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Physics and Astronomy Department, Catania University

# ***ISOTROPIZATION OF QGP***

*Initial Stages 2014*

*December 5*

*Napa, CA*



# In this talk:

- Transport theory for heavy ion collisions
- ***Isotropization***
- Conclusions and Outlook

More in Plumari's talk

## *Catania Transport Group*

### Collaborators:

- *Vincenzo Greco*
- *Lucia Oliva*
- *Armando Puglisi*
- *Salvatore Plumari*
- *Francesco Scardina*



# Boltzmann equation and QGP

In order to *simulate* the temporal evolution of the fireball we solve the *Boltzmann equation* for the parton distribution function  $f$ :

$$\left\{ p^\mu \partial_\mu + \left[ p_\nu F^{\mu\nu} + m \partial^\mu m \right] \partial_{p_\mu} \right\} f(x, p) = C[f]$$



**Field interaction (EoS)**

**Collision integral**

**Collision integral:** change of  $f$  due to collision processes in the phase space volume centered at  $(\mathbf{x}, \mathbf{p})$ .

*Responsible for deviations from ideal hydro (non vanishing  $\eta/s$ ).*

*We map by  $C[f]$  the phase space evolution of a fluid which dissipates with a given value of  $\eta/s$ .*

One can expand  $C[f]$  over microscopic details ( $2 \leftrightarrow 2, 2 \leftrightarrow 3 \dots$ ), but in a hydro language this is irrelevant: **only the global dissipative effect of  $C[f]$  is important.**

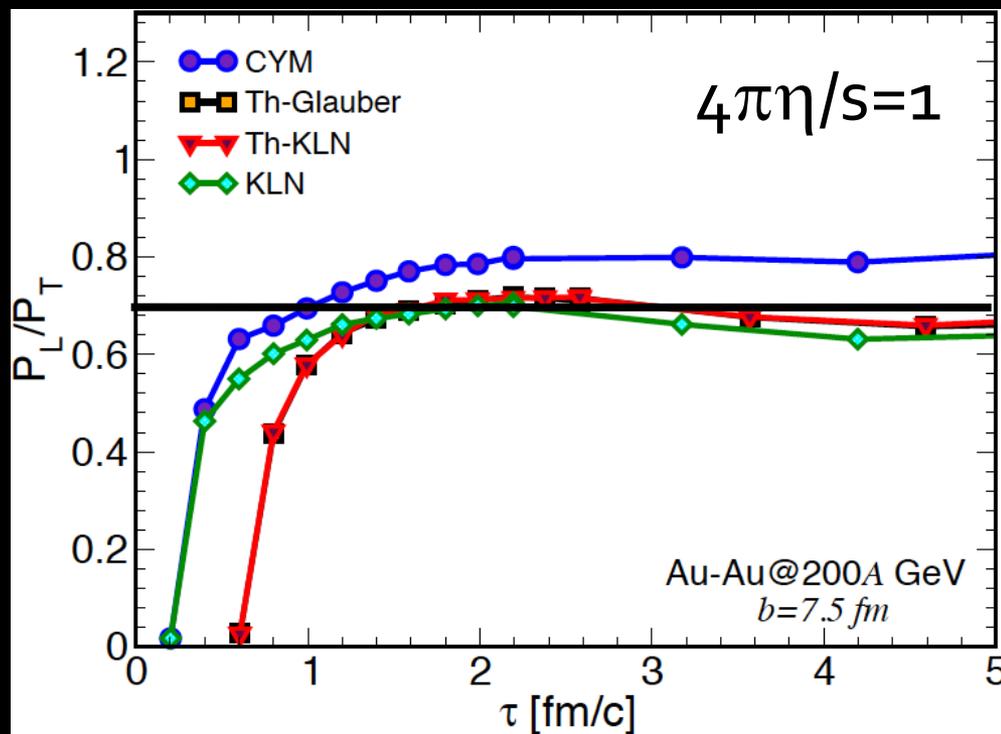
# Pressure isotropization

$$T^{\mu\nu} = \int \frac{d^3p}{(2\pi)^3} \frac{p^\mu p^\nu}{E} f(x, p)$$



$$P_L = T_{zz}, \quad P_T = \frac{T_{xx} + T_{yy}}{2}$$

*computed in the local rest frame*



CYM (IP-Glasma) spectrum:  
 Courtesy of B. Schenke & R. Venugopalan

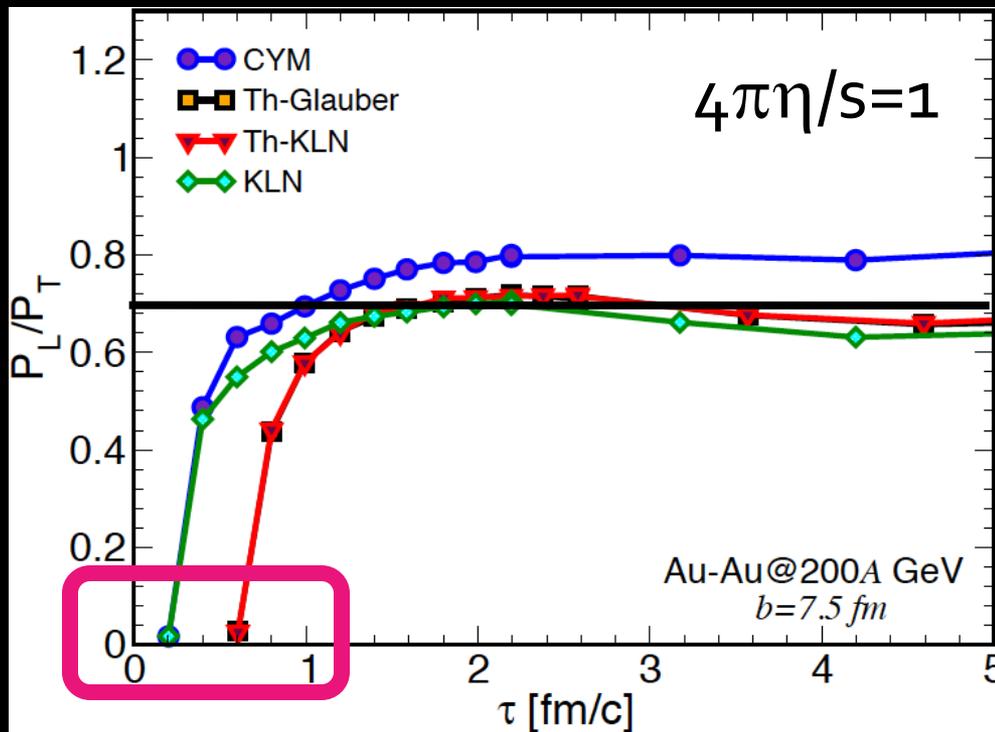
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*Initially  $P_L=0$ : the motion in the longitudinal direction is a pure flow*

