

Calculating Jet Shape Modifications in Heavy Ion Collisions Using Soft-Collinear Effective Theory

Yang-Ting Chien

Los Alamos National Laboratory

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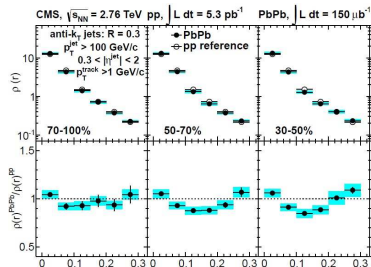
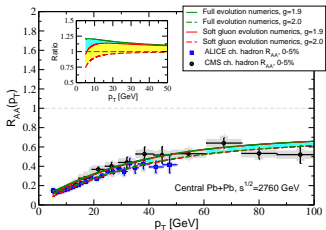
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In collaboration with Ivan Vitev

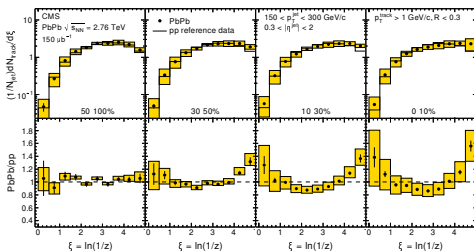
Outline

- Jet quenching and modification
 - Jet shapes in proton and heavy ion collisions
- Resummation using Soft-Collinear Effective Theory (SCET)
 - Factorization theorem
 - Renormalization group evolution
- Medium Modification using SCET with Glauber gluons (SCET_G)
 - Medium induced splitting functions
 - Modifications at first order in opacity expansion
- Preliminary results

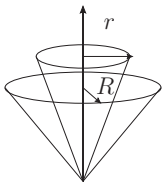
Jet quenching phenomenology



- Charged hadron suppression (R_{AA})
 - Hadron/Jet **quenching**
 - **Kinematics**
- Modifications of jet shapes and jet fragmentation functions
 - Medium **modification**
 - **Jet substructure**
- Measurements at CMS
 - PLB 730 (2014) 243
 - PRC 90 (2014) 024908



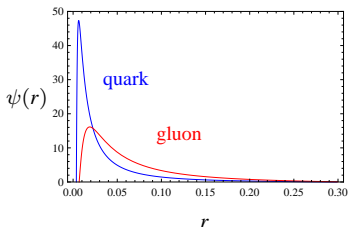
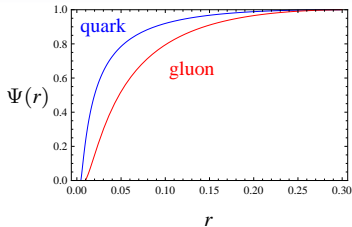
Jet shape, a classic jet substructure observable (Ellis, Kunszt, Soper)



$$\Psi_J(r, R) = \frac{\sum_{r_i < r} E_{Ti}}{\sum_{r_i < R} E_{Ti}}$$

$$\langle \Psi \rangle = \frac{1}{N_J} \sum_J \Psi_J(r, R)$$

$$\psi(r, R) = \frac{d\langle \Psi \rangle}{dr}$$



- Jet shapes probe the energy distribution inside a jet
- Quark jets are more localized whereas gluon jets are more spread out
- Quark-gluon discrimination
- The infrared structure of QCD induces Sudakov logarithms
- Fixed order calculation breakdowns at small r
- Large logarithms of the form $\alpha_s^n \log^m r/R$ ($m \leq 2n$) need to be resummed

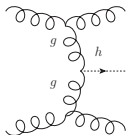
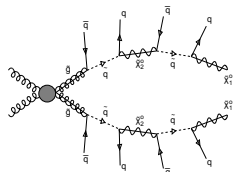
Jet shapes in proton and heavy ion collisions

In **proton** collisions,

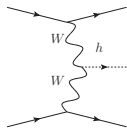
- Quark-gluon discrimination
 - Many SM and BSM signals are quark-heavy
 - QCD backgrounds are mostly gluon-heavy
- Boosted particle (H , W , Z , t) tagging
- Standard input for tuning Monte Carlo event generators

