

SUSY 2015 - Particle Cosmology Session

" Looking for Dark Matter in Dwarf Spheroidal Galaxies "

M.V., P.Ullio (in preparation)



M. Valli

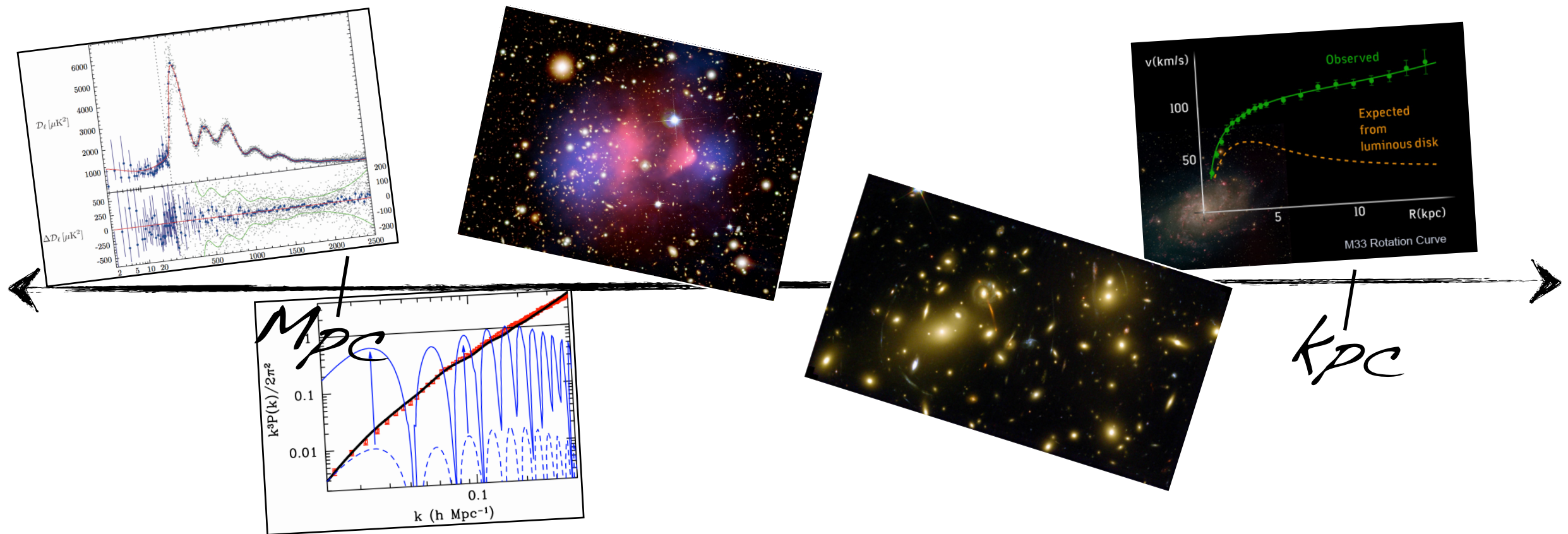


Lake Tahoe (USA),
August 24 2015

Supported by:

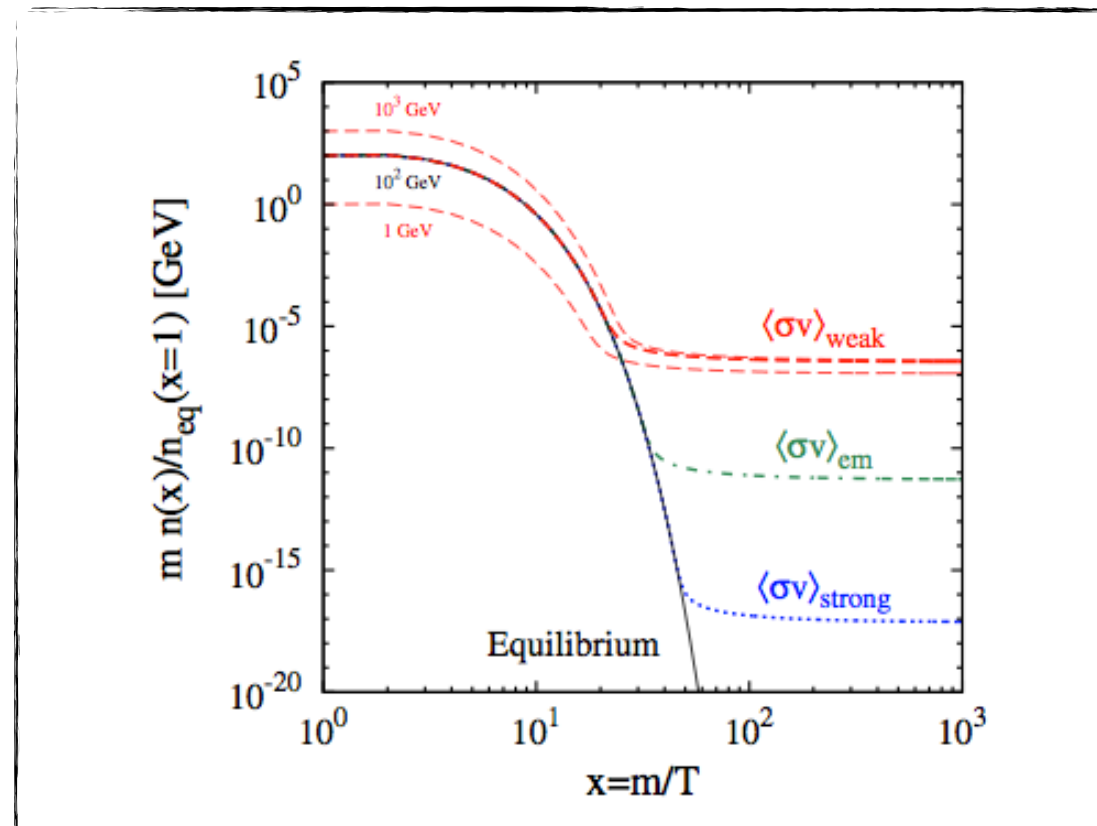


Evidence in favor of Dark Matter existence @ different scales ...



(Steigman et al. '12)

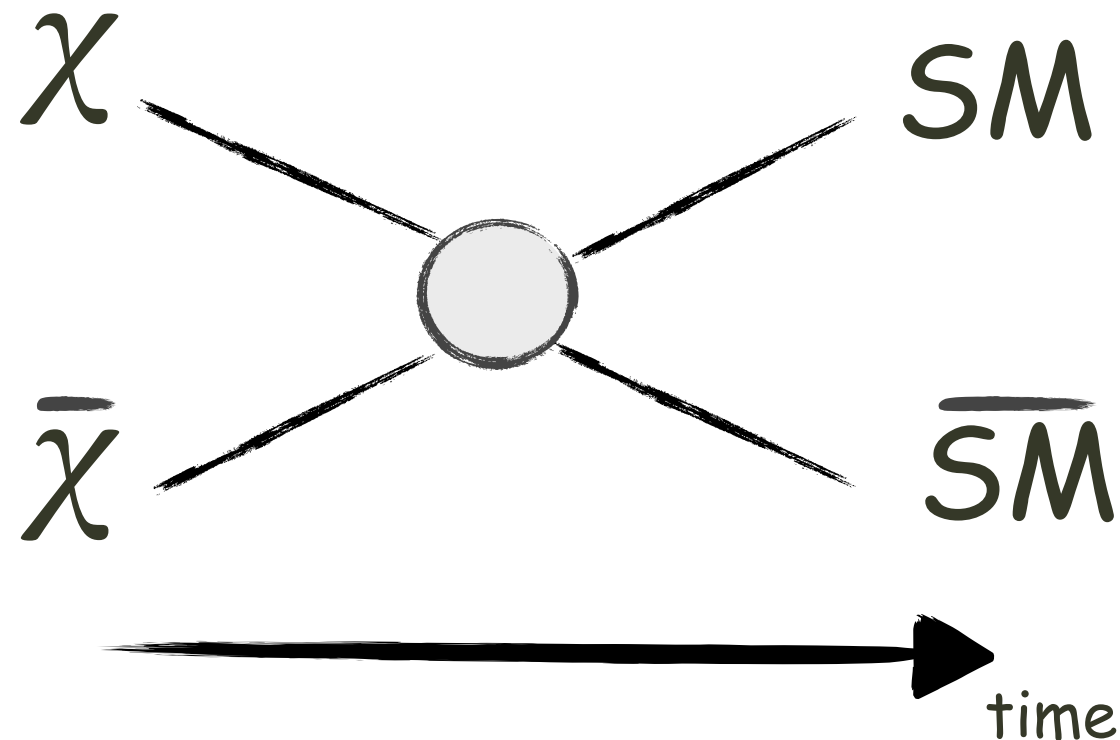
Beyond the Standard Model of Particle Physics opportunity !



