

# Initial-state angular asymmetries in pA collisions

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based on work done with Adrian Dumitru  
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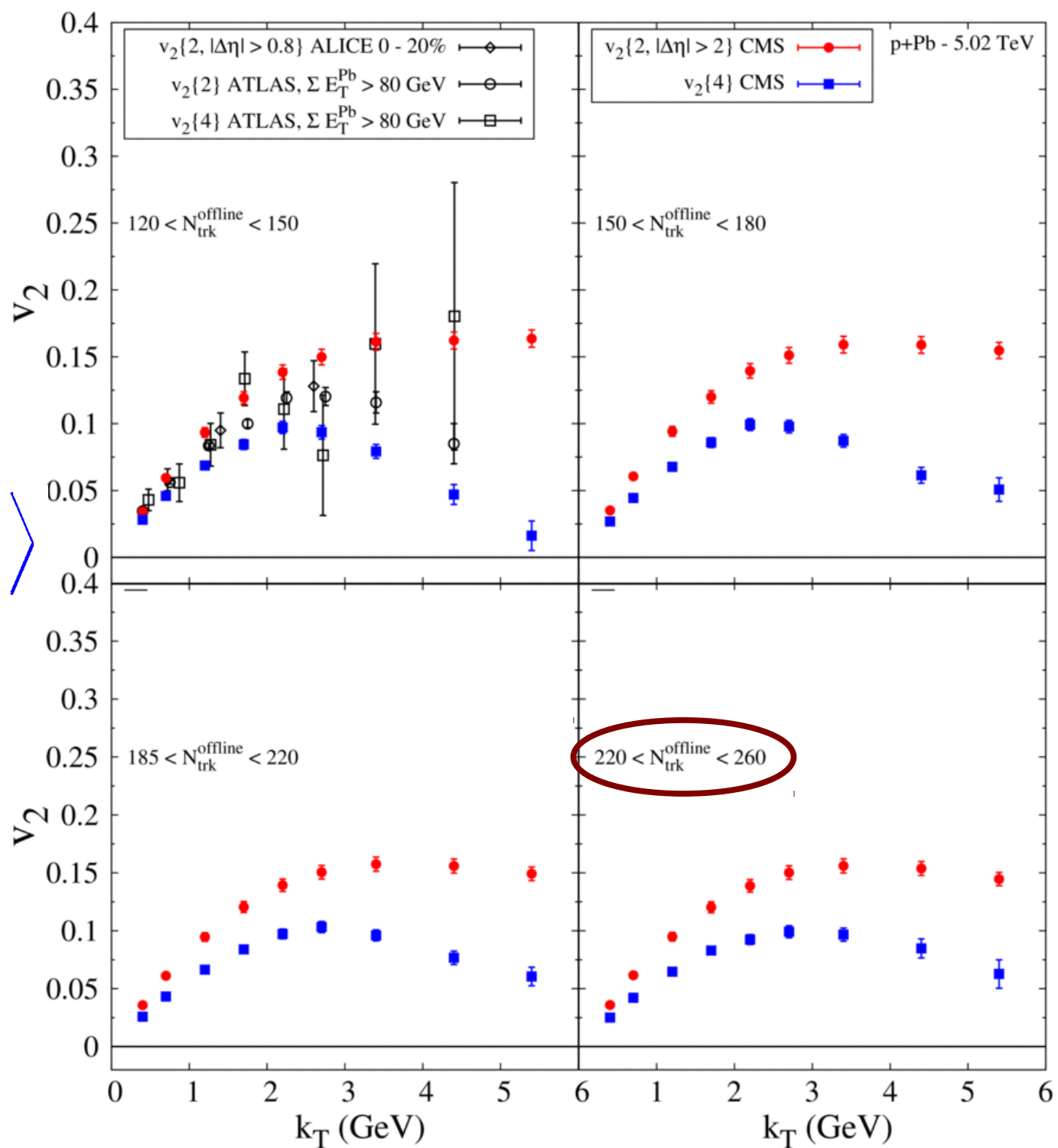
***IS2014, Dec., 3<sup>rd</sup> – 7<sup>th</sup>, 2014, Napa, CA***

# Outline:

- ◆ Rotational symmetry breaking and initial-state  $v_n$  generated by  $\vec{E}$  field “domains”
- ◆ Single domain case
- ◆ Domain model
- ◆ Genuine m-particle correlation
- ◆ Summary

# ATLAS, ALICE & CMS data for $v_2(p_T)$ in high mult. p+Pb @ 5TeV

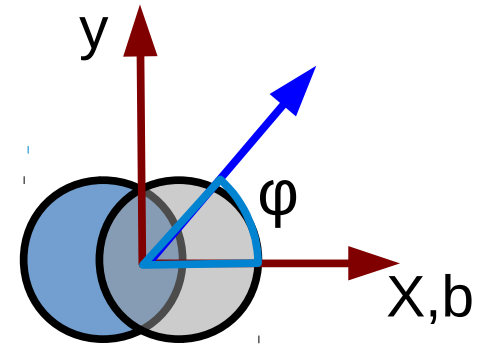
$$v_n\{2\}^2 = \left\langle e^{in(\phi_1 - \phi_2)} \right\rangle$$



# Angular asymmetries $v_n$

$$v_n = \langle \cos n\phi \rangle$$

avg on 1-particle distribution with  $\phi \rightarrow -\phi$  symmetry



classical impact parameter picture

## 2D rotational symmetry spontaneously broken:

Non-central collisions –emergence of an event plane given by  $\vec{b} - z$

- for even  $n = 2m$ :  $\langle \cos n\phi \rangle = +\langle \cos n(\phi + \pi) \rangle$   $\mathbf{P} = +$
- for odd  $n = 2m+1$ :  $\langle \cos n\phi \rangle = -\langle \cos n(\phi + \pi) \rangle$   $\mathbf{P} = -$

# Spontaneous breaking of rotational symmetry: $\vec{E}$ field “domains”

Emergence of an event plane given by  $\vec{E} - z$

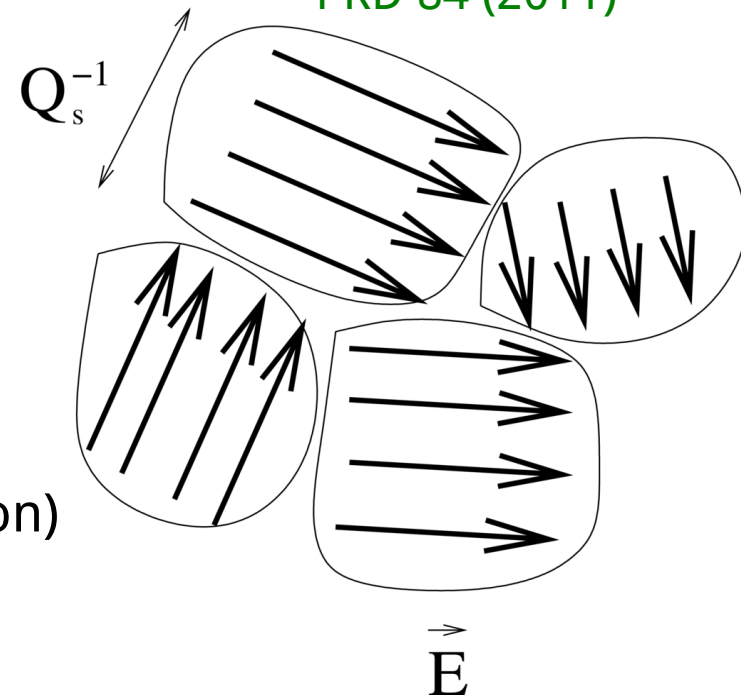
Kovner & Lublinsky:  
PRD 84 (2011)

- $\vec{E}$  field “domains”: generates even  $v_n$

$$D(\vec{r}) = \left\langle e^{-\frac{1}{2N_c} \text{Tr}(g \vec{r} \cdot \vec{E})^2} \right\rangle$$

$$g^2 r^i r^j \langle \text{tr} E^i E^j \rangle \sim r^2 Q_s^2 \left[ 1 + \mathcal{A}(\cos^2 \phi_r - \frac{1}{2}) \right]$$

(avg. over all configurations but for a fixed  $\vec{E}$  orientation)



- coherent fluctuation in  $Q_s$ :  
generates odd  $v_n \rightarrow$  odderon (not this talk)
- Angular dependence of *single-particle* distribution,  
*any* particle correlated with “event plane”

# Single-inclusive distribution in q+A elastic scattering:

$$\frac{dN}{d^2k} = \int d^2r e^{-i\vec{k}\cdot\vec{r}} D(\vec{r})$$

dipole S-matrix (real part)

**Qualitative work:** no final state effects and no proton PDF convolution

MV model dipole:

$$D(\vec{r}) = \exp \left[ -\frac{1}{4} r^2 Q_s^2 (1 - \mathcal{A} + 2\mathcal{A} \cos^2 \phi_r) \log \frac{1}{r\Lambda} \right]$$

polarization amplitude

Fourier transform at  $k_T \gg Q_s$ :

$$\frac{dN}{k_T dk_T d\phi_k} = \frac{1}{2\pi} \frac{Q_s^2}{k_T^4} [1 - 2\mathcal{A} + 4\mathcal{A} \cos^2 \phi_k]$$