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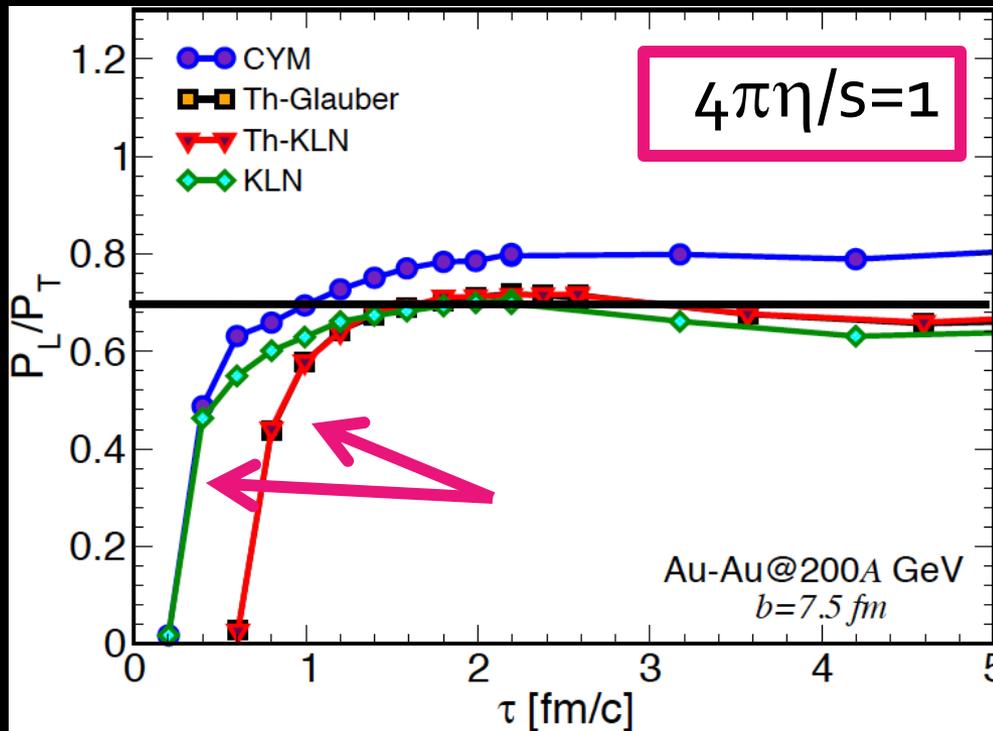
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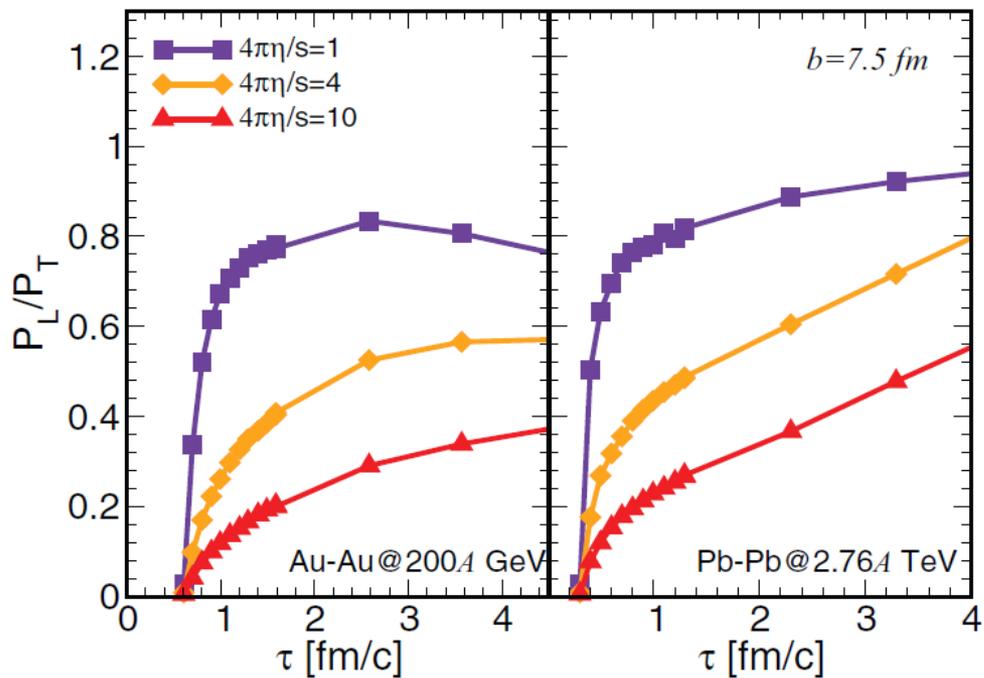
*Thanks to strong coupling, the system efficiently removes the anisotropy*

CYM (IP-Glasma) spectrum:  
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***Fast isotropization in strong coupling:  $\tau$  less than 1 fm/c***

