

# Production of forward jets in high energy factorization

#### Krzysztof Kutak



Based on:

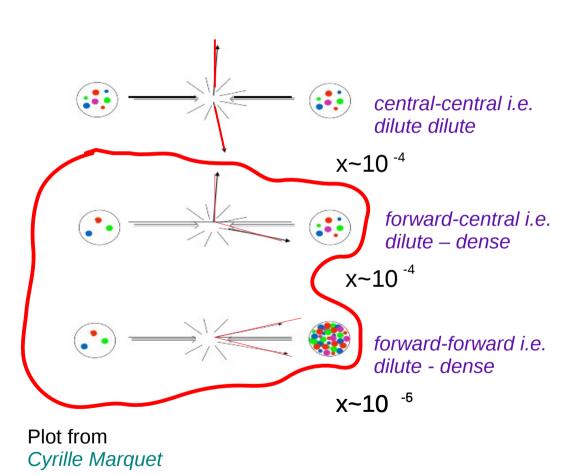
1409.3822 K.Kutak

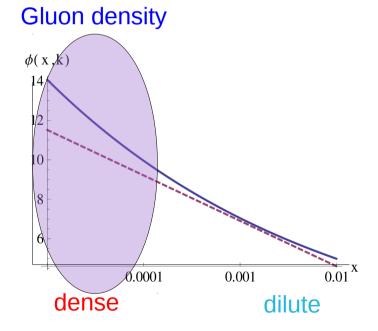
Phys.Lett. B737 (2014) 335-340, A. van Hameren, P. Kotko, K. Kutak, S. Sapeta

Phys. Rev. D 89, 094014 (2014), A. van Hameren, P. Kotko, K. Kutak, C. Marquet, S. Sapeta

Phys. Rev. D 86, 094043 (2012), Krzysztof Kutak, Sebastian Sapeta

## LHC as a scanner of gluon



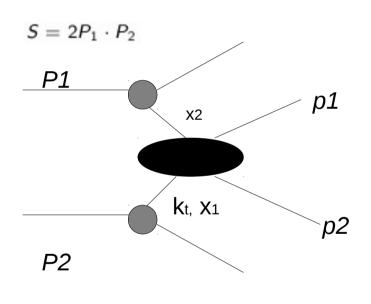


#### Hybrid factorization and dijets

$$\frac{d\sigma}{dy_1 dy_2 dp_{1t} dp_{2t} d\Delta\phi} = \sum_{a,c,d} \frac{p_{t1} p_{t2}}{8\pi^2 (x_1 x_2 S)^2} |\mathcal{M}_{ag\to cd}|^2 x_1 f_{a/A}(x_1, \mu^2) \mathcal{F}_{g/B}(x_2, k^2) \frac{1}{1 + \delta_{cd}}$$

Can be obtained from CGC after neglecting nonlinearities In that limit gluon density is just the dipole gluon density

