

Two Higgs Doublets – with and without Dark Matter

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From Higgs to Dark Matter
Geilo, Norway, 2014-12-15

Outline

1. Two Higgs doublets
2. 2HDM with dark matter
3. 2HDM at the LHC (without dark matter)

Disclaimer: Not a review. Highly biased on my own work.

Extensive recent work on different aspects of this model:

Ferreira, Santos, Branco, Silva, Osland, Moretti, Lipniacka, Pruna, Haber, Kraml, Gunion, Grzadkowski, Krawczyk, Pich, Tuzon, Carena, Wagner, Yaguna, Lopez-Val, Plehn, Rathsman, Nierste, Wiebusch, Craig, Thomas, Reece, Mühlleitner, Spira, Harlander, Liebler, ..., ...

The general two-Higgs-doublet Model (2HDM)

- Two complex SU(2) doublets ($Y=1$): Φ_1, Φ_2

- Scalar potential:

$$\begin{aligned} V_{2\text{HDM}} = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - \left[m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] \\ & + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) \\ & + \left\{ \frac{1}{2} \lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \left[\lambda_6 \left(\Phi_1^\dagger \Phi_1 \right) + \lambda_7 \left(\Phi_2^\dagger \Phi_2 \right) \right] \left(\Phi_1^\dagger \Phi_2 \right) + \text{h.c.} \right\} \end{aligned}$$

- Complex phases on $\lambda_5, \lambda_6, \lambda_7$ and m_{12} can give rise to tree-level **CP-violation** (restricted by data). This talk: CP conservation.
- Reparametrization invariance: $\Phi_a = U_{ab} \Phi_b \quad (a = 1, 2)$

The general two-Higgs-doublet Model (2HDM)

- Introducing an explicit basis in (Φ_1, Φ_2) space: $\tan \beta = \frac{v_2}{v_1}$

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \cos \beta - H^+ \sin \beta) \\ v \cos \beta - h \sin \alpha + H \cos \alpha + i (G^0 \cos \beta - A \sin \beta) \end{pmatrix}$$

$$\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \sin \beta + H^+ \cos \beta) \\ v \sin \beta + h \cos \alpha + H \sin \alpha + i (G^0 \sin \beta + A \cos \beta) \end{pmatrix}$$

- Five physical Higgs states following EWSB:

Two CP-even Higgs bosons: h, H

$m_h < m_H$, mixing angle α

One CP-odd Higgs boson: A

One charged Higgs pair: H^{\pm}



2HDM with Dark Matter

Mainly based on A. Goudelis, B. Herrmann, OS, [1303.3010]

The Higgs basis

- Among all basis choices, there is a special case: the *Higgs basis*
Only one of the doublets acquires a vev

$$H_1 = \cos \beta \Phi_1 + \sin \beta \Phi_2 \quad \langle H_1^0 \rangle = \frac{v}{\sqrt{2}} \quad \langle H_2^0 \rangle = 0$$

$$H_2 = -\sin \beta \Phi_1 + \cos \beta \Phi_2$$

$$\begin{aligned} \mathcal{V} = & Y_1 H_1^\dagger H_1 + Y_2 H_2^\dagger H_2 + [Y_3 H_1^\dagger H_2 + \text{h.c.}] \\ & + \frac{1}{2} Z_1 (H_1^\dagger H_1)^2 + \frac{1}{2} Z_2 (H_2^\dagger H_2)^2 + Z_3 (H_1^\dagger H_1) (H_2^\dagger H_2) + Z_4 (H_1^\dagger H_2) (H_2^\dagger H_1) \\ & + \left\{ \frac{1}{2} Z_5 (H_1^\dagger H_2)^2 + [Z_6 (H_1^\dagger H_1) + Z_7 (H_2^\dagger H_2)] H_1^\dagger H_2 + \text{h.c.} \right\} , \end{aligned}$$

- Imposing an exact Z_2 symmetry in this basis there is *no mixing* between the doublets. The second doublet (without Yukawa couplings) becomes *inert*. Inert Doublet Model (IDM)

Ma, [hep-ph/0601255]; Barbieri, Hall, Rychkov, [hep-ph/0603188]

IDM at leading order

- Scalar potential:

$$V_0 = \mu_1^2 |H|^2 + \mu_2^2 |\Phi|^2 + \lambda_1 |H|^4 + \lambda_2 |\Phi|^4 + \lambda_3 |H|^2 |\Phi|^2 + \lambda_4 |H^\dagger \Phi|^2 + \frac{\lambda_5}{2} [(H^\dagger \Phi)^2 + \text{h.c.}]$$

- One doublet, H , is identified with SM Higgs

$$H = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + h^0 + iG^0) \end{pmatrix} \quad \Phi = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}} (H^0 + iA^0) \end{pmatrix}$$

Here: $m_{h^0} \simeq 125 \text{ GeV}$

- Lightest Z_2 -odd particle (LOP) stable \rightarrow Dark Matter candidate
 - Neutral DM candidate can be either H^0 or A^0 (equivalent)

Beyond leading order

- Model parametrizations

$$\{\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, \mu_2\} \quad \{m_{h^0}, m_{H^0}, m_{A^0}, m_{H^\pm}, \lambda_L, \lambda_S\}$$

are equivalent at leading order:

$$m_{h^0}^2 = \mu_1^2 + 3\lambda_1 v^2, \quad \lambda_L = \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)$$

$$m_{H^0}^2 = \mu_2^2 + \lambda_L v^2, \quad \lambda_S = \frac{1}{2}(\lambda_3 + \lambda_4 - \lambda_5)$$

$$m_{A^0}^2 = \mu_2^2 + \lambda_S v^2, \quad g_{h_{\text{SM}}H^0H^0} \propto \lambda_L$$

$$m_{H^\pm}^2 = \mu_2^2 + \frac{1}{2}\lambda_3 v^2, \quad g_{h_{\text{SM}}A^0A^0} \propto \lambda_S$$

- Beyond tree-level should relate input parameters to (in principle) measurable quantities (e.g. on-shell masses, couplings, ...)
Here: 1-loop calculation of pole masses (MSbar ren.)

Model constraints

- Perturbativity

$$|\lambda_i|, |g_i|, |y_i| \leq K. \quad K = 4\pi$$

- S-matrix unitarity for gauge/Higgs boson scattering

$$|f(\lambda_i(Q))| < C$$

Ginzburg, Ivanov, PRD72 (2005) 115010

- Positivity of the potential (*absolute stability*)

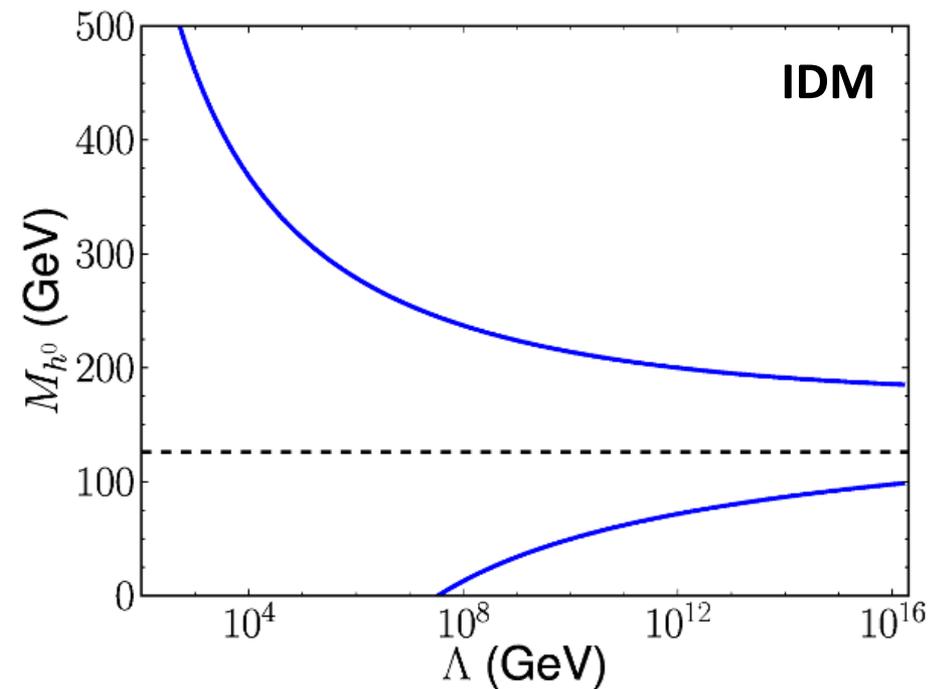
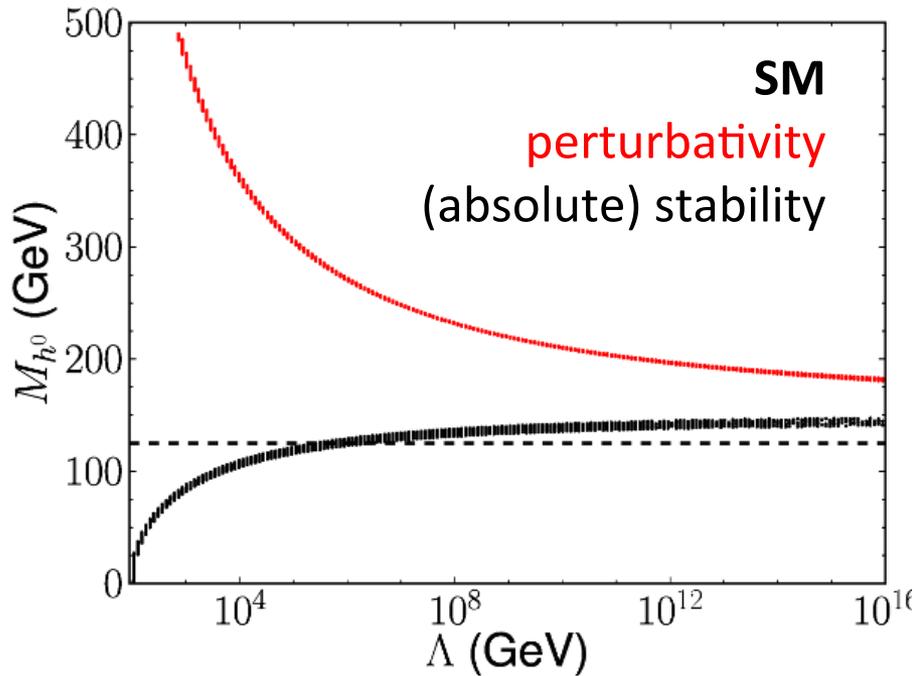
$$\lambda_1(Q), \lambda_2(Q) > 0,$$

$$\lambda_3(Q) > -2\sqrt{\lambda_1(Q)\lambda_2(Q)},$$

$$\lambda_3(Q) + \lambda_4(Q) - |\lambda_5(Q)| > -2\sqrt{\lambda_1(Q)\lambda_2(Q)}$$

- Constraints at input scale $Q = M_Z$, or higher scales (RGE)

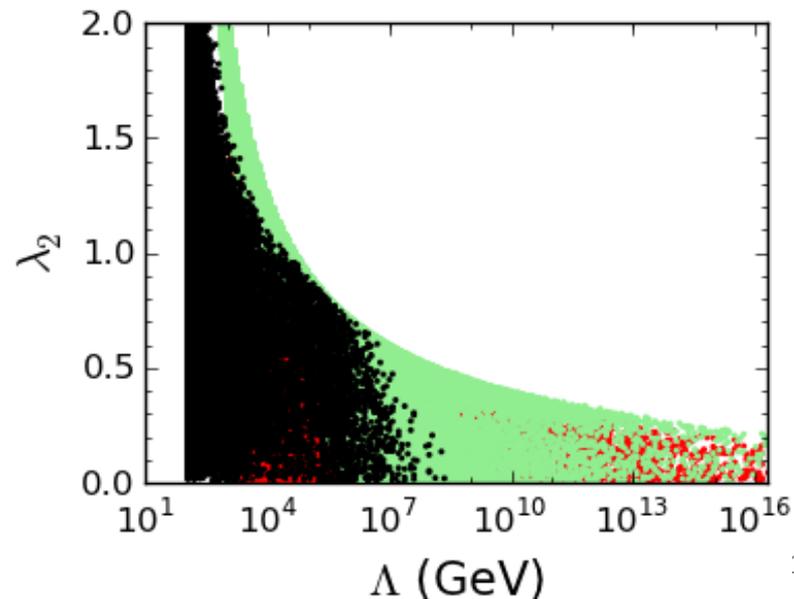
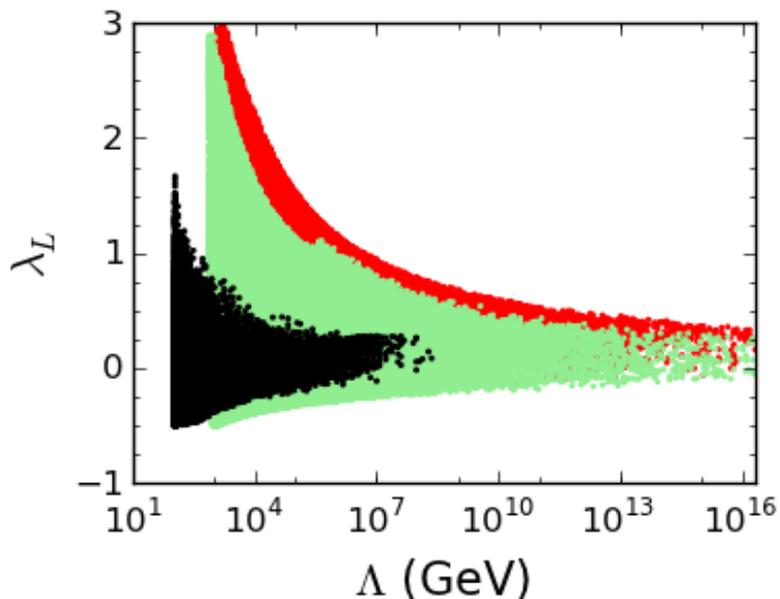
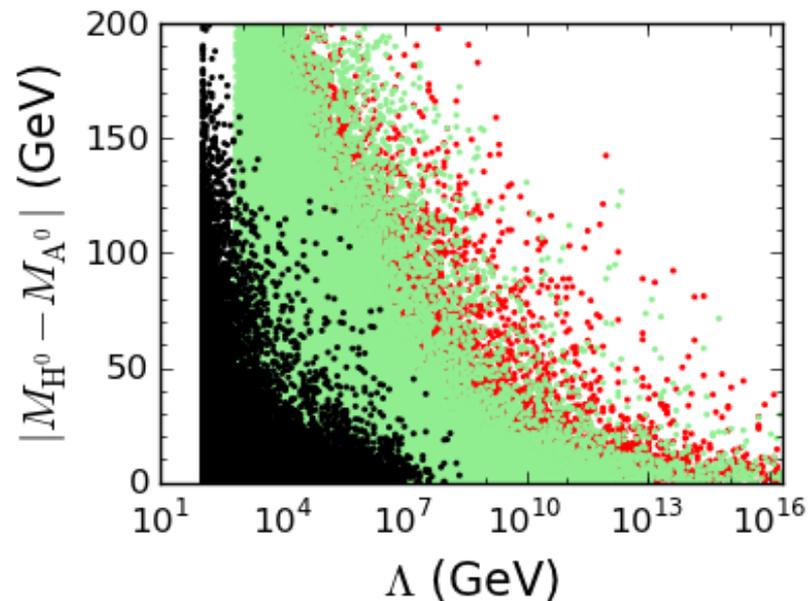
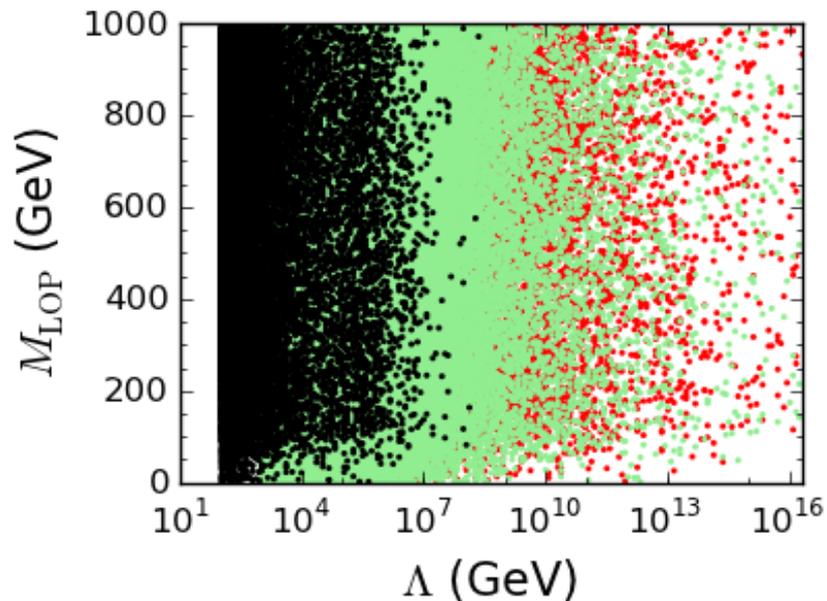
Stabilizing the vacuum



- Simple 1-loop RGE comparison, 1-loop pole masses (capital M_h)
- The second doublet can compensate top Yukawa coupling which drives the SM quartic negative
-> Absolute stability for $M_h = 125$ GeV possible up to high scales
(Beyond 1-loop SM somewhat improved) [Degrassi et al, \[1205.6497\]](#), [\[1307.3536\]](#)

1-loop RG analysis of the IDM

Perturbativity fails - Unitarity fails - Stability fails



DM Relic Density

- DM relic density calculated assuming thermal production
MicrOMEGAS (incl. 3/4-body final states)

Bélanger, Boudjema, Pukhov, Semenov, [1305.0237]

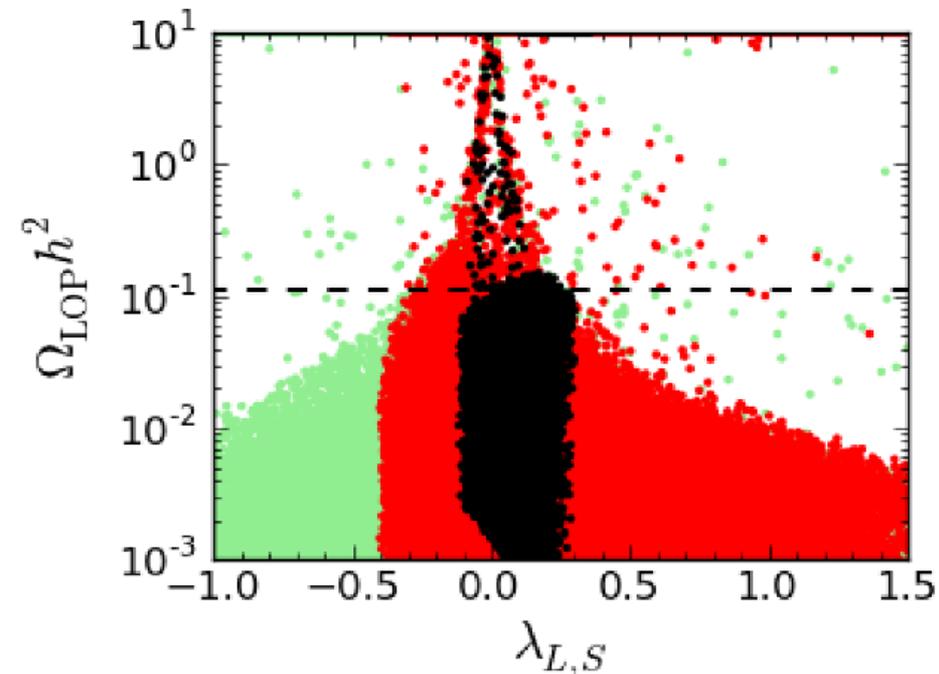
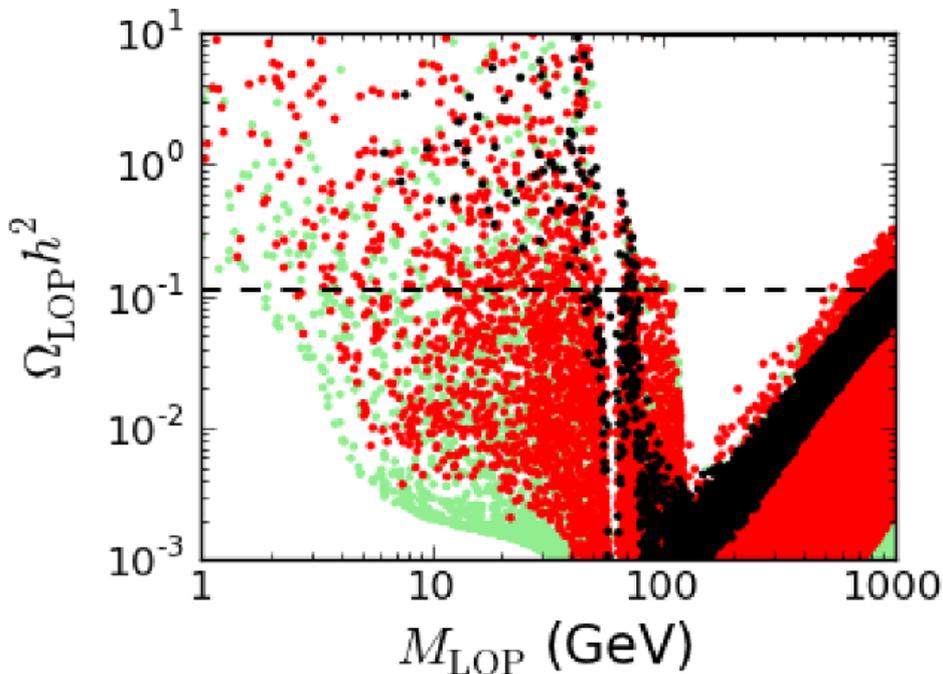
- Dotted line is WMAP 7-year limit (Planck similar)