Azimuthal harmonics :

- $v_2(k_T) = \mathcal{A} \left( 1 + \frac{\#}{k_T^2} \right)$

- $v_4(k_T) \sim 1/k_T^2$

\*\*\* no  $v_{2n}$  without polarization! \*\*\*

Fourier transform at  $k_T < Q_s$  :

$$\frac{dN}{k_T dk_T d\phi_k} \sim \exp \left[ -\frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \left( \frac{\cos^2 \phi_k}{1 + \mathcal{A}} + \frac{\sin^2 \phi_k}{1 - \mathcal{A}} \right) \right]$$

Azimuthal harmonics :

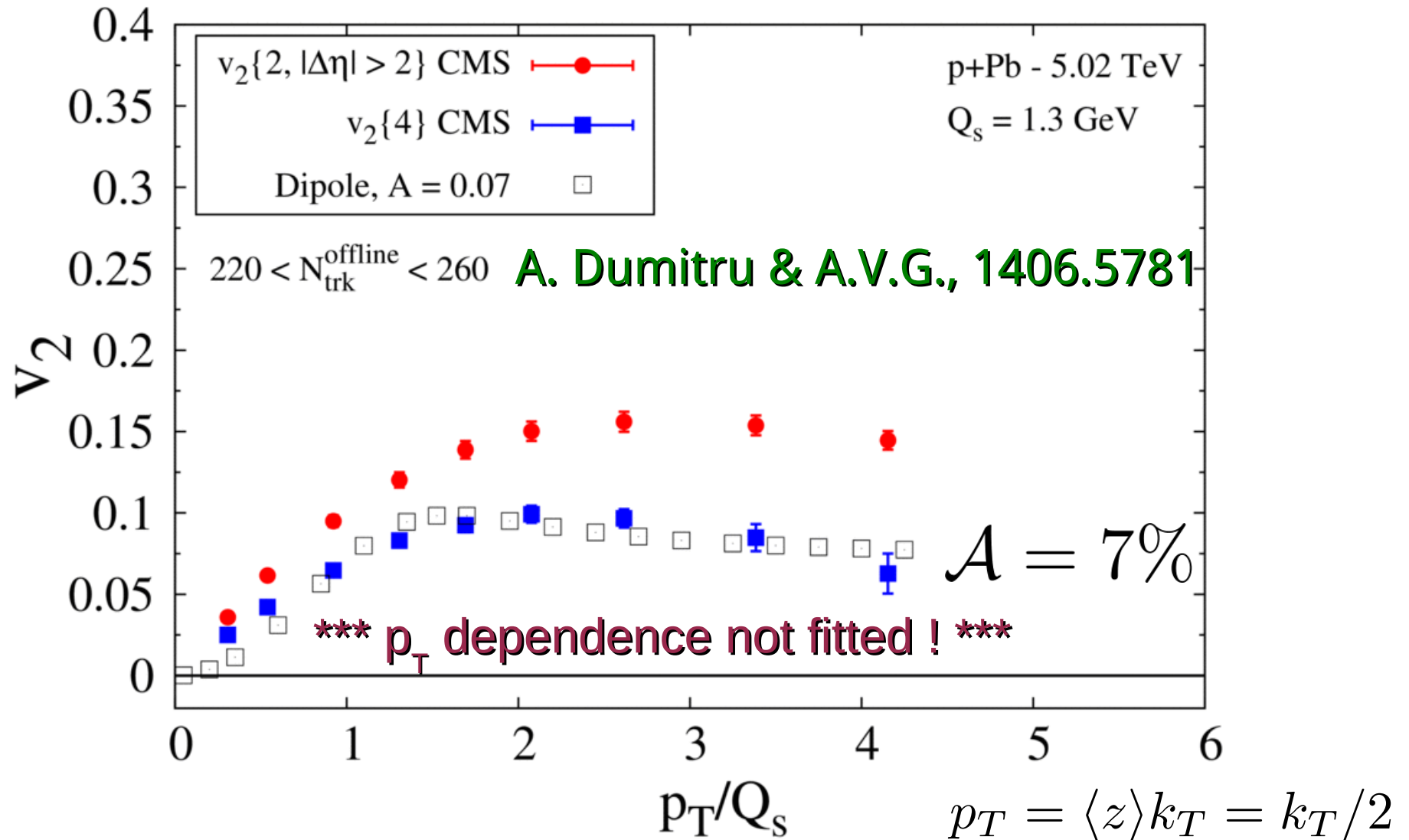
$$v_2(k_T) = \frac{I_1 \left( \frac{\mathcal{A}}{1 - \mathcal{A}^2} \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \right)}{I_0 \left( \frac{\mathcal{A}}{1 - \mathcal{A}^2} \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \right)} \simeq \frac{\mathcal{A}}{2} \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda}$$

$$v_4(k_T) = \frac{I_2 \left( \frac{\mathcal{A}}{1 - \mathcal{A}^2} \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \right)}{I_0 \left( \frac{\mathcal{A}}{1 - \mathcal{A}^2} \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \right)} \simeq \frac{\mathcal{A}^2}{8} \left( \frac{k_T^2}{Q_s^2 \log Q_s / \Lambda} \right)^2$$

- $v_2 \sim \mathcal{A} k_T^2$
  - $v_4 \sim (v_2)^2 \longrightarrow$  suppressed
- \*\*\* no  $v_{2n}$  without polarization! \*\*\*



# Numerical Fourier transform: single domain case



●  $A \sim 7\%$

●  $v_4 < 1\%$  -try domain model

# Domain model :

$$v_n^2\{2\} e^{i\psi} \equiv \left\langle e^{in(\phi_1 - \phi_2)} \right\rangle$$

$$= \frac{1}{\mathcal{N}} \int \frac{d\phi_1}{2\pi} \frac{d\phi_2}{2\pi} e^{in\phi_1} e^{-in\phi_2} \frac{dN}{k_T dk_T d\phi_1} \frac{dN}{k_T dk_T d\phi_2}$$

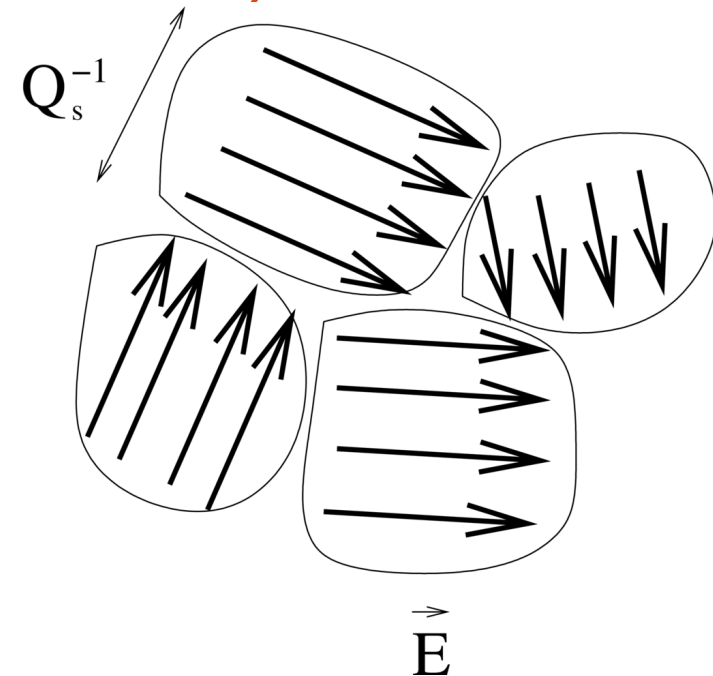
**+ two-particle correl.**  $\longrightarrow$  in a couple of slides