In **heavy ion** collisions,

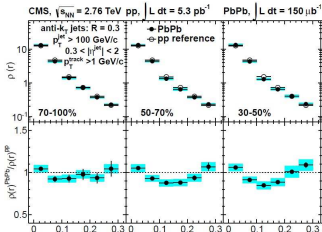
- Probing the properties of the QGP
 - Modification of jet shapes is sensitive to the medium properties
 - Quark and gluon jets are modified differently
- Underlying events are a big issue
 - η -reflected background subtraction at CMS
- As in proton collisions, initial state radiation and non-perturbative effects are power corrections which have sizable effects at the peripheral of jets
- Precision calculation of jet shapes involves a lot more complications



gluon fusion



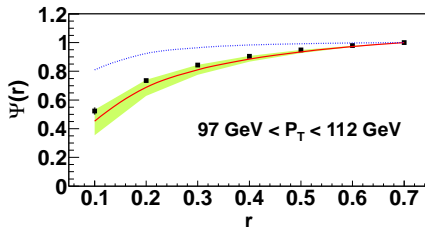
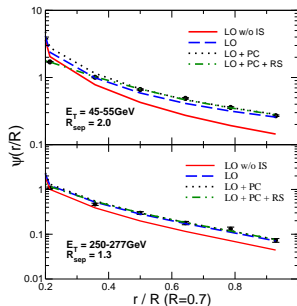
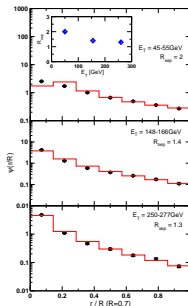
vector boson fusion



Jet shape calculations with pQCD (Seymour, Vitev et al, and Yuan et al.)

In **proton** collisions,

- pQCD calculation with a parameter R_{sep} fits the CDF data.
 - R_{sep} : effective angular separation in leading-order parton splitting
 - Resummation using the modified leading logarithmic approximation
 - Initial state radiation and power corrections examined
- Resummation performed differently in another pQCD calculation
 - The LO result is not enough
- The jet algorithm dependence still needs to be explored
 - iterative cone algorithm at Tevatron
 - anti- k_T algorithm at the LHC
- Formation of jets (physical) from partons (unphysical) is already quite nontrivial in proton collisions



Jet shape calculations with pQCD and energy loss (Vitev et al)

In **heavy ion** collisions,

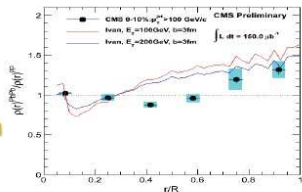
- The jet shape modification is not well described by the energy loss formalism
- We will use effective field theory techniques to expand the full QCD contributions with a systematic power counting

■ A preliminary result

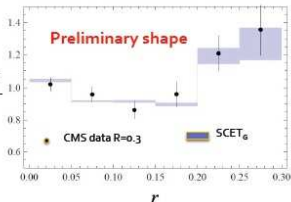
- Need to combine with the splitting functions evaluated numerically for the same medium geometry and expansion, present predictions for the upcoming run at the LHC

- Even with the caveats, the improvement in the calculation can be significant

Y.-T. Chien et al. In preparation

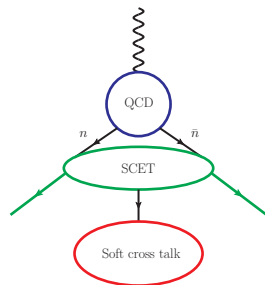


$$\frac{\Psi(r)^{PbPb}}{\Psi(r)^{PP}}$$



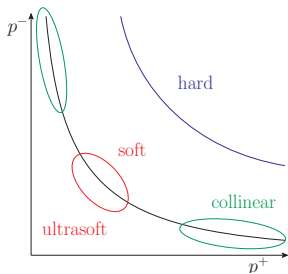
Soft-Collinear Effective Theory (SCET)

- Effective field theory techniques are most useful when there is clear scale separation
- SCET separates physical degrees of freedom in QCD by a systematic expansion in power counting
 - Match SCET with QCD at the hard scale by integrating out the **hard** modes
 - Integrating out the off-shell modes gives **collinear Wilson lines** which describe the collinear radiation
 - The soft sector is described by **soft Wilson lines** along the jet directions
- Soft-collinear decoupling holds at leading power in the Lagrangian, which leads to the factorization theorems of cross sections



