

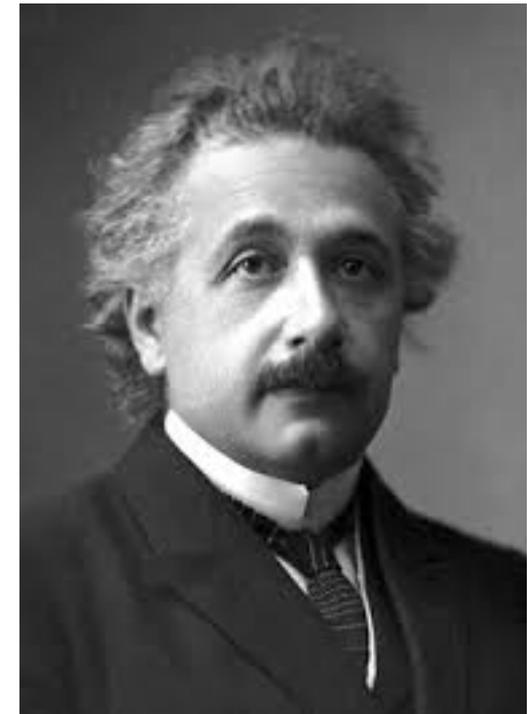
**SUSY with radiatively-driven naturalness:**  
implications for LHC and ILC searches  
(for dark matter: see plenary talk by KJ Bae)



Howard Baer  
University of Oklahoma

SUSY 2015, Granlibakken

twin pillars of guidance:  
naturalness & simplicity



“The appearance of fine-tuning  
in a scientific theory is like a  
cry of distress from nature,  
complaining that something  
needs to be better explained”

S. Weinberg

“Everything should be  
made as simple as  
possible, but not  
simpler”

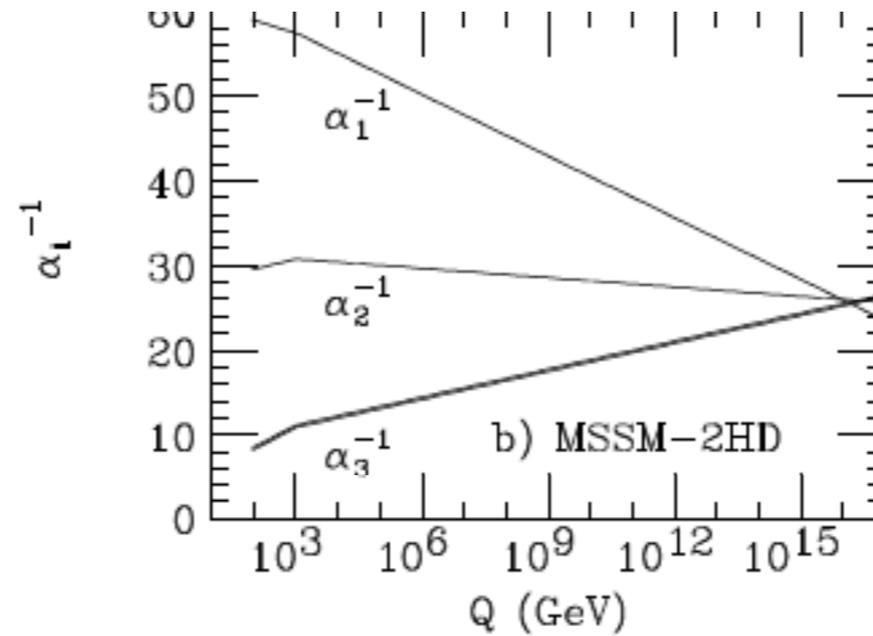
A. Einstein

# many venerable papers on SUSY naturalness!

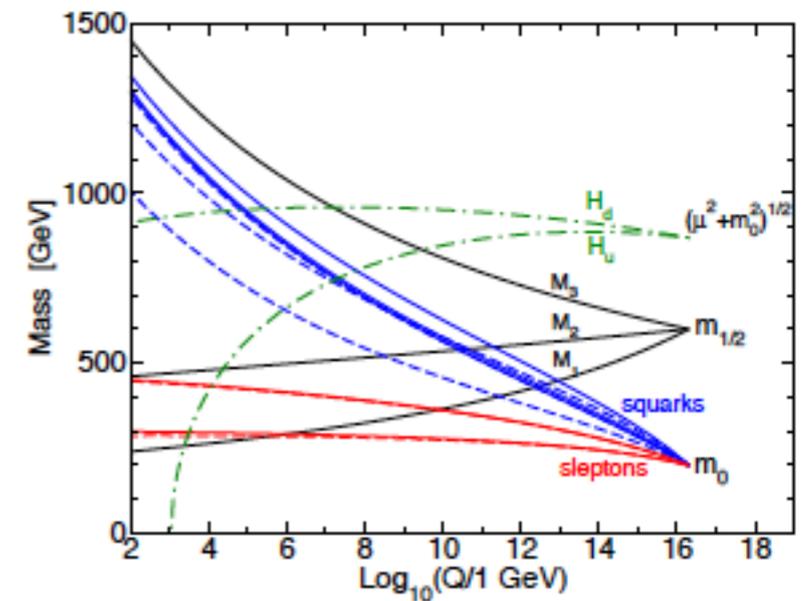
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# Three times SUSY has met the challenge from data

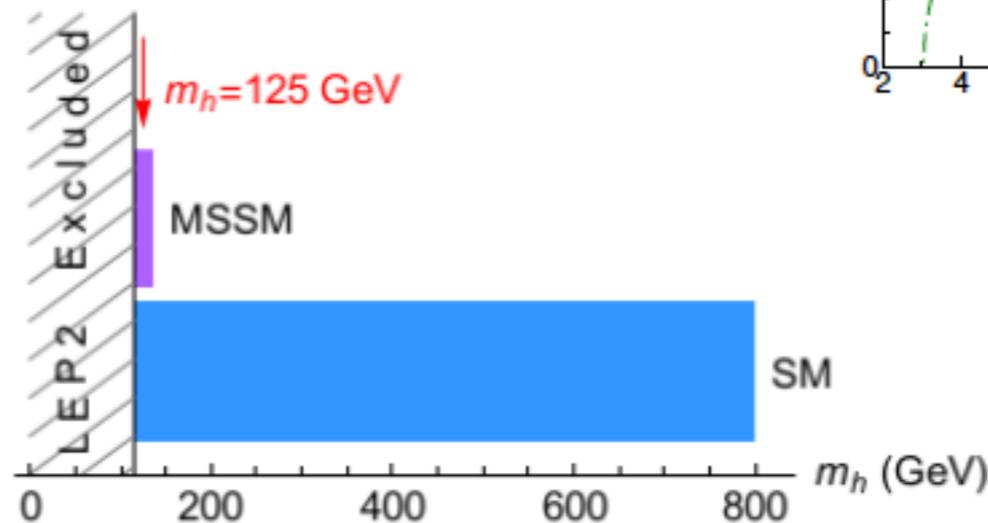
LEP gauge coupling measurements



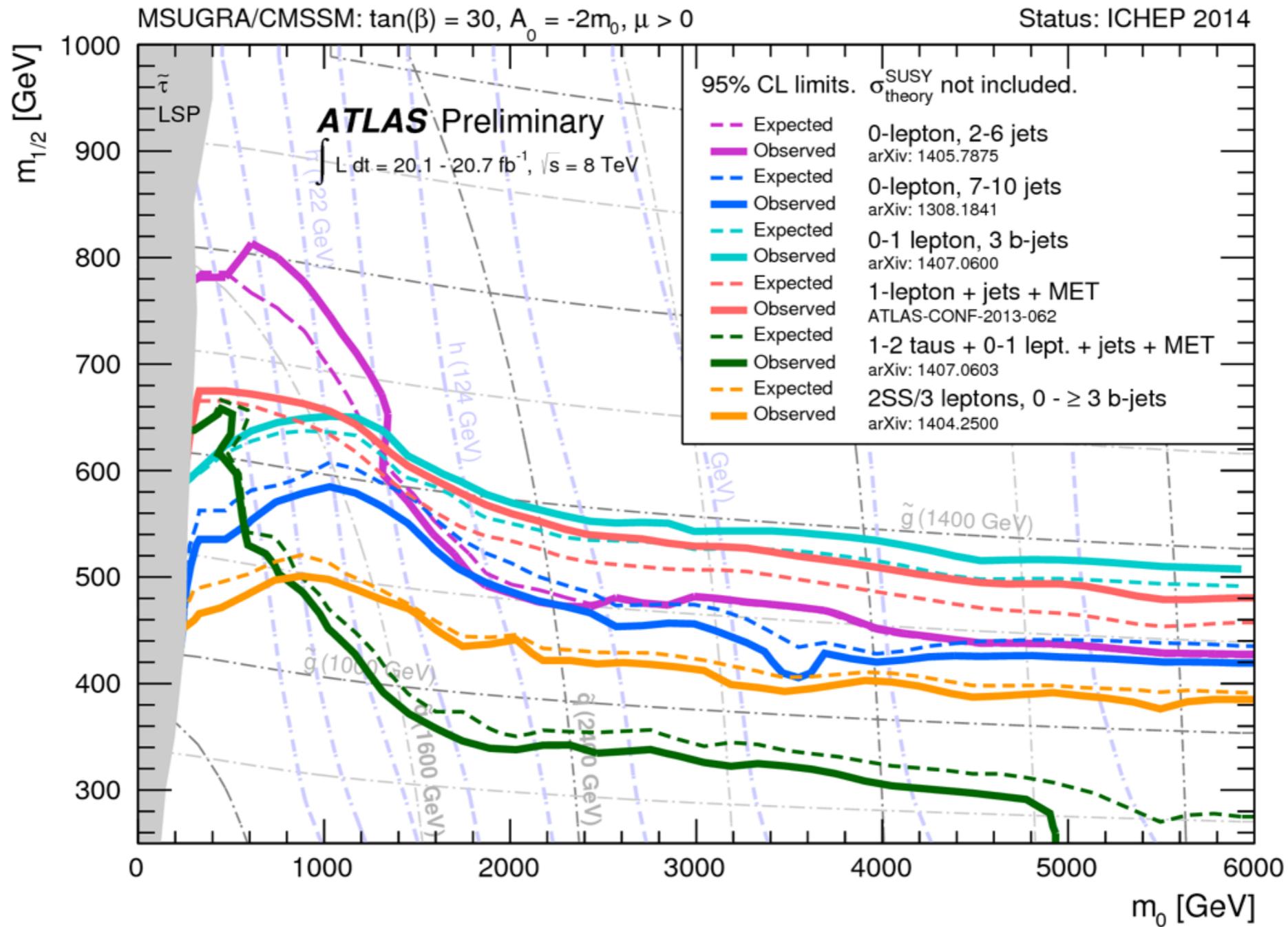
Tevatron:  
 $m(t) \sim 173.2$  GeV  
 for EWSB



LHC:  
 $m(h) = 125.1$  GeV



# But where are the sparticles?



$$m_{\tilde{g}} > 1.3 \text{ TeV} \quad (m_{\tilde{q}} \gg m_{\tilde{g}})$$

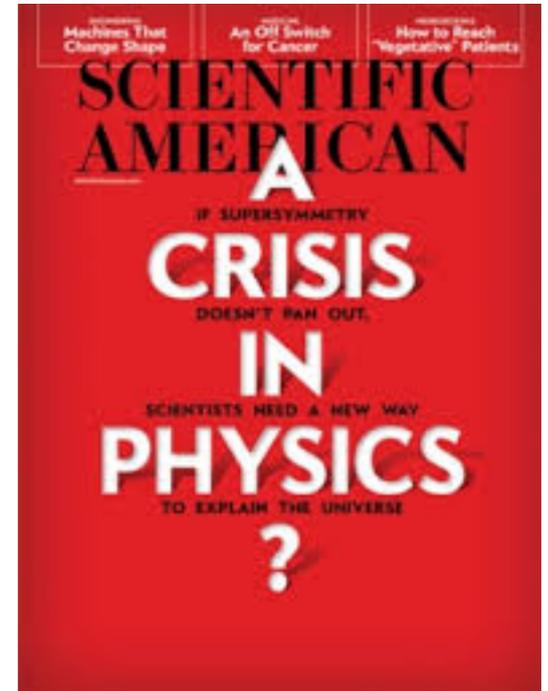
$$m_{\tilde{g}} > 1.8 \text{ TeV} \quad (m_{\tilde{q}} \sim m_{\tilde{g}})$$

$$m_h \simeq 125.1 \text{ GeV} \Rightarrow m_{\tilde{t}_{1,2}} \sim \text{TeV}$$

# Is there a **crisis** in physics?

We have heard for a long time that  
(natural) SUSY requires  
superpartners at the weak scale

Also claim is naturalness requires  
3 third generation squarks  $< 600$  GeV



## Where are the WIMPs “predicted” by WIMP miracle?

*This unshakable fidelity to supersymmetry is widely shared. Particle theorists do admit, however, that the idea of natural supersymmetry is already in trouble and is headed for the dustbin of history unless superpartners are discovered soon...*

Lykken & Spiropolu

It's great to see such a high-profile public discussion of the implications of the collapse of the paradigm long-dominant in some circles which sees SUSY extensions of the Standard Model as the way forward for the field.

Peter Woit blog,  
April 15, 2014

## What does naturalness mean?

Most claims against SUSY stem from **overestimates** of EW fine-tuning.

These arise from violations of the

## Prime directive on fine-tuning:

“Thou shalt not claim fine-tuning of **dependent** quantities one against another!”

HB, Barger, Mickelson, Padeffke-Kirkland, arXiv:1404.2277



Is  $\mathcal{O} = \mathcal{O} + b - b$  fine-tuned for  $b > \mathcal{O}$ ?

# First: Naturalness in the Standard Model

SM case: invoke a single Higgs doublet

$$V = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 \quad m_h^2 = m_h^2|_{tree} + \delta m_h^2|_{rad} \quad m_h^2|_{tree} = 2\mu^2$$

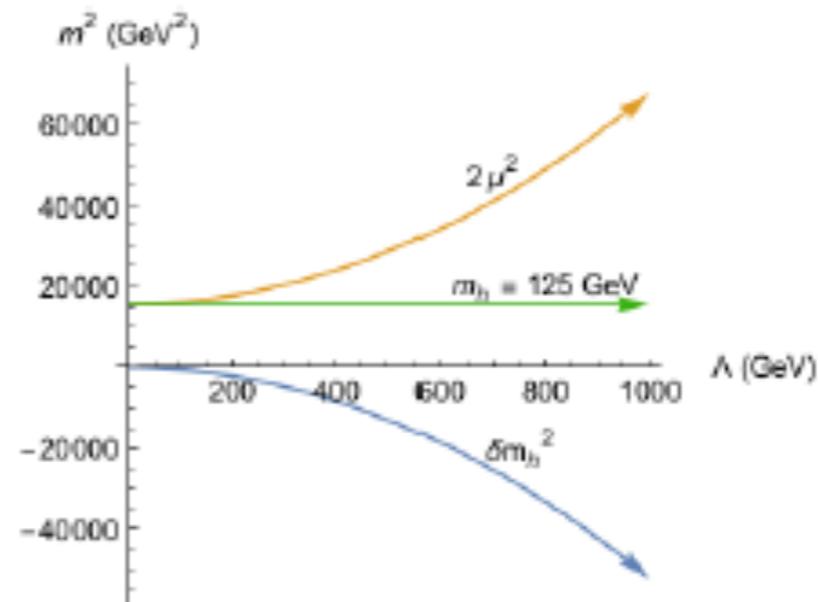
$$\delta m_h^2|_{rad} \simeq \frac{3}{4\pi^2} \left( -\lambda_t^2 + \frac{g^2}{4} + \frac{g^2}{8 \cos^2 \theta_W} + \lambda \right) \Lambda^2$$

$m_h^2|_{tree}$  and  $\delta m_h^2|_{rad}$  are independent,

If  $\delta m_h^2$  blows up, can freely adjust (tune)  $2\mu^2$  to maintain  $m_h = 125.5$  GeV

