

Thermal Charm production in Pb+Pb @ 40 TeV

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- ❑ Introduction
- ❑ Charm production in pQCD
- ❑ Charm production in QGP
- ❑ Charm production in Pb+Pb @ 40 TeV
- ❑ Summary

Why is understanding charm production important in Pb+Pb @ 40 TeV?

- Charmonium production: Braun-Munzinger, Thews, Greco
 - Yield depends quadratically on the charm quark number in statistical, kinetic, and coalescence models
 - Enhanced charm production could lead to possible charmonium enhancement instead of suppression so far observed at RHIC and LHC
- Charmed exotics production: Lee, Yasui, Liu & Ko, EPJC 54, 259 (2008); Cho et al., PRL 106, 212001 (2011); PRC 84, 064910 (2011)
 - Consideration of the color-spin interaction leads to possible stable charmed tetraquark meson $T_{cc}(ud\bar{c}\bar{c})$ and pentaquark baryon $\Theta_{sc}(udusc\bar{c})$
 - Enhanced charm production in Pb+Pb @ 40 TeV makes FCC a possible factory for studying charmed exotics

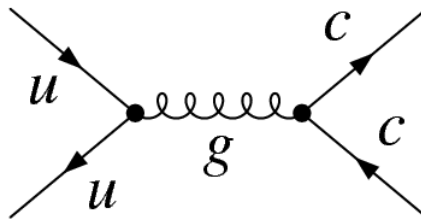
Four stages of charm production in HIC

- Direct production: Mueller, Wang (92); Vogt (94); Gavin (96)
 - Mainly from initial gluon fusions
 - About 3 pairs in mid-rapidity at RHIC (from STAR collaboration)
 - About 20 pairs in mid-rapidity at LHC @ 2.76 TeV
 - About 40 pairs in Pb+Pb @ 40 TeV
- Pre-thermal production: Lin, Gyulassy (95), Levai, Mueller, Wang (95).....
 - Not important based on minijet gluons
 - Production from initial strong color field?
- Thermal production from QGP: Levai & Vogt (97), Zhang (08)
 - Important if initial temperature of QGP is high
- Thermal production from hadronic matter: Cassing et al. (99), Liu & Ko (02)
 - Such as $\pi N \rightarrow \Lambda_c D$ and $\rho N \rightarrow \Lambda_c D$
 - Expect small effect on charm production in HIC