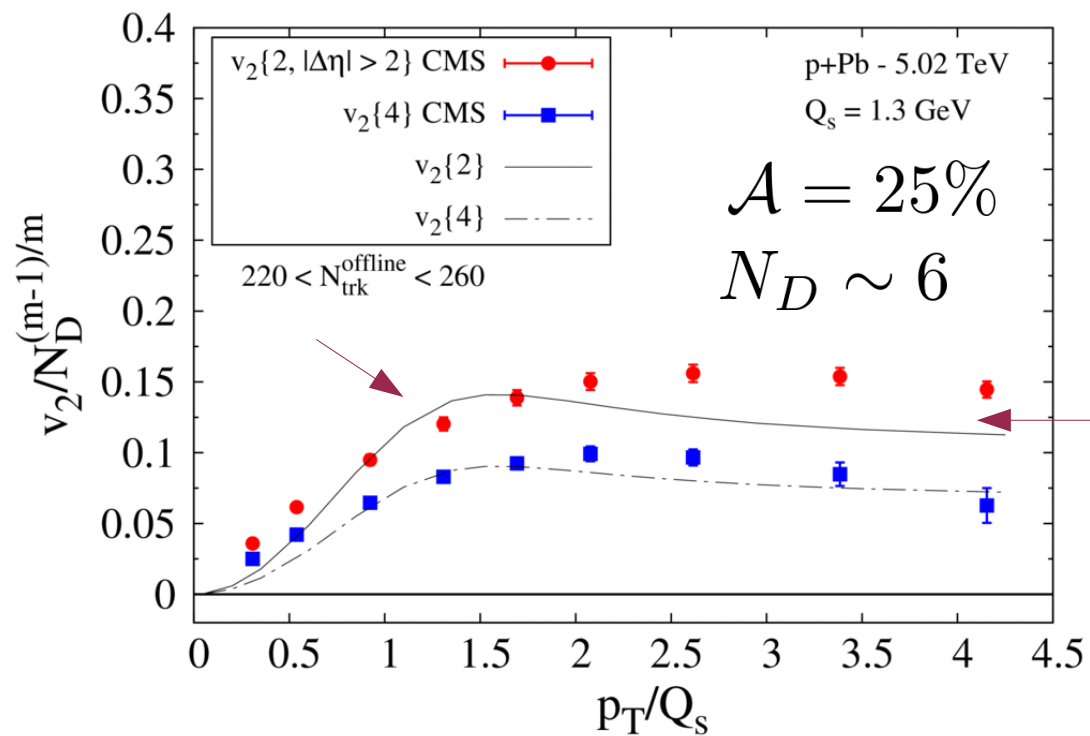
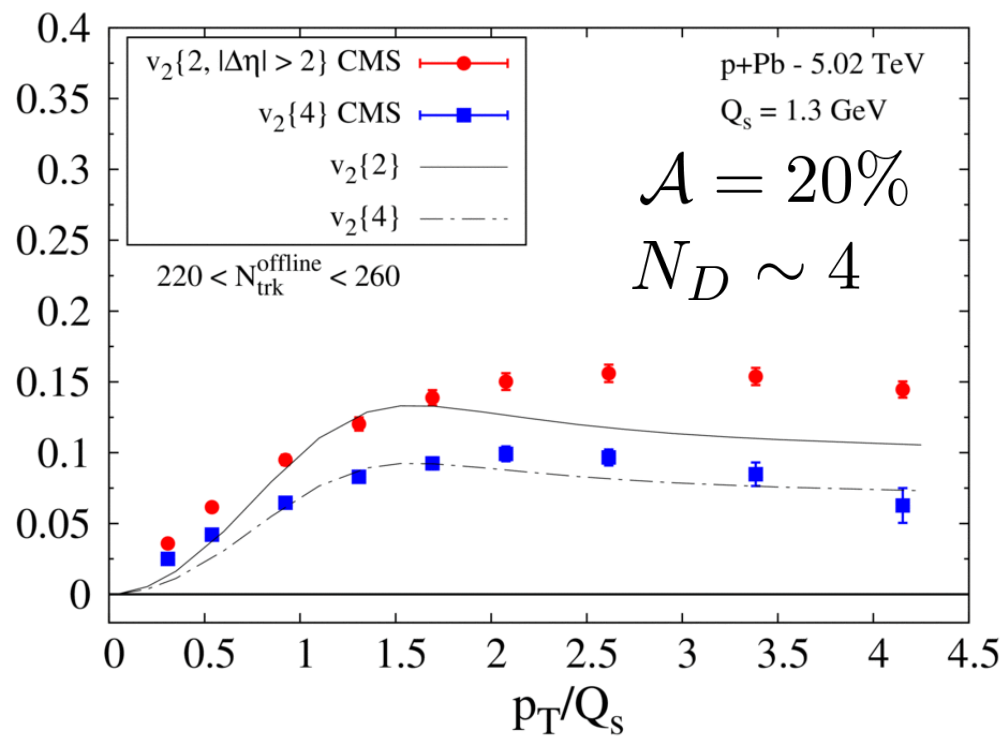
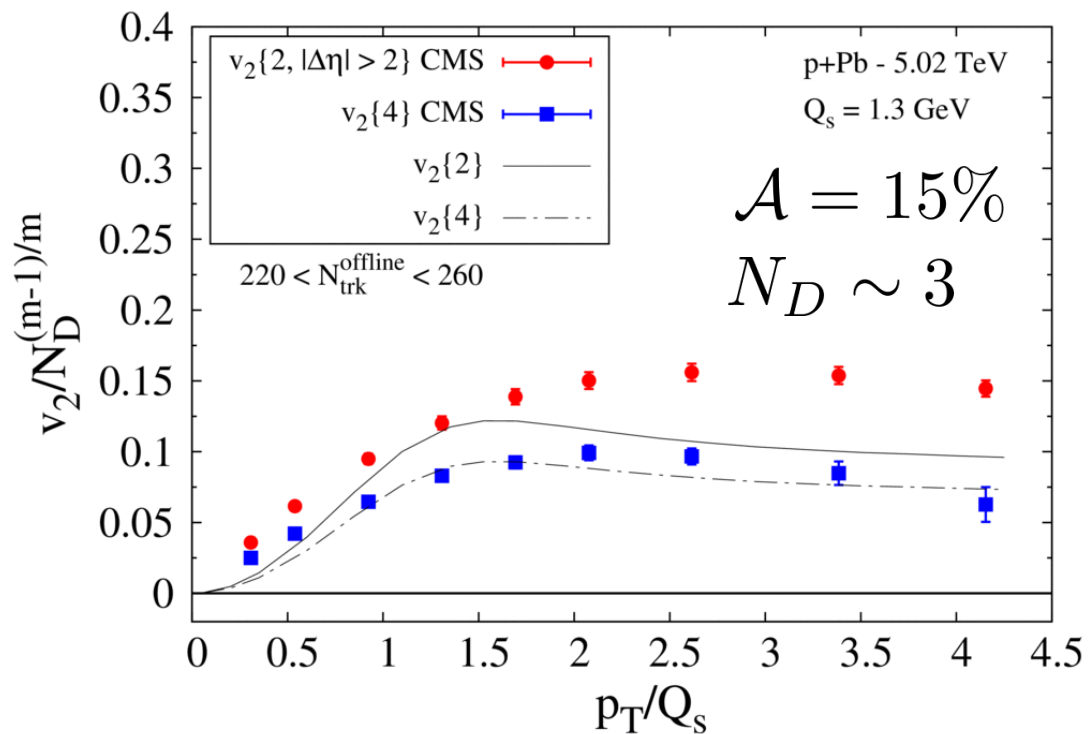
$$(v_n\{m\})^m = (v_n\{1\})^m \quad (\text{all } m \text{ particles in same domain})$$