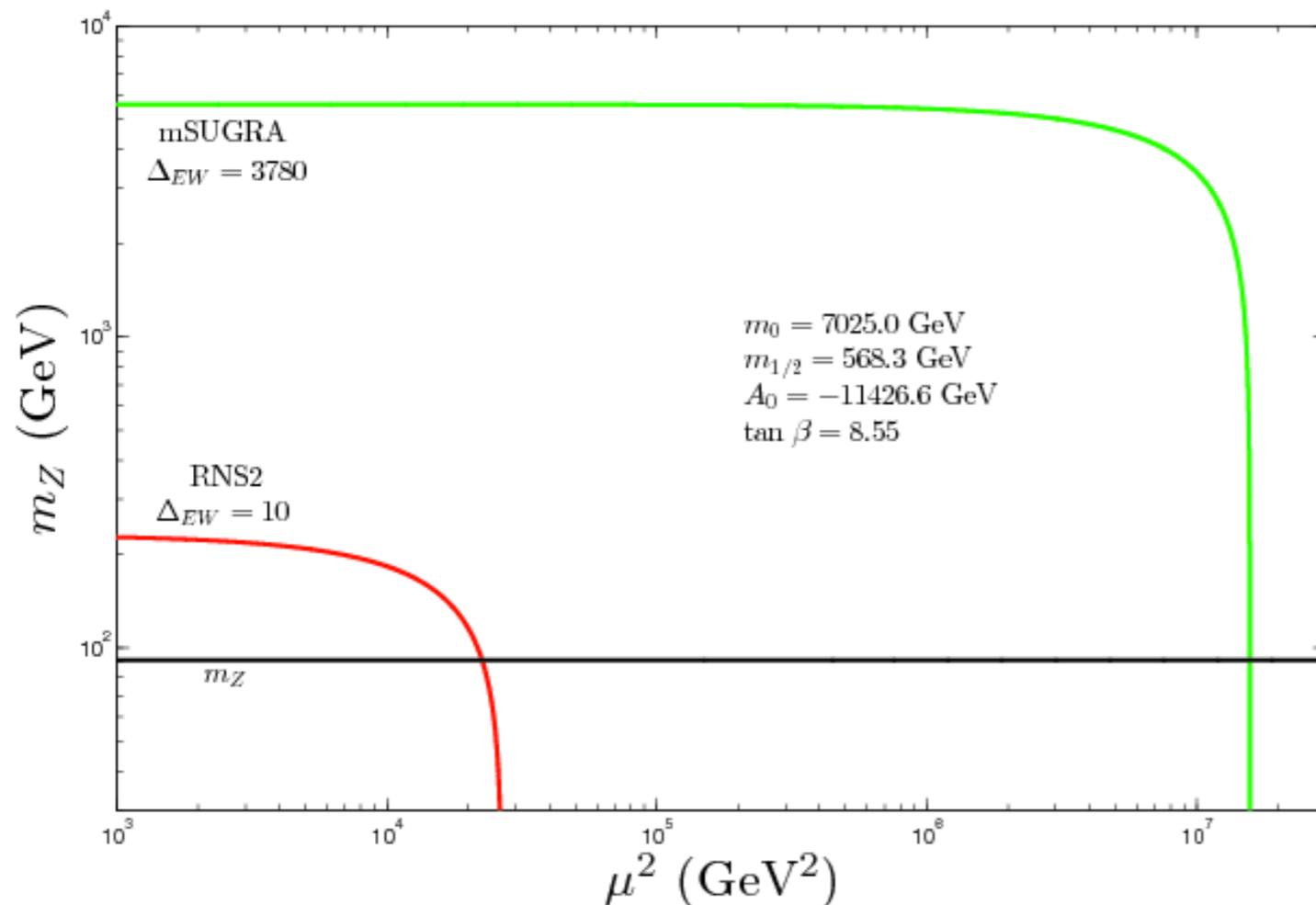
$$\Delta_{SM} \equiv \delta m_h^2|_{rad} / (m_h^2/2)$$

$$\Delta_{SM} < 1 \Rightarrow \Lambda \sim 1 \text{ TeV}$$



simple electroweak fine-tuning in MSSM:  
 dial value of  $\mu$  so that Z mass comes out right:  
 everybody does it but it is hidden inside spectra  
 codes (Isajet, SuSpect, SoftSUSY, Spheno, SSARD)

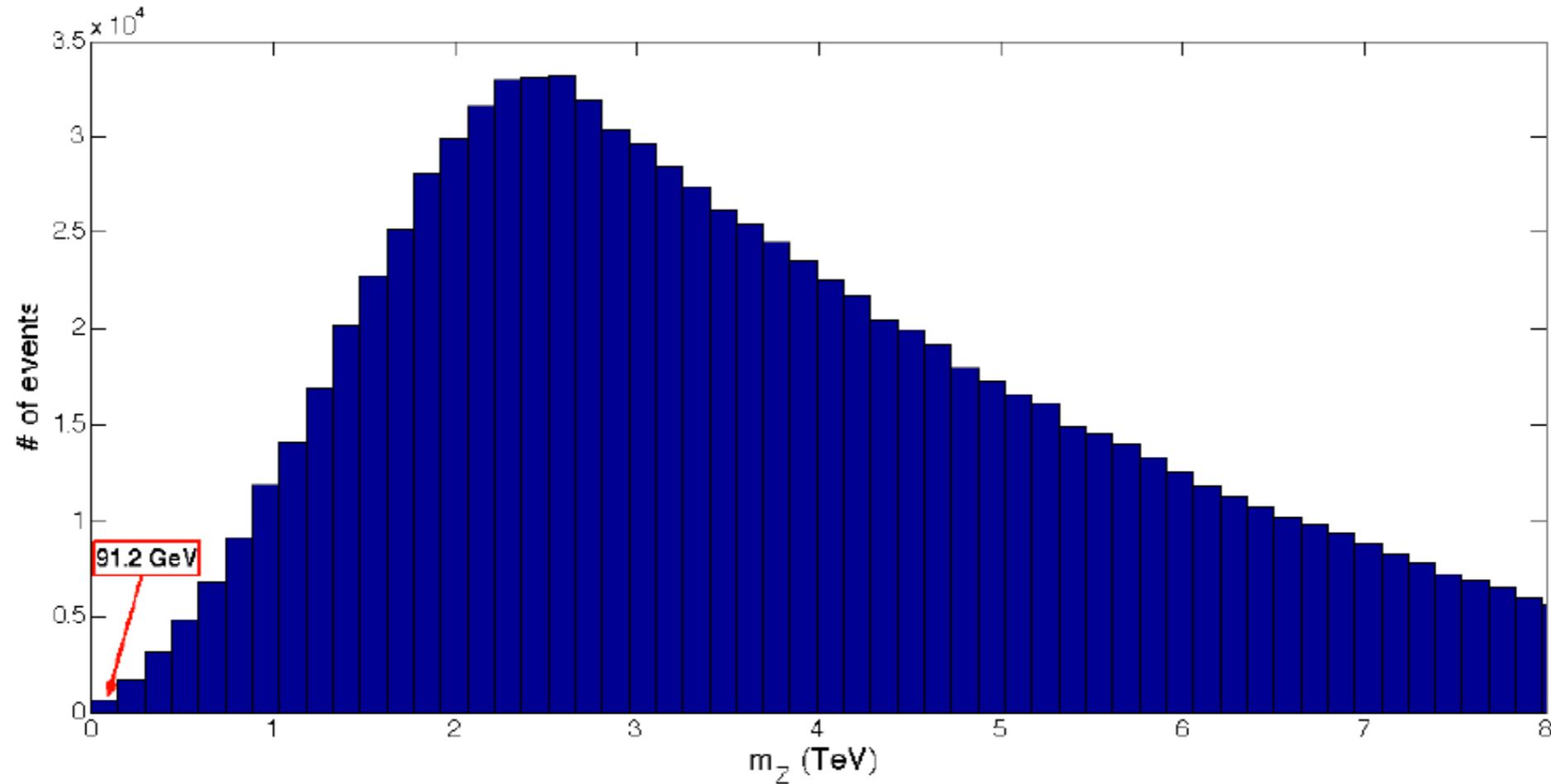
$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \Sigma_u^u - \mu^2$$



e.g. in CMSSM/  
 mSUGRA:  
 one then concludes  
 nature  
 gives this:



# If you didn't fine-tune, then here is $m(Z)$



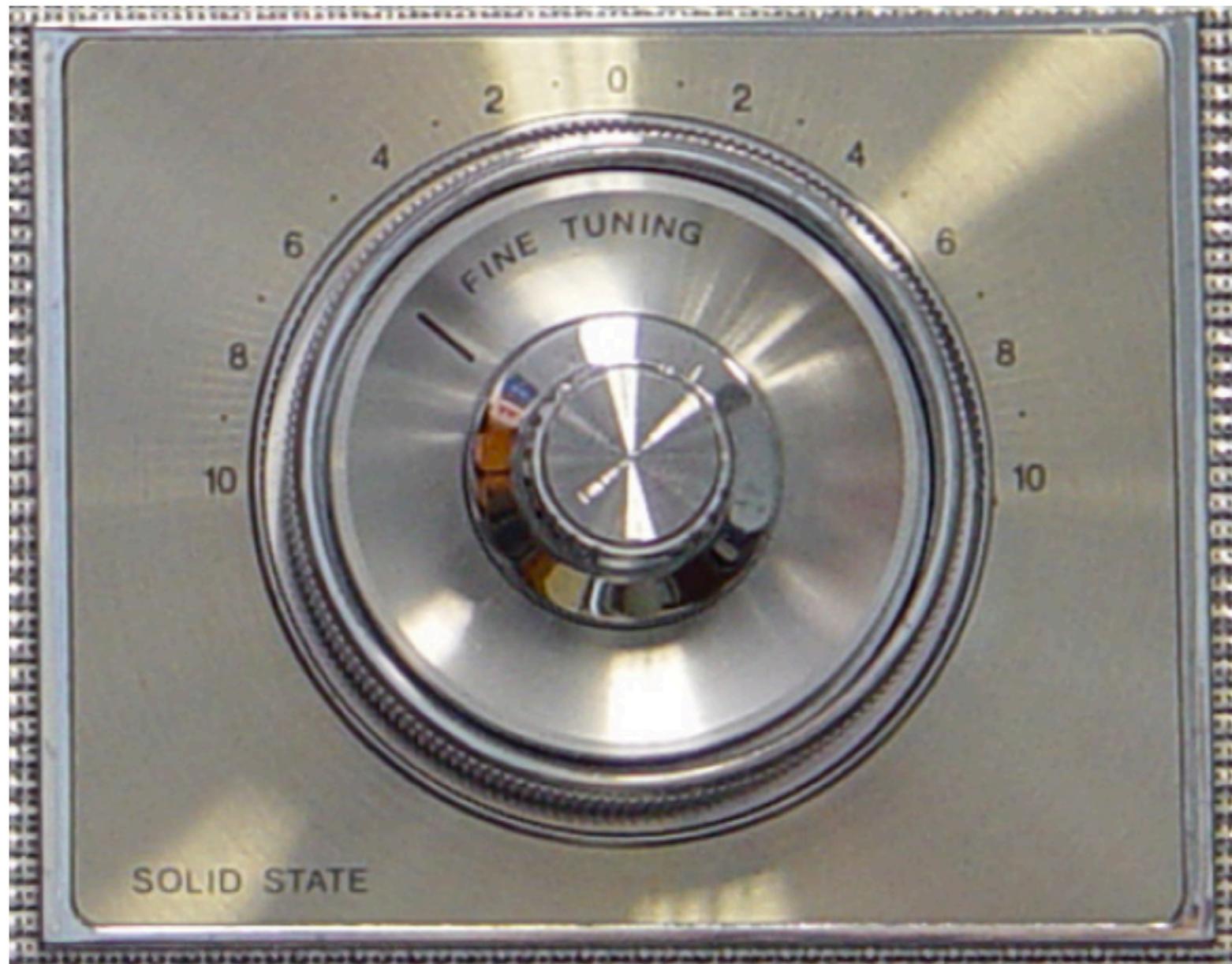
The 20 dimensional pMSSM parameter space then includes

$M_1, M_2, M_3,$   
 $m_{Q_1}, m_{U_1}, m_{D_1}, m_{L_1}, m_{E_1},$   
 $m_{Q_3}, m_{U_3}, m_{D_3}, m_{L_3}, m_{E_3},$   
 $A_t, A_b, A_\tau,$   
 $m_{H_u}^2, m_{H_d}^2, \mu, B.$

scan over parameters

Natural value of  $m(Z)$  from  
pMSSM is  $\sim 2-4$  TeV

# Three measures of fine-tuning:



# #1: Simplest SUSY measure: $\Delta_{EW}$

Working only at the weak scale, minimize scalar potential: calculate  $m(Z)$  or  $m(h)$

No large uncorrelated cancellations in  $m(Z)$  or  $m(h)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$  should be driven to small negative values such that  $-m_{H_u}^2 \sim 100 - 200 \text{ GeV}$  at the weak scale and
- that the radiative corrections are not too large:  $\Sigma_u^u \lesssim 100 - 200 \text{ GeV}$

CETUP\*-12/002, FTPI-MINN-12/22, UMN-TH-3109/12, UH-511-1195-12

Radiative natural SUSY with a 125 GeV Higgs boson

Howard Baer,<sup>1</sup> Vernon Barger, Peisi Huang,<sup>2</sup> Azar Mustafayev,<sup>3</sup> and Xerxes Tata<sup>4</sup>

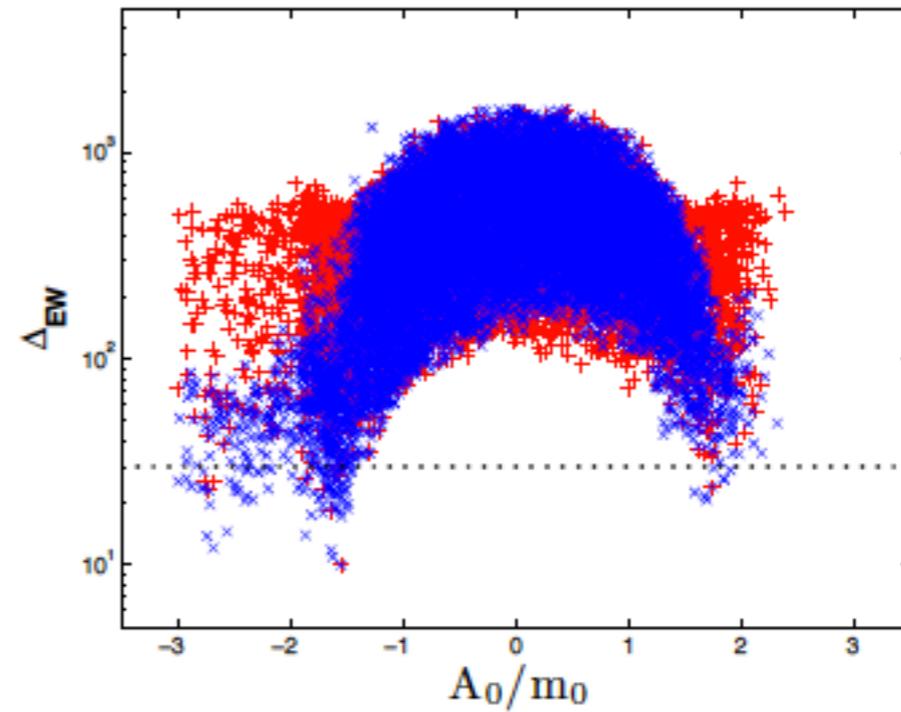
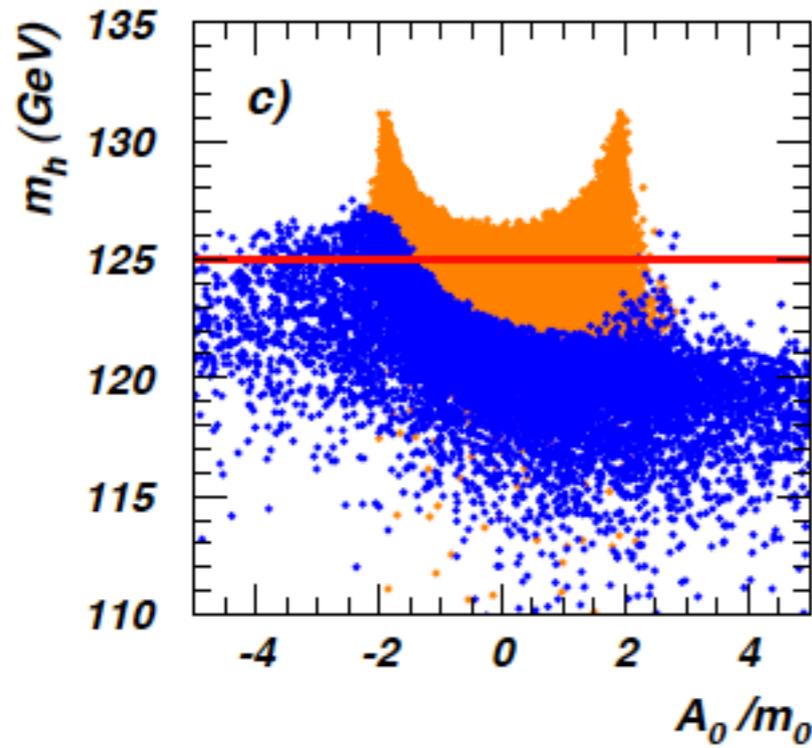
<sup>1</sup>Dept. of Physics and Astronomy, University of Oklahoma, Norman, OK, 73019, USA

<sup>2</sup>Dept. of Physics, University of Wisconsin, Madison, WI 53706, USA

<sup>3</sup>W. L. Fine Institute for Theoretical Physics, University of Minnesota, Minneapolis, MN 55455, USA

PRL109 (2012) 161802

Large value of  $A_t$  reduces  $\Sigma_u^u(\tilde{t}_{1,2})$  contributions to  $\Delta_{EW}$  while uplifting  $m_h$  to  $\sim 125$  GeV



$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[ f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 \left(\frac{1}{4} - \frac{2}{3}x_W\right) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta \left(\frac{1}{4} - \frac{2}{3}x_W\right)$$

$$F(m^2) = m^2 \left( \log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

## #2: Higgs mass or large-log fine-tuning $\Delta_{HS}$

$$m_h^2 \simeq \mu^2 + m_{H_u}^2 + \delta m_{H_u}^2|_{rad}$$

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left( -\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right) \quad X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$$

neglect gauge pieces, S,  $m_{H_u}$  and running;  
then we can integrate from  $m(\text{SUSY})$  to  $\Lambda$

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{\text{SUSY}})$$

$$\Delta_{HS} \sim \delta m_h^2 / (m_h^2/2) < 10$$

$$m_{\tilde{t}_{1,2}, \tilde{b}_1} < 500 \text{ GeV}$$

$$m_{\tilde{g}} < 1.5 \text{ TeV}$$

old natural SUSY

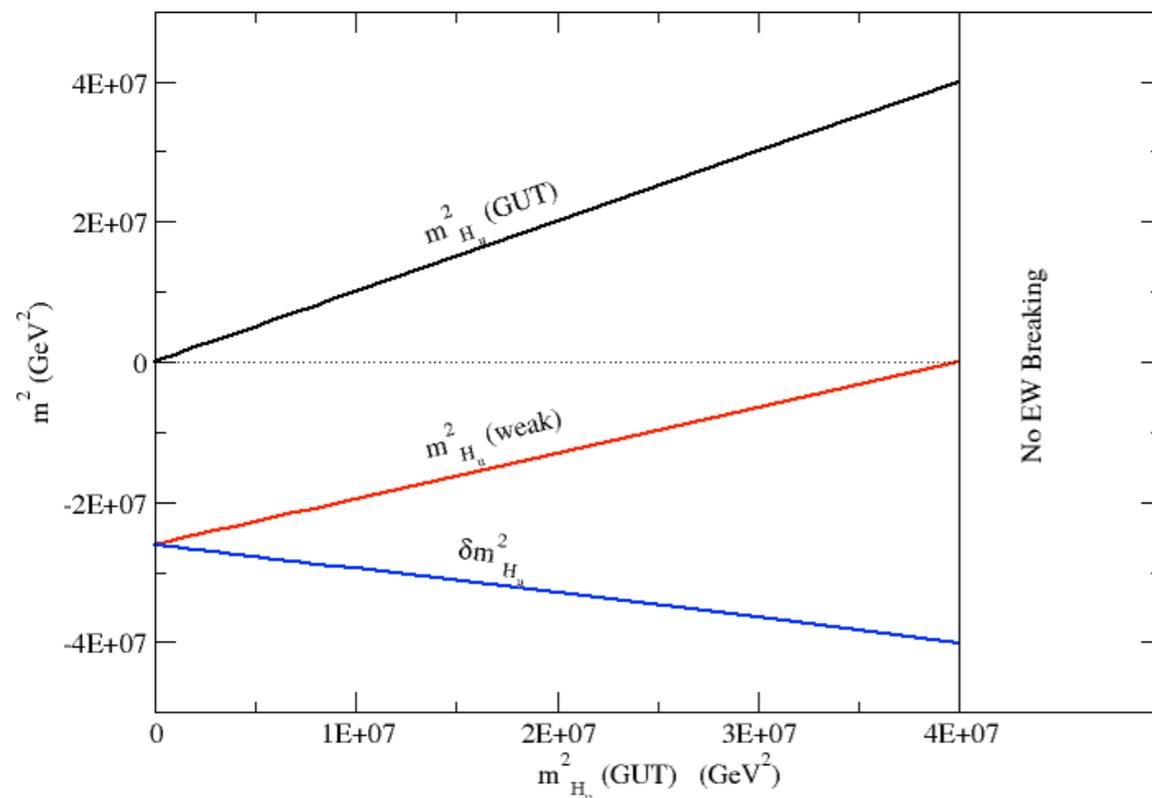
then

$A_t$  can't be too big

What's wrong with this argument?  
 In zeal for simplicity, have made several simplifications: most **egregious** is that one sets  $m(H_u)^2=0$  at beginning to simplify

$m_{H_u}^2(\Lambda)$  and  $\delta m_{H_u}^2$  are *not* independent!