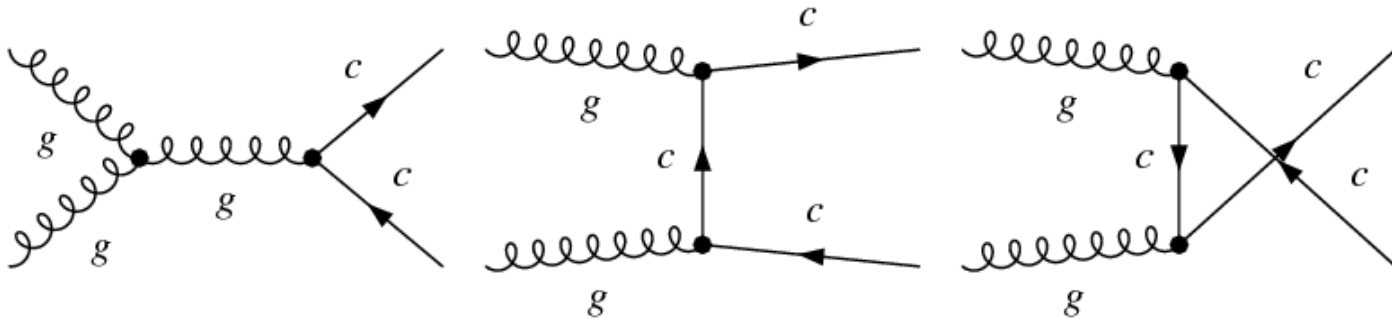
Charm production in pQCD

- Leading-order diagrams for charm production

1) $q\bar{q} \rightarrow c\bar{c}$

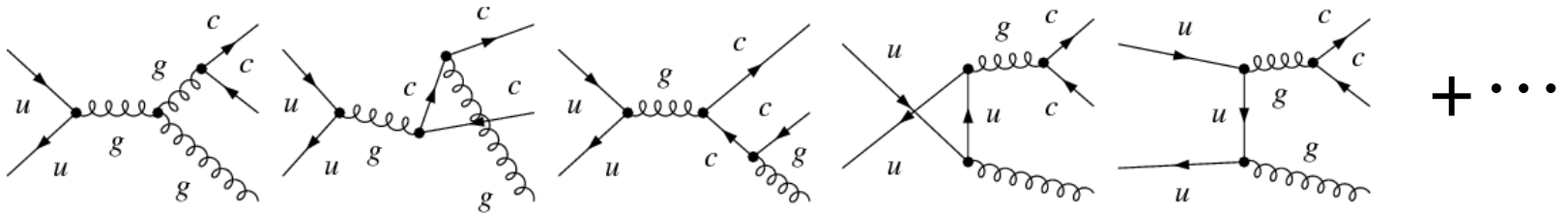


2) $gg \rightarrow c\bar{c}$

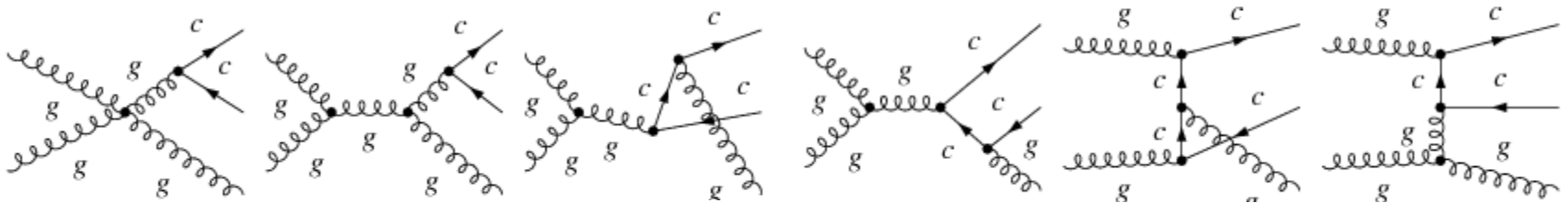


- Next-Leading-order diagrams for charm production

1) $q\bar{q} \rightarrow c\bar{c}g$



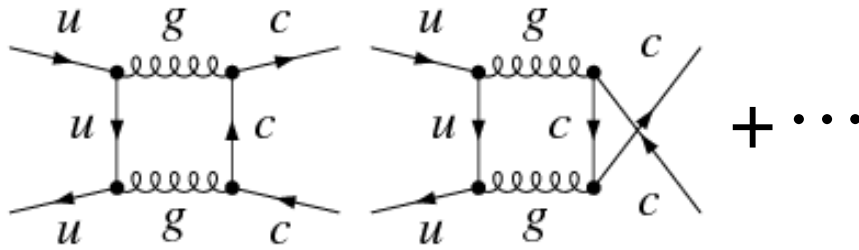
2) $gg \rightarrow c\bar{c}g$



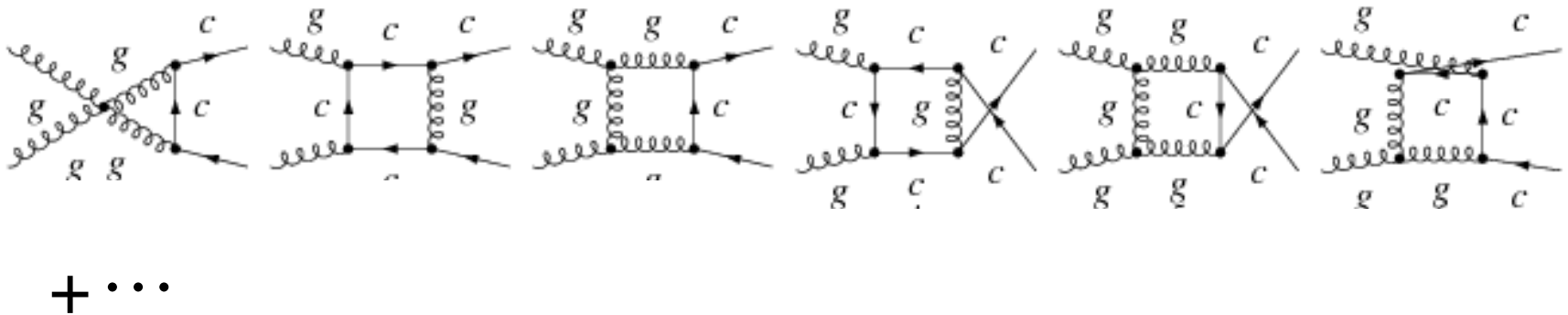
+ ...