$$0.1018 \leq \Omega_{\text{LOP}} h^2 \leq 0.1234$$

■ Point valid at input (EW) scale

■ Point valid up to (at least) $\Lambda = 10$ TeV

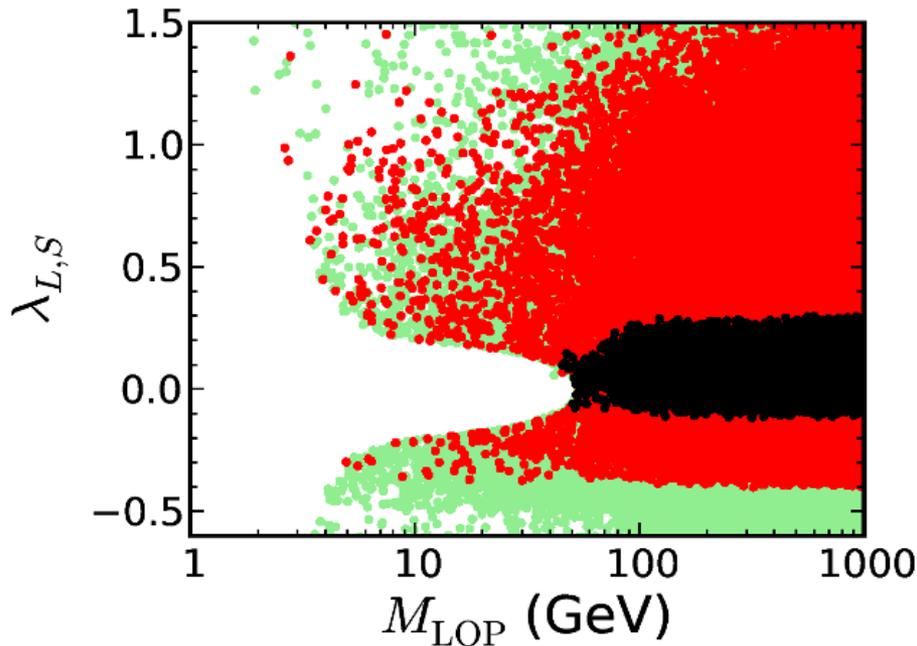
■ Point valid up to GUT scale (10^{16} GeV)



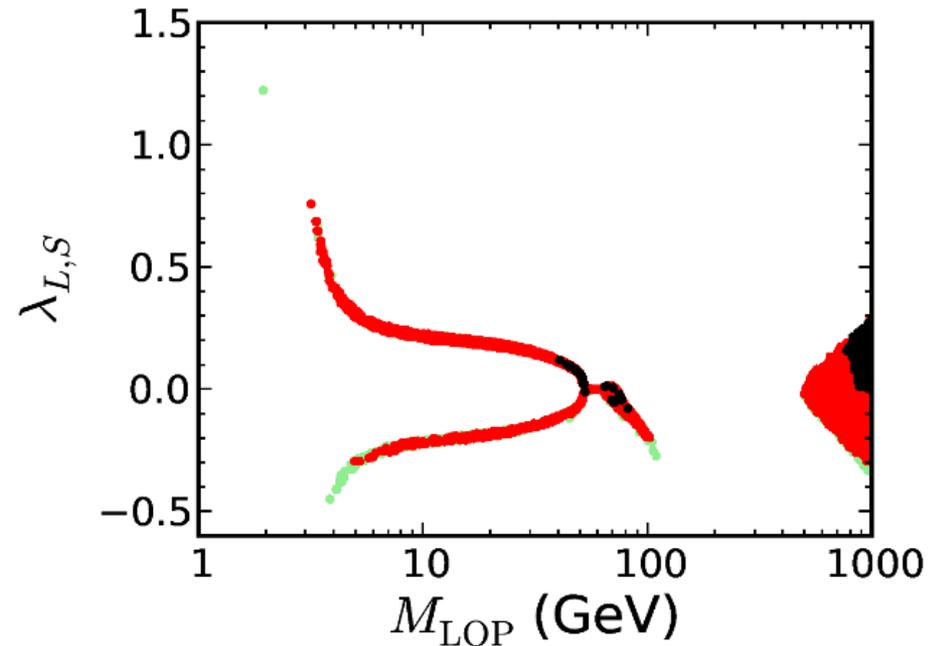
DM Relic Density

- Like in other models, the precise knowledge of the relic density effectively reduces dimensionality of parameter space

$$\Omega_{\text{LOP}} h^2 \leq 0.1234$$



$$0.1018 \leq \Omega_{\text{LOP}} h^2 \leq 0.1234$$

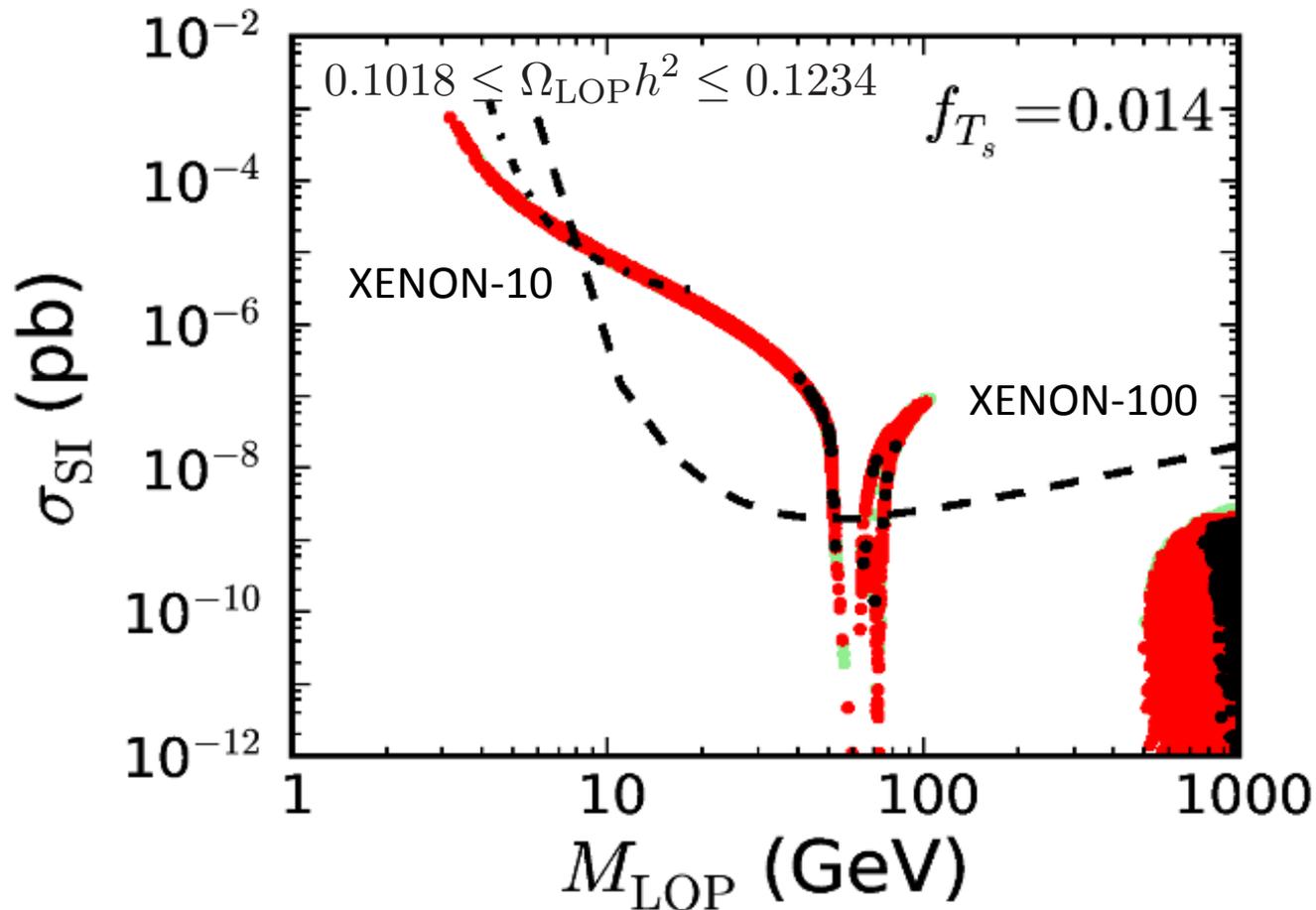


- Theoretical precision probably not comparable with current experimental knowledge of Ω_{DM} (true for many models). Framework for inclusion of effects beyond LO in progress.

Direct detection

- Assuming that DM has not been observed in any direct detection experiment, we can use e.h. the XENON upper limit on σ_{SI}

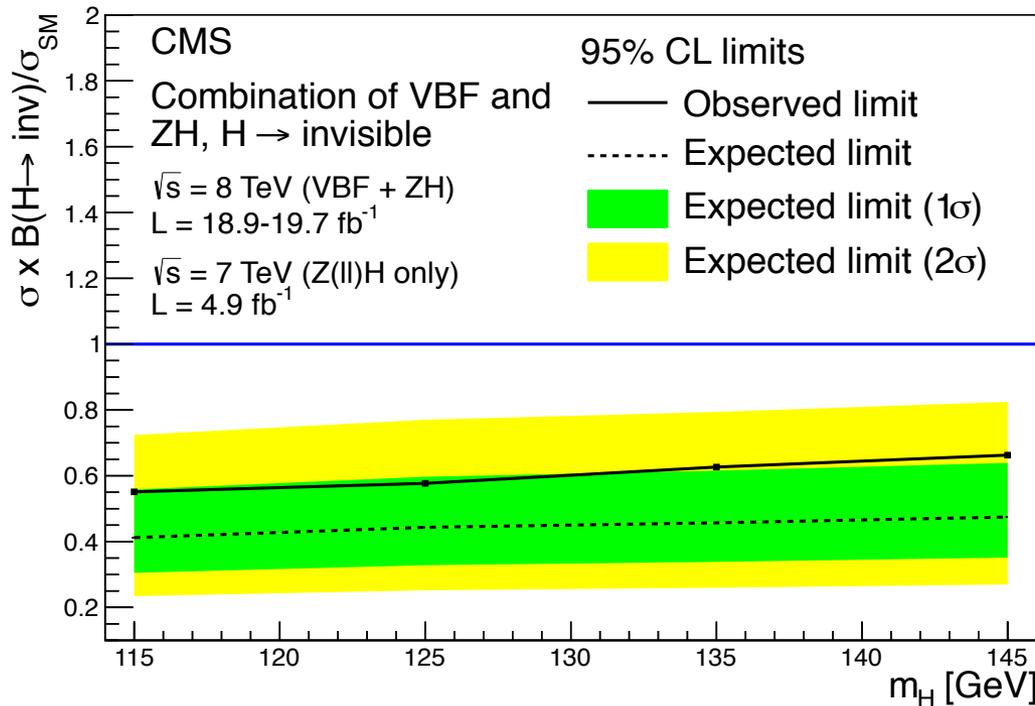
XENON Collaboration, [1104.2549], [1104.3088]



Invisible Higgs decays

- Both ATLAS and CMS have performed searches for “invisible” decays of the 125 GeV Higgs (invisible = missing E_T)

$$pp \rightarrow ZH, Z \rightarrow \ell^+ \ell^-$$



Assuming SM production:
 $BR(h^0 \rightarrow \text{inv.}) \lesssim 0.6$

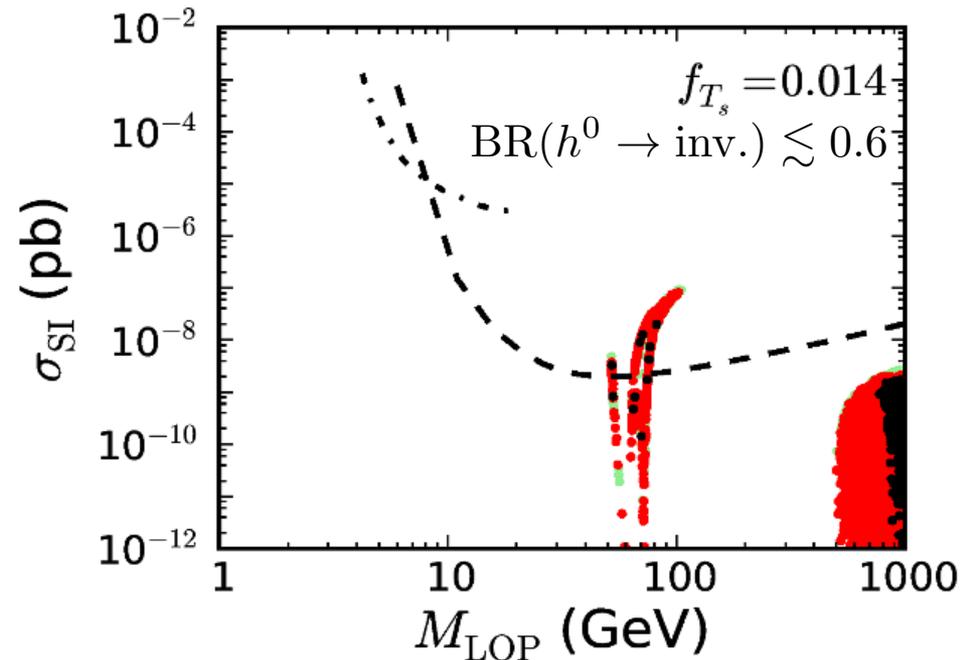
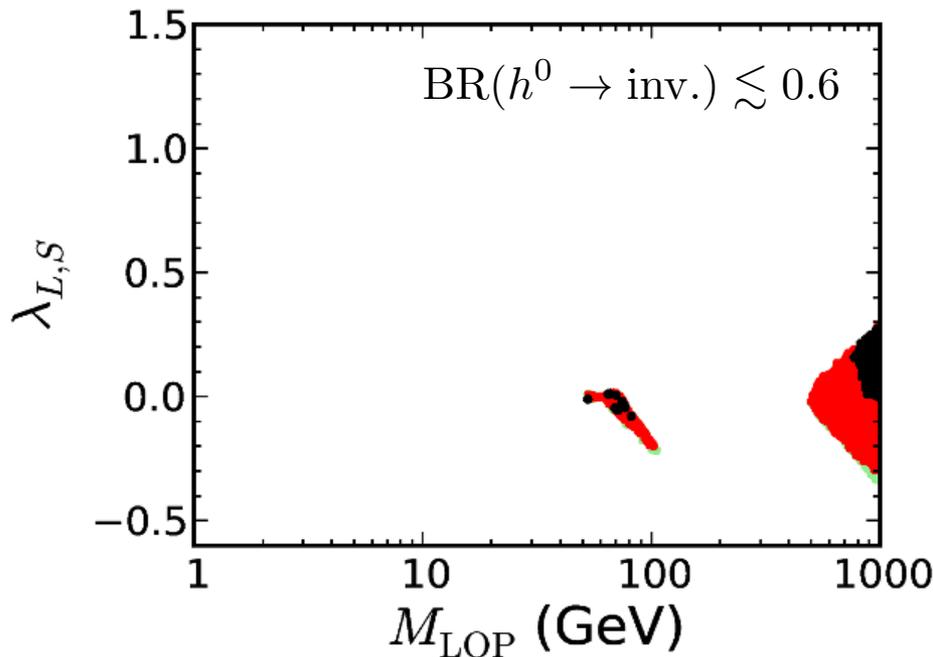
IDM constraints from invisible Higgs decays

- In the IDM, this constraint would apply to the case

$$h \rightarrow H^0 H^0 \quad (h \rightarrow A^0 A^0)$$

- Remember:

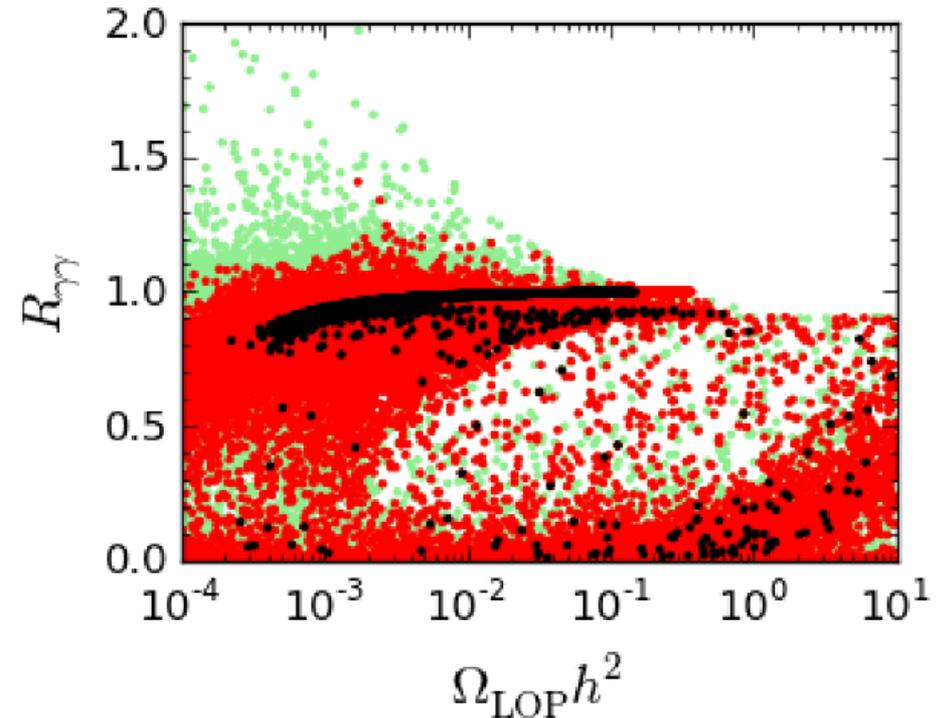
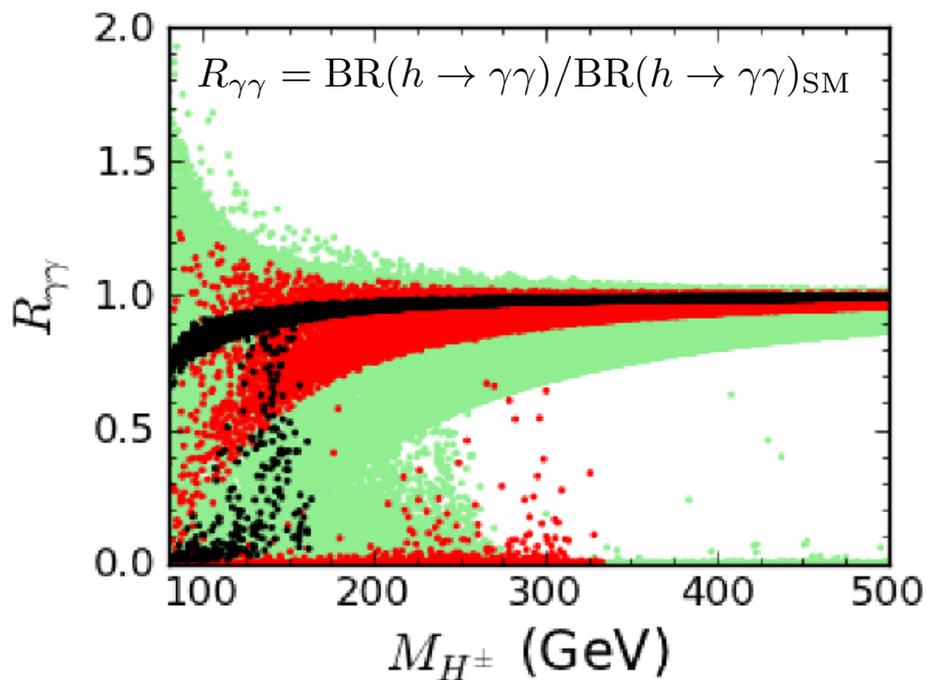
$$g_{h_{\text{SM}} H^0 H^0} \propto \lambda_L \quad g_{h_{\text{SM}} A^0 A^0} \propto \lambda_S$$



