

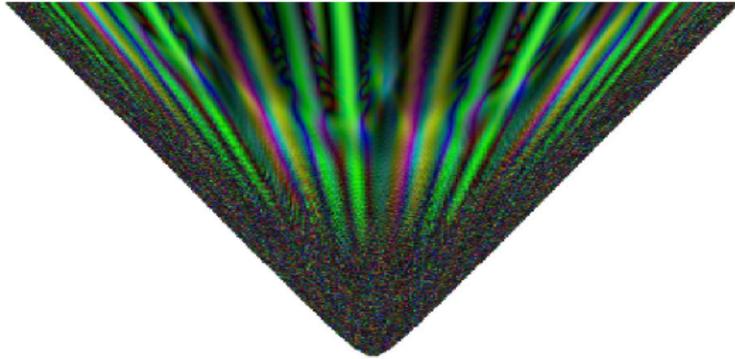
# Quantized fermions in semi-classical Yang-Mills evolution

Maximilian Attems

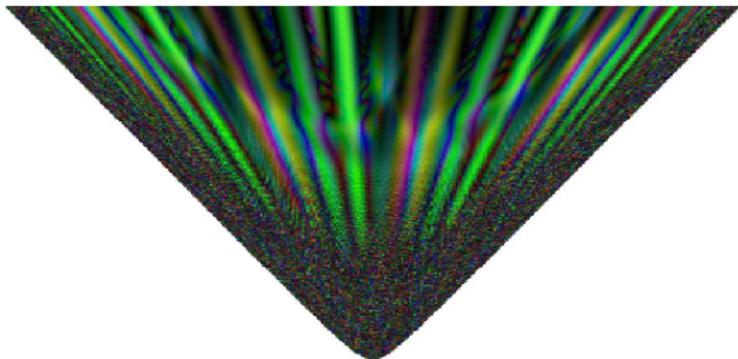
University of Barcelona

Collaborators: Owe Philipsen, Christian Schäfer

Initial State 2014



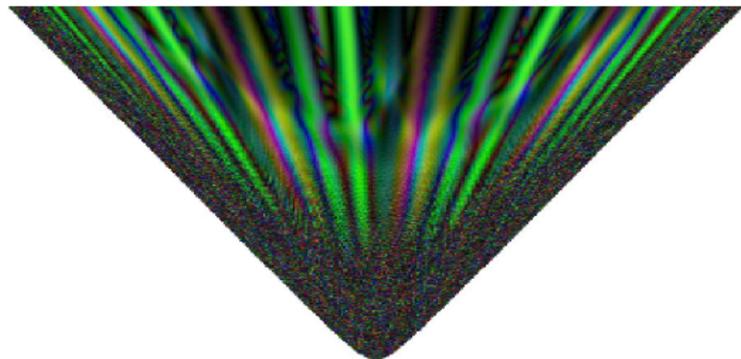
Visualization of Chromo-Weibel  
instabilities in Bjorken expansion  
[Attems, Rebhan, Strickland 09]



Visualization of Chromo-Weibel instabilities in Bjorken expansion  
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Weak coupling setup:

- CGC initial condition
- SU(3)
- Addition of fermionic degree of freedom



Visualization of Chromo-Weibel instabilities in Bjorken expansion  
[Attems, Rebhan, Strickland 09]

Weak coupling setup:

- CGC initial condition
- $SU(3)$
- Addition of fermionic degree of freedom

Ultimate goals:

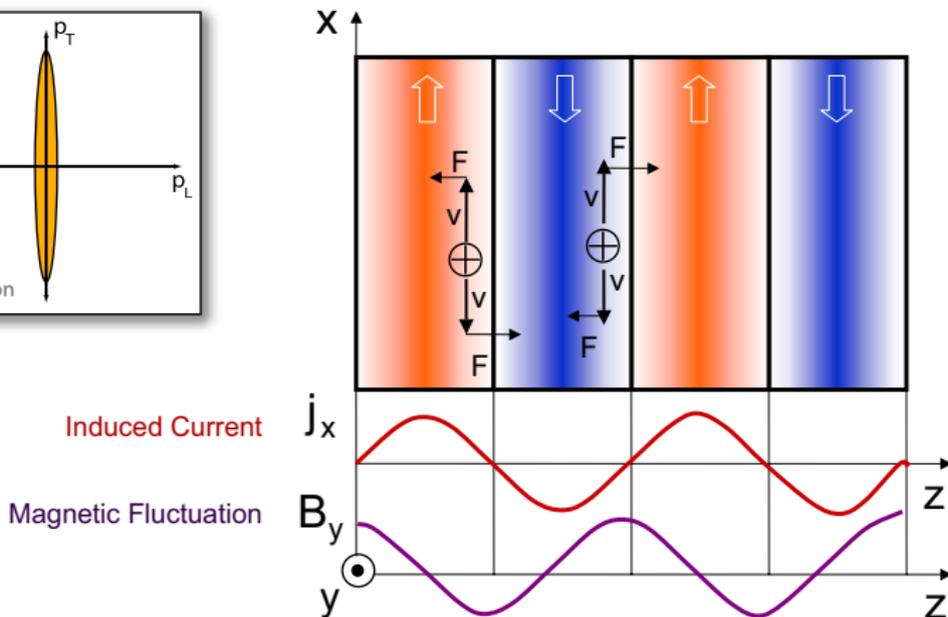
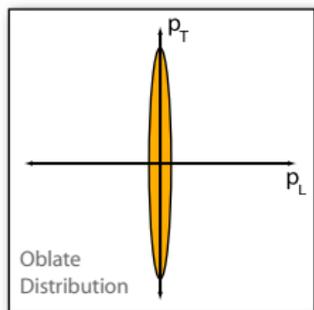
- Derivation of the thermalization time
- Hydrodynamization for both strongly and weakly coupled approaches