- Virtual corrections to leading-order diagrams

1) $q\bar{q} \rightarrow c\bar{c}$

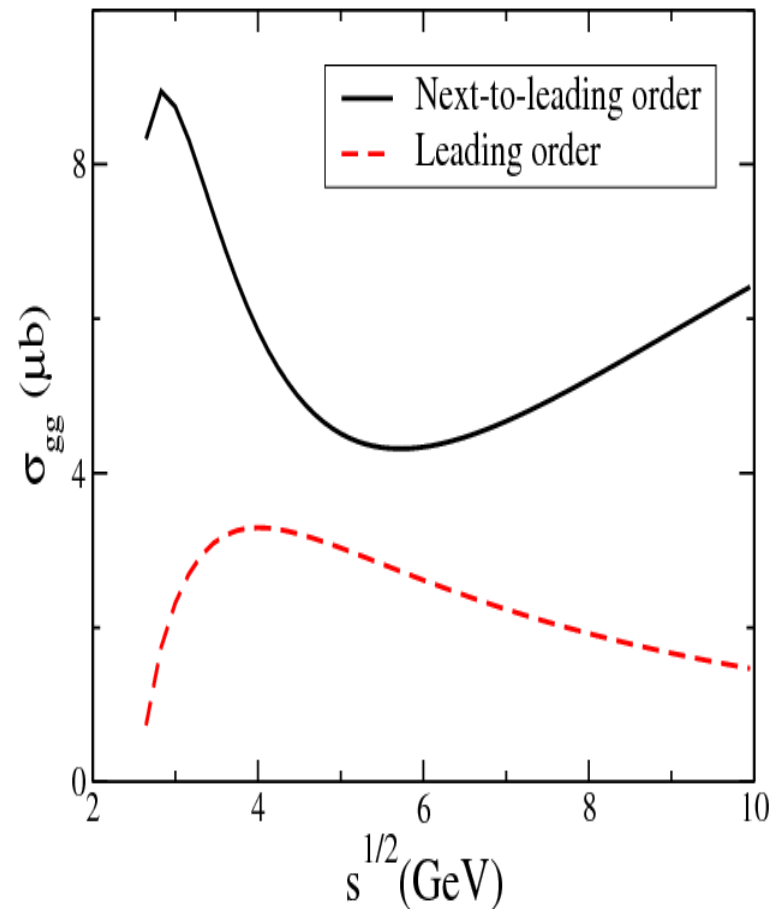
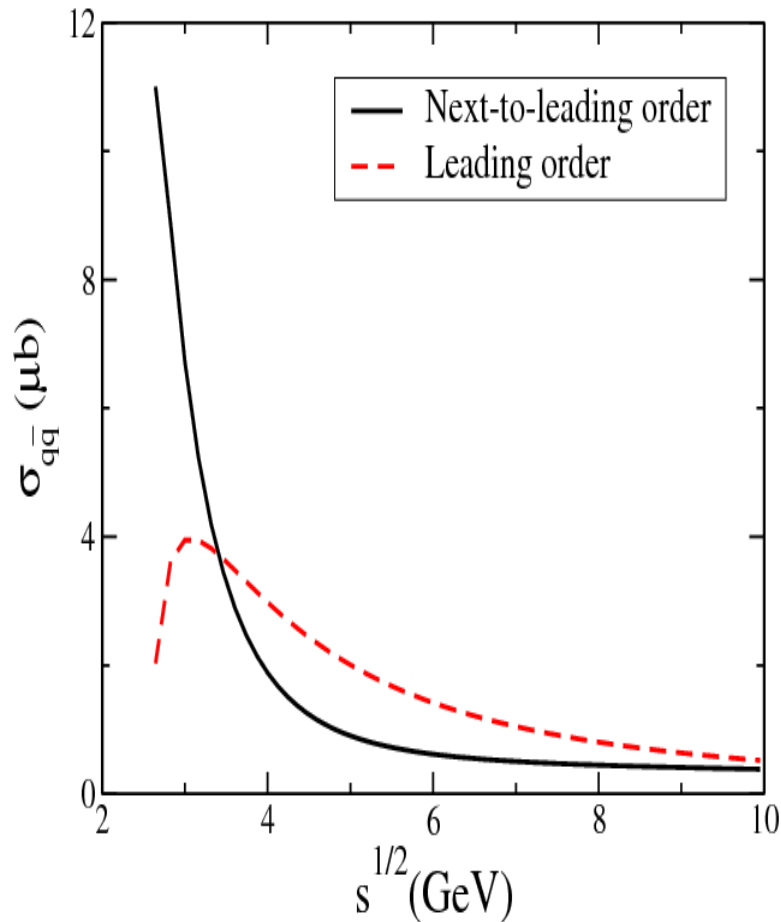