$$= 0 \quad (\geq 1 \text{ particle in other domain})$$

$$v_n\{m\} = \frac{v_n\{1\}}{N_D^{(m-1)/m}}$$

**probability of having all m particles in same domain**

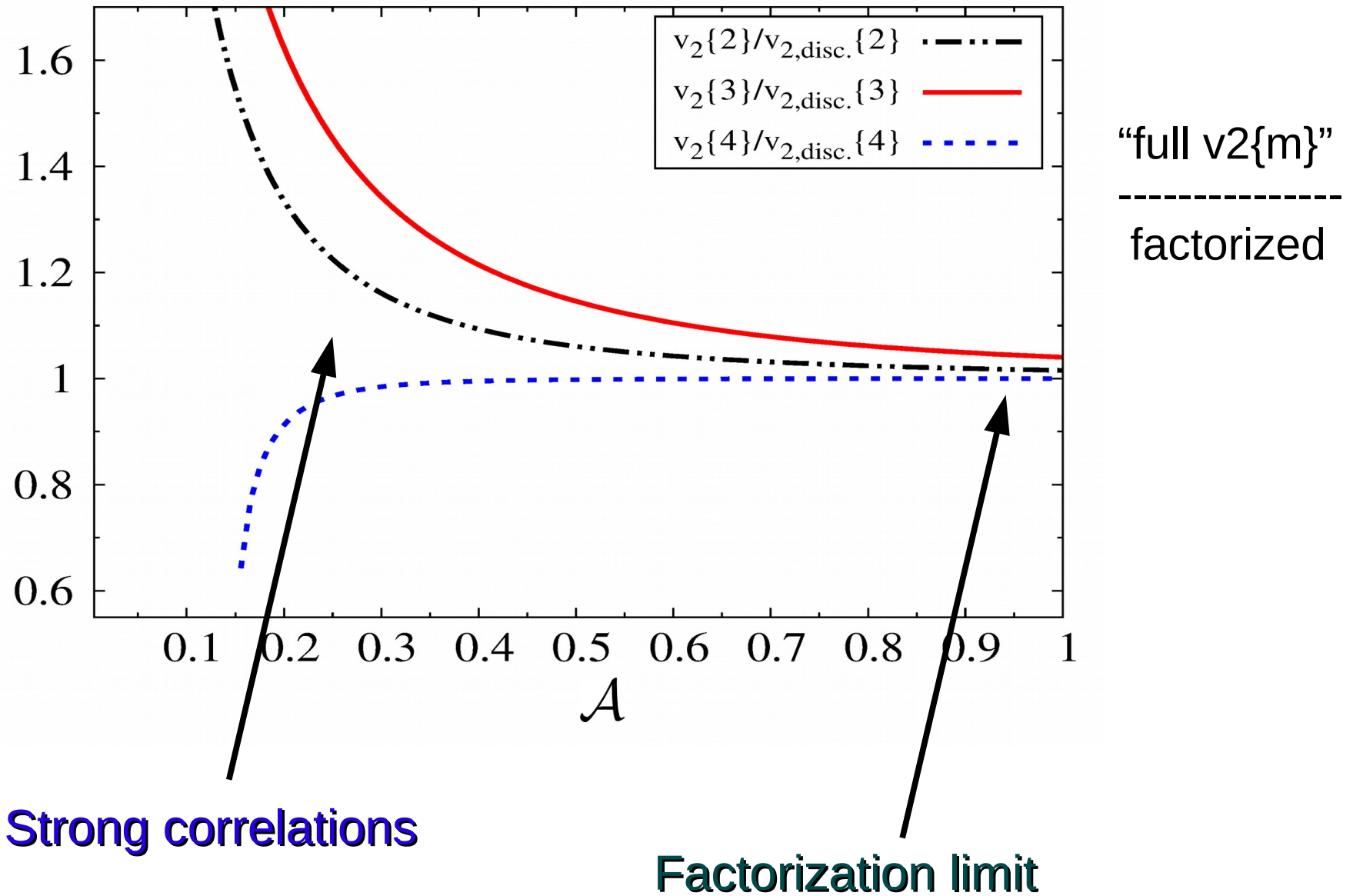




●  $\mathcal{A} \sim 15\% - 25\%$

●  $N_D \sim 3 - 6$

# How about genuine multi-particle correlations?



# Genuine multi-particle correlations cont'd

A.~Dumitru, L.~McLerran and  
V.~Skokov, arXiv:1410.4844 [hep-ph].

$$c_2\{2\} = \langle e^{2i(\phi_1 - \phi_2)} \rangle$$

$$c_2\{4\} = \langle e^{2i(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle - 2 \langle e^{2i(\phi_1 - \phi_3)} \rangle \langle e^{2i(\phi_2 - \phi_4)} \rangle$$

From MV model (high  $p_T$ ):

$$\text{2-part. corr.} \rightarrow \langle S \rangle \sim \left( \frac{(ig)^2}{2N_c} \right)^2 \langle \text{tr}(\vec{r}_1 \cdot \vec{E}(\vec{b}_1))^2 \text{tr}(\vec{r}_2 \cdot \vec{E}(\vec{b}_2))^2 \rangle$$

$$(v_2\{2\})^2 = c_2\{2\} \equiv \frac{1}{N_D} \left( (v_2\{1\})^2 + \frac{1}{4(N_c^2 - 1)} \right) = \frac{1}{N_D} \left( \mathcal{A}^2 + \frac{1}{4(N_c^2 - 1)} \right)$$

**disconnected contribution**

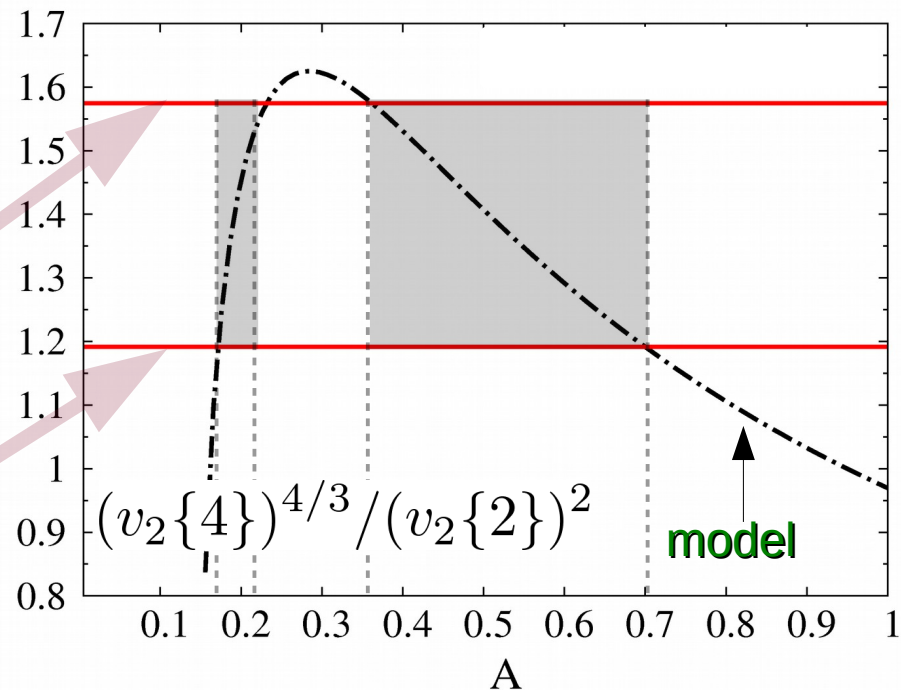
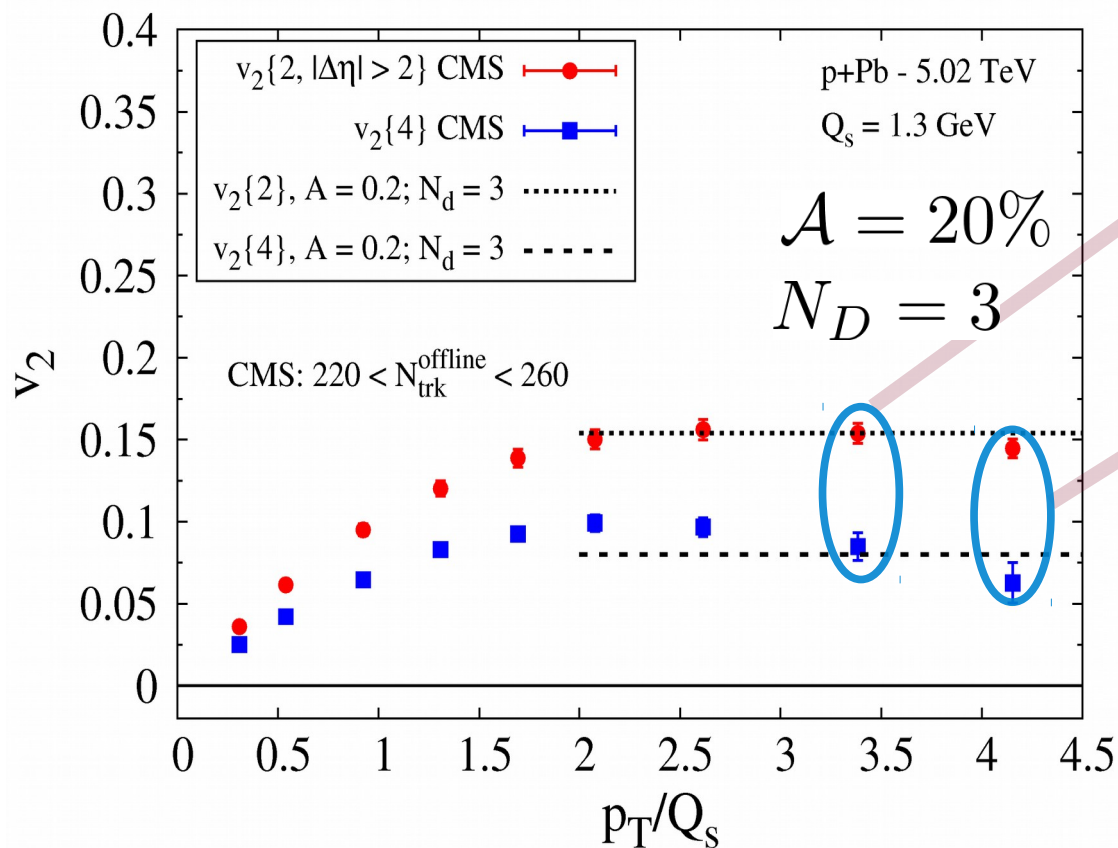
**(i.e. factorizable)**