## 1 SU(3) Yang-Mills

- Weibel Instabilities
- Transverse thermalization
- Energy densities
- Pressures
- Chromo-Weibel Instabilities

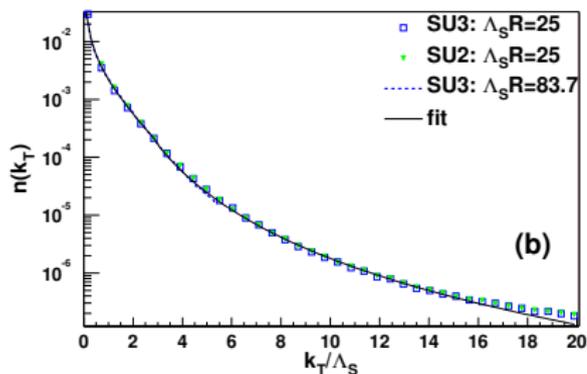
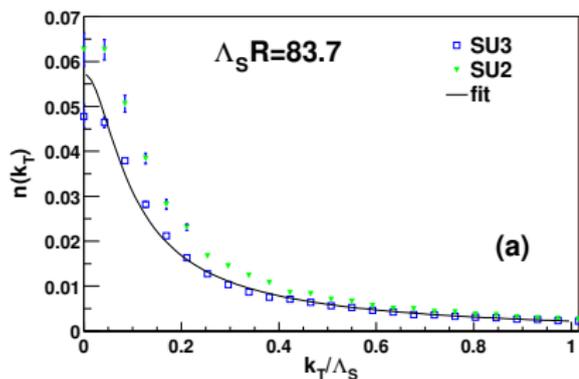
## 2 SU(3) Yang-Mills coupled to fermions

- Stochastic Fermions
- Energy densities
- Pressures



[Mrowczynski 1993; Strickland 2006]: Illustration of the mechanism of filamentation instabilities with Lorentz force.

# Transverse thermalization



CGC setup at time scales  $Q_S^{-1}$  [Krasnitz, Nara, Venugopalan 2001]

$$\mathcal{L}^G = \frac{1}{g^2 a^3} \text{Tr} \left( -\frac{1}{\xi} \sum (\mathbb{1} - U_{ij}(x)) + \xi \sum (\mathbb{1} - U_{i0}) \right)$$

USQCD lattice gauge software  
with SU(3) particle content:

$$E_i(x) = \partial_0 A_i$$

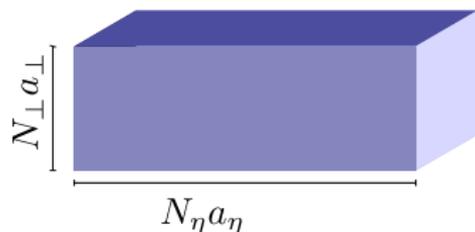
$$U_i(x) = e^{igaA_i(x)}$$

temporal gauge:

$$A_0(x) = 0, U_0(x) = 1$$

lattice size for leapfrog EOM:

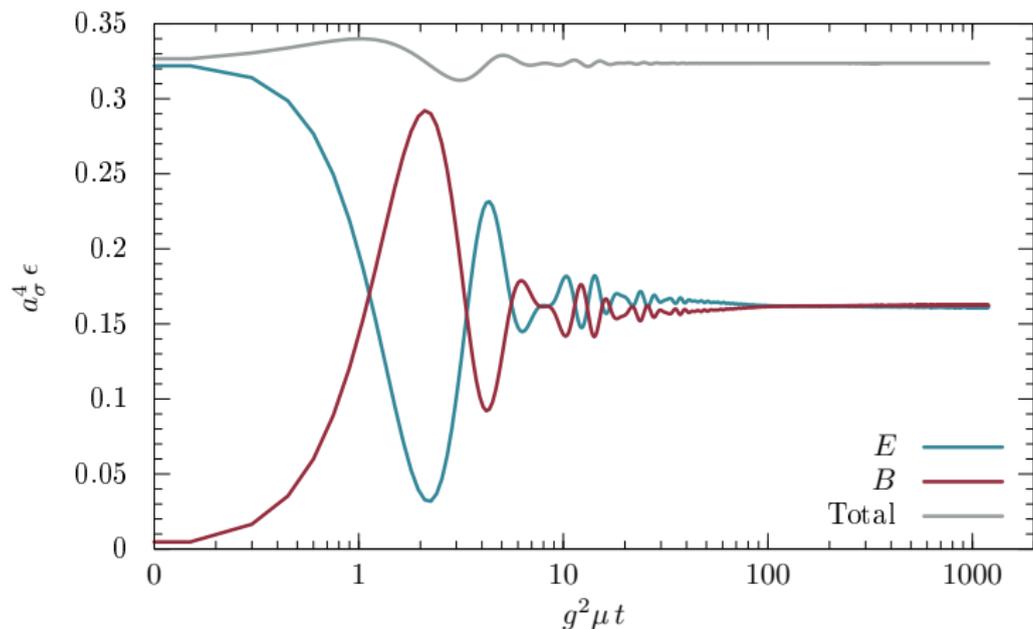
$$g^2 \mu \approx 2\text{GeV}, a_{\perp} = \frac{g^2 \mu^L}{2\text{GeV}}$$