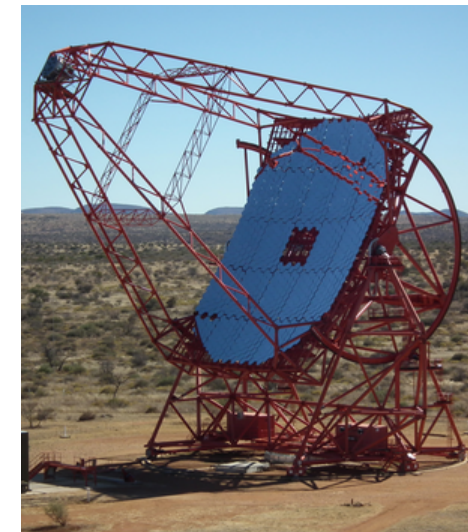
$$\Omega_{\chi} h^2 \sim \frac{3 \times 10^{-27} cm^3 s^{-1}}{\langle \sigma v \rangle_{f.o.}}$$

Weakly Interacting Massive Particles miracle

WIMP annihilation in the Sky



γ rays



Expected flux of prompt gamma to be detected ?

$$\phi_{\gamma} \propto \langle \sigma v \rangle \times J \rightarrow \sim \int d\ell \rho_{\chi}^2(r(\ell)) / m_{\chi}^2$$

Milky Way Galactic Center: $J \sim 10^{23} \text{ GeV}^2/\text{cm}^5$... GC promising target!
 ... but **complicated background!**

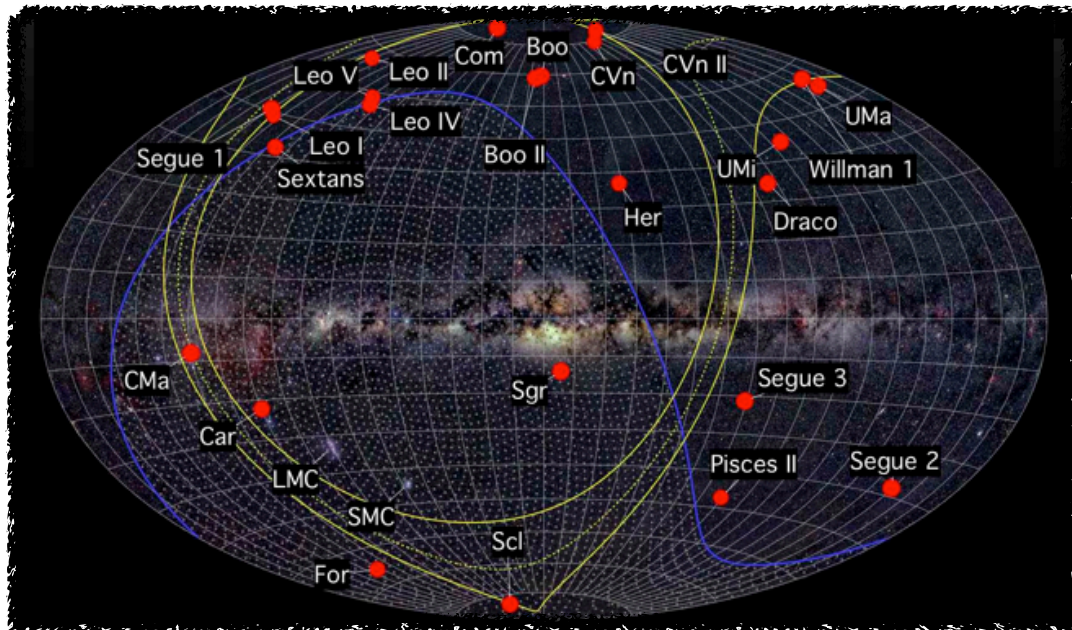
(**unresolved PS**, see [R.Bartels et al. arXiv:1506.05105](#), [S.K.Lee et al. arXiv:1506.05124](#);
GDE mismodeling, see [D.Gaggero, M.Taoso, A.Urbano, M.V., P.Ullio arXiv:1507.06129](#))

Dwarf spheroidal galaxies (dSphs) are the ideal targets!

$$\frac{M}{L} \sim 10^{2-3} \times \frac{M_{\odot}}{L_{\odot}}$$

very faint objects with
large mass-to-light ratio!

In particular, for Milky Way satellites:



high latitude position
suppressed gamma-ray flux
from standard processes

heliocentric distances
about 70 - 250 kpc

high
J-value

✓ photometry for stellar density profile , $I(R)$

✓ spectroscopy for line-of-sight kinematics , $\sigma_{los}(R)$

✗ full 3D kinematical knowledge , $\beta(r) \equiv 1 - \sigma_t^2(r)/\sigma_r^2(r)$

Moment-based Dynamical Mass Modeling

dSph as a collisionless system (Binney & Tremaine '08):

$$\odot \partial_t f + \underline{v} \cdot \nabla_{\underline{x}} f - \nabla_{\underline{x}} \phi \cdot \nabla_{\underline{v}} f = 0$$

$f(\underline{x}, \underline{v}, t)$, p.d.f. of system tracer
 $\phi(\underline{x})$, total grav. pot. of system

(1) dynamical equilibrium

(2) non rotating spherical system ("spheroidal" galaxies)

$$\rightarrow \frac{d(\nu \sigma_r^2)}{dr} + 2 \frac{\beta \nu \sigma_r^2}{r} = -G_N \frac{\nu M}{r^2}$$

where ν is the 3D stellar density, $\nu(I)$.

Regarding kinematical observables:

$$\sigma_{los}^2 = \frac{1}{I} \int_{R^2}^{\infty} \left(1 - \beta \frac{R^2}{r^2}\right) \frac{\nu \sigma_r^2}{\sqrt{r^2 - R^2}} dr^2$$

*Jeans
analysis*

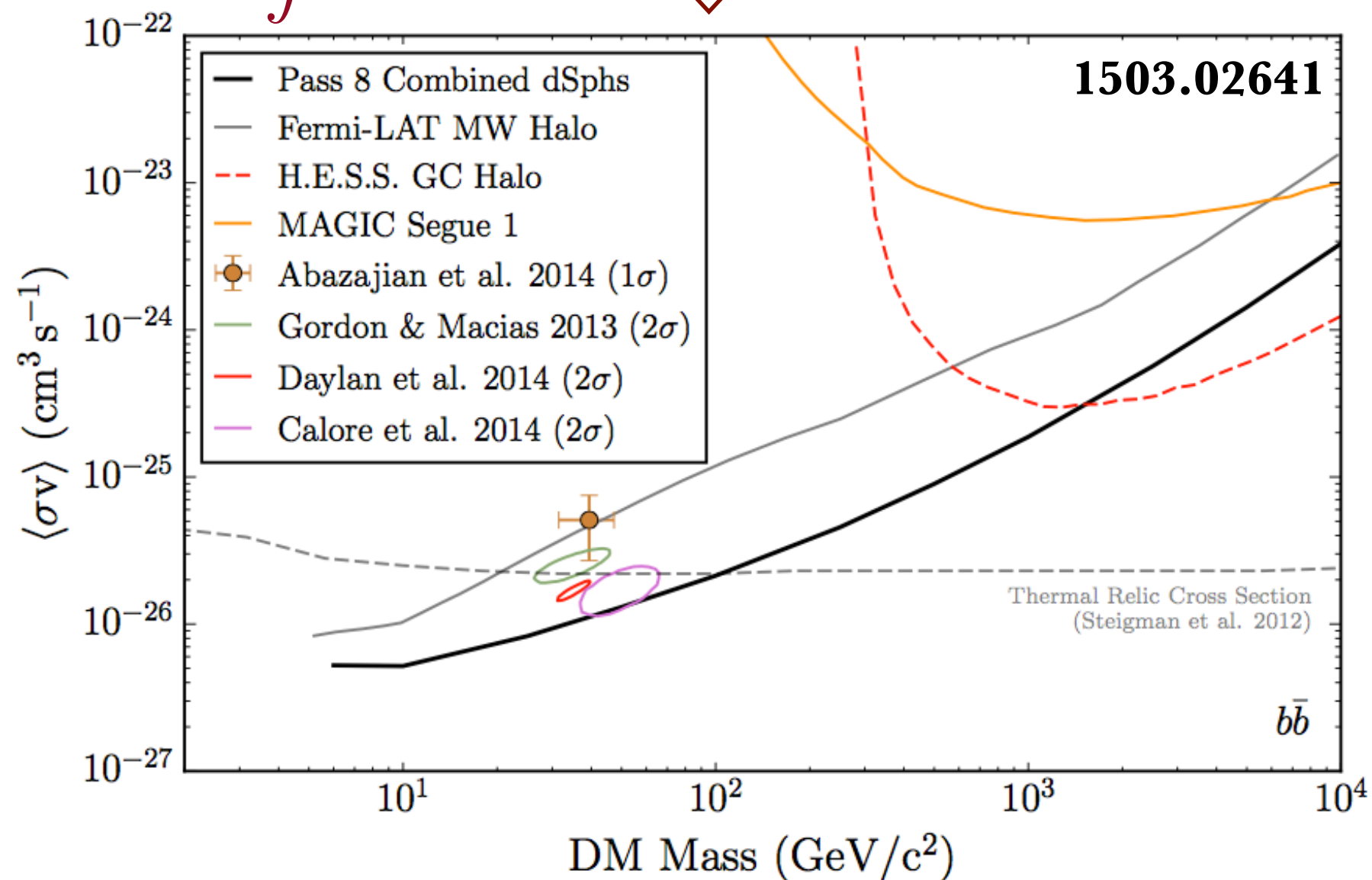
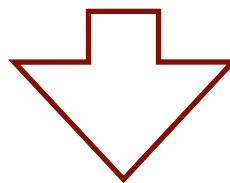
dSph \equiv collisionless spherical system in dynamical equilibrium

