### $sin (2\beta_s)$ status from CDF

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## Introduction

## Beyond the Standard Model

- CP violation in B<sup>0</sup><sub>s</sub> meson system is an excellent way to search for new physics
  - B-factories have established that, at tree level, NP effects, if existing in  $B^0$ ,  $B^+$ decays, have a magnitude < O(10%). However, there exists an important corner not explored by them: the  $B^0_s$  system
  - CP violation in B<sup>0</sup><sub>s</sub> predicted to be extremely small in the SM.
  - Contribution from new physics could come through the enhancement of loop processes

### What Is what we measure?

look at any difference in properties like decay rate, angular decomposition of the amplitude, etc between a decay and its "mirror image" resulting from C and P transformations

## Neutral B<sub>s</sub> system

• Time evolution of B<sub>s</sub> flavor eigenstates from Schrödinger equation:

$$i\frac{d}{dt}\left(\begin{array}{c}B_s^0(t)\\\overline{B}_s^0(t)\end{array}\right) = H\left(\begin{array}{c}B_s^0(t)\\\overline{B}_s^0(t)\end{array}\right) \equiv \underbrace{\left[\left(\begin{array}{cc}M_0 & M_{12}\\M_{12}^* & M_0\end{array}\right) - \frac{i}{2}\underbrace{\left(\begin{array}{cc}\Gamma_0 & \Gamma_{12}\\\Gamma_{12}^* & \Gamma_0\end{array}\right)\right]}_{\text{decay matrix}}\left(\begin{array}{c}B_s^0(t)\\\overline{B}_s^0(t)\end{array}\right)$$

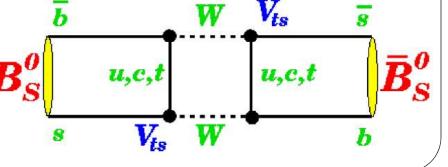
The magnitude of the box diagram gives the oscillation frequency

$$\Delta m_s = m^H - m^L \approx 2|M_{12}|$$
;  $\Delta m_s = 17.77 \pm 0.12 \text{ ps}^{-1} \text{(CDF)}$ 

- The phase of the diagram gives the complex number  $q/p = e^{-i \phi s}$  where  $\phi_s = arg (-M_{12}/\Gamma_{12})$  [ CP-violating phase]
- Mass eigenstates have different decay widths (lifetimes)

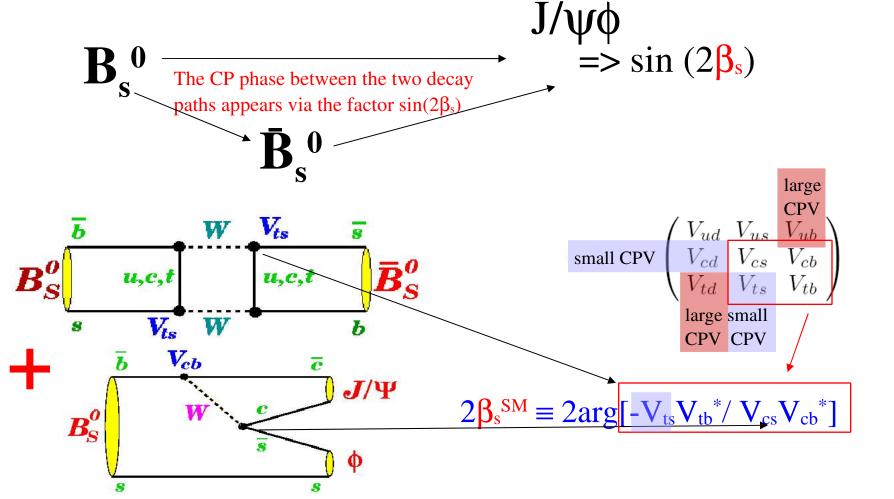
$$\Delta\Gamma = \Gamma_{\rm I} - \Gamma_{\rm H} \approx 2 |\Gamma_{\rm 12}| \cos \phi_{\rm s}$$
;  $\Delta\Gamma = 0.07 \pm 0.04~ps^{-1}$  [A.Lenz et al, JHEP06(2007)072]

• Mixing phase – sensitive to NP  $|B_S^{\prime\prime}|$ 



## CP Violation in the S.M $(B_s^0 \rightarrow J/\psi \phi)$

• The chance to observe CP violation comes from interference between decay-only and decay-through-mixing amplitudes