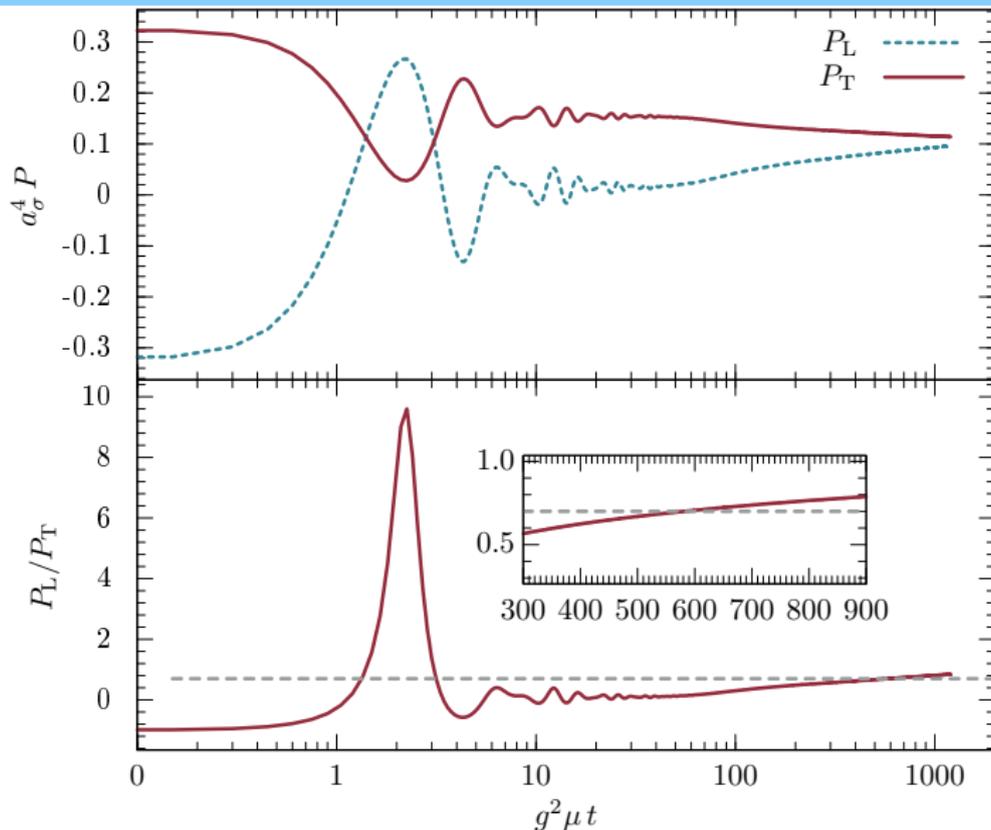
isotropic lattice length:

$$a_{\perp} = a_z$$

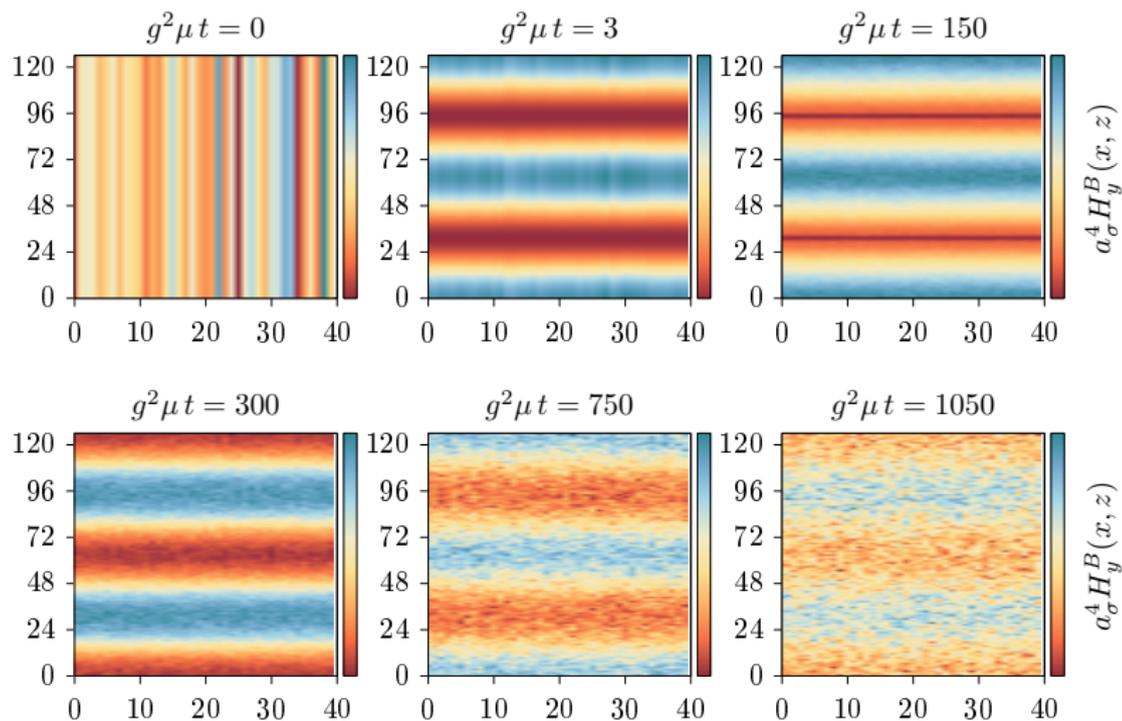
$$N_{\eta} \times N_{\perp}^2 = 128 \times 40^2$$

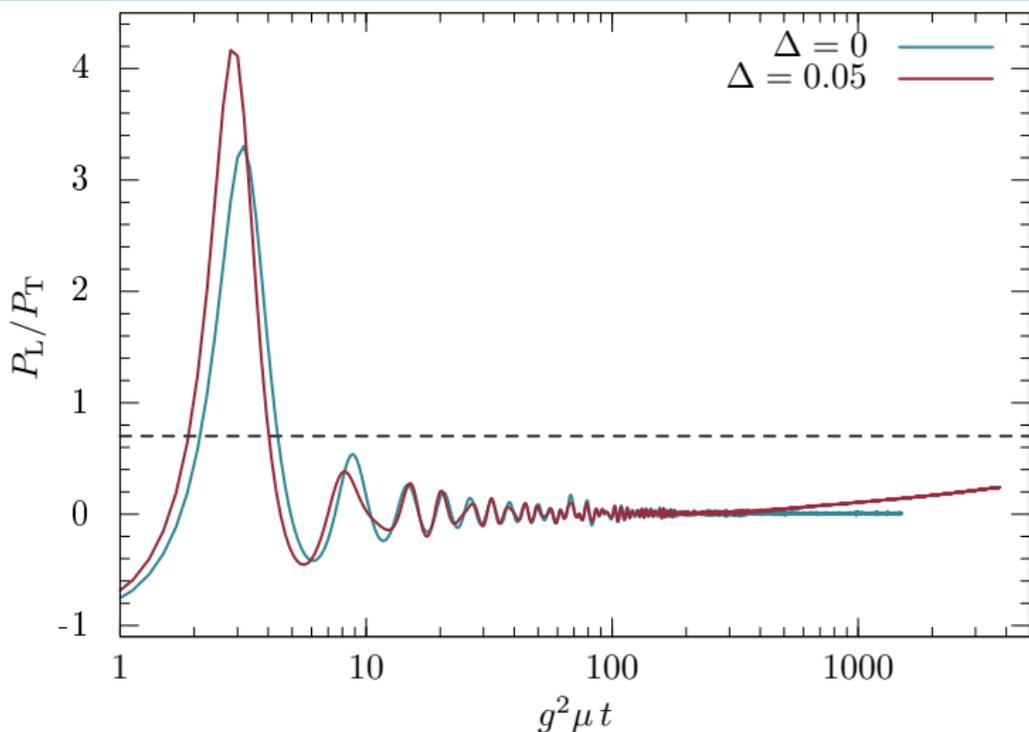


Chromo-electric and chromo-magnetic energy density evolution  
 [MA, Philipsen, Schäfer 2014]

