Abstract

We present a parametrization for the Dark Energy (DE) Equation of State (EoS) that has a transition at pivotal redshift $z_T$ between the present day value $w_0$ to an early time $w_i$ and the steepness of this transition is given in terms of the $\theta$ parameter. We study if a late time transition is favored by BAO measurements and Planck priors.

According to our results, an EoS with a present value of $w_0 = -0.91$ and a high redshifts value $w_i \equiv w(z \to \infty) = w_0 - w_{z_T} = -0.62$, featuring a transition at a redshift of $z_T = 1.16$ with an exponent $\theta = 0.95$ is a good fit to the observational data. We found good agreement between the model and the data reported by the different surveys.

The constraints imposed by the available BAO measurements and its physical behavior are discussed.

Parametrization of the DE EoS

We are modeling the DE equation of state (EoS) with the following parametrization:

$$w_d(z) = w_0 + (w_i - w_0) \left( \frac{1}{1 + \left( \frac{z}{z_T} \right)^\theta} \right)^\theta$$

where $w_0$ and $w_i$ represent the value for $w(z)$ at large redshifts and at present day, respectively whereas $z_T$ represents the transition redshift in between both values with its steepness modulated by $\theta$. This transition is motivated by scalar field dynamics such as for example quintessence models.

![Evolution of the EoS for the best fit models found by minimizing the $\chi^2$ function for different data sets and intervals for the parameters minimized.](image)

Figure: Evolution of the EoS for the best fit models found by minimizing the $\chi^2$ function for different data sets and intervals for the parameters minimized.

For $z_T = q = 1$ our parametrization reduces to the Taylor expansion EoS $w = w_0 + w_i (1 - a)$ widely used in many cosmological observational analysis. The value of $w_0$ is restricted by observations to be close to $-1$ ($w = -1.55^{+0.06}_{-0.08}$) according to the 95% limits imposed by Planck TT, TE, EE latest measurements [Ade et al., 2015]. Nevertheless, the behavior and properties at different cosmic epochs is much poorly constrained by current observations.

Observational Data: BAO

We made use of the observational points from the six-degree-field galaxy survey (6dFGS [Beutler et al., 2011]), Sloan Digital Sky Survey Data Release 7 and 11 (SDSS DR7 [Ross et al., 2015] and SDSS DR11 [Anderson et al., 2014]), the WiggleZ dark energy survey [Kozin et al., 2014]) and the Lyman $\alpha$ Forest (Ly-$\alpha$-F) measurements from the Baryon Oscillation Spectroscopic Data Release 11 (BOSS DR11 [Font-Ribera et al., 2014], [Delubac et al., 2015]) as analyzed and reported by Gong et al 2015 [Gong et al., 2015]. Additionally to the free parameters in the equation 1 we also investigate the constraints on $\Omega_m$ and $H_0$ (or equivalently $h$), resulting in the set $\theta = \{w_0, w_i, q, \Omega_m, H_0\}$. Using this data sets we minimized the relative $\chi^2$ function. When including the information from Planck $\pm 1\sigma$ in the limits to constrain $\Omega_m$ and $H_0$, we labeled those results as “BAO + Planck”, otherwise they were labeled “BAO”.

![Figure: Fitting to the observational data points by the resulting best fit models.](image)

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Constraints

When using the BAO measurements we got a reduced chi-squared function of $\chi^2_{red} = 0.95$ and parameters $\{w_0 = -0.91, w_i = -0.62, z_T = 1.16, q = 9.95, \Omega_m = 0.3247, H_0 = 60.67\}$. We found weak constraints on the value for the new parameters $z_T$ and $\theta$ as shown in this 3D contour plot displaying the 1-$\sigma$ (orange)-2-$\sigma$ (blue) contours around the minimum.

![The $w_0$ vs $w_i$ space of parameters.](image)

Figure: The $w_0$ vs $w_i$ space of parameters.

Comparison to LCDM

![Figure: BAO contours in blue and “BAO+Planck” in green.](image)

Figure: Figure (a) shows the contours corresponding to $r_{BAO}(z)$ measurements while (b) corresponds to $D_V(z)$ data. In blue we portrait the contours corresponding to the BFM and the LCDM contours are shown in red.

Planck Priors

![Figure: Comparison of the different data: $r_{BAO}(z)$ with or without Ly-$\alpha$-F measurements and $D_V(z)$.](image)

Different data sets

![Figure: Comparison of the different data: $r_{BAO}(z)$ with or without Ly-$\alpha$-F measurements and $D_V(z)$.](image)

Conclusions

A steep EoS for the DE was favored by the available BAO data when including Planck priors. We obtained good fittings to the observational data and a very steep EoS as result from numerical minimization. We compared the results obtained by using $r_{BAO}(z)$ data including and excluding the Ly-$\alpha$-F measurements and when using $D_V(z)$ measurements instead. The comparison to LCDM model was investigated and some tension was found when $D_V(z)$ data was used. The impact of the priors from Planck was also analyzed and led us to the same conclusion. Finally, the use of the Ly-$\alpha$-F points in $r_{BAO}(z)$ data set was studied and found they restrict the values of $h$ and $\Omega_m$.

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