

SUSY 2015 - Flavor Violation Theory & Experiment

$$\underline{B \rightarrow K^* \mu \mu}$$

Charming Penguins
strike back again ?

M.Ciuchini, M.Fedele, E.Franco, S.Mishima,
A.Paul, L.Silvestrini, M.V. (in preparation)



M. Valli

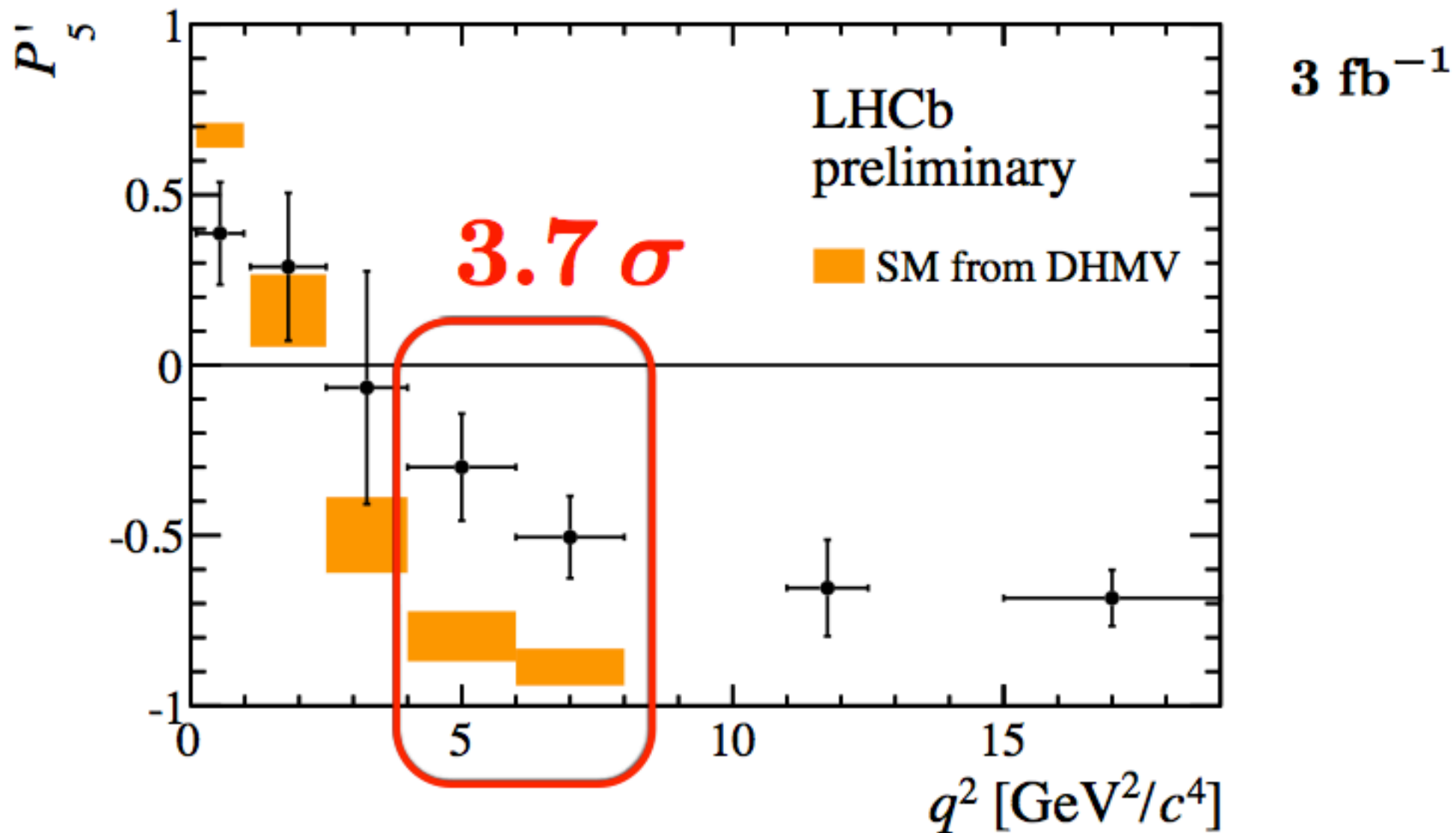


Lake Tahoe (USA),
August 24 2015

Supported by:



The P'_5 anomaly



S. Descotes-Genon, L. Hofer, J. Matias, and J. Virto

JHEP 1412 (2014) 125, arXiv:1407.8526

B to $K^* \mu^+ \mu^-$ generalities

In the Standard Model (SM), FCNCs arise only @ loop-level

→ NP can sizably contribute to these rare processes

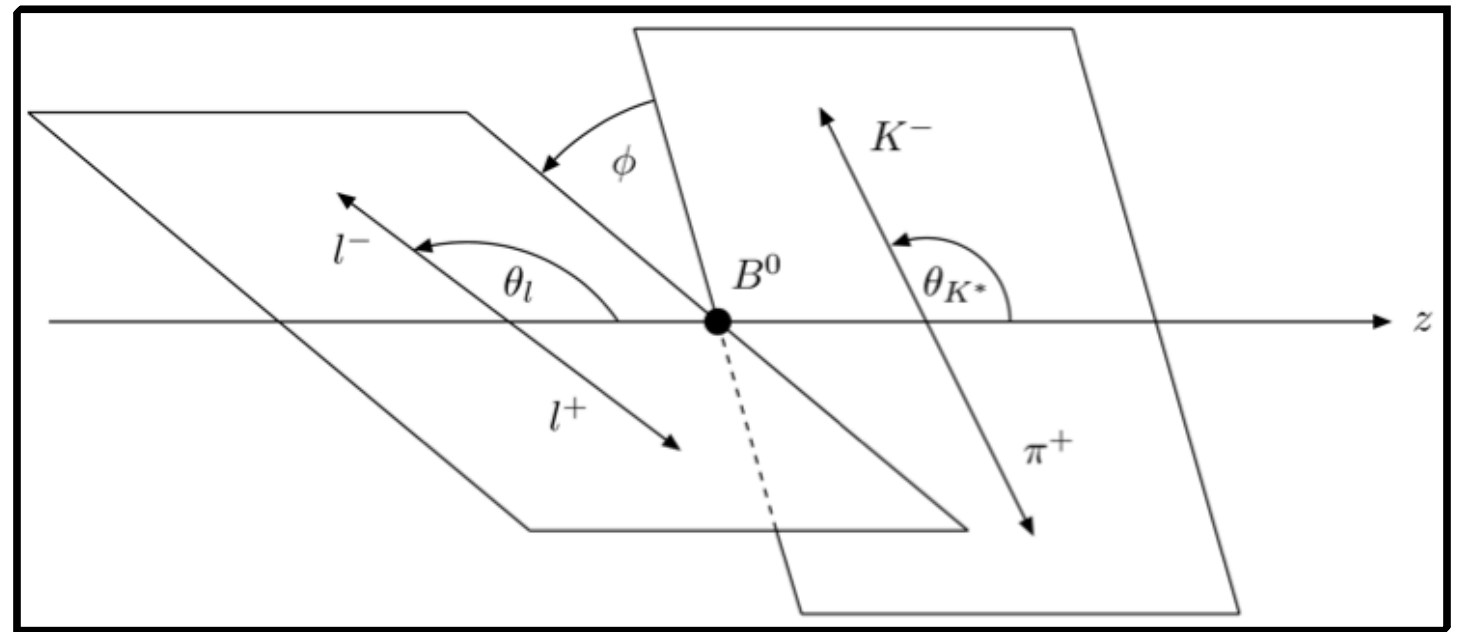
Angular Analysis

θ_K in K^* rest frame

θ_l in dilepton CM frame

ϕ boost-invariant w.r.t. z-axis

$q^2 \equiv$ invariant dilepton mass



$$\frac{d^{(4)}\Gamma}{dq^2 d(\cos \theta_l) d(\cos \theta_k) d\phi} = \frac{9}{32\pi}$$

$$\begin{aligned} & \times \left(I_1^s \sin^2 \theta_k + I_1^c \cos^2 \theta_k + (I_2^s \sin^2 \theta_k + I_2^c \cos^2 \theta_k) \cos 2\theta_l \right. \\ & + I_3 \sin^2 \theta_k \sin^2 \theta_l \cos 2\phi + I_4 \sin 2\theta_k \sin 2\theta_l \cos \phi \\ & + I_5 \sin 2\theta_k \sin \theta_l \cos \phi + (I_6^s \sin^2 \theta_k + I_6^c \cos^2 \theta_K) \cos \theta_l \\ & + I_7 \sin 2\theta_k \sin \theta_l \sin \phi + I_8 \sin 2\theta_k \sin 2\theta_l \sin \phi \\ & \left. + I_9 \sin^2 \theta_k \sin^2 \theta_l \sin 2\phi \right) \end{aligned}$$

$$S_i = \left(I_i^{(s,c)} + \bar{I}_i^{(s,c)} \right) / \Gamma'$$

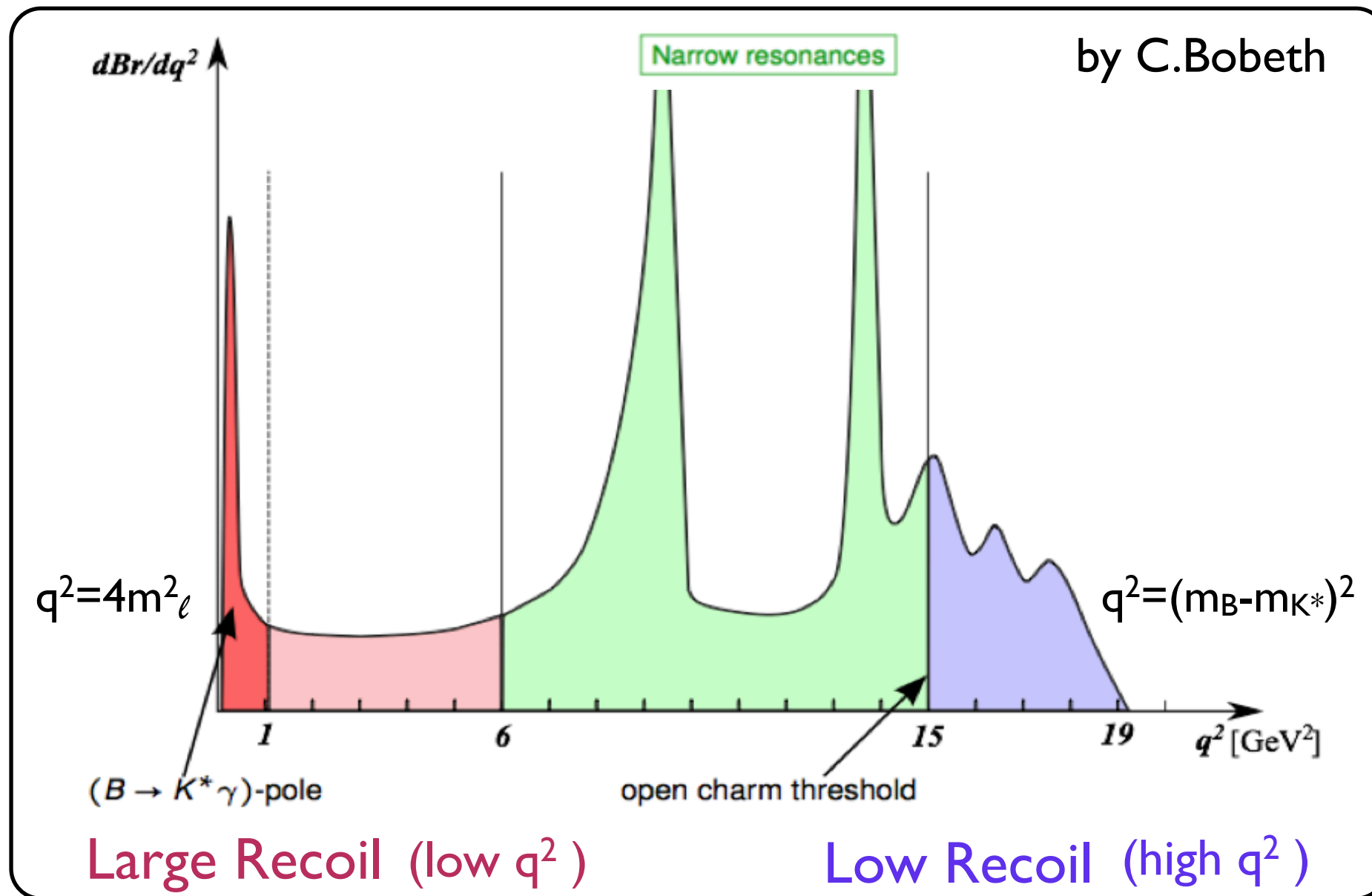
$$(2\Gamma' \equiv d\Gamma/dq^2 + d\bar{\Gamma}/dq^2)$$