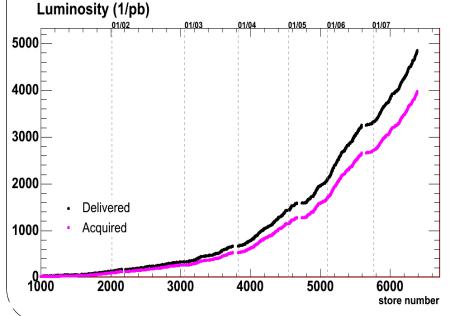
CP violation phase  $\beta_s$  in SM is predicted to be very small

## **Experiment Overview**

### Introduction to the CDF II detector

CDF II detector includes (relevant to this analysis)

- Central tracking: silicon vertex detector surrounded by a drift chamber
  - $p_T$  resolution  $\Delta p_T/p_T = 0.0015 p_T$
  - vertex resolution ~ 25 μm
- Particle identification (PID):  $dE/dx \sim 1.5 \sigma$  separation for K/pi with p>2 GeV and TOF ~2  $\sigma$  K/pi with p<1.5-1.8 GeV.
- Good e and μ identification by calorimeters and muon chambers

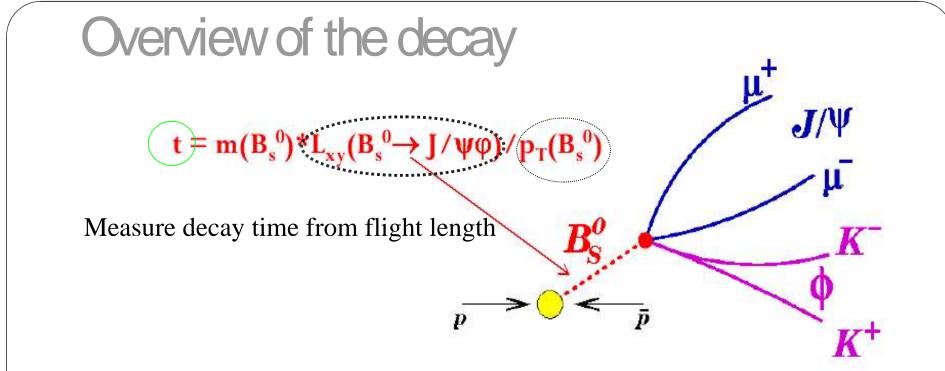


Excellent performance of Tevatron accelerator

→ excellent mass and vertex rec.

- CDF has already 4 fb<sup>-1</sup> on tape
- Expect 6-8 fb<sup>-1</sup> by end of the run 2
- This analysis uses 2.8 fb<sup>-1</sup> (but

equivalent to 2.0 fb<sup>-1</sup>, no PID 2<sup>nd</sup> half)



- $B_s^0$  travels ~ 450 µm before decaying into  $J/\psi$  and  $\phi$
- Spin-0 B<sub>s</sub><sup>0</sup> decays to spin-1 J/ $\psi$  and spin-1  $\phi$  $\Rightarrow$  final states with l = 0, 2 (CP-even) and l = 1 (CP-odd)
- Maximum sensitivity to phase (sin  $2\beta_s$ ) depends on decay time resolution and separation of CP at decay and initial flavour of  $B_s^0/\overline{B}_s^0$
- Purpose: disentangle all these features and measure the phase8

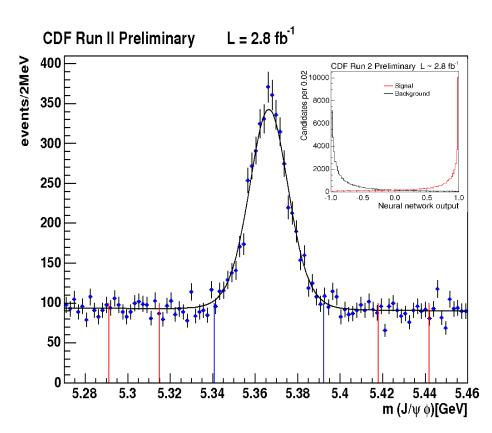
## Measurement Strategy

- Reconstruct  $B_s^0 \to J/\psi(\to \mu^+\mu^-) \phi(\to K^+K^-)$
- Use angular properties of the J/ $\psi$   $\phi$  decay to separate angular momentum states which correspond to CP eigenstates
- Identify initial state of  $B_s$  meson (flavour tagging) and thus separate time evolution of  $B_s^0$  and  $\overline{B}_s^0$  to maximize sensitivity to CP asymmetry (sin  $2\beta_s$ )
- Perform un-binned maximum likelihood fit to extract signal parameters of interest (e.g.  $\beta_s$ ,  $\Delta\Gamma = \Gamma_L \Gamma_H$ )