**violates prime directive!**



The larger  $m_{H_u}^2(\Lambda)$  becomes, then the larger becomes the cancelling correction!

To fix: combine dependent terms:

$m_h^2 \simeq \mu^2 + (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2)$  where now both  $\mu^2$  and  $(m_{H_u}^2(\Lambda) + \delta m_{H_u}^2)$  are  $\sim m_Z^2$

After re-grouping:  $\Delta_{HS} \simeq \Delta_{EW}$

Instead of: the radiative correction  $\delta m_{H_u}^2 \sim m_Z^2$   
we now have: the radiatively-corrected  $m_{H_u}^2 \sim m_Z^2$

Recommendation: put this horse out to pasture

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

R.I.P.

sub-TeV 3rd generation squarks **not** required for naturalness

# #3: EENZ/BG traditional measure $\Delta_{BG}$

$$\Delta_{BG} \equiv \max_i [c_i], \quad \text{where } c_i = \left| \frac{\partial \ln m_Z^2}{\partial \ln p_i} \right| = \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

the  $p_i$  constitute the fundamental parameters of the model.

for pMSSM, obviously  $\Delta_{BG} \simeq \Delta_{EW}$

## What about models defined at high scale?

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \mu^2$$



express **weak scale value** in terms of high scale parameters

Express  $m(Z)$  in terms of GUT scale parameters:

$$m_Z^2 \simeq -2m_{H_u}^2 - 2\mu^2 \quad (\text{weak scale relation})$$

$$-2\mu^2(m_{SUSY}) = -2.18\mu^2$$

$$\begin{aligned} -2m_{H_u}^2(m_{SUSY}) = & 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004m_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

all GUT scale parameters

Ibanez, Lopez, Munoz;  
Lleyda, Munoz

Kane, King

Abe, Kobayashi, Omura;  
S. P. Martin

For generic parameter choices,  $\Delta_{BG}$  is large

But if:  $m_{Q_{1,2}} = m_{U_{1,2}} = m_{D_{1,2}} = m_{L_{1,2}} = m_{E_{1,2}} \equiv m_{16}(1,2)$  then  $\sim 0.007m_{16}^2(1,2)$

Even better:  $m_{H_u}^2 = m_{H_d}^2 = m_{16}^2(3) \equiv m_0^2 \Rightarrow -0.017m_0^2$

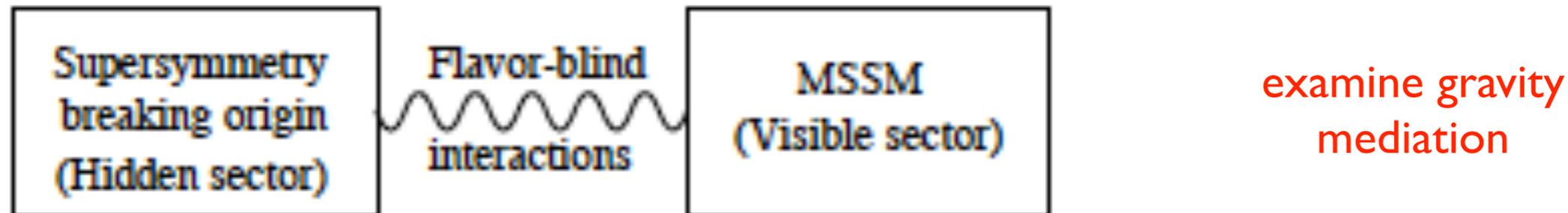
For correlated parameters, EWFT collapses in 3rd gen. sector!

Feng, Matchev, Moroi

- Usually  $\Delta_{BG}$  is applied to *multi-parameter effective theories* where multiple soft terms are adopted as parameter set.
- For these theories, the multiple soft terms parametrize our ignorance of details of the hidden sector SUSY breaking.
- But in supergravity, for any given hidden sector, soft terms are all *dependent* and can be computed as multiples of  $m_{3/2}$ .

Thus, the usual evaluation of  $\Delta_{BG}$  also **violates the prime directive!**

To properly apply BG measure, need to identify  
**independent** soft breaking terms



For any particular SUSY breaking hidden sector,  
 each soft term is some multiple of gravitino mass  $m_{3/2}$

$$m_{H_u}^2 = a_{H_u} \cdot m_{3/2}^2,$$

$$m_{Q_3}^2 = a_{Q_3} \cdot m_{3/2}^2,$$

$$A_t = a_{A_t} \cdot m_{3/2},$$

$$M_i = a_i \cdot m_{3/2},$$

....

Soni, Weldon (1983);  
 Kaplunovsky, Louis (1992);  
 Brignole, Ibanez, Munoz (1993)

Since we don't know hidden sector, we impose parameters  
 which parameterize our ignorance:

**but this doesn't mean each parameter is independent**

e.g. dilaton-dominated SUSY breaking:  $m_0^2 = m_{3/2}^2$  with  $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

Writing each soft term as a multiple of  $m(3/2)$  then we allow for correlations/cancellations:

$$m_Z^2 = -2.18\mu^2 + a \cdot m_{3/2}^2$$

GUT scale param's

numerical co-efficient which depends on hidden sector

for naturalness, then

$$\mu^2 \sim m_Z^2 \quad \text{and} \quad a \cdot m_{3/2}^2 \sim m_Z^2$$

either  $m_{3/2} \sim m_Z$  or  $a$  is small

$$m_Z^2 \simeq -2\mu^2(\text{weak}) - 2m_{H_u}^2(\text{weak}) \simeq -2.18\mu^2(\text{GUT}) + a \cdot m_{3/2}^2$$

then

$$-m_{H_u}^2(\text{weak}) \sim a \cdot m_{3/2}^2 \sim m_Z^2$$

$$\lim_{n_{SSB} \rightarrow 1} \Delta_{BG} \rightarrow \Delta_{EW}$$

Thus, correctly applying these measures by first collecting dependent quantities, we find that— at tree level— all agree:

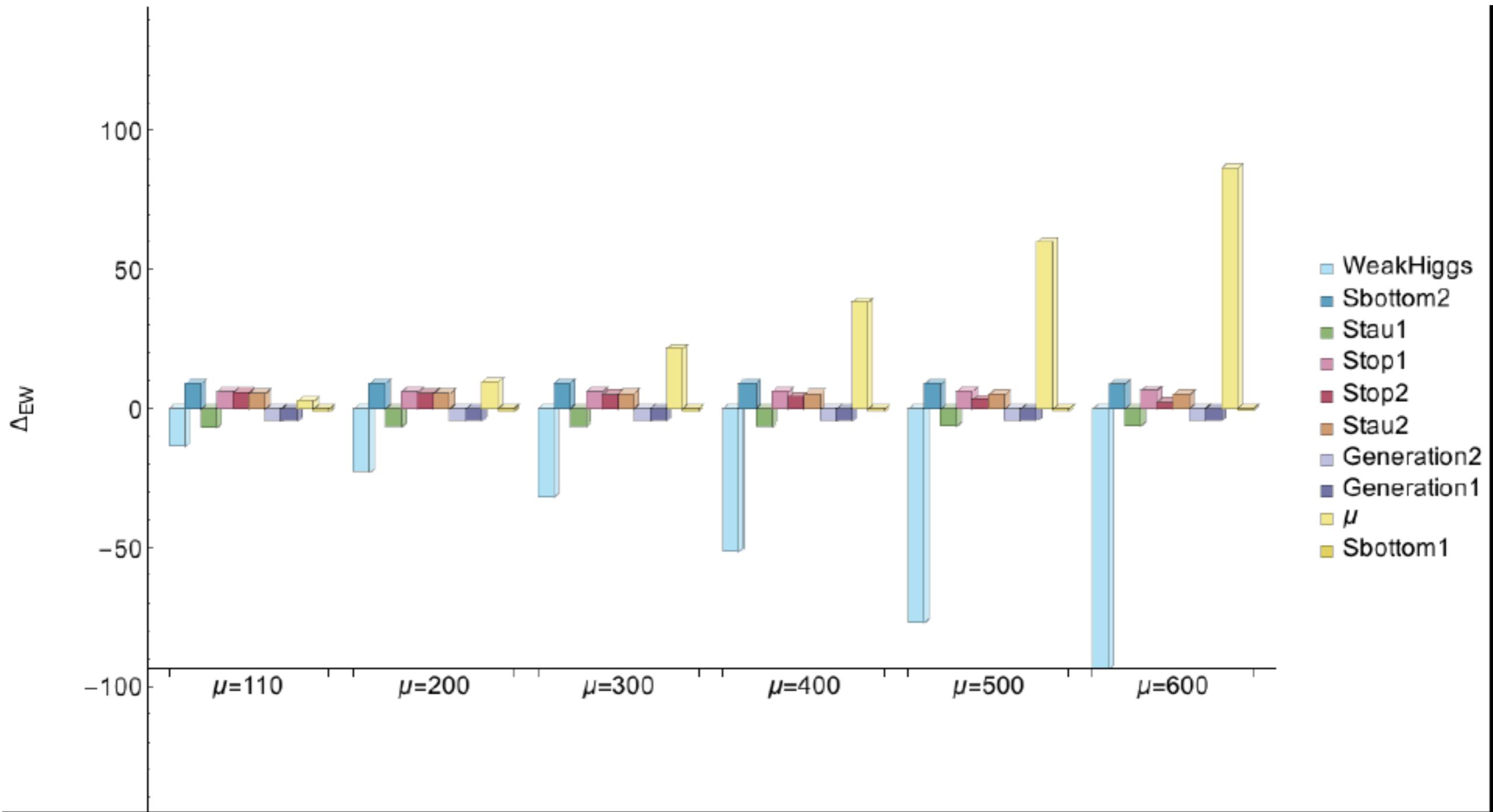
$$\Delta_{HS} \simeq \Delta_{BG} \simeq \Delta_{EW}$$

Due to ease of use and including radiative corrections, and due to its explicit model independence, we will use

$\Delta_{EW}$   
for remainder of talk

hard wired in  
Isasugra

# How much is too much fine-tuning?

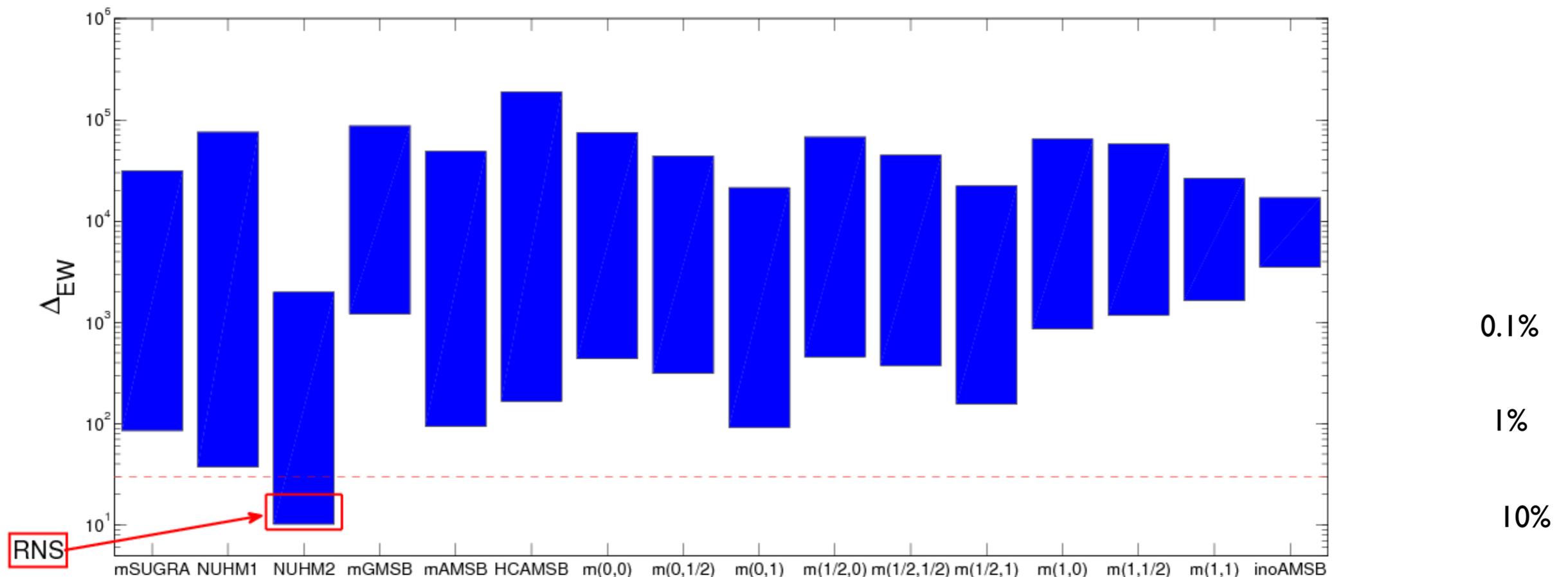


Visually, large fine-tuning has already developed by  $\mu \sim 350$  or  $\Delta_{EW} \sim 30$

$\Delta_{EW}$  is highly selective:  
 most constrained models are ruled out  
 except NUHM2 and its generalizations:

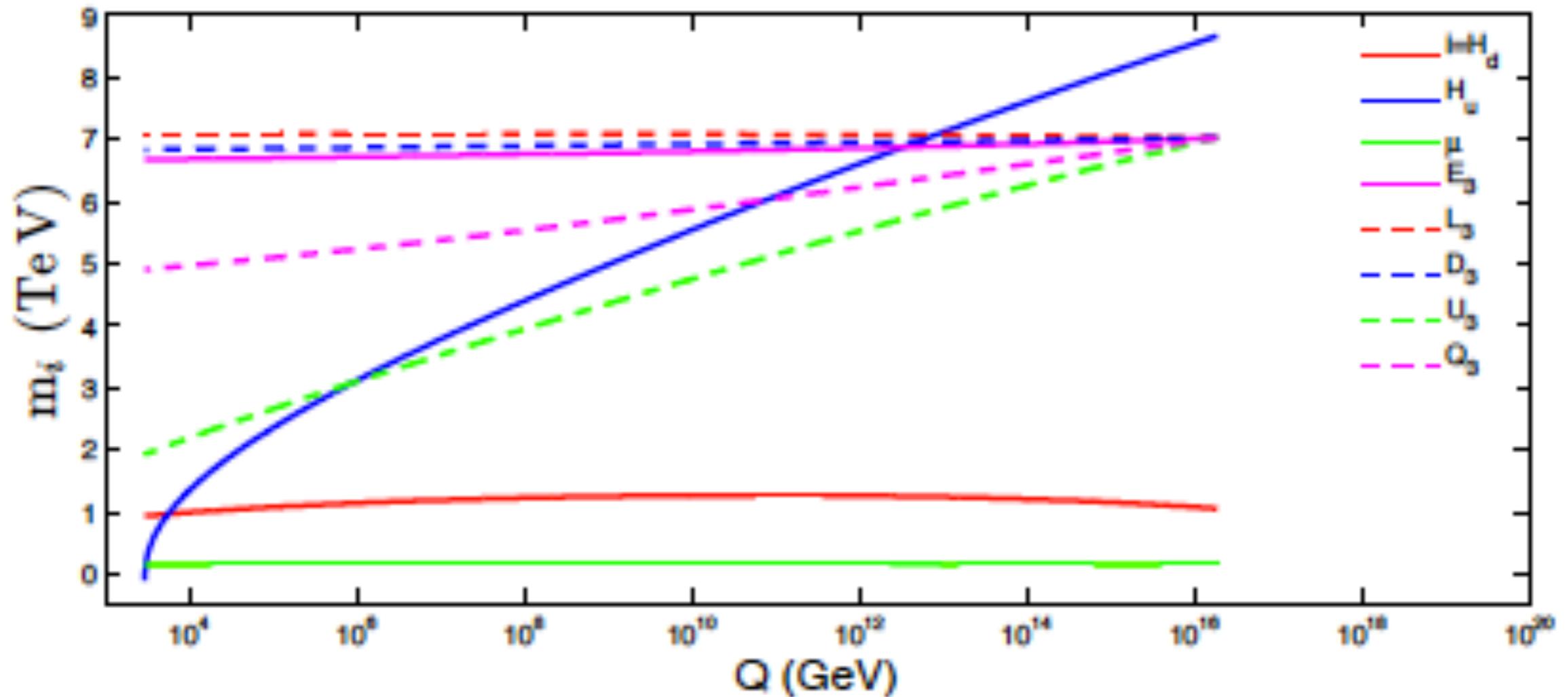
J. Ellis, K. Olive and Y. Santoso, *Phys. Lett. B* 539 (2002) 107; J. Ellis, T. Falk, K. Olive and Y. Santoso, *Nucl. Phys. B* 652 (2003) 259; H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, *J. High Energy Phys.* 0507 (2005) 065.

