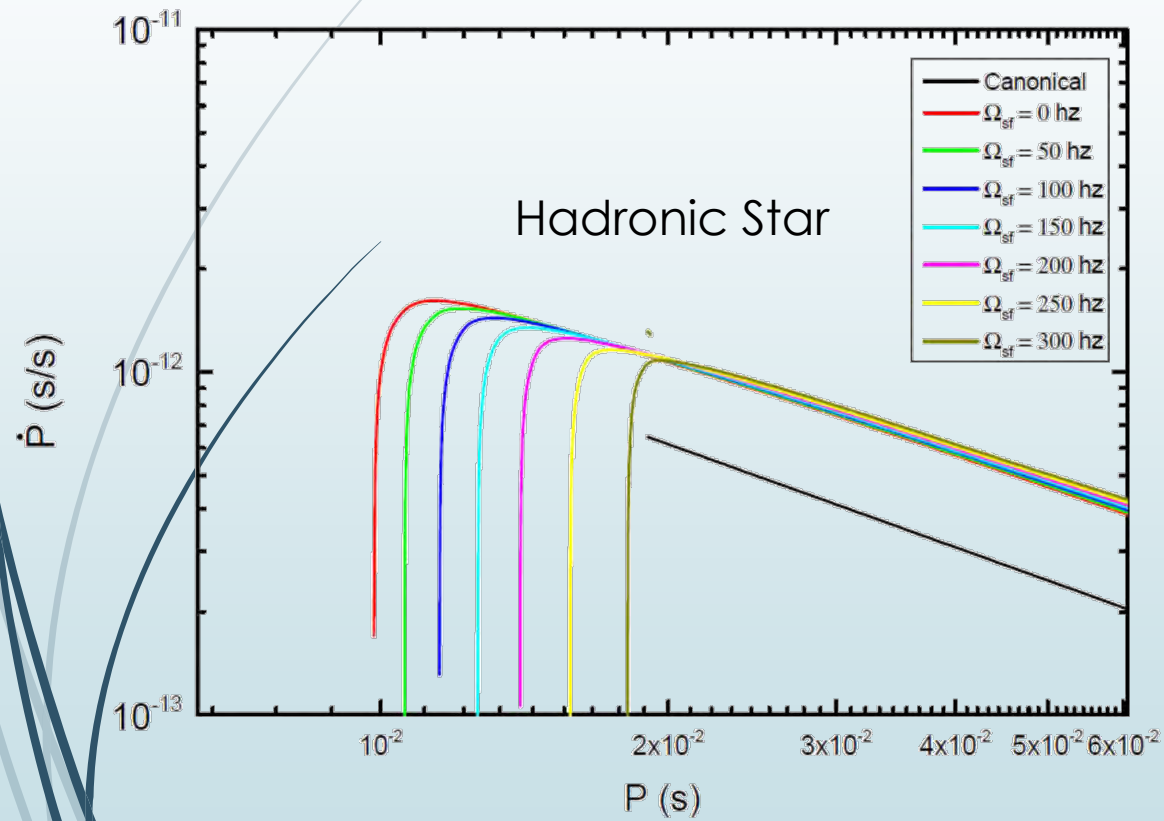
Spin Evolution



Pdot evolution

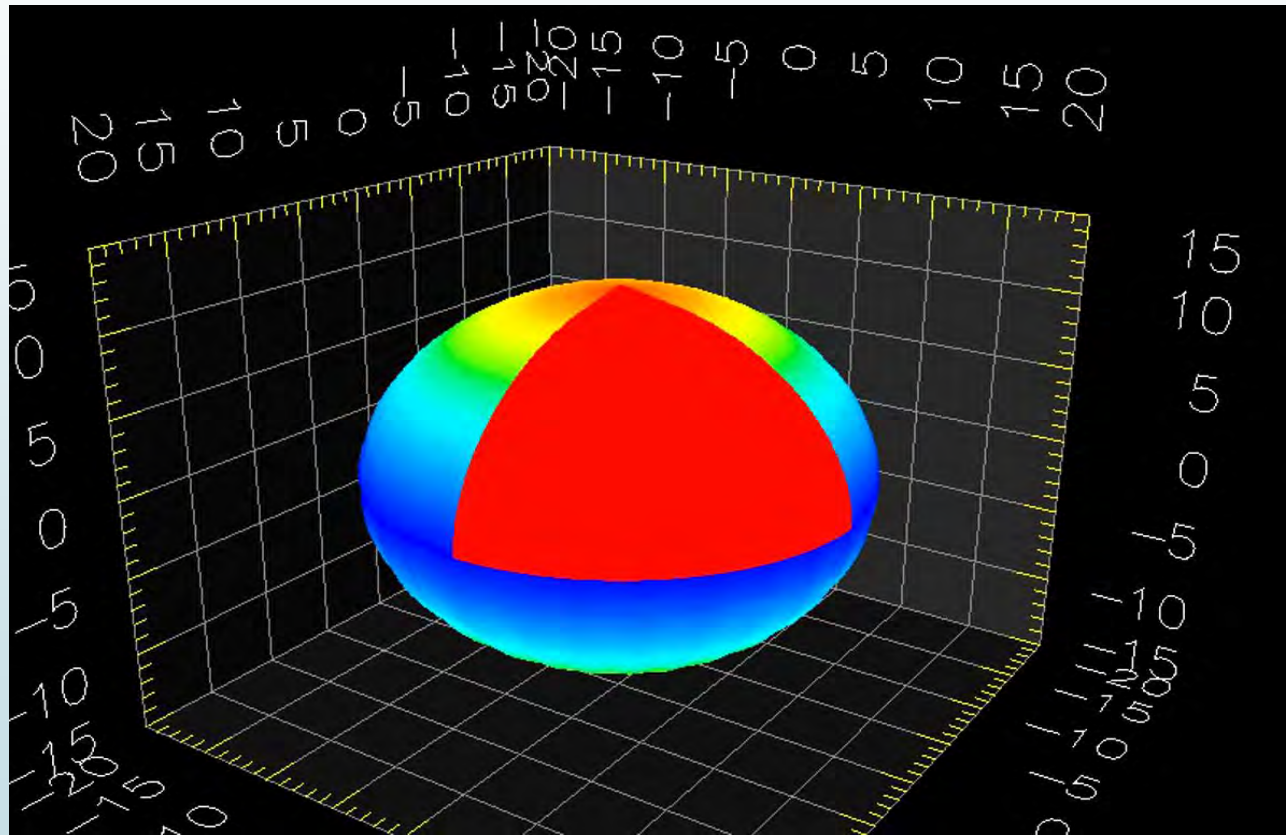


P-Pdot diagram



Next Steps

- Include rotation and magnetic field effects



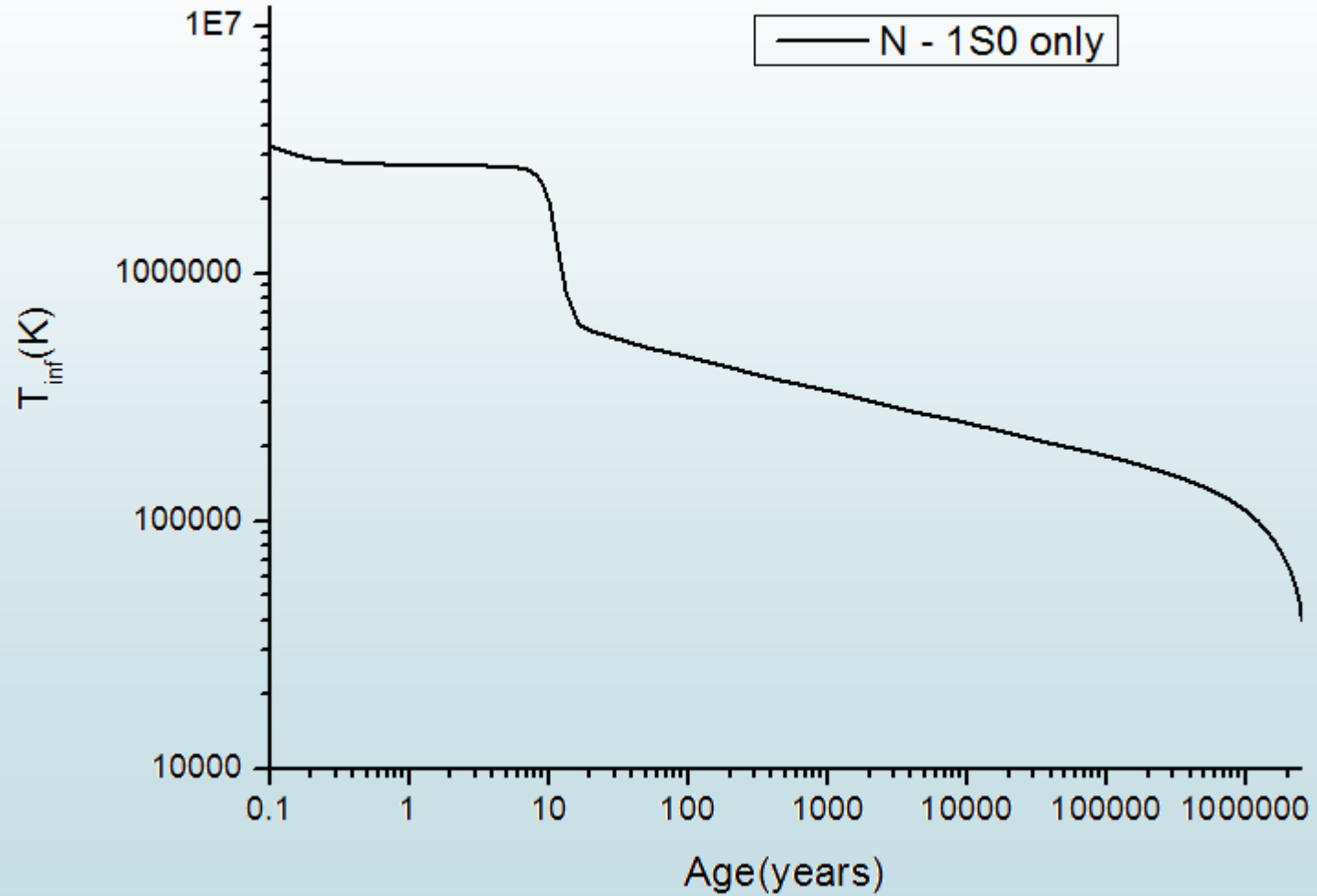


Conclusions

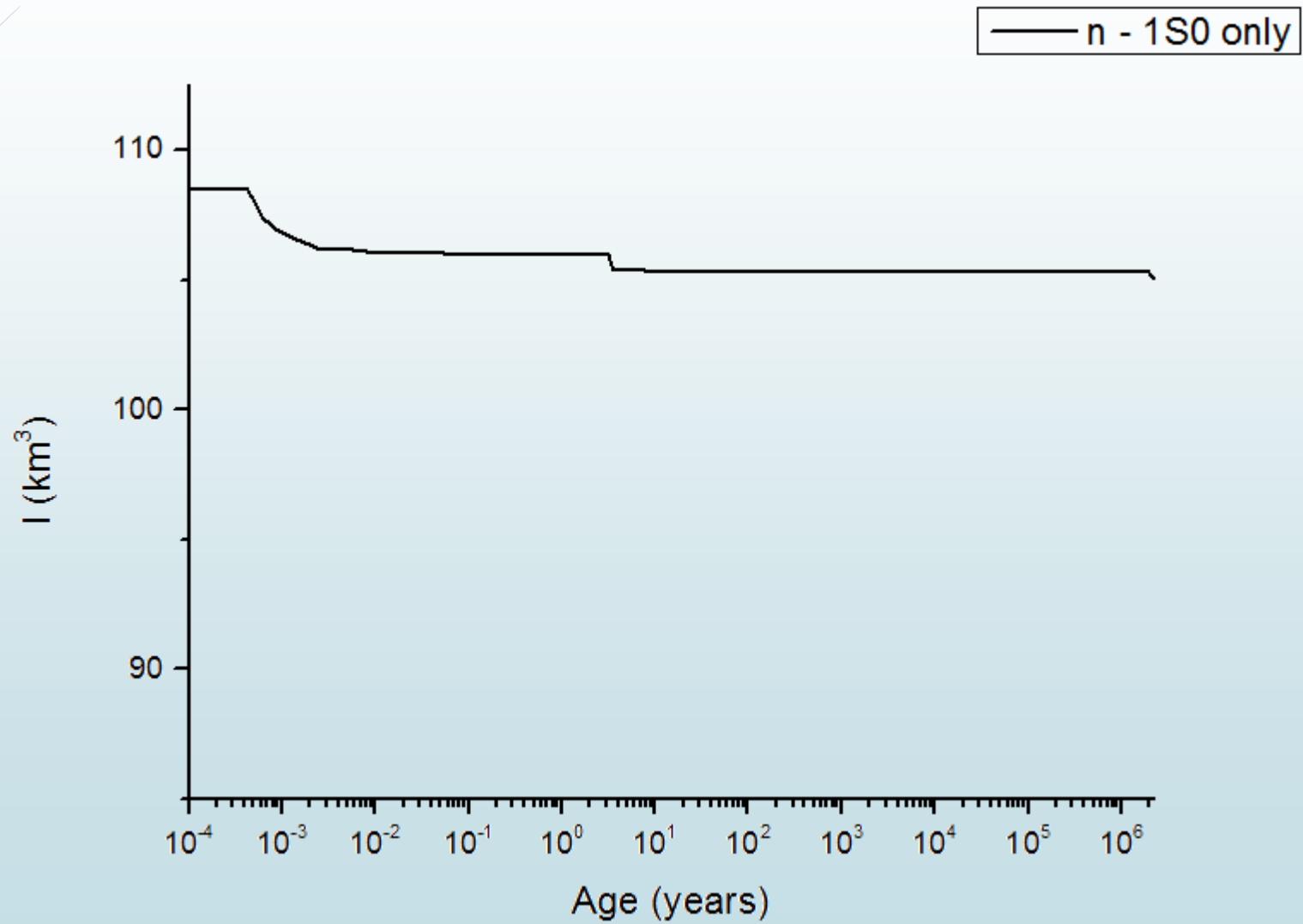


- ▶ Submerged magnetic fields may explain the existence of braking indices smaller than one.
- ▶ Superfluidity effects may also play a role in the spin-evolution of the object.
- ▶ Observation of spin properties may be used to constrain the inner composition.
- ▶ Need to explore further pairing patterns and microscopic models.