Deak, Jung, KK, Hautmann '09 Deak, Jung, KK, Hautmann' 10



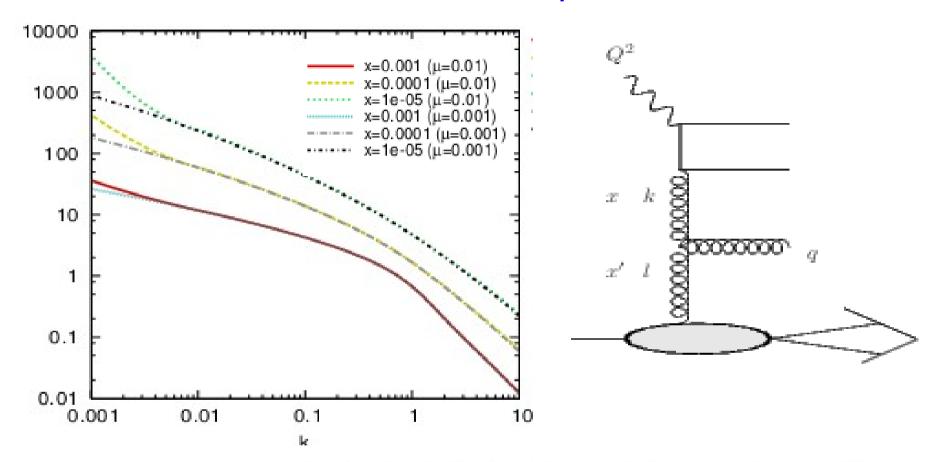
$$\Delta \phi$$

$$\mathcal{F}(x, k^2) = \frac{N_c}{\alpha_s (2\pi)^3} \int d^2b \int d^2r e^{ik \cdot r} \nabla_r^2 N(r, b, x)$$

Consistent with definition of gluon density from Dominguez, Marquet, Xiao, Yuan '10

- Resummation of logs of x and logs of hard scale
- Knowing well parton densities at large
- x one can get information about low x physics

## The BFKL equation



$$\mathcal{F}(x,k^2) = \mathcal{F}_0(x,k^2) + \overline{\alpha}_s \int_{x/x_0}^1 \frac{dz}{z} \int_0^\infty \frac{dl^2}{l^2} \left[ \frac{l^2 \mathcal{F}(x/z,l^2) - k^2 \mathcal{F}(x/z,k^2)}{|k^2 - l^2|} + \frac{k^2 \mathcal{F}(x/z,k^2)}{\sqrt{(4l^4 + k^4)}} \right]$$

when 
$$k > 1$$

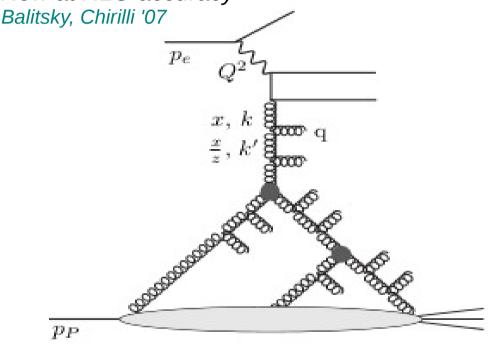
$$\mathcal{F}(x, k^2) = \mathcal{F}_0(x, k^2) + \bar{\alpha}_s \int_{x/x_0}^1 \frac{dz}{z} \int_{k_0^2}^{k^2} dl^2 \frac{\mathcal{F}(x/z, l^2)}{k^2}$$

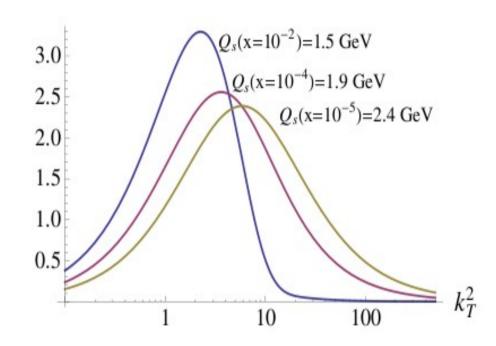
## The BK equation for unintegrated gluon density

Originally formulated in "x" space

Balitsky '96, Kovchegov'99

Now at NLO accuracy

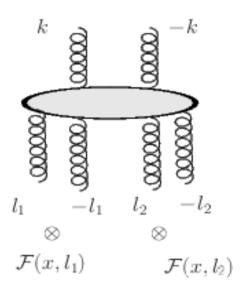




$$\mathcal{F}(x,k^{2}) = \mathcal{F}_{0}(x,k^{2}) + \overline{\alpha}_{s} \int_{x/x_{0}}^{1} \frac{dz}{z} \int_{0}^{\infty} \frac{dl^{2}}{l^{2}} \left[ \frac{l^{2}\mathcal{F}(x/z,l^{2}) - k^{2}\mathcal{F}(x/z,k^{2})}{|k^{2} - l^{2}|} + \frac{k^{2}\mathcal{F}(x/z,k^{2})}{\sqrt{(4l^{4} + k^{4})}} \right] - \frac{2\alpha_{s}^{2}\pi}{N_{c}R^{2}} \int_{x/x_{0}}^{1} \frac{dz}{z} \left\{ \left[ \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \mathcal{F}(x/z,l^{2}) \right]^{2} + \mathcal{F}(x/z,k^{2}) \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \ln\left(\frac{l^{2}}{k^{2}}\right) \mathcal{F}(x/z,l^{2}) \right\}$$