scan over p-space with  $m(h)=125.5\pm 2.5$  GeV:



HB, Barger, Mickelson, Padelfke-Kirkland, PRD89 (2014) 115019

Applied properly, all three measures agree:  
**naturalness is unambiguous and highly predictive!**



Radiatively-driven natural SUSY, or RNS:

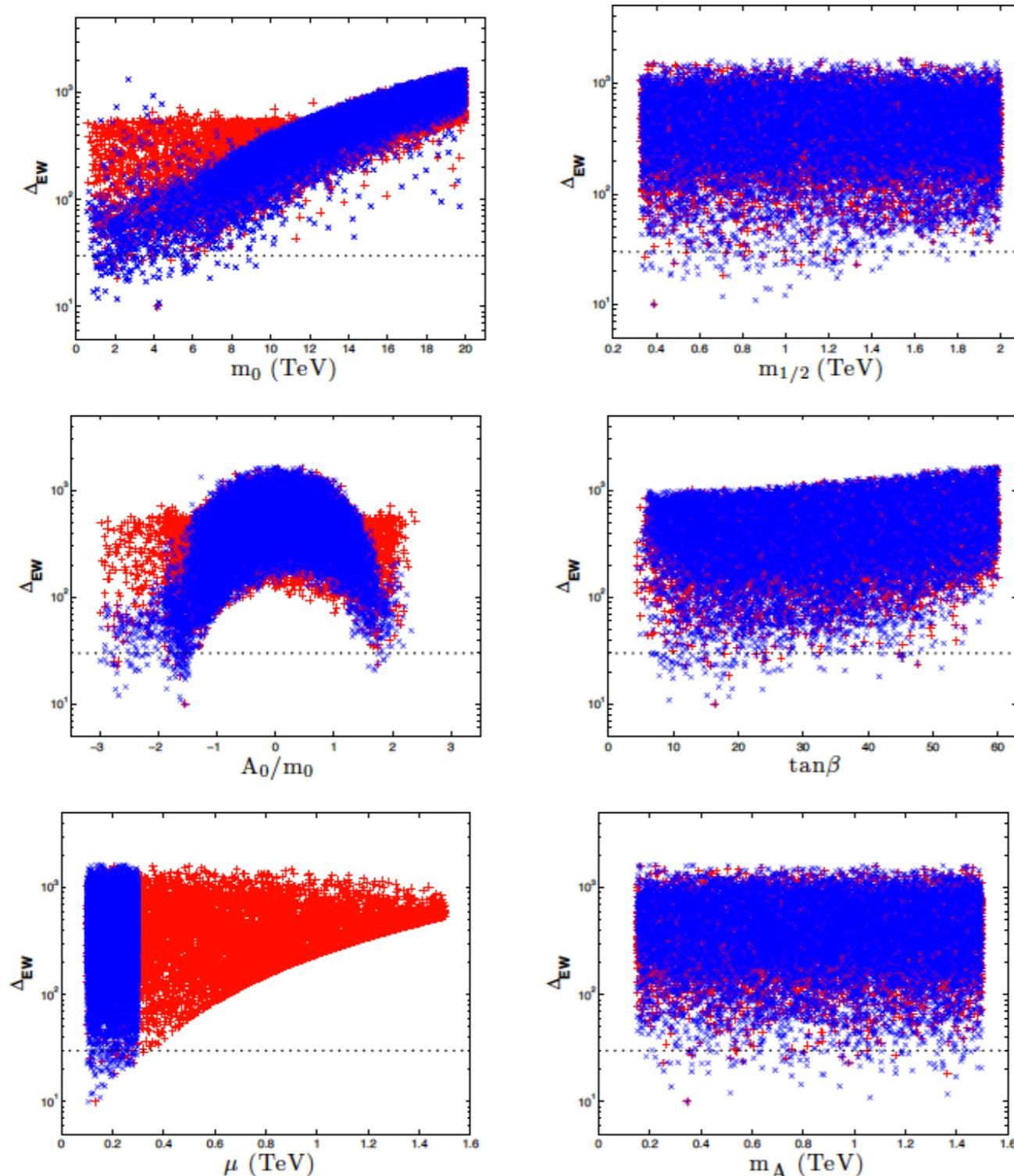
(typically need  $m_{Hu} \sim 25\text{--}50\%$  higher than  $m_0$ )

H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [arXiv:1212.2655 [hep-ph]].

Which parameter choices lead to low  
EWFT and how low can  $\Delta_{EW}$  be?

get upper bounds on parameters and spectra!

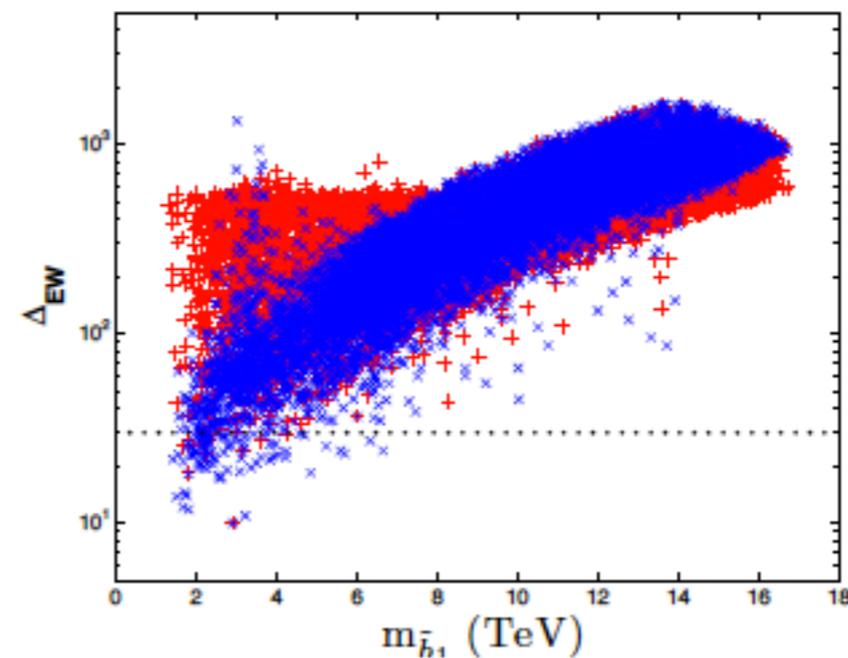
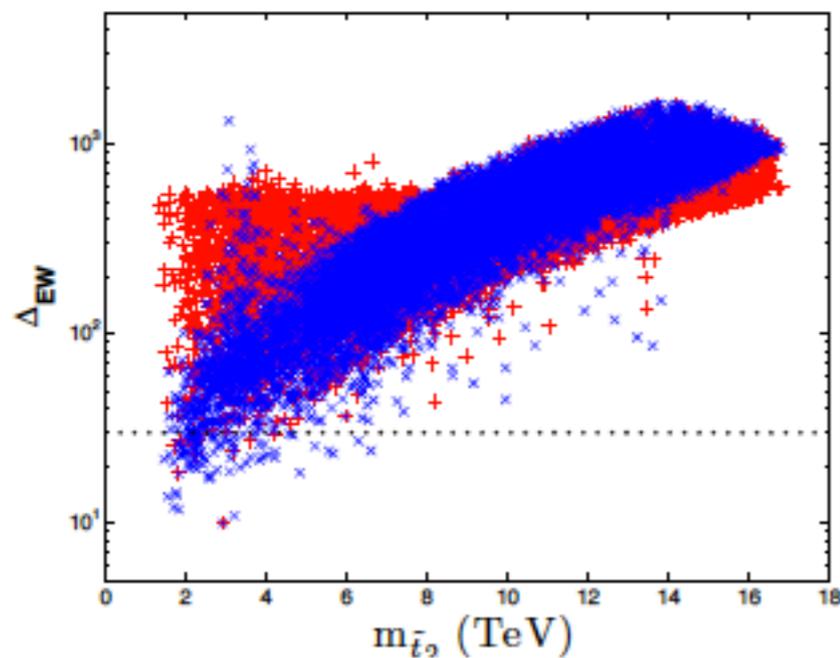
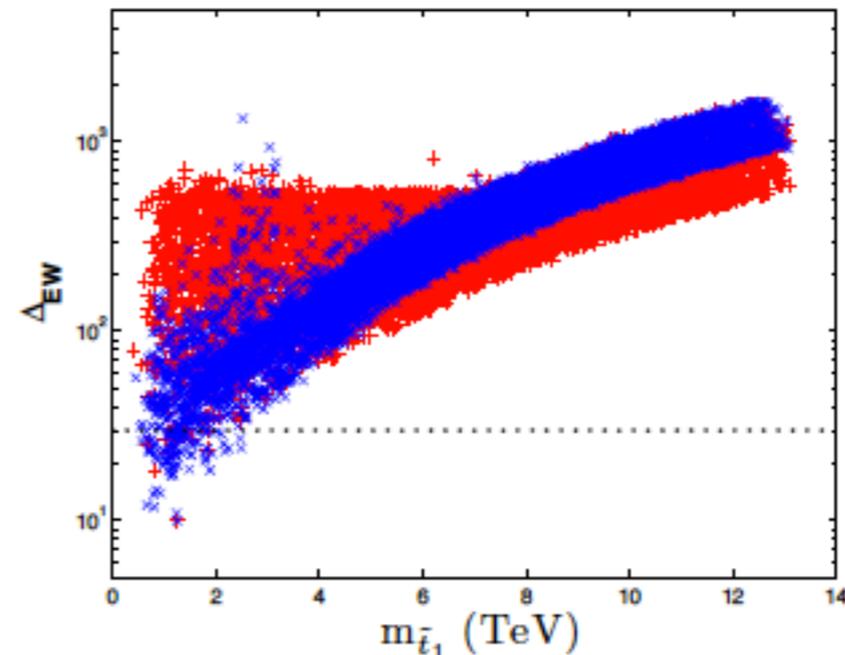
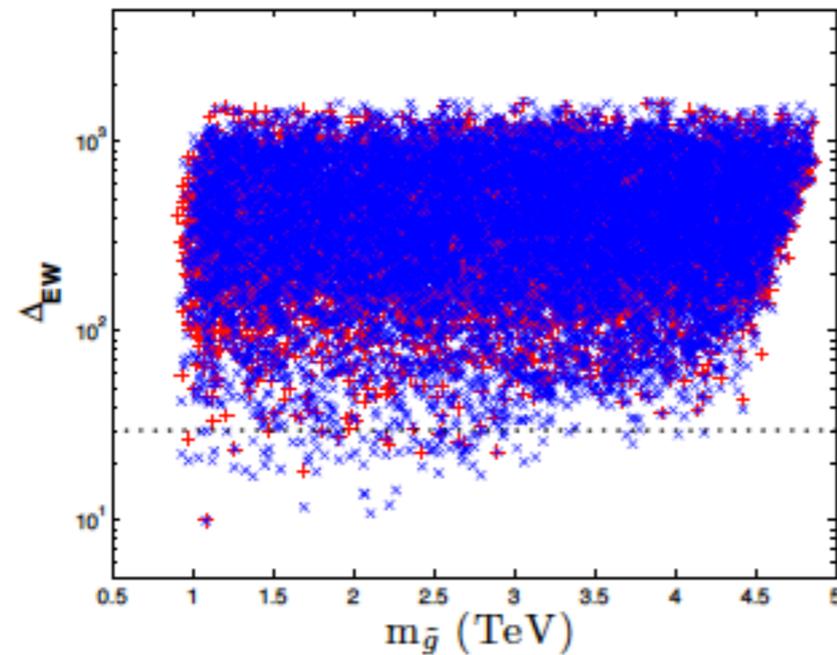


$\Delta_{EW} \sim 10$  or 10% *EWFT*

High-scale models with  
low  $\Delta_{EW}$  :

HB, Barger, Huang, Mickelson, Mustafayev, Tata,  
arXiv:1212.2655

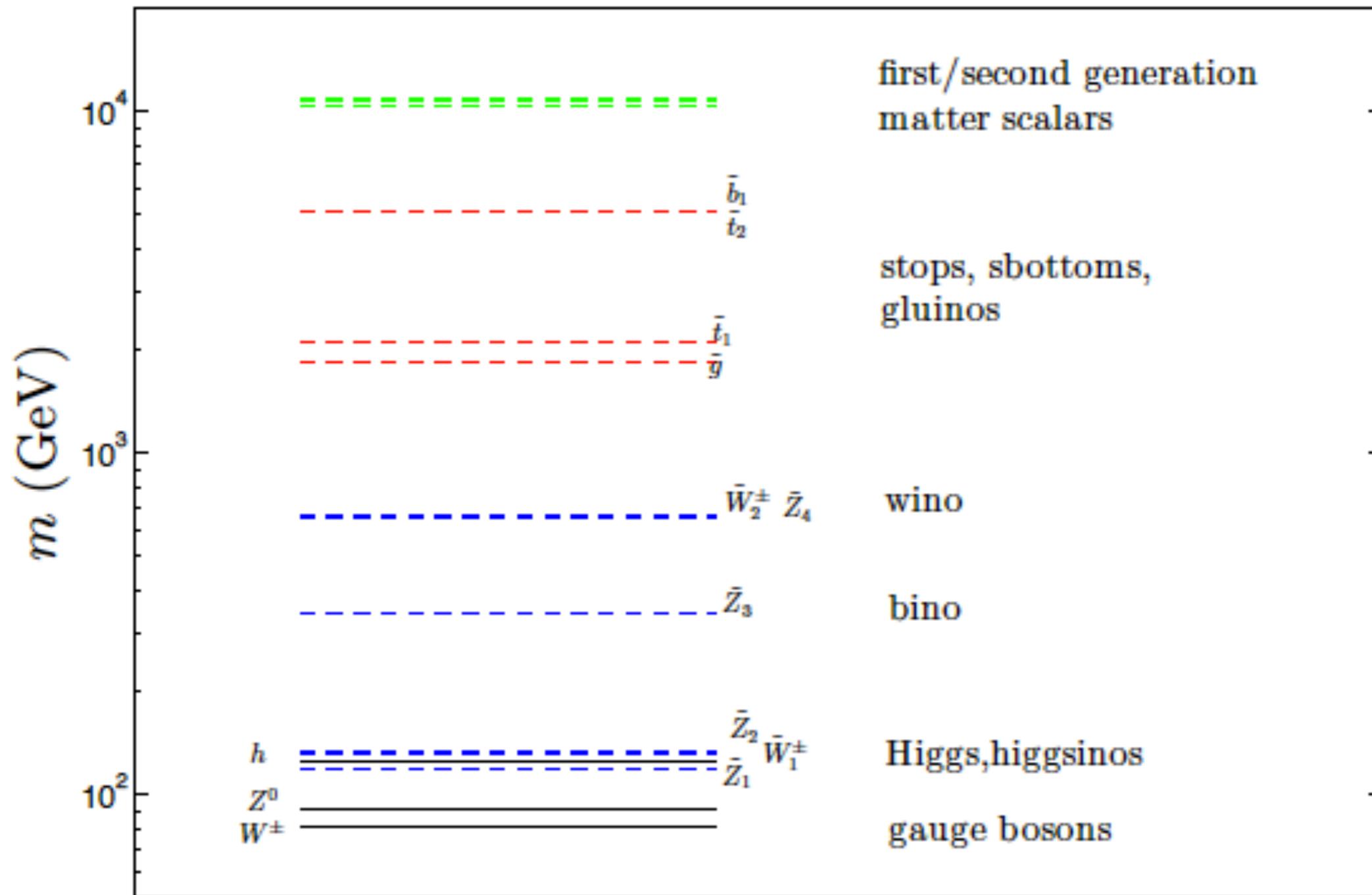
# Upper bounds on sparticle masses:



$m(\tilde{t}_1) \sim 1-3$  TeV  
 $m(\tilde{t}_2, \tilde{b}_1) \sim 2-4$  TeV  
 $m(\tilde{g}, \tilde{l}_n) \sim 1-4$  TeV

higher than old NS models and  
allows for  $m(h) \sim 125$  GeV within MSSM

# Typical spectrum for low $\Delta_{EW}$ models



There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

SUSY  $\mu$  problem:  $\mu$  term is SUSY, not SUSY breaking:  
expect  $\mu \sim M(\text{Pl})$  but phenomenology requires  $\mu \sim m(\text{Z})$

- NMSSM:  $\mu \sim m(3/2)$ ; beware singlets!
- Giudice–Masiero:  $\mu$  forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- Kim–Nilles: invoke SUSY version of DFSZ axion  
solution to strong CP:

KN: PQ symmetry forbids  $\mu$  term,  
but then it is generated via PQ breaking

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$\mu \sim \lambda f_a^2 / M_P$$

$$m_{3/2} \sim m_{hid}^2 / M_P$$

$$f_a \ll m_{hid}$$

Higgs mass tells us where  
to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

# Little Hierarchy from radiative PQ breaking? exhibited within context of MSY model

Murayama, Suzuki, Yanagida (1992);

Gherghetta, Kane (1995)

Choi, Chun, Kim (1996)