Power counting in SCET

- The scaling of modes:
 - $p_h : Q(1, 1, 1)$, $p_c : Q(1, \lambda^2, \lambda)$ and $p_s : Q(\lambda, \lambda, \lambda)$
- Q is at the **hard** scale which is the energy of the jet
- λ is the power counting parameter satisfying $\lambda < R$
 - The energy outside jets is power suppressed
- QCD = $\mathcal{O}(\lambda^0) + \mathcal{O}(\lambda^1) + \dots$ in SCET
- $Q\lambda$ is the **jet** scale which is significantly lower than Q



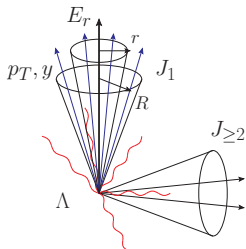
- Jet shapes have dominant contributions from the **collinear** sector

$$\Psi(r) = \frac{E_c^{<r} + E_s^{<r}}{E_c^{<R} + E_s^{<R}} = \frac{E_c^{<r}}{E_c^{<R}} + \mathcal{O}(\lambda)$$

- Contributions from the (ultra)soft mode are power suppressed
- λ is typically small because of dynamical threshold enhancement
- For high p_T and small jets, power corrections are small and the leading power contribution is a very good approximation of the full QCD result
- Contributions of $\mathcal{O}(r)$ and $\mathcal{O}(R)$ are small and power suppressed, but contributions of $\mathcal{O}(r/R)$ are not necessarily small

Factorization theorem for jet shapes in proton collisions

- Without loss of generality, we demonstrate the calculation in e^+e^- collisions since the initial state radiation in proton collisions contributes as power corrections



- The factorization theorem for the differential cross section of the production of N jets with p_{T_i}, y_i , the energy E_r inside the cone of size r in **one** jet, and an energy cutoff Λ outside all the jets is the following,

$$\frac{d\sigma}{dp_{T_i} dy_i dE_r} = H(p_{T_i}, y_i, \mu) J_1^{\omega_1}(E_r, \mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)$$

- For the differential jet rate (without measuring E_r)

$$\frac{d\sigma}{dp_{T_i} dy_i} = H(p_{T_i}, y_i, \mu) J_1^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)$$

- Here $J_1^{\omega}(E_r, \mu) = \sum_{X_c} \langle 0 | \bar{\chi}_{\omega}(0) | X_c \rangle \langle X_c | \chi_{\omega}(0) | 0 \rangle \delta(E_r - \hat{E}^{<r}(X_c, \text{algorithm}))$ and $\omega = 2E_J$ is twice the jet energy and is the label of the collinear jet field in SCET
- $J_i^{\omega}(\mu)$ are the "unmeasured jet functions" (Ellis et al)
- All the jet and soft functions have the R dependence from the jet algorithm

Factorization theorem for jet shapes (continued)

The averaged energy inside the cone of size r in jet 1 is the following

$$\langle E_r \rangle_\omega = \frac{1}{\frac{d\sigma}{dp_{Ti}dy_i}} \int dE_r E_r \frac{d\sigma}{dp_{Ti}dy_i dE_r} = \frac{H(p_{Ti}, y_i, \mu) J_{E,r1}^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)}{H(p_{Ti}, y_i, \mu) J_1^{\omega_1}(\mu) J_2^{\omega_2}(\mu) \dots S_{1,2,\dots}(\Lambda, \mu)} = \frac{J_{E,r1}^{\omega_1}(\mu)}{J_1^{\omega_1}(\mu)}$$

Here $J_{E,r}^\omega(\mu) = \int dE_r E_r J^\omega(E_r, \mu)$ is referred to as the "jet energy function."

- All the hard, unmeasured jet and soft functions cancel
- The integral jet shape, averaged over all jets, is the following

$$\langle \Psi \rangle = \frac{1}{\sigma_{\text{total}}} \int_{PS} dp_T dy \frac{d\sigma}{dp_T dy} \Psi_\omega, \text{ where } \Psi_\omega = \frac{J_{E,r}(\mu)/J(\mu)}{J_{E,R}(\mu)/J(\mu)} = \frac{J_{E,r}(\mu)}{J_{E,R}(\mu)}$$

- Using the collinear SCET Feynman rules, the jet energy function $J_{E,r}(\mu)$ and its anomalous dimension are calculated at $\mathcal{O}(\alpha_s)$ for both quark jets and gluon jets