**connected contribution**

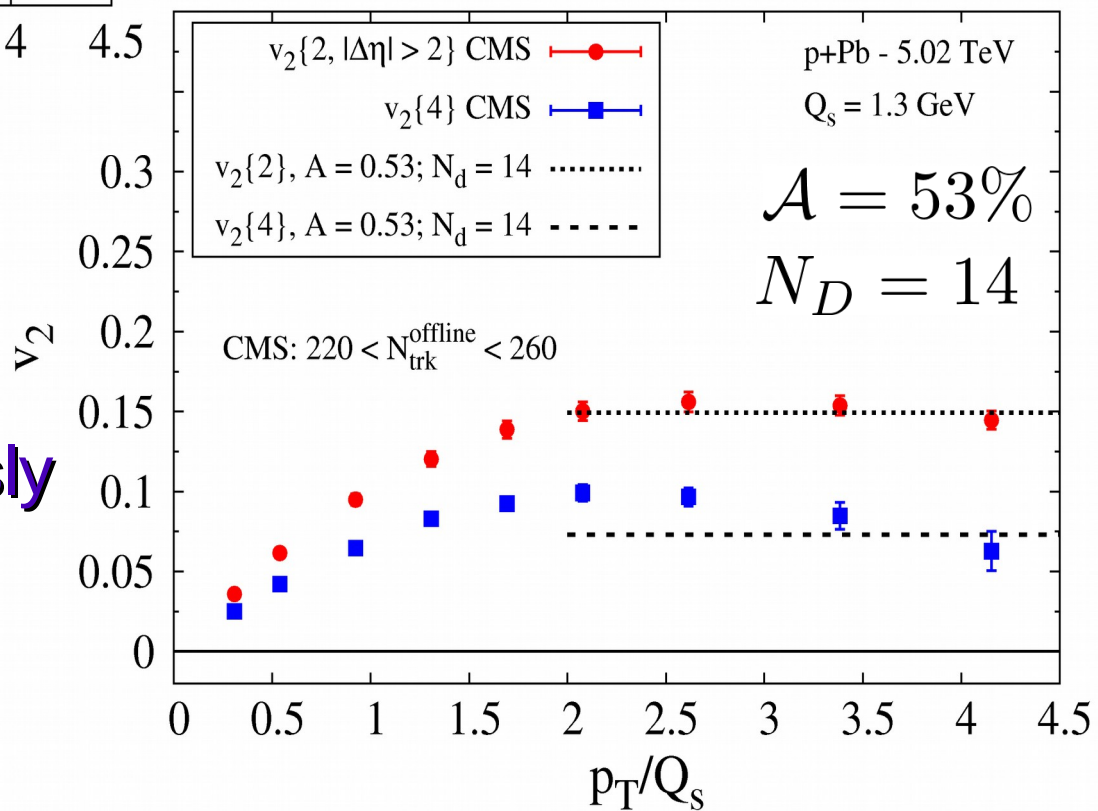
$$(v_2\{4\})^4 \equiv -c_2\{4\} = \frac{1}{N_D^3} \left( (v_2\{1\})^4 - \frac{1}{4(N_c^2 - 1)^3} \right) = \frac{1}{N_D^3} \left( \mathcal{A}^4 - \frac{1}{4(N_c^2 - 1)^3} \right)$$

(around  $c_2\{4\} \sim 0$ )

More details → Adrian's and Vladimir's talks



- Corrections improve the high-pt region
- $v_2\{2\}$  and  $v_2\{4\}$  simultaneously
- Two solutions for  $\mathcal{A}$



# How about 3-particle correlations ?

(again: high  $p_T$ )

with Dumitru  
& Skokov

$$c_2\{3\} = \left\langle e^{2i(\phi_1 + \phi_2 - 2\phi_3)} \right\rangle$$

requires v4-like contribution from particle 3 –expand S-matrix to order  $r_1^2, r_2^2, r_3^4$

$$\frac{1}{2} \left( \frac{(ig)^2}{2N_c} \right)^4 \left\langle \text{tr} (\vec{r}_1 \cdot \vec{E}(\vec{b}_1))^2 \text{tr} (\vec{r}_2 \cdot \vec{E}(\vec{b}_2))^2 \left[ \text{tr} (\vec{r}_3 \cdot \vec{E}(\vec{b}_3))^2 \right]^2 \right\rangle$$

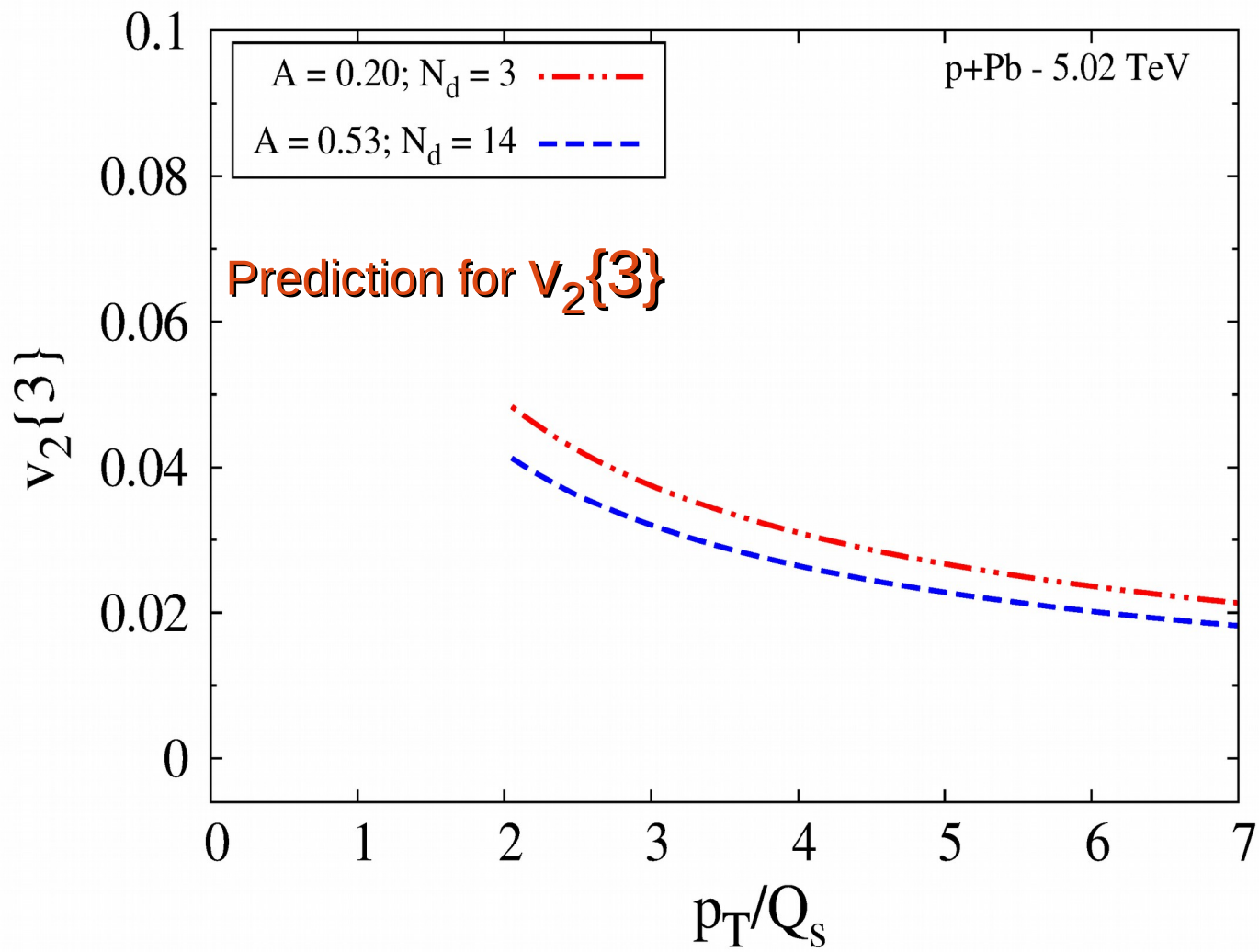
gives ( $A \sim 1/N_c$ ):

$$c_2\{3\} \sim \frac{Q_s^2}{k_{\perp 3}^2} \frac{1}{N_D^2} \left[ \frac{1}{2} A^4 + \frac{1}{2} A^2 \frac{1}{N_c^2 - 1} + \frac{1}{16} \left( \frac{1}{N_c^2 - 1} \right)^2 \right]$$