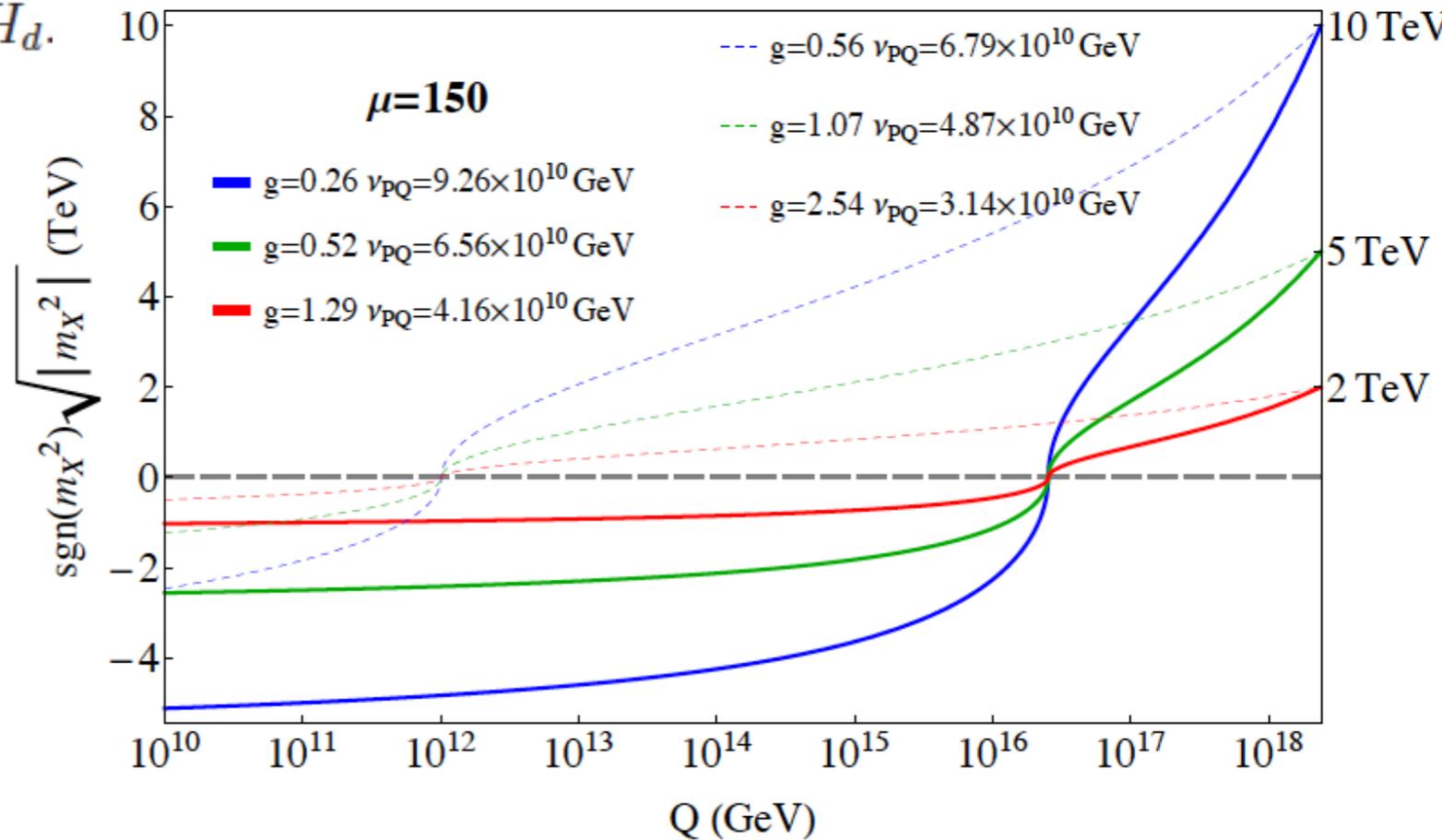
Bae, HB, Serce, PRD91 (2015) 015003

augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

$$M_{N_i^c} = v_X h_i |_{Q=v_X}$$

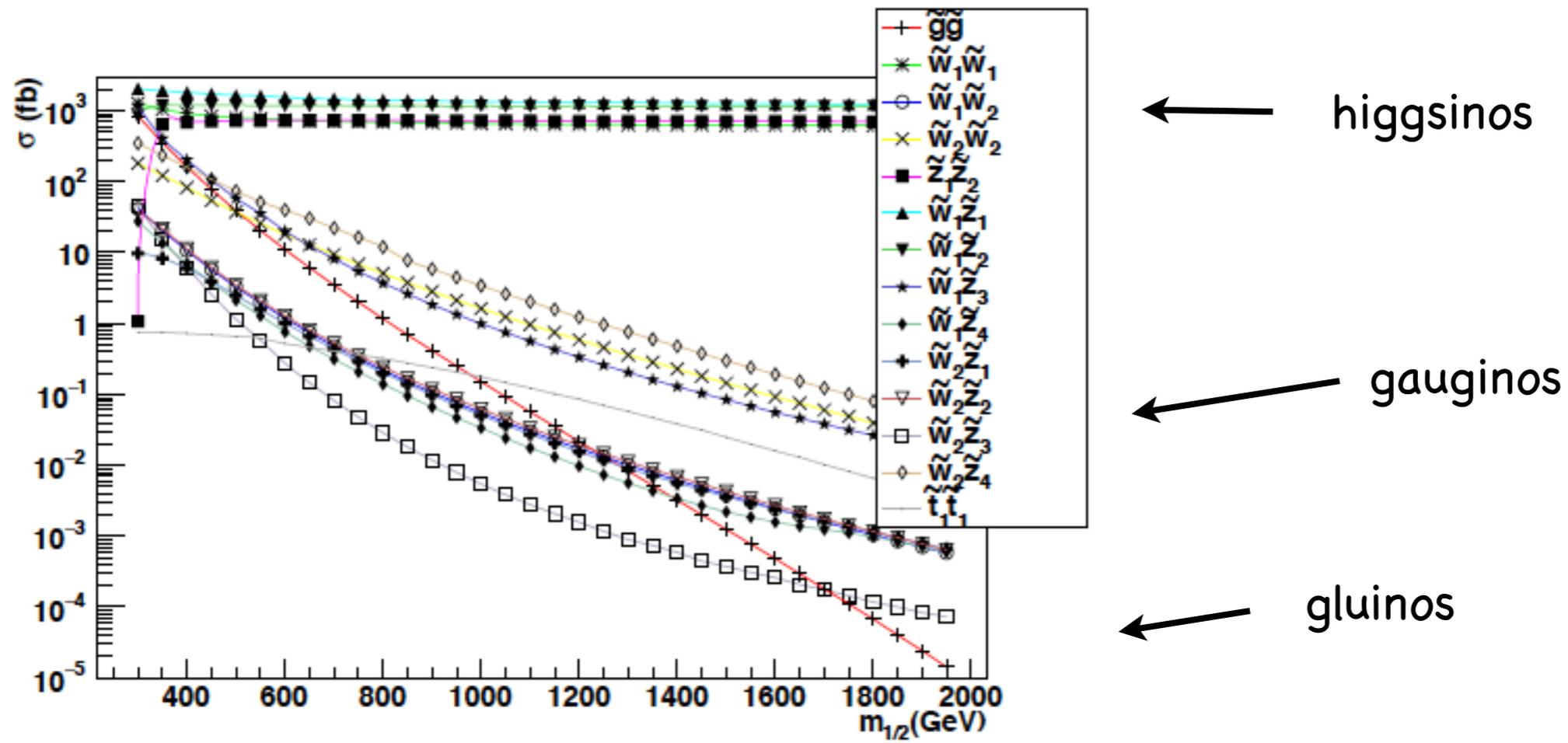
$$\mu = g \frac{v_X v_Y}{M_P}.$$



Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

# Prospects for discovering RNS at LHC and ILC

# Sparticle prod'n along RNS model-line at LHC14:



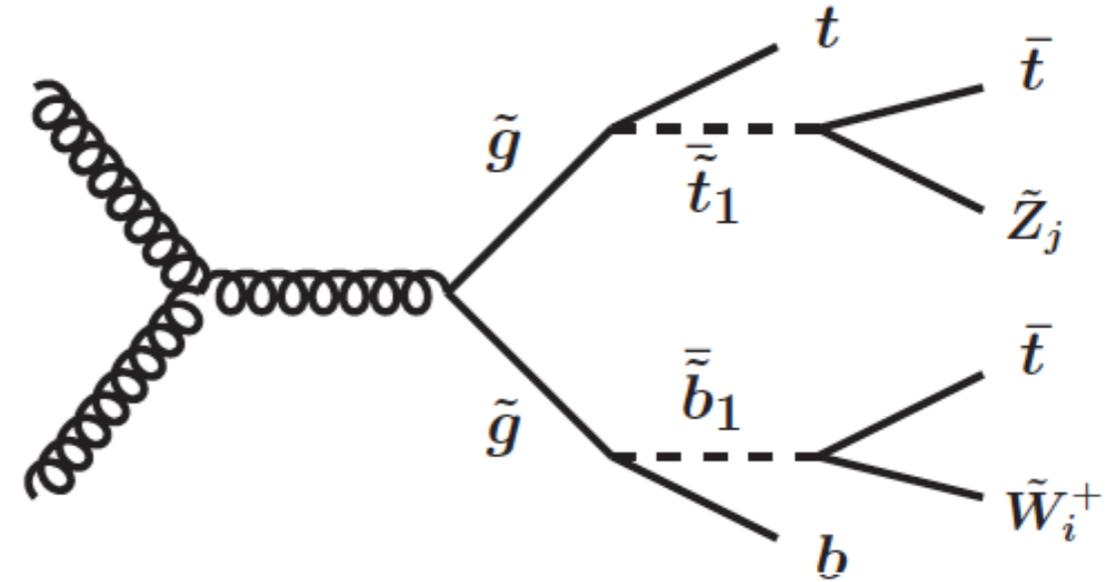
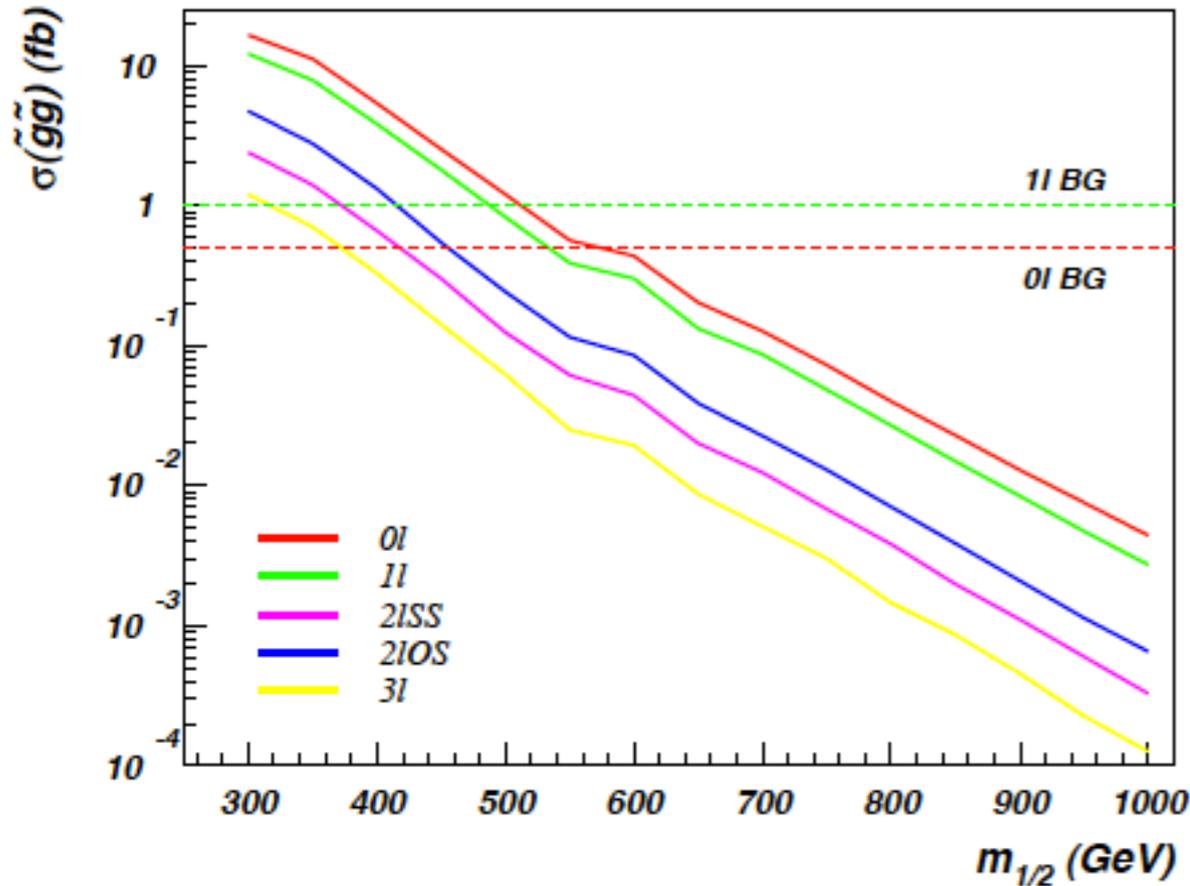
higgsino pair production dominant—but only soft visible energy release from higgsino decays

largest visible cross section: **wino pairs**

gluino pairs sharply dropping

# gluino pair cascade decay signatures

NUHM2:  $m_0=5\text{ TeV}$ ,  $A_0=-1.6m_0$ ,  $\tan\beta=15$ ,  $\mu=150\text{ GeV}$ ,  $m_A=1\text{ TeV}$



Particle	dom. mode	BF
$\tilde{g}$	$\tilde{t}_1 t$	$\sim 100\%$
$\tilde{t}_1$	$b\tilde{W}_1$	$\sim 50\%$
$\tilde{Z}_2$	$\tilde{Z}_1 f\bar{f}$	$\sim 100\%$
$\tilde{Z}_3$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{Z}_4$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{W}_1$	$\tilde{Z}_1 f\bar{f}'$	$\sim 100\%$
$\tilde{W}_2$	$\tilde{Z}_i W$	$\sim 50\%$

Table 1: Dominant branching fractions of various sparticles along the RNS model line for  $m_{1/2} = 1\text{ TeV}$ .

Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$
10	1.4
100	1.6
300	1.7
1000	1.9

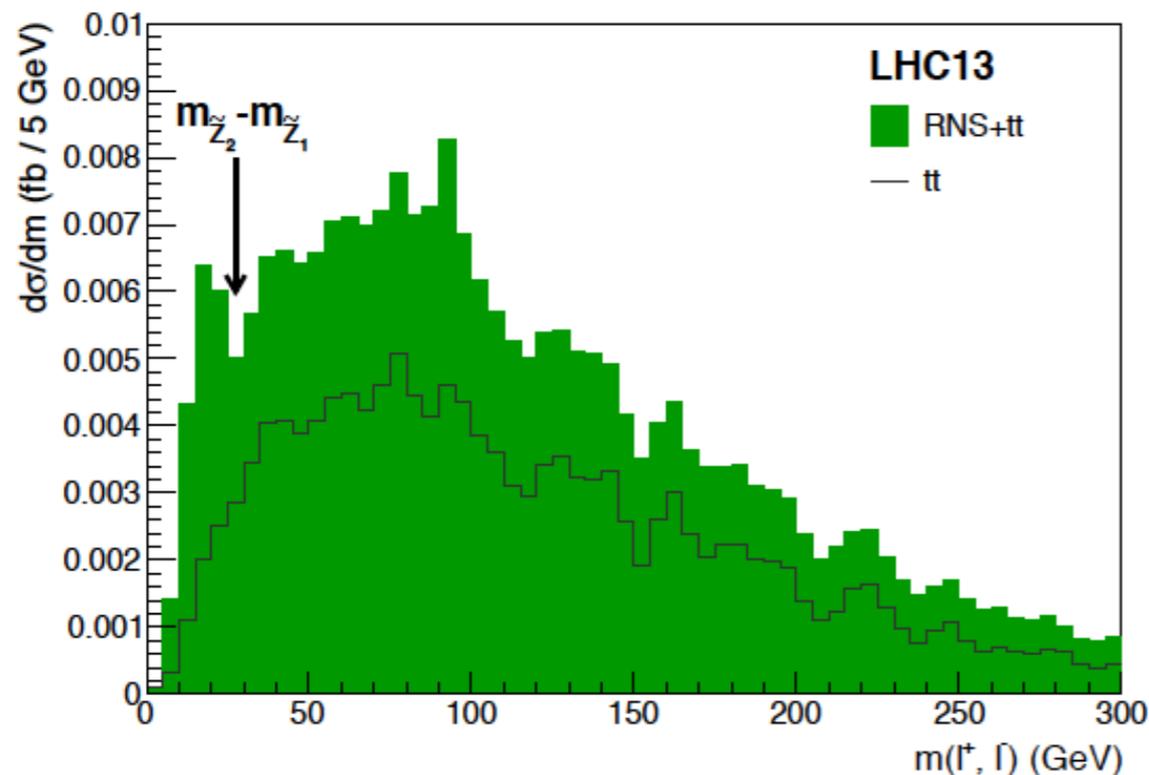
LHC14 reach  
in  $m(\text{gluino})$  (TeV)

since  $m(\text{gluino})$  extends to  $\sim 5\text{ TeV}$ ,  
**LHC14 can see about half** the natural SUSY  
parameter space in these modes