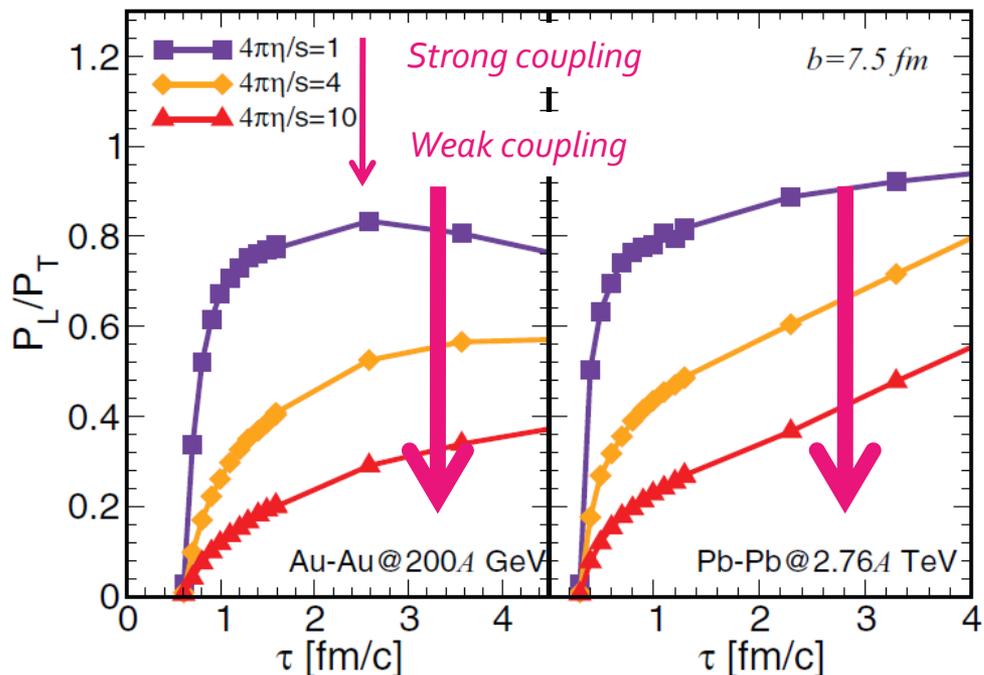
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## Role of the coupling strength



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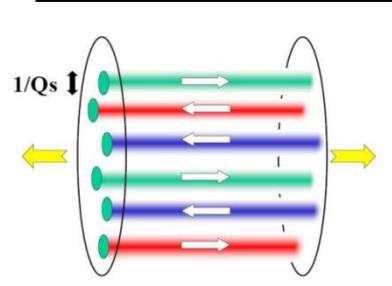


*With larger viscosities the system does not remove efficiently anisotropy*

- ✧ For  $\eta/s > 0.3$  one misses fast isotropization in  $P_L/P_T$  ( $\tau$  about 2-3 fm/c)
- ✧ For  $\eta/s \approx$  pQCD no isotropization

*These calculations ignore the initial fields dynamics, which instead plays a role in the initial stages.*

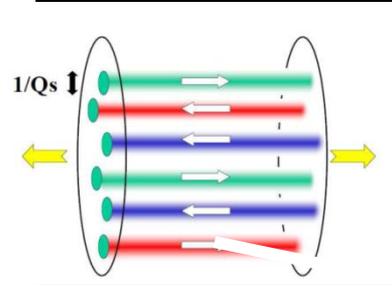
# Abelian Flux Tube



**Purpose:** understanding the role of the initial fields on isotropization and evolution of QGP

**Method:** implementing a simple model of initial field configuration, simpler to treat analytically/numerically than glasma

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## Abelian Flux Tube (AFT)

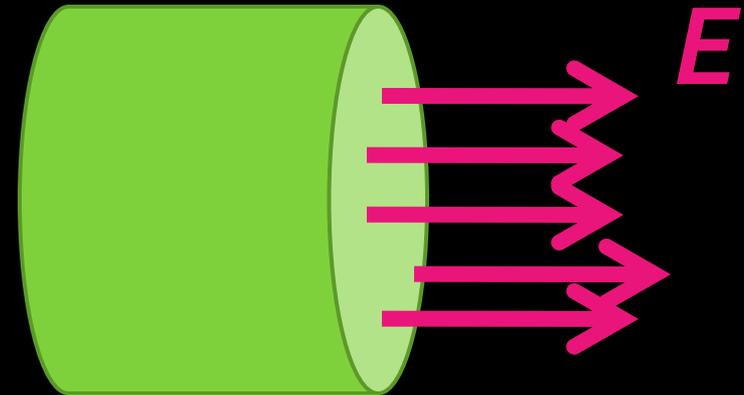
[Florkowski and Riblevsky., PRD 88 (2013)]

### Working assumptions

- ♠ Fields evolve according to abelian (i.e. Maxwell) equations
- ♠ No longitudinal (chromo-)magnetic field
- ♠ Flux tubes decay via Schwinger mechanism

### Further simplifications

- 🌀 Only 1-dimensional (longitudinal) expansion
- 🌀 Only gluons



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$$\partial_\mu F^{\mu\nu} = j_D^\mu + j_M^\mu$$