2) $gg \rightarrow c\bar{c}$



Charm quark production cross sections

P. Nason, S. Dawson & R.K. Ellis, NPB 303, 607 (1988)



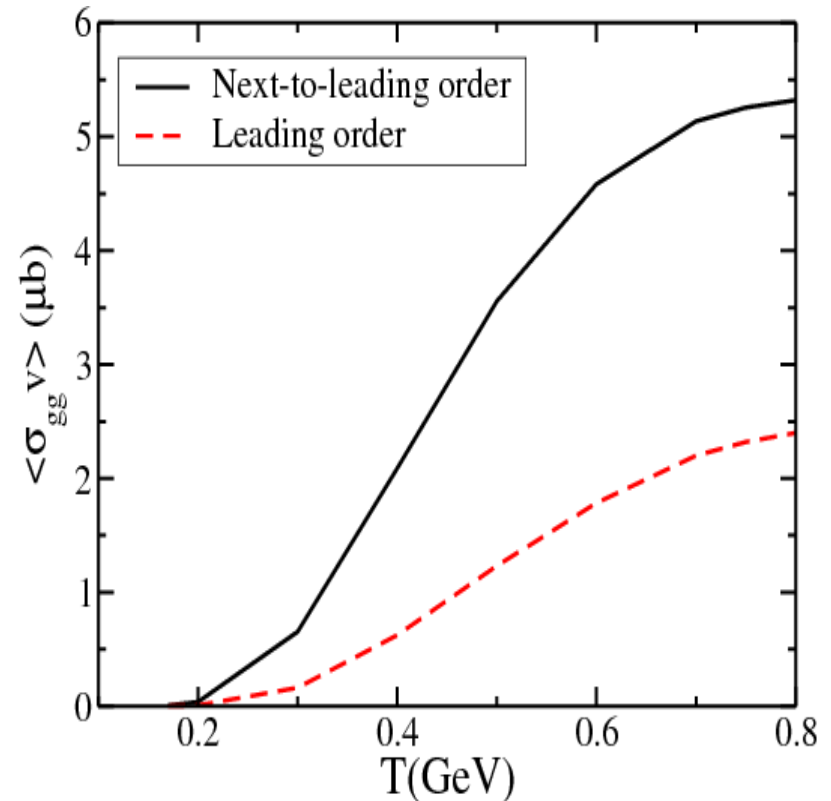
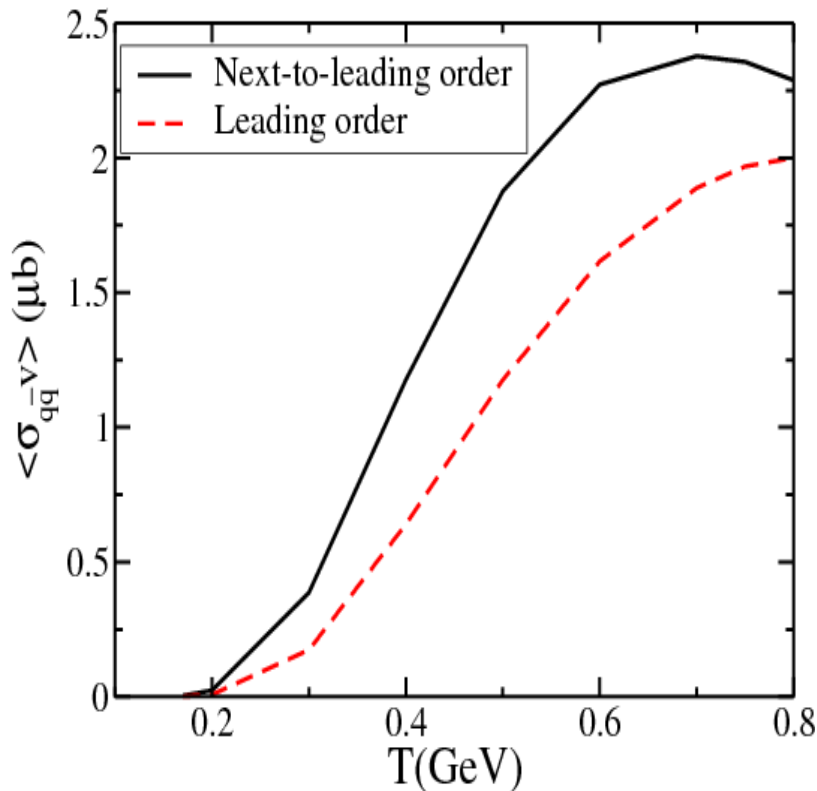
Next-to-leading order generally gives a larger cross section than the leading order except in qqbar annihilation at high energies.

Thermal averaged charm production cross sections

$$\langle \sigma_{ab \rightarrow cd} V \rangle = \frac{\int d^3 p_a d^3 p_b f_a(p_a) f_b(p_b) \sigma_{ab \rightarrow cd} V}{\int d^3 p_a d^3 p_b f_a(p_a) f_b(p_b)}$$