- IDM can live either close to Higgs resonance ($M_{\text{LOP}} \simeq 50 - 80$ GeV) or at high mass, $M_{\text{LOP}} \gtrsim 500$ GeV

Implications for 125 GeV Higgs at LHC

- Besides the invisible decays, H^\pm in the IDM can modify the loop-induced decays of a SM-like h^0



- When IDM makes up all DM, there is no enhancement of the two photon rate (even before constraints).
In agreement with current experimental results ☺

LHC Signatures of IDM Dark Matter

- Two mass regions for IDM Dark Matter:

$$M_{\text{DM}} = 50 - 80 \text{ GeV}, M_{\text{DM}} > 500 \text{ GeV}$$

- Direct production of DM pair possible only through Higgs channel

$$pp \rightarrow h^{(*)} \rightarrow H^0 H^0$$

also production through gauge bosons of

$$pp \rightarrow Z^{(*)} \rightarrow H^0 A^0$$

$$pp \rightarrow W^{\pm(*)} \rightarrow H^0 H^{\pm}$$

- Only possible decays are within the inert doublet, i.e.

$$A^0 \rightarrow H^0 Z^{(*)} \quad H^{\pm} \rightarrow H^0 W^{\pm(*)} \quad H^{\pm} \rightarrow A^0 W^{\pm(*)}$$

- Weak-scale xsections with multi-lepton signatures + E_T -miss

2HDM at the LHC (without Dark Matter)

Higgs Couplings

- Couplings to vector bosons determined by mixing angle

$$\frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = \sin(\beta - \alpha) \quad \frac{g_{HVV}}{g_{HVV}^{\text{SM}}} = \cos(\beta - \alpha) \quad g_{AVV} = 0$$

Alignment: $\sin(\beta - \alpha) \rightarrow 1$ possible with or without decoupling

- 2HDM Yukawa couplings in arbitrary basis

$$\begin{aligned} -\mathcal{L}_Y = & \frac{1}{\sqrt{2}} \bar{D} \left[\kappa^D s_{\beta-\alpha} + \rho^D c_{\beta-\alpha} \right] Dh + \frac{1}{\sqrt{2}} \bar{D} \left[\kappa^D c_{\beta-\alpha} - \rho^D s_{\beta-\alpha} \right] DH + \frac{i}{\sqrt{2}} \bar{D} \gamma_5 \rho^D DA \\ & + \frac{1}{\sqrt{2}} \bar{U} \left[\kappa^U s_{\beta-\alpha} + \rho^U c_{\beta-\alpha} \right] Uh + \frac{1}{\sqrt{2}} \bar{U} \left[\kappa^U c_{\beta-\alpha} - \rho^U s_{\beta-\alpha} \right] UH - \frac{i}{\sqrt{2}} \bar{U} \gamma_5 \rho^U UA \\ & + \frac{1}{\sqrt{2}} \bar{L} \left[\kappa^L s_{\beta-\alpha} + \rho^L c_{\beta-\alpha} \right] Lh + \frac{1}{\sqrt{2}} \bar{L} \left[\kappa^L c_{\beta-\alpha} - \rho^L s_{\beta-\alpha} \right] LH + \frac{i}{\sqrt{2}} \bar{L} \gamma_5 \rho^L LA \\ & + \left[\bar{U} (V_{\text{CKM}} \rho^D P_R - \rho^U V_{\text{CKM}} P_L) DH^+ + \bar{\nu} \rho^L P_R LH^+ + \text{h.c.} \right]. \end{aligned}$$

H.E.Haber, D.O'Neil [hep-ph/0602242]

- If ρ^F and κ^F are not simultaneously diagonal the Higgs sector mediates tree-level FCNC (-> strongly restricted from data)

Absence of tree-level FCNC → 2HDM Types

- To get rid of these FCNC naturally, implement a (softly broken) Z_2 symmetry → 2HDM *Types* depending on fermion Z_2 charges

$$\rho_F \propto \kappa_F = \frac{\sqrt{2}}{v} M_F$$

Barger, Hewitt, Philips, PRD41 (1990)

Type	U_R	D_R	L_R	ρ^U	ρ^D	ρ^L
I	+	+	+	$\kappa^U \cot \beta$	$\kappa^D \cot \beta$	$\kappa^L \cot \beta$
II	+	-	-	$\kappa^U \cot \beta$	$-\kappa^D \tan \beta$	$-\kappa^L \tan \beta$
III	+	-	+	$\kappa^U \cot \beta$	$-\kappa^D \tan \beta$	$\kappa^L \cot \beta$
IV	+	+	-	$\kappa^U \cot \beta$	$\kappa^D \cot \beta$	$-\kappa^L \tan \beta$

Type III = Type Y = “Flipped”

Type IV = Type X = “Lepton-spec.”

- Promotes $\tan \beta$ to a physical parameter (basis with $\lambda_6 = \lambda_7 = 0$)
- MSSM: Type-II couplings at tree level, broken by Δ_b corrections

Model predictions for the LHC

- Two bundles of codes provide complete 2HDM predictions of cross sections + branching ratios, including available higher-order (mostly QCD) corrections

SusHi + 2HDMC

Harlander, Mantler, Liebler, [1212.3249]
Eriksson, Rathsman, OS, [0902.0851]

HIGLU+HDECAY

Spira et al, [hep-ph/9510347], [hep-ph/9704448]

LHC Higgs Cross Section Working Group

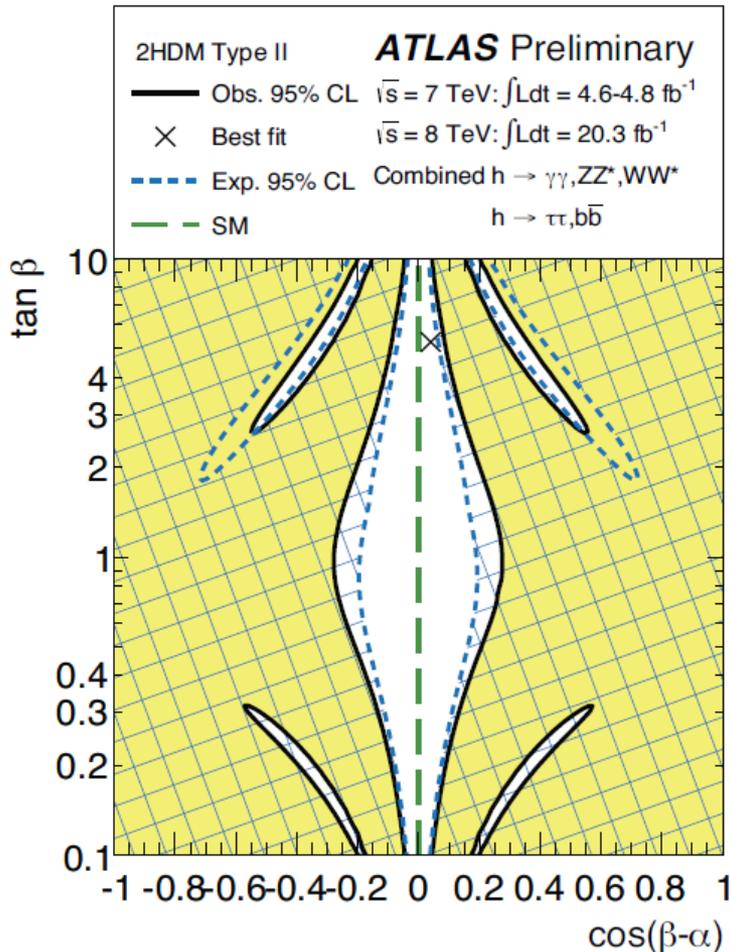
Interim recommendations for the evaluation of Higgs production cross sections and branching ratios at the LHC in the Two-Higgs-Doublet Model

R. Harlander¹, M. Mühlleitner², J. Rathsman³, M. Spira⁴, O. Stål⁵
[LHCHXSWG-2013-001], [1312.5571]

First LHC analyses of 2HDM

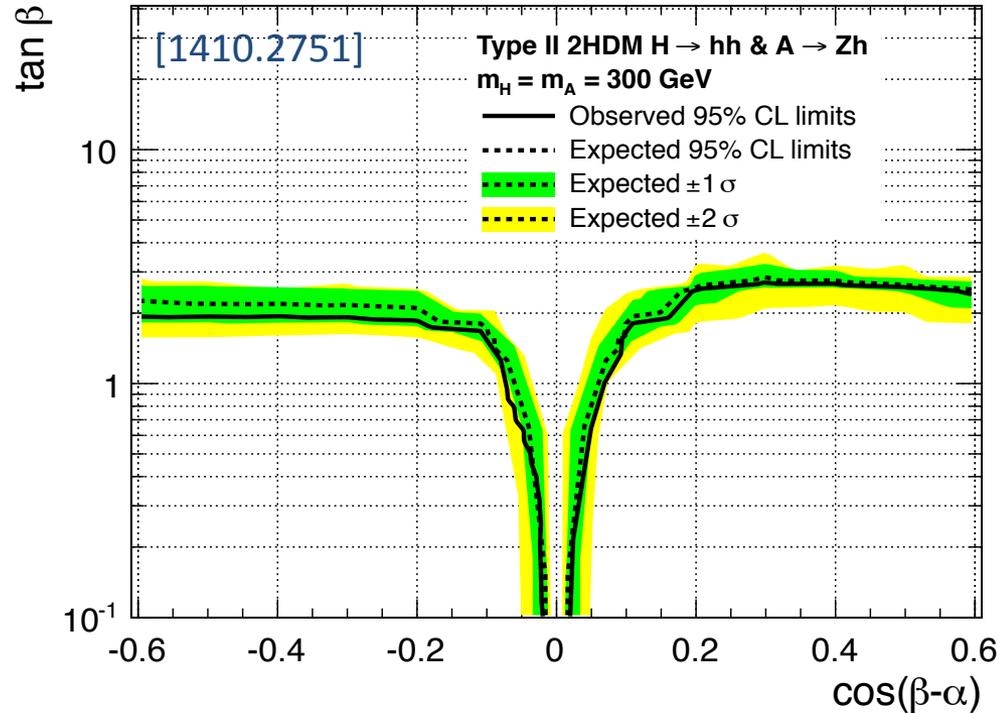
- Reinterpretation of 125 GeV coupling measurements

ATLAS-CONF-2014-010



CMS

19.5 fb⁻¹ (8 TeV)



- Genuine 2HDM searches
- BR($H \rightarrow hh$) sensitive to full model
 $M_H = M_A = 300 \text{ GeV}$ “best case”

Preparing for run-II: Benchmarks

In collaboration with H.E. Haber

- Like most theorists (I think) I favor keeping experimental searches as model-independent as possible.
- Still, in many situations it also makes sense to consider specific models.
- The role of benchmarks is to:
 - Motivate experimental searches to exploit all channels
 - Improve search strategies using model-specific information
 - Combine different channels to improve sensitivity
 - Define unambiguous and complete sets of parameters
 - Be able to consider relevant model constraints
 - Provide language to compare exp \leftrightarrow exp and exp \leftrightarrow th

Model parametrization

- Even with restrictions to CP conservation and soft Z_2 (Types) there remains seven free parameters:

$$\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, m_{12}^2, \tan \beta$$

or

$$m_h, m_H, m_A, m_{H^\pm}, \sin(\beta - \alpha), m_{12}^2, \tan \beta$$

- Hybrid basis: $m_h, m_H, \cos(\beta - \alpha), \tan \beta, Z_4, Z_5, Z_7$

$$m_H > m_h \quad 0 < \beta < \pi/2 \quad 0 \leq s_{\beta-\alpha} \leq 1$$

+ “Type” condition on the Yukawa couplings

- Higgs basis condition for soft Z_2 -breaking:

$$(Z_1 - Z_2) [Z_1 Z_7 + Z_2 Z_6 - Z_{345} Z_{67}] + 2Z_{67}^2 (Z_6 - Z_7) = 0$$

- Symmetry manifest: ($\lambda_6 = \lambda_7 = 0$) in basis for specified $\tan \beta$

Mass relations

- Remaining masses fixed by the quartic Higgs basis couplings:

$$m_A^2 = m_H^2 s_{\beta-\alpha}^2 + m_h^2 c_{\beta-\alpha}^2 - Z_5 v^2$$

$$m_{H^\pm}^2 = m_A^2 - \frac{1}{2}(Z_4 - Z_5)v^2$$

(Z_7 only enters in triple/quartic scalar interactions)

- Theoretical constraints:

$$|Z_i| \lesssim \mathcal{O}(1)$$

- Further constraints on the choice of benchmarks come from observed properties of 125 GeV Higgs and wishful(?) thinking about observable signatures

Benchmark scenarios

H.E. Haber, OS, [to appear]

(see also Baglio, Eberhardt, Nierste, Wiebusch, [1403.1264];)

■ Scenario A

“Standard” scenario with lightest Higgs at 125 GeV

$$M_h = 125 \text{ GeV} < M_H < M_A = M_{H^\pm}.$$

Useful for H searches in “standard” modes.

■ Scenario B

“Inverted” scenario with heavy CP-even Higgs at 125 GeV

$$M_h < M_H = 125 \text{ GeV} < M_A = M_{H^\pm}. \text{ Useful for } h \text{ searches.}$$

■ Scenario C

Overlapping CP-even and CP-odd Higgses @ 125 GeV

$$M_h = M_A = 125 \text{ GeV} < M_H = M_{H^\pm}. \text{ Test sensitivity to mixed CP.}$$

Benchmark scenarios

■ Scenario D

Heavy CP-even Higgs with non-SM decays, e.g. $H \rightarrow A Z$, $H \rightarrow H^+ W^-$
 $M_h = 125 \text{ GeV} < M_A / M_{H^\pm} < M_H$. Useful for H searches in cascades.

■ Scenario E

Scenario for heavy CP-odd / charged Higgs with
 $A \rightarrow H^+ W^-$ or $H^+ \rightarrow A W^+$. Useful for A (H^\pm searches) in cascades.

■ Scenario F

h with SM-like couplings to up-type fermions and vector bosons,
but flipped sign of coupling to down-type fermions.

■ Scenario G

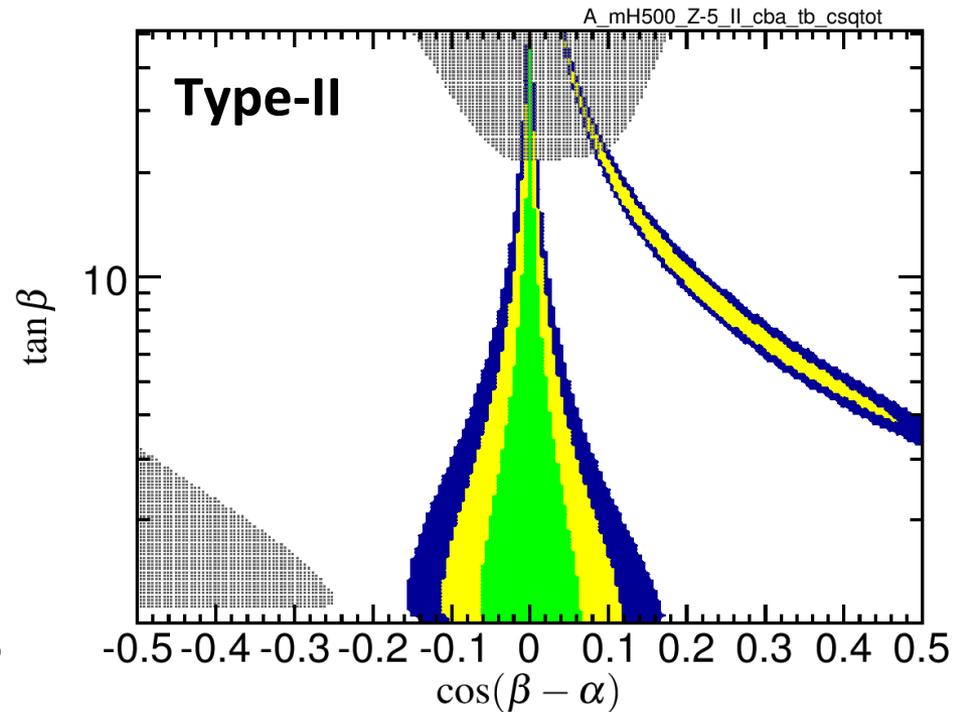
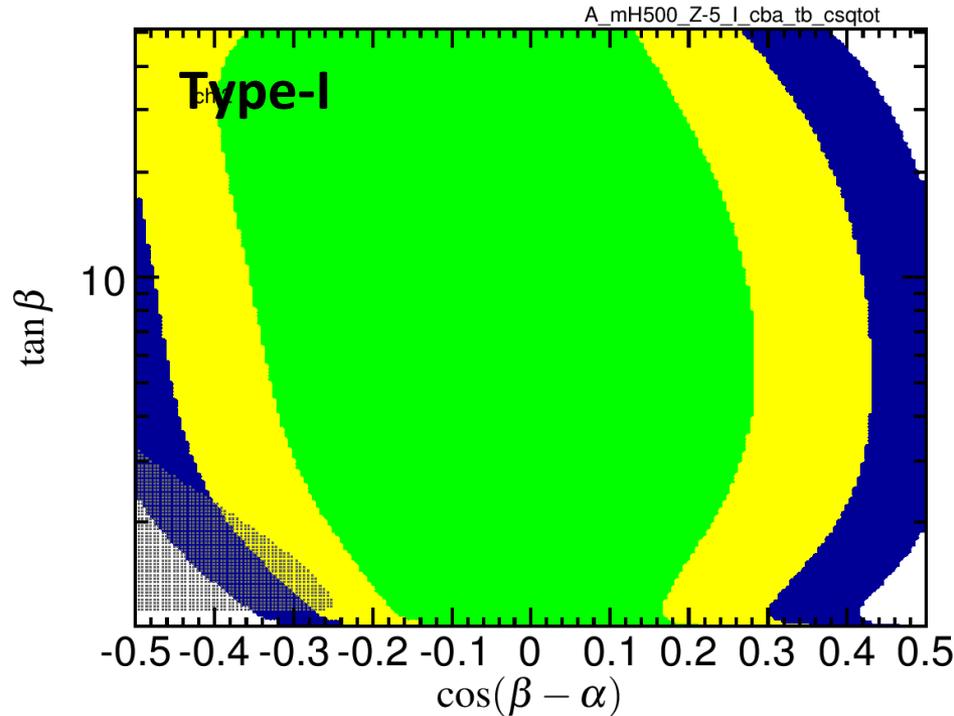
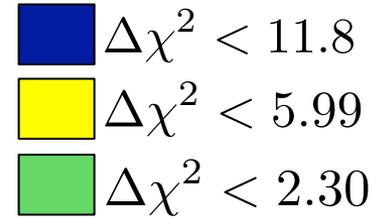
“MSSM”-like (mass-degenerate) scenario for heavy Higgs bosons
 $M_h = 125 \text{ GeV} < M_H = M_A = M_{H^\pm}$, decoupling as $M \gg v$.