SPHERICAL JEANS
EQUATION



$$\sigma_{los}(R) = f(I, \rho_\chi, \beta)$$

$$\int d\beta p(\beta)$$



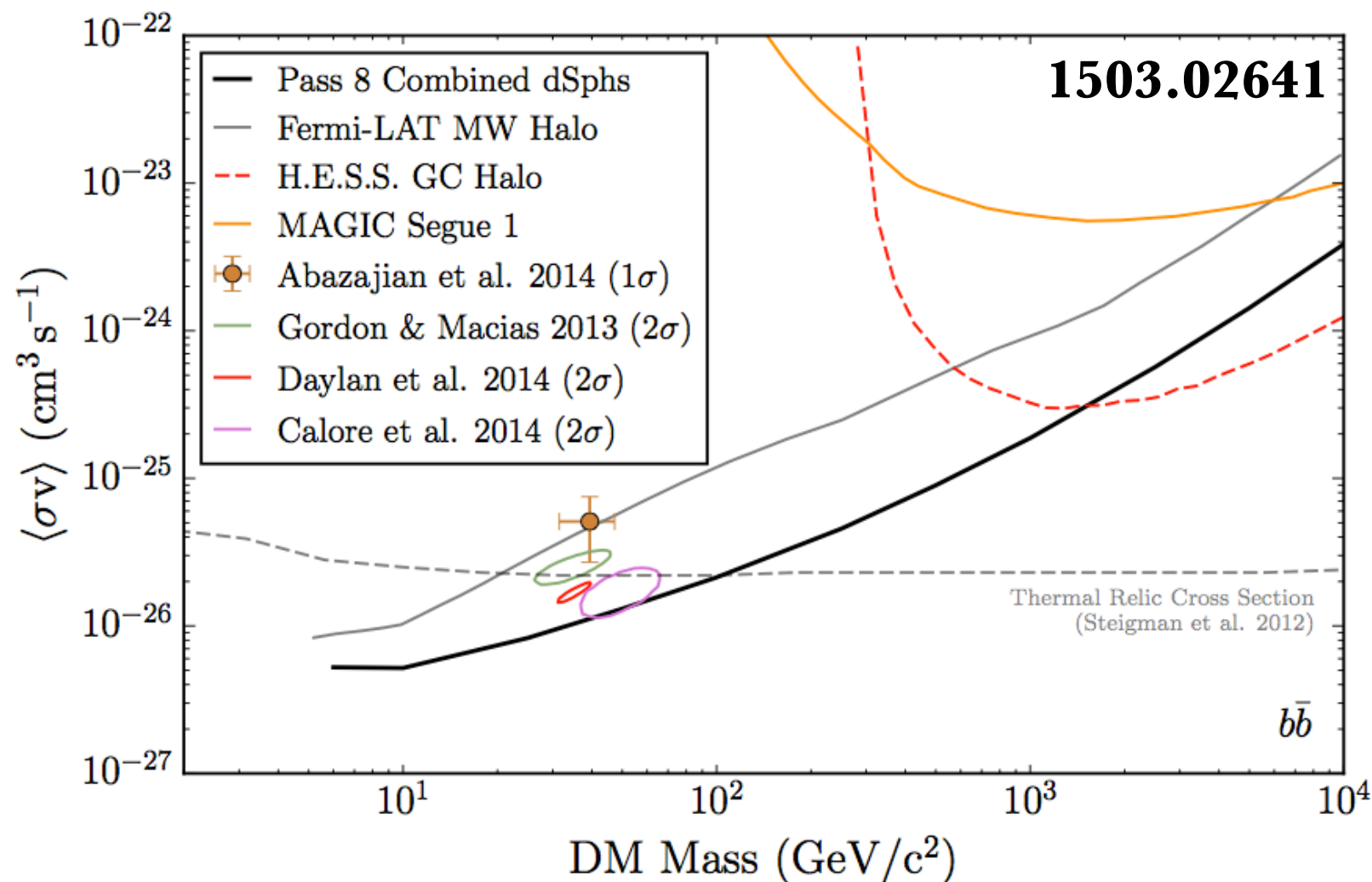
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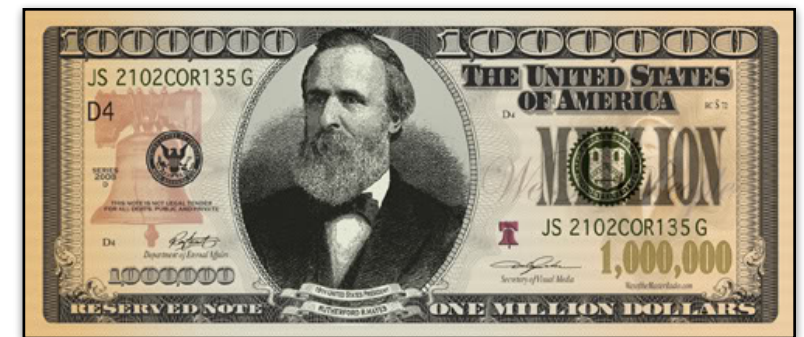
$$\sigma_{los}(R) = f(I, \rho_\chi, \beta)$$

$$\int d\beta p(\beta)$$

$$-\infty < \beta(r) \leq 1$$



1 Million Dollar Question



How do you marginalize on something you do not know?