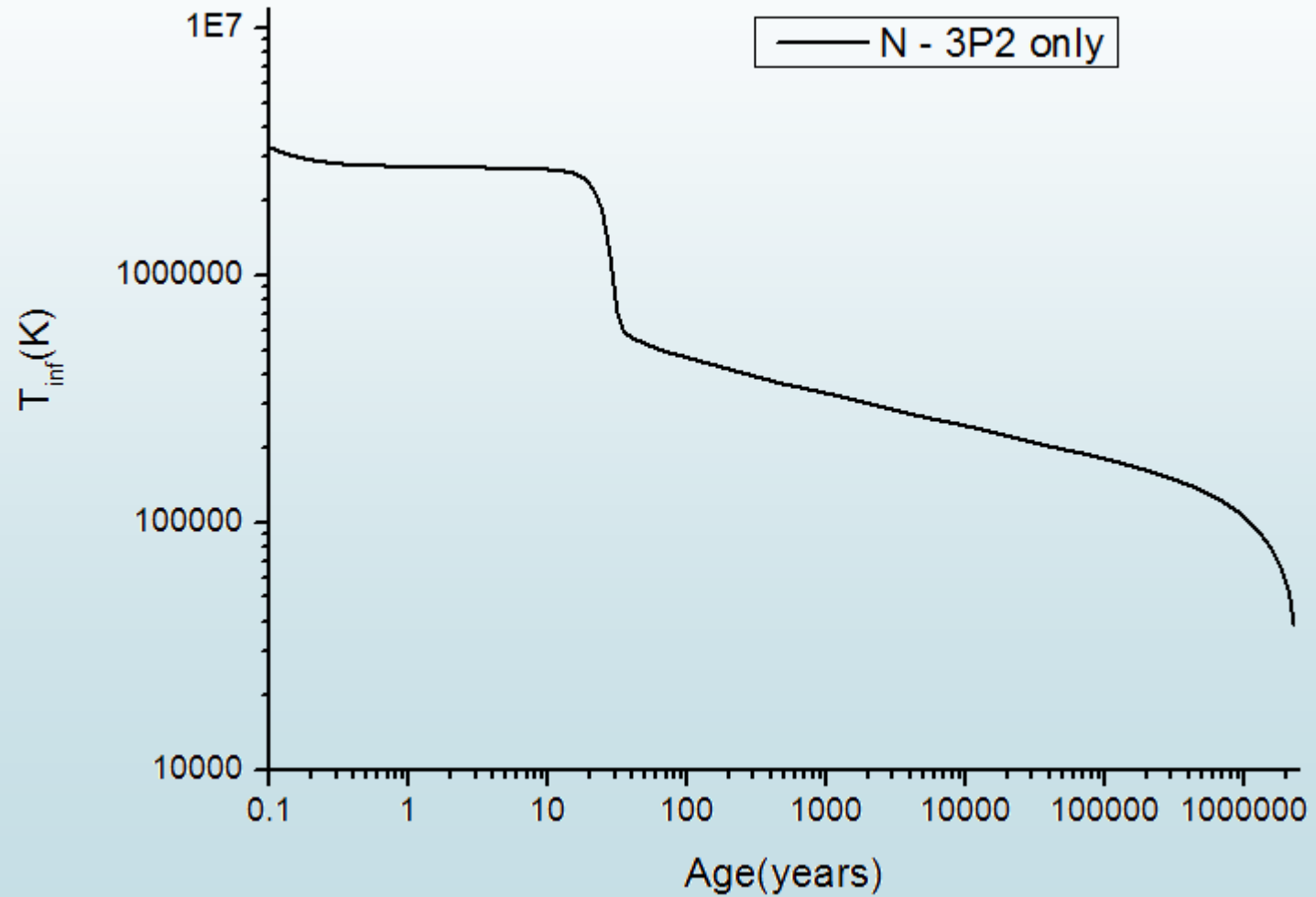
Cooling



Cooling

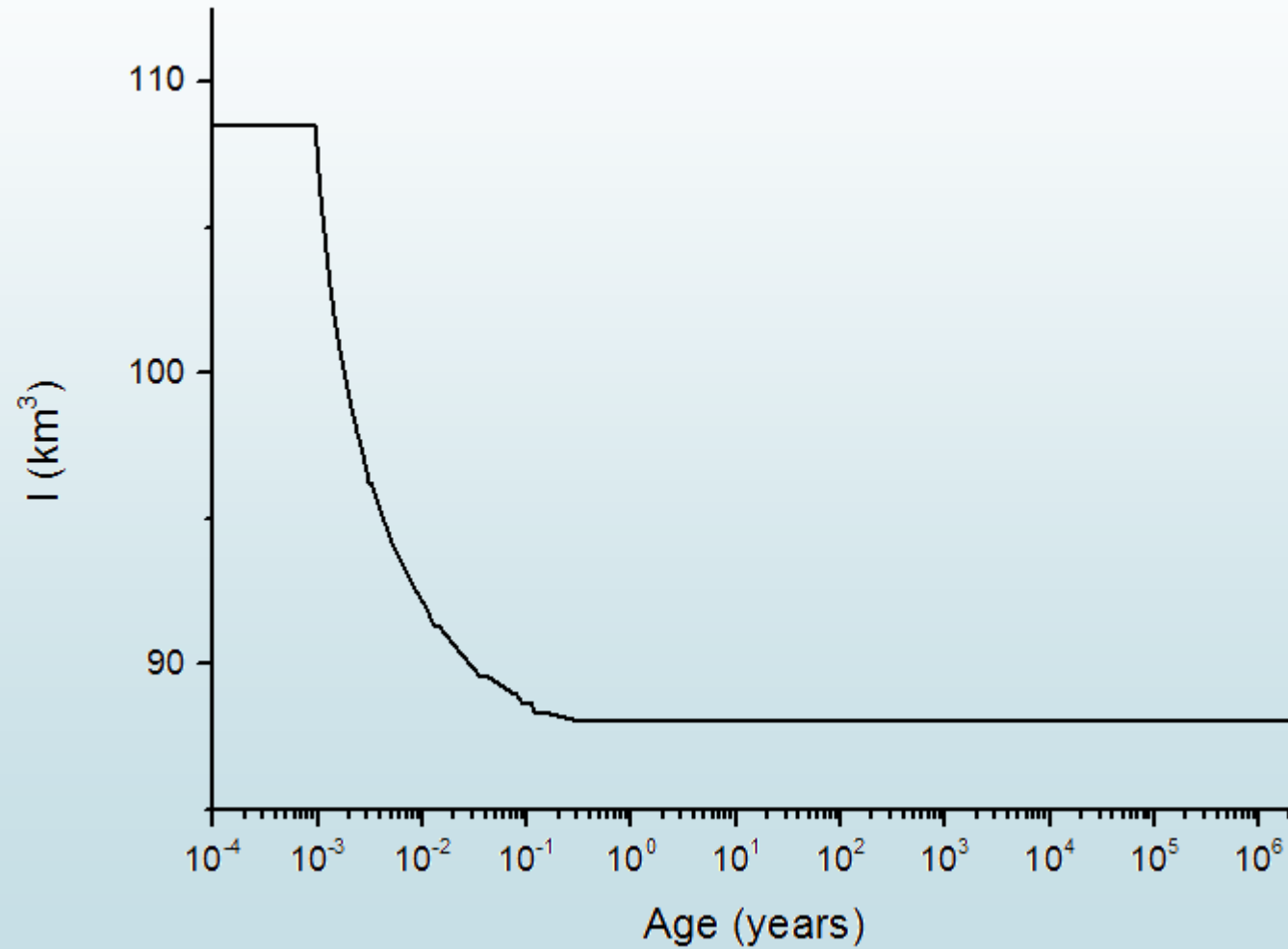


Cooling

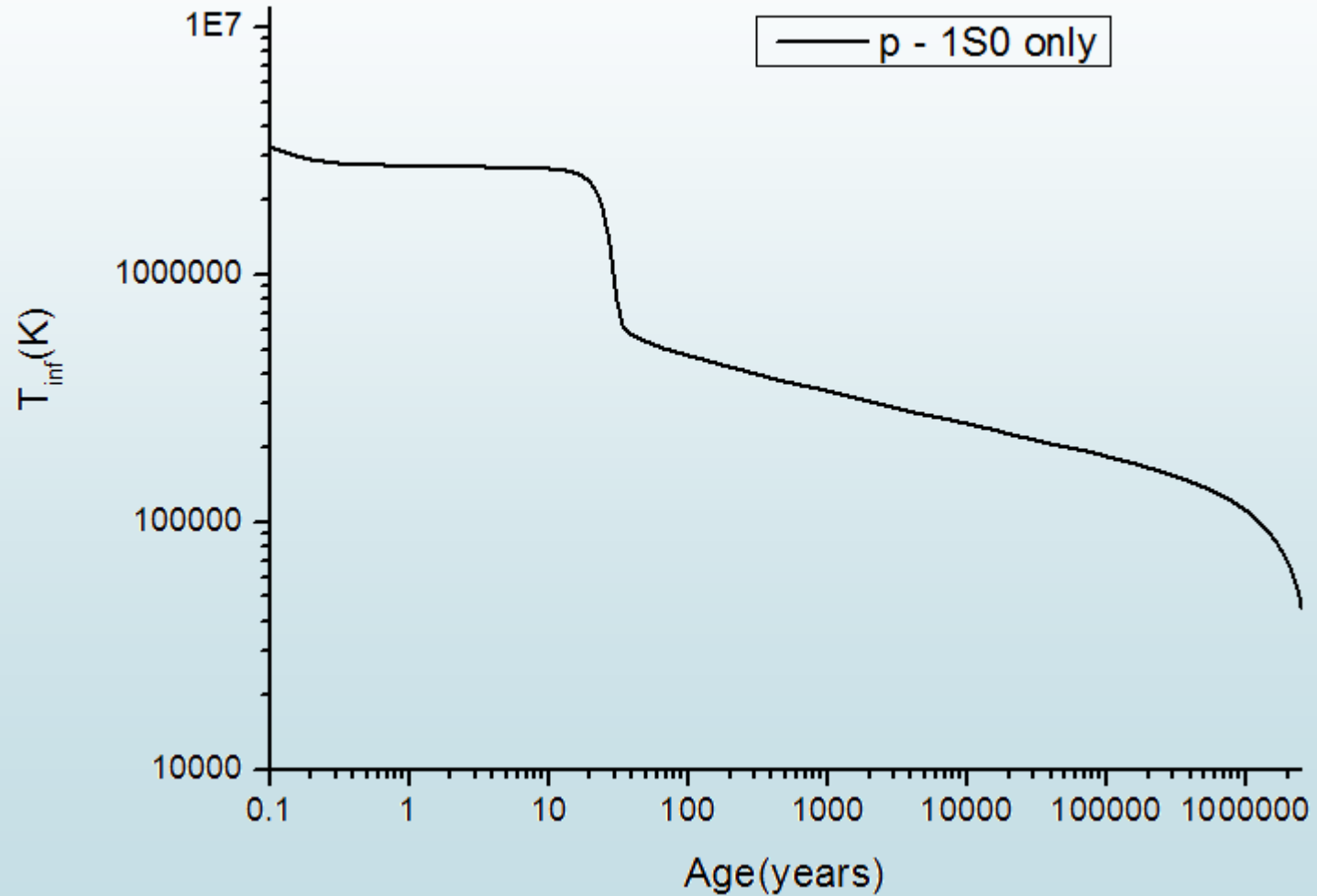


Cooling

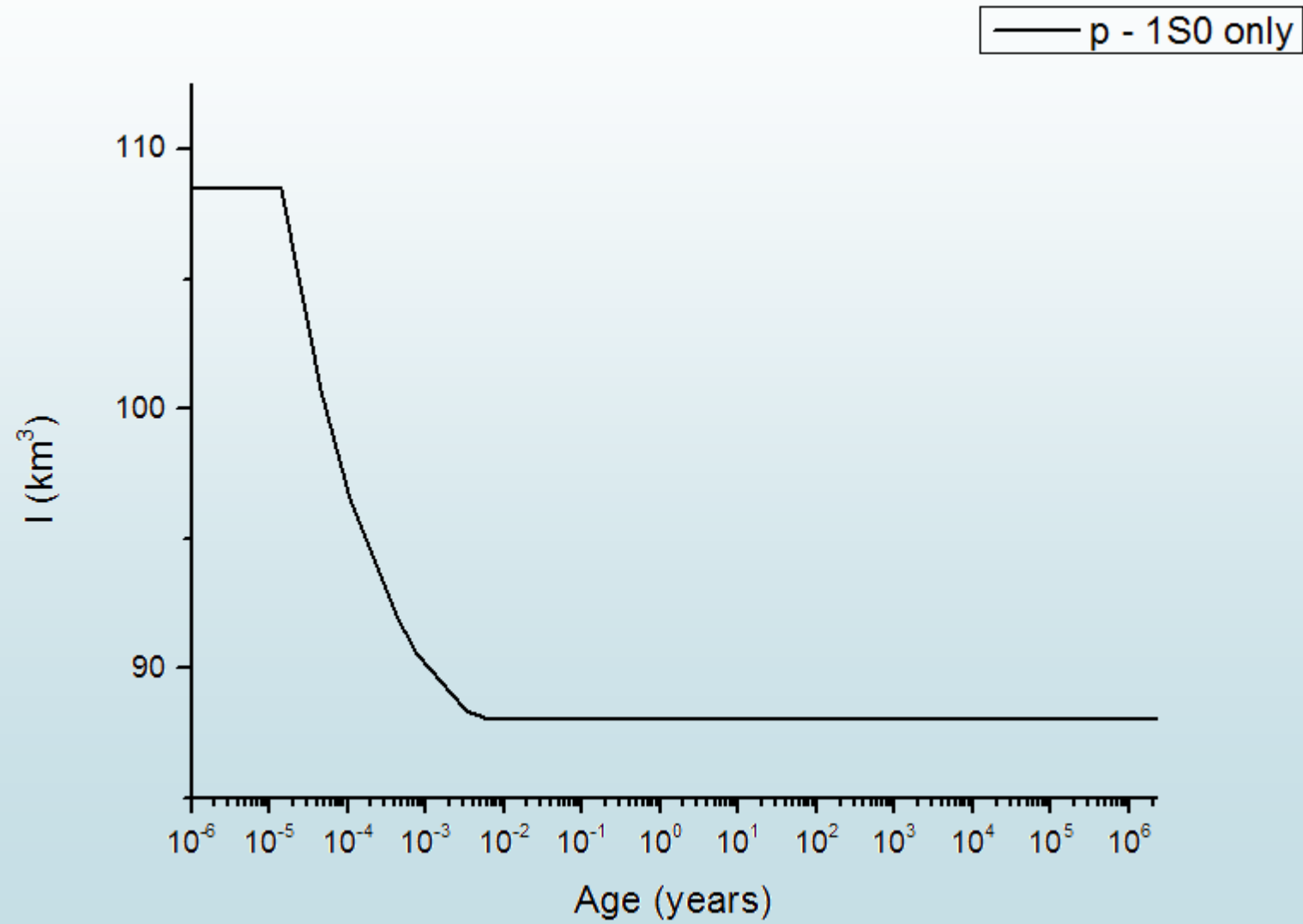
— n - 3P2 only