## $B_s^0 \rightarrow J/\psi \phi$ Signal Selection

- Use an artificial neural network (ANN) to efficiently separate signal from background
- ANN training
  - Signal from Monte Carlo reconstructed as it is in data
  - Bkg. from J/ψφ sidebands
- Variables used in network
  - $B_s^0$ :  $p_T$  and vertex prob.
  - $J/\psi$ :  $p_T$  and vertex prob.
  - $\bullet$   $\phi$ : mass and vertex prob.
  - $K^+, K^-$ :  $p_T$  (NO PID)

 $N(B_s^{\ 0}) \sim 3200$  ( with PID expect ~3800 )



## Angular Analysis of Final States

Maximum sensitivity to phase if *CP*-even *and CP*-odd states are separated

We start with a sample of

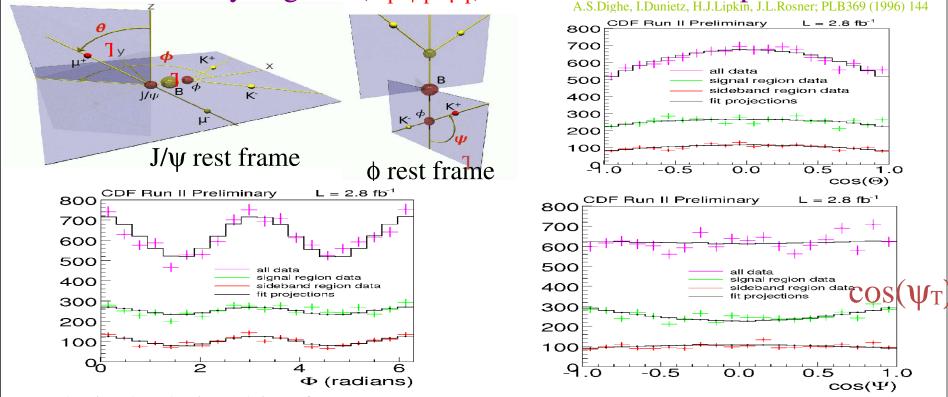
$$B_s^0$$
 and  $\bar{B}_s^0 \rightarrow J/\psi \phi$   $(J/\psi \rightarrow \mu^+ \mu^-, \phi \rightarrow K^+ K^-)$ 

and we measure the time when each decay occurred.

Then, we need to know the CP of the final state ...

but we can only do it on a statistical basis

- $^{\prime}$ •B → VV (our B<sub>s</sub><sup>0</sup> → J/ψ φ but also B<sup>0</sup> → J/ψ K\*<sup>0</sup> , ...) decay to two CP even states (S-wave or D-wave) and one CP odd (P-wave)
- Alternatively to the S,P,D-wave states one can use the "transversity basis": three independent components that use the vector mesons polarizations w.r.t. their direction of motion (pol.states  $P_0, P_\parallel, P_\perp$ )
- the "transversity angles"  $(\theta_T, \phi_T, \psi_T)$  are sensitive to the polarizations



Analytical relationships from A.S.Dighe, et al, EPJ C6 (1999) 647 Angular correlations in decay products ⇒ separation of CP-components

## Flavor Tagging

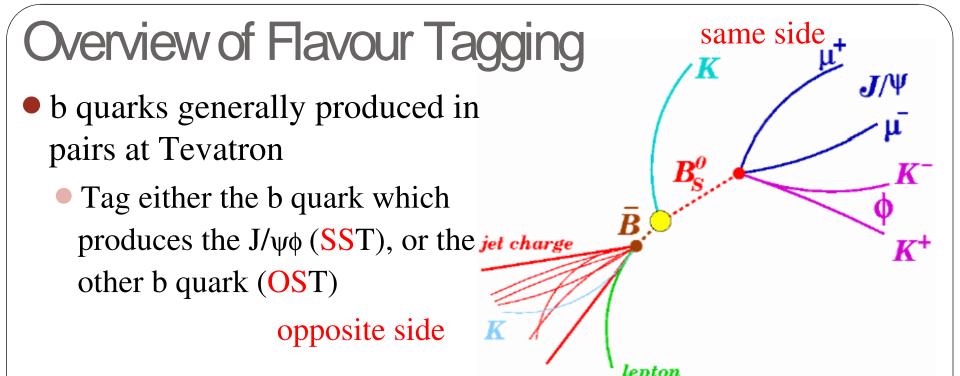
Maximum sensitivity to phase if  $B_s^0$  and  $B_s^0$  separated

We have a sample of

$$B_s^0$$
 and  $\bar{B}_s^0 \rightarrow J/\psi \phi$   $(J/\psi \rightarrow \mu^+ \mu^-, \phi \rightarrow K^+ K^-)$ 

of known decay-time and CP.

It will help to know whether a meson or an anti-meson was produced in the *pp* interaction...