8 CP-AVERAGED OBSERVABLES

$$F_L, A_{FB}, S_{3,4,5,7,8,9}$$

State-of-the art experimental cuts and event reconstruction allow an angular analysis in bins of q^2 : $\langle I_i^{(c,s)} \rangle = \int_{q_{min}^2}^{q_{max}^2} dq^2 I_i^{(c,s)}(q^2)$

3 distinct regions in the dilepton mass spectrum:



Experimental binning from latest data release, [LHCb-CONF-2015-002](#):

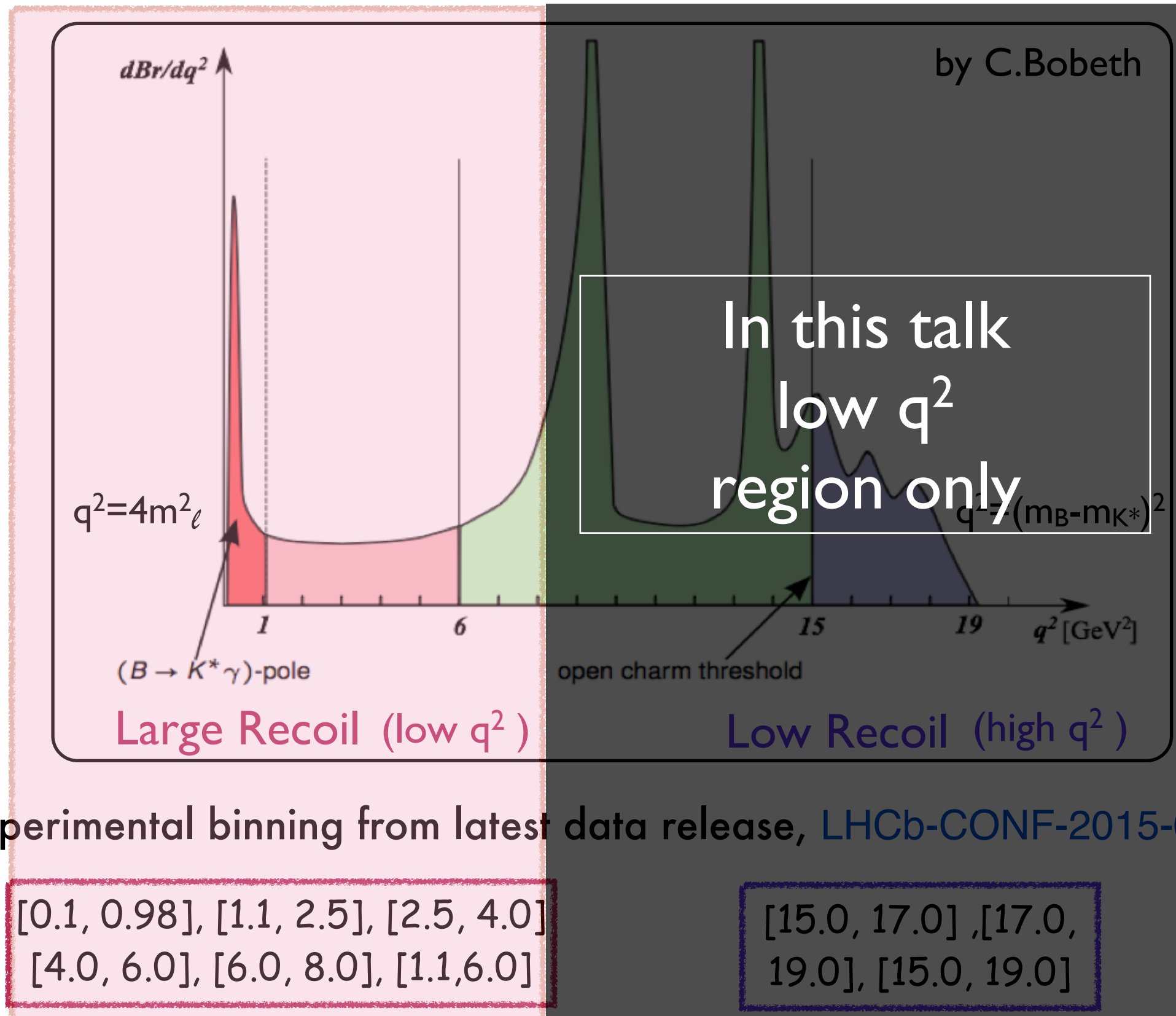
[0.1, 0.98], [1.1, 2.5], [2.5, 4.0]
[4.0, 6.0], [6.0, 8.0], [11.0, 16.0]

[15.0, 17.0], [17.0, 19.0], [15.0, 19.0]

[GeV^2]

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3 distinct regions in the dilepton mass spectrum:



The decay in the Standard Model

B to K* $\mu\mu$ decay belongs to $b \rightarrow s$ transitions

$$Q_1^{q=u,c} = (\bar{s}_L \gamma_\mu T^a q_L)(\bar{q}_L \gamma^\mu T^a b_L)$$

$$Q_2^{q=u,c} = (\bar{s}_L \gamma_\mu q_L)(\bar{q}_L \gamma^\mu b_L)$$

$$P_3 = (\bar{s}_L \gamma_\mu b_L) \sum_q (\bar{q} \gamma^\mu q)$$

$$P_4 = (\bar{s}_L \gamma_\mu T^a b_L) \sum_q (\bar{q} \gamma^\mu T^a q)$$

$$P_5 = (\bar{s}_L \gamma_{\mu 1} \gamma_{\mu 2} \gamma_{\mu 3} b_L) \sum_q (\bar{q} \gamma^{\mu 1} \gamma^{\mu 2} \gamma^{\mu 3} q)$$

$$P_6 = (\bar{s}_L \gamma_{\mu 1} \gamma_{\mu 2} \gamma_{\mu 3} T^a b_L) \sum_q (\bar{q} \gamma^{\mu 1} \gamma^{\mu 2} \gamma^{\mu 3} T^a q)$$

$$Q_{8g} = \frac{g_s}{16\pi^2} m_b \bar{s} \sigma_{\mu\nu} P_R G^{\mu\nu} b$$

$$Q_{7\gamma} = \frac{e}{16\pi^2} m_b \bar{s} \sigma_{\mu\nu} P_R F^{\mu\nu} b$$

$$Q_{9V} = \frac{\alpha_{em}}{4\pi} (\bar{s} \gamma_\mu P_L b)(\bar{\ell} \gamma^\mu \ell)$$

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$$\mathcal{H}_{\text{eff}}^{\Delta B=1} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$$

@ dimension 6, 10 operators

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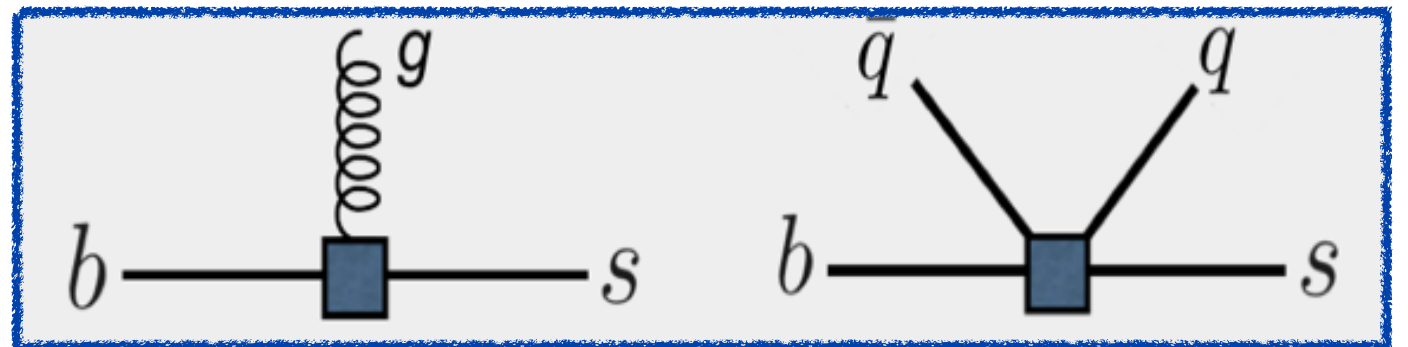
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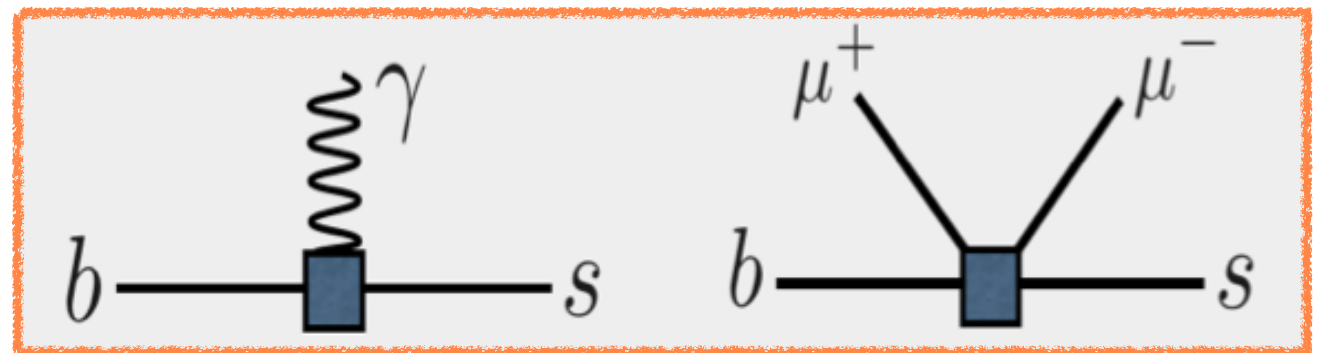
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@ dimension 6, 10 operators

$$\mathcal{H}_{\text{eff}}^{\Delta B=1} \sim \sum_i C_i \mathcal{O}_i$$

Short-distance physics:

- 2-loop QCD matching
- 3-loop 10 x 10 ADM

Running from m_W down to m_b :

$$C_1 = -0.26, \quad C_2 = 1.01, \quad C_7 = -0.3$$

$$C_8 = -0.17, \quad C_9 = 4.21, \quad C_{10} = -4.1$$

and all the rest < 0.01 .

In the SM, $\langle M \ell \ell | \mathcal{H}_{\text{eff}}^{\text{sl}} | \bar{B} \rangle$ corresponds to the following helicity amplitudes:

$$\begin{aligned} H_V(\lambda) &\propto C_9 \tilde{V}_{L\lambda} + \frac{2m_b m_B}{q^2} C_7 \tilde{T}_{L\lambda} \\ H_A(\lambda) &\propto C_{10} \tilde{V}_{L\lambda} \quad (\lambda = 0, \pm) \\ H_P &\propto \frac{2m_l m_B}{q^2} C_{10} \left(1 + \frac{m_s}{m_B} \right) \tilde{S} \end{aligned}$$

The angular coefficients $I^{(c,s)}$ are functions of these amplitudes, as well as the CP averaged observables we are ultimately interested in.

For example,

$$\begin{aligned} I_1^c &= F \left(\frac{1}{2} (|H_V^0|^2 + |H_A^0|^2) + |H_P^0|^2 + \frac{2m_l^2}{q^2} (|H_V^0|^2 - |H_A^0|^2) \right), \\ I_1^s &= F \left(\frac{\beta^2 + 2}{8} (|H_V^+|^2 + |H_V^-|^2 + |H_A^+|^2 + |H_A^-|^2) + \frac{m_l^2}{q^2} (|H_V^+|^2 - |H_V^-|^2 - |H_A^+|^2 + |H_A^-|^2) \right) \end{aligned}$$

where:

$$\begin{aligned} F &= \frac{\lambda^{1/2} \beta q^2}{3 \times 2^5 \pi^3 m_B^3} \text{BR}(K^* \rightarrow K\pi), \quad \beta = \sqrt{1 - \frac{4m_l^2}{q^2}}, \\ \lambda &= m_B^4 + m_{K^*}^4 + q^4 - 2(m_B^2 m_{K^*}^2 + m_B^2 q^2 + m_{K^*}^2 q^2). \end{aligned}$$

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➔ 7 q^2 -dependent form factors to be computed

At low q^2 , most recent determination in **Bharucha, Straub, Zwicky (1503.05534)**, through QCD Sum Rules on the Light-Cone (LCSR).