Scenario A: Lightest 2HDM Higgs@125 GeV

- χ^2 fit of light Higgs signal rates with **HiggsSignals**

$$M_H = 500 \text{ GeV} < M_A = M_{H^\pm}$$

-> Talk by P. Bechtle

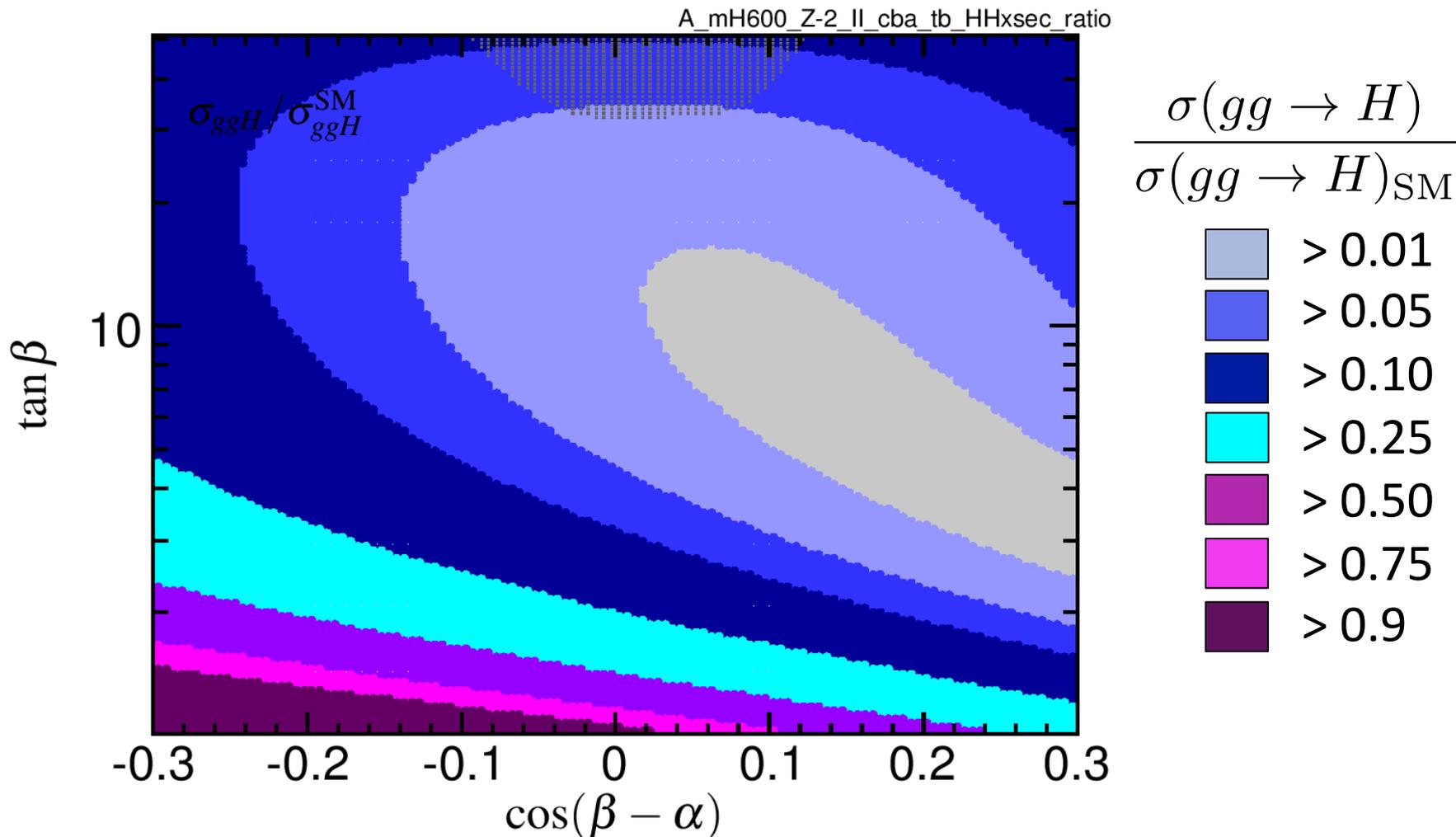


- Type-II couplings much more restricted around alignment, in particular for high $\tan\beta$. Exception: flipped-sign scenario (F)

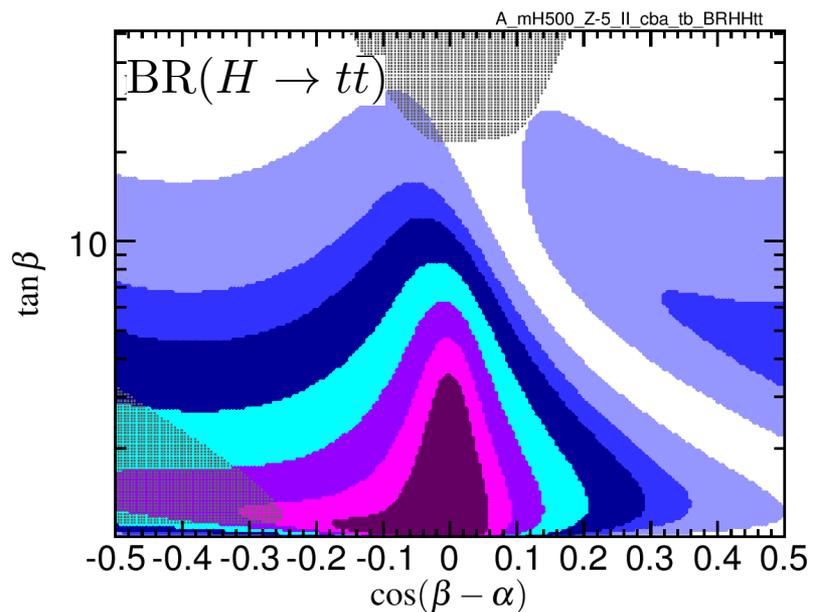
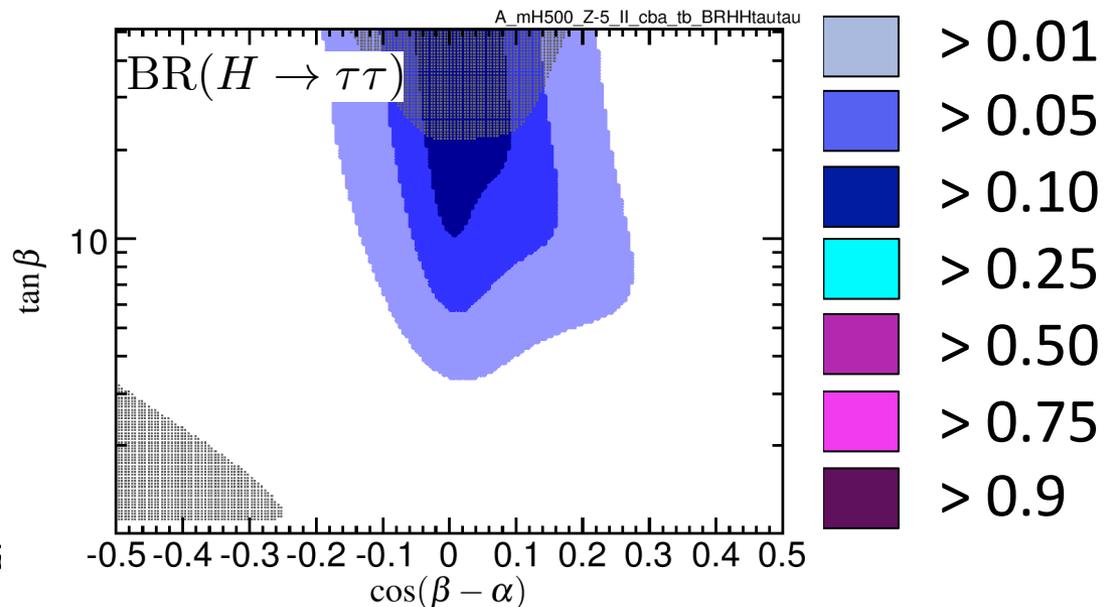
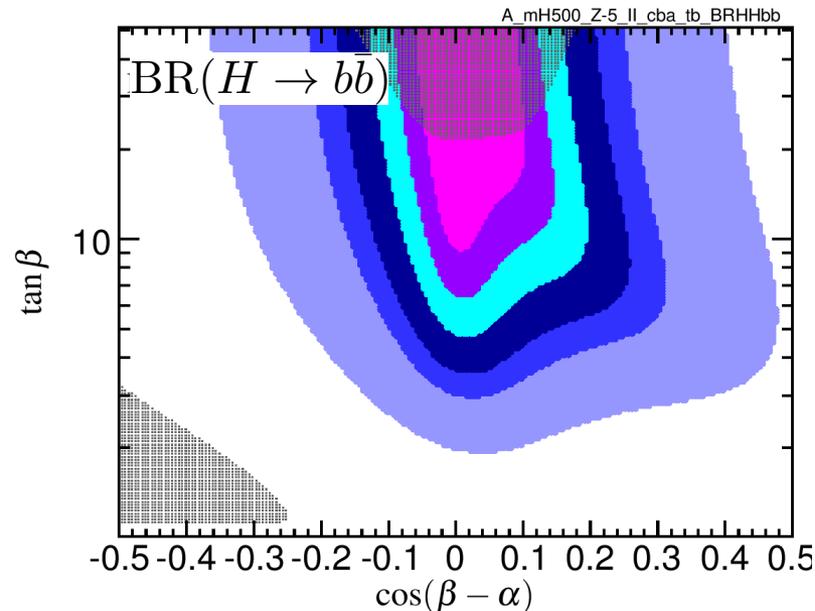
Ferreira, Haber, Gunion, Santos, [1403.4736]

Type-II: Heavy Higgs production

- Since the H must have suppressed couplings to gauge bosons, only $gg \rightarrow H$ and $b\bar{b} \rightarrow H$ (at high $\tan \beta$)



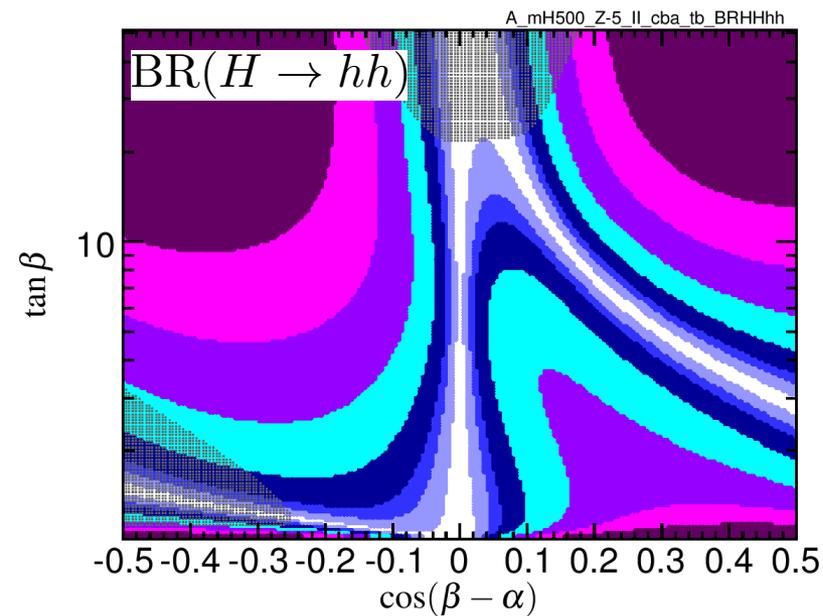
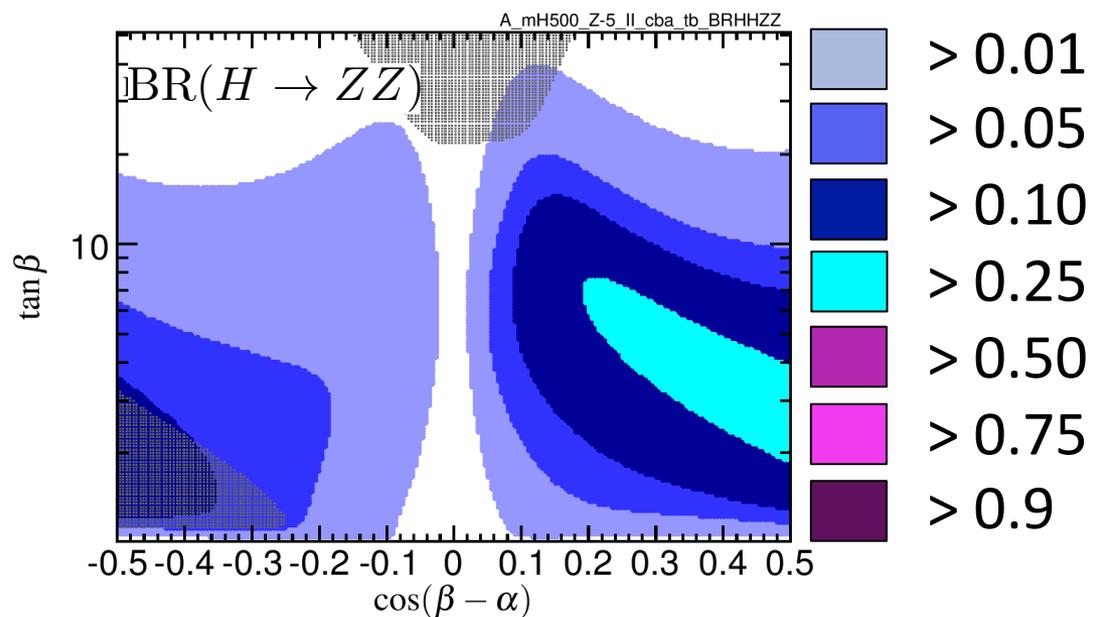
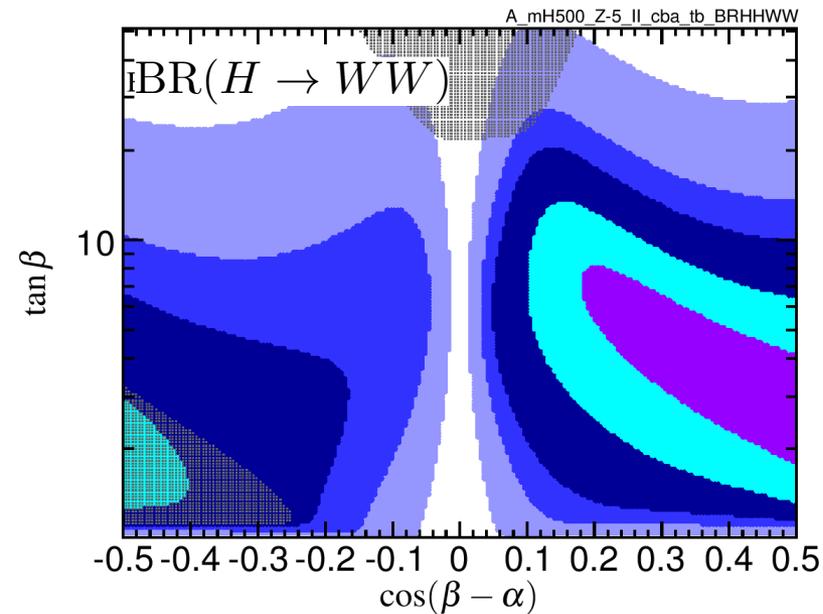
Type-II: H decays to fermions



$$m_H = 500 \text{ GeV}$$

- Fermions dominate close to alignment limit
- Complementarity between up- and down-type modes typical of Type-II

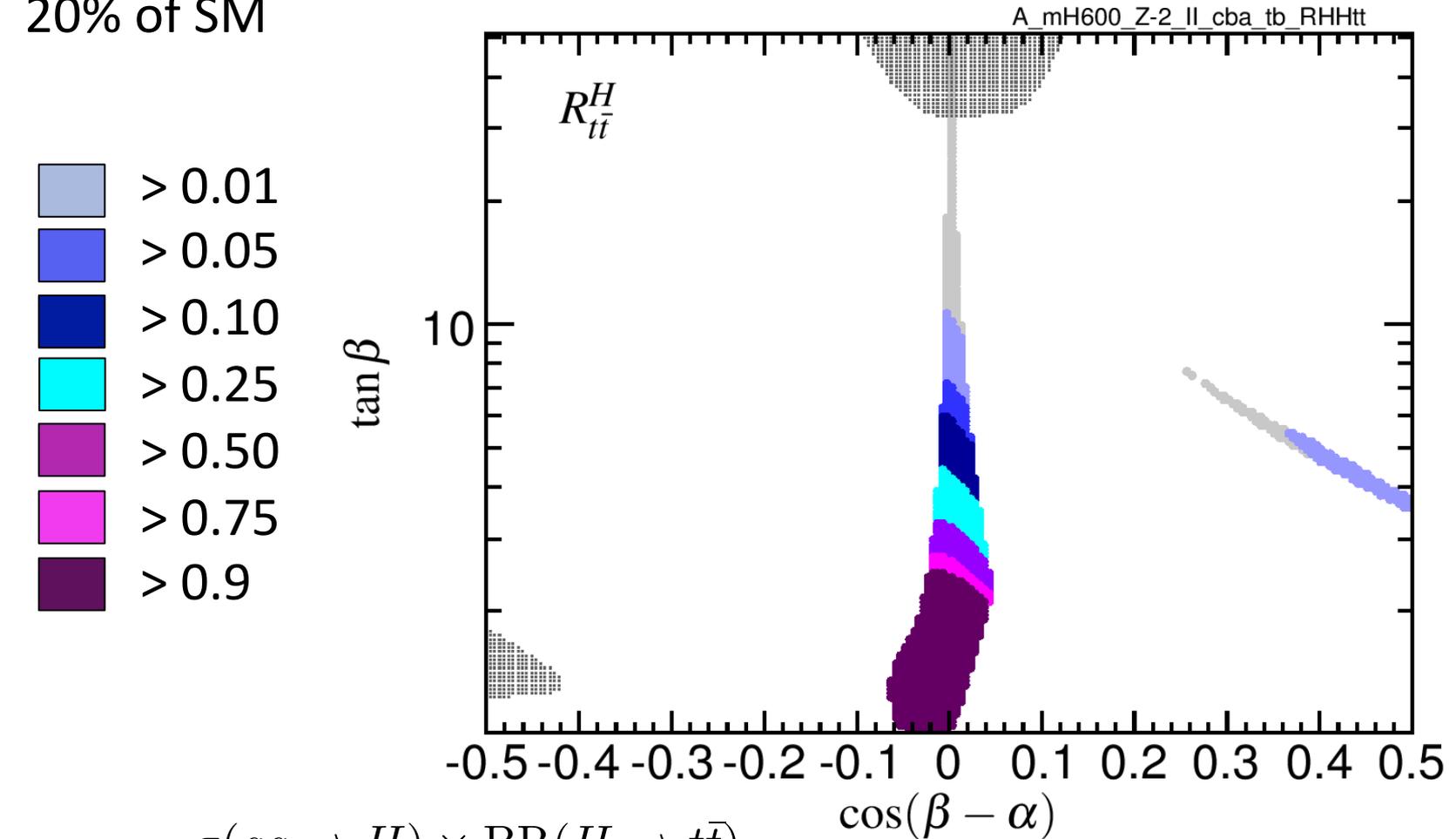
Type-II: H decays to bosons



- Bosonic modes become important away from the alignment limit ->
 - Difficult to access in favored region of parameter space

Type-II: The allowed parameter space

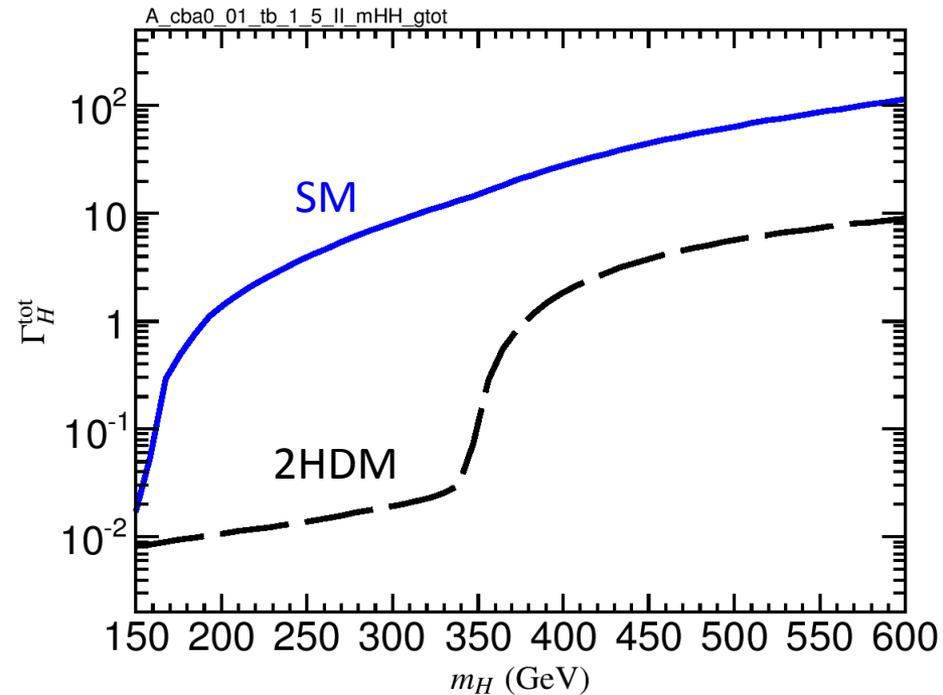
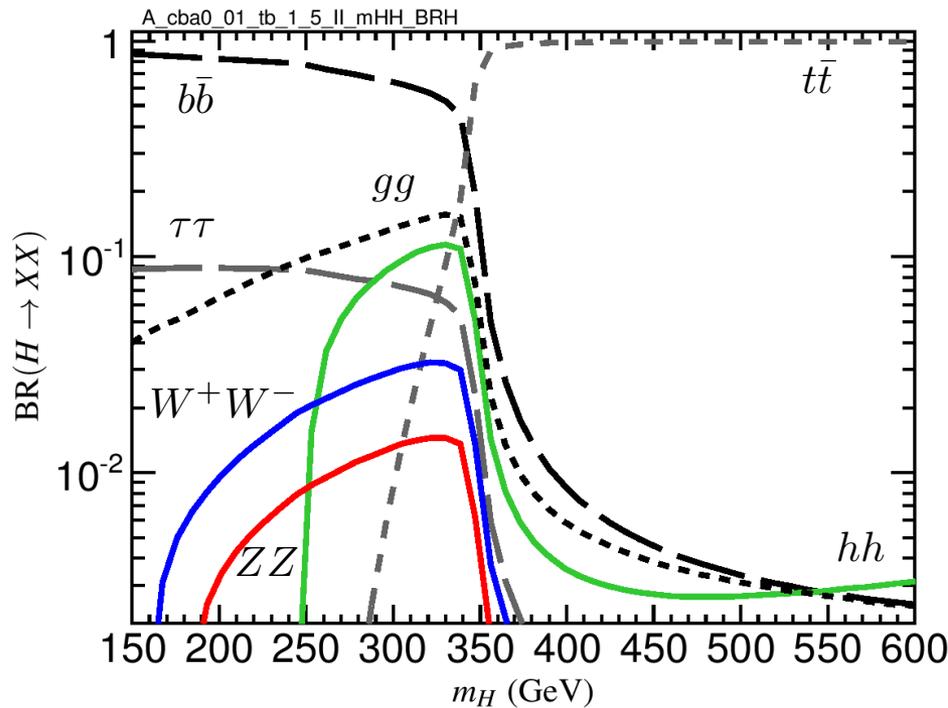
- Applying theory constraints and rates of 125 GeV Higgs within 20% of SM



$$R_{tt}^H = \frac{\sigma(gg \rightarrow H) \times \text{BR}(H \rightarrow t\bar{t})}{[\sigma(gg \rightarrow H) \times \text{BR}(H \rightarrow t\bar{t})]_{\text{SM}}}$$