Renormalization group evolution of jet energy functions

$$\frac{dJ_{E,r}^q(r, R, \mu)}{d \ln \mu} = \left[-C_F \Gamma_{\text{cusp}} \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma_{J^q} \right] J_{E,r}^q(r, R, \mu)$$

$$\frac{dJ_{E,r}^g(r, R, \mu)}{d \ln \mu} = \left[-C_A \Gamma_{\text{cusp}} \ln \frac{\omega^2 \tan^2 \frac{R}{2}}{\mu^2} - 2\gamma_{J^g} \right] J_{E,r}^g(r, R, \mu)$$

- The anomalous dimensions of the jet energy functions are

$$\gamma_{J^q} = -3C_F, \quad \gamma_{J^g} = -\beta_0 = -\frac{11}{3}C_A + \frac{4}{3}T_F n_f$$

- The same anomalous dimensions as the unmeasured jet functions
- The anomalous dimensions are R dependent and r independent
- Ψ_ω is renormalization group invariant

$$\Psi_\omega = \frac{J_{E,r}(\mu)}{J_{E,R}(\mu)} = \frac{J_{E,r}(\mu_{j_r})}{J_{E,R}(\mu_{j_R})} U_J(\mu_{j_r}, \mu_{j_R})$$

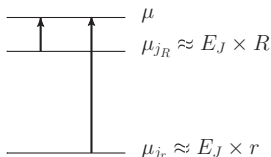
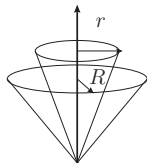
- Identify the natural scale μ_{j_r} to eliminate large logarithms in $J_{E,r}(\mu_{j_r})$
- The RG evolution kernel $U_J(\mu_{j_r}, \mu_{j_R})$ resums the large logarithms

Natural scales

- The quark jet energy function at $\mathcal{O}(\alpha_s)$ is the following

$$\frac{2}{\omega} J_{E,r}^q = \frac{\alpha_s C_F}{2\pi} \left[\frac{1}{2} \ln^2 \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} - \frac{3}{2} \ln \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} - 2 \ln X \ln \frac{\omega^2 \tan^2 \frac{r}{2}}{\mu^2} + 2 - \frac{3\pi^2}{4} \right. \\ \left. + 6X - \frac{3}{2}X^2 - \left(\frac{1}{2}X^2 - 2X^3 + \frac{3}{4}X^4 + 2X^2 \log X \right) \tan^2 \frac{R}{2} \right], \text{ where } X = \frac{\tan \frac{r}{2}}{\tan \frac{R}{2}} \approx \frac{r}{R}$$

- The scale $\mu_{j_r} = \omega \tan \frac{r}{2} \approx E_J \times r$ eliminates large logarithms in $J_{E,r}^q$ at $\mathcal{O}(\alpha_s)$
- $J_{E,r}(\mu)$ and $J_{E,R}(\mu)$ have the same anomalous dimensions but different scales



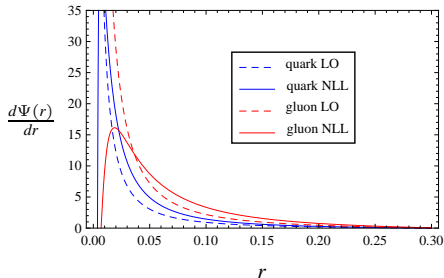
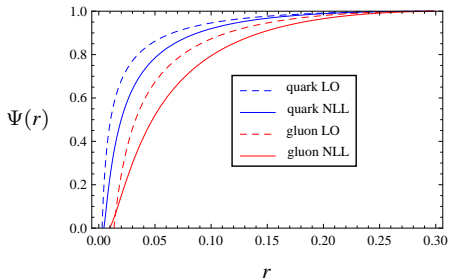
RG evolution between μ_{j_r} and μ_{j_R} resums $\log \mu_{j_r} / \mu_{j_R} = \log r / R$

Resummed jet energy functions

- $\log r/R$ are resummed using the RG kernels in SCET ($i = q, g$)