disconnected,  
4 dipoles

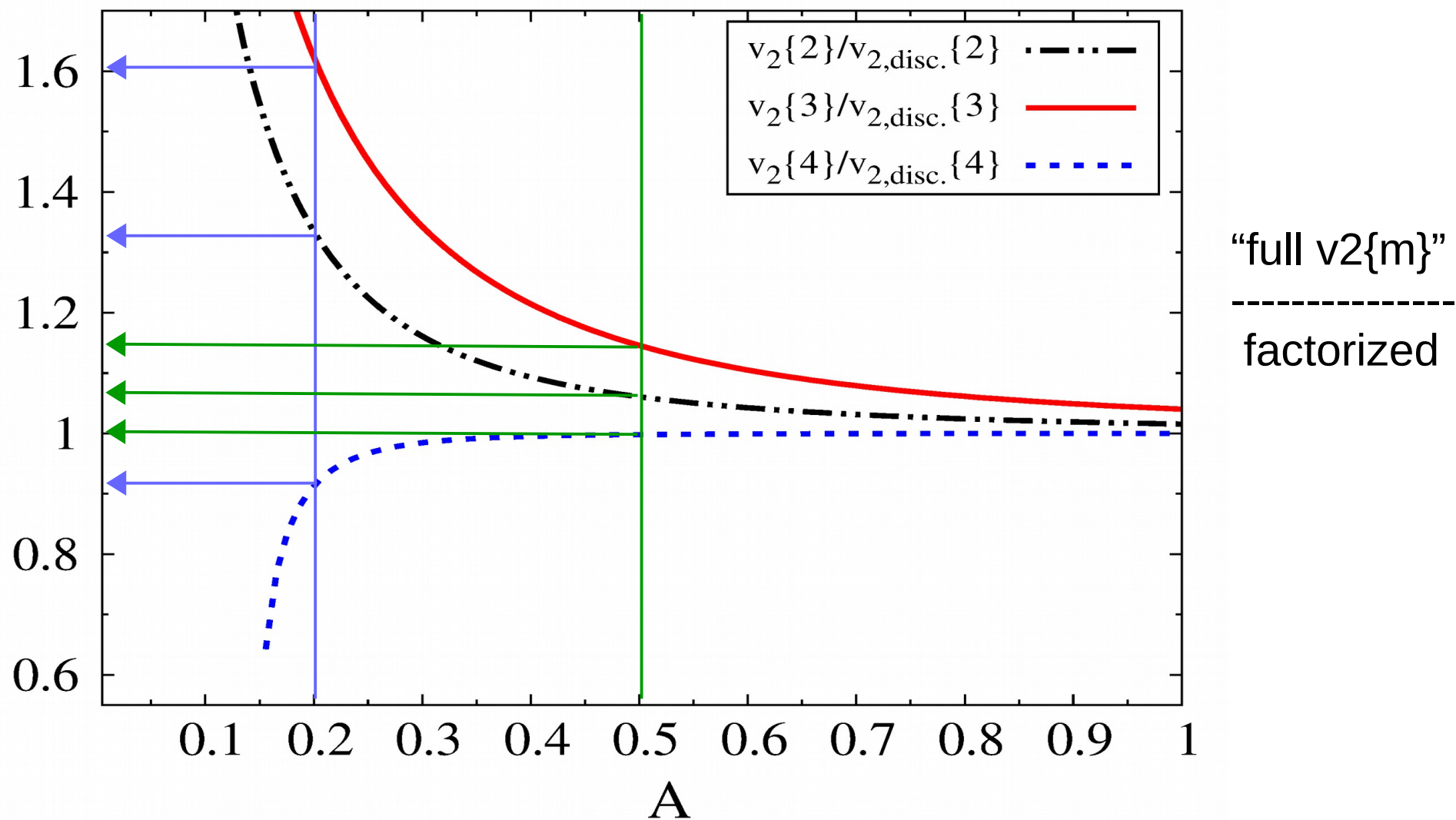
3-particle connected,  
 $dN_1 * dN_3$

2 2-particle connected,  
 $dN_2 * dN_2$



Are the connected diagrams important?





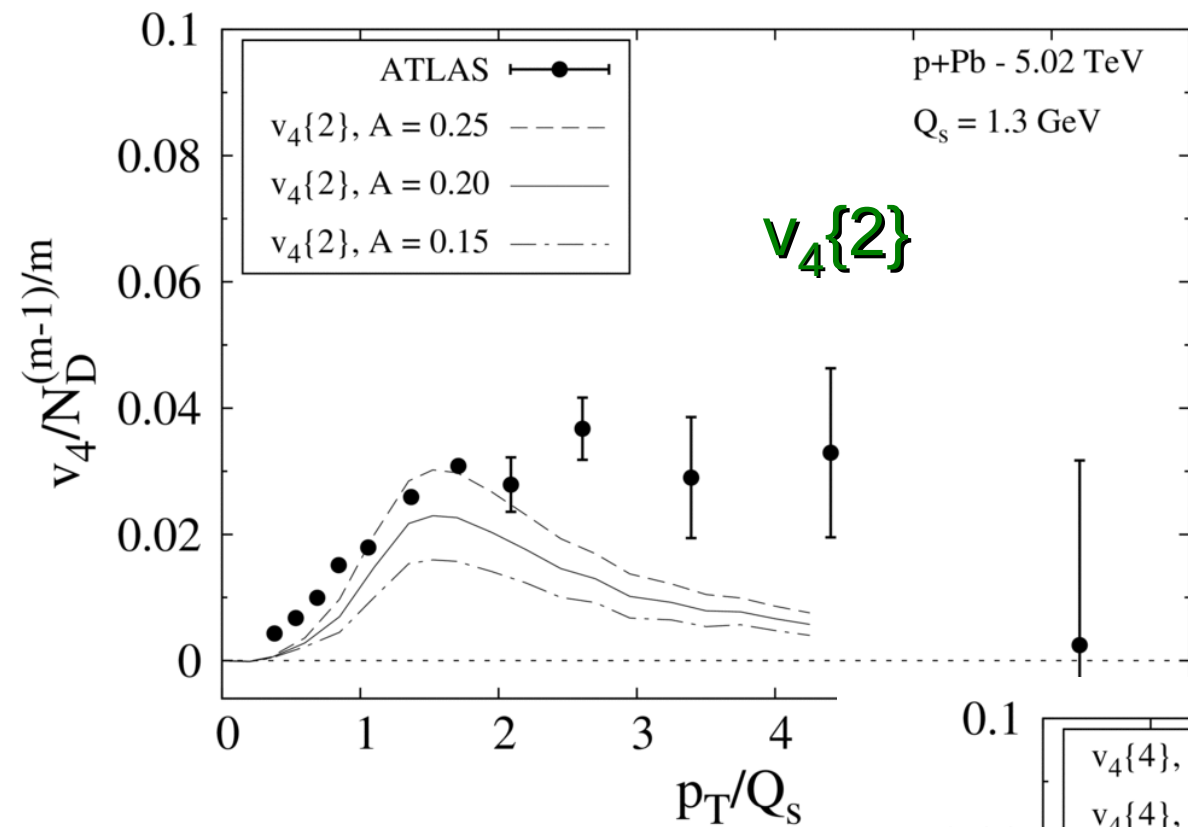
$A$	$v_2\{2\}/v_{2,disc.\{2\}}$	$v_2\{3\}/v_{2,disc.\{3\}}$	$v_2\{4\}/v_{2,disc.\{4\}}$
0.2	1.3	1.6	0.9
0.5	1.05	1.15	1.0

# Summary / Outlook

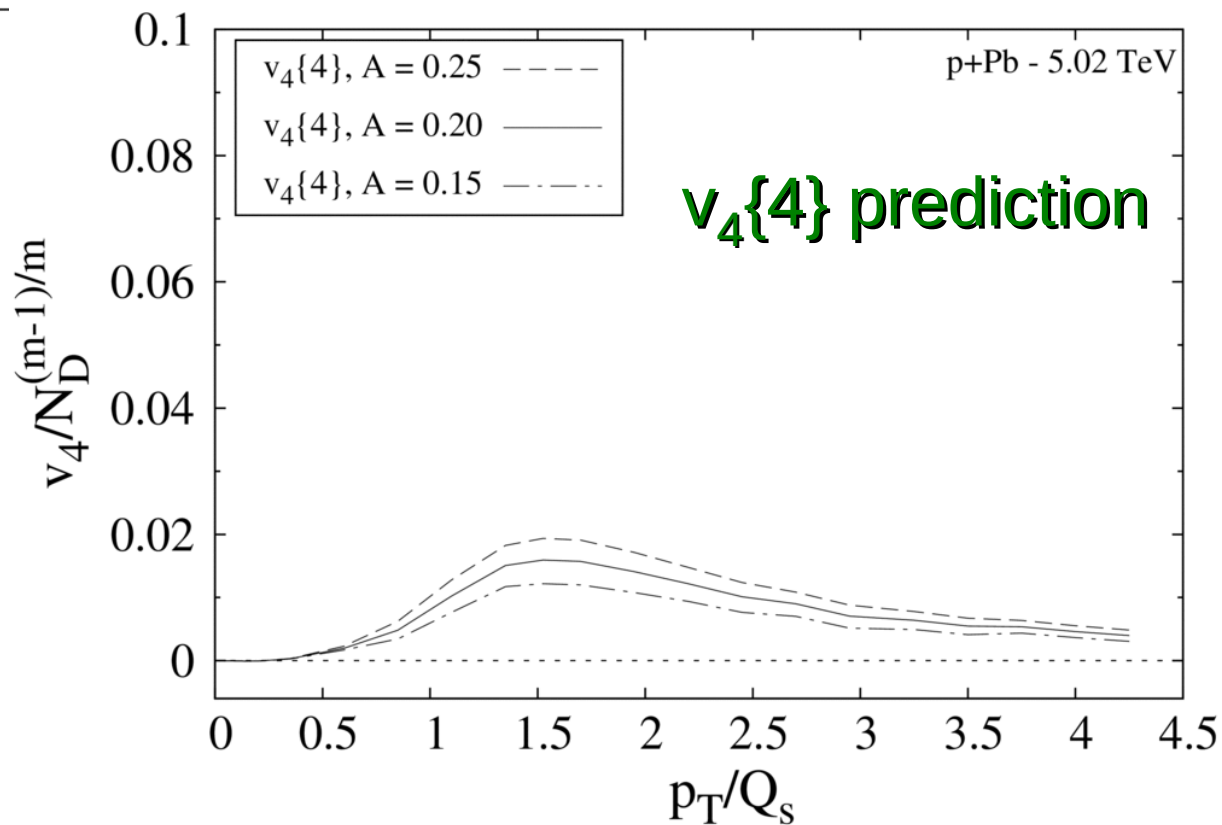
- Initial-state  $v_n$  due to anisotropic target E field
- Connected diagrams improve the high-pt region description
- Allows fitting  $v_2\{2\}$  and  $v_2\{4\}$  simultaneously
- Can not uniquely fix  $\mathcal{A}$  and  $N_D$  from high  $p_T$  alone
- $\mathcal{A} \gg 0.2$  results ruled out by  $v_2\{4\}$  low pt data ?