Thermal masses

$$m_q = \frac{gT}{\sqrt{6}}, \quad m_g = \frac{gT}{\sqrt{2}}$$

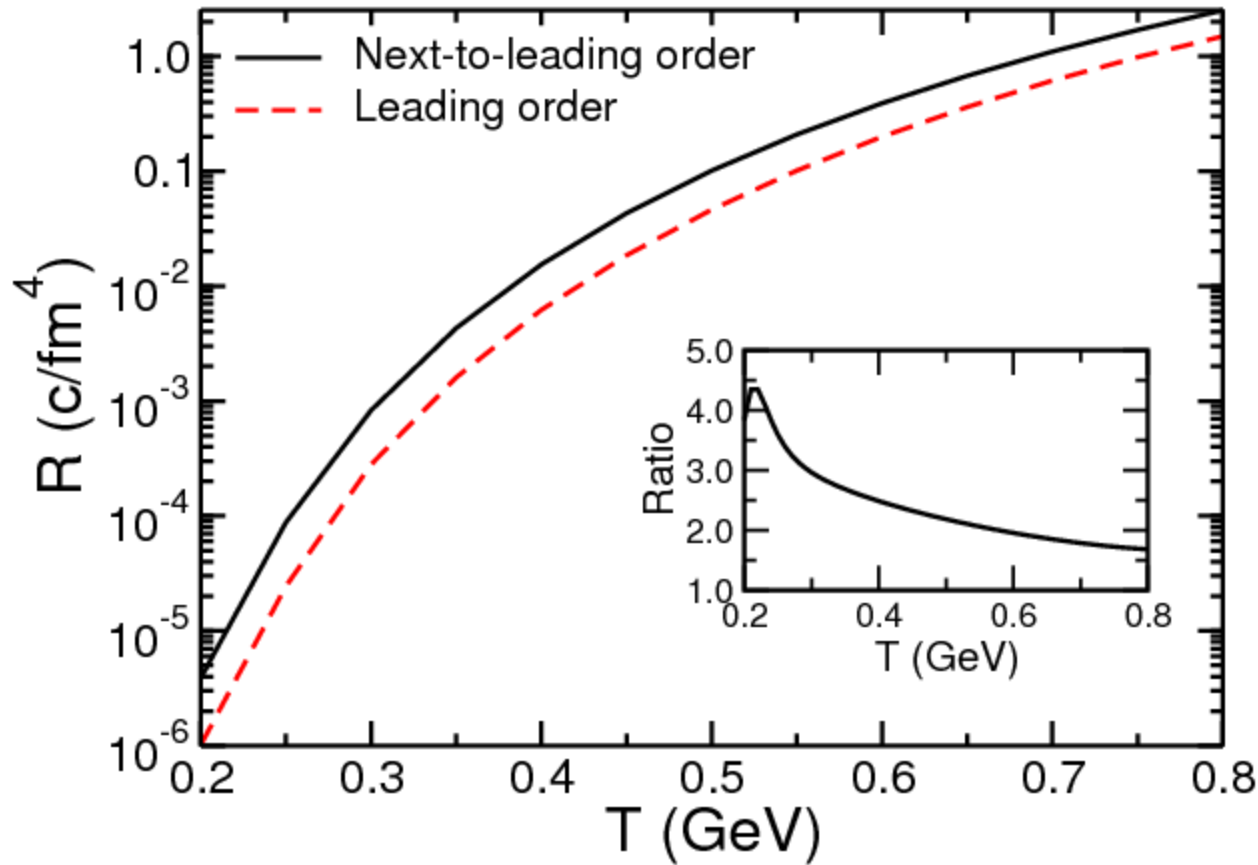


Thermal averaged cross sections are larger in next-to-leading order, particularly in the $g\bar{g}$ channel. Slightly smaller if using massless partons.⁸

Charm production rate

Zhang, Liu & Ko, PRC 77, 024901 (2008)

$$R = \left[\langle \sigma_{q\bar{q} \rightarrow c\bar{c}} \mathbf{v} \rangle + \langle \sigma_{q\bar{q} \rightarrow c\bar{c}g} \mathbf{v} \rangle \right] n_q^{\text{eq}} n_{\bar{q}}^{\text{eq}} + \frac{1}{2} \left[\langle \sigma_{gg \rightarrow c\bar{c}} \mathbf{v} \rangle + \langle \sigma_{gg \rightarrow c\bar{c}g} \mathbf{v} \rangle \right] (n_g^{\text{eq}})^2$$

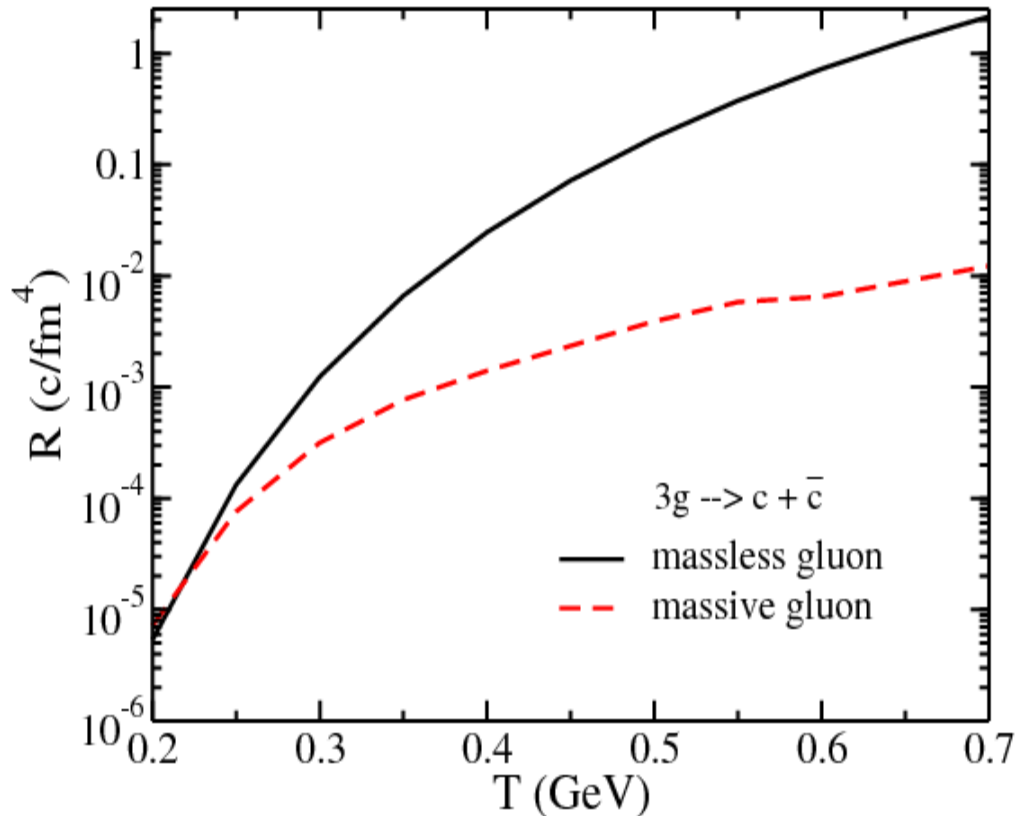


Production rate increases exponentially with temperature

Charm production from three-gluon interaction $ggg \rightarrow c\bar{c}$

Determine rate for $ggg \rightarrow c\bar{c}$ from $c\bar{c} \rightarrow ggg$ via detailed balance

$$R \propto \frac{1}{3} \int \prod_{i=1}^5 d^3 p_i f_i(p_i) |M_{ggg \rightarrow c\bar{c}}|^2 \delta^{(4)}(p_1 + p_2 + p_3 - p_4 - p_5) \propto \langle \sigma_{c\bar{c} \rightarrow ggg} v \rangle n_c^{\text{eq}} n_{\bar{c}}^{\text{eq}}$$