Kwiecinski, KK '01 Nikolaev, Schafer '06

## The BK equation



$$\mathcal{V}(k,-k;l_1,-l_1,l_2,-l_2) = \frac{\pi\alpha_s^2}{N_cR^2} \left[ 2\theta(l_1^2-k^2)\theta(l_2^2-k^2) + k^2\ln\frac{l_1^2}{l_2^2}\delta(l_1^2-k^2)\theta(l_2^2-l_1^2) + k^2\ln\frac{l_2^2}{l_1^2}\delta(l_2^2-k^2)\theta(l_1^2-l_2^2) \right]$$

Bartel,KK '07

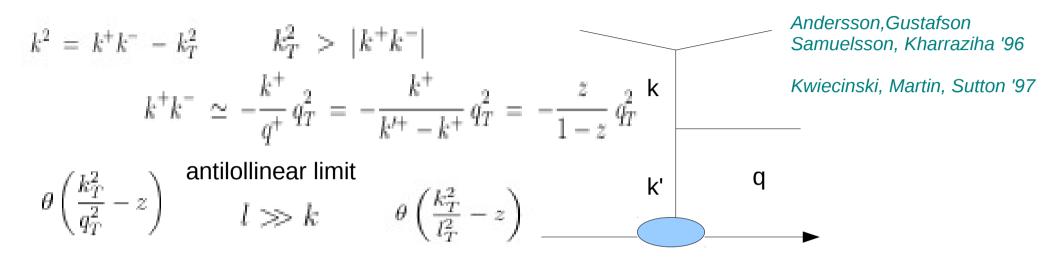
Anticollinear pole dominates TPV is 0 in DLL

$$\mathcal{F}(x,k^{2}) = \mathcal{F}_{0}(x,k^{2}) + \overline{\alpha}_{s} \int_{x/x_{0}}^{1} \frac{dz}{z} \int_{0}^{\infty} \frac{dl^{2}}{l^{2}} \left[ \frac{l^{2}\mathcal{F}(x/z,l^{2}) - k^{2}\mathcal{F}(x/z,k^{2})}{|k^{2} - l^{2}|} + \frac{k^{2}\mathcal{F}(x/z,k^{2})}{\sqrt{(4l^{4} + k^{4})}} \right] - \frac{2\alpha_{s}^{2}\pi}{N_{c}R^{2}} \int_{x/x_{0}}^{1} \frac{dz}{z} \left\{ \left[ \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \mathcal{F}(x/z,l^{2}) \right]^{2} + \mathcal{F}(x/z,k^{2}) \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \ln\left(\frac{l^{2}}{k^{2}}\right) \mathcal{F}(x/z,l^{2}) \right\}$$

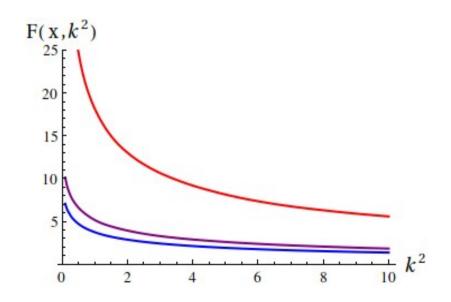
when k>>l

$$\mathcal{F}(x,k^2) = \mathcal{F}_0(x,k^2) + \bar{\alpha}_s \int_{x/x_0}^1 \frac{dz}{z} \int_{k_0^2}^{k^2} dl^2 \frac{\mathcal{F}(x/z,l^2)}{k^2}$$