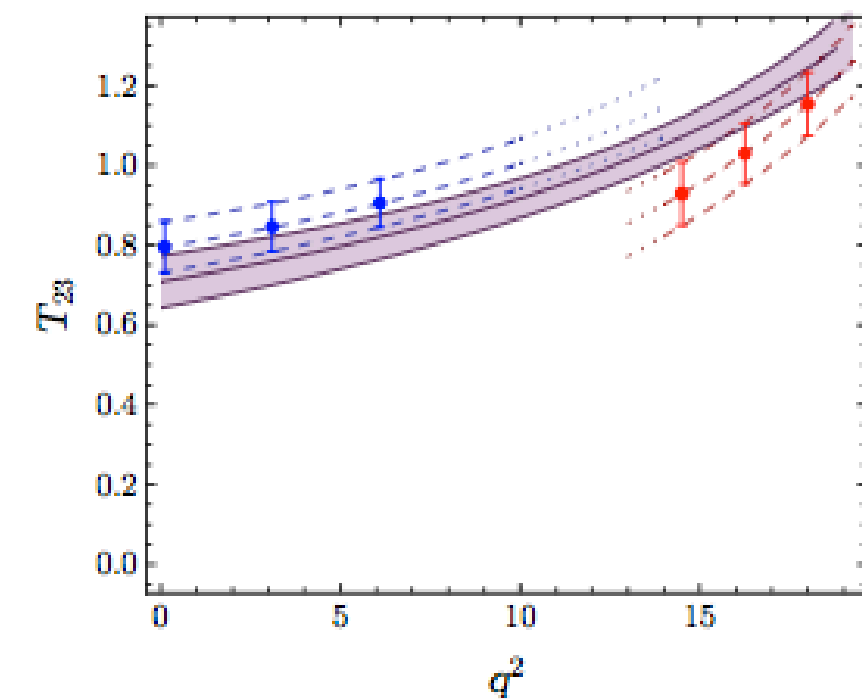
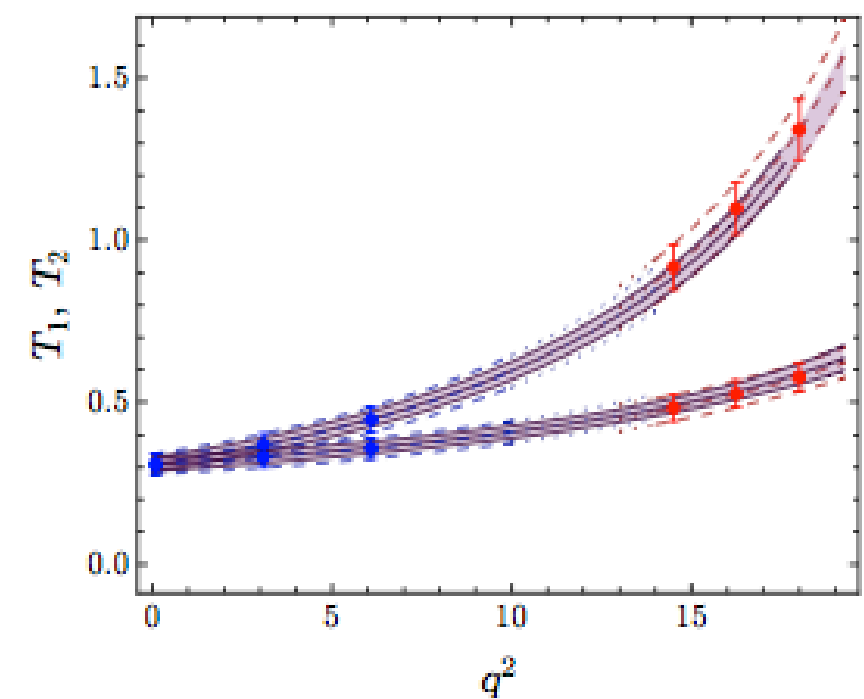
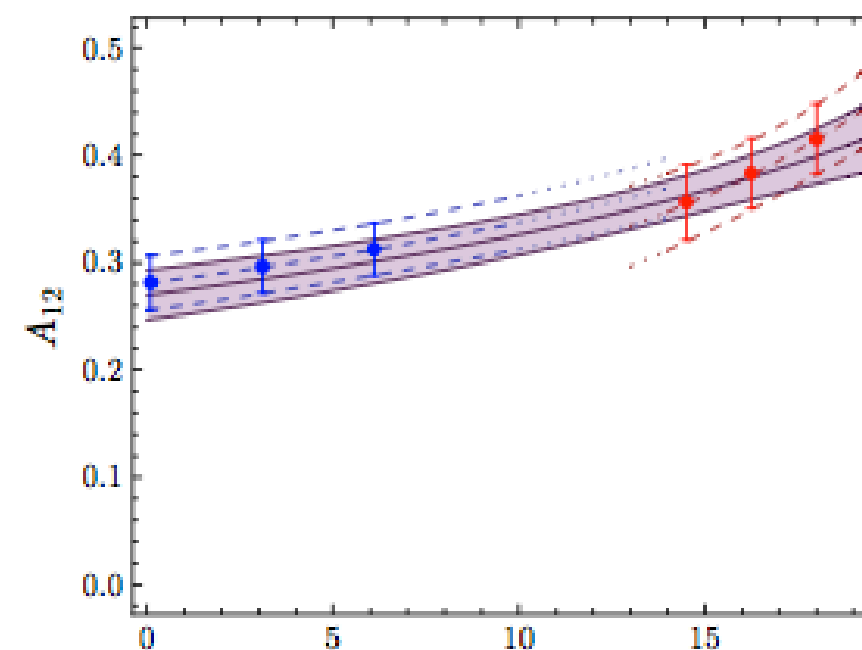
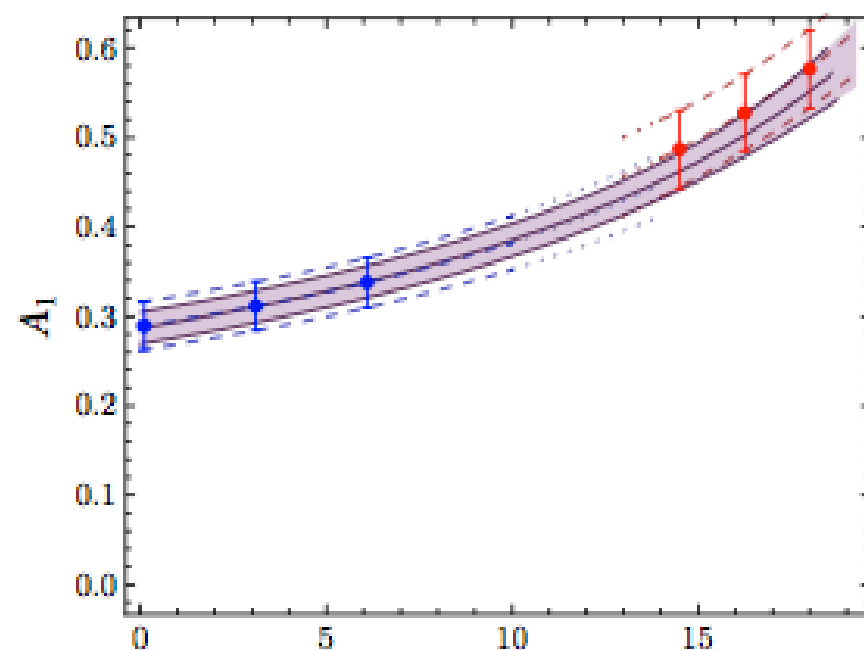
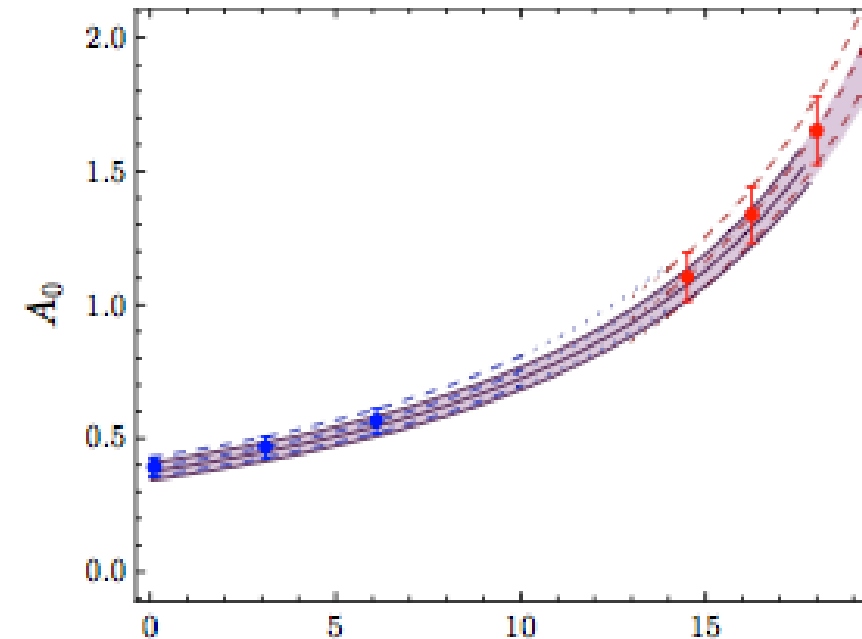
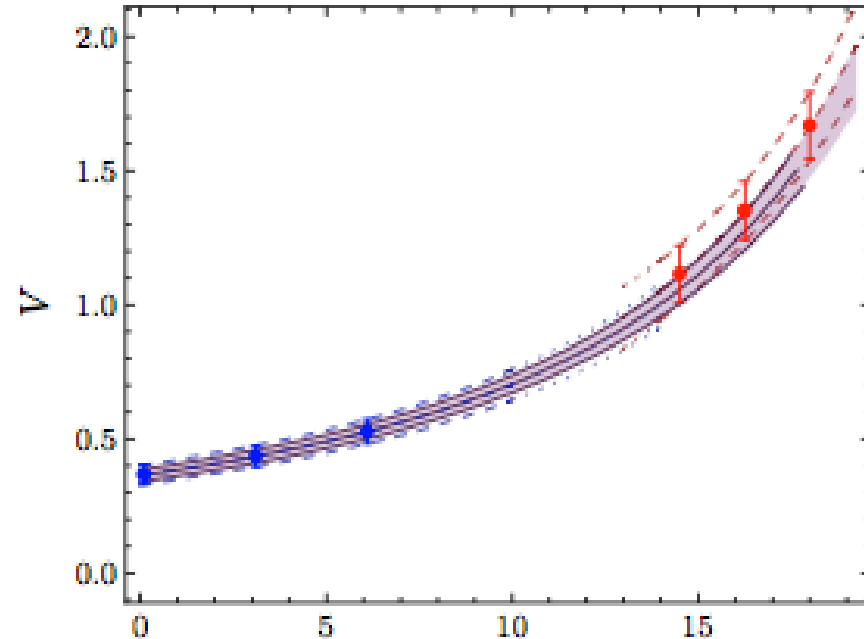
$$F^{(i)}(q^2) = \sum_k \alpha_k^{(i)} \frac{[z(q^2) - z(0)]^k}{1 - \left(q/m_R^{(i)}\right)^2} \quad \left| \quad \begin{aligned} z(t) &= \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}} \\ \text{where } t_{\pm} &= (m_B \pm m_{K^*})^2 \text{ and} \\ t_0 &= t_+(1 - \sqrt{1 - t_-/t_+}). \end{aligned} \right.$$

given up to $k=2$

Low recoil
region
1501.00367

Lattice
VS
LCSR

1503.05534
Large recoil
region



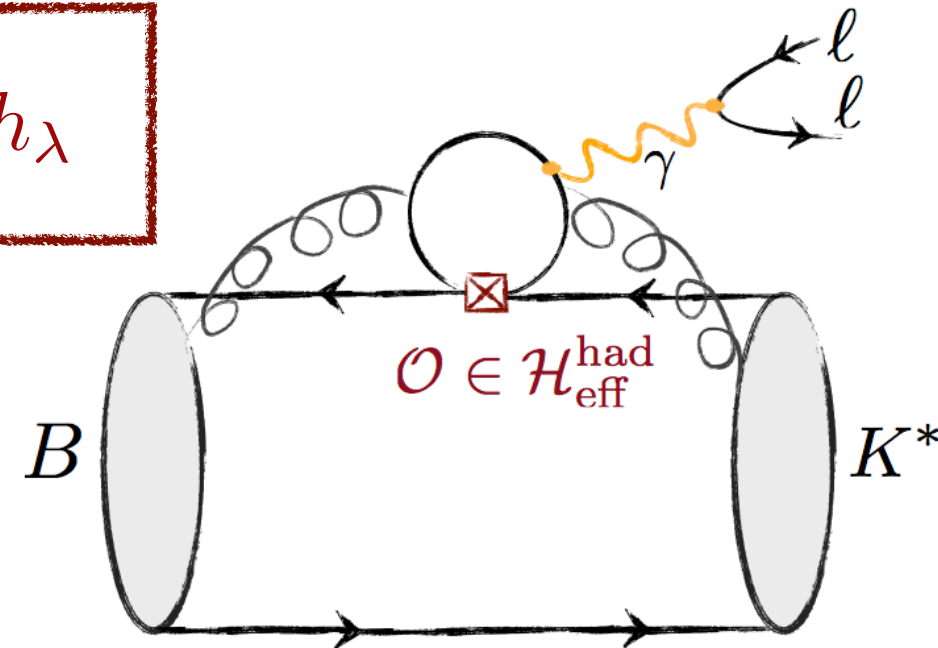
What about the hadronic part of the effective Hamiltonian?