Gluon density $\sim 0.5/\text{fm}^3$ at T_c
and much larger initially

- Negligible rate for massive gluons as the threshold becomes larger than the charm pair mass
- With massless gluons, the rate is comparable to that of two-body processes

Charm production in Pb+Pb @ 40 TeV

- Fire cylinder evolution: Bjorken's boost invariant expansion, with local density proportional to the thickness function $T_{AB}(\mathbf{x}_T)$, and entropy conservation

$$s(\mathbf{x}_T, \tau) = \frac{\tau_0}{\tau} s(\mathbf{x}_T, \tau_0), \quad s(\mathbf{x}_T, \tau) = s(\mathbf{0}, \tau) \frac{T_{AB}(\mathbf{x}_T)}{T_{AB}(\mathbf{0})}$$

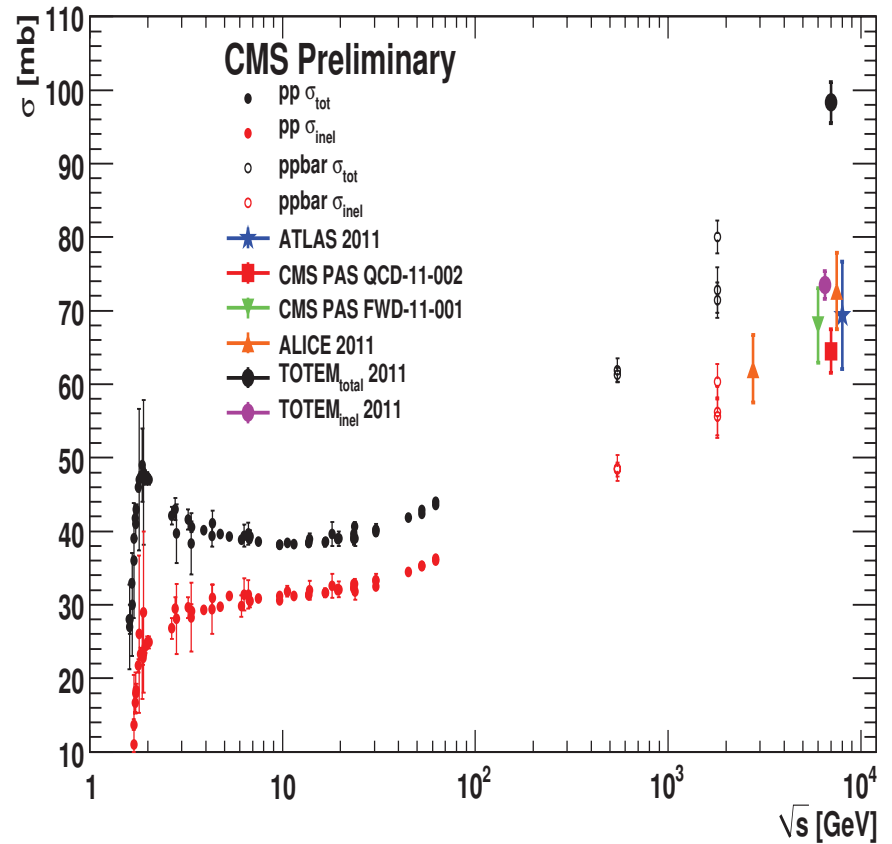
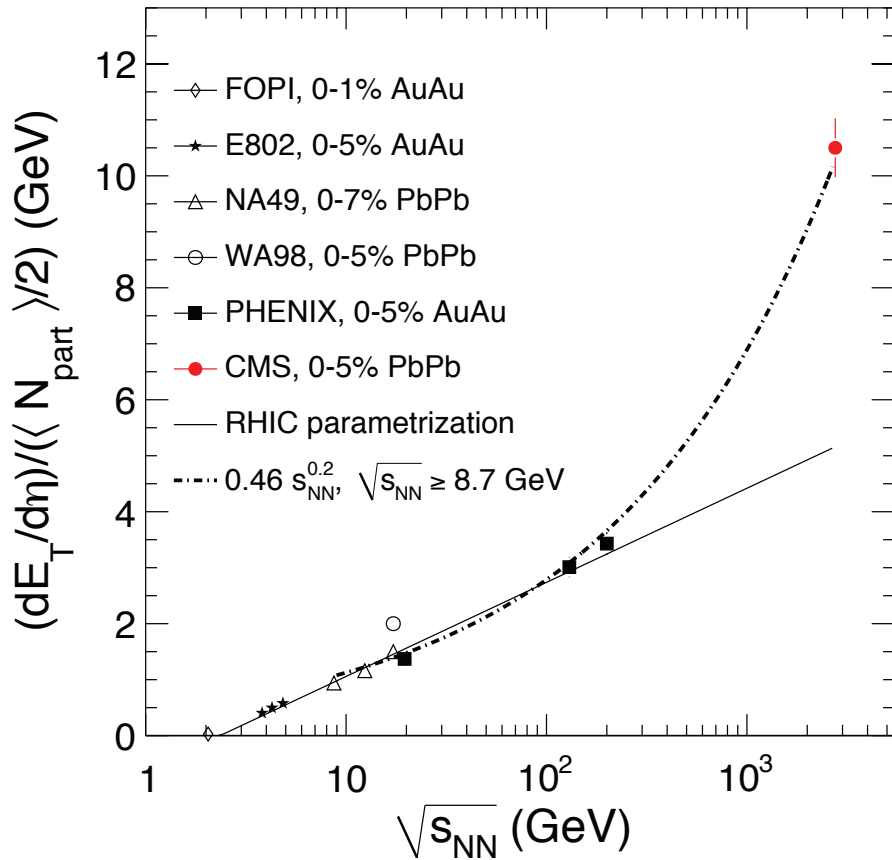
- Equation of state: Non-interacting massless parton for QGP and massive hadrons for hadronic matter with a bag constant such that phase transition temperature $T_c = 165$ MeV
- Initial charm quark number: About 43 pairs from PYTHIA, corresponding to 0.026 pairs per p+p collision or