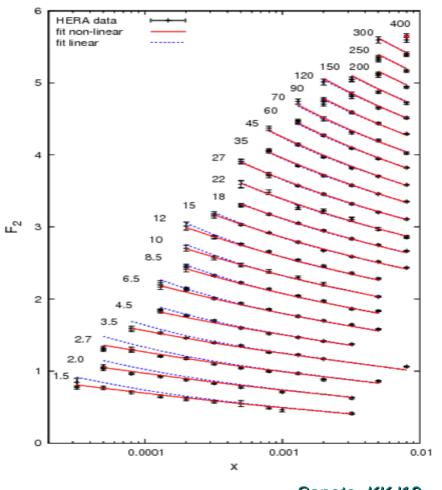
#### The kinematical constraint effects



$$\begin{split} f(x,k^2) &= f_0(x,k^2) \\ &+ \overline{\alpha}_s \int_x^1 \frac{dz}{z} \int_0^\infty \frac{dl^2}{l^2} \bigg[ \frac{\theta(k^2/l^2-z) f(x/z,l^2) - f(x/z,k^2)}{|k^2-l^2|} + \frac{f(x/z,k)}{\sqrt{(4l^4+k^4)}} \bigg] \end{split}$$



## BFKL applied to DIS - some recent results

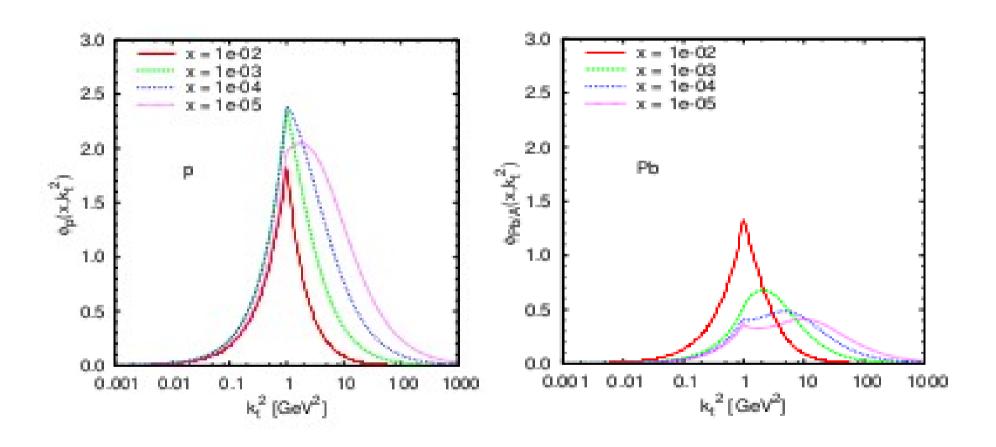


p  $Q^2$   $Q^2$ 

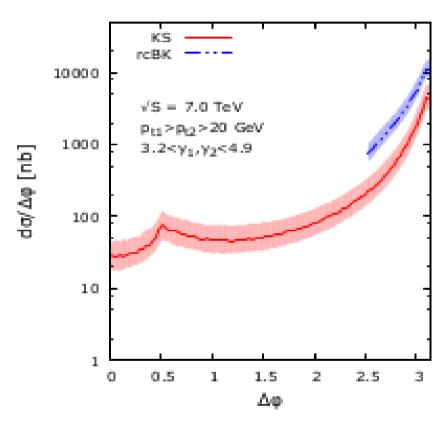
FromBK equation with corrections of higher order