It can contribute to $H_V(\lambda)$ through the insertion of E.M. currents!

$$H_V(\lambda) \propto C_9 \tilde{V}_{L\lambda} + \frac{2m_b m_B}{q^2} C_7 \tilde{T}_{L\lambda} - \frac{16\pi^2 m_B^2}{q^2} h_\lambda$$

where the above hadronic contribution reads:

$$h_\lambda(q^2) = \frac{\epsilon_\mu^*(\lambda)}{m_B^2} \int d^4x e^{iqx} \langle \bar{K}^* | T \{ j_{\text{em}}^\mu(x) \mathcal{H}_{\text{eff}}^{\text{had}}(0) \} | \bar{B} \rangle$$



This correlator is the weakest part of the theoretical prediction.

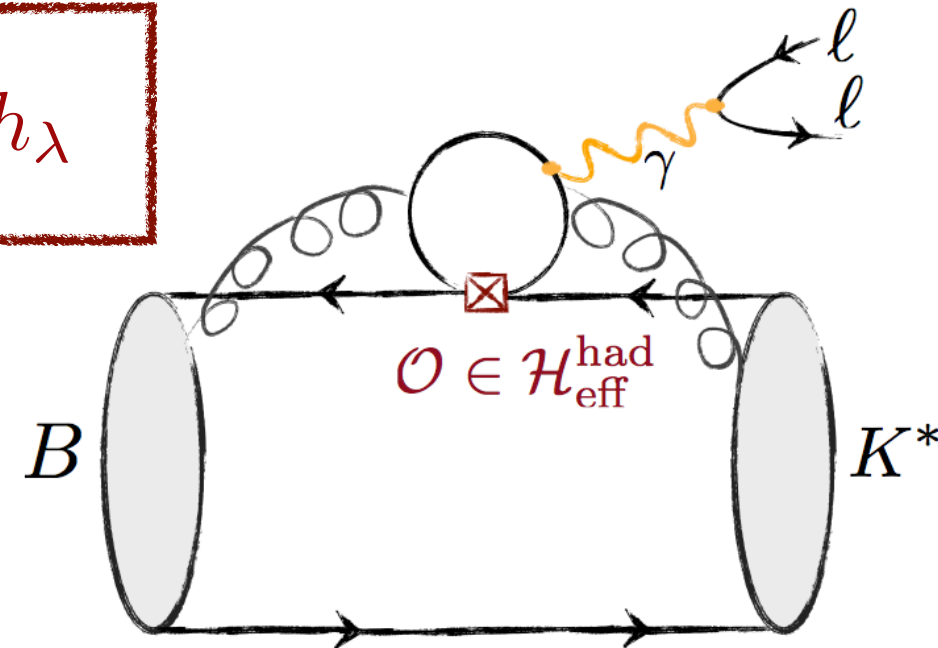
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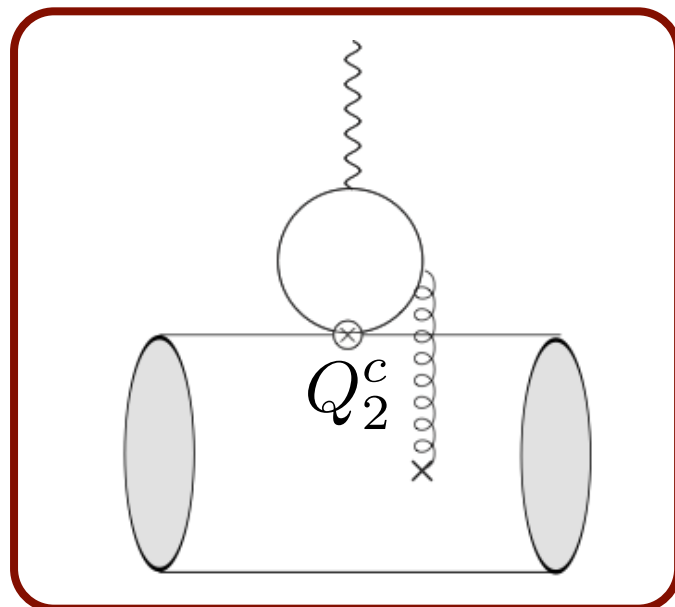
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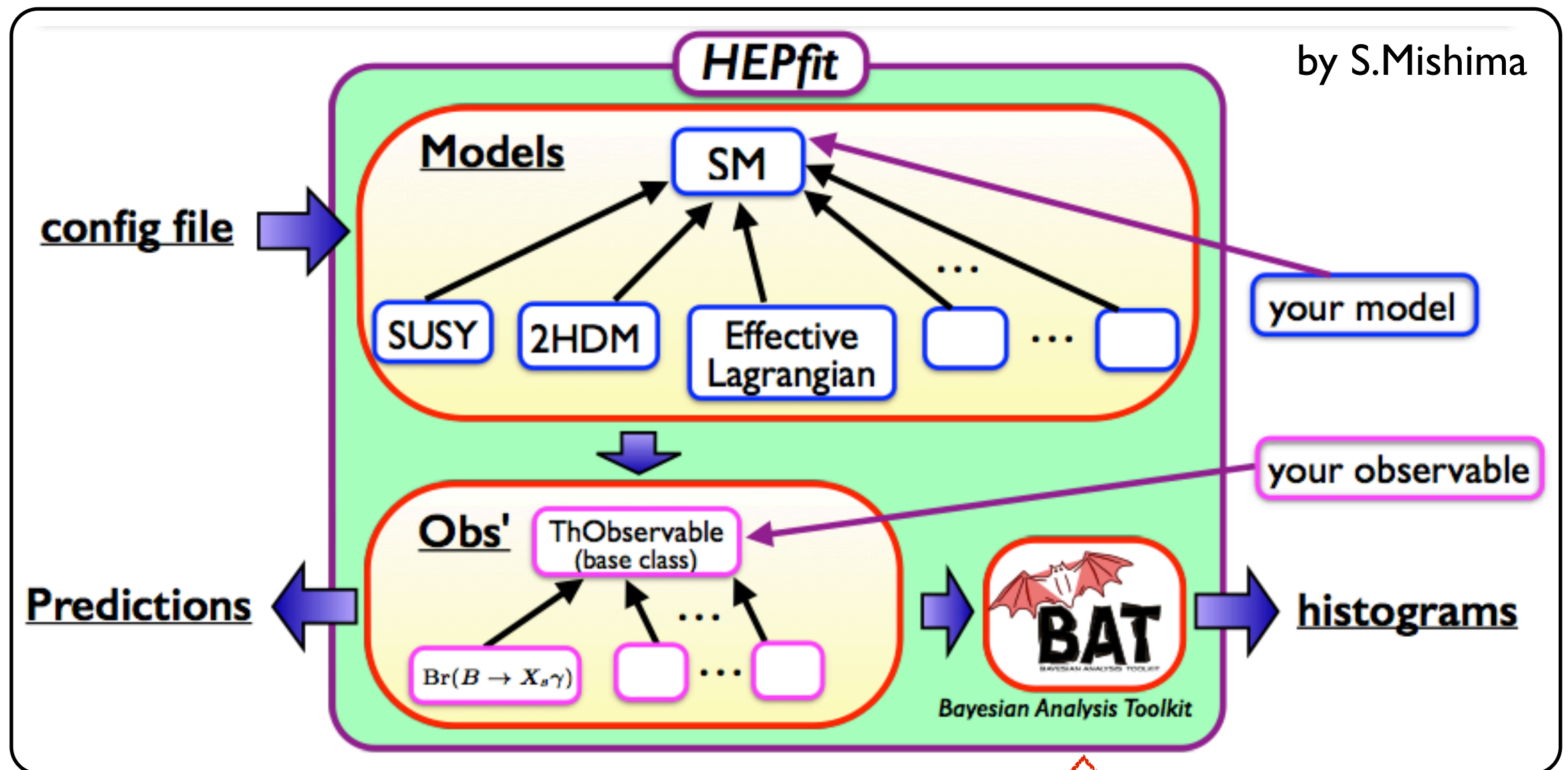
A big effort has been done by Khodjamirian et al., 1006.4945, where the charm-loop + single soft gluon emission was computed.



DRAWBACKS:

- still partial estimate of the effect, valid for $q^2 \lesssim 1 \text{ GeV}^2$ only
- multiple soft gluon emission suppressed as far as $q^2 \ll 4 m_c^2$

HEPfit: Our weapon of choice

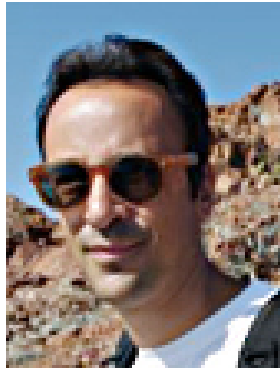


Full-fledged statistical data analysis **in this work** carried out by means of Bayes Theorem

$$\mathcal{P}(\lambda | \mathcal{D}) \propto \mathcal{P}(\mathcal{D} | \lambda) \mathcal{P}_o(\lambda)$$

λ posterior likelihood λ prior

the HEPfit group:
@present



L.Silvestrini



M.Ciuchini



S.Mishima



E.Franco



L.Reina



M.Pierini

+ 7 postdocs

+ 4 PhD students

HEPfit is a framework for calculating observables (Flavour, EWPT, Higgs) in the SM and Beyond, constraining the parameter space with a global fit

It is a **public code** written in C++ with MPI parallelization, with GSL, Boost, ROOT and BayesPy analysis toolkit (BAT) dependencies.

HEPfit will be officially released with a user friendly cross-platform CMake + a detailed documentation of the code (technical paper + Doxygen!)

First official release soon!

Developer version already available @ <https://github.com/silvest/HEPfit>

Do not miss tomorrow's talk of A. Paul!

Our Analysis in the low q^2 region

MAIN THEORY INPUT:

For the form factors, LCSR state-of-the-art estimate in **1503.05534**:

parameters: $3 \times 7 - 2 = 19$ (with 19×19 correlation matrix)

Following [Jager & Camalich'14, 1412.3183](#), we parametrized the non-factorizable hadronic contribution as:

$$h_\lambda(q^2) = h_\lambda^{(0)} + h_\lambda^{(1)} q^2 + \underline{h_\lambda^{(2)} q^4}, \quad (\lambda = 0, \pm)$$

TO PROVIDE A MORE RELIABLE DESCRIPTION ABOVE FEW GeV^2

parameters: $3 \times 3 \times 2 = 18$

to which we assigned a generous prior (all flatly distributed in $\pm 2 \times 10^{-4}$).