$$\frac{d\sigma_{pp}^{c\bar{c}}}{dy}(\sqrt{s} = 40 \text{ TeV}) = 1.4 \text{ mb}$$

compared to

$$\frac{d\sigma_{pp}^{c\bar{c}}}{dy}(\sqrt{s} = 2.76 \text{ TeV}) = 0.62 \text{ mb}$$

■ Transverse energy



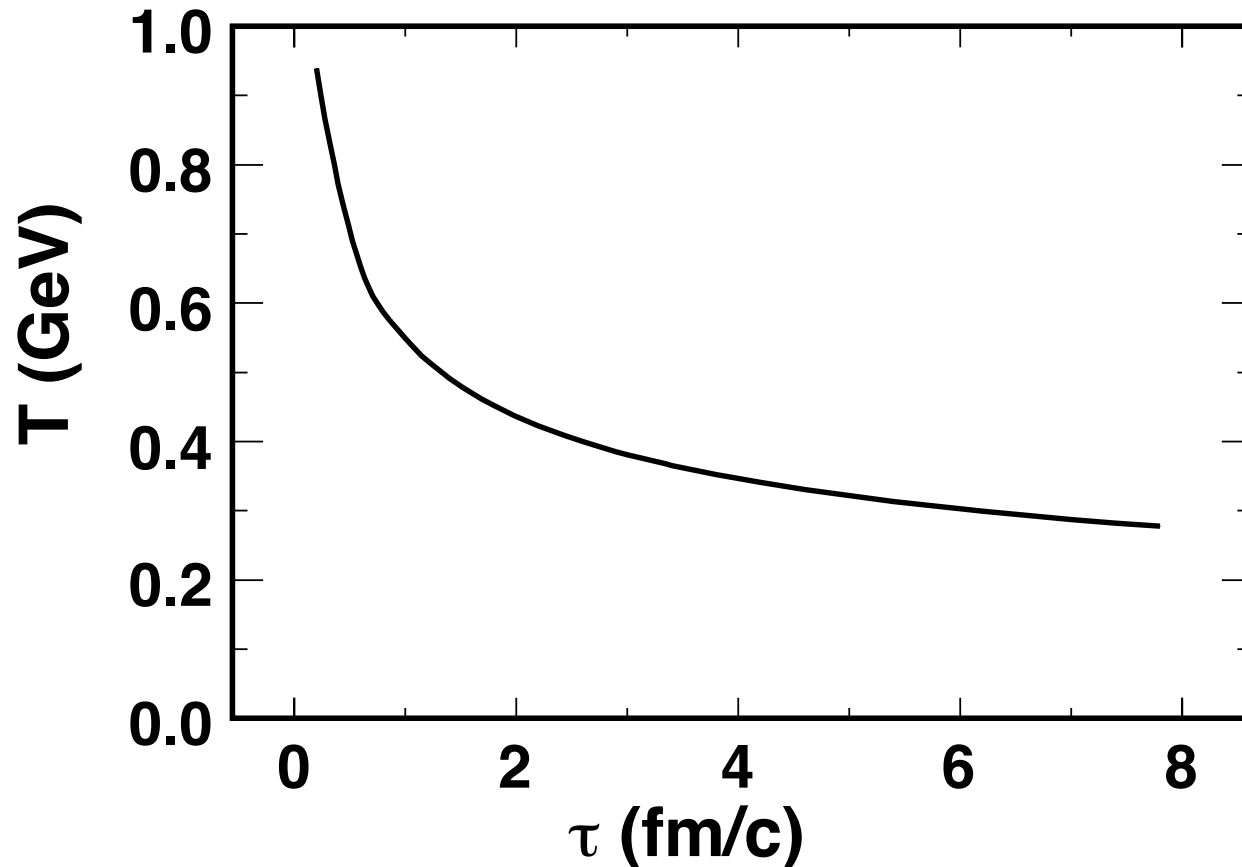
$$\frac{dE_T/d\eta}{0.5N_{\text{part}}} = 0.46 \left(\frac{\sqrt{s_{\text{NN}}}}{1 \text{ GeV}} \right)^{0.4} \text{ GeV} \quad \sigma_{pp}^{\text{in}} = 8.20 \ln \frac{\sqrt{s}}{1.436 \text{ GeV}} \text{ mb}$$

$$\rightarrow N_{\text{part}}(40 \text{ TeV}) \approx 408 \rightarrow \frac{dE_T}{d\eta}(40 \text{ TeV}) \approx 6,500 \text{ GeV}$$