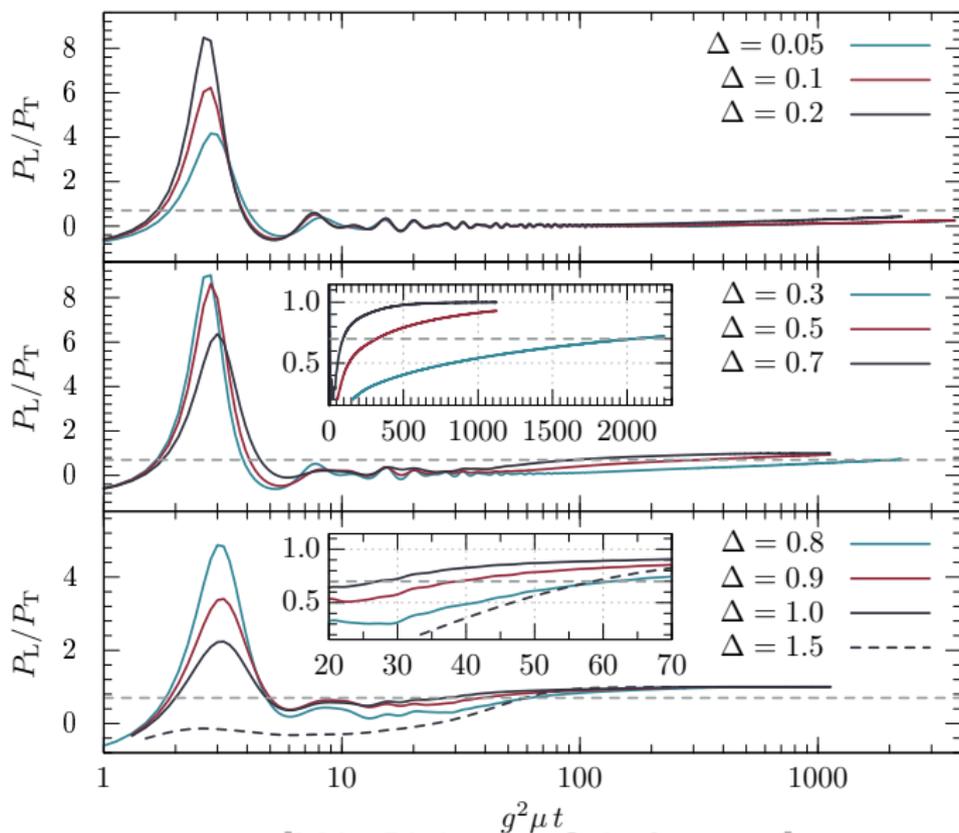


Pressures evolution [MA, Philipsen, Schäfer 2014]

Local  $B_y$  energy density evolution [MA, Philipsen, Schäfer 2014]



Pressures comparison [MA, Philipsen, Schäfer 2014]



Pressures comparison [MA, Philipsen, Schäfer 2014]

## 1 SU(3) Yang-Mills

- Weibel Instabilities
- Transverse thermalization
- Energy densities
- Pressures
- Chromo-Weibel Instabilities

## 2 SU(3) Yang-Mills coupled to fermions

- Stochastic Fermions
- Energy densities
- Pressures

- Quantum mechanical treatment via mode function expansion [Aarts, Smit 1998]
- Introduce two kinds of fermions: Male and female

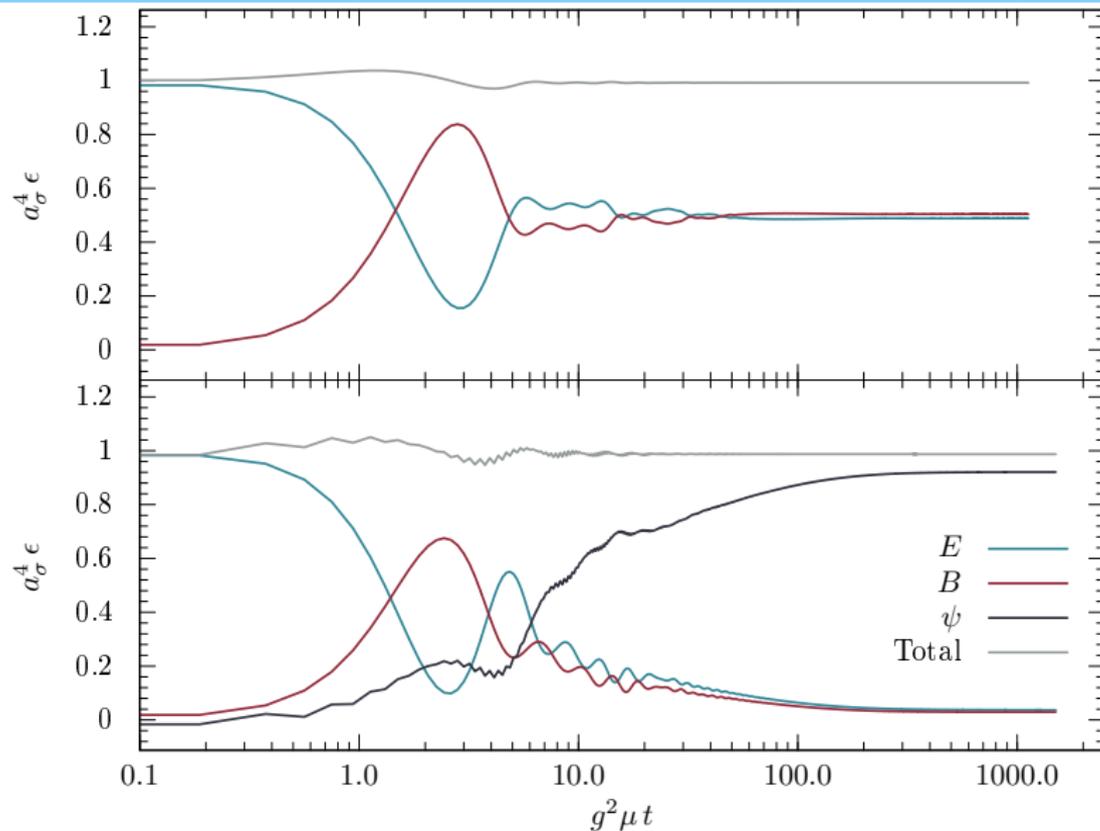
$$D(x, y) = \langle \psi_M(x) \bar{\psi}_F(y) \rangle = \langle \psi_F(x) \bar{\psi}_M(y) \rangle .$$