EXPERIMENTAL INFO EXPLOITED:

$$F_L, A_{FB}, S_{3,4,5,7,8,9}$$

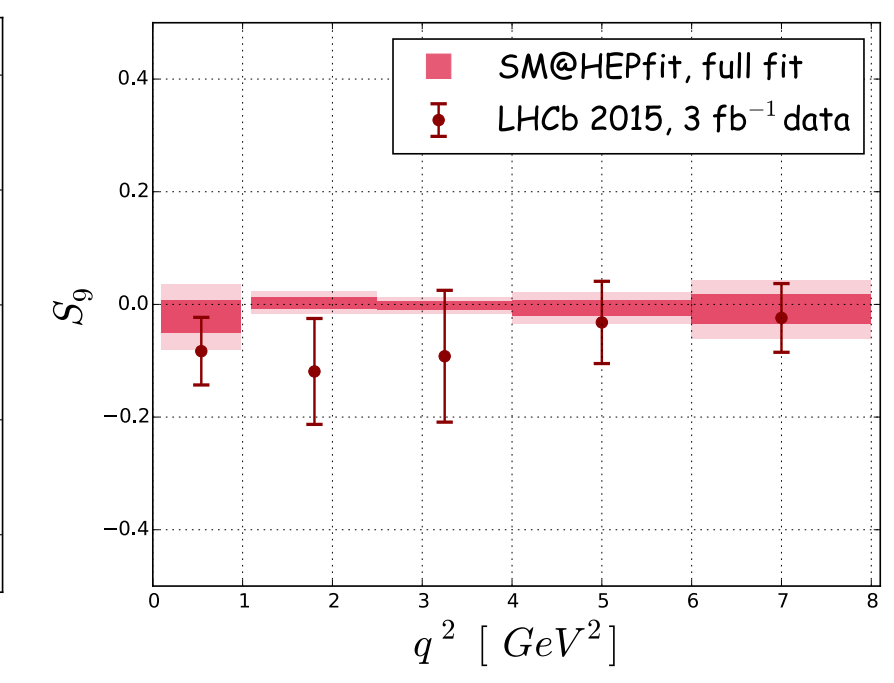
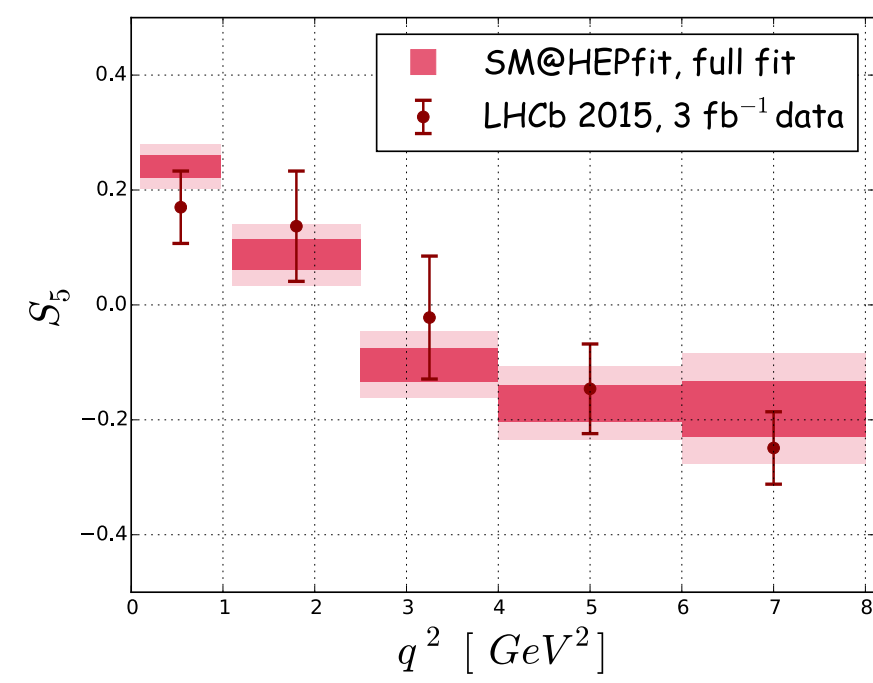
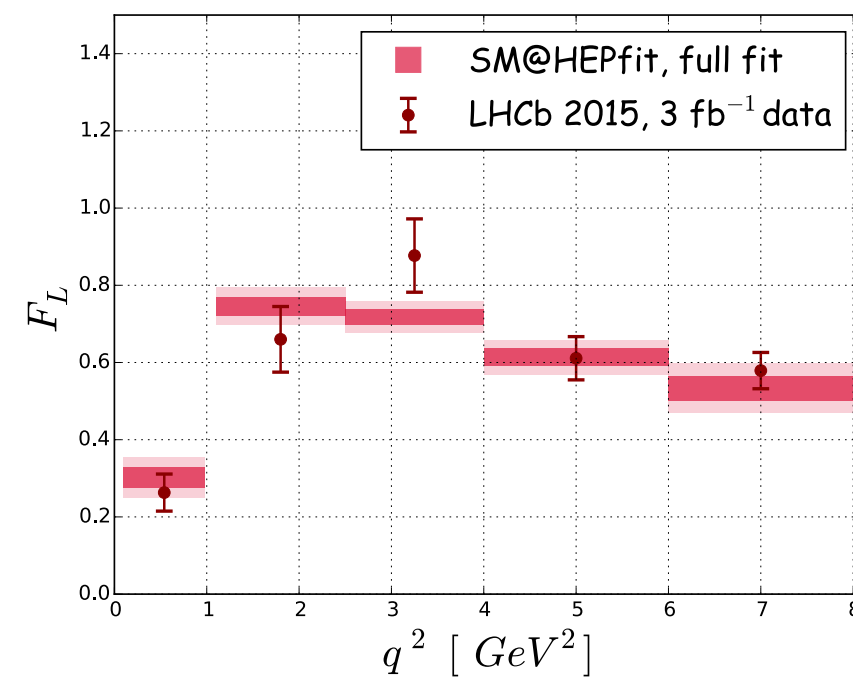
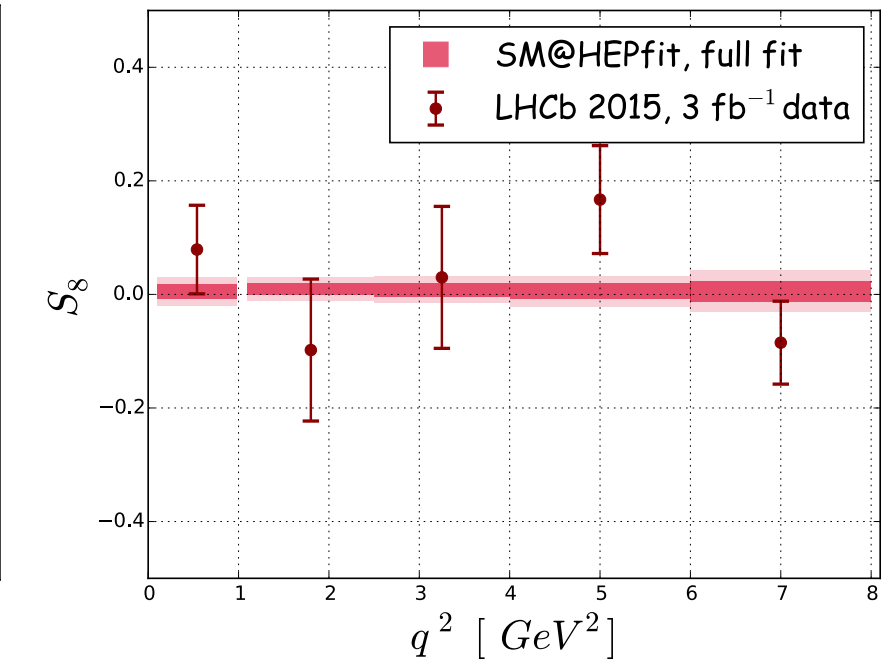
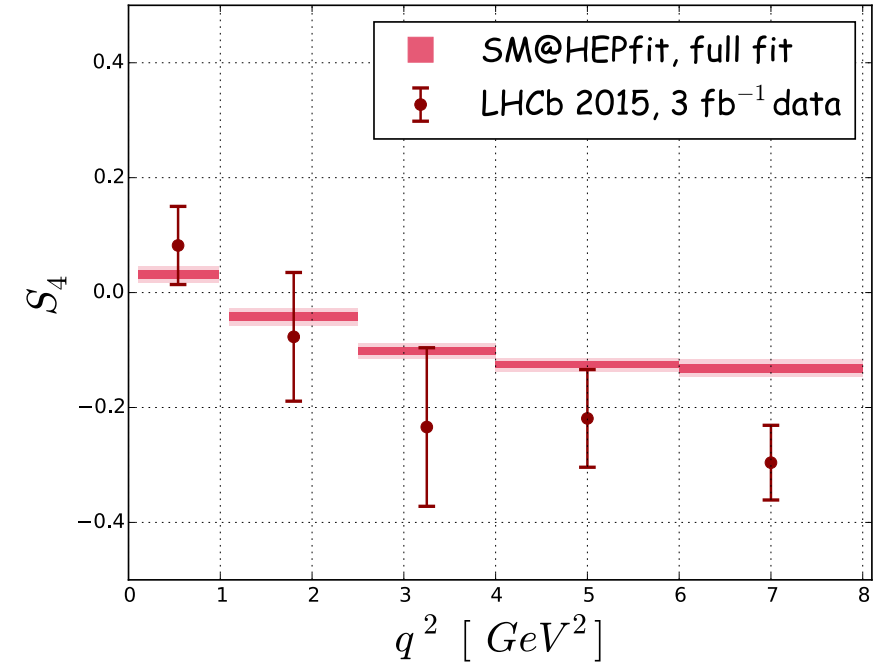
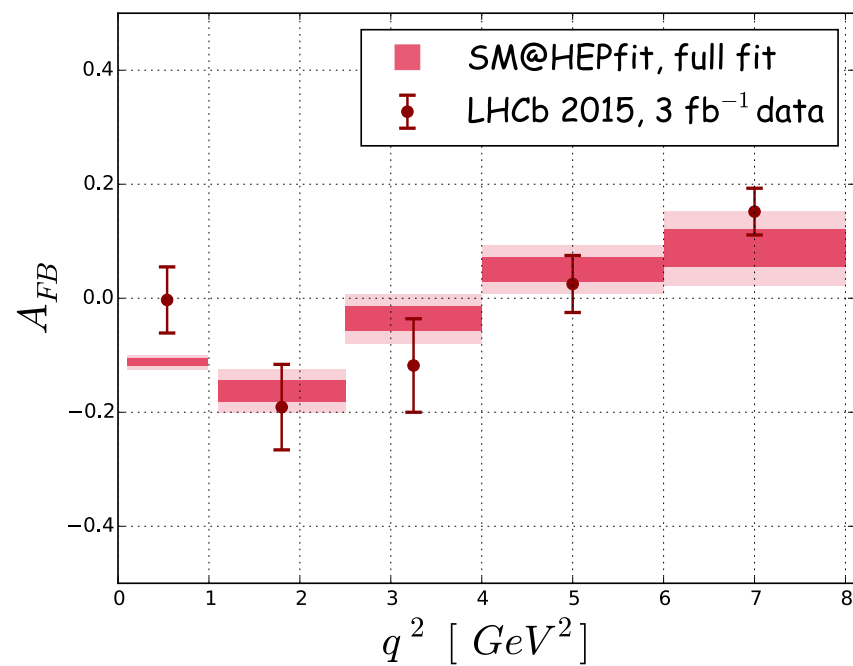
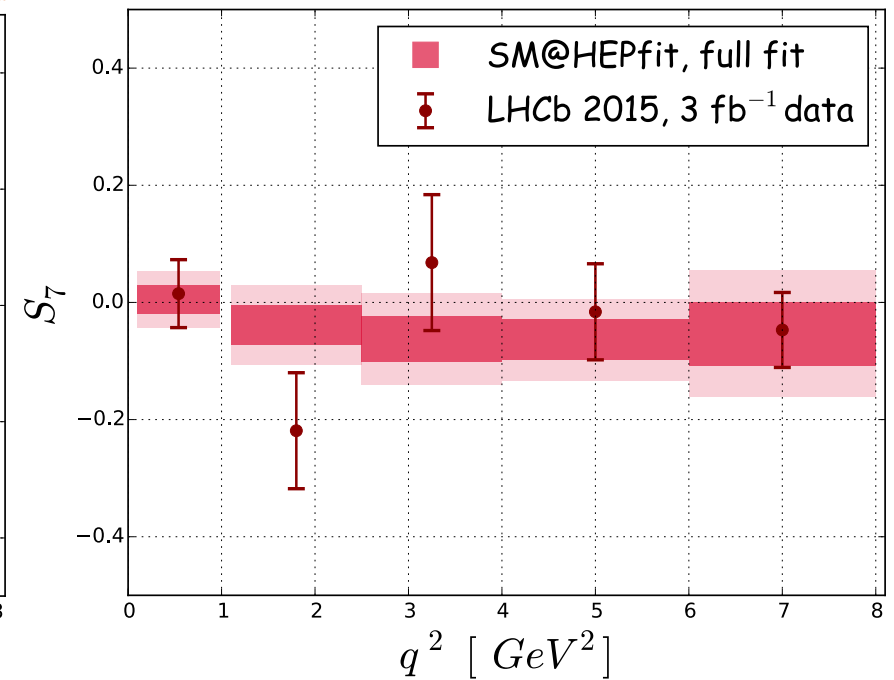
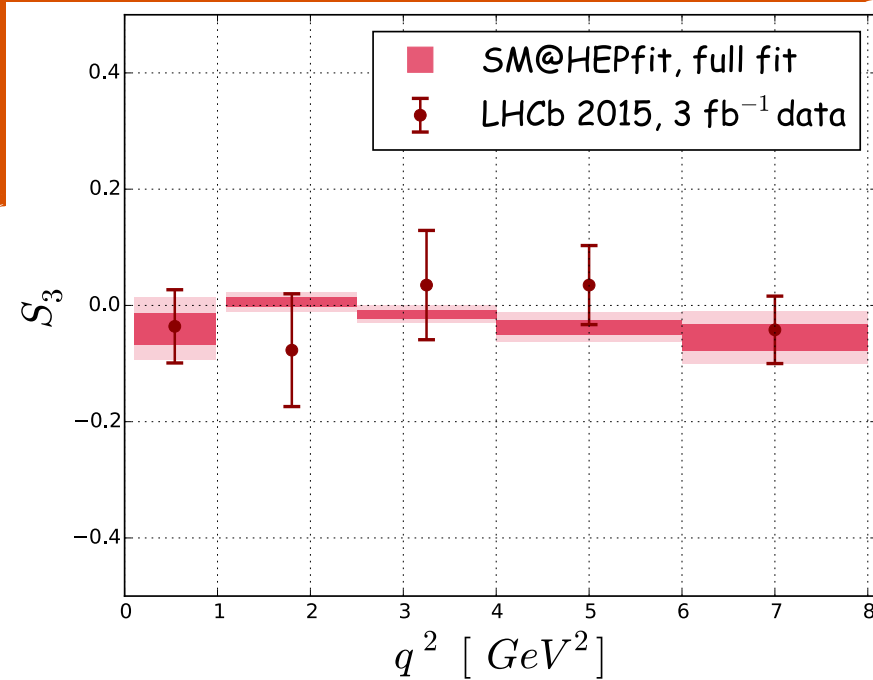
[LHCb-CONF-2015-002](#)