- Temperature at center ($\mathbf{x}_T = 0$) of firecylinder at $\tau_f = 5$ fm/c

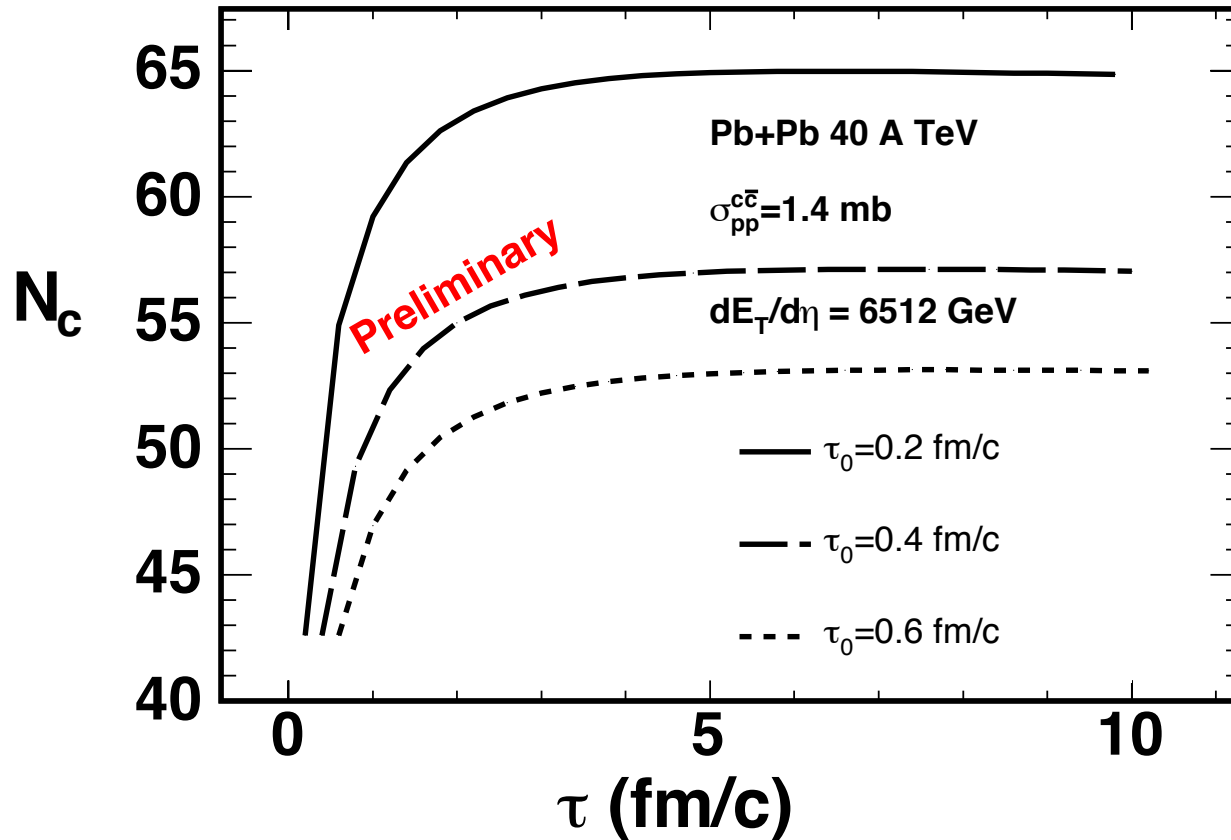
$$\int d\mathbf{x}_T \epsilon(s(\mathbf{x}_T, \tau_f)) = \frac{1}{\tau_f} \frac{dE_T}{d\eta} \rightarrow T(\mathbf{x}_T = \mathbf{0}, \tau_f) \approx 350 \text{ MeV}$$

- Time evolution of temperature at center: determined from entropy conservation through EOS



- Time evolution of charm quark number (not including $ggg \rightarrow c\bar{c}$)

$$\partial_\tau(\tau n_c) = \tau R \left[1 - \left(\frac{n_c}{n_c^{\text{eq}}} \right)^2 \right], \quad n_c^{\text{eq}} = \frac{3Tm_c^2}{\pi^2} K_2(m_c/T)$$



- Enhancement: $\sim 50\%$ for QGP thermalization time $\tau_0 = 0.2 \text{ fm/c}$, $\sim 35\%$ for $\tau_0 = 0.4 \text{ fm/c}$, $\sim 20\%$ at $\tau_0 = 0.6 \text{ fm/c}$

Summary

- Thermal charm production rate increases exponentially with the temperature of QGP.
- Next-to-leading order enhances thermal production rate by more than a factor of 2.
- Charm production from three-gluon interactions is important if gluons are massless.
- Thermal charm production may be enhanced by 50% in Pb+Pb @ 40 TeV, from 43 pairs to 65 pairs.
- Understanding thermal charm quark production is important for understanding charmonium production in HIC.
- Pb+Pb @ 40 TeV provides the possibility to search for charmed exotics such as charmed tetraquark mesons and pentaquark baryons.