$$(i\gamma^\mu \partial_\mu - m + g\mathfrak{R}\Phi(x) - ig\mathfrak{S}\Phi(x)\gamma^5)\psi_g(x) = 0 .$$

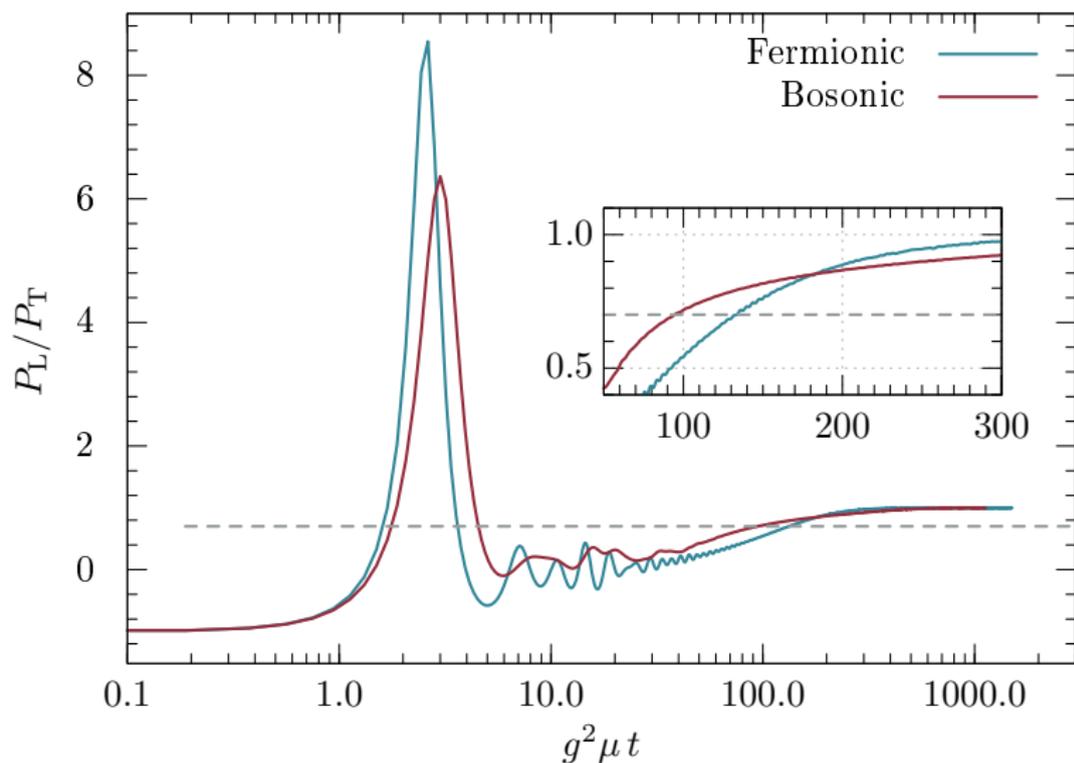
- Define Fourier transformed stochastic fields

$$\psi_g(\vec{p}) = \int_{\vec{x}} e^{ip_j x^j} \psi_g(\vec{x}), \quad \bar{\psi}_g(\vec{x}) = \int_{\vec{p}} e^{-ip_j x^j} \bar{\psi}_g(\vec{p}) . \quad (1)$$

- Simulate ladder operators with complex random numbers  $\xi$  and  $\eta$  [Borsanyi, Hindmarsh 2009]