$8 \times 6 = 48$ (with 8×8 correlation matrix per bin)

$$\mathcal{B}(B \rightarrow K^* \mu \mu) \quad 1 \times 4 \rightarrow 52 \quad , \quad \mathcal{B}(B \rightarrow K^* \gamma) \rightarrow 53$$

HEPfit

full fit



Switching off one observable per time, one can fit again and look @

The PULL of the FIT

$$\frac{\mathcal{O}_{th} - \mathcal{O}_{exp}}{\sqrt{\sigma_{th}^2 + \sigma_{exp}^2}}$$

Bin q^2 [GeV^2/c^4]	A_{FB}	F_L	S_3	S_4	S_5	S_7	S_8	S_9
[0.1, 0.98]	1.9	-0.9	0.0	0.7	-1.2	0.1	0.9	-1.2
[1.1, 2.5]	-0.6	-0.9	-0.8	-0.3	0.7	-2.0	-0.8	-1.3
[2.5, 4]	-1.3	1.8	0.6	-1.0	0.7	0.5	0.2	-0.8
[4, 6]	-0.6	0.5	1.1	-1.1	-0.4	-0.1	1.7	-0.5
[6, 8]	0.7	1.4	0.3	-2.5	-1.5	-0.3	-1.2	0.4
[1.1, 6]	-1.3	0.6	0.9	-1.0	0.4	-0.8	0.5	-0.7

No statistically significant deviation from the angular observables.

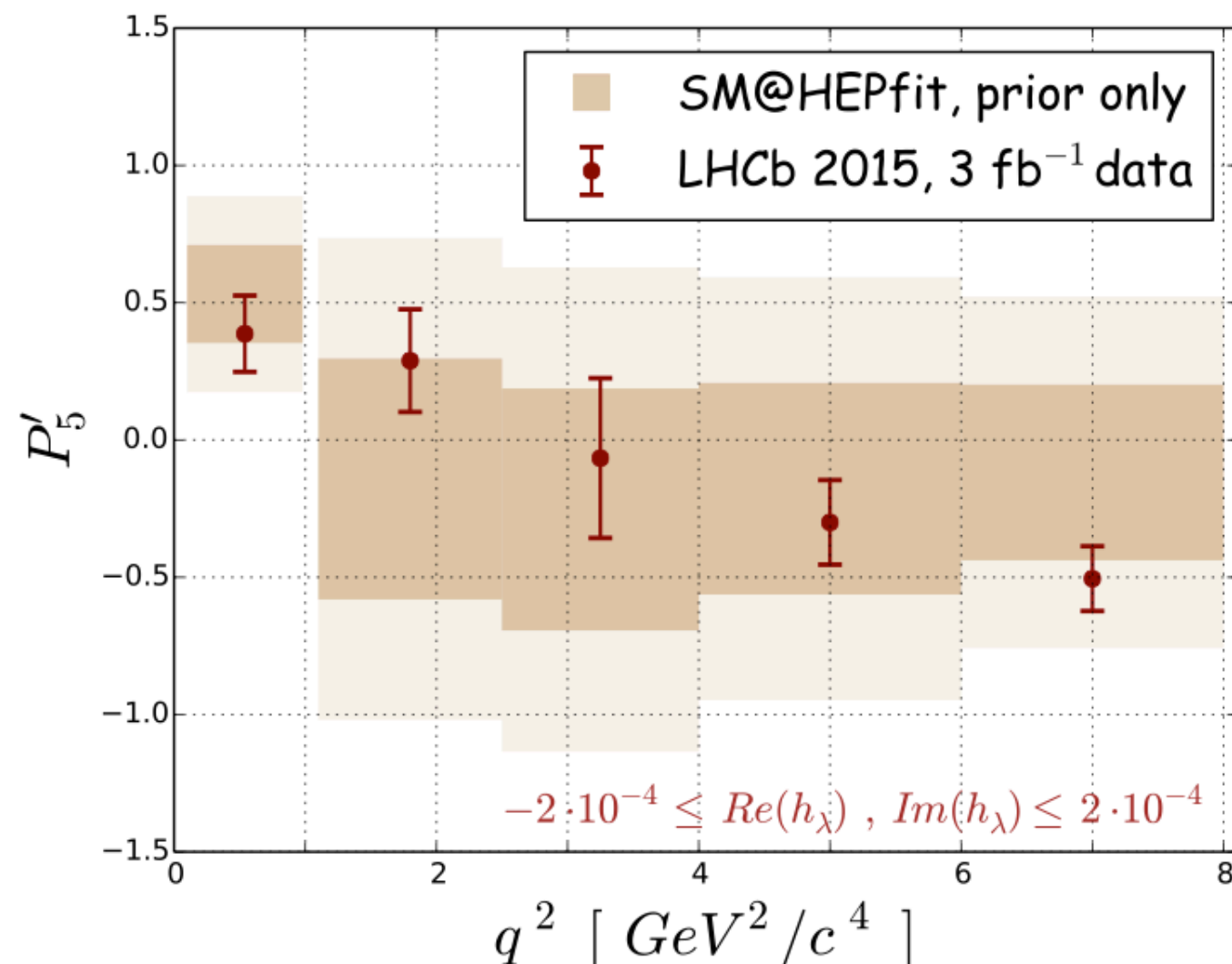
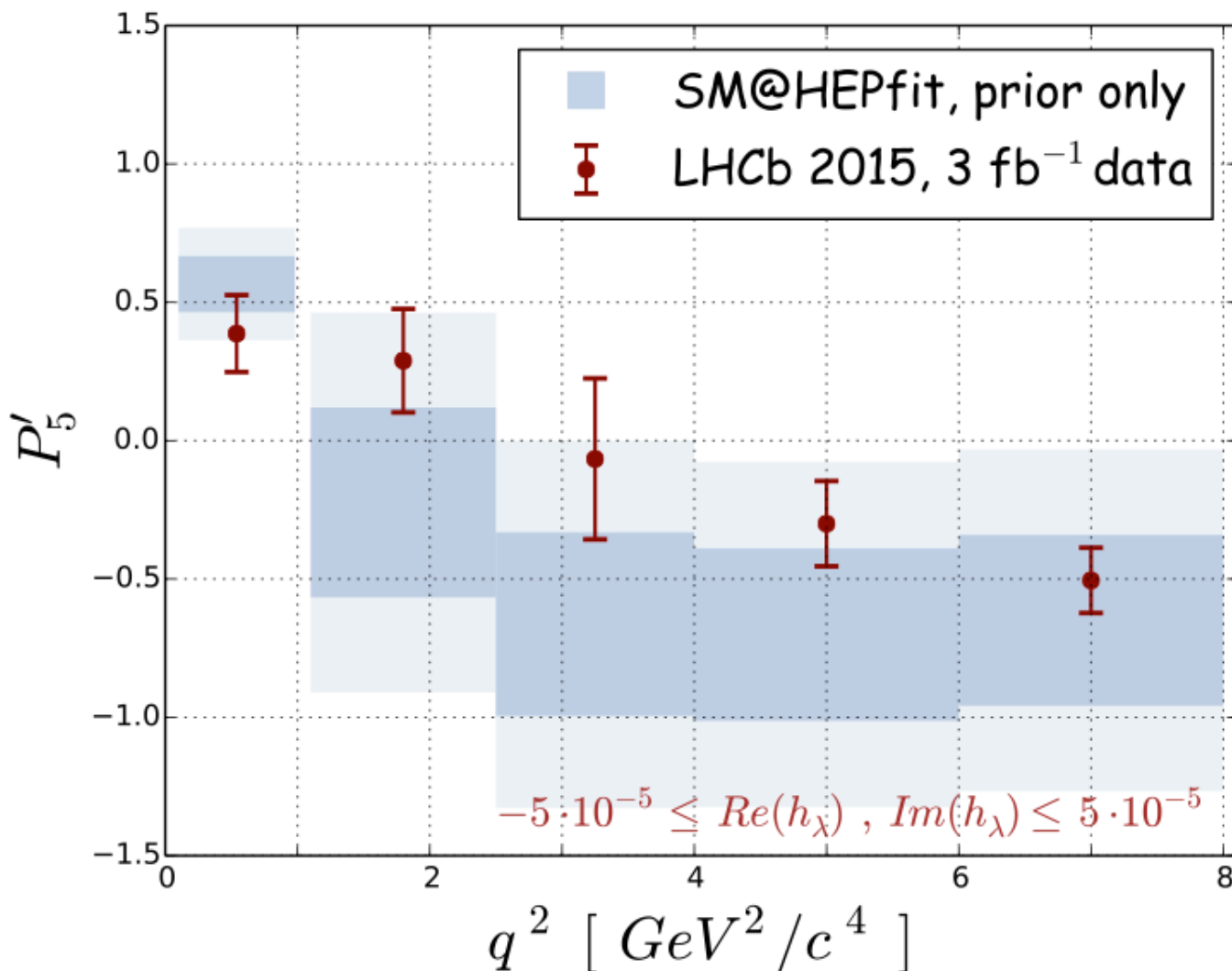
(the result concerning the branching ratios is good as well)

Cleaness of the “clean” P'_5

Some peculiar ratios of observables have been proposed with the aim of exploiting possible form factor/hadronic uncertainty cancellations.
(see Descotes-Genon et al.'13 and ref. therein)