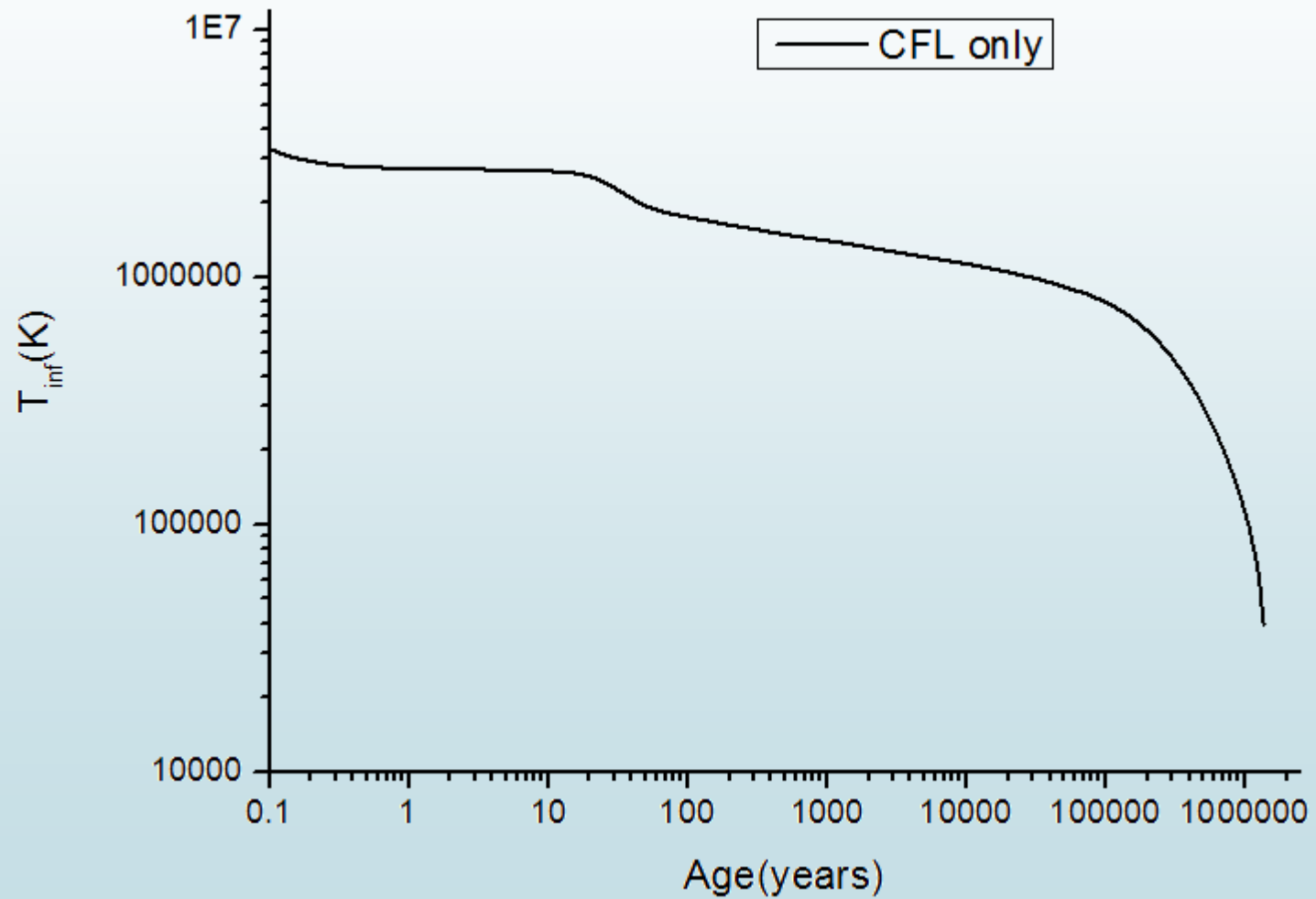
Cooling



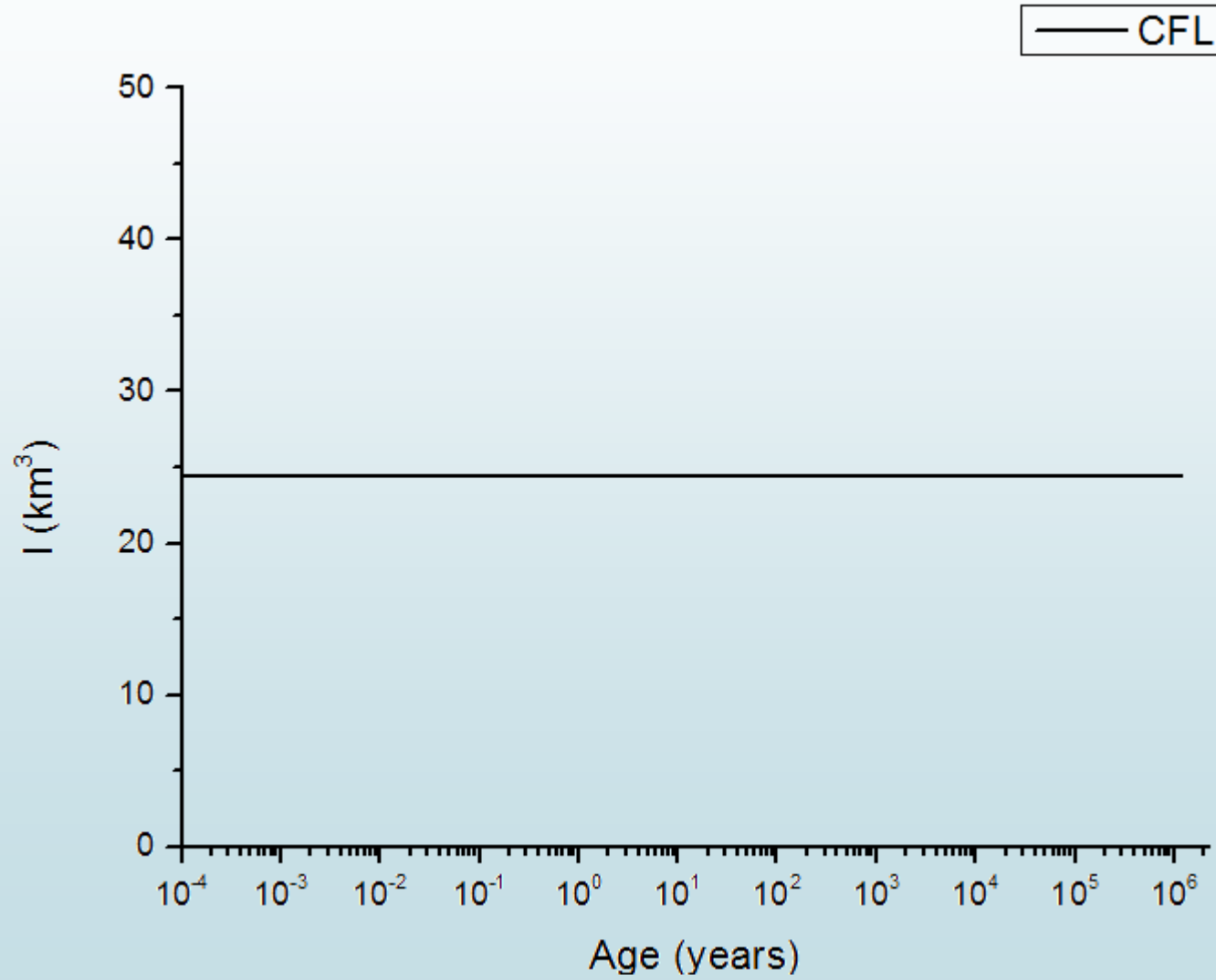
Cooling



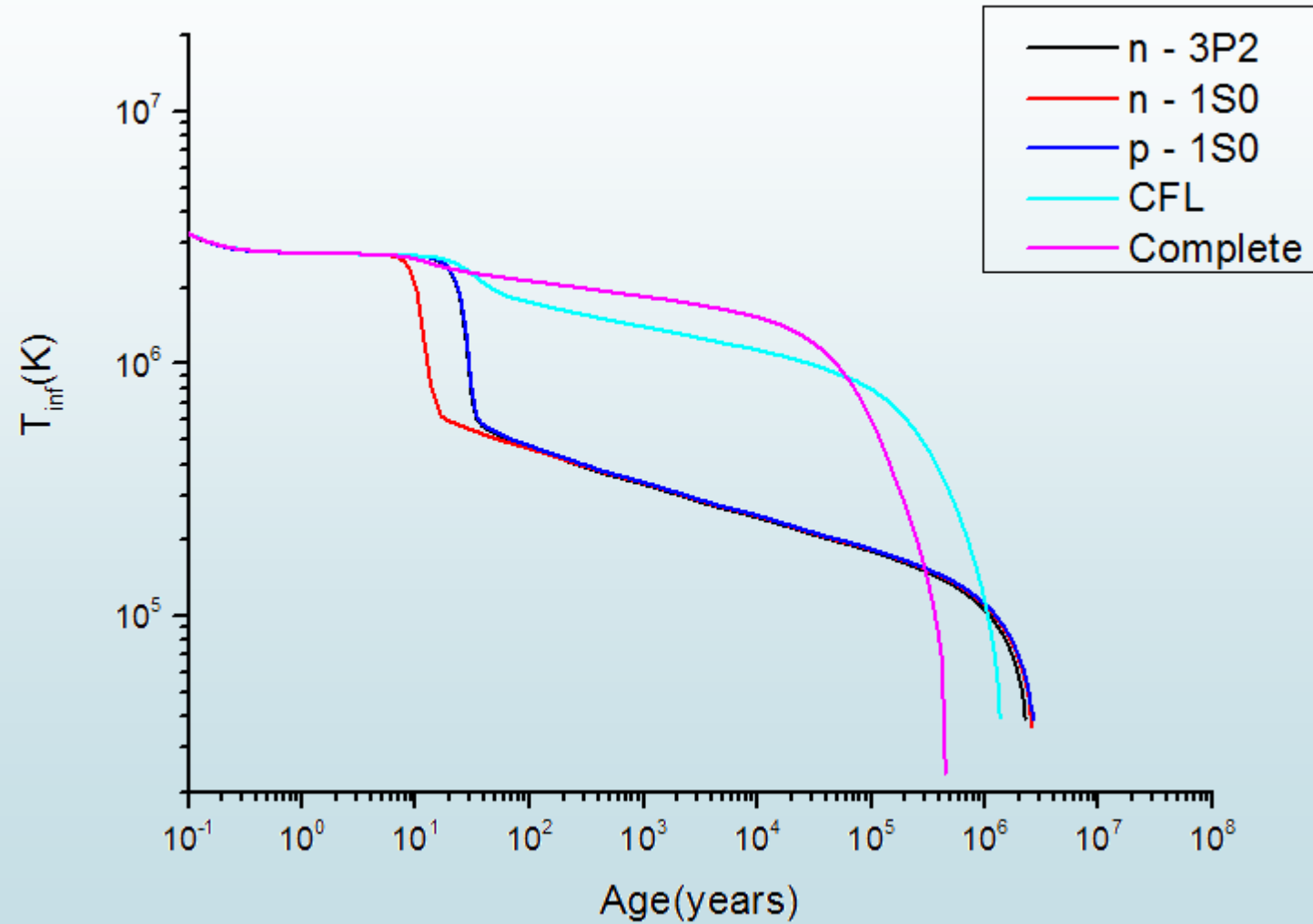
Cooling



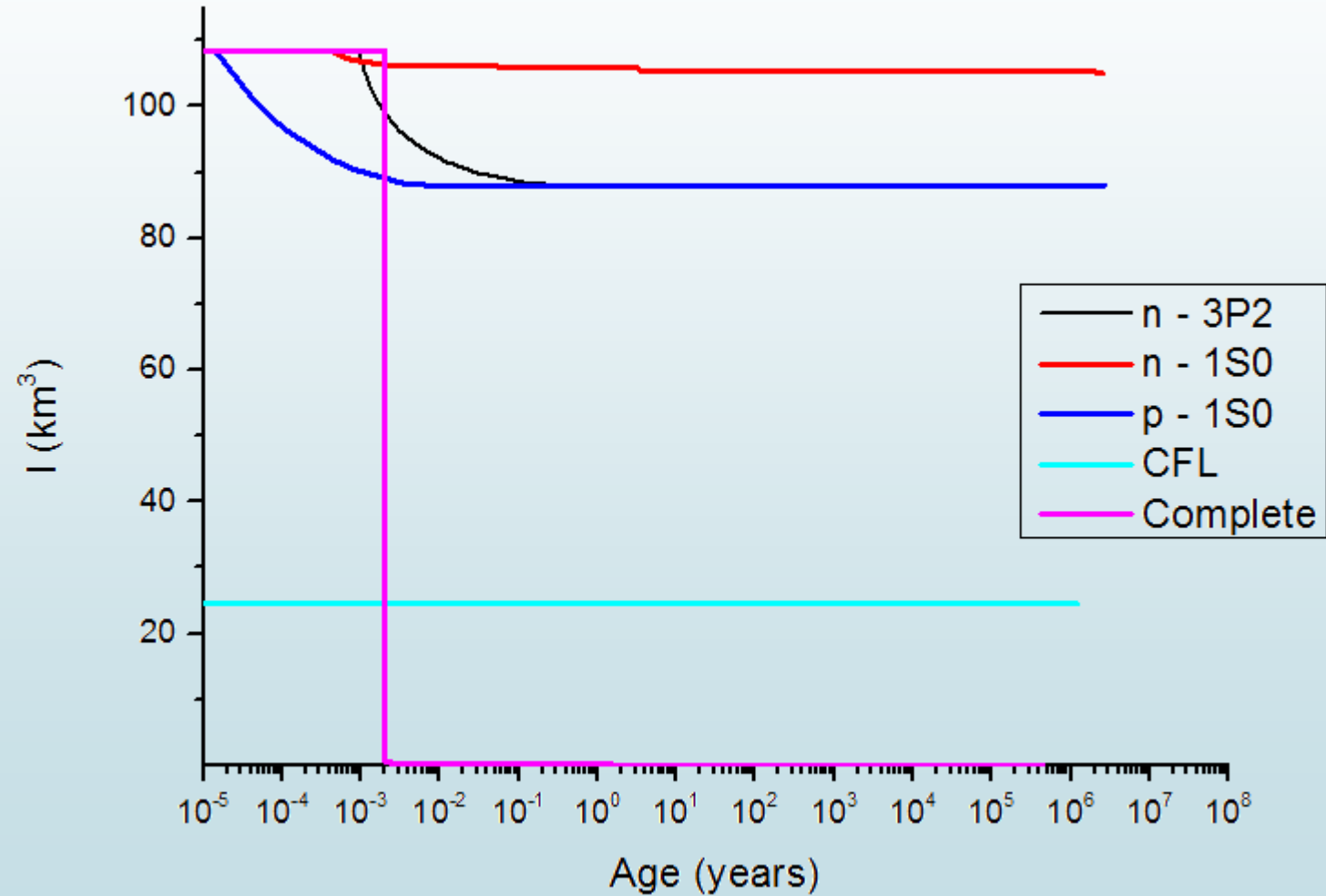
Cooling



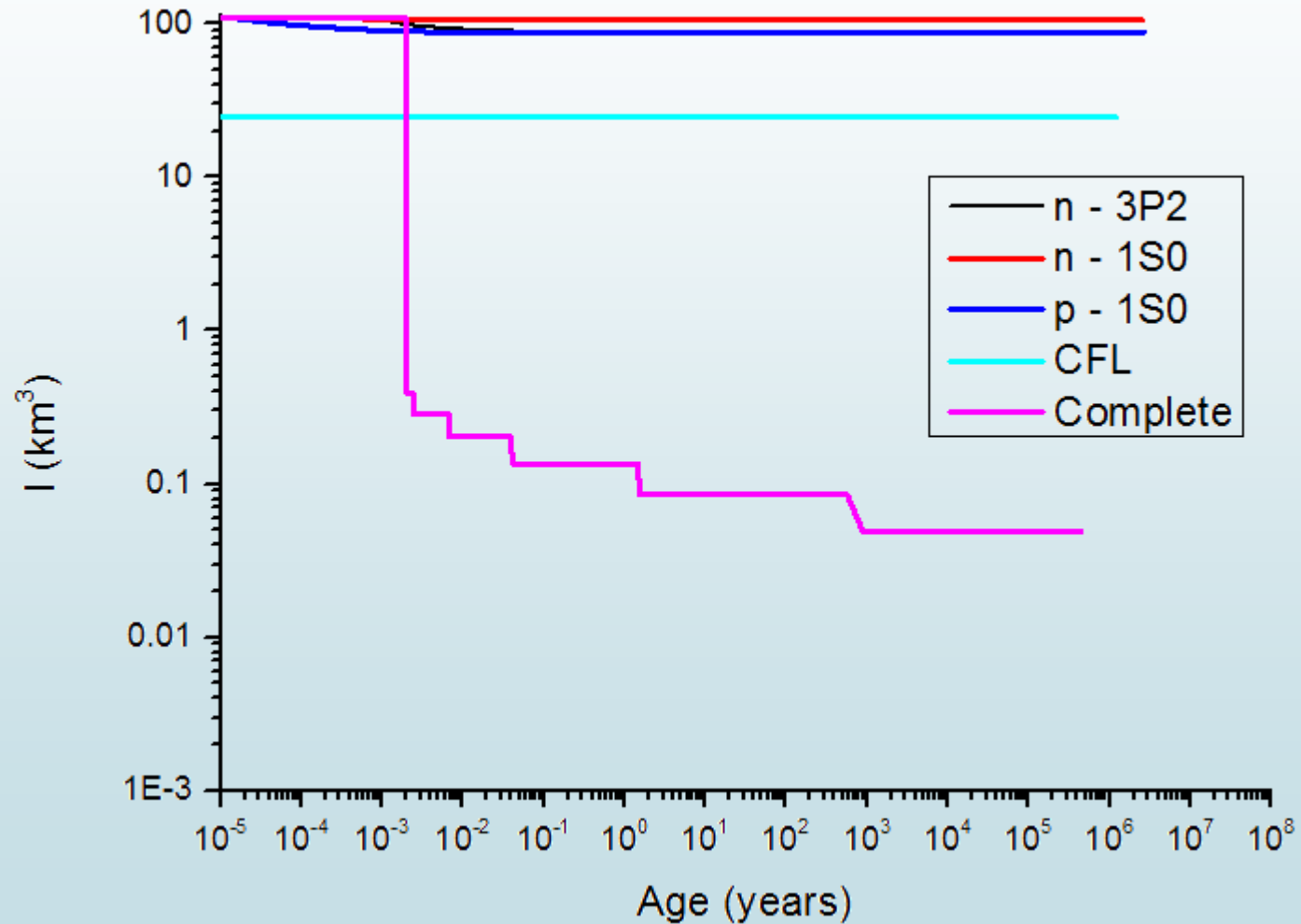