$$E_z(t) = E_z(0) - \int_0^t d\tau (j_D^z(\tau) + j_M^z(\tau))$$

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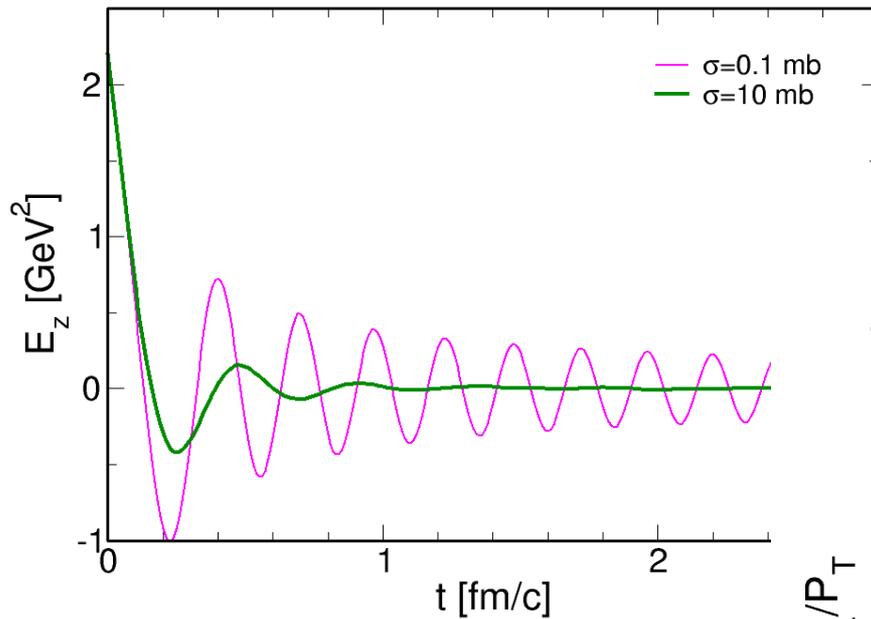
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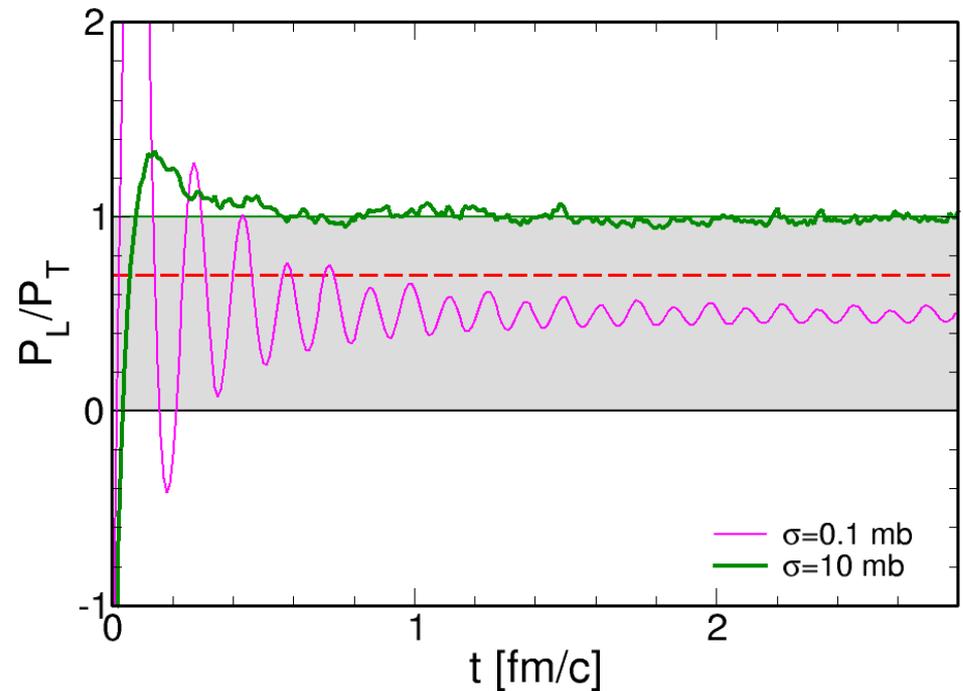
*$j_D$  e  $j_M$  depend on distribution function, hence link Maxwell and Boltzmann equations*

# Abelian Flux Tube

*Electric field for static box*



*Pressures for static box*

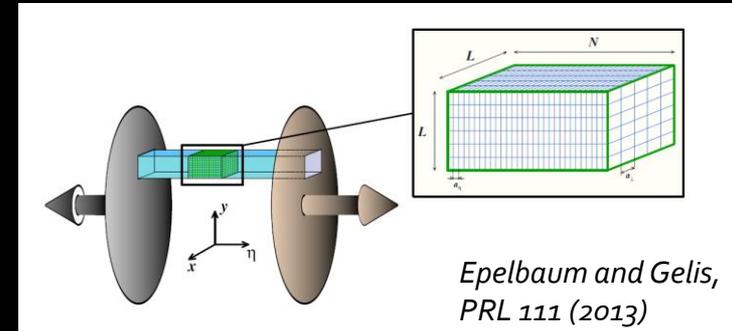
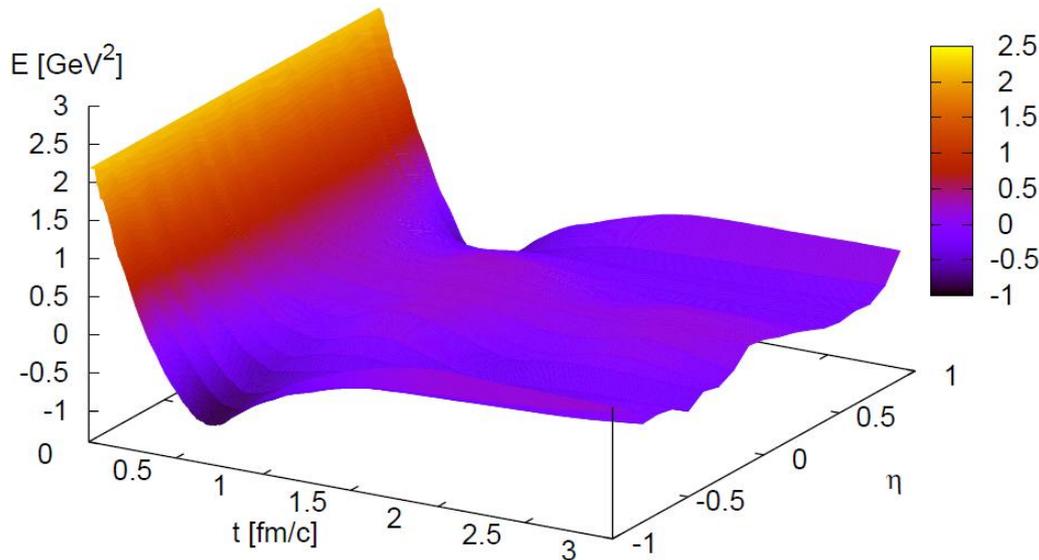