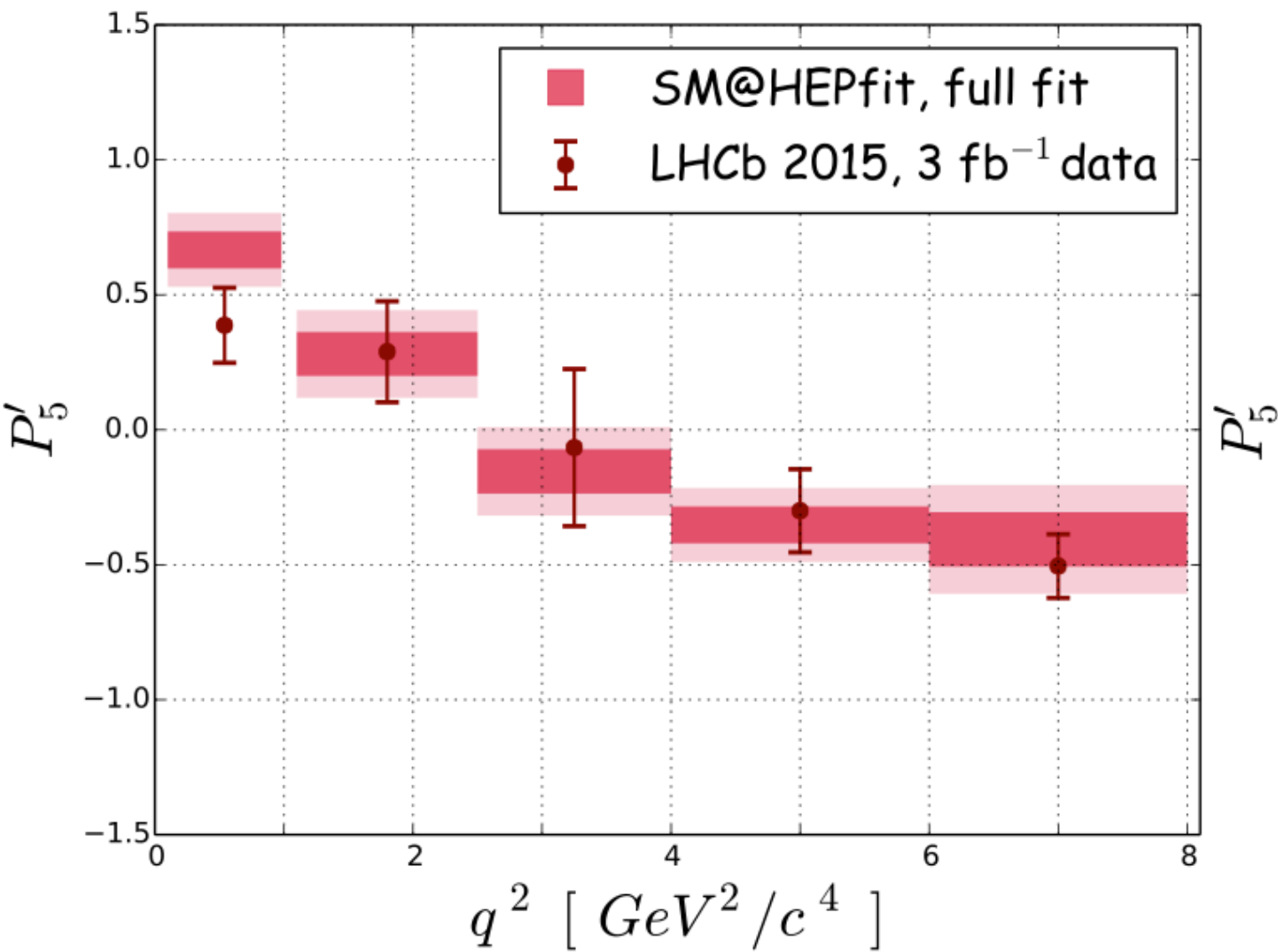
One example on top of some others:

$$P'_5 \equiv \frac{S_5}{\sqrt{F_L(1 - F_L)}} \quad (q^2 \gtrsim m_\mu^2)$$

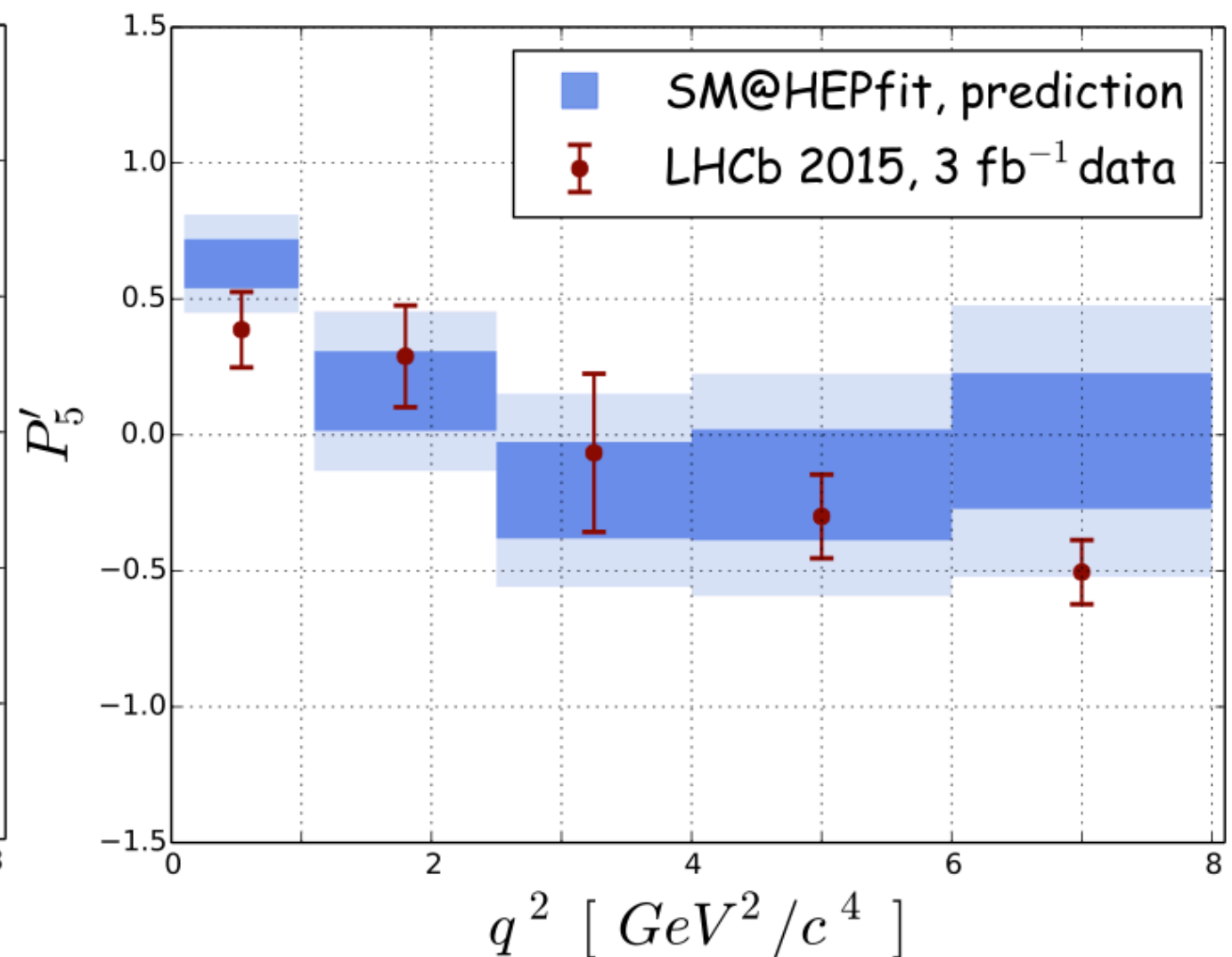


Our data-blind analysis with large hadronic contributions clearly shows a large shift in both the central values + inflation of errors!

Fit & Prediction of P'_5

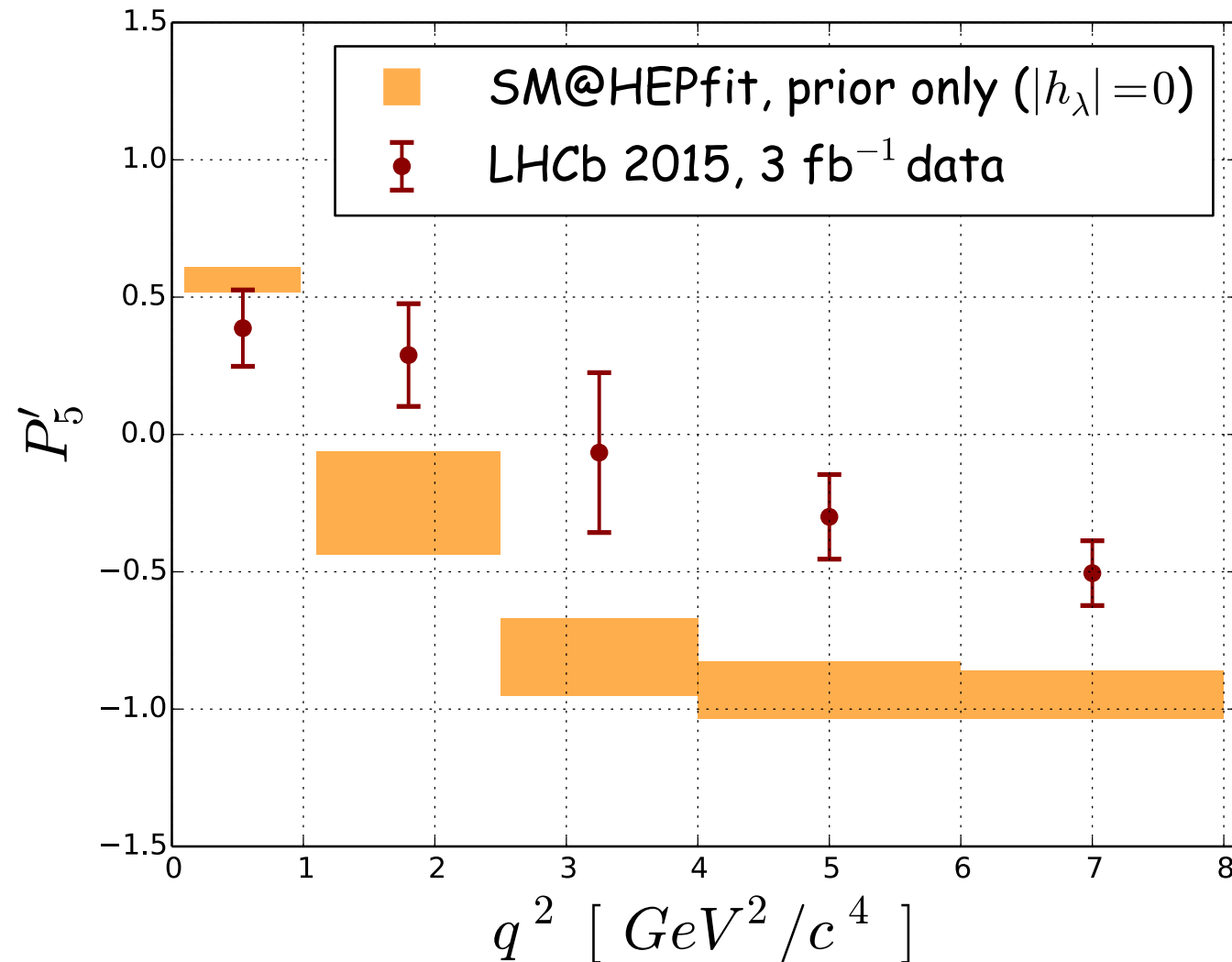


(computed from the helicity amplitudes,
i.e. not from fit result of S_5 and F_L)