Scenario A: Type-II Benchmark

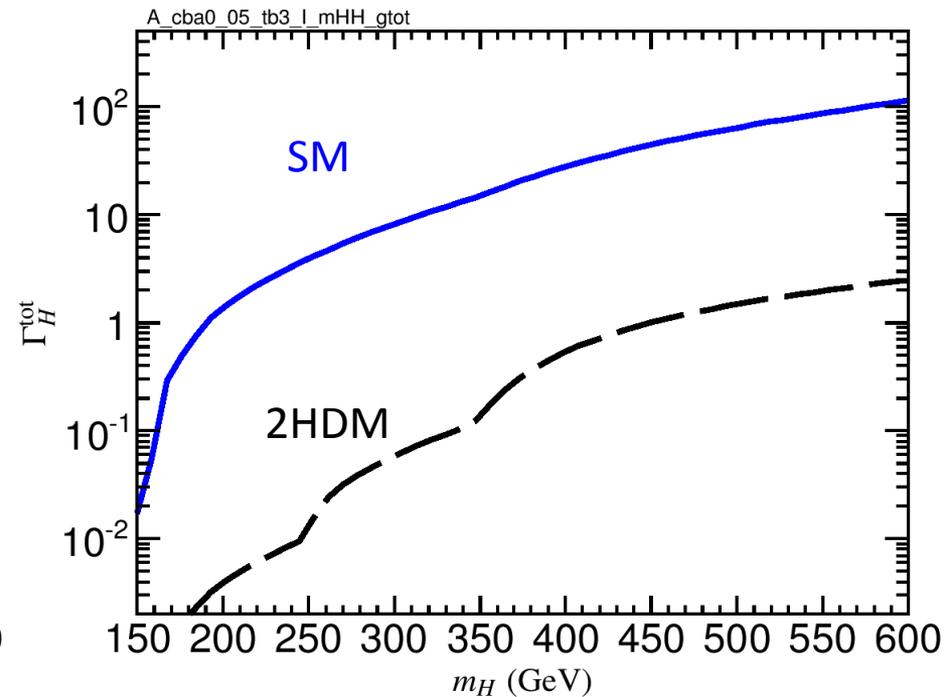
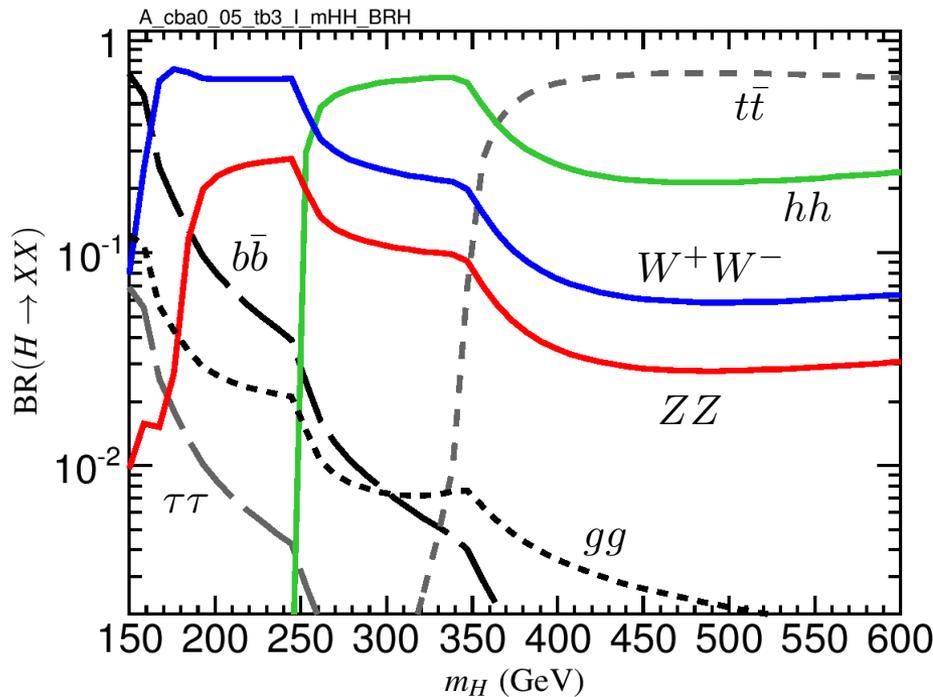
- 1D Benchmark can be defined by choosing fixed values for $c_{\beta-\alpha}$ and $\tan \beta$ inside allowed region. Ex: $\cos(\beta-\alpha) = 0.01$, $\tan \beta = 1.5$



- Maximizes production and decay to $t\bar{t}$
Total H width remains relatively small, $\Gamma_H/\Gamma_{SM} < 0.1$

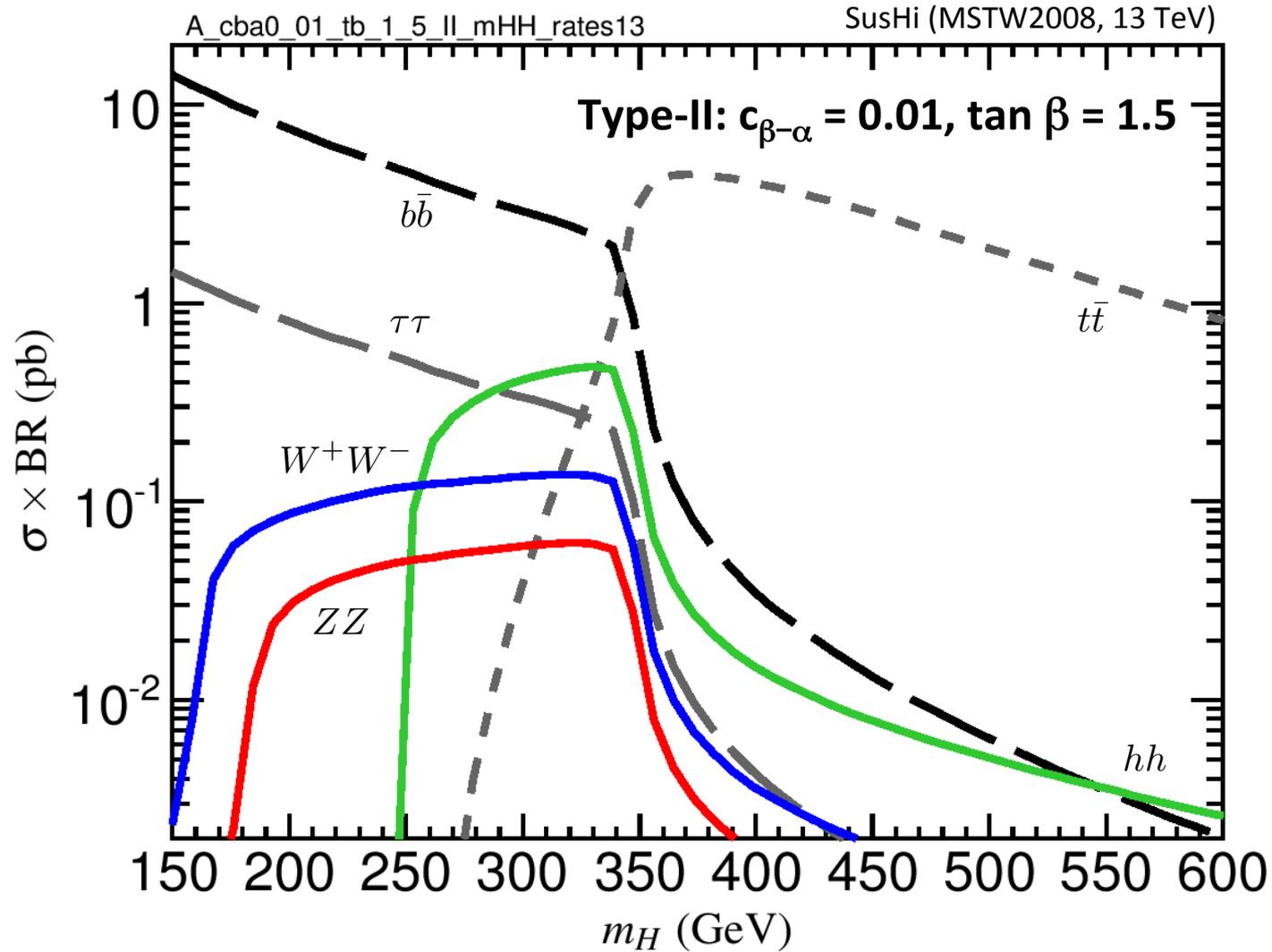
Scenario A: Type-I Benchmark

- For Type-I, larger deviations from SM in the coupling to vector bosons is allowed. Ex: $\cos(\beta-\alpha) = 0.05$, $\tan \beta = 3$

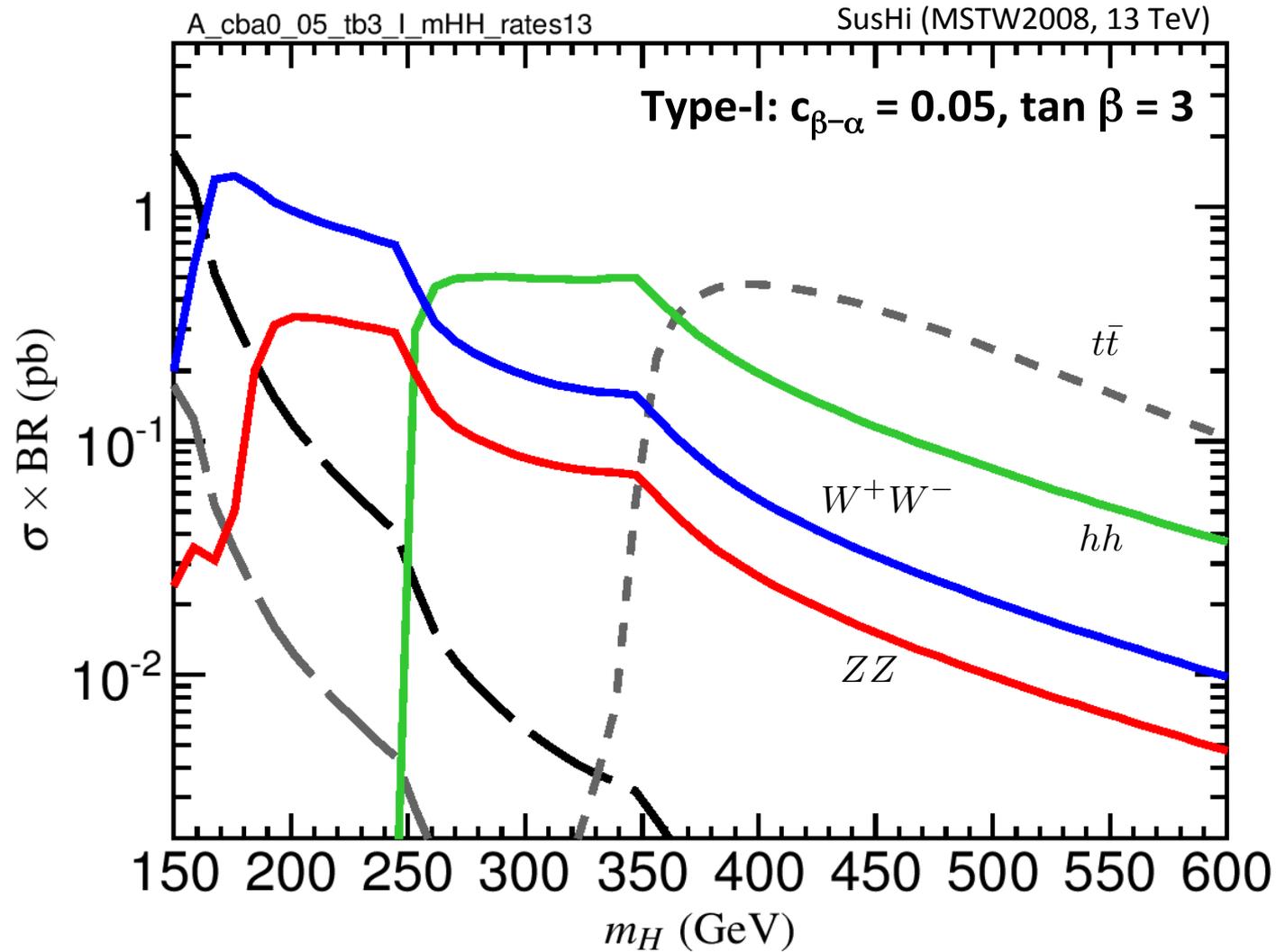


- Sizeable branching ratios to bosonic final states, total width small

Total rates for LHC-13



Total rates for LHC-13

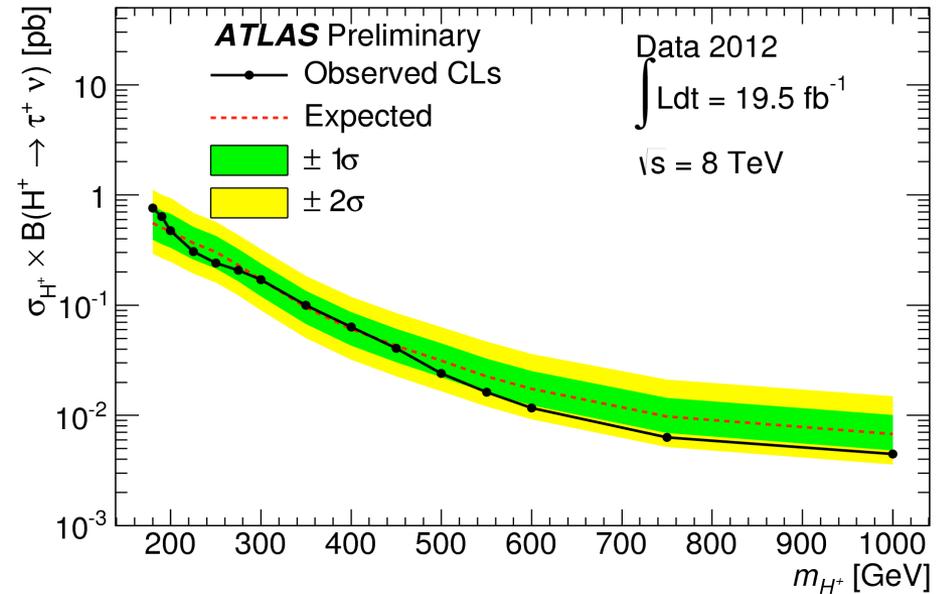
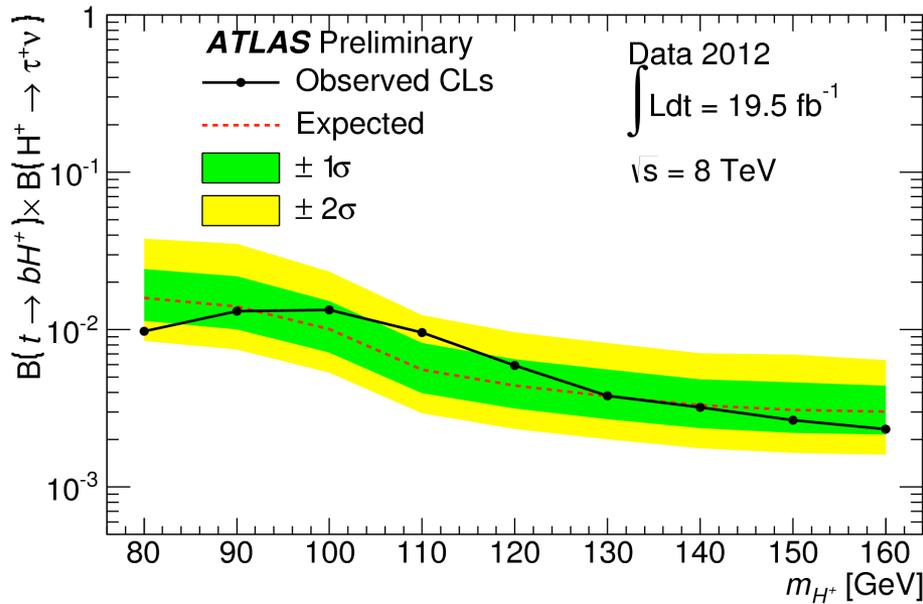


Charged Higgs

- Interesting component of all models with multiple Higgs doublets, mass related to neutral scalars through SU(2) (custodial) symmetry
- Fewer signatures to consider (if neutral Higgs channels closed)

$$M_{H^\pm} < m_t$$

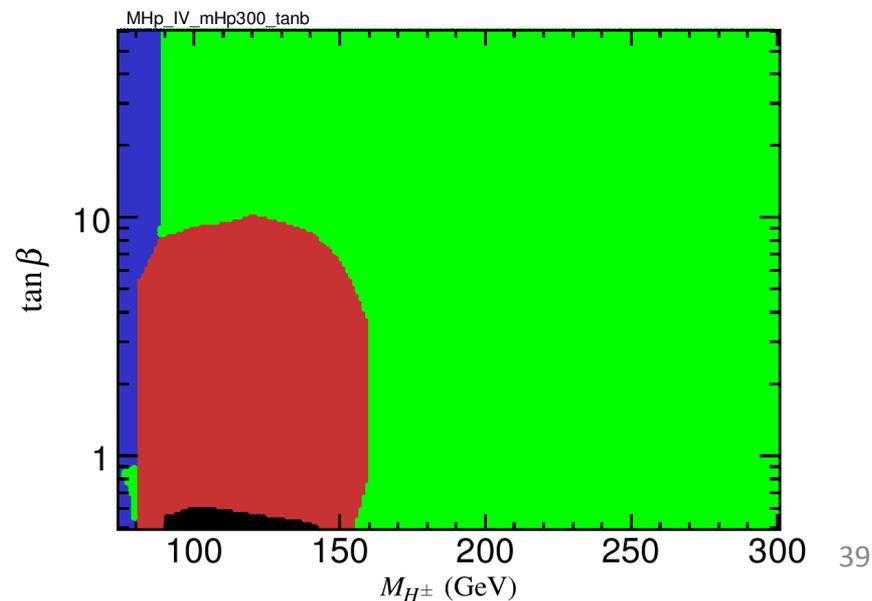
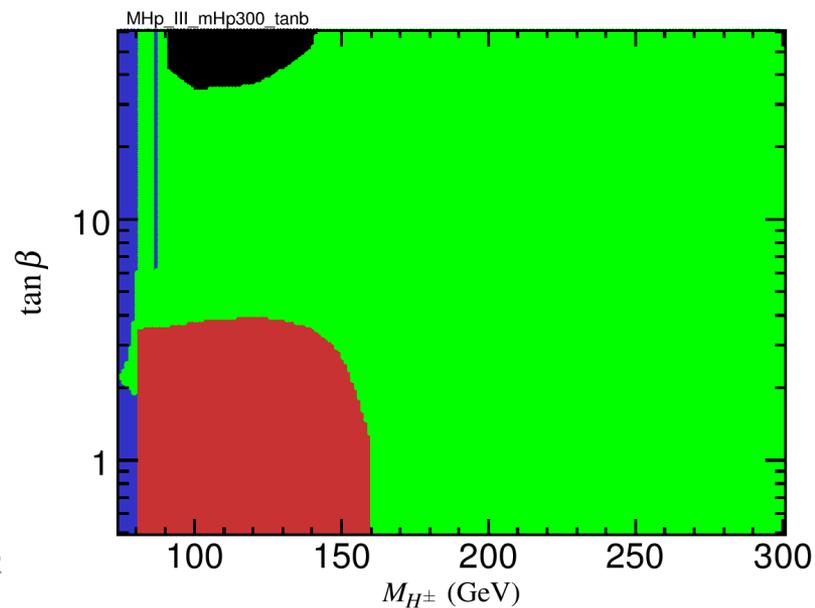
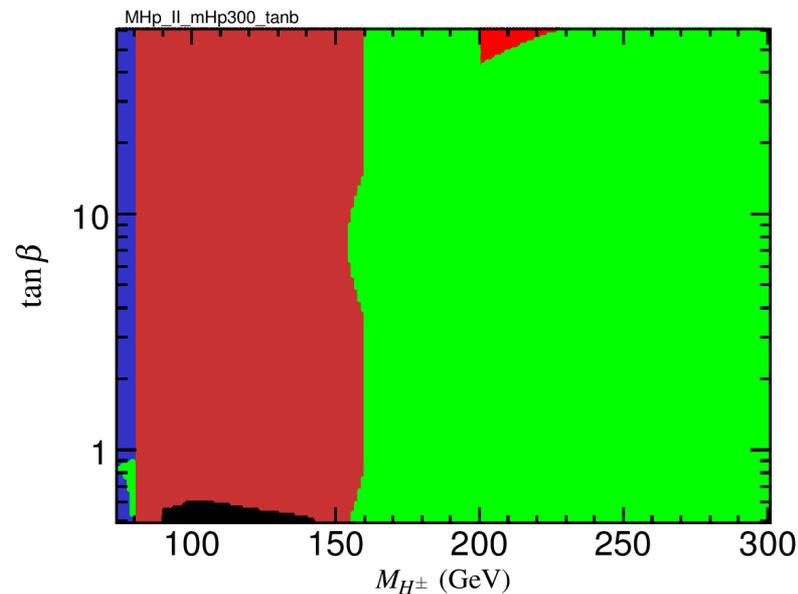
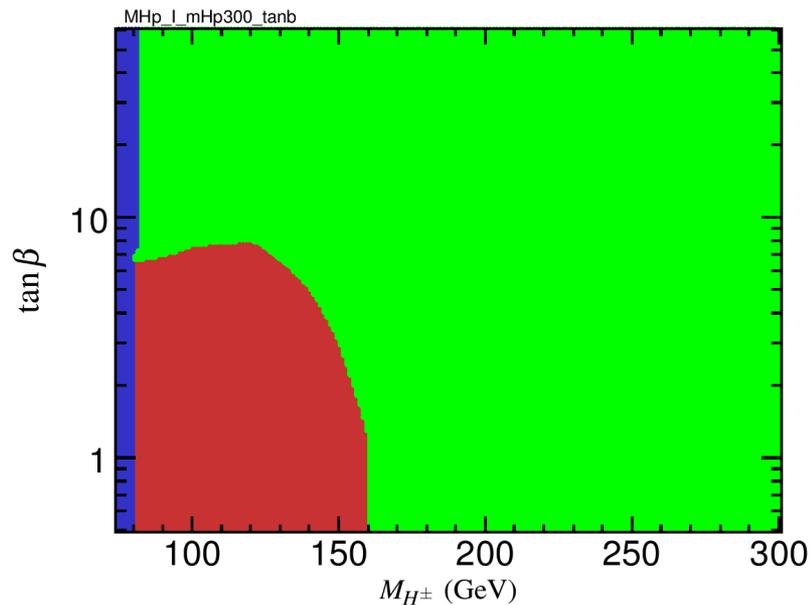
$$M_{H^\pm} > m_t$$