If so: large connected contributions to m-particle correlation functions

# Backup Slides



- model predicts  $v_4\{4\} \ll v_2\{4\}$
- also,  $v_4\{4\}$  drops with  $p_T$



## Now let's get even with the odderon:

$$iO(\vec{r}) = \frac{1}{2N_c} \text{tr} \langle V_x V_y^\dagger - V_y V_x^\dagger \rangle$$


for C-even MV action,  $S_{\text{MV}} = \int d^2x \frac{\rho^a \rho^a}{2\mu^2} \quad \rightarrow O(r) = 0$

however, adding cubic Casimir  $-\frac{d^{abc} \rho^a \rho^b \rho^c}{\kappa_3} \quad \rightarrow O(r) \neq 0$

[ Kovchegov, Szymanowski & Wallon: PLB 586 (2004);  
Jeon & Venugopalan: PRD 71 (2005) ]

Technical side remarks:

- Beyond perturbative treatment of  $\sim \rho^3$  operator one needs to add quartic Casimir  $\sim \rho^4$  too
- Even though  $\kappa_3 \sim A^{2/3}$ , at small  $r$  one has that  $O(r) \sim A^{1/3}$ , just as  $D(r)$



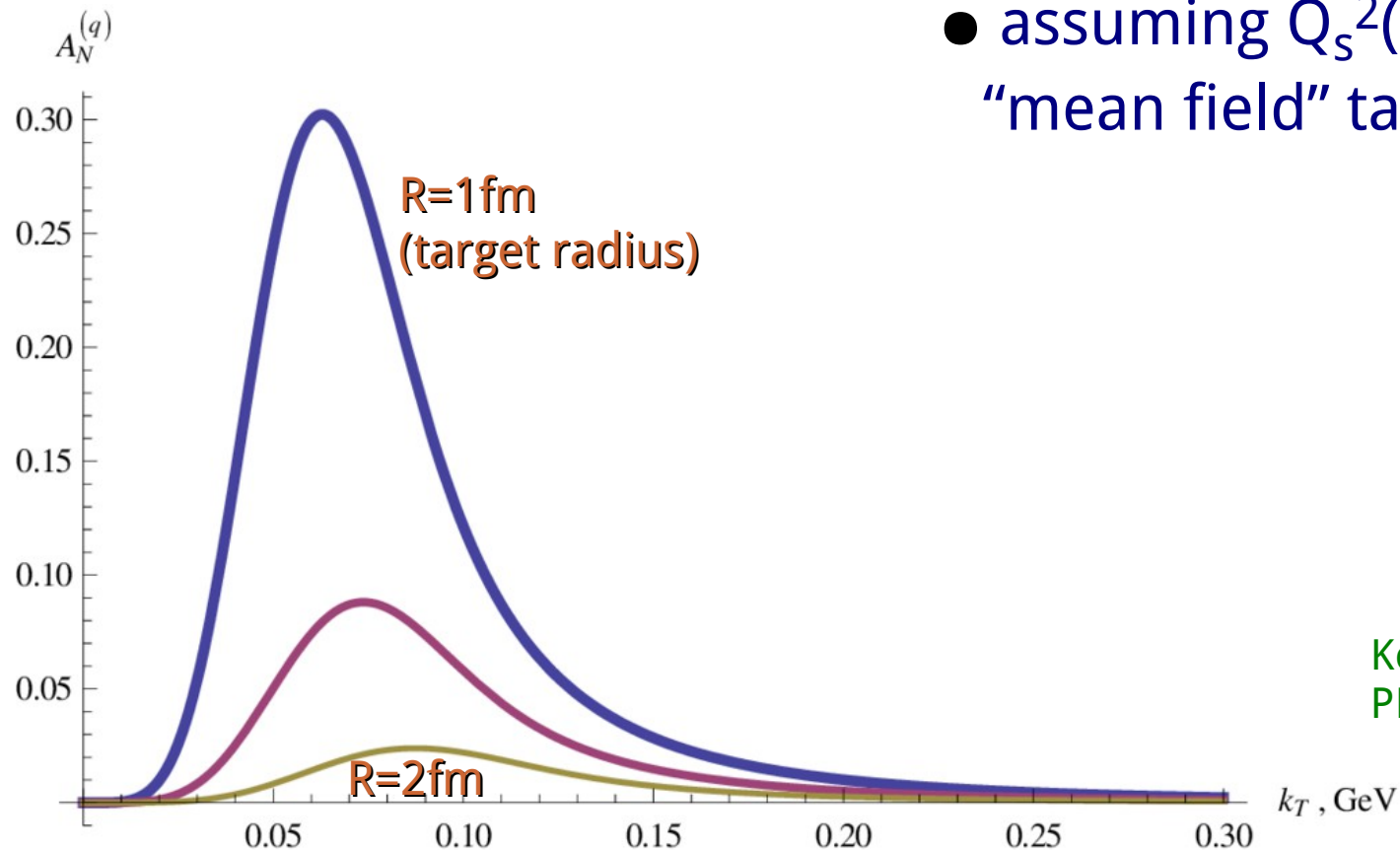
$$\sim \frac{1}{\kappa_3} A \sim A^{1/3}$$

# Single transverse spin asymmetry in pA

In quasi-classical approximation:

$$iO(\vec{r}, \vec{b}) \sim i\alpha_s \vec{r} \cdot \vec{\nabla}_b D(\vec{r}, \vec{b})$$

$$D(\vec{r}, \vec{b}) = e^{-\frac{1}{4}r^2 Q_s^2(b) \log \frac{1}{r\Lambda}}$$



# semi-cl. odderon cont'd

Target fluctuations (single mode):

$$\frac{Q_s^2(\vec{s})}{Q_s^2} = 1 + \int \frac{d^2q}{(2\pi)^2} \delta f(\vec{q}) e^{i\vec{q}\cdot\vec{s}}$$

$$\delta f(\vec{q}) = \frac{(2\pi)^2}{2} \mathcal{B}(q_0) [(1+i)\delta(\vec{q} - \vec{q}_0) + (1-i)\delta(\vec{q} + \vec{q}_0)]$$

→

$$iO(\vec{r}) \sim \frac{i}{2} \alpha_s r^2 Q_s^2 \mathcal{B}(q_0) \sin\left(\frac{1}{2} r q_0 \cos \phi_r\right) \log \frac{1}{\Lambda r} e^{-\frac{1}{4} r^2 Q_s^2 \log \frac{1}{\Lambda r}}$$

high  $k_T$  / small  $r$  :

$$\frac{dN}{d^2k_T} \sim \mathcal{B}(q_0) \left(\frac{q_0}{k_T}\right) \frac{Q_s^2}{k_T^4} \cos(\phi_k)$$

- $V_1 \neq 0$

- $V_3 = 0$

## semi-cl. odderon cont'd

for  $v_3 \neq 0$  we need a "string" (analogous to AdS/CFT calculation):

$$iO(\vec{r}) \sim i\alpha_s \vec{r} \cdot \vec{\nabla}_b D(\vec{r}, \vec{b}) \rightarrow i\alpha_s \int_{\vec{y}}^{\vec{x}} d\vec{s} \cdot \vec{\nabla}_s D(\vec{r}, \vec{s})$$

$r = x - y$  ,  $\vec{b} = \frac{\vec{x} + \vec{y}}{2}$

Target fluctuations ( $dq_0/q_0$  spectrum with exp. cutoff):

$$\frac{Q_s^2(\vec{s})}{Q_s^2} = 1 + \int \frac{d^2q}{(2\pi)^2} \delta f(\vec{q}) e^{i\vec{q} \cdot \vec{s}}$$

$$\delta f(\vec{q}) = \frac{(2\pi)^2}{2} \mathcal{B} \int \frac{dq_0^2}{q_0^2} e^{-q_0/Q_c} [(1+i)\delta(\vec{q} - \vec{q}_0) + (1-i)\delta(\vec{q} + \vec{q}_0)]$$

$$iO(\vec{r}) \sim i\alpha_s r^2 Q_s^2 \mathcal{B} \arctan\left(\frac{1}{2} r Q_c \cos \phi_r\right) D(\vec{r}) \log \frac{1}{r\Lambda}$$

all  $v_{2n+1}$ , awesome...