Sapeta, KK '12

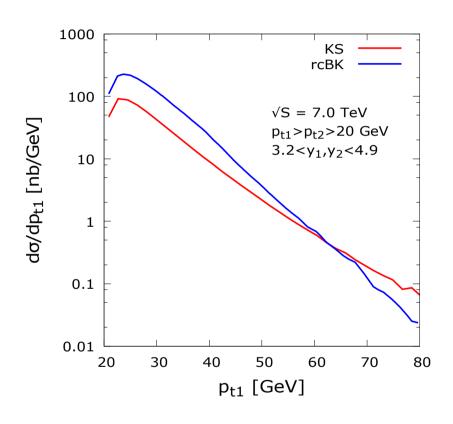
## Glue in p vs. glue in Pb



#### Results for decorelations



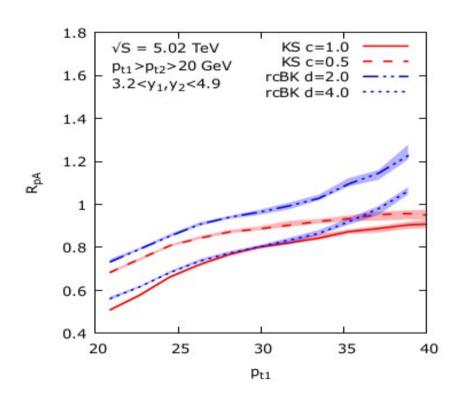
Results obtained with gluons coming from two prescriptions to improve the LL BK equation

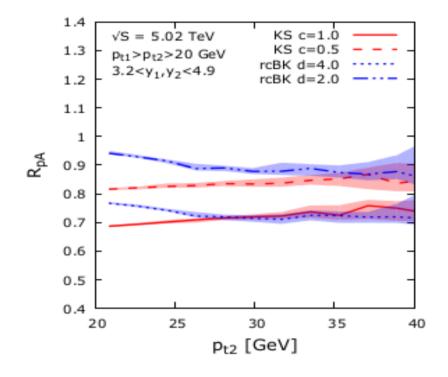


Better behaviour of KS at large pt

## Forward-forward dijets

A. van Hameren, Kotko, KK, Marquet, Sapeta '14





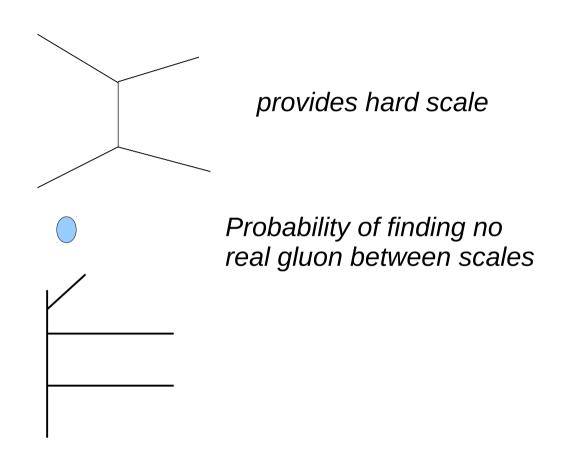
rcBK: not correct at large pt KS: reaches unity at large pt

Studies of sub-leading jet gives more pronounced signal of nonlinear effects.

## Introducing hard scale dependence

Nonlinear extension of CCFM not applied so far to phenomenology

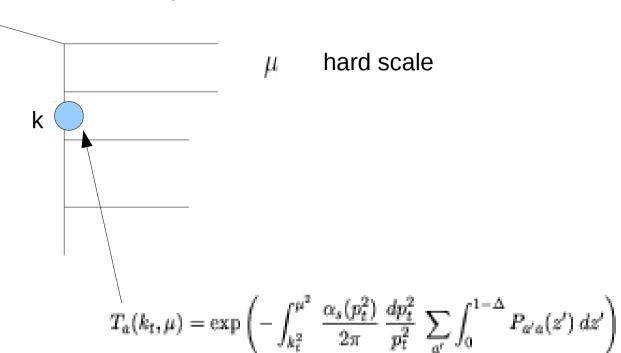
Include the effect in the last step of evolution