SST: exploits the charge/species correlations with associated particles produced in fragmentation that results in the reconstructed meson

OST: exploits the decay products of the other b-hadron in the event

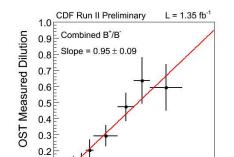
 The final tag is the combination (properly weighted) of all the different tagging methods

Output: decision (b-quark or  $\bar{b}$ -quark) and the quality of that decision

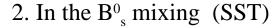
## Quantifying Tagging Power

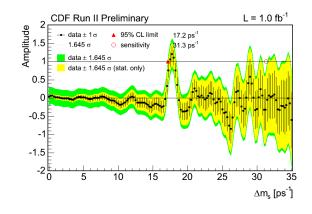
- To quantify tagging we use:
  - Efficiency  $\varepsilon = N_{\text{tagged}} / N_{\text{total}} = (N_{\text{RS}} + N_{\text{WS}}) / (N_{\text{RS}} + N_{\text{WS}} + N_{\text{NT}})$
  - "Dilution"  $D = P_{tag} P_{mistag} = (N_{RS}-N_{WS})/(N_{RS}+N_{WS})$

Each tag decision comes with an dilution estimate (event-per-event dilution), validated:



1. Using  $B^{\pm}$  (OST)





• The statistical power of the tagging is quantified by  $\varepsilon < D^2 >$  typically 4.8 % as detailed next.

$$\varepsilon = 96 \pm 1\%$$
 $\sqrt{\text{D}^2} = 11 \pm 2 \%$ 
 $\varepsilon < \text{D}^2 > = 1.2 \%$ 

SST

**OST Predicted Dilution** 

$$\varepsilon = 50 \pm 1\%$$
  
 $\sqrt{\text{CD}^2} = 27 \pm 4\%$   
 $\varepsilon < \text{D}^2 > = 3.6 \%$ 

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[used in 1st half only]

### Un-binned Likelihood Fit

We have a sample of

$$B_s^0$$
 and  $\bar{B}_s^0 \rightarrow J/\psi \phi (J/\psi \rightarrow \mu^+ \mu^-, \phi \rightarrow K^+ K^-)$ 

of "known" decay-time, CP and production flavor.

But this information is not know on a per-candidate basis. Wrap it up in a fit.

### Overview of fit

Single event likelihood decomposed and factorized in:  $f_s P_s(m|\sigma_m) P_s(t, \vec{\rho}, \xi|\mathcal{D}, \sigma_t) P_s(\sigma_t) P_s(\mathcal{D})$ 

$$+(1-f_s)P_b(m)P_b(t|\sigma_t)P_b(\vec{
ho})P_b(\sigma_t)P_b(\sigma_t)$$

 $P_s$ : probability distribution functions (PDFs) for signal  $P_b$ : PDFs for background

 $f_s$ : signal fraction (fit parameter)

- Measured quantities that enter in the fit and their PDFs
  - reconstructed mass of  $B_s^0$ ,  $\overline{B}_s^0$  and its error, decay time and its error, transversity angles, flavour tag decision, dilution D
  - Parameters in the fit : the relevant ones :  $\beta_s$ ,  $\Delta\Gamma$
- plus many nuisance parameters: mean width  $\Gamma = (\Gamma_L + \Gamma_H)/2$ ,

$$|A_{\parallel}(0)|^2$$
,  $|A_{\parallel}(0)|^2$ ,  $|A_{0}(0)|^2$ ,  $\delta_{\parallel} = \arg(A_{\parallel} A_{0}^*)$ ,  $\delta_{\perp} = \arg(A_{\perp} A_{0}^*)$  ...

### Results

Both CDF and D0 have published their 1<sup>st</sup> determination of bounds on mixing-induced CP violation in  $B_s^{\ 0} \to J/\psi \ \phi$  (references bellow). Today I will show :

- $\rightarrow$  new  $(2\beta_s, \Delta\Gamma)$  confidence region (CDF, 2.8 fb<sup>-1</sup>, ~2 fb<sup>-1</sup> equiv.)
- $\rightarrow$  new  $2\beta_s$  confidence interval (CDF, 2.8 **fb**<sup>-1</sup>, ~2 **fb**<sup>-1</sup> equiv.)