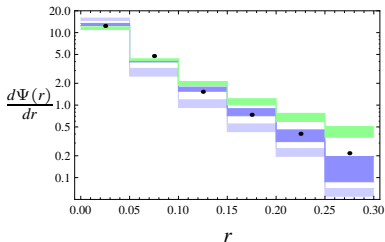
$$\Psi_{\omega}^i(r, R) = \frac{J_r^{iE}(r, R, \mu_{j_r})}{J_R^{iE}(R, \mu_{j_R})} \exp[-2 C_i S(\mu_{j_r}, \mu_{j_R}) + 2 A_{j_i}(\mu_{j_r}, \mu_{j_R})] \left(\frac{\mu_{j_r}^2}{\omega^2 \tan^2 \frac{R}{2}} \right)^{C_i A_{\Gamma}(\mu_{j_R}, \mu_{j_r})}$$

$$S(\nu, \mu) = - \int_{\alpha_s(\nu)}^{\alpha_s(\mu)} d\alpha \frac{\Gamma_{\text{cusp}}(\alpha)}{\beta(\alpha)} \int_{\alpha_s(\nu)}^{\alpha} \frac{d\alpha'}{\beta(\alpha')}, \quad A_X(\nu, \mu) = - \int_{\alpha_s(\nu)}^{\alpha_s(\mu)} d\alpha \frac{\gamma_X(\alpha)}{\beta(\alpha)}$$



- Integral and differential jet shapes of 100 GeV quark and gluon jets at LO and NLL

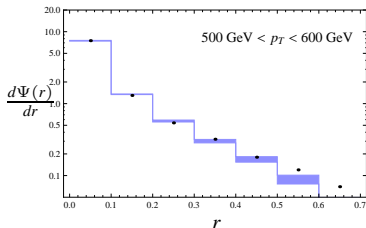
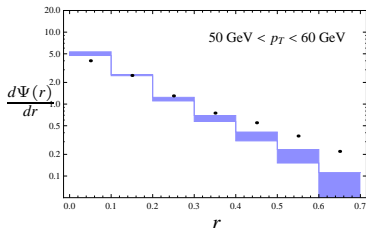
Comparison with the CMS data at 2.76 TeV



– Differential jet shapes in proton collisions with the center of mass energy at 2.76 TeV

- The blue bands (LO and NLL) are for $R=0.3$ anti- k_T jets with $p_T > 100$ GeV and $0.3 < |\eta| < 2$
 - Resummation is necessary
- The green band is for $R=0.3$ cone jets
 - The difference for jets reconstructed using different algorithms is of $\mathcal{O}(r/R)$
- Bands are theory uncertainties estimated by varying μ_{j_r} and μ_{j_R}
- In the region $r \approx R$ we may need higher fixed order calculations and include power corrections

Comparison with the CMS data at 7 TeV

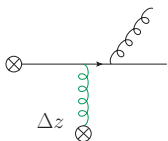


- The blue band (NLL) is for $R=0.7$ anti- k_T jets with $|\eta| < 1$
- For low p_T jets, power corrections give significant contributions
- For high p_T jets, the SCET calculation reproduces the peak region very well

SCET works in jet shapes in proton collisions

– Differential jet shapes in proton collisions with the center of mass energy at 7 TeV

Jets in heavy ion collisions



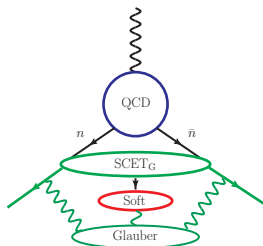
- Ultra-relativistic heavy ion collisions create a strongly interacting medium which is referred to as the Quark-Gluon Plasma (QGP)
- Jets passing through QGP are observed to be quenched
- Coherent multiple scattering and induced radiation play an important role in jet modifications
- From thermal field theory and lattice QCD calculations, the picture of quasi-particles with Debye-screened potentials and masses seems to be a reasonable modeling of the local properties of QGP (the Gyulassy-Wang model)
- Depending on the relative sizes of radiation formation time and parton mean free path, the Landau-Pomeranchuk-Migdal (LPM) effect can be sizable

$$\frac{x E}{(q_{\perp} - k_{\perp})^2} \text{ v.s. } \Delta z$$

- There have been at least four approaches in capturing the LPM effect in the context of parton multiple scattering (AMY, BDMPS/Z, Higher-Twist and GLV)
- Can we extend SCET to describe the formation of jets in the QGP?