## Introducing hard scale dependence

Probability of finding no real gluon Between scales  $\mu$  and k

Survival probability of the gap without emissions



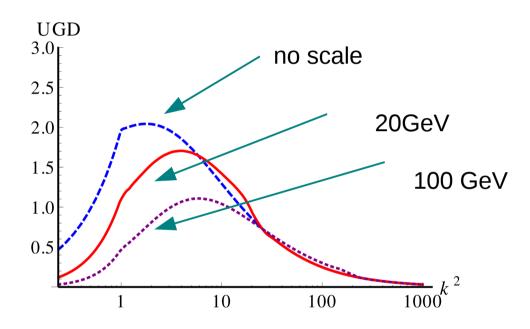
Kutak '14

$$\mathcal{A}(x,k^2,\mu^2) = \theta(\mu^2 - k^2)T_s(\mu^2,k^2) \frac{xg(x,\mu^2)}{xg_{hs}(x,\mu^2)} \mathcal{F}(x,k^2) + \theta(k^2 - \mu^2)\mathcal{F}(x,k^2).$$

$$xg_{hs}(x,\mu^2) = \int^{\mu^2} dk^2 T_s(\mu^2,k^2) \mathcal{F}(x,k^2), \ xg(x,\mu^2) = \int^{\mu^2} dk^2 \mathcal{F}(x,k^2)$$

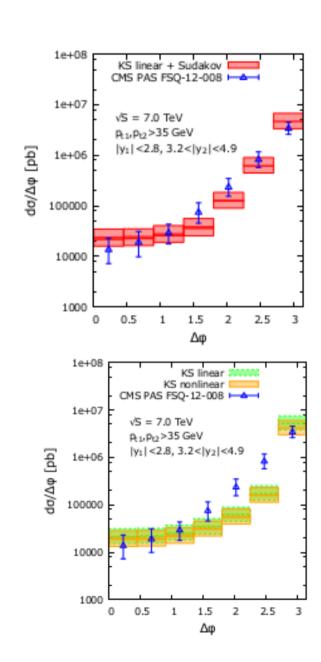
## Saturation scale in equation with coherence forward-forward jets

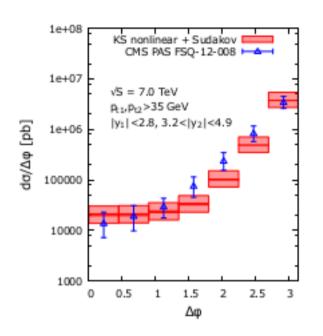
Kutak '14



Low kt gluons are suppressed. The conservation of probability leads to change of shape of gluon density which depends on the hard scale

#### Decorelations inclusive scenario



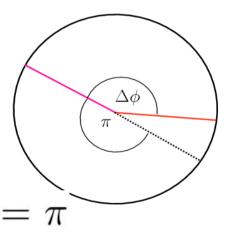


In pure DGLAP approach i.e  $2 \rightarrow 2 + pdf$  one would get delta function at