[the results are not intended to be published, just an update for ICHEP, next publication: PRD in winter with full PID and ~4 **fb**<sup>-1</sup>]

→ combined CDF and D0 (from previous measurements, Phys. Rev. Lett. 100, 161802 [2008, CDF 1.35 **fb**<sup>-1</sup>] and arXiv:0802.2255 [hep-ph, 2008, D0 2.8 **fb**<sup>-1</sup>])

### Likelihood

Symmetry in likelihood expression :

$$2\beta_s \to \pi - 2\beta_s \,, \; \Delta\Gamma \to -\Delta\Gamma, \, \delta \, \to 2\pi - \delta, \, \delta_\perp \to \; \pi - \delta_\perp$$

- These yield multiple solutions with non-Gaussian uncertanties, biased estimates, etc
- → Point estimate irrealistic → quote confidence region

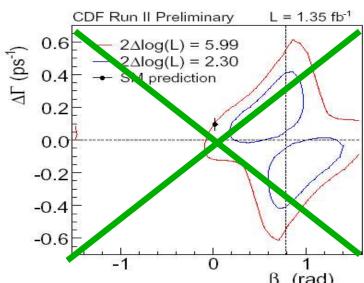
• using profile likelihood ratio ordering with rigorous frequentist inclusion of systematic uncertainties

### Probabilistic method has to provide proper coverage

F-C guarantees coverage at quoted C.L. Accounts for non-asymptotic behavior of likelihood, i.e. log(L) non-parabolic, and possible large fluctuations of L shape from experiment-to-experiment

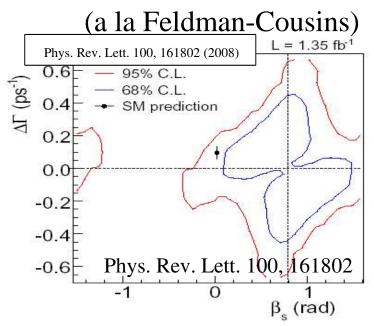
Excludes a given  $\beta_s$ - $\Delta\Gamma$  pair if it can be excluded for any choice of the 20+ nuisance parameters within  $5\sigma$  of their estimated values

#### 2D-Likelihood contour



Does **not** has coverage: the resulting confidence region does not contain the true value with desired CL independently of true value

Profile-Likelihood Ratio ordering



Above procedure has been corrected to have right coverage

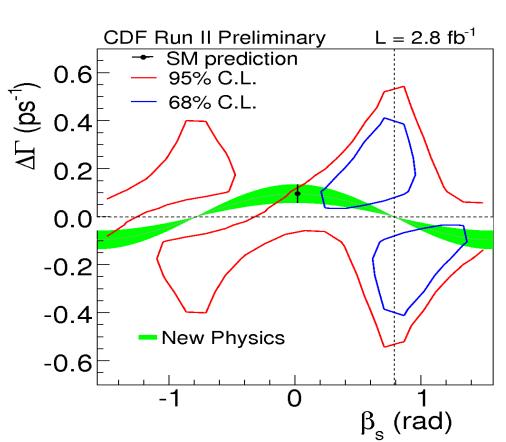
Example of 2D-L contour vs Profile-L Ratio ordering for the 1.35 fb<sup>-1</sup> CDF result

## Flavor Tagged $2\beta_s$ - $\Delta\Gamma$ Confidence Region

Confidence region with profile-Likelihood Ratio ordering and rigorous frequentist inclusion of systematic uncertainties. 2D region is projection of a multidimensional region in the space of all (27) fit parameters

Assuming the SM, the probability of observing a fluctuation as large or larger than what observed in data is 7%, corresponding to  $1.8\sigma$ 

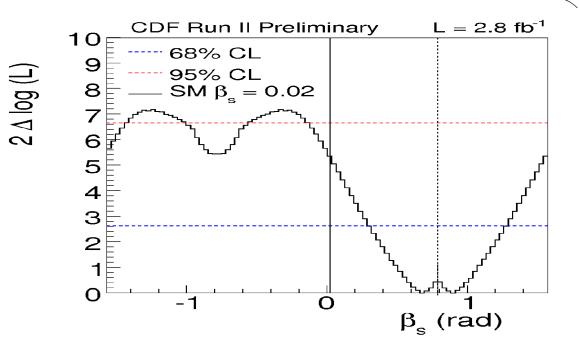
Expect to shrink further once PID will be available for full dataset



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## β<sub>s</sub> 1D Intervals

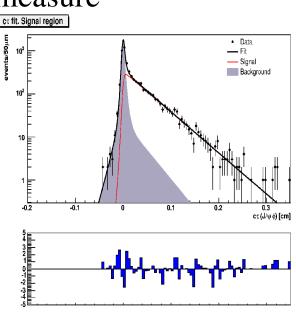
- $\Delta\Gamma$  treated as a nuisance parameter
  - $\Rightarrow$  β<sub>s</sub> ∈ [0.28, 1.29] at 68% CL



• Assuming no CP violation ( $\beta_s = 0$ ), we also measure

$$c\tau_s = 459 \pm 12 \text{ (stat)} \pm 3 \text{ (syst)} \text{ } \mu\text{m}$$
  