# Abelian Flux Tube

## Electric field for expanding geometry

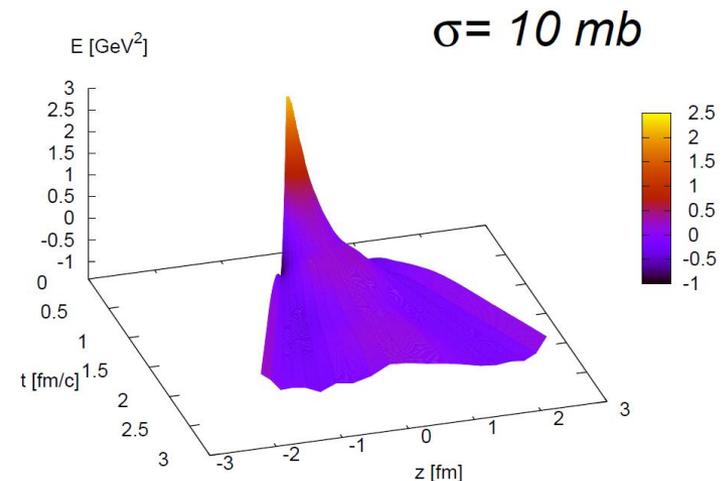
Strong coupling

$$\sigma = 10 \text{ mb}$$



Epelbaum and Gelis,  
PRL 111 (2013)

## Electric field for expanding geometry $t$ - $z$ space



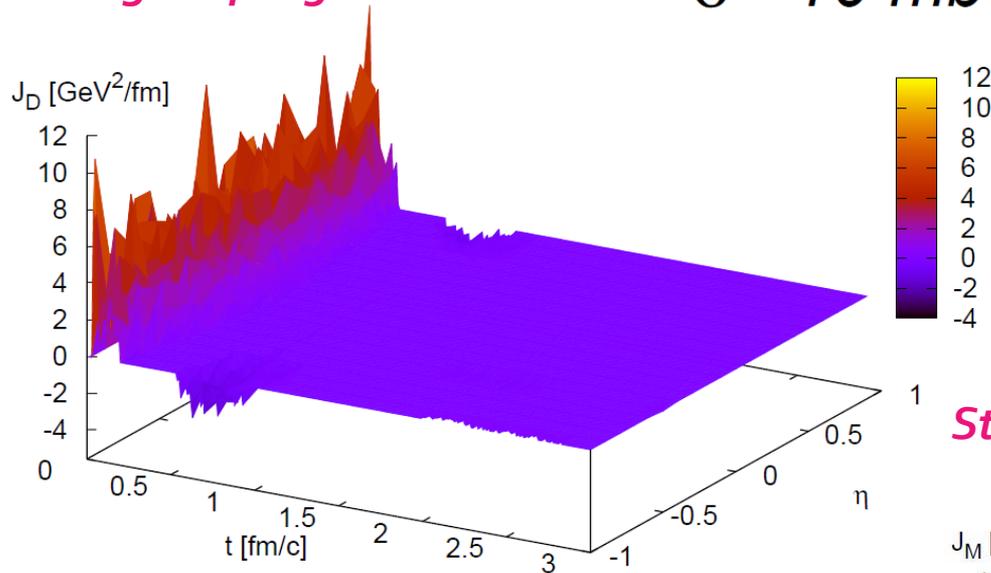
In strong coupling regime the electric field decays very quickly because currents are suppressed

# Abelian Flux Tube

## Polarization current

Strong coupling

$\sigma = 10 \text{ mb}$

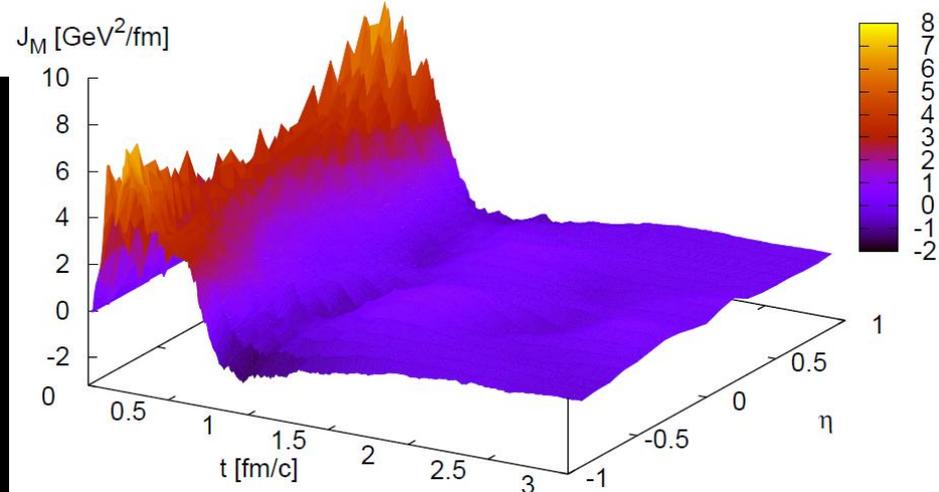


Fast decay of electric field allows pair creation just in a very short initial time range