Sudakov effects by reweighing implemented in LxJet Monte Carlo P. Kotko

A.v.Hameren, P.Kotko, KK, S.Sapeta '14

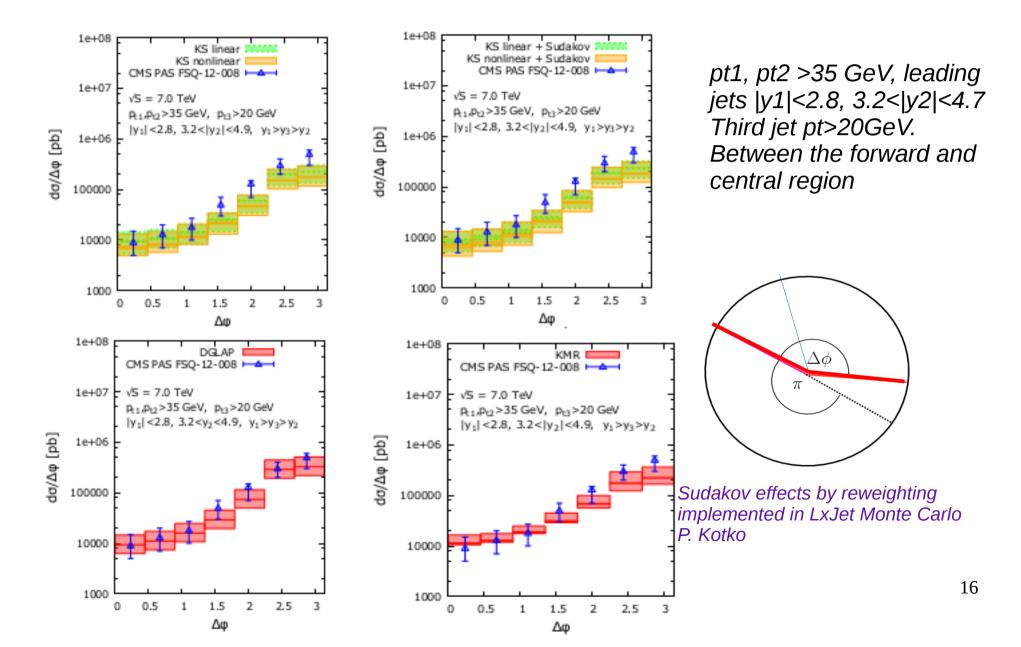
pt1,pt2 >35, leading jets |y1|<2.8, 3.2<|y2|<4.7 No further requirement on jets



Studied also context of RHIC Albacete, Marquet '10

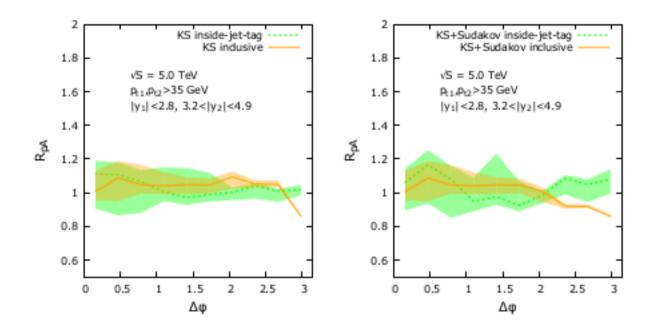
## Decorelations inside jet tag scenario

A.v.Hameren, P.Kotko, KK, S.Sapeta '14



## Predictions for p-Pb for forward-central

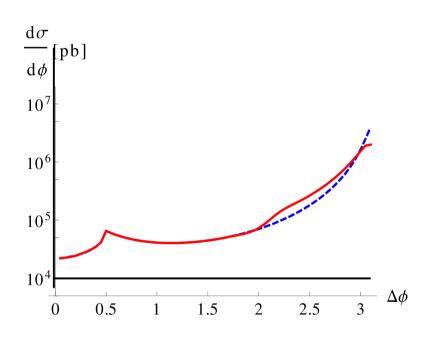
A.v.Hameren, P.Kotko, KK, S.Sapeta '14

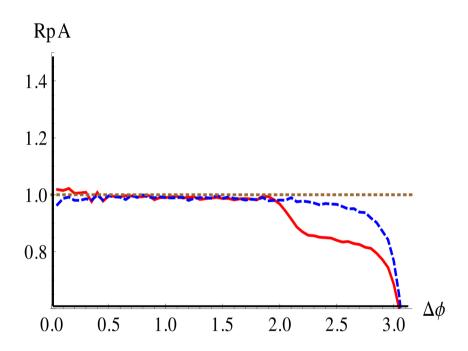


- •Sudakov enhances saturation effects
- •However, saturation effects are rather weak for forward-central jets

## Predictions for p-Pb for forward-forward

Kutak '14





- •The hard scale effects make the potential signatures of saturation more pronounced.
- "Pb" affected more by saturation than "p" therefore we see more significant effect.

#### Conclusions and outlook

- •Achieved good description of forward-central jet measurement
- •Predictions for forward-forward dijets pPb are provided
- •Open question description of the decorelations within CCFM. It includes Sudakov and low x dynamics.
- Open question description of the decorelations within nonlinear extension of CCFM