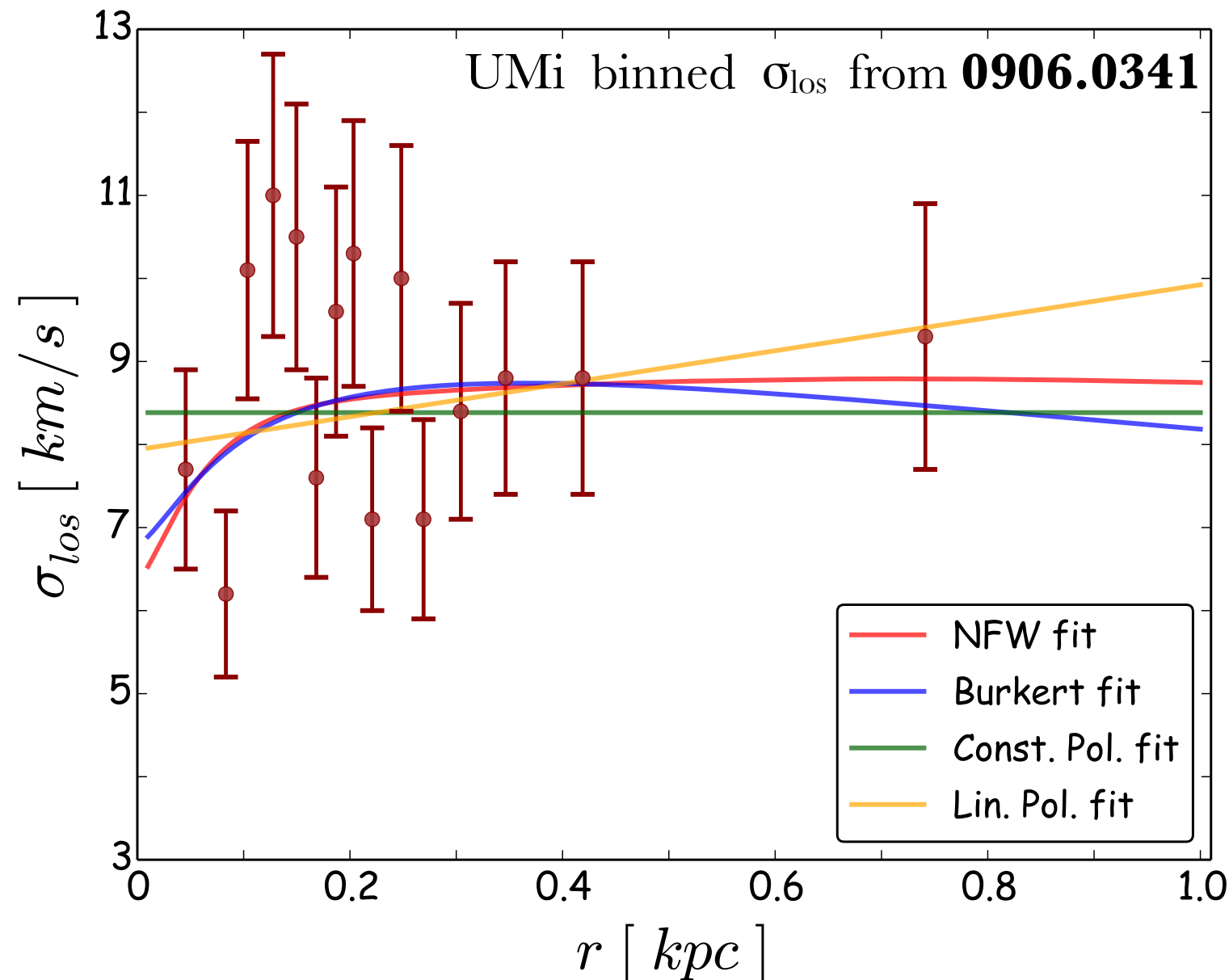
OUR NOVEL APPROACH

to attack the problem in a different way
it may be worth inverting standard logic!

Jeans Inversion

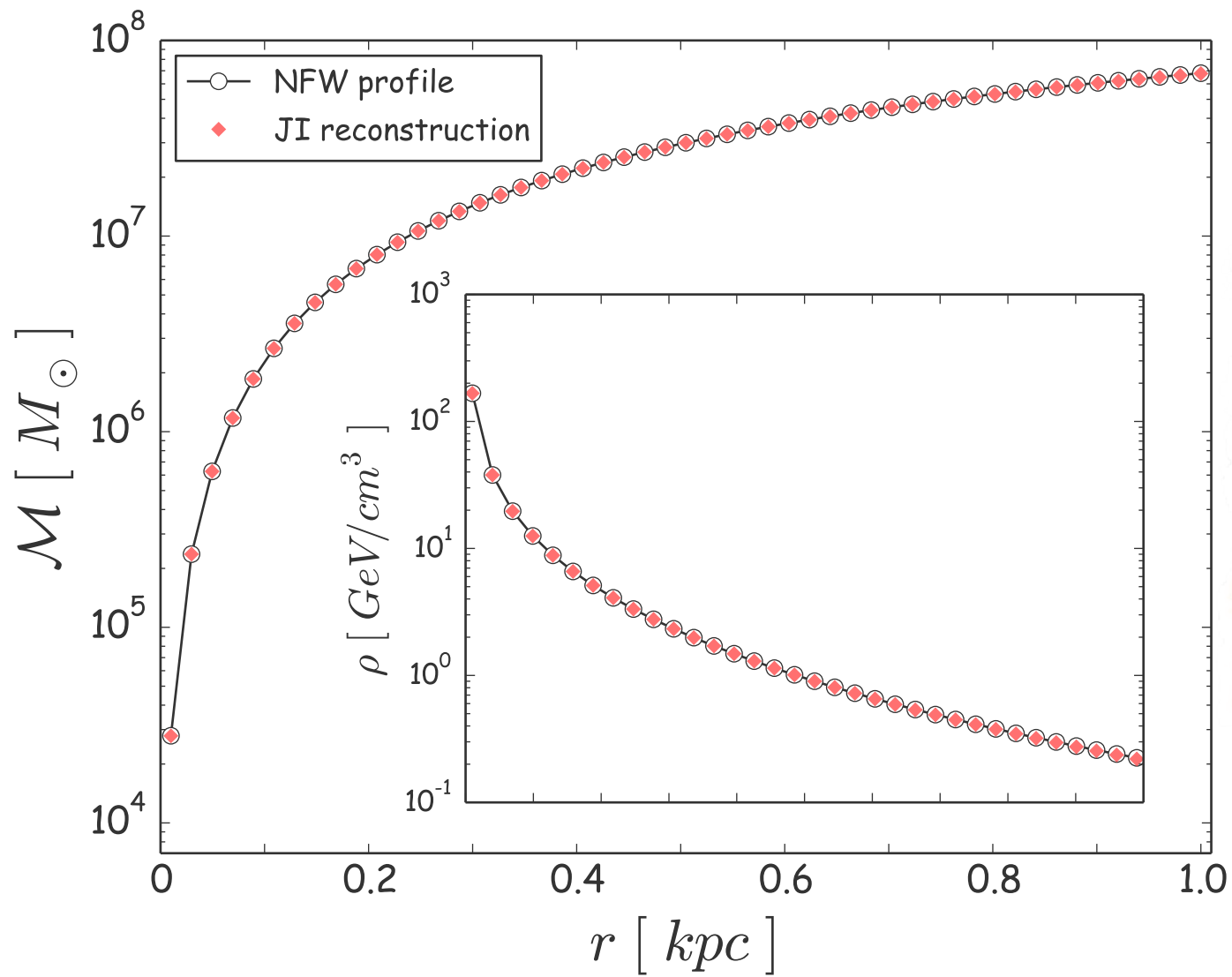
$$\sigma_{los}(R) = f(I, \rho_x, \beta)$$

$$\mathcal{M}_\beta(r) = \mathcal{F}(\sigma_{los}, I, \beta)$$



FOR A GIVEN FIT
OF LINE-OF-SIGHT
DISPERSION DATA
ONE GETS A
MASS PROFILE
IN TERMS OF $\beta(r)$

**WE BREAK
MASS-ANISOTROPY
DEGENERACY!**



The general expression for the Jeans inversion is of the form:

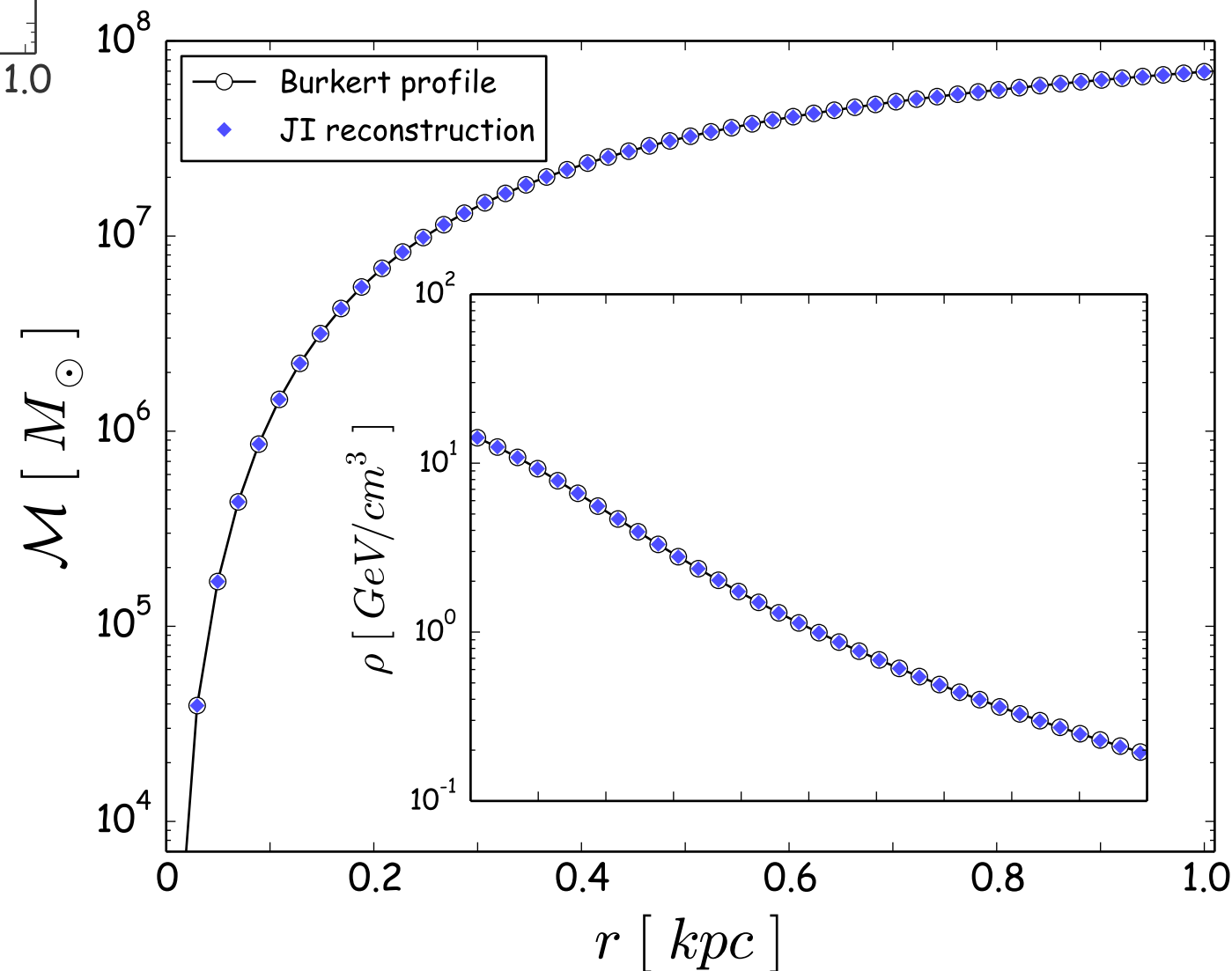
$$\mathcal{M}_\beta = \mathcal{A}_\beta(I) \int_r^\infty dR \frac{d^2 P}{(dR^2)^2} W_\beta(R, r)$$