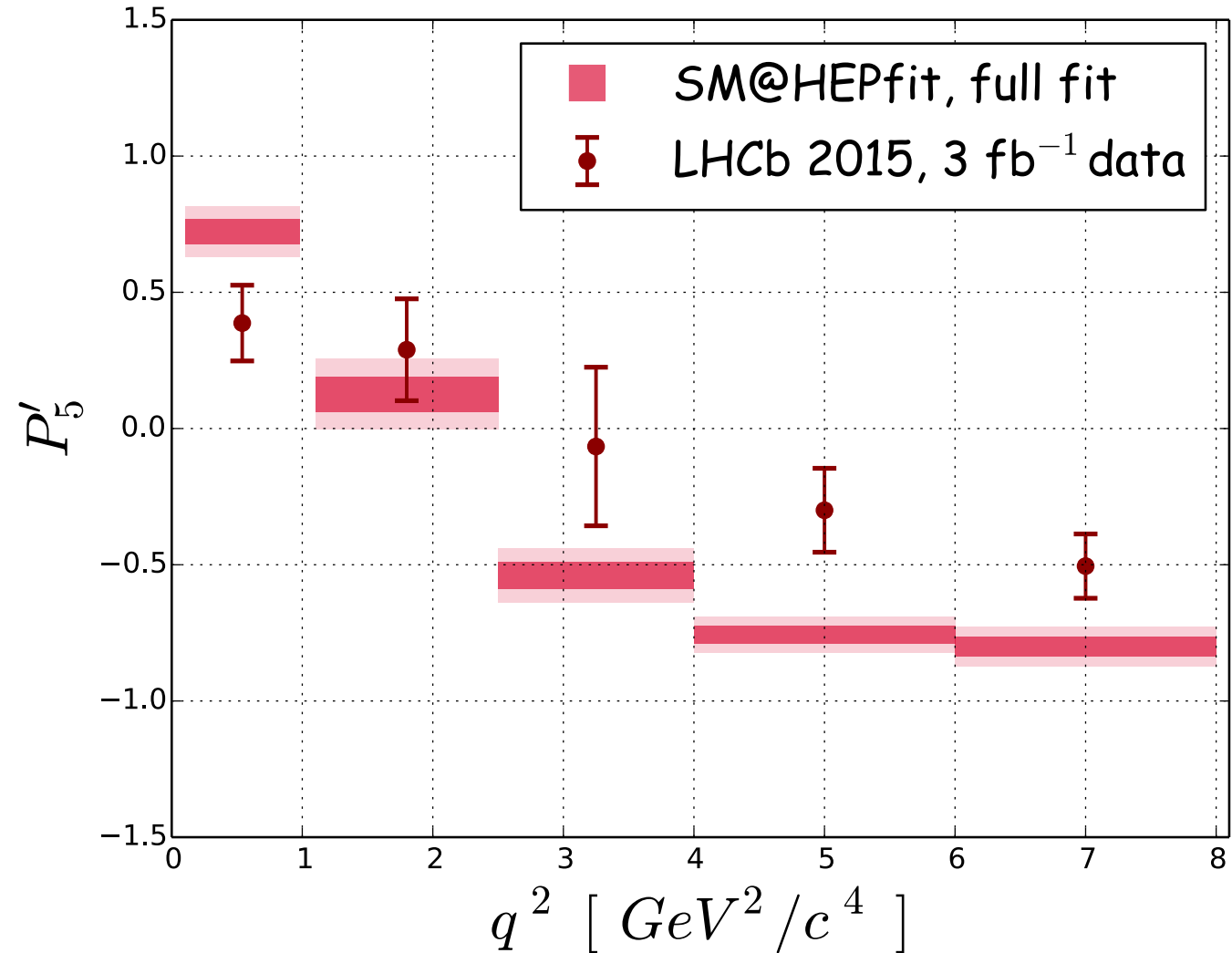
(switching off S_5 and F_L together)

How to get the Anomaly



Data-blind estimation.
No "charm-loop effect".

(1 sigma band here entirely due to
LCSR form factors uncertainties)



Fit with Khodjamirian et al.
estimate imposed in the whole
 q^2 range [0.98,8] GeV².

Face to face with hadronic contributions

One can easily read the size of the hadronic contribution h_λ as a shift in C_9 .

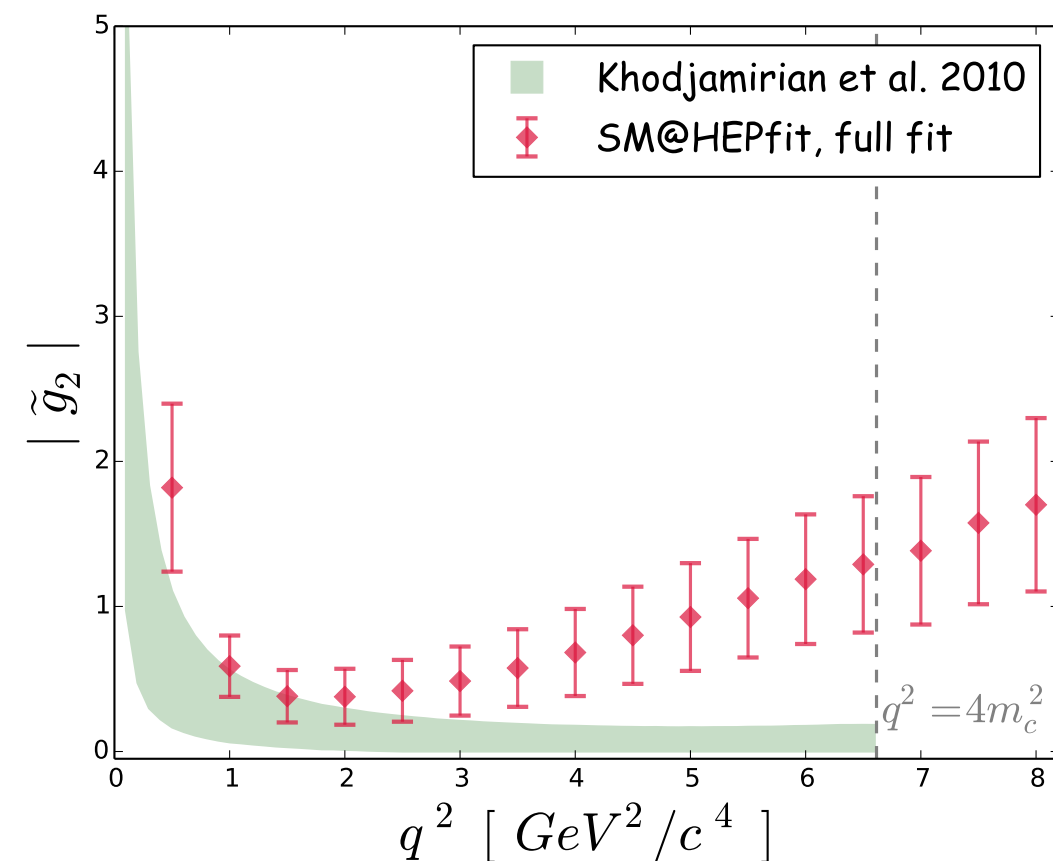
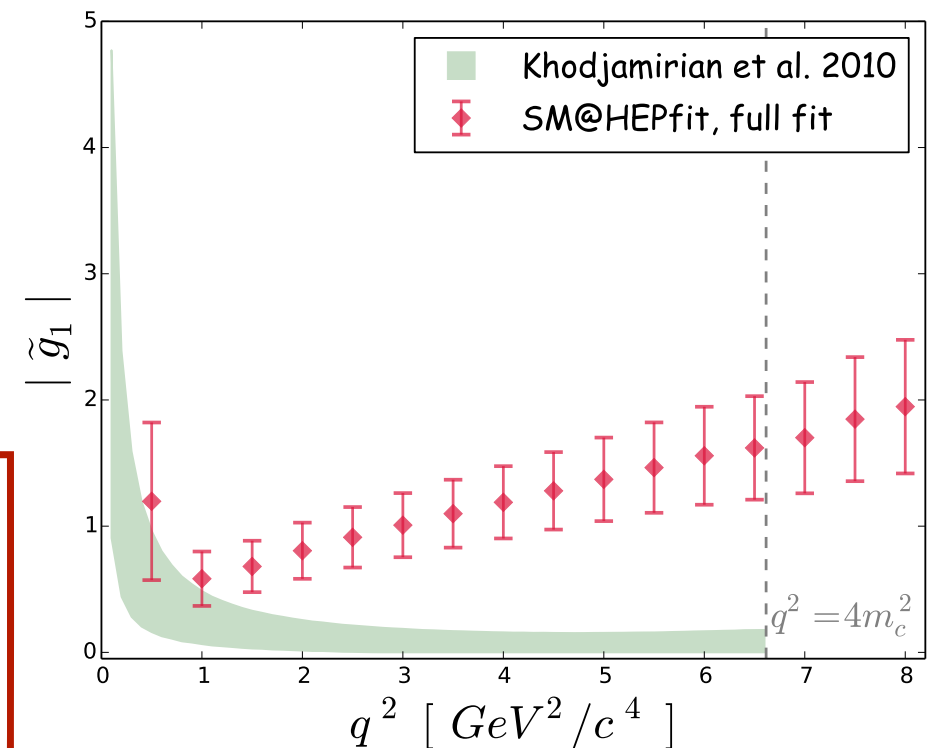
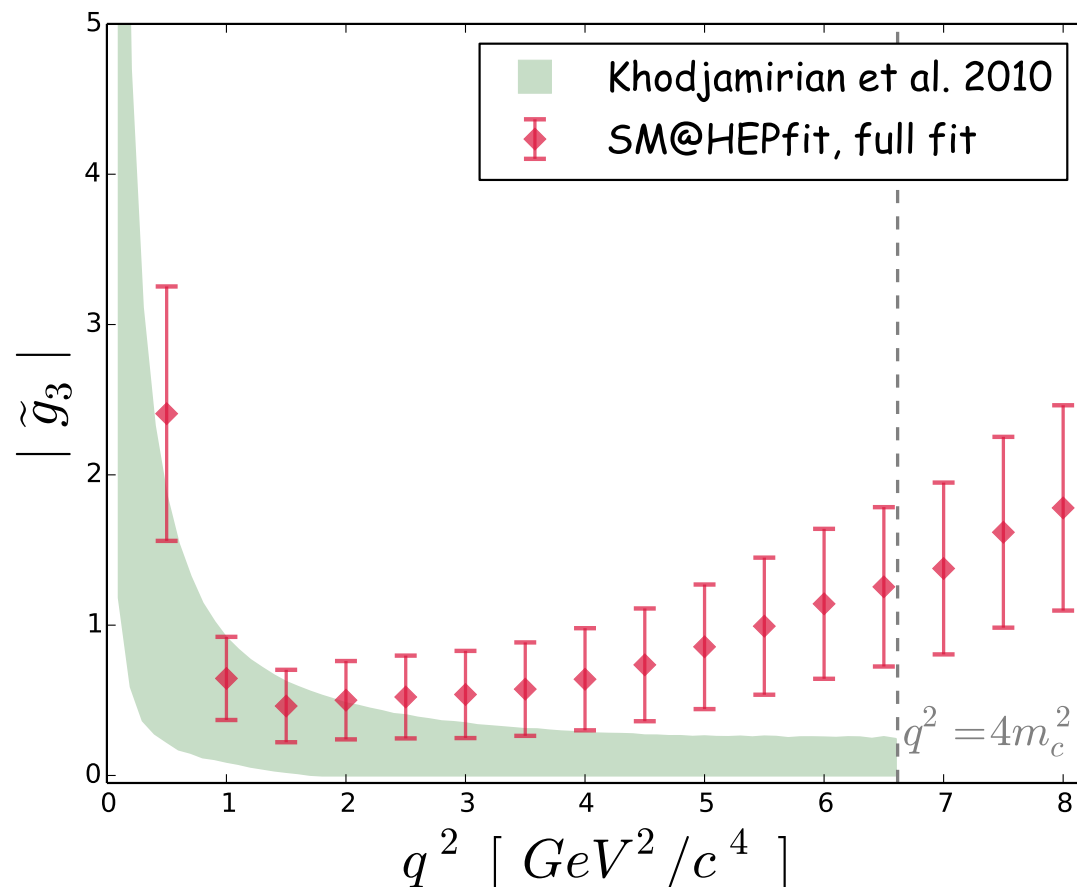
Eventually, to compare with the literature:

$$\tilde{g} \equiv \Delta C_9^{(\text{non pert.})} / (2C_1)$$

hadronic contribution extracted is compatible with theory estimate order of magnitude for $q^2 \lesssim 1 \text{ GeV}^2$ and grows for larger q^2 towards charm resonances ... it goes as expected!

DISCLAIMER:

Generic NP contribution in a Wilson coefficient would not bring any q^2 dependence.



ANOMALY

anomaly | əˈnɒm(ə)li |

noun (pl. **anomalies**)

: something that deviates from what is standard, normal, or expected

: *there are a number of anomalies in the present system*

Hadronic (charm) effects can sizably affect your prediction.

This is what one could expect to find in B to $K^* \ell \ell$.

That is what we were able to extract from available data.

At present, no anomaly can be possibly claimed.

Thank You!