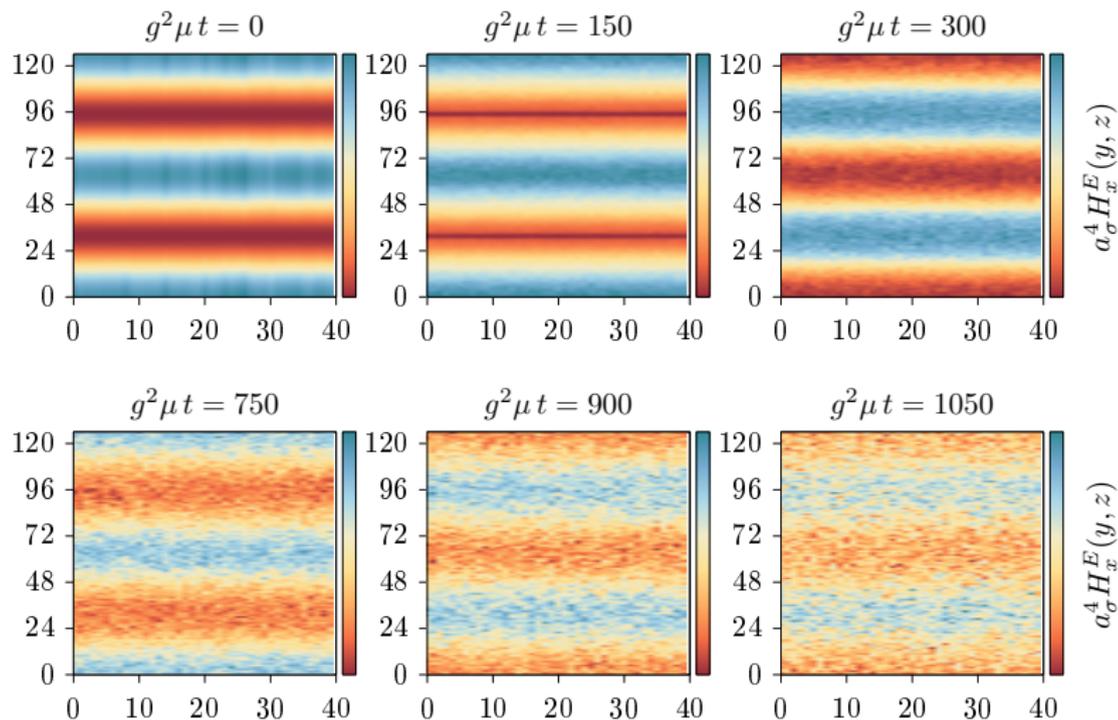


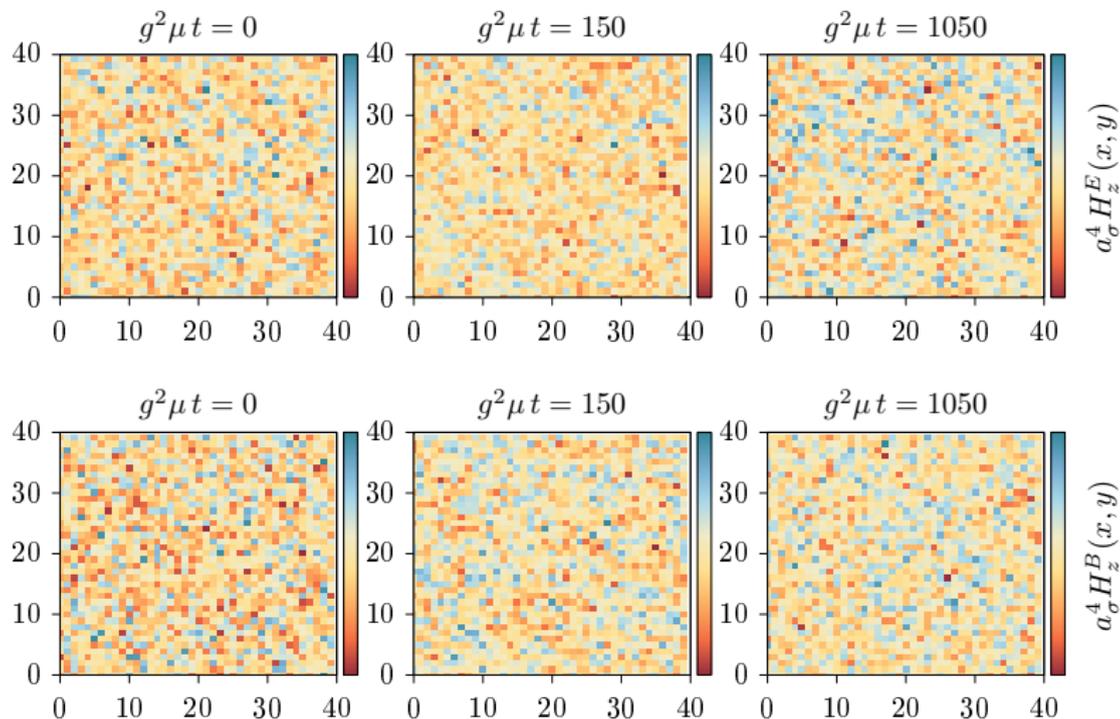
Quantized fermions [MA, Philipsen, Schäfer 2014]



Quantized fermions [MA, Philipsen, Schäfer 2014]