# LHC14 has some reach for RNS; if a signal is seen, should be characteristic

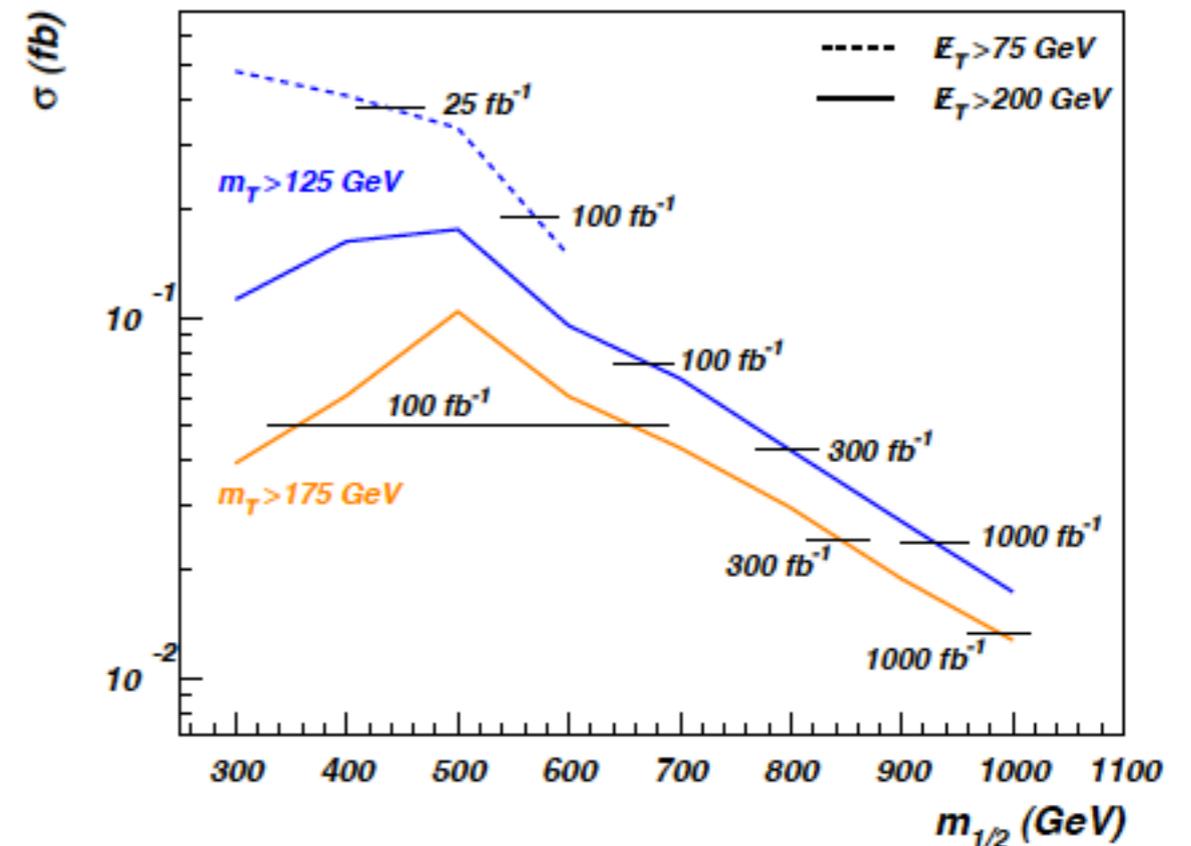
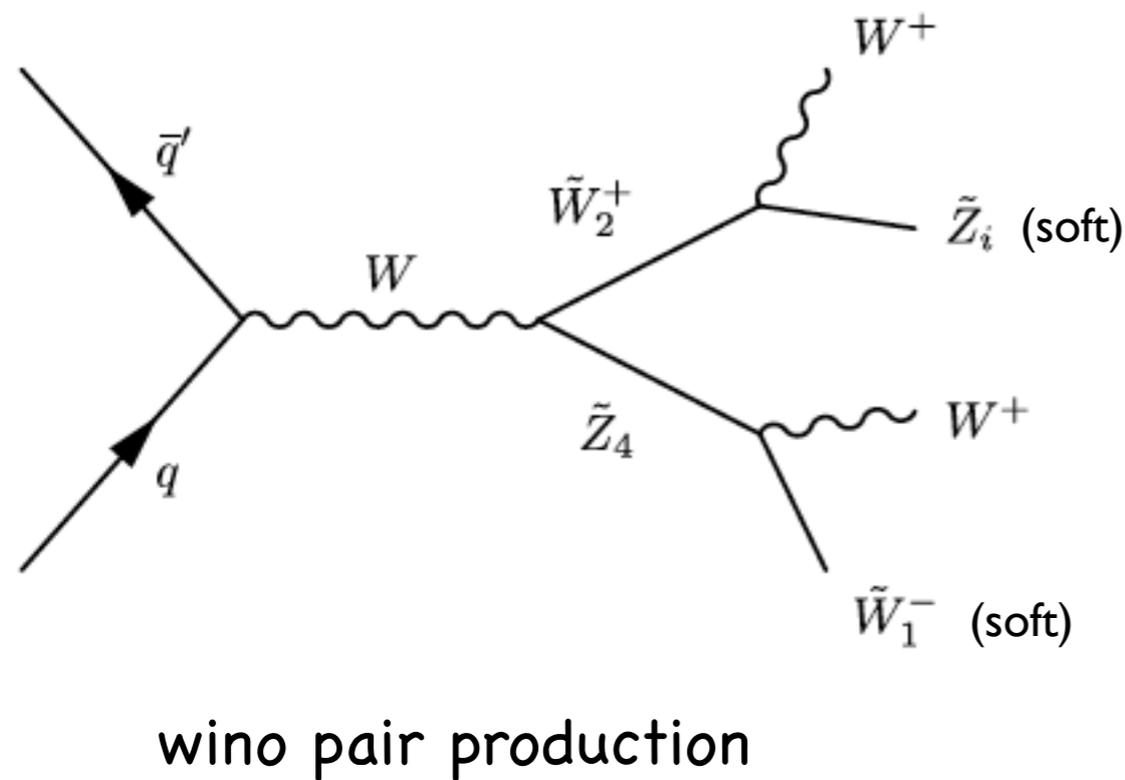
Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$	SSdB	$WZ \rightarrow 3\ell$	$4\ell$
10	1.4	–	–	–
100	1.6	1.6	–	$\sim 1.2$
300	1.7	2.1	1.4	$\gtrsim 1.4$
1000	1.9	2.4	1.6	$\gtrsim 1.6$

$5\sigma$  reach of LHC14 in terms of  $m_{\tilde{g}}$  for various Int. Lum.



OS/SF dilepton mass  
edge apparent from  
cascade decays  
with  $z_2 \rightarrow z_1 + l + l\bar{l}$

# Characteristic same-sign diboson (SSdB) signature from SUSY models with light higgsinos!

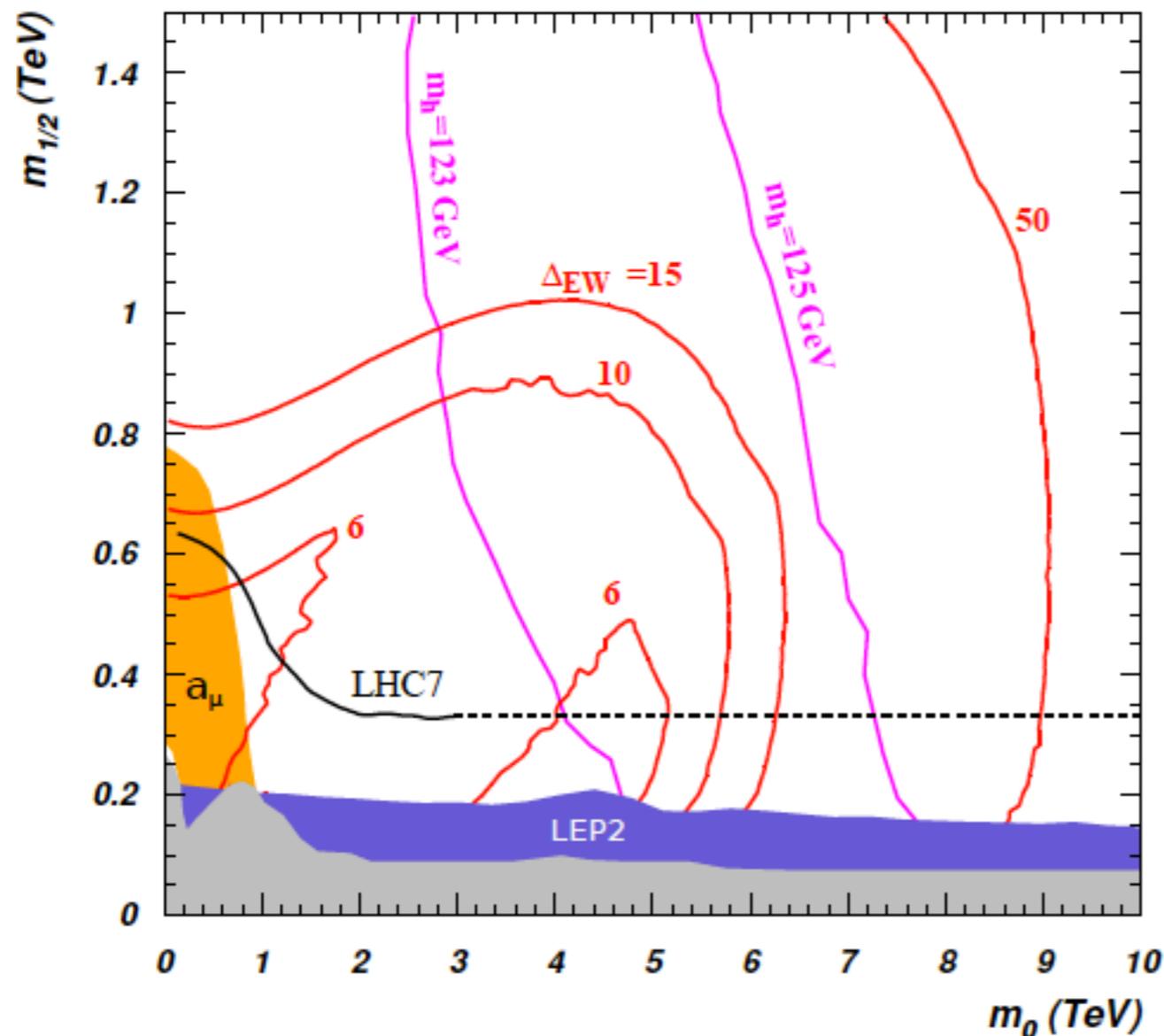


This channel offers best reach of LHC14 for RNS;  
it is also indicative of wino-pair prod'n  
followed by decay to higgsinos

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev, W. Sreethawong and X. Tata,  
*Phys. Rev. Lett.* **110** (2013) 151801.

# Good old $m_0$ vs. $m_{1/2}$ plane still viable, but require low $\mu$ (NUHM2)

NUHM2:  $\tan\beta=10$ ,  $A_0=-1.6m_0$ ,  $\mu=150$  GeV,  $m_t=173.2$  GeV

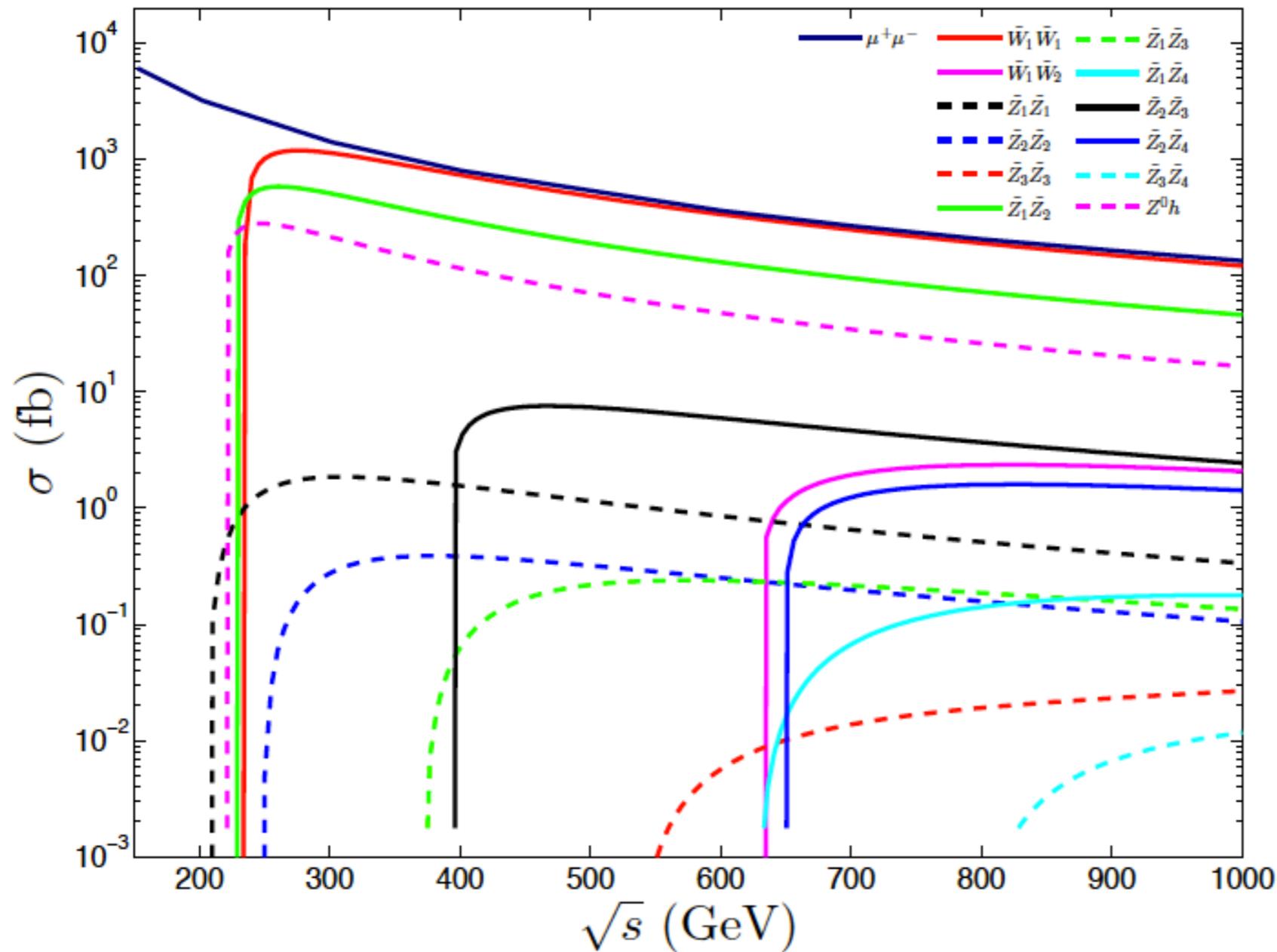


$\mu = 150$  GeV throughout which is allowed for NUHM2

# Smoking gun signature: light higgsinos at ILC:

ILC is Higgs/higgsino factory!

ILC1:  $m_0 = 7025$  GeV,  $m_{1/2} = 568.3$  GeV,  $A_0 = -11426.6$  GeV,  $\tan\beta = 10$ ,  $\mu = 115$  GeV,  $m_A = 1000$  GeV



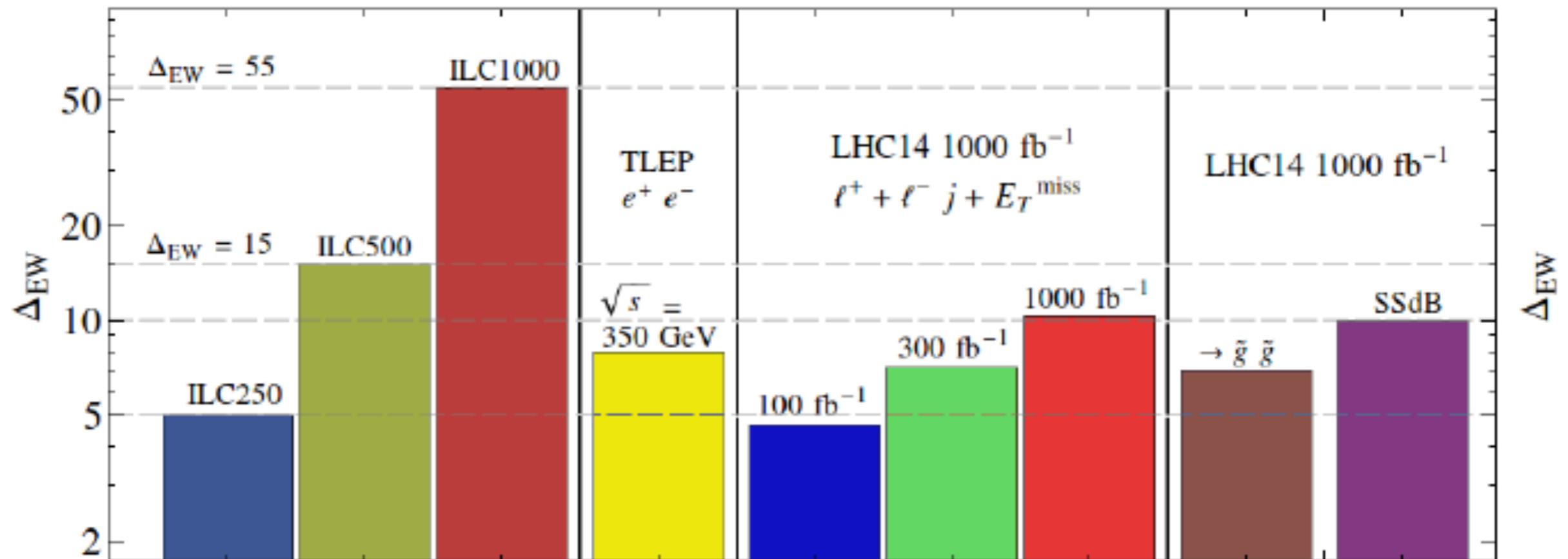
$$\sigma(\text{higgsino}) \gg \sigma(Zh)$$