## Electric current

Strong coupling

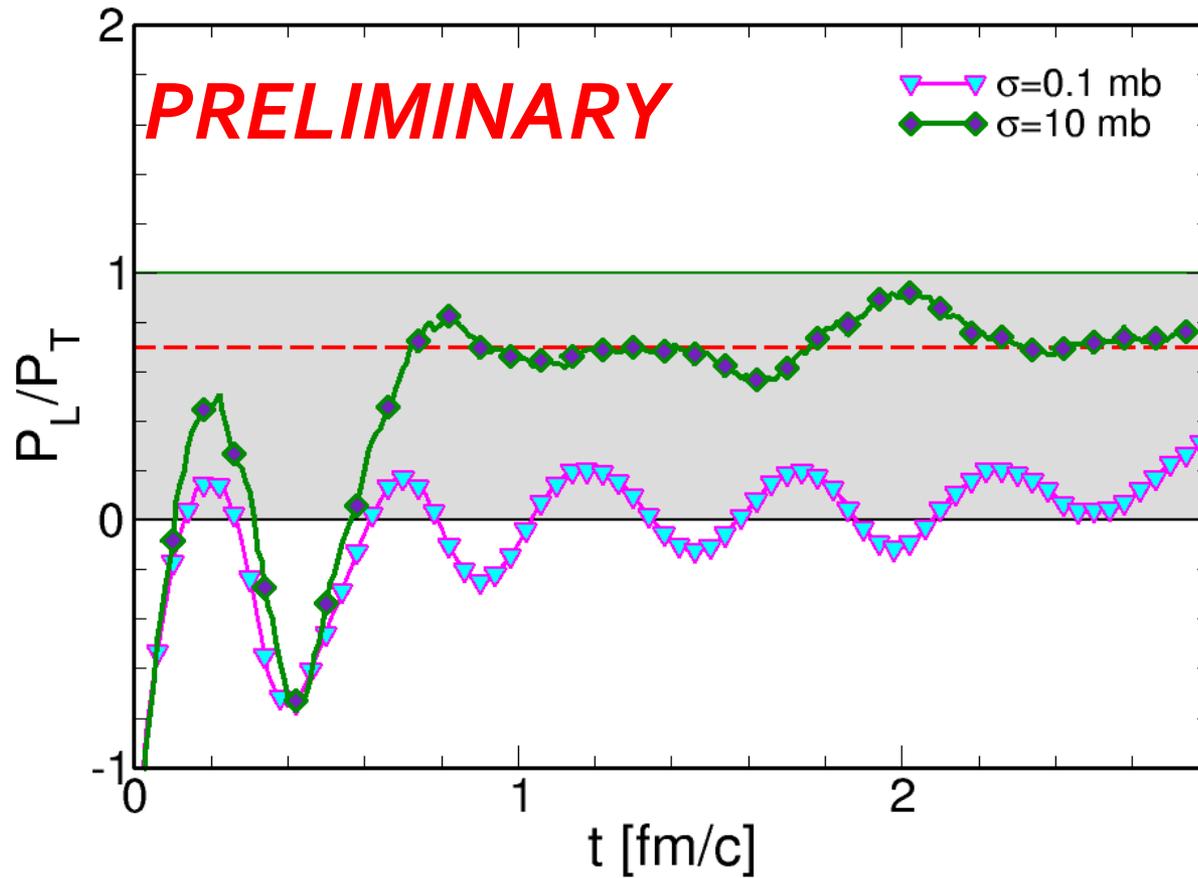
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Strong coupling favors momentum randomization, inhibiting electric current

# AFT isotropization

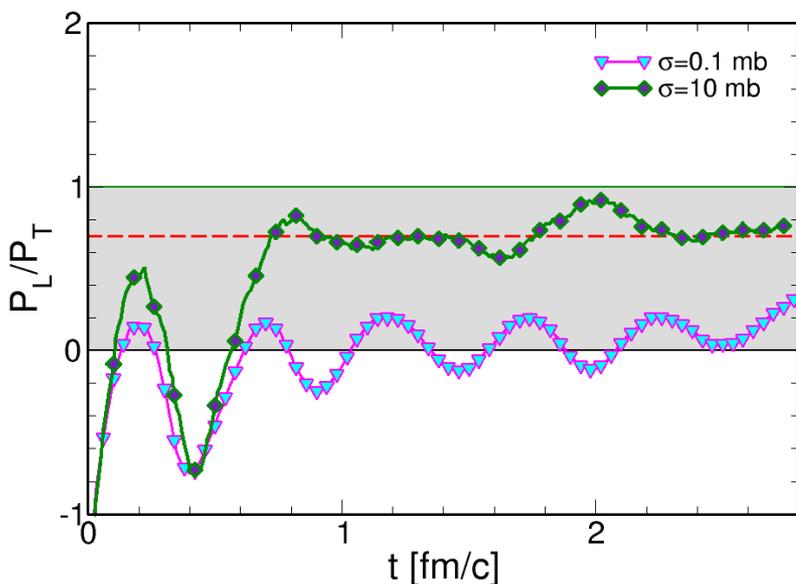
*Pressure isotropization for expanding geometry*