 $\Delta\Gamma_s = 0.02 \pm 0.05 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ ps}^{-1}$   
and the transversity amplitudes  
 $|A_{||}(0)|^2 = 0.241 \pm 0.019 \text{ (stat)} \pm 0.007$ 

 $|A_0(0)|^2 = 0.508 \pm 0.024 \text{ (stat)} \pm 0.008$ 



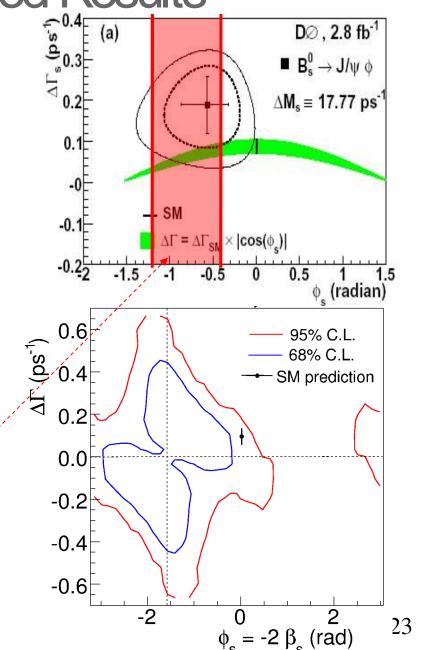
### Reminder: DØ published Results

- DØ observes a fluctuation consistent with CDF
- Chooses to quote the results in terms of  $\phi_s = -2\beta_s$  (arXiv:0802.2255)
- DØ quotes a point-estimate with strong phases constrained from

$$B^0 \rightarrow J/K^{*0}$$

$$\phi_s = -0.57^{+0.24}_{-0.30}(\text{stat})^{+0.07}_{-0.02}(\text{syst})$$

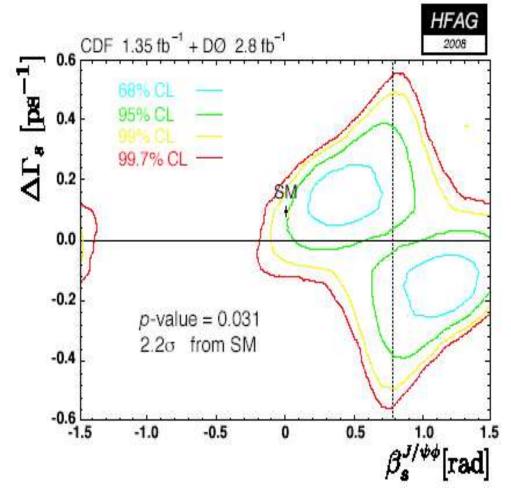
- This makes the result dependent on theoretical assumptions
- Can be compared to CDF published constrained result
  2β ∈ [0.40,1.20] @ 68% CL



### Tevatron combination

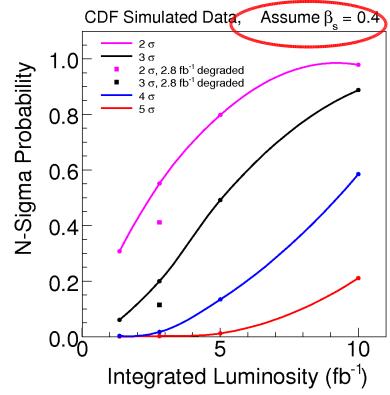
Combine CDF and D0 iso-CL regions with no constrains and previously checked for coverage (a' la HFAG):

 $2.2\sigma$  consistency with SM.



### **Future**

- Tevatron can search for anomalously large values of  $\beta_s$
- Shown results 2.8 fb<sup>-1</sup>, but 4 fb<sup>-1</sup> already on tape to be analysed soon
- Expect 6-8 fb<sup>-1</sup> by the end of the run 2
- Analysis to be improved and optimized:
  - better flavour tagging
  - calibrated PID
  - more statistics from other triggers
- If  $\beta_s$  is indeed large CDF results have good chance to prove it



- CPV in B<sub>s</sub> system is one of the main topics in LHC<sub>b</sub> B Physics program
  - → will measure mixing phase with great precision

## Conclusions

### Conclusions

- First update on larger dataset confirms old result and provides tighter constraints (15% to 7% agreement with SM), although several ingredients are still in the works
- Best measurements of  $B_s$  decay width difference and one of the best lifetime measurements
- Both CDF and DØ observe 1-2 sigma  $\beta_s$  deviations from SM predictions. SM agreement reduces to  $2.2\sigma$  when combined.
- Interesting to see how these effects evolve with more data