Cooling



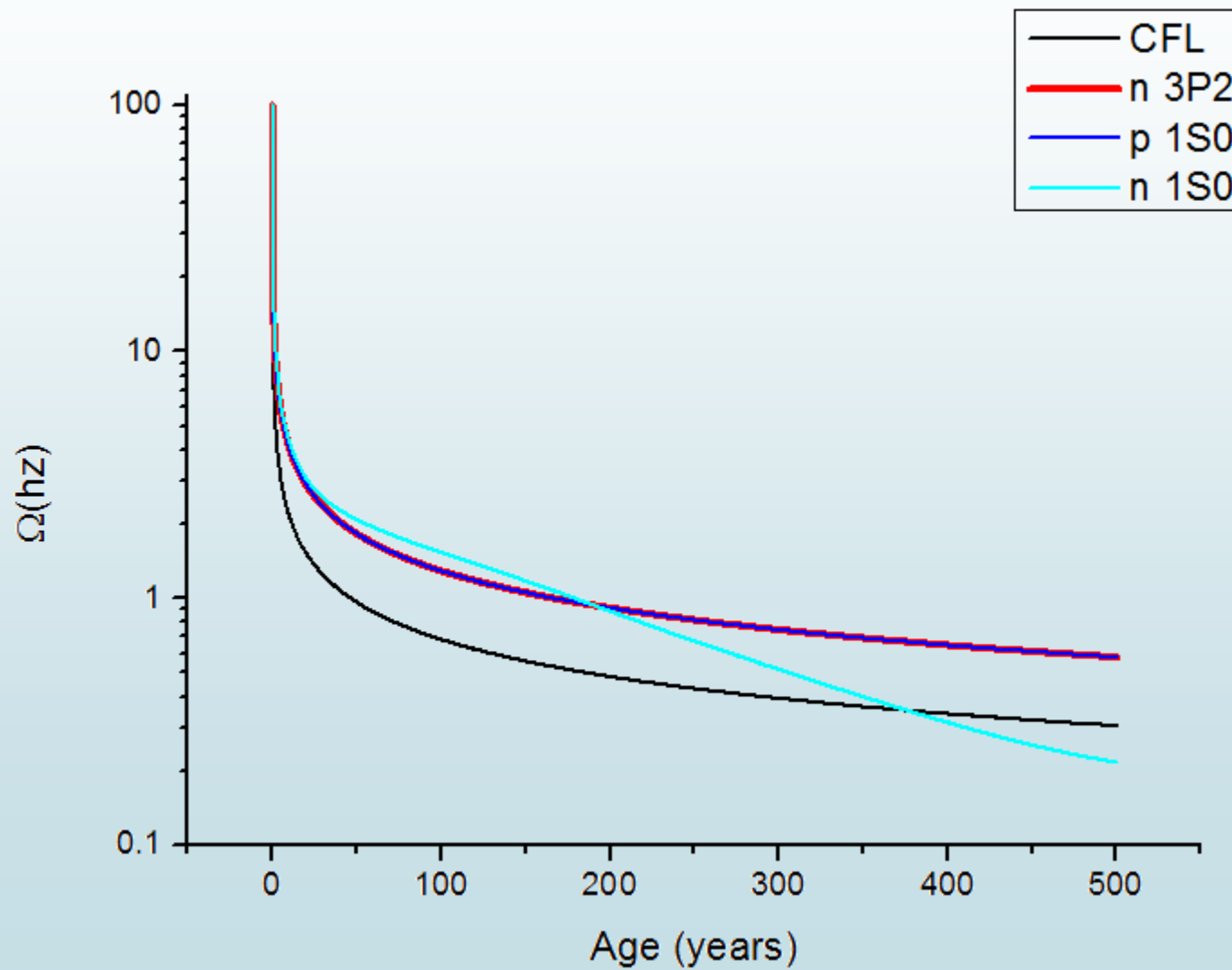
Moment of Inertia



Moment of Inertia

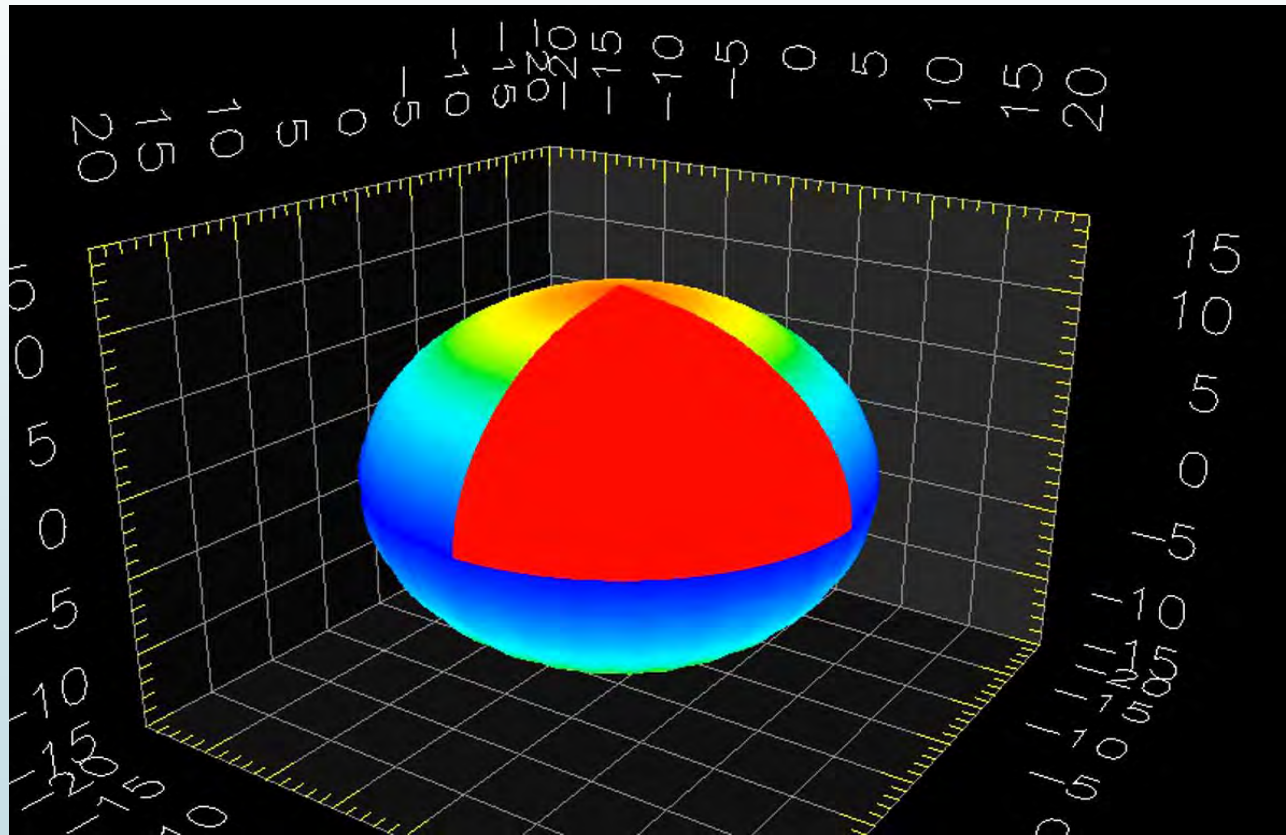


Frequency



Next Steps

- ▶ Include rotation and magnetic field effects



A dark grey arrow points to the right from the left edge of the slide. Below it, several thin, curved lines in shades of blue and grey sweep across the left side of the slide, creating a dynamic, abstract background element.

Conclusions and outlook

- There is something missing in the traditional Braking model....
- One can hope to explain the observed data by either changes in the magnetic field or the moment of inertia of the star.
- We believe that the most likely scenario involves a growing magnetic field together with changes in the moment of inertia.
- Changes in the moment of inertia may be triggered by cooling and/or spin evolution.
- Next: Include a self-consistent spin-magneto-hydro-thermal evolution.