ATLAS-CONF-2014-050

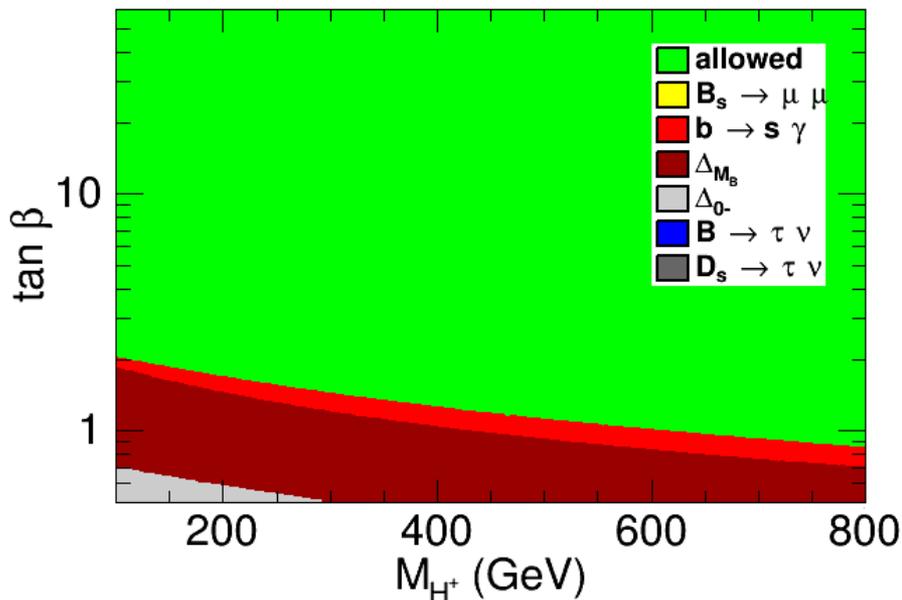
2HDM interpretation of Charged Higgs searches

F. Mahmoudi, OS, [to appear]

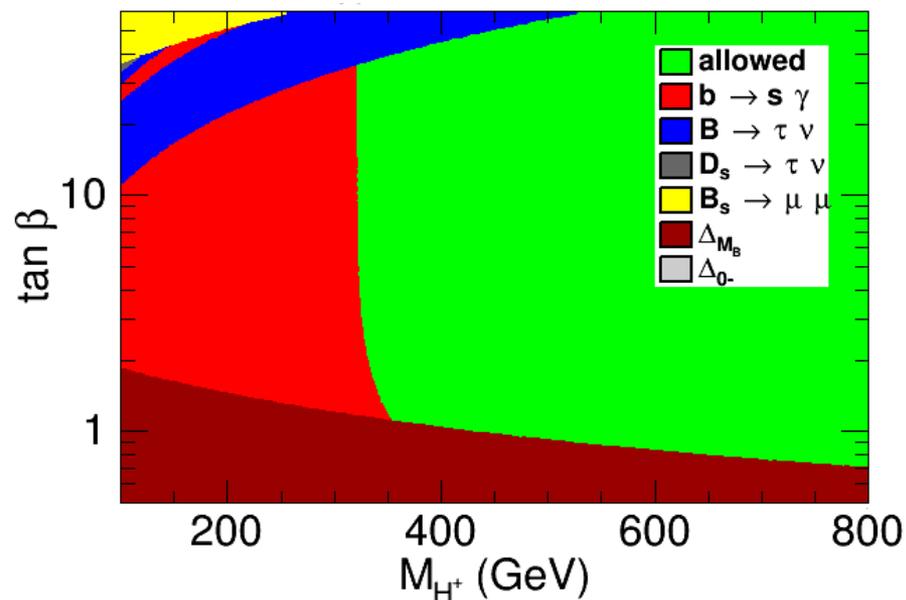


Low-energy constraints F. Mahmoudi, OS, [to appear]

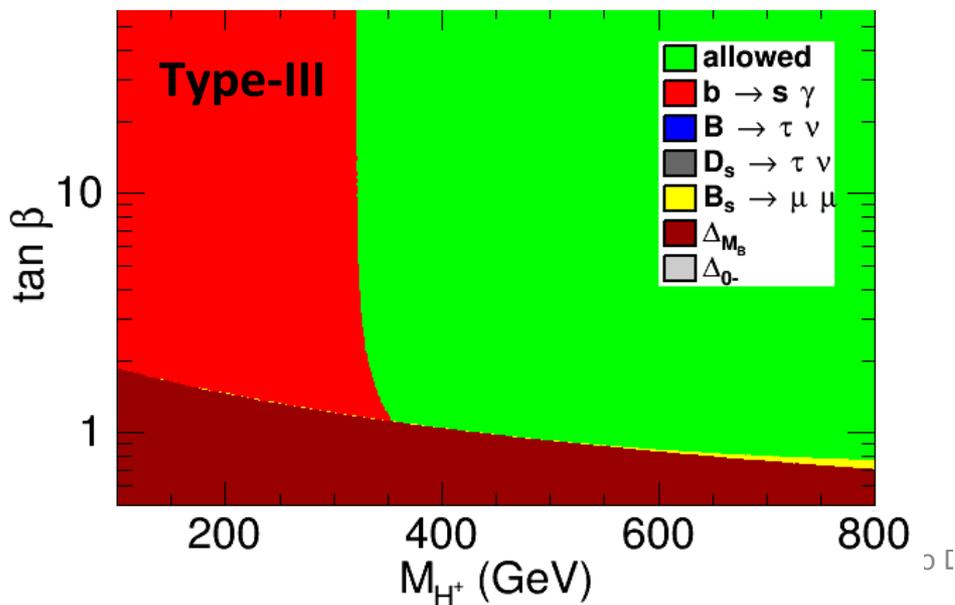
Type-I



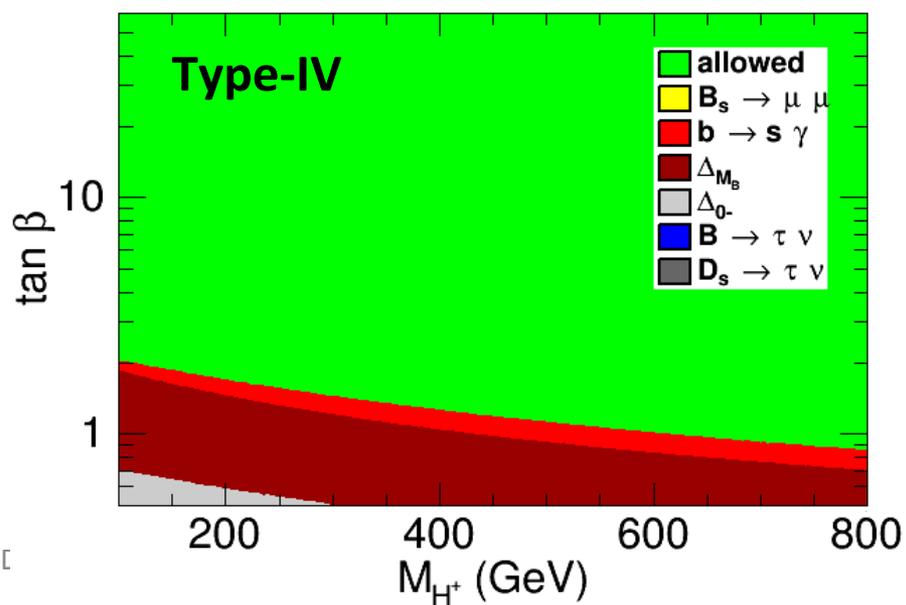
Type-II



Type-III



Type-IV



Conclusions

- The 2HDM remains a useful theoretical playground to study both phenomenology of scalar dark matter and searches for additional Higgs bosons at the LHC
- With all constraints taken into account, IDM dark matter restricted to Higgs pole: $M_{\text{DM}} \simeq M_{h^0}/2$ or $M_{\text{DM}} \gtrsim 500 \text{ GeV}$
- First LHC analyses of 2HDM already there, preparing for run-II:
 - “Official” cross sections and branching ratios available for experimental collaborations using public tools
 - Benchmarks covering different interesting signatures

Geilo-2016

From the Second discovered Higgs boson to Dark Matter?

Backup

2HDMC (2-Higgs Doublet Model Calculator)

- Object-oriented C++ code implementing calculations for the general (CP-conserving) 2HDM in different parametrizations

D. Eriksson (Ericsson), OS (Stockholm), J. Rathsmann (Lund)

[0902.0851]

<http://2hdmc.hepforge.org>

- First released in 2009, current public version is 1.6.5
- Includes links to SusHi (cross sections), HiggsBounds (Higgs search limits), SuperIso (flavor physics), MadGraph (event generation)
- Can be used either as a library, or for simple applications through one of the provided example programs for different input bases

Boring numerical comparisons...

[1312.5571]

	2HDMC		HDECAY		Γ_{2H}/Γ_{HD}
	BR	Γ (GeV)	BR	Γ (GeV)	
$h \rightarrow b\bar{b}$	0.6812	3.790×10^{-3}	0.6827	3.820×10^{-3}	0.992
$\tau^+\tau^-$	6.587×10^{-2}	3.664×10^{-4}	6.548×10^{-2}	3.664×10^{-4}	1.000
$\mu^+\mu^-$	2.332×10^{-4}	1.297×10^{-6}	2.318×10^{-4}	1.297×10^{-6}	1.000
$s\bar{s}$	2.484×10^{-4}	1.382×10^{-6}	2.503×10^{-4}	1.400×10^{-6}	0.987
$c\bar{c}$	3.059×10^{-2}	1.701×10^{-4}	2.976×10^{-2}	1.665×10^{-4}	1.022
gg	8.110×10^{-2}	4.511×10^{-4}	8.166×10^{-2}	4.569×10^{-4}	0.987
$\gamma\gamma$	1.130×10^{-3}	6.284×10^{-6}	1.117×10^{-3}	6.250×10^{-6}	1.006
$Z\gamma$	8.728×10^{-4}	4.855×10^{-6}	8.677×10^{-4}	4.855×10^{-6}	1.000
W^+W^-	0.1233	6.859×10^{-4}	0.1226	6.860×10^{-4}	1.000
ZZ	1.540×10^{-2}	8.569×10^{-5}	1.531×10^{-2}	8.566×10^{-5}	1.000
Total width	5.563×10^{-3}		5.595×10^{-3}		0.994
$H \rightarrow b\bar{b}$	8.492×10^{-5}	1.536×10^{-4}	8.526×10^{-5}	1.542×10^{-4}	0.996
$\tau^+\tau^-$	9.667×10^{-6}	1.748×10^{-5}	9.667×10^{-6}	1.748×10^{-5}	1.000
$\mu^+\mu^-$	3.419×10^{-8}	6.182×10^{-8}	3.419×10^{-8}	6.183×10^{-8}	1.000
$s\bar{s}$	3.070×10^{-8}	5.552×10^{-8}	3.115×10^{-7}	5.636×10^{-8}	0.985
$c\bar{c}$	3.787×10^{-6}	6.848×10^{-6}	3.706×10^{-6}	6.706×10^{-6}	1.021
$t\bar{t}$	5.976×10^{-6}	1.081×10^{-5}	5.986×10^{-6}	1.082×10^{-5}	0.998
gg	8.382×10^{-5}	1.516×10^{-4}	8.669×10^{-5}	1.568×10^{-4}	0.967
$\gamma\gamma$	1.642×10^{-5}	2.969×10^{-5}	1.653×10^{-5}	2.989×10^{-5}	0.993
$Z\gamma$	5.300×10^{-5}	9.584×10^{-5}	5.300×10^{-5}	9.584×10^{-5}	1.000
W^+W^-	0.5872	1.062	0.5872	1.062	1.000
ZZ	0.2606	0.4713	0.2606	0.4712	1.000
hh	0.1493	0.2699	0.1493	0.2700	1.000
$W^\pm H^\mp$	2.658×10^{-3}	4.806×10^{-3}	2.663×10^{-3}	4.815×10^{-3}	0.998
Total width	1.808		1.808		1.000

From Hybrid basis to Higgs basis

- Higgs basis condition for soft Z_2 -breaking:

$$(Z_1 - Z_2) [Z_1 Z_7 + Z_2 Z_6 - Z_{345} Z_{67}] + 2Z_{67}^2 (Z_6 - Z_7) = 0$$

- Preferred basis in which soft Z_2 -breaking is manifest:

$$\tan 2\beta = \pm \frac{|Z_6| + \varepsilon_6 \varepsilon_7 |Z_7|}{Z_2 - Z_1}$$

- Remaining quartic couplings (in the Higgs basis) determine the CP-odd and charged Higgs masses:

$$m_A^2 = m_H^2 s_{\beta-\alpha}^2 + m_h^2 c_{\beta-\alpha}^2 - Z_5 v^2$$

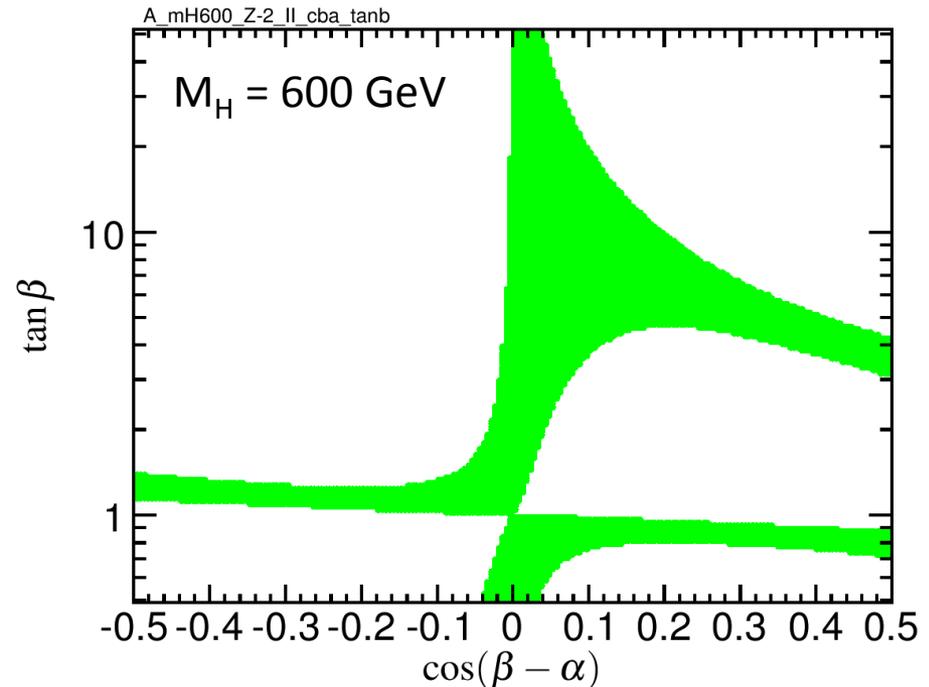
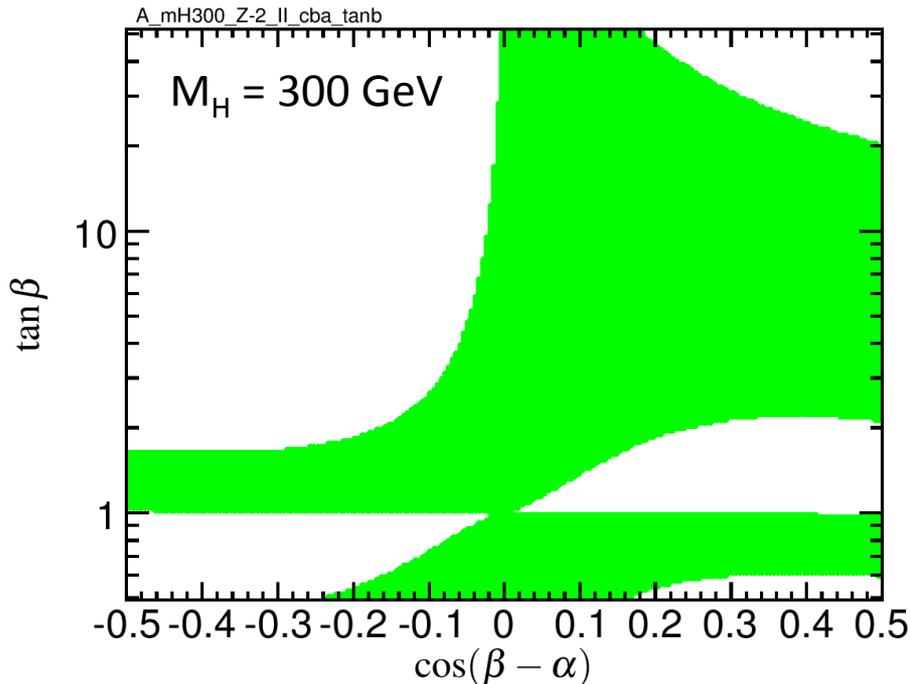
$$m_{H^\pm}^2 = m_A^2 - \frac{1}{2} (Z_4 - Z_5) v^2$$

Theoretical constraints restricts coupling space

- As before, S-matrix unitarity and positivity of Higgs potential:

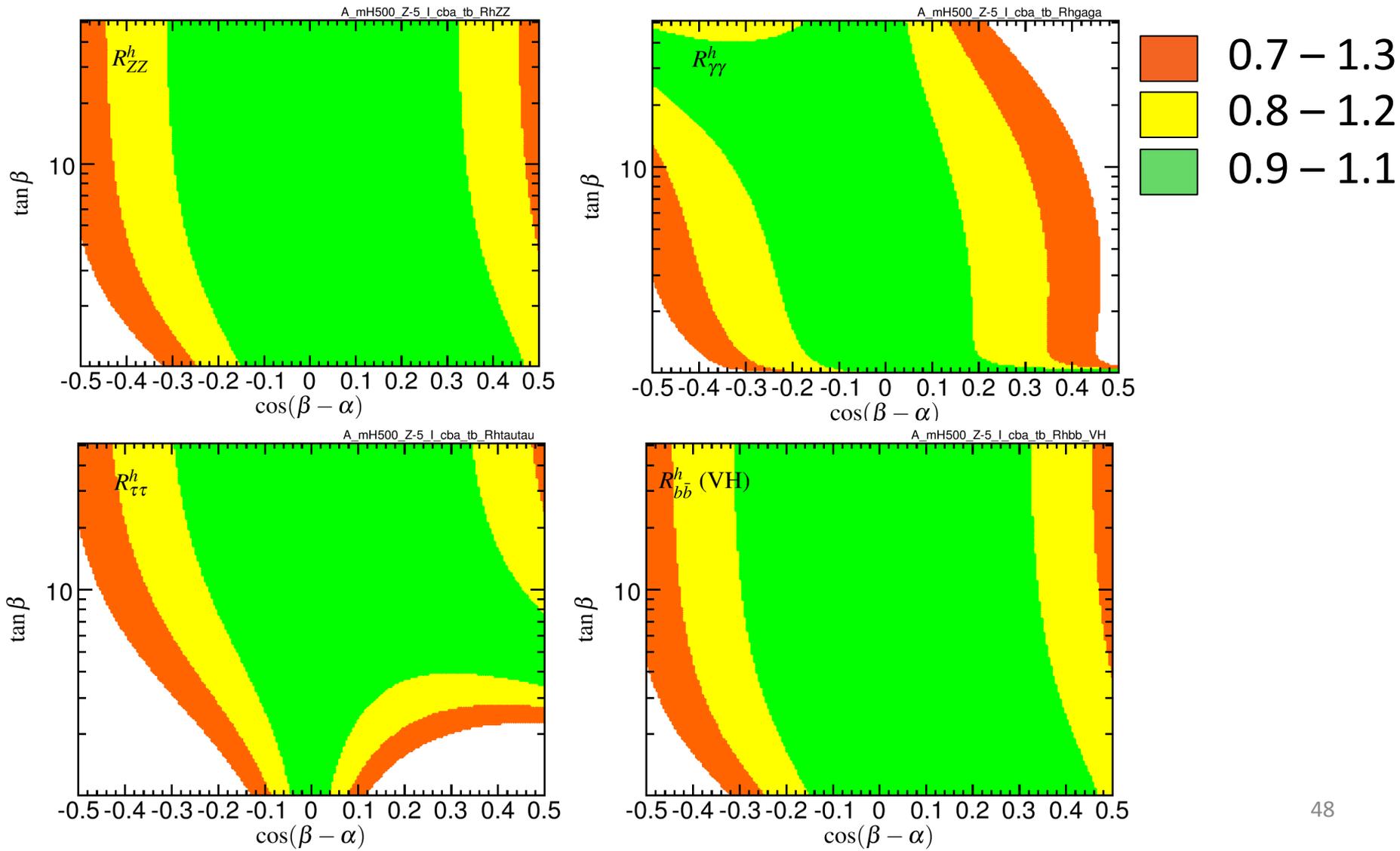
$$Z_i \sim \mathcal{O}(1)$$

Ex: $M_h = 125 \text{ GeV} < M_H < M_A = M_{H^\pm}$ ($Z_4 = Z_5 < -2$, $Z_7 = 0$)



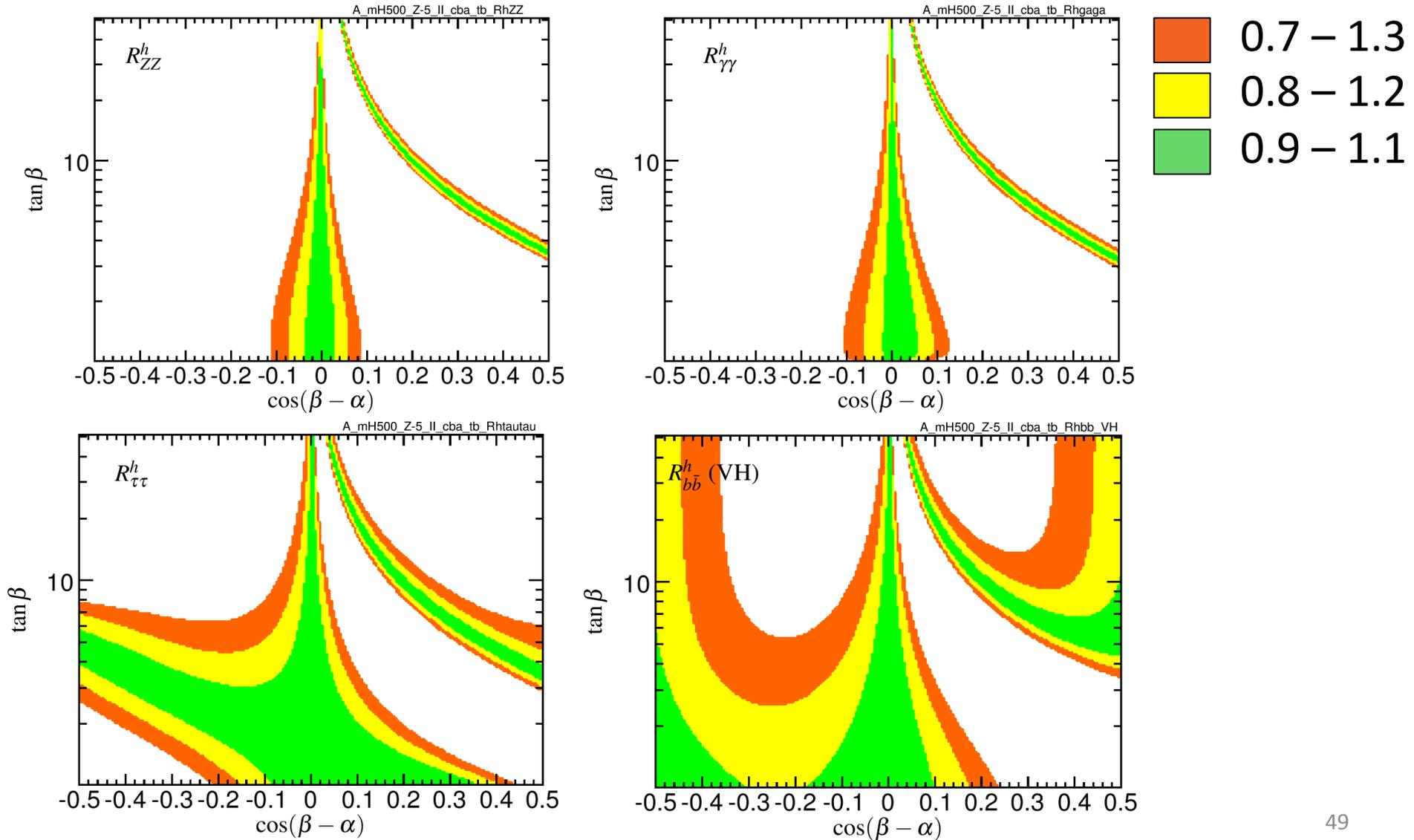
- Allowed parameter region tends towards alignment ($c_{\beta-\alpha} \rightarrow 0$) at high $\tan \beta$, positive values of $c_{\beta-\alpha}$ preferred

Scenario A (Type-I): Light Higgs rates

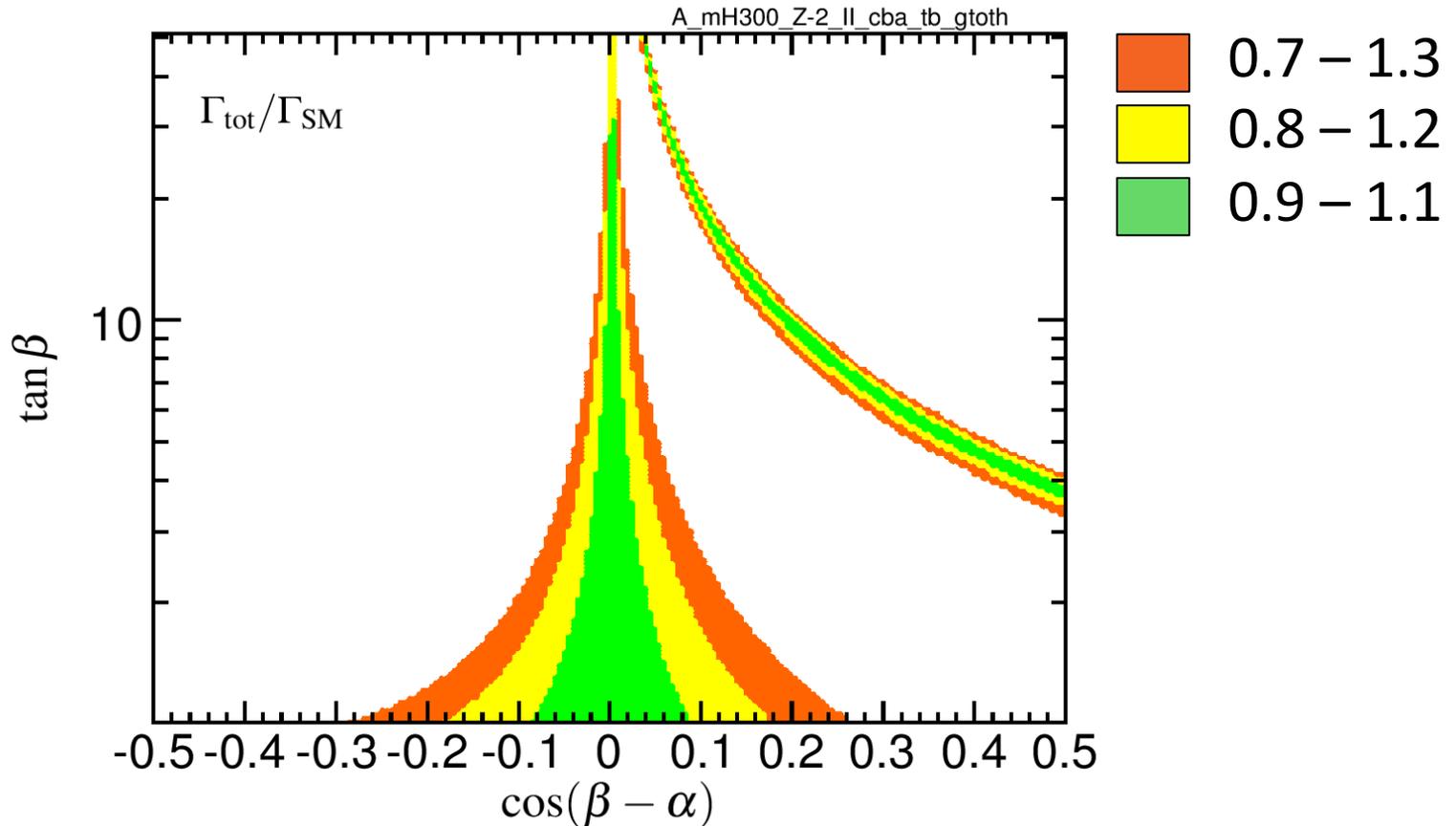


Scenario A (Type-II): Light Higgs rates

- Allowed region driven by total width ($h \rightarrow b\bar{b}$)



Total width

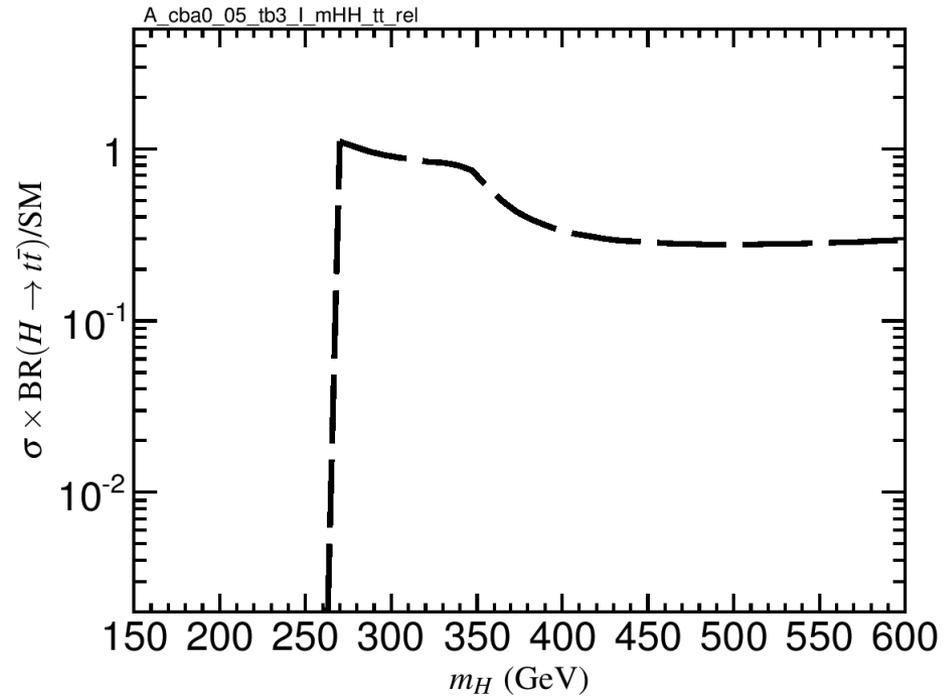
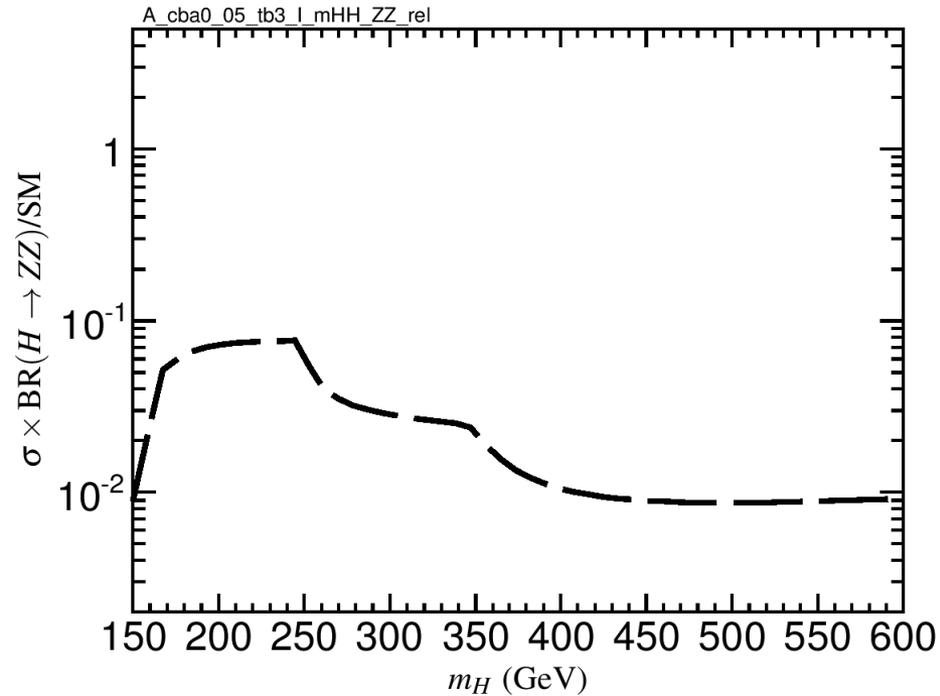


- The experimentally favored region is driven by the total h width, which in turns follow closely the coupling to b quarks

$$\frac{g_{hdd}}{g_{hdd}^{\text{SM}}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

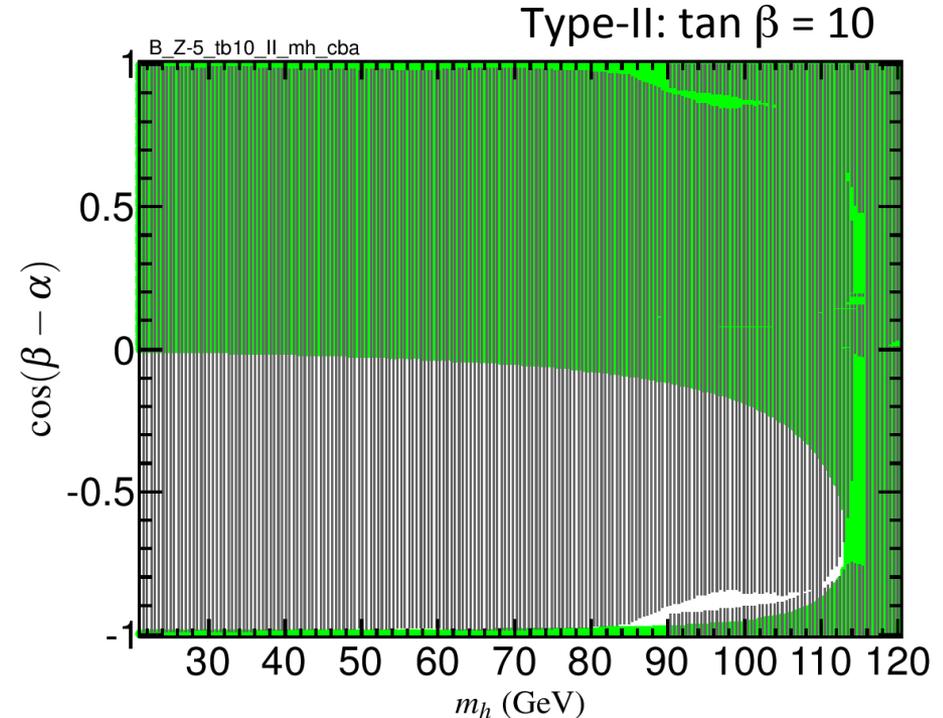
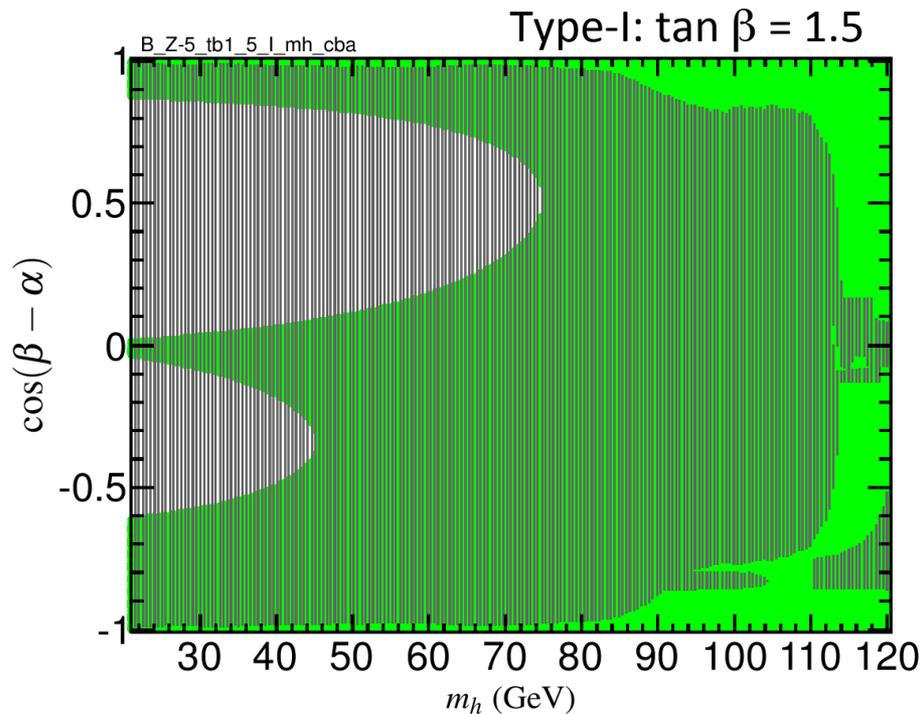
Scenario A (Type-I): Rates relative to SM

- Rates relative to SM for $\cos(\beta-\alpha) = 0.05$, $\tan \beta = 3$ (Type-I)



Scenario B

- “Inverted” scenario with lightest Higgs below 125 GeV, second CP-even Higgs, H, as the SM-like Higgs at 125 GeV
 $M_h < M_H = 125 \text{ GeV} < M_A = M_{H^\pm}$ (M_{H^\pm} above 350 GeV for Type-II)