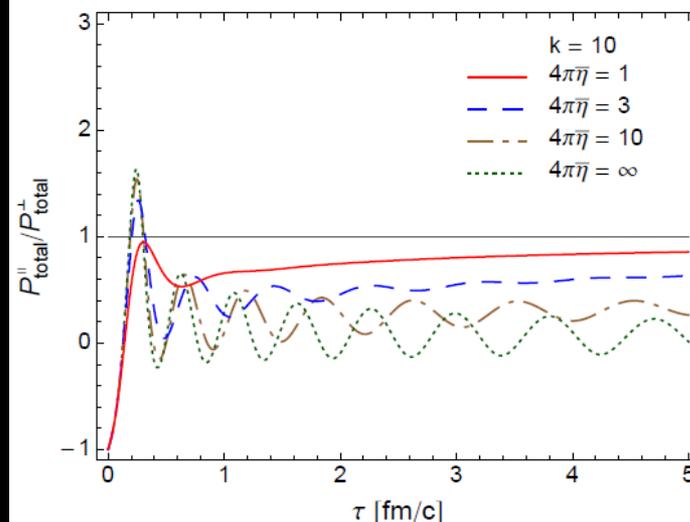
# AFT isotropization

*Qualitative agreement with previous calculations*

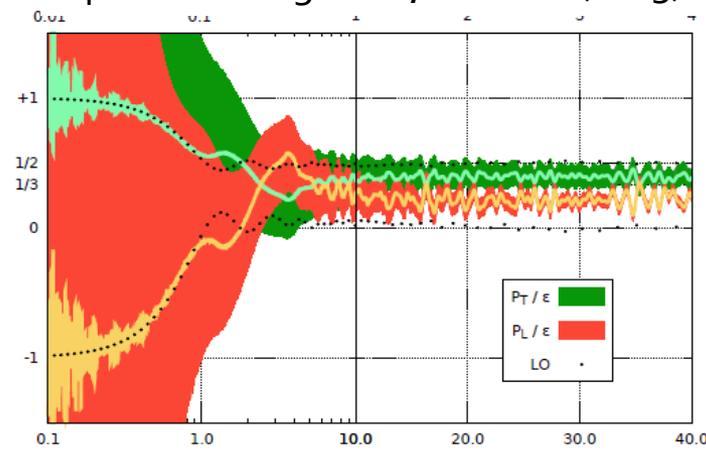
**PRELIMINARY**



Florkowski and Rivlebsky, PRD 88 (2013)



Epelbaum and Gelis, PRL 111 (2013)



# Conclusions and Outlook

- *Relativistic Kinetic Theory* permits to compute *isotropization efficiency* when initial field dynamics is included.
- *Include quarks and study particle production via flux tube decay*
- *Going beyond 1D expansion*



*Thanks for your attention*



*Good wood does not grow in comfort:  
the stronger the wind, the stronger the tree is.*

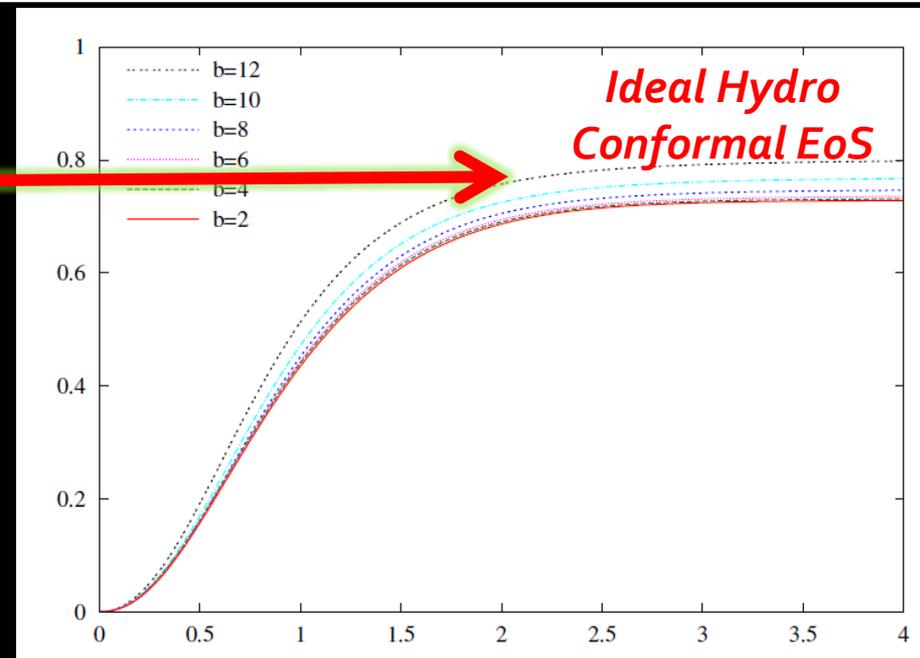
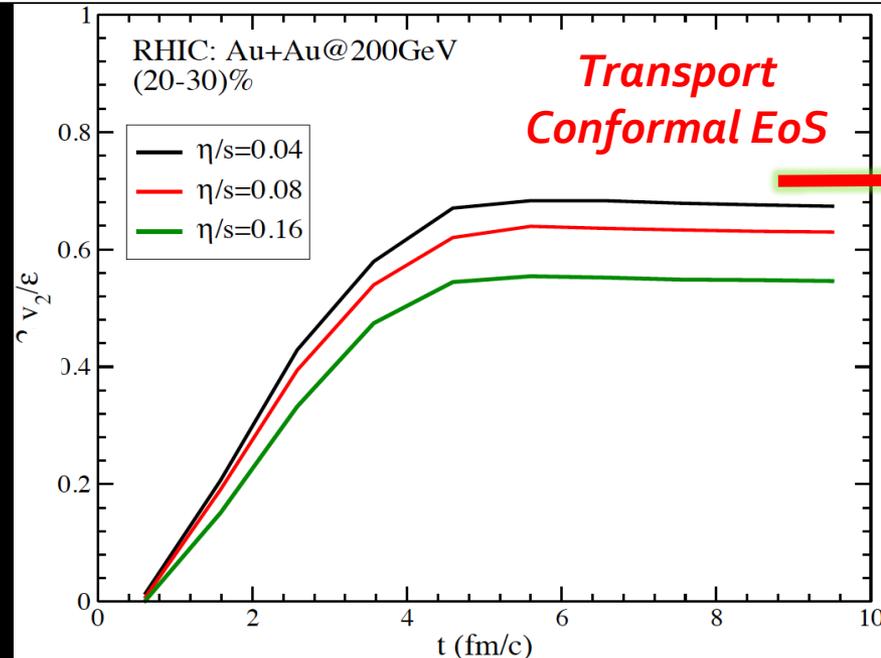


# Appendix

# Transport *gauged* to hydro

We use *Boltzmann equation* to simulate a fluid at *fixed  $\eta/s$*  rather than fixing a set of microscopic processes.

*Total Cross section* is computed in each configuration space cell according to *Chapman-Enskog equation* to give the *wished value of  $\eta/s$* .