10–15 GeV higgsino mass  
gaps no problem  
in clean ILC environment

HB, Barger, Mickelson, Mustafayev, Tata  
arXiv:1404.7510

ILC either sees light higgsinos or natural SUSY dead

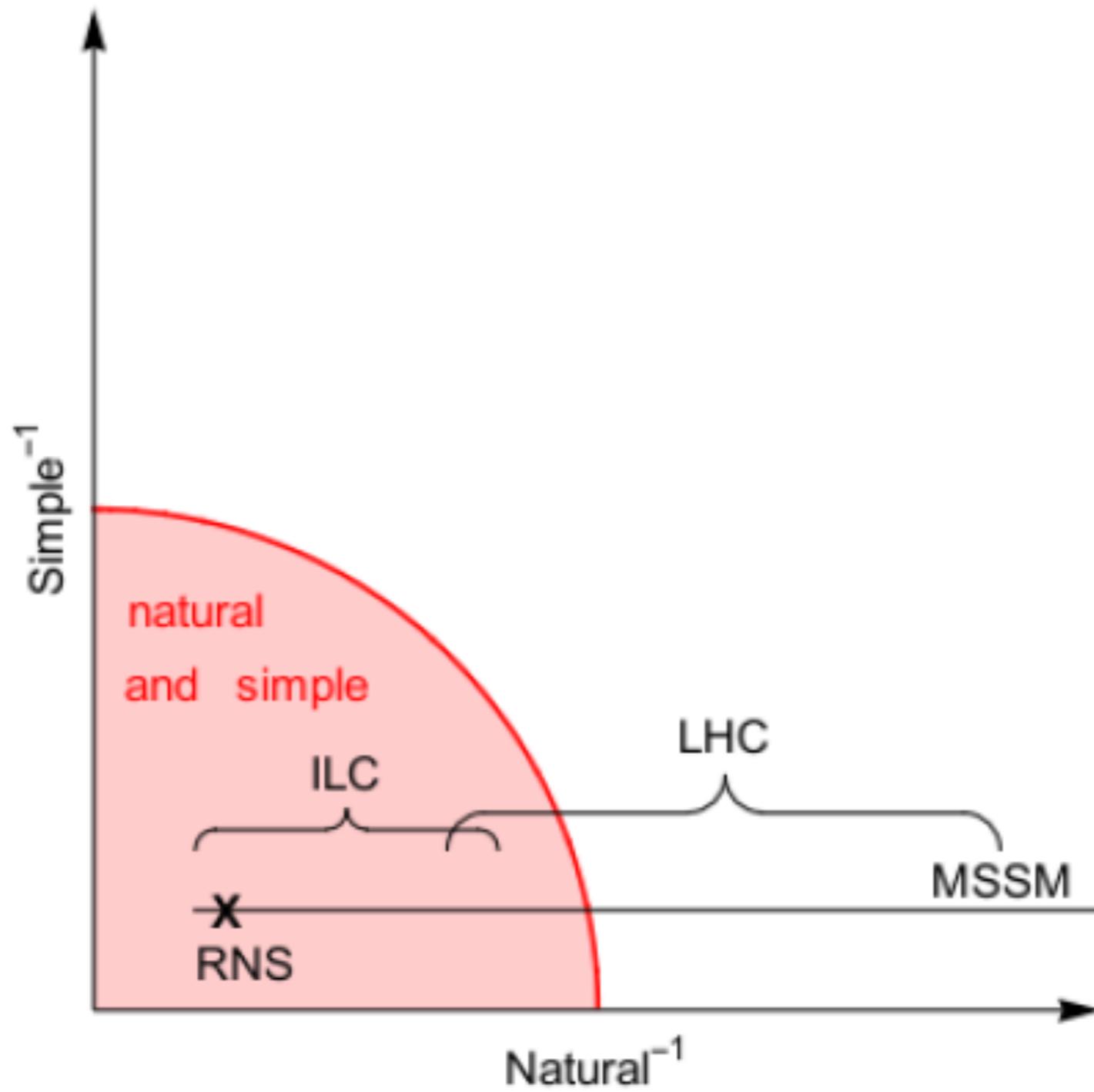
# Future collider reach for naturalness



When to give up on naturalness in SUSY?  
 If ILC(600-700 GeV) sees no light higgsinos

# Conclusions: status of SUSY post LHC8

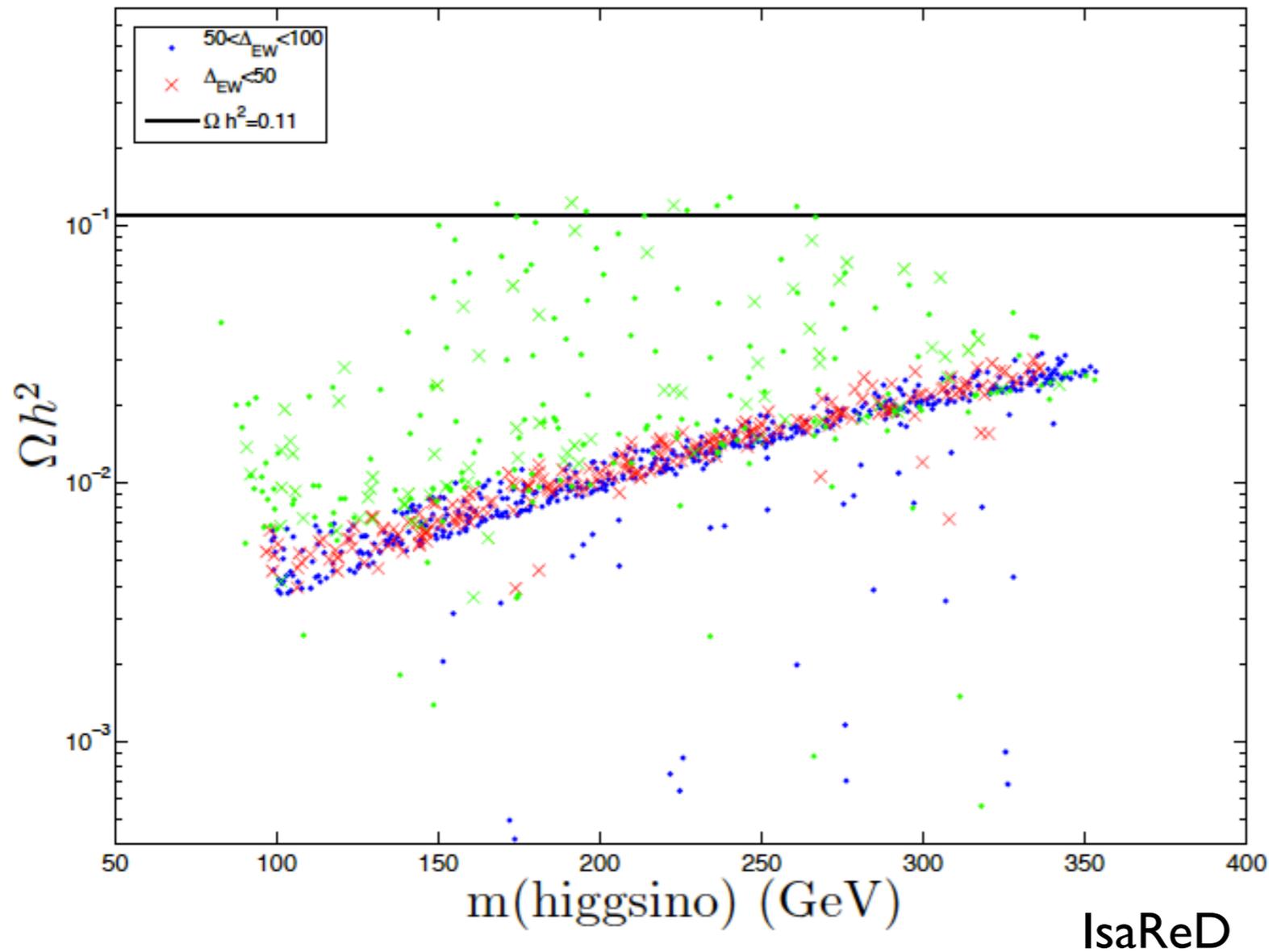
- SUSY EWFT **non-crisis**: EWFT allowed at 10% level in radiatively-driven natural SUSY: SUGRA GUT paradigm is just fine in NUHM2 but CMSSM/others fine-tuned
- naturalness maintained for  $\mu \sim 100\text{--}200$  GeV;  $t_1 \sim 1\text{--}2$  TeV,  $t_2 \sim 2\text{--}4$  TeV, highly mixed;  $m(\tilde{g}, \tilde{u}) \sim 1\text{--}5$  TeV
- LHC14 w/  $300 \text{ fb}^{-1}$  can see about half of RNS parameter space
- **$e^+e^-$  collider with  $\sqrt{s} \sim 500\text{--}600$  GeV needed to find predicted light higgsino states**
- Discovery of and precision measurements of light higgsinos at ILC!
- RNS spectra characterized by mainly higgsino-like WIMP: standard relic underabundance
- SUSY DFSZ/MSY invisible axion model:  
solves strong CP and  $\mu$  problems while allowing for  $\mu \sim m(Z)$
- Expect mainly axion CDM with 5–10% higgsino-like WIMPs over much of p-space
- Ultimately detect **both axion and higgsino-like WIMP**



Backup..

Dark matter in RNS

# Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;  
red/blue: allowed

HB, Barger, Mickelson

Factor of 10–15 too low

But so far we have addressed only **Part 1**  
of fine-tuning problem:

In QCD sector, the term  $\frac{\bar{\theta}}{32\pi^2} F_{A\mu\nu} \tilde{F}_A^{\mu\nu}$  must occur

But neutron EDM says it is not there: strong CP problem

(frequently ignored by SUSY types)

Best solution after 35 years:

PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

Changes DM calculus:

expect mixed WIMP/axion DM (**2 particles**)

## Axion cosmology

★ Axion field eq'n of motion:  $\theta = a(x)/f_a$

$$- \ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$$

$$- V(\theta) = m_a^2(T) f_a^2 (1 - \cos \theta)$$

– Solution for  $T$  large,  $m_a(T) \sim 0$ :

$$\theta = \text{const.}$$

–  $m_a(T)$  turn-on  $\sim 1$  GeV

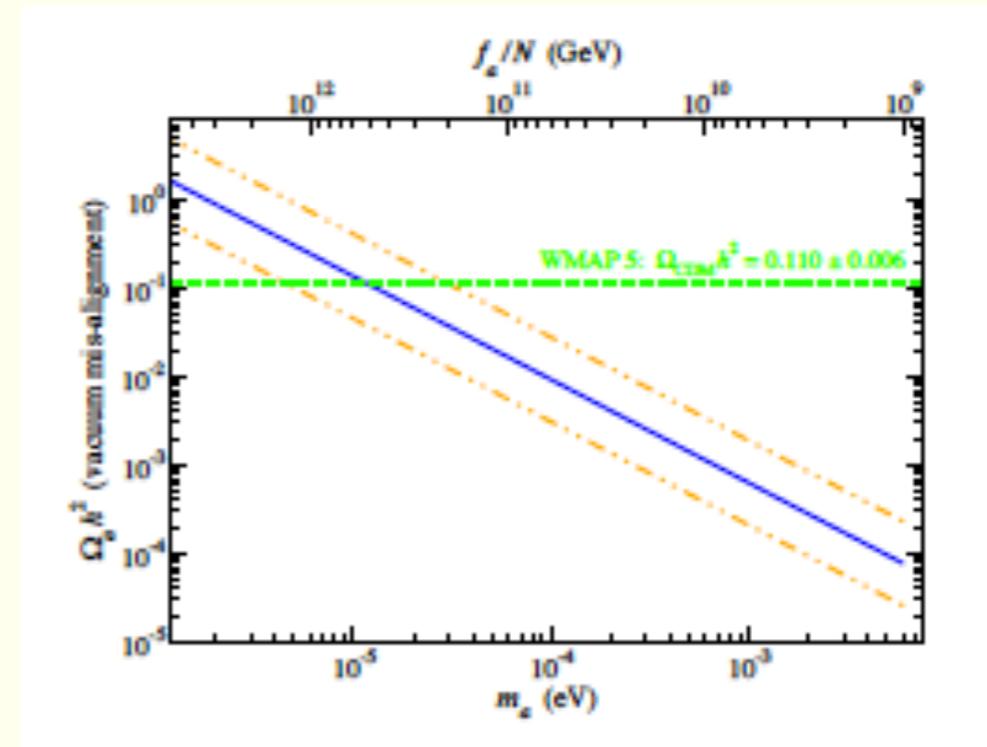
★  $a(x)$  oscillates,

creates axions with  $\vec{p} \sim 0$ :

production via vacuum mis-alignment

$$\star \Omega_a h^2 \sim \frac{1}{2} \left[ \frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$$

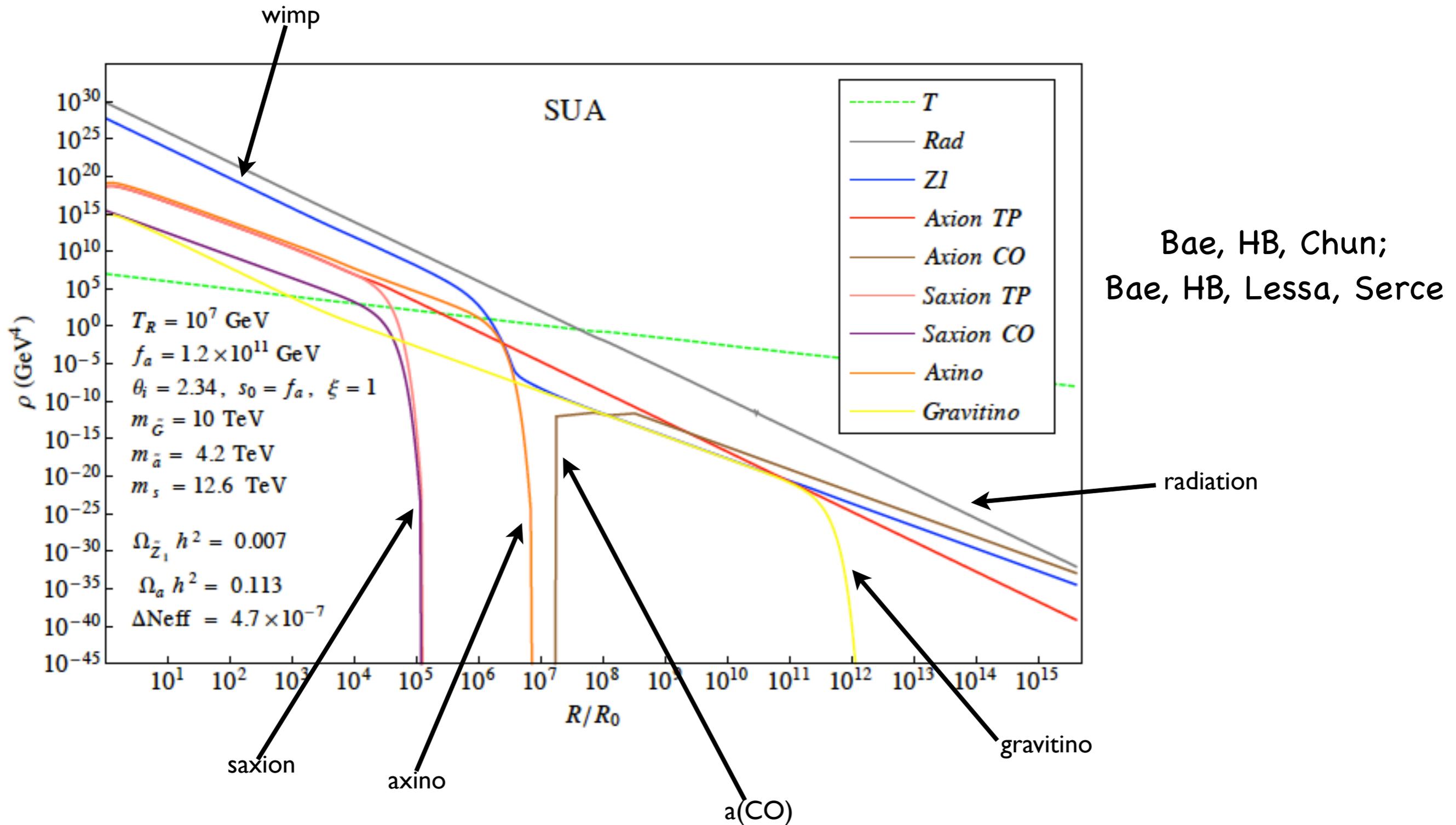
★ astro bound: stellar cooling  $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$