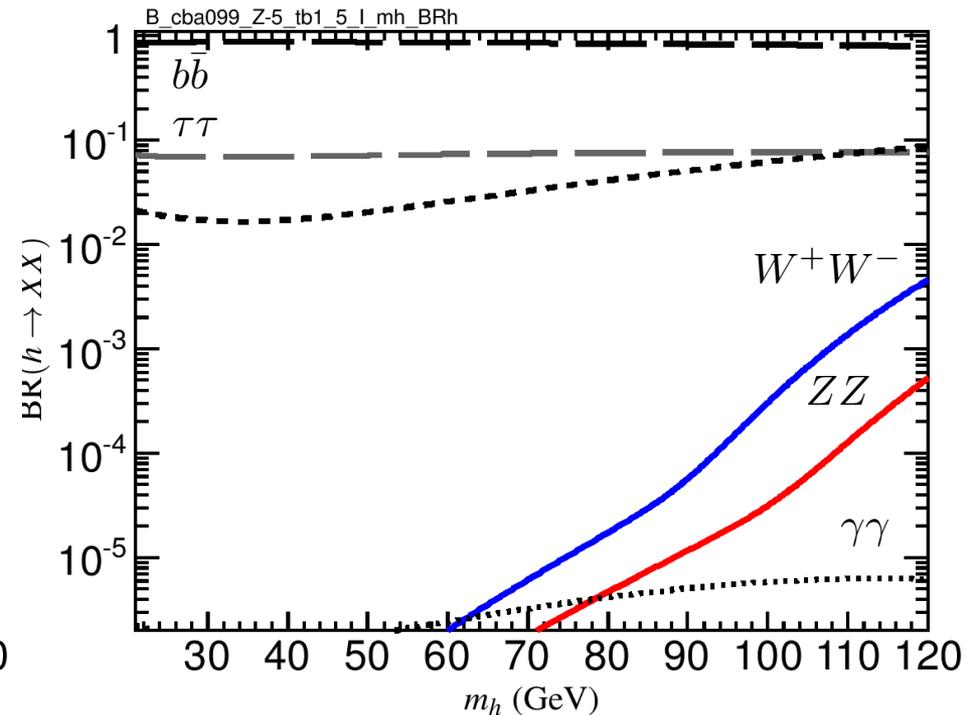
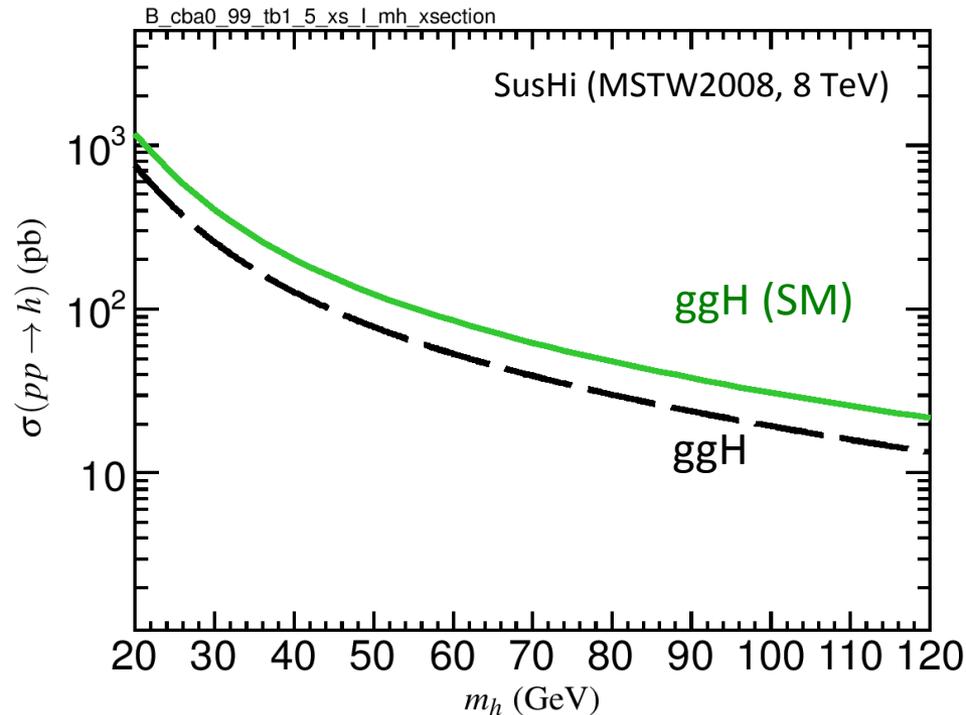


- Constraints from LEP/Tevatron/LHC (gray). Below 90 GeV only allowed solution is alignment of heavy Higgs: $|c_{\beta-\alpha}| \rightarrow 1$
 In Type-II also LHC constraints at higher $\tan \beta$ for $m_h > 90 \text{ GeV}$.

Scenario B (Type-I): Decays

- Fix the remaining free parameter $c_{\beta-\alpha}$ to ensure H SM-like, get predictions for varying M_h

Type-I: $\tan \beta = 1.5$, $c_{\beta-\alpha} = 0.99$, $M_H = 125.5$ GeV



- gg cross section similar to SM, which modes could be used?

Scenario C

Overlapping CP-even and CP-odd Higgses @ 125 GeV

$$M_h = M_A = 125 \text{ GeV} < M_H = M_{H^\pm}$$

$$Z_5 = \frac{m_H^2 - m_h^2}{v^2} s_{\beta-\alpha}^2 \quad Z_4 = -Z_5 - 2 \frac{m_H^2 - m_h^2}{v^2} c_{\beta-\alpha}^2$$

$$Z_7 = -Z_5$$

Scenario C: Degenerate states

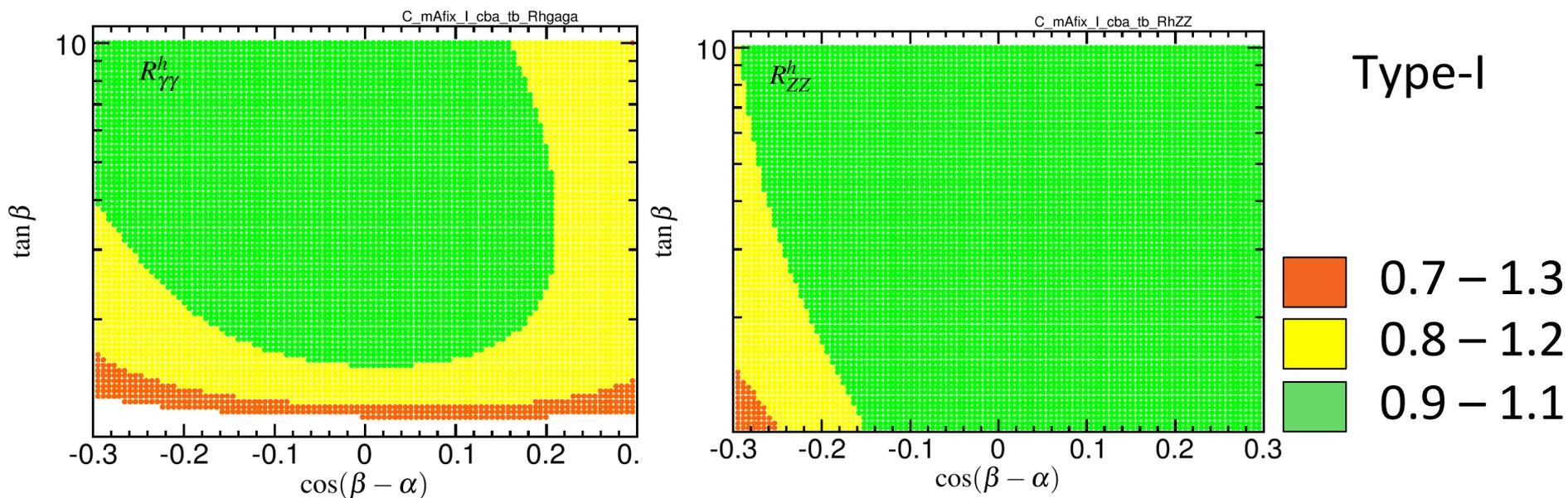
- Our framework is CP-conserving, but Scenario C can “emulate” a CP-admixture for the signal in some channels:

$h/A \rightarrow \gamma\gamma$ (inclusive) – A contribution exists, O(%) – interesting?

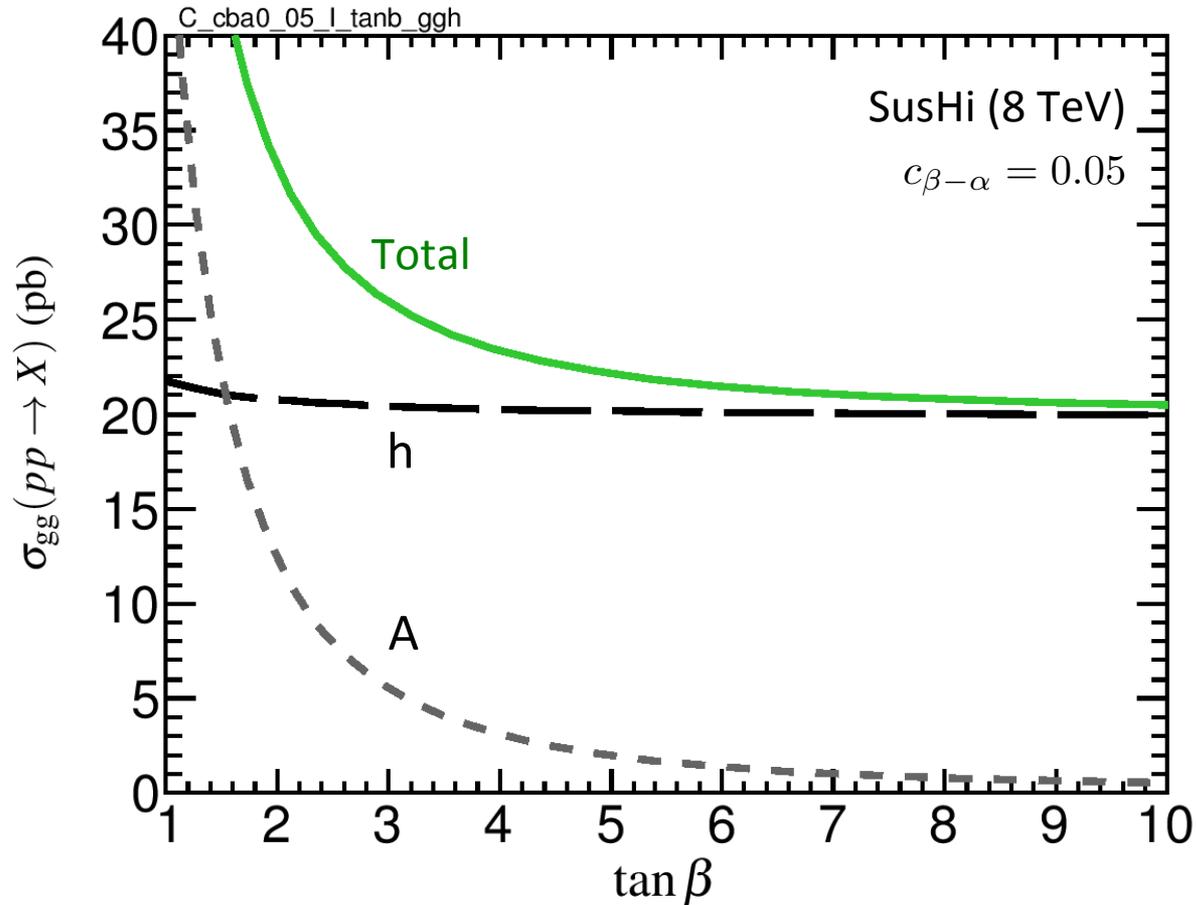
$h/A \rightarrow WW/ZZ$ (inclusive) – no tree-level A coupling

$h/A \rightarrow bb$ (VH) – no tree-level A coupling (inclusive/ttH - yes)

$h/A \rightarrow \tau\tau$ (inclusive) – similar h/A contributions possible



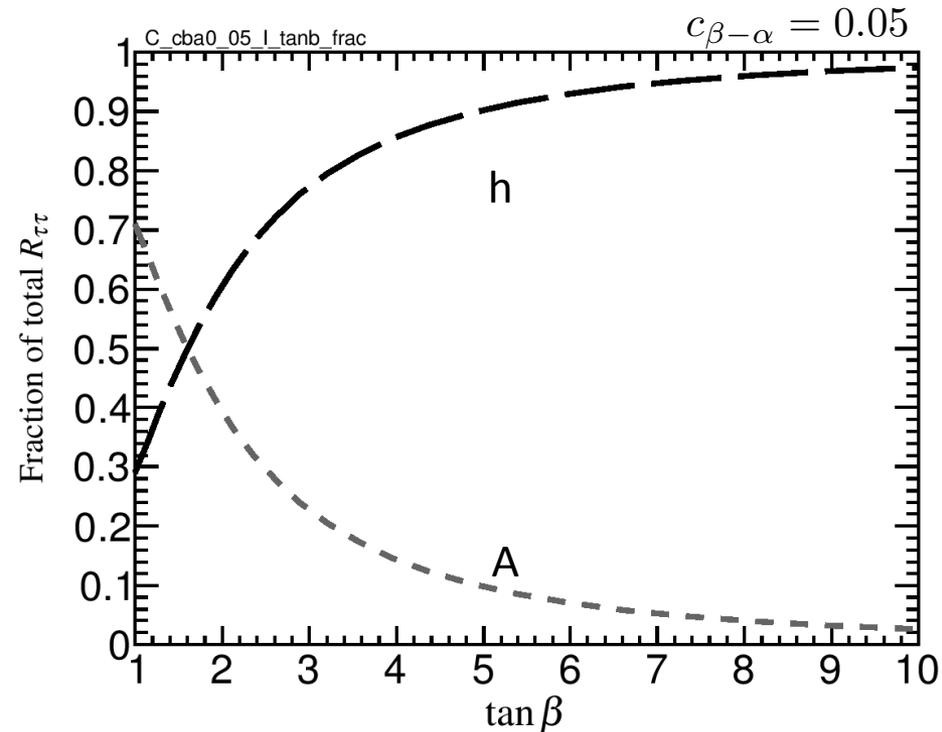
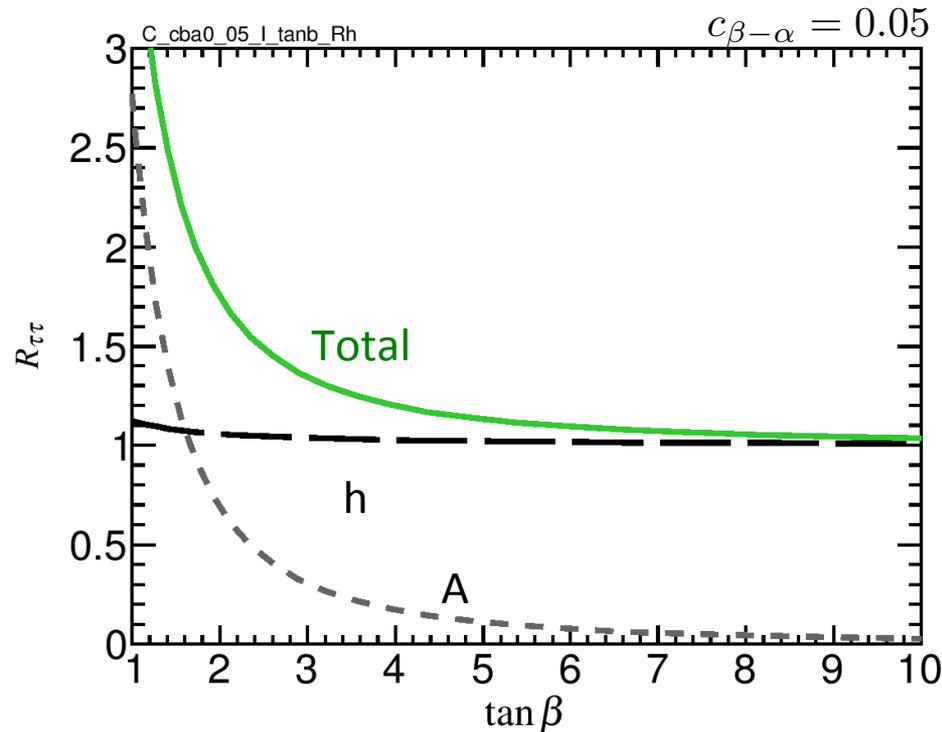
Scenario C: h/A production



- Total cross section dominated by SM-like h for high $\tan\beta$ (Yukawa decoupling in Type-I)

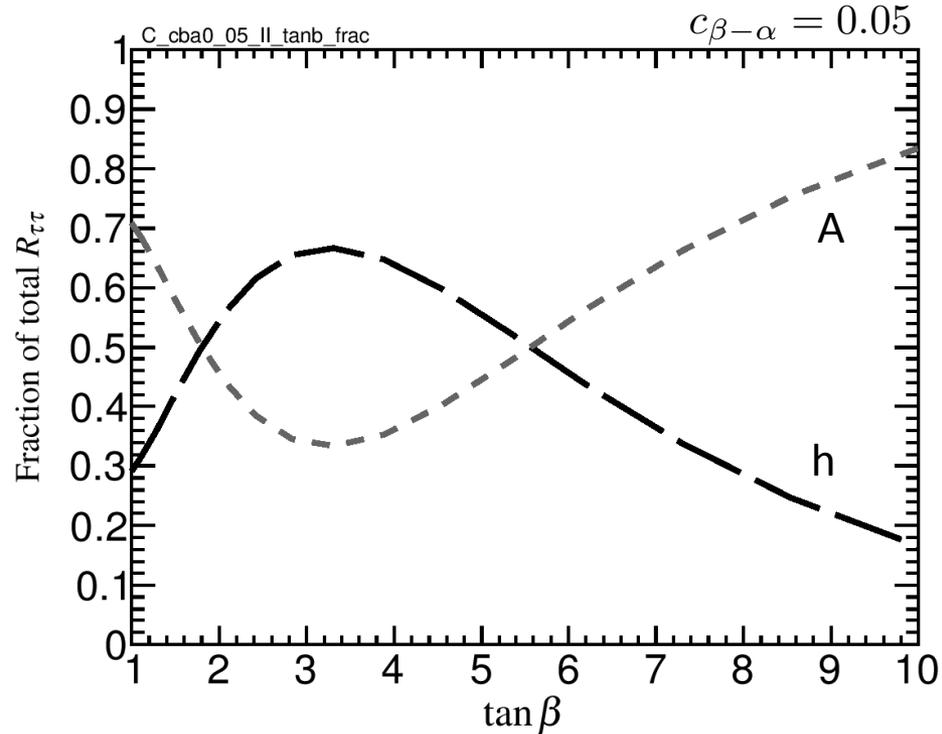
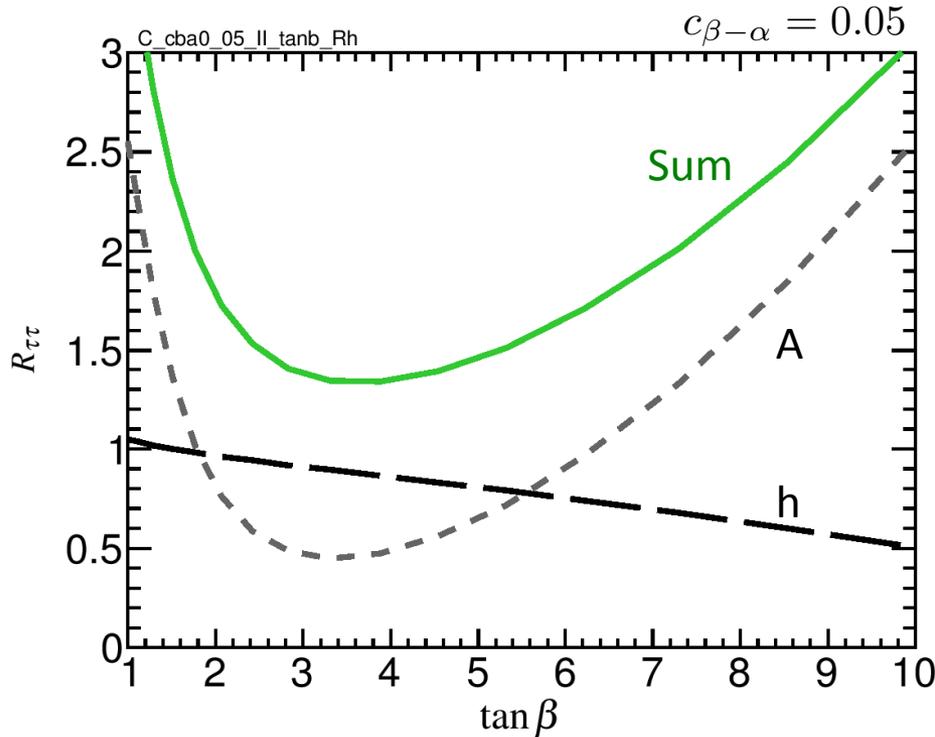
Inclusive $\tau\tau$ signal composition

$$R_{\tau\tau}^{h/A} = \frac{\sigma(pp \rightarrow h/A) \times \text{BR}(h/A \rightarrow \tau\tau)}{\sigma(pp \rightarrow H_{\text{SM}}) \times \text{BR}(H_{\text{SM}} \rightarrow \tau\tau)}$$



- The currently allowed value for the $\tau\tau$ rate (within errors) could easily accommodate for a large CP-odd contribution

Scenario C (Type-II): $\tau\tau$ composition



- Larger variation in h rate from $\text{BR}(h \rightarrow \tau\tau)$ (non-zero $c_{\beta-\alpha}$)
 Relative contribution of CP-odd Higgs always above 35%
- Low/high $\tan \beta$ in principle excluded from direct searches / rates
 Define benchmark at minimum of combined rate