where the pressure P is defined as

$$P = I \sigma_{los}^2$$

The inversion works pretty well also for the halo density.

$$\rho_{\chi\beta} = \frac{1}{4\pi r^2} \frac{d\mathcal{M}_\beta}{dr}$$



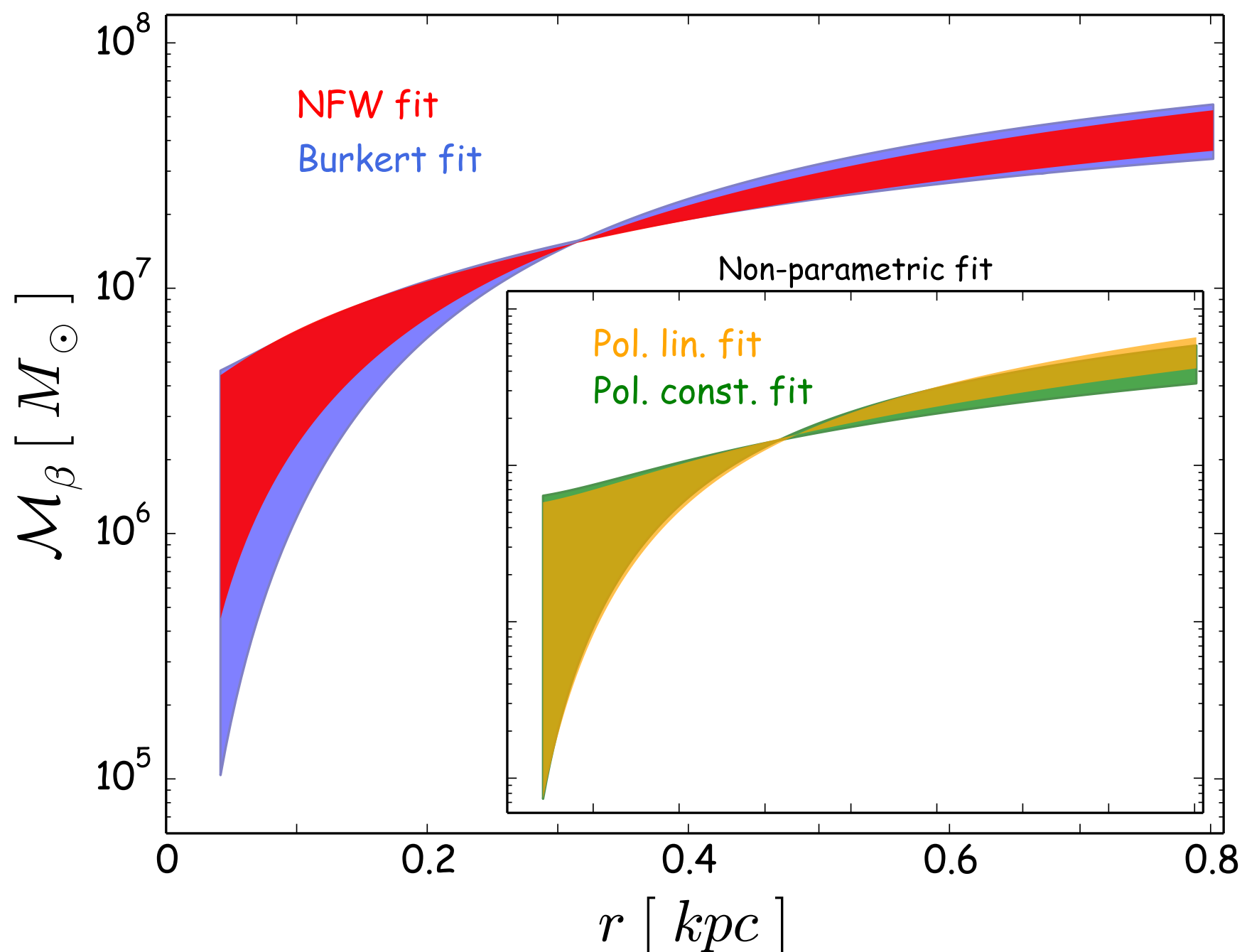
The simplest case one can consider is $\beta(r) = \text{const.}$ and can be worked out in great detail. Even for this simple case, one needs to check:

$$1) \quad \mathcal{M}_\beta > 0$$

$$2) \quad \mathcal{M}_\beta(r') - \mathcal{M}_\beta(r) \geq 0 \quad \text{if} \quad r' \geq r$$

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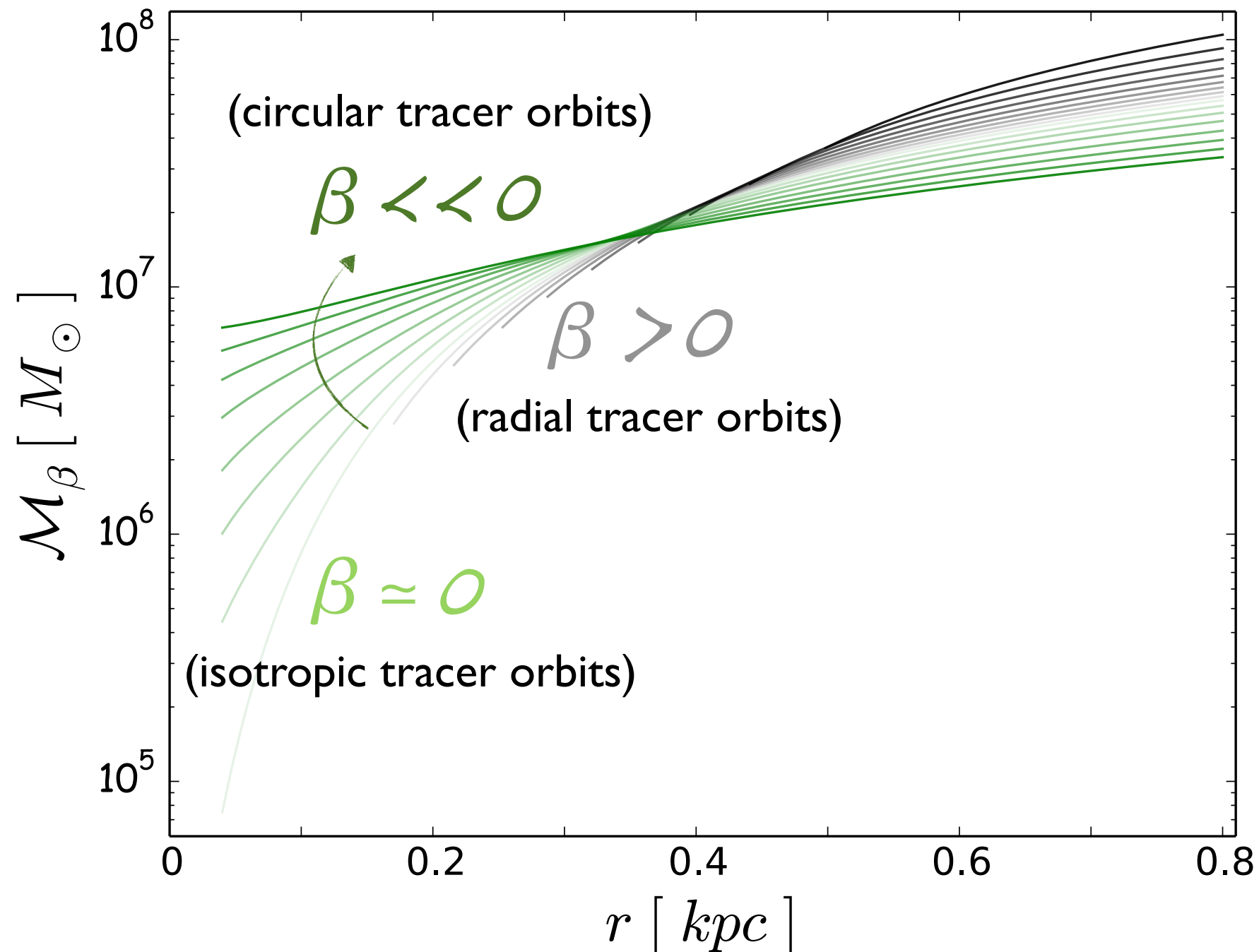
- 1) $\mathcal{M}_\beta > 0$
- 2) $\mathcal{M}_\beta(r') - \mathcal{M}_\beta(r) \geq 0$ if $r' \geq r$



One of our benchmark cases for the fit of σ_{los} data is a constant.