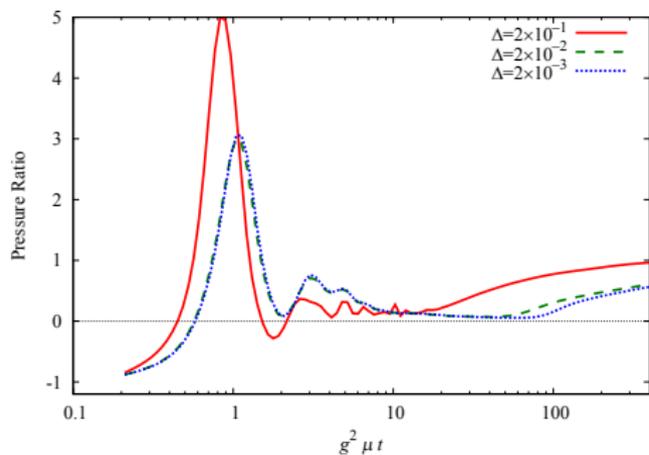
- In order to achieve an isotropisation time comparable with results from equivalent  $SU(2)$  simulations for  $SU(3)$  the fluctuation seed has to be increased from  $\Delta = 0.2$  to  $\Delta = 0.7$ .
- We found evidence for the emergence of the chromo-Weibel instability displayed by the filaments in the local energy densities.
- We investigated the effect of fermionic degrees of freedom on the isotropisation process: We observe a strong increase of fermionic energy density from the highly populated bosonic fields. This leads to a slight change of the isotropisation time.

Local  $E_x$  energy density evolution [MA, Philipsen, Schäfer 2014]

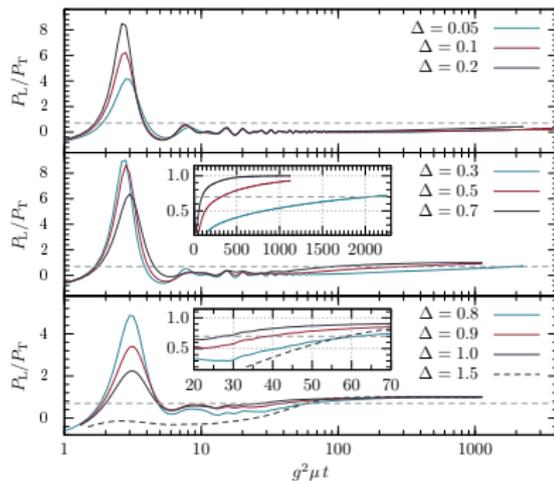


Local  $E$  and  $B$  energy density evolution in  $xy$  plane [MA,  
Philipsen, Schäfer 2014]

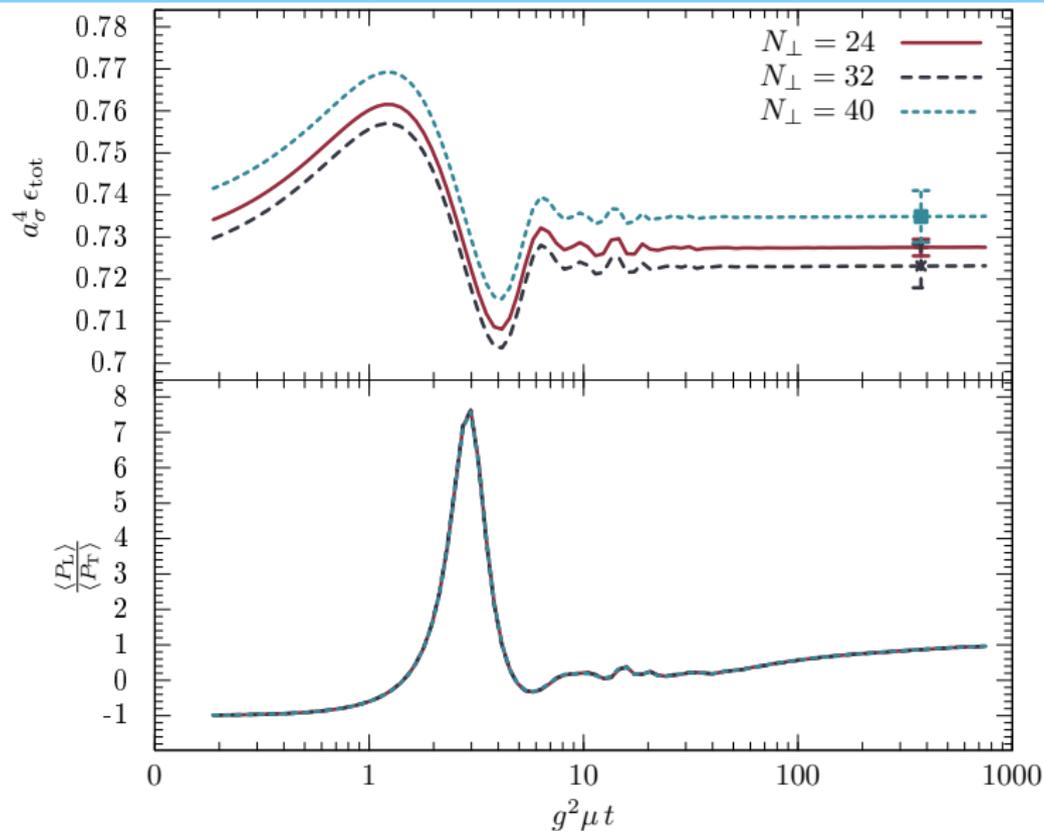
# SU(2) versus SU(3)