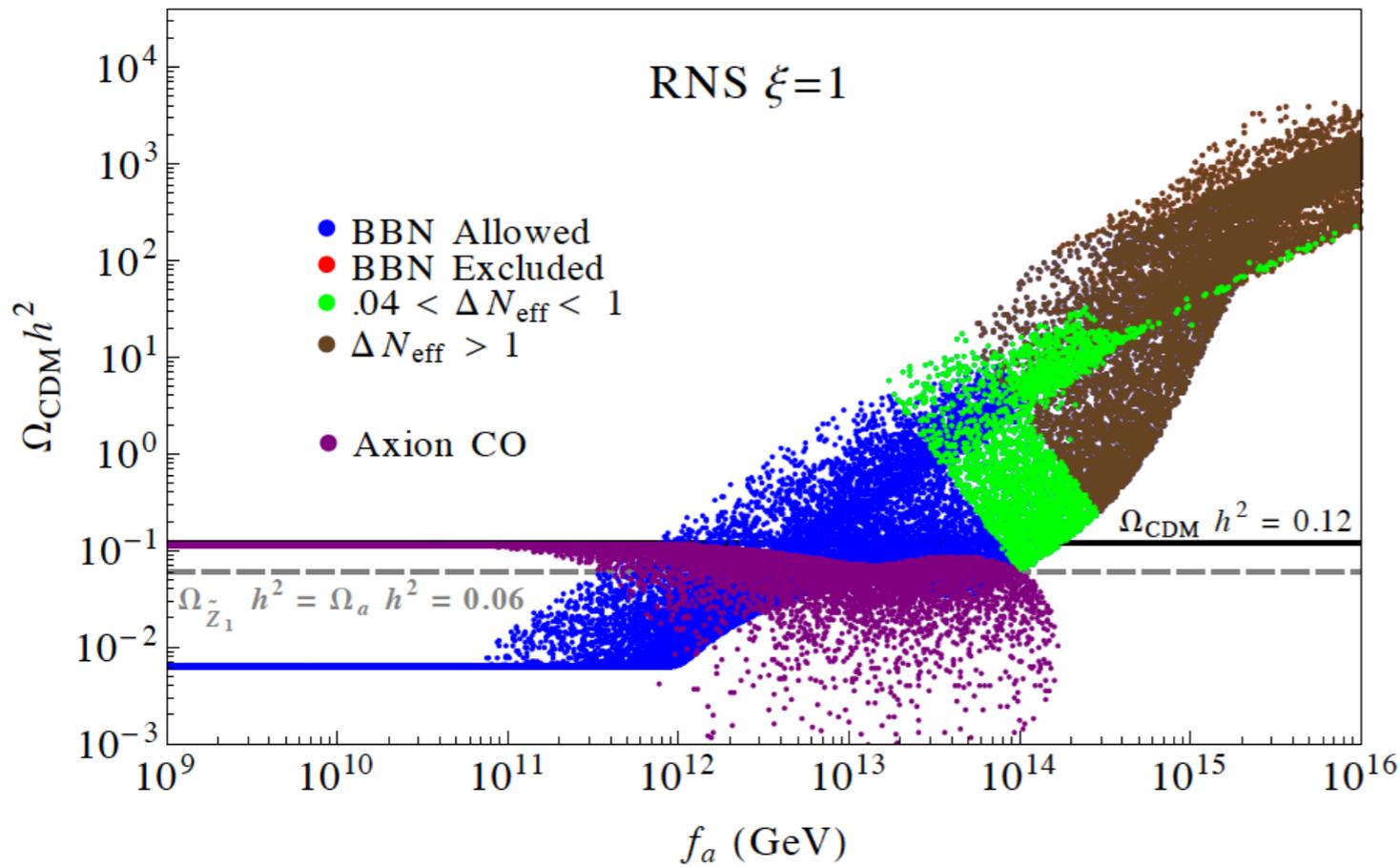


# mixed axion-neutralino production in early universe

- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY

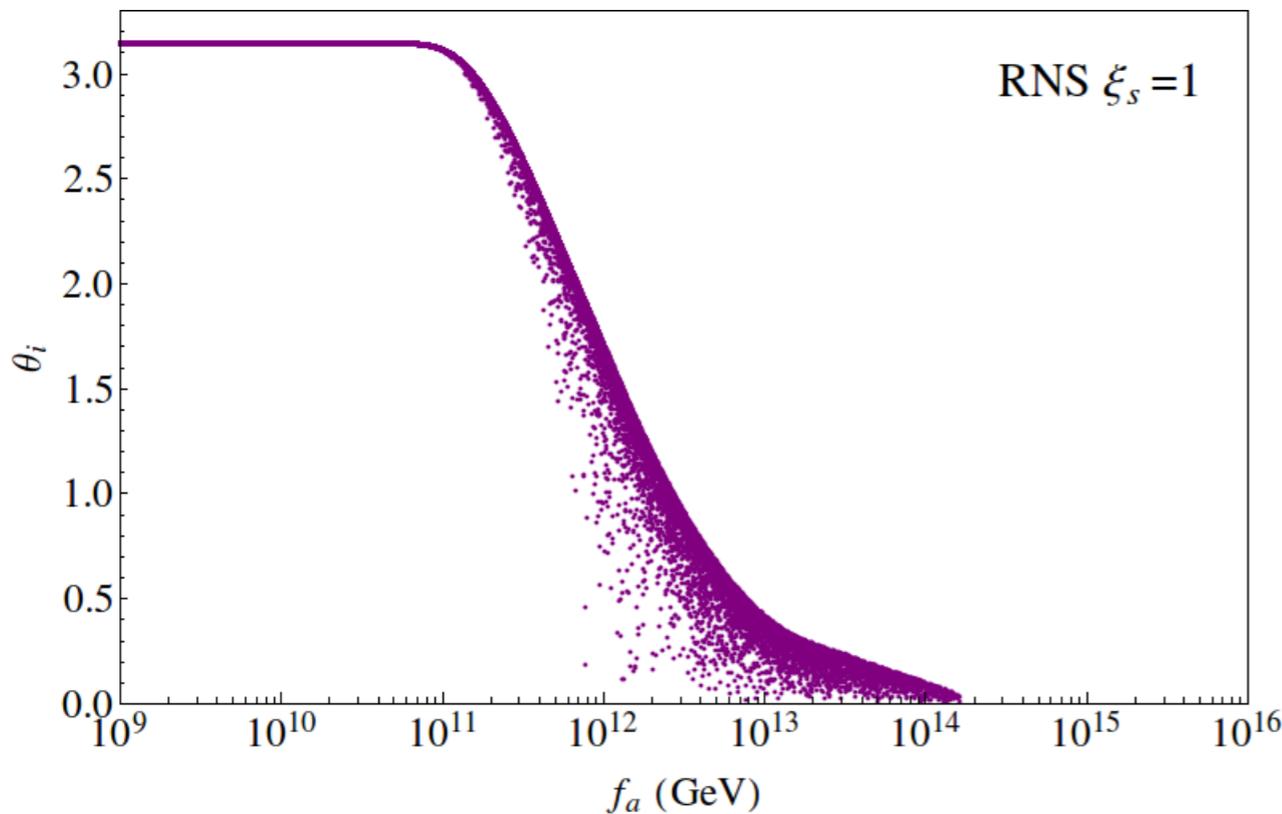
# DM production in SUSY DFSZ: solve eight coupled Boltzmann equations





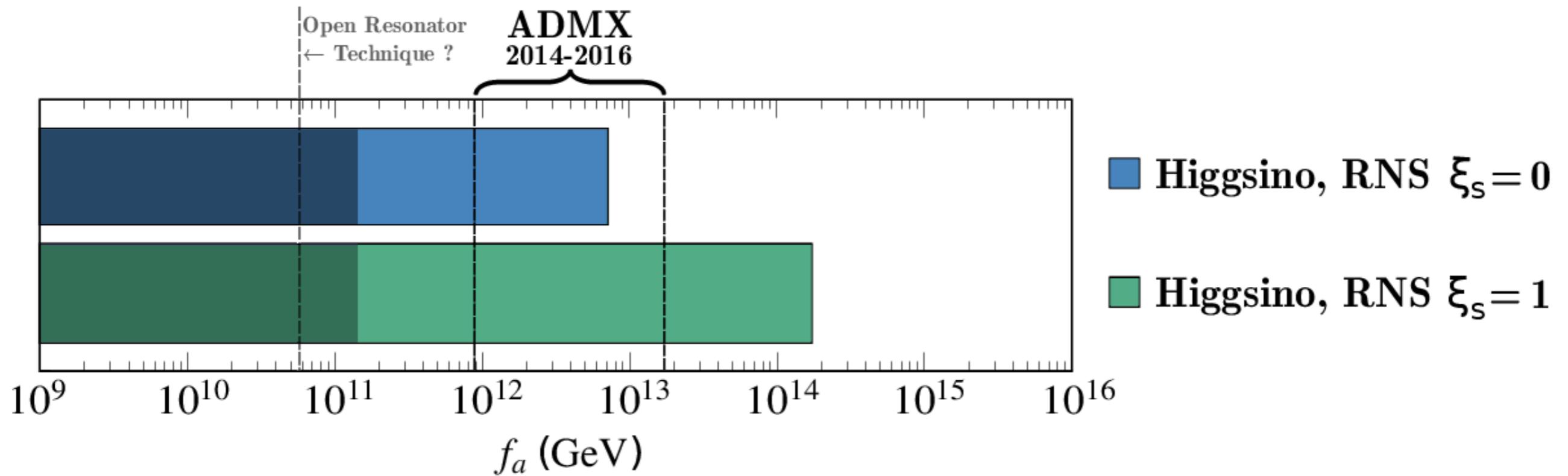
higgsino abundance

axion abundance



mainly axion CDM  
 for  $f_a < \sim 10^{12}$  GeV;  
 for higher  $f_a$ , then  
 get increasing wimp  
 abundance

Bae, HB, Lessa, Serce



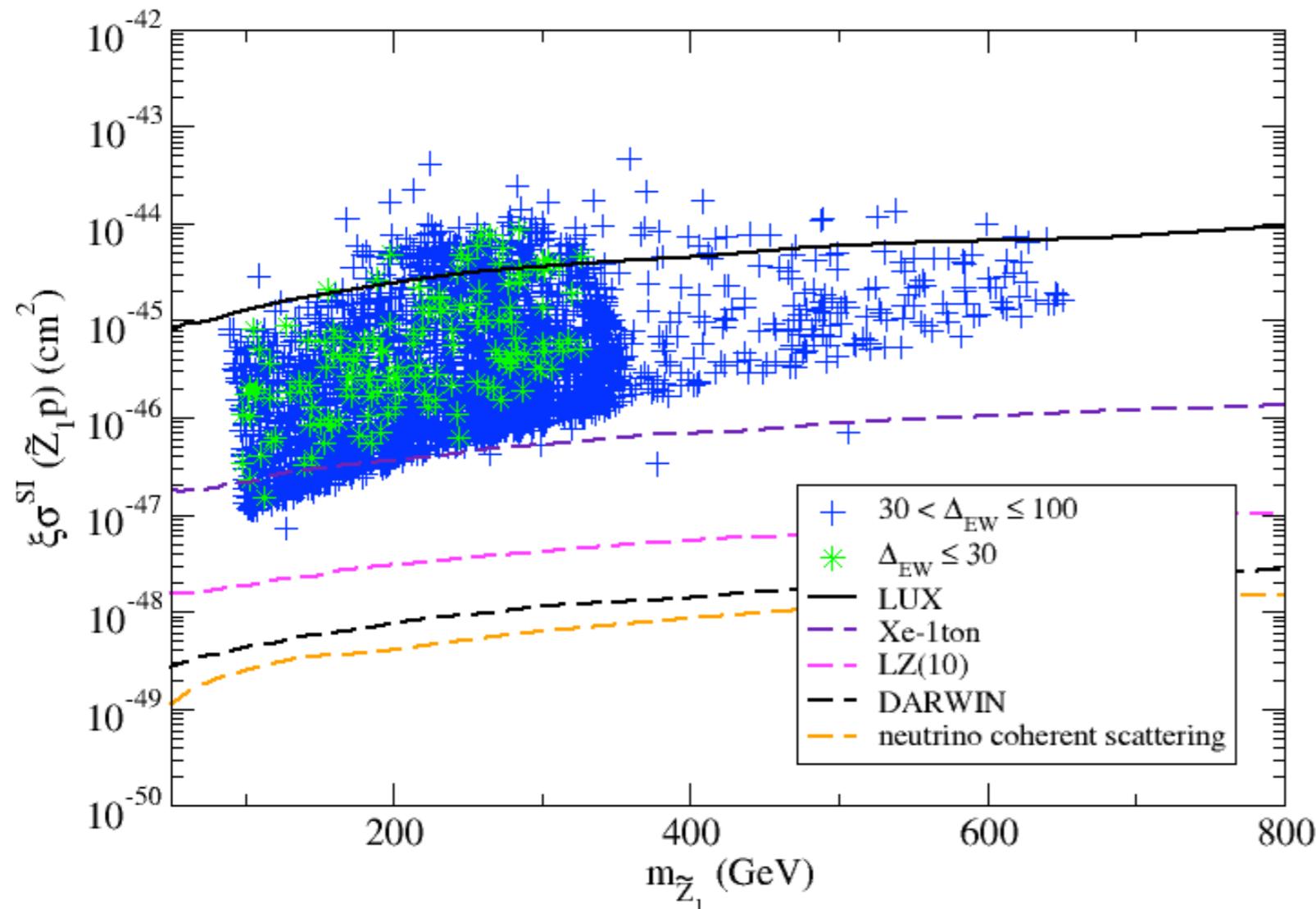
range of  $f_a$  expected from SUSY  
with radiatively-driven naturalness  
compared to ADMX axion reach

# Direct higgsino detection rescaled for minimal local abundance

Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{\tilde{Z}}_1 \tilde{Z}_1 h$$

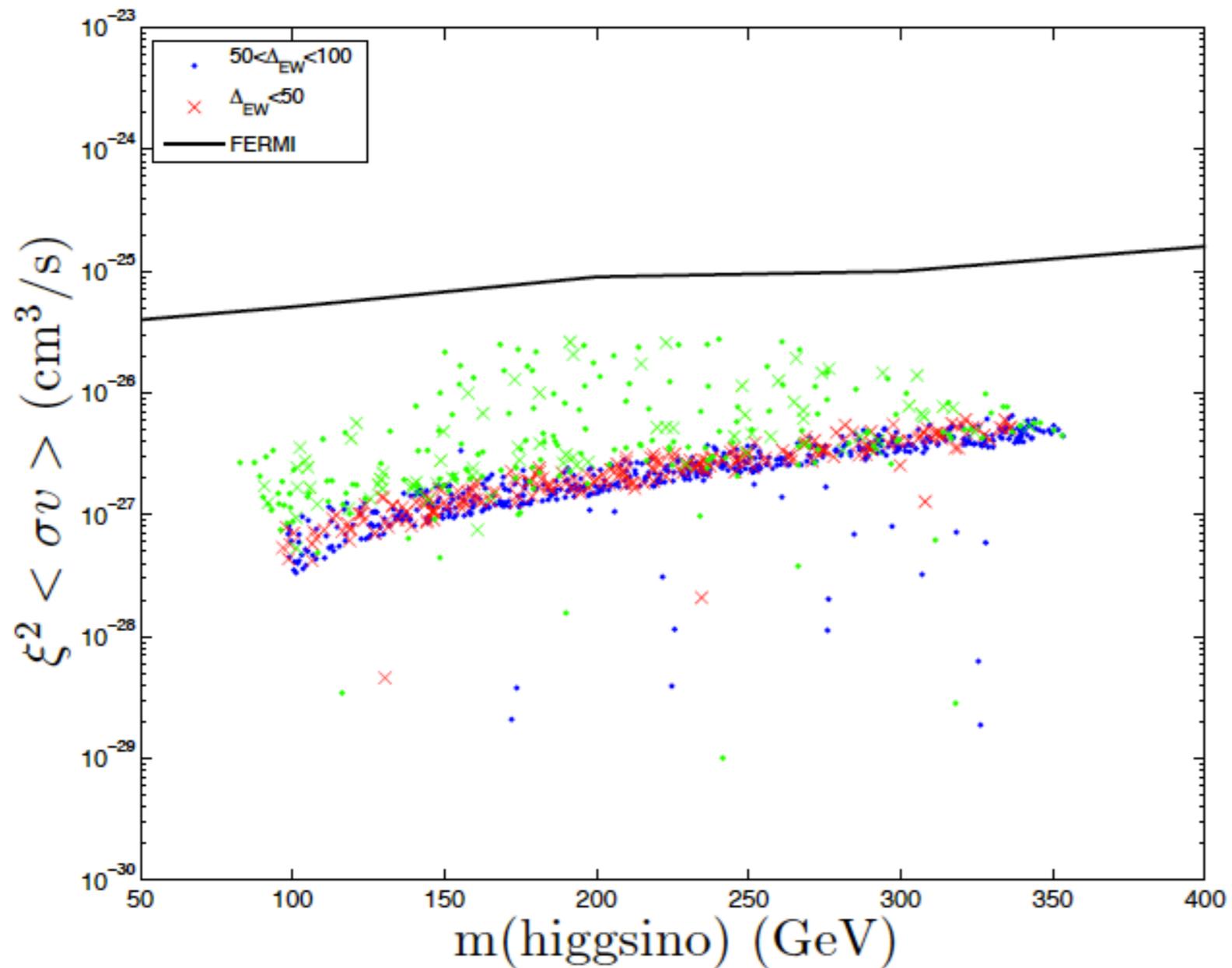
$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$



Deployment of Xe-1ton,  
LZ, SuperCDMS  
coming soon!

Can test completely with ton scale detector  
or equivalent (subject to minor caveats)

# Higgsino detection via halo annihilations:

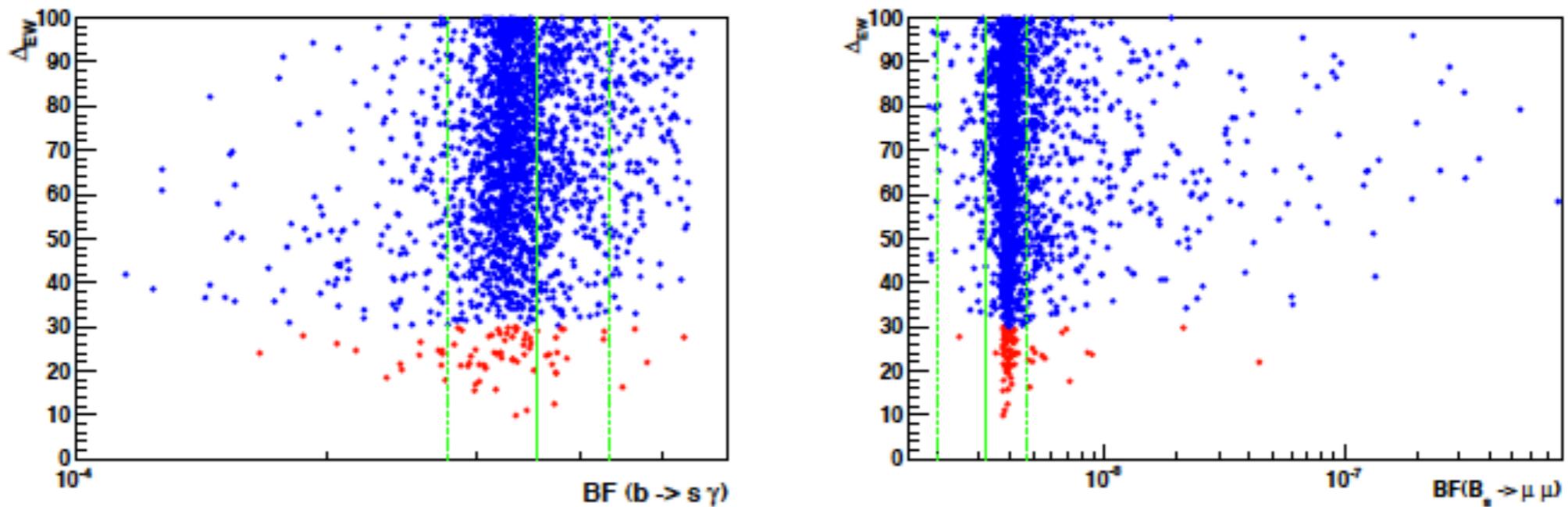


green: excluded by Xe-100

annihilation rate is high but rescaling is **squared**

Gamma-ray sky signal is factor 10-20 below current limits

What happens to B constraints?  
These are trouble for older Natural SUSY models  
which required light top/bottom squarks



Heavier top squarks,  $m(A)$  ameliorate these