For this simple fit, assuming also the orbital anisotropy to be constant in radius, an analytic expression holds in our Jeans inversion approach.

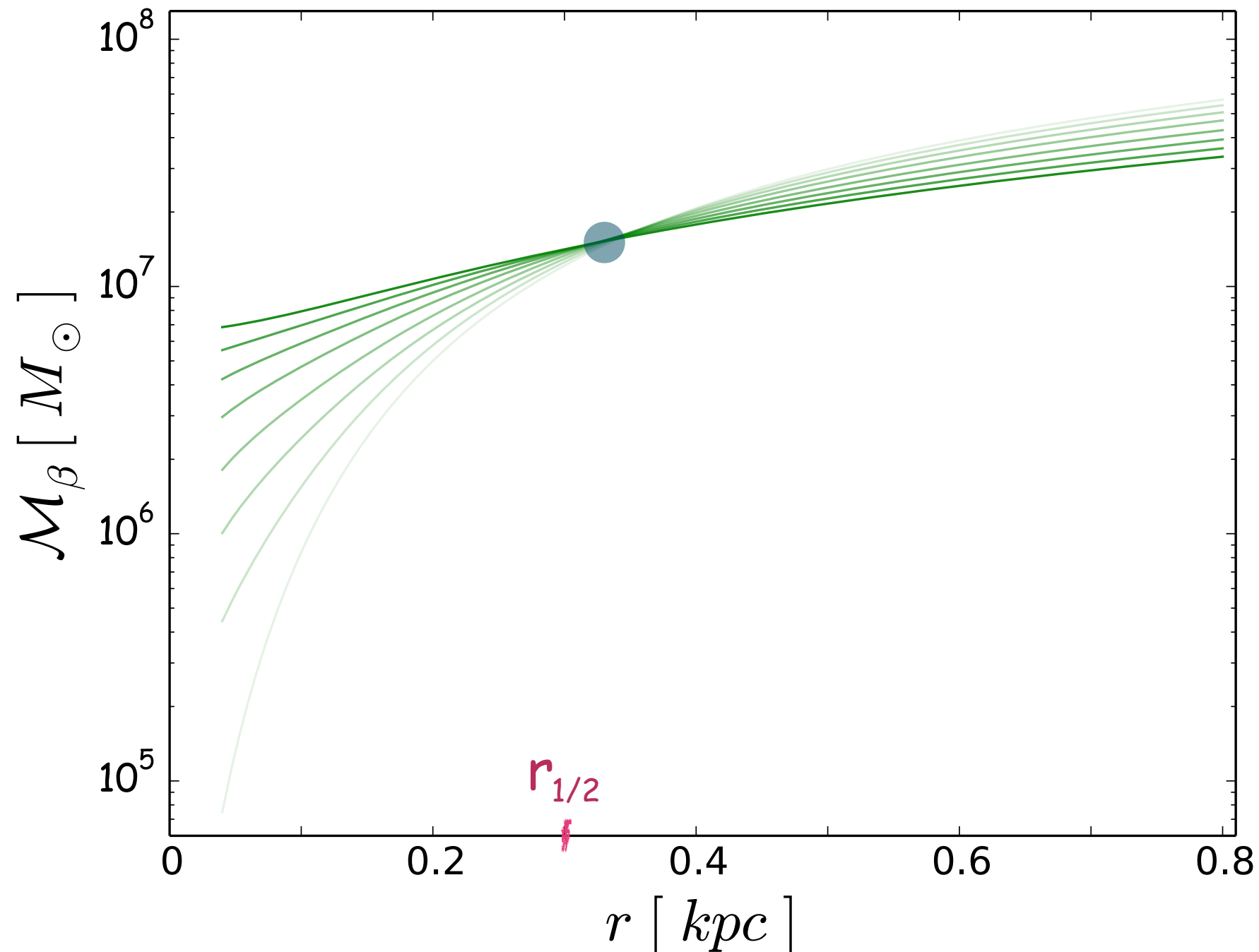
Studying the analytical mass profile:



One of our benchmark cases for the fit of σ_{los} data is a constant.

For this simple fit, assuming also the orbital anisotropy to be constant in radius, an analytic expression holds in our Jeans inversion approach.

If one restricts it to the physical mass profiles:

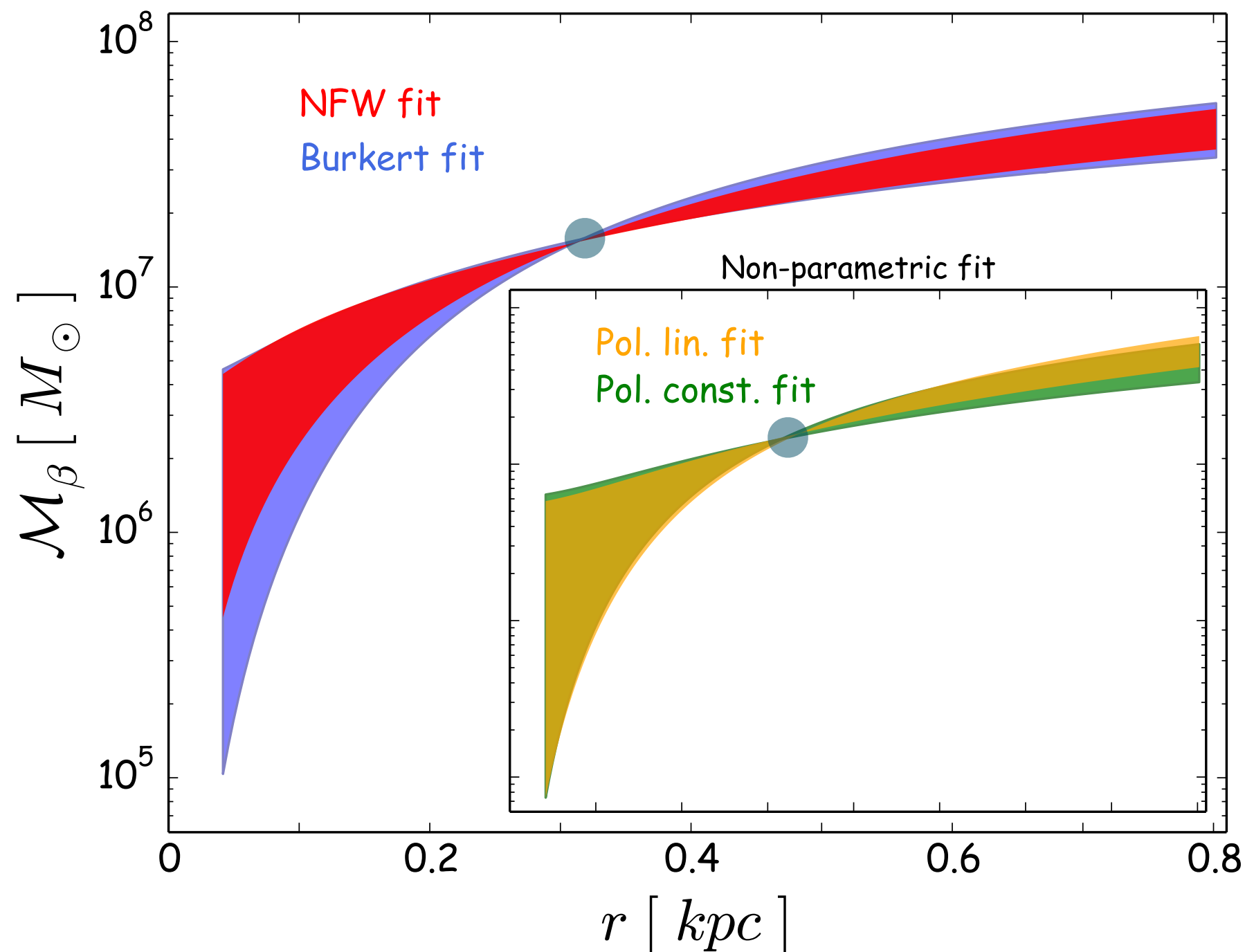


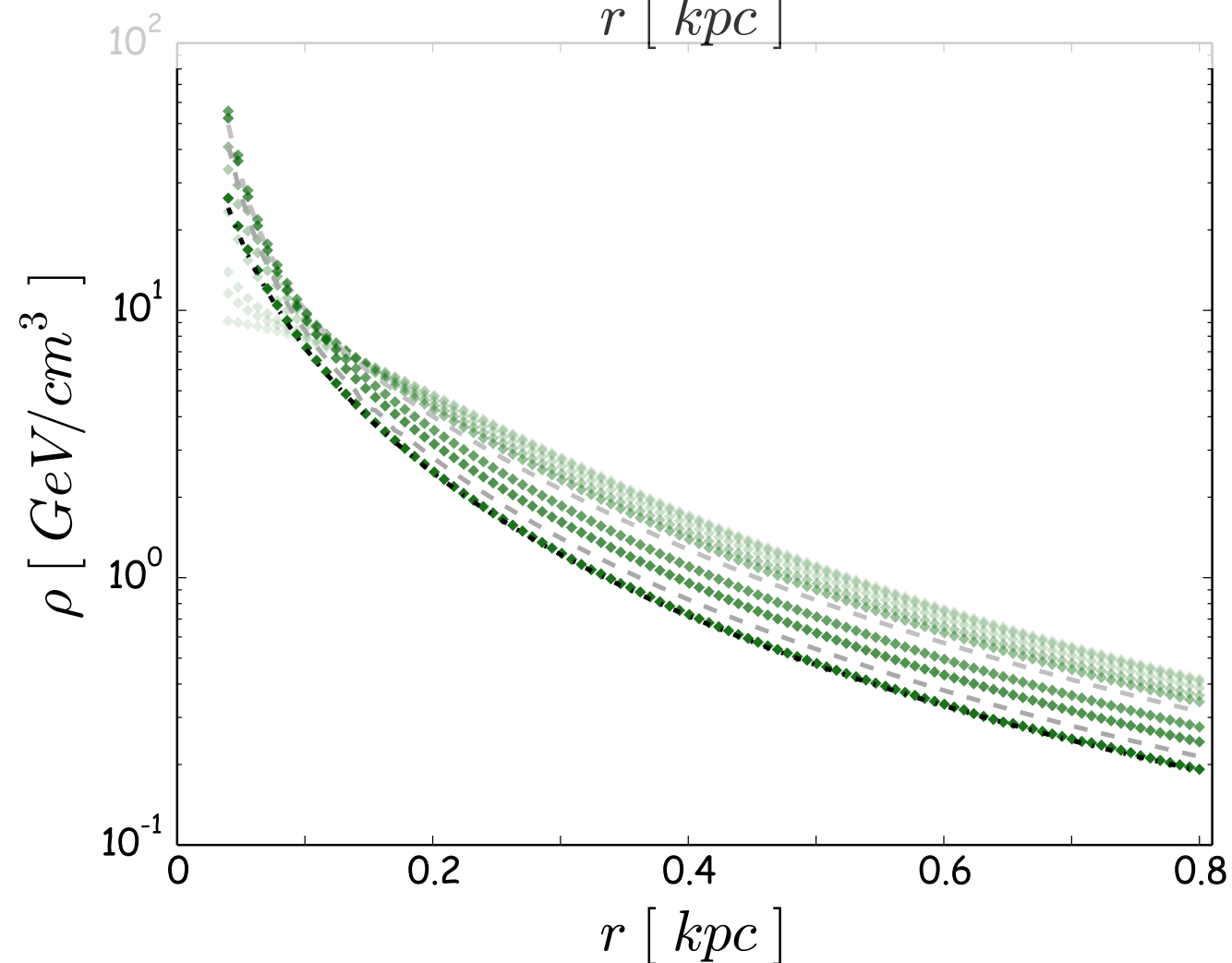
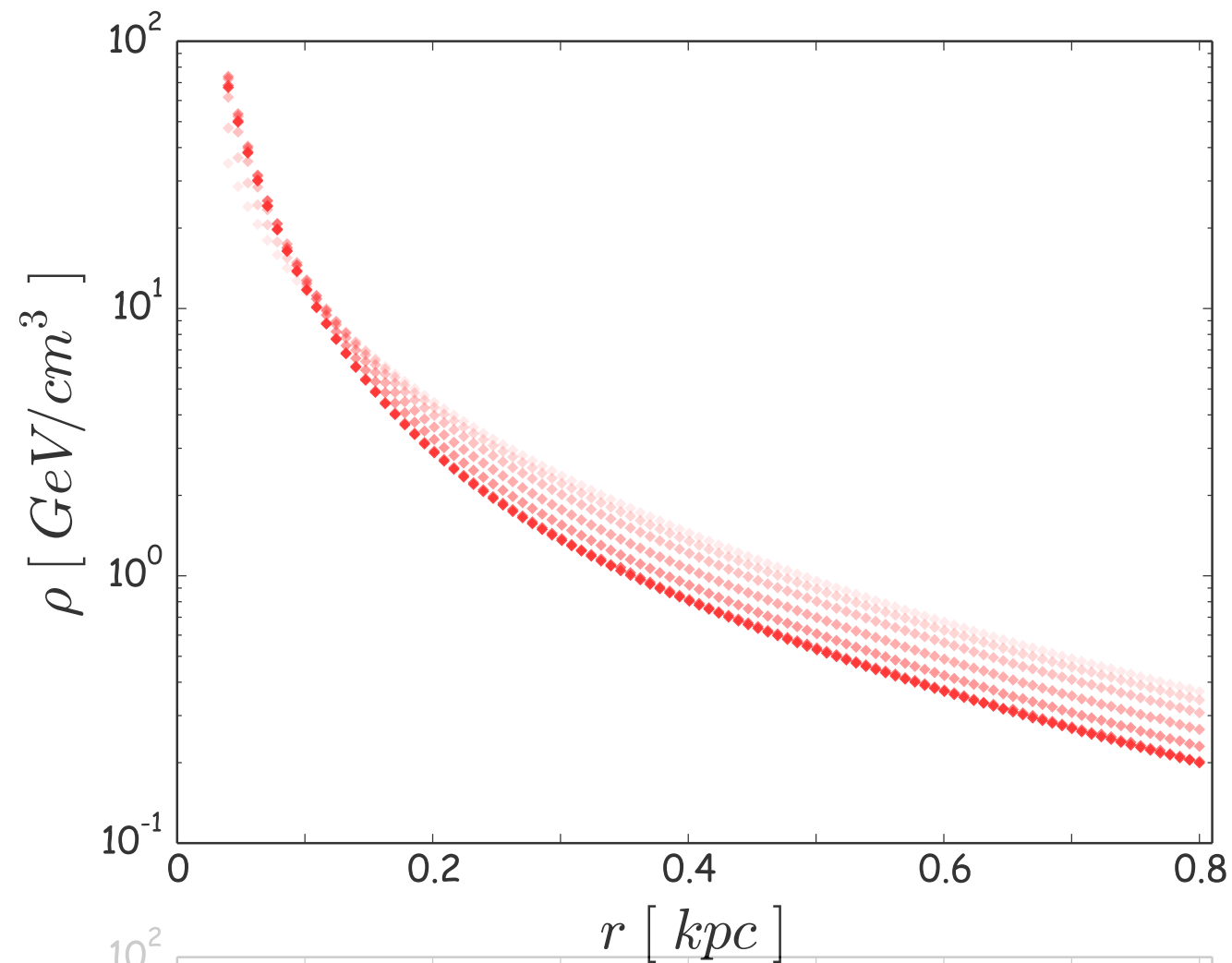
We give a proof of existence for a very good (but not exact) mass estimator

(see e.g. **0908.2995**)