# Back up

### **Un-binned Likelihood Fit**

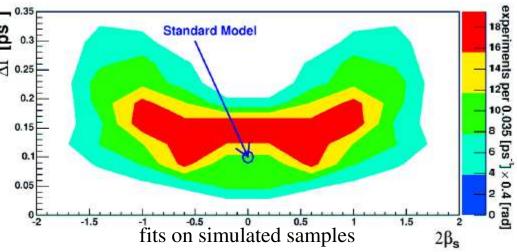
• Fit with separate PDFs for signal and background

$$f_s P_s(m|\sigma_m) P_s(ct, \vec{\rho}, \xi | \mathcal{D}, \sigma_{ct}) P_s(\sigma_{ct}) P_s(\mathcal{D})$$
$$+ (1 - f_s) P_b(m) P_b(ct|\sigma_{ct}) P_b(\vec{\rho}) P_b(\sigma_{ct}) P_b(\mathcal{D})$$

- $P_s(m|\sigma_m)$  Single Gaussian fit to signal mass
- $P_s(ct, \rho, \xi | D, \sigma_{ct})$  Probability for  $\overline{B}_s^0/B_s^0$
- P<sub>b</sub>(m) Linear fit to background mass distribution
- $P_b(ct|\sigma_{ct})$  Prompt background, one negative exponential, and two positing exponentials
- $P_b(\rho)$  Empirical background angle probability distributions
- Use scaled event-per-event errors for mass and lifetime fits and event-per-event dilution

#### $\beta_s$ in Untagged Analysis

- Fit for the CPV phase
- Biases and non-Gaussian estimates ₹ 0.25 in pseudo-experiments
- Strong dependence on true values for biases on some fit parameters.



a) Dependence on one parameter in the likelihood vanishes for some values of other parameters:

$$\cos(\delta_{\perp})\sin(2\beta_s)\sinh(\Delta\Gamma t/2)$$

b) L invariant under two transformations:

$$2\beta_s \rightarrow -2\beta_s, \ \delta_{\perp} \rightarrow \delta_{\perp} + \pi$$

→ 4 equivalent minima

$$\Delta\Gamma \rightarrow -\Delta\Gamma$$
,  $2\beta_s \rightarrow 2\beta_s + \pi$ 

### Angular Probability Distribution: time evolution

General relation for B-> VV

$$\frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} \propto |A_0|^2 \mathcal{T}_+ f_1(\vec{\rho}) + |A_{\parallel}|^2 \mathcal{T}_+ f_2(\vec{\rho})$$

$$+ |A_{\perp}|^2 \mathcal{T}_- f_3(\vec{\rho}) + |A_{\parallel}| |A_{\perp}| \mathcal{U}_+ f_4(\vec{\rho})$$

$$+ |A_0| |A_{\parallel}| \cos(\delta_{\parallel}) \mathcal{T}_+ f_5(\vec{\rho})$$

$$+ |A_0| |A_{\perp}| \mathcal{V}_+ f_6(\vec{\rho}), \qquad \text{Time dep}$$

 $A_0$ ,  $A_{\parallel}$ ,  $A_{\perp}$ : transition amplitudes to a given polarization state at t=0

Time dependence appears in T, U, V. Different for  $\mathbf{B}_s^0$  and  $\mathbf{\bar{B}}_s^0$ 

$$\frac{d^4P(t,\vec{\rho})}{dtd\vec{\rho}} \propto |A_0|^2 \mathcal{T}_+ f_1(\vec{\rho}) + |A_{\parallel}|^2 \mathcal{T}_+ f_2(\vec{\rho})$$

anti-
$$B_{s}^{0}$$
 +  $|A_{\perp}|^{2}$  $T_{-}f_{3}(\vec{\rho})$  +  $|A_{\parallel}||A_{\perp}|U_{-}f_{4}(\vec{\rho})$  +  $|A_{0}||A_{\parallel}|\cos(\delta_{\parallel})T_{+}f_{5}(\vec{\rho})$  +  $|A_{0}||A_{\perp}|V_{-}f_{6}(\vec{\rho})$ ,

f(): angular distribution for a given polarization state

• 
$$\rho = \{\cos \theta_{T}, \phi_{T}, \cos \psi_{T}\}$$

### Angular Probability Distribution: time evolution

• Separate terms for  $B_s^0$ ,  $\bar{B}_s^0$ 

$$\mathcal{T}_{\pm} = e^{-\Gamma t} \left[ \cosh \left( \frac{\Delta \Gamma}{2} t \right) \mp \cos(2\beta_s) \sinh \left( \frac{\Delta \Gamma}{2} t \right) \mp \eta \sin(2\beta_s) \sin(\Delta m_s t) \right]$$

where  $\eta = +1$  for P and -1 for  $\bar{P}$ 

$$\mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times \left[ \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t) - \cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_s) \sin(\Delta m_s t) \right]$$

$$\pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_s) \sinh\left(\frac{\Delta \Gamma t}{2}\right)$$

$$\mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times \left[ \sin(\delta_{\perp}) \cos(\Delta m_s t) - \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t) \right]$$