Expansion for  $1/r \gg Q_s, Q_c$  :

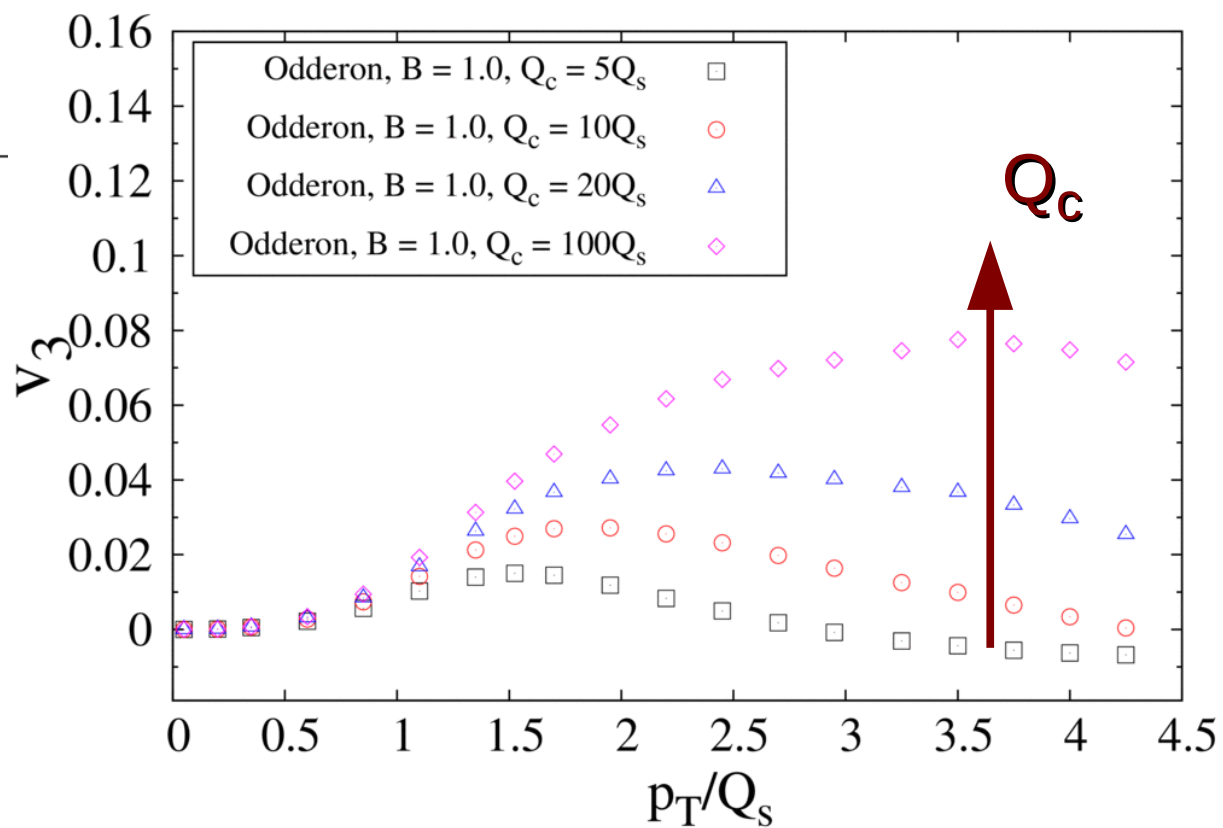
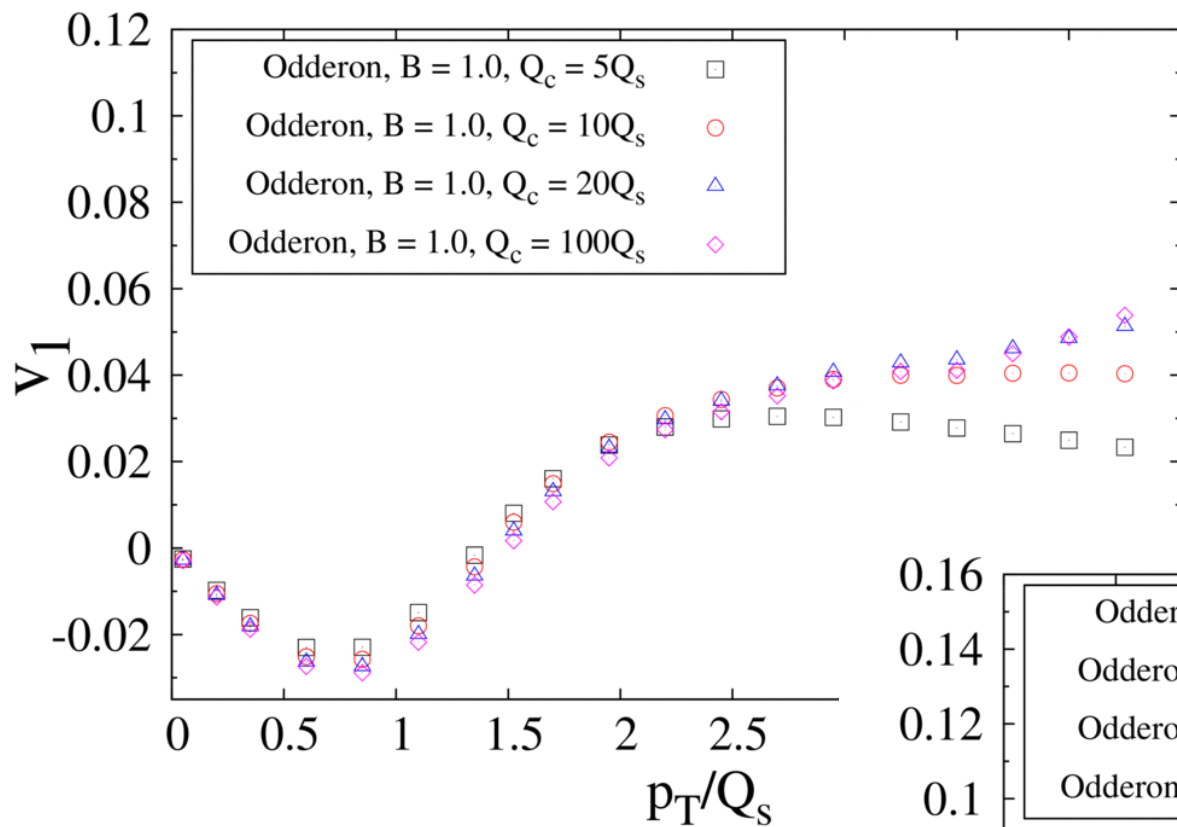
$$iO(\vec{r}) \sim r^3 Q_c \cos \phi_r \left[ 1 - \frac{r^2}{4} \left( Q_s^2 \log \frac{1}{r} + \frac{1}{3} Q_c^2 \cos^2 \phi_r \right) \right]$$

● isotr.:  $\sim r^2 \rightarrow 1/k_T^4$

●  $v_1$ :  $\sim r^3 \rightarrow 1/k_T^5$

●  $v_3$ :  $\sim r^5 \rightarrow 1/k_T^7$

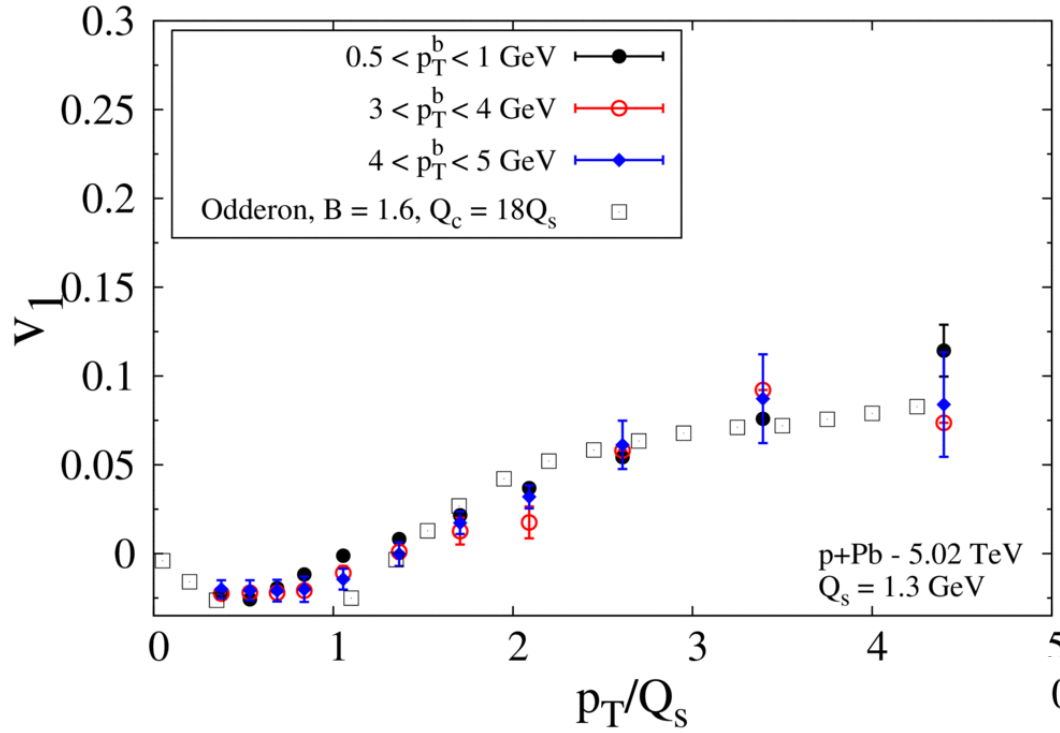
# Numerical F.T. of $O(r)$ : behavior of cutoff $Q_c$



- $v_1$  affected only at high  $p_T$
- low  $Q_c$  kills  $v_3$ :

$$\int d\vec{s} \cdot \vec{\nabla}_s Q_s^2 \rightarrow \vec{r} \cdot \vec{\nabla}_b Q_s^2$$

# Numerical F.T. of $O(r)$ : comparison to data; $v_1$ and $v_3$



- one fluctuation amplitude  $B=1.6$  fits  $v_1$  and  $v_3$  simultaneously
- large  $Q_c \sim 18 Q_s$  gives decent  $p_T$  dependence for both  $v_1$  and  $v_3$