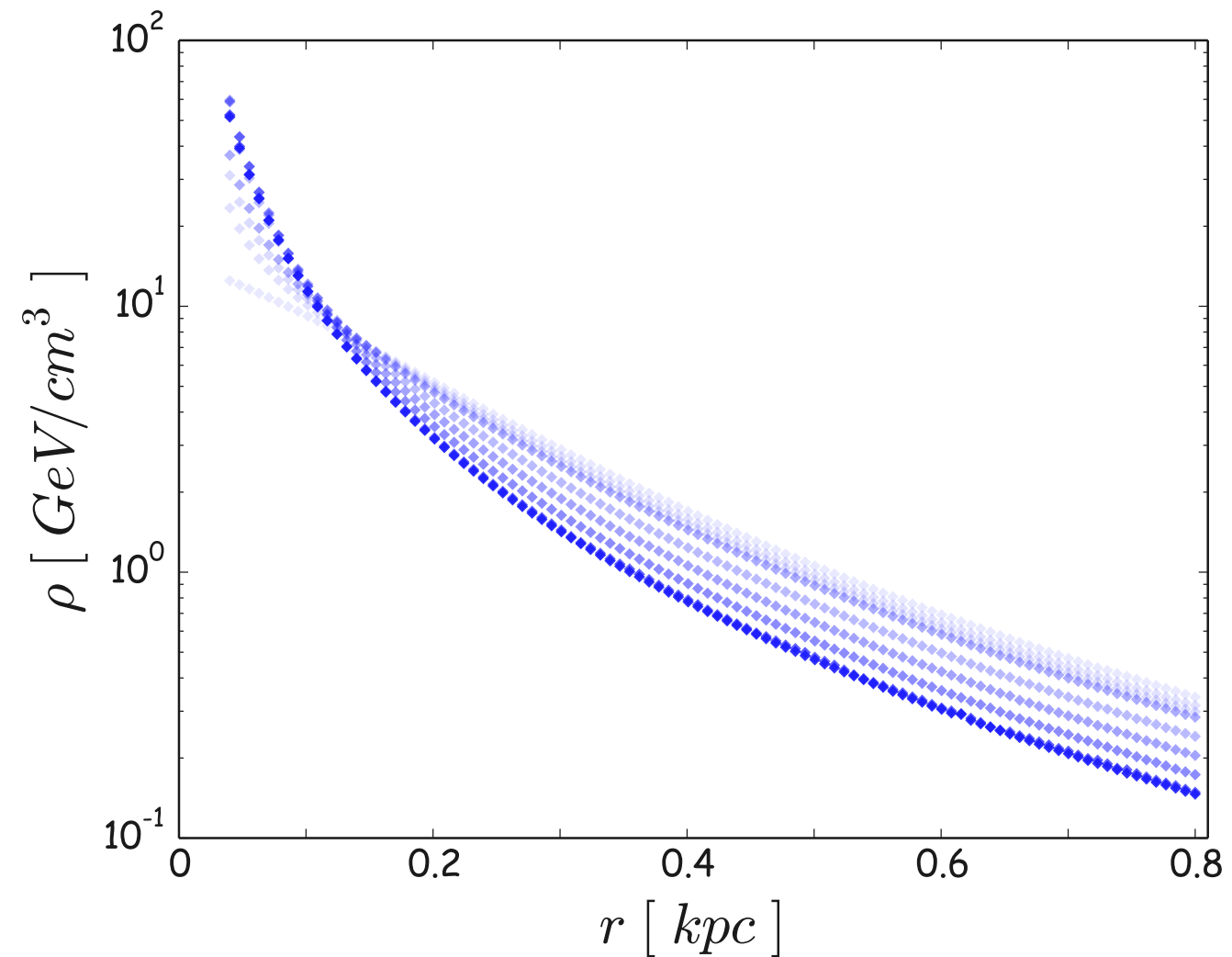
$$\mathcal{R}_{\bar{\beta}} \equiv 1 - \mathcal{M}_{\bar{\beta}} / \mathcal{M}_0 \quad \rightarrow \quad \mathcal{R}_{\bar{\beta}}(r_{\star}) = 0, \quad r_{\star} = r_{\star \bar{\beta}} \quad r_{\star} \cong r_{1/2}$$

mild dependence
on β (% effect)





Negative anisotropy seems
to require cuspier profiles.

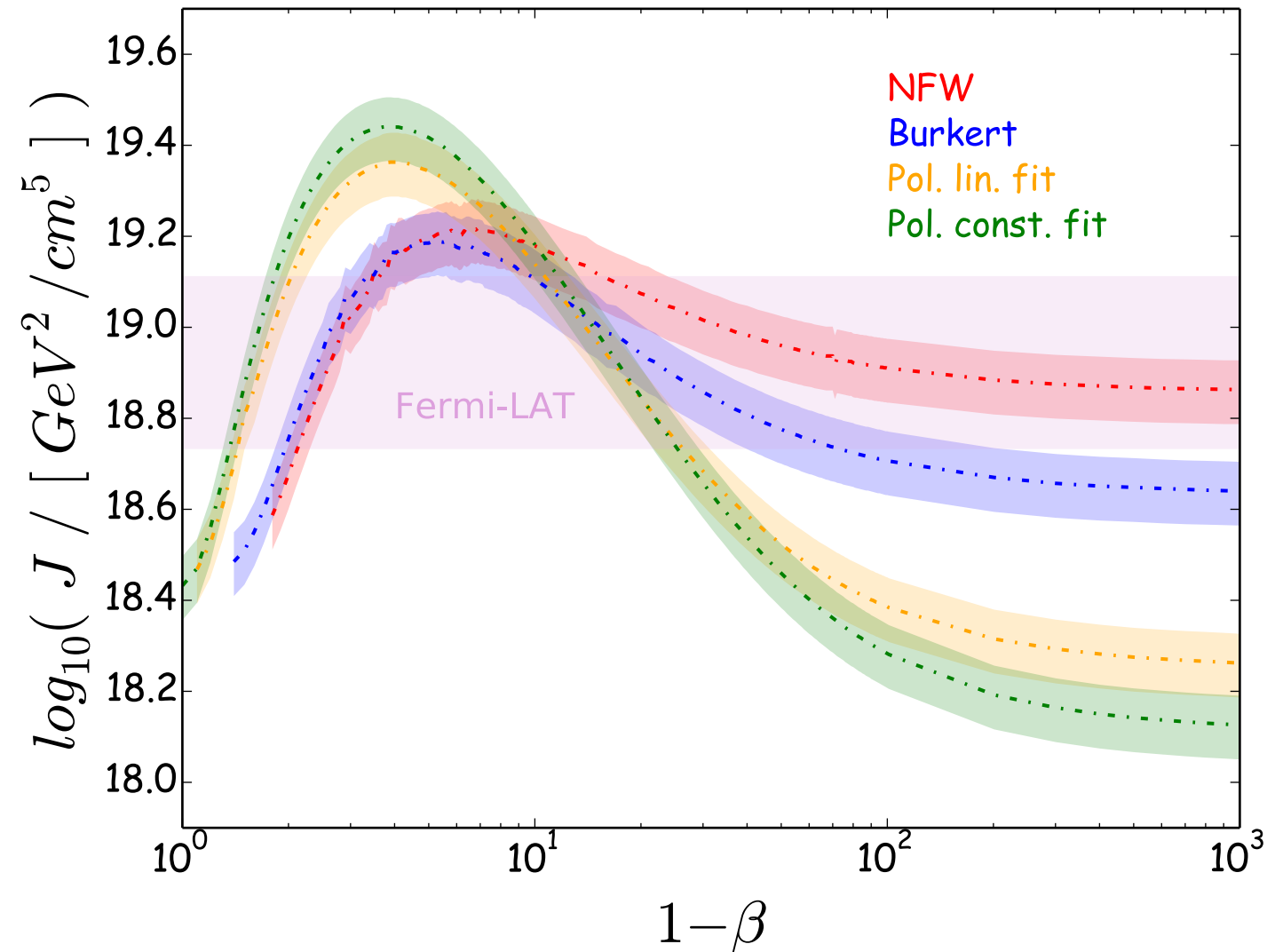


In the **constant fit case**,
 $M_{1/2}$ constraint turns out
to be slightly milder.

The halo density then can
“shift down” a bit more.

For the J -factor, one needs to integrate the squared halo density along the l.o.s. .

Since the Jeans inversion is defined only in the range of data, we make a conservative assumption for the halo density nearby the center, i.e. $\rho(r < r_1) = \rho(r_1)$, $r_1 \simeq 10$ pc .



1. Fermi-LAT 1σ band does not capture well the whole uncertainty related to β .
2. In all our 4 benchmark cases, J_{\min} results to be close to the most recent estimate of the J -factor used by the Fermi coll. to obtain DM bounds.

We extensively test the value of J_{\min} against different choices of $\beta(r)$, finding it to be solid even in the case of wildly varying radial profiles.

Final Remarks

dSph galaxies represent a unique Dark Matter laboratory
(both for Indirect Searches as well as for N-body simulations)

They can confirm/falsify the Dark Matter
interpretation of the GeV excess @ the GC

In this work we actually probed the robustness of the current tight upper-bound on $\langle \sigma v \rangle$ against what can be considered the greatest theoretical bias in the modeling of these DM dominated objects.

From this perspective, dSph constraints turned out to be quite solid ... maybe a sort of milestone for DM Indirect Searches!

Thank You!