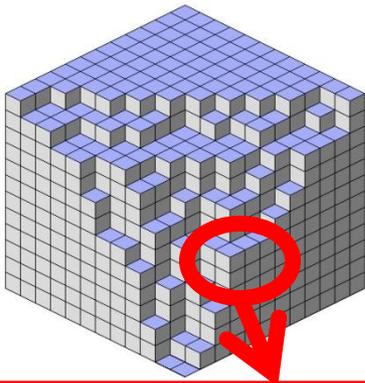
Bhalerao *et al.*, PLB627 (2005)

There is agreement of hydro with transport also in the **non dilute limit**

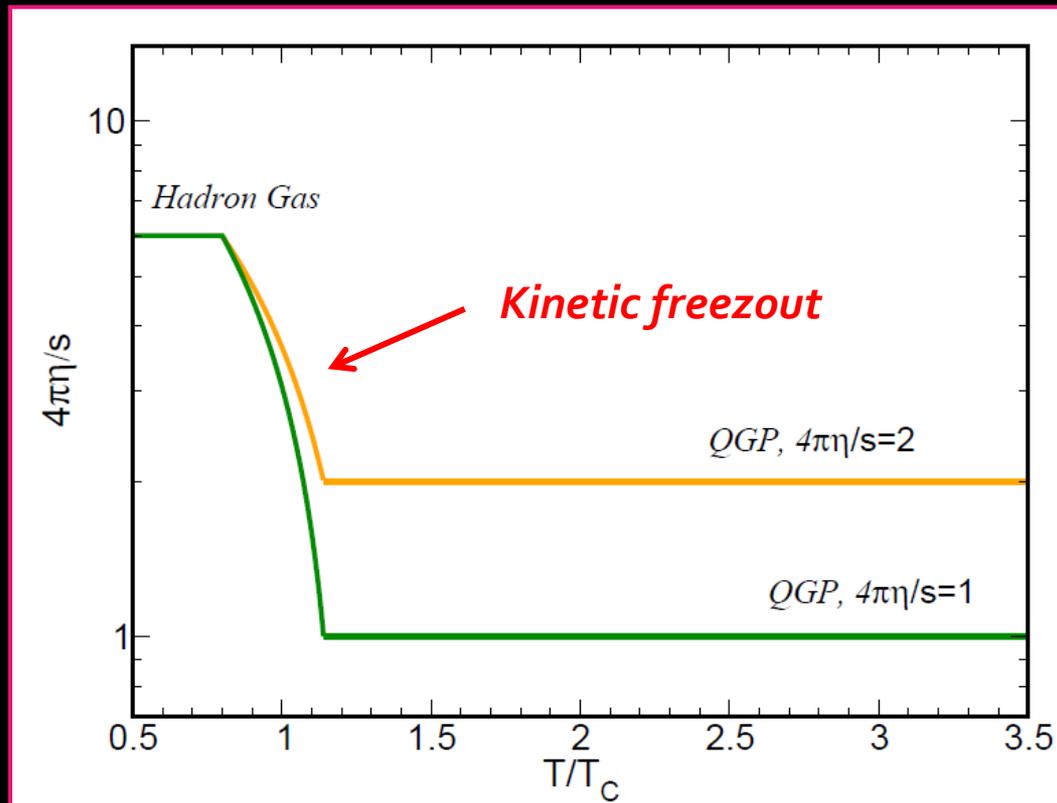
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$$\frac{\eta}{s} = \frac{\langle p \rangle}{g(m_D) \rho \sigma} \frac{1}{\sigma}$$

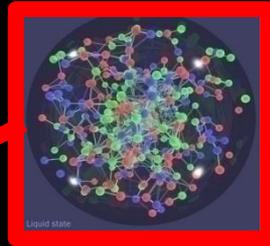
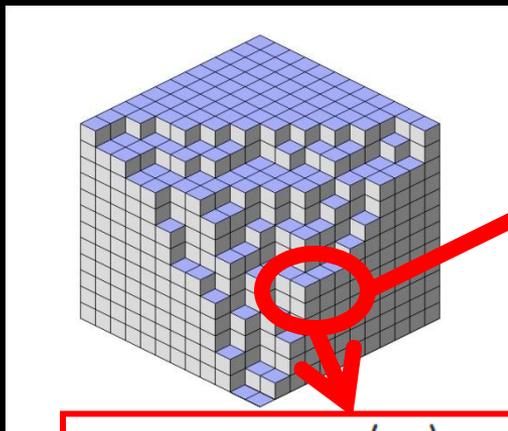


A *smooth kinetic freezout* is implemented in order to gradually reduce the strength of the interactions as the temperature decreases below the critical temperature.

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*Total Cross section* is *computed* in *each configuration space cell* according to *Chapman-Enskog equation* to give the *wished value of eta/s*.



(.) Collision integral is gauged in each cell to assure that the fluid dissipates according to the desired value of eta/s.

(.) Microscopic details are not important: the specific microscopic process producing eta/s is not relevant, only macroscopic quantities are, in analogy with hydrodynamics.

$$\frac{\eta}{s} = \frac{\langle p \rangle}{g(m_D)\rho\sigma} \frac{1}{\sigma}$$

## Transport

Description in terms of parton distribution function



## Hydro

Dynamical evolution governed by macroscopic quantities

# Why transport for uRHICs?

$$\left\{ p^\mu \partial_\mu + \left[ p_\nu F^{\mu\nu} + m \partial^\mu m \right] \partial_\mu^p \right\} f(x, p) = C[f]$$

- Starting from 1-body distribution function  $f(x, p)$  and not from  $T_{\mu\nu}$ :
  - Implement non-equilibrium implied by CGC-Qs scale (beyond  $\epsilon_x$ )
  - Include off-equilibrium at high and intermediate  $p_T$ :
    - Relevant at LHC due to large amount of minijet production*
  - freeze-out self-consistently related with  $\eta/s(T)$
- It's not an expansion in  $\eta/s$ :
  - valid also at high  $\eta/s \rightarrow$  LHC ( $T \gg T_c$ )
- Appropriate for heavy quark dynamics
- $f(x, p)$  and kinetic equations are useful to grasp informations about early glasma evolution

# AFT isotropization