SCET with Glauber gluons (SCET_G)

- From the pinch analysis, the Glauber region of phase space is the other relevant mode
- SCET_G was constructed from SCET bottom up (Idilbi et al, Vitev et al)
 - Glauber gluon momentum scales as $p_G : Q(\lambda^2, \lambda^2, \lambda)$
 - Glauber gluons are off-shell modes providing momentum transfer transverse to the jet direction
 - Glauber gluons are treated as background fields generated from the colored charges in the QGP
- In principle, Glauber gluons interact with both the collinear and the soft modes
- However, jet shapes have dominant contributions from the collinear sector so the Glauber-collinear interaction is the most relevant



Jet shape modifications in heavy ion collisions

- The jet energy function can be calculated from integrating the splitting functions $dN_{i \rightarrow jk}/dx d^2k_{\perp}$ over an appropriate phase space. At leading order,

$$J_{E,r}^i(\mu) = \sum_{j,k} \int_{PS} dx dk_{\perp} \frac{dN_{i \rightarrow jk}}{dx d^2k_{\perp}} E_r(x, k_{\perp})$$

- Medium-induced splitting functions have been calculated using SCET_G (Vitev et al). Just to illustrate, in the small- x limit,

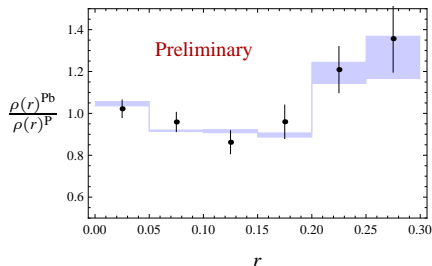
$$\frac{dN_{q \rightarrow qg}^{med}}{dx d^2k_{\perp}} = \frac{C_F \alpha_s}{\pi^2} \frac{1}{x} \int_0^L \frac{d\Delta z}{\lambda} \int d^2q_{\perp} \frac{1}{\sigma_{el}} \frac{d\sigma_{el}}{d^2q_{\perp}} \frac{2k_{\perp} \cdot q_{\perp}}{k_{\perp}^2 (q_{\perp} - k_{\perp})^2} \left[1 - \cos\left(\frac{(q_{\perp} - k_{\perp})^2 \Delta z}{x\omega}\right) \right]$$

- Jet shapes get modified through the modification of jet energy functions

$$\Psi(r) = \frac{J_{E,r}^{vac} + J_{E,r}^{med}}{J_{E,R}^{vac} + J_{E,R}^{med}} = \frac{J_{E,r}^{vac}}{J_{E,R}^{vac}} \frac{J_{E,R}^{vac}}{J_{E,R}^{vac} + J_{E,R}^{med}} + \frac{J_{E,r}^{med}}{J_{E,R}^{vac} + J_{E,R}^{med}}$$

- Large logarithms in $\Psi^{vac}(r) = J_{E,r}^{vac}/J_{E,R}^{vac}$ have been resummed
- There are no large logarithms in $J_{E,r}^{med}$ at first order in opacity $\mathcal{O}(L/\lambda)$ due to the LPM effect
- The RG evolution of medium-modified jet energy functions is the same

Preliminary result



- We plot the ratio of the differential jet shapes in lead-lead and proton collisions for gluon jets with $p_T = 100$ GeV and $y = 0$
- The data is for the centrality bin between 30 – 50%
- Jet shapes have to be averaged with the appropriate cross sections
- Power corrections are important around $r \approx R$
- The preliminary result above uses a static QGP model with $\lambda_g = 1$ fm, $L = 3$ fm, $m = 0.75$ GeV

Conclusions

- Jet shapes in proton collisions are calculated in the SCET collinear sector
 - The factorization theorem is written down
 - Jet energy functions are calculated at $\mathcal{O}(\alpha_s)$ for quark and gluon jets
 - Large logarithms are resummed to NLL using RG evolution
- Jet shapes in heavy ion collisions are calculated in SCET_G
 - Medium-induced splitting functions are used to calculate the modification of jet energy function
 - Preliminary results agree with the CMS data very well
- Work in progress and future work
 - Check the numerics of jet shape modifications with a more realistic QGP model
 - Making predictions for the LHC Run-2
 - Paper in preparation (hopefully arXiv:150n.xxxx with $2 \leq n \leq 4$)
 - Calculate the modification of jet fragmentation function using SCET_G
 - ...