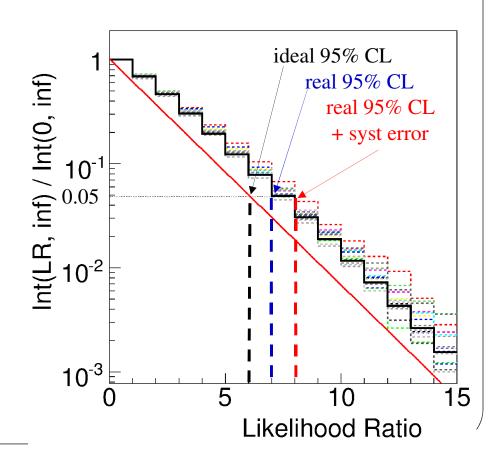
$$\pm \left[ \cos(\delta_{\perp}) \sin(2\beta_s) \sinh\left(\frac{\Delta \Gamma t}{2}\right) \right]$$
Terms with  $\Delta m_s$  dependence; they are different for different initial state flavor

 $\delta_{\parallel}$  = arg( $A_{\parallel} A_0^*$ ),  $\delta_{\perp}$  = arg( $A_{\perp} A_0^*$ ) are the phases of  $A_{\parallel}$  and  $A_{\perp}$  relative to  $A_0$ Knowledge of  $B_s^0$  mixing frequency needed(well measured by CDF- $\frac{3}{2}$ 0)

#### **Systematics**

- Systematic uncertainties studied by varying all nuisance parameters +/-  $5 \sigma$  from observed values and repeating LR curves (dotted histograms)
- Nuisance parameters:
  - lifetime, lifetime scale factor uncertainty,
  - strong phases,
  - transversity amplitudes,
  - background angular and decay time parameters,
  - dilution scale factors and tagging efficiency
  - mass signal and background parameters
  - ...

- Take the most conservative curve (dotted red histogram) as final result



## CP violating phases: $\phi_s$ vs $\beta_s$

- $2\beta_s = 2 \text{arg} \left[ -V_{ts} V_{tb}^* / V_{cs} V_{cb}^* \right] \sim 4.4^\circ \text{ (SM)} \text{ phase of } b \rightarrow ccs$  transition that accounts for interference of decay and mixing+decay
- $\phi_s = arg[-M_{12}/\Gamma_{12}] \sim 0.24^\circ$  (SM)  $arg[M_{12}] = arg(V_{tb}V_{ts}^*)^2$  matrix element that connects matter to antimatter through oscillation.
  - $arg[\Gamma_{12}] = arg[(V_{cb}V^*_{cs})^2 + V_{cb}V^*_{cs}V_{ub}V^*_{us} + (V_{ub}V^*_{us})^2]$  width of matter and antimatter into common final states.
  - Both SM values experimentally unaccessible by current experiments (assumed zero). If NP occurs in mixing:

$$\begin{split} & \varphi_{\text{s}} = \varphi_{\text{s}}^{\text{ SM}} + \varphi_{\text{s}}^{\text{ NP}} \thicksim \varphi_{\text{s}}^{\text{ NP}} \\ & 2\beta_{\text{s}} = 2\ \beta_{\text{s}}^{\text{ SM}} - \varphi_{\text{s}}^{\text{ NP}} \thicksim - \varphi_{\text{s}}^{\text{ NP}} \end{split}$$

- ▶ B → VV (our B<sub>s</sub><sup>0</sup> → J/ψ φ but also B<sup>0</sup> → J/ψ K\*<sup>0</sup>, ...) decay to two CP even states (S-wave or D-wave) and one CP odd (P-wave)
- Alternatively to the S,P,D-wave states one can use the "transversity basis": the three independent components in which the vector mesons polarizations w.r.t. their direction of motion are:
  - longitudinal (0) CP even - transverse but parallel to each other (||)
  - transverse but perpendicular to each other (\(\preceq\)\) CP odd

Each final pol.state  $P_0, P_{\parallel}, P_{\parallel}$  has transition amplitude  $A_0, A_{\parallel}, A_{\parallel}; \langle B^0 | P \rangle = A_0$ The  $\langle B^0_{s,phys}(t) | P \rangle = A(t)$  are convolutions of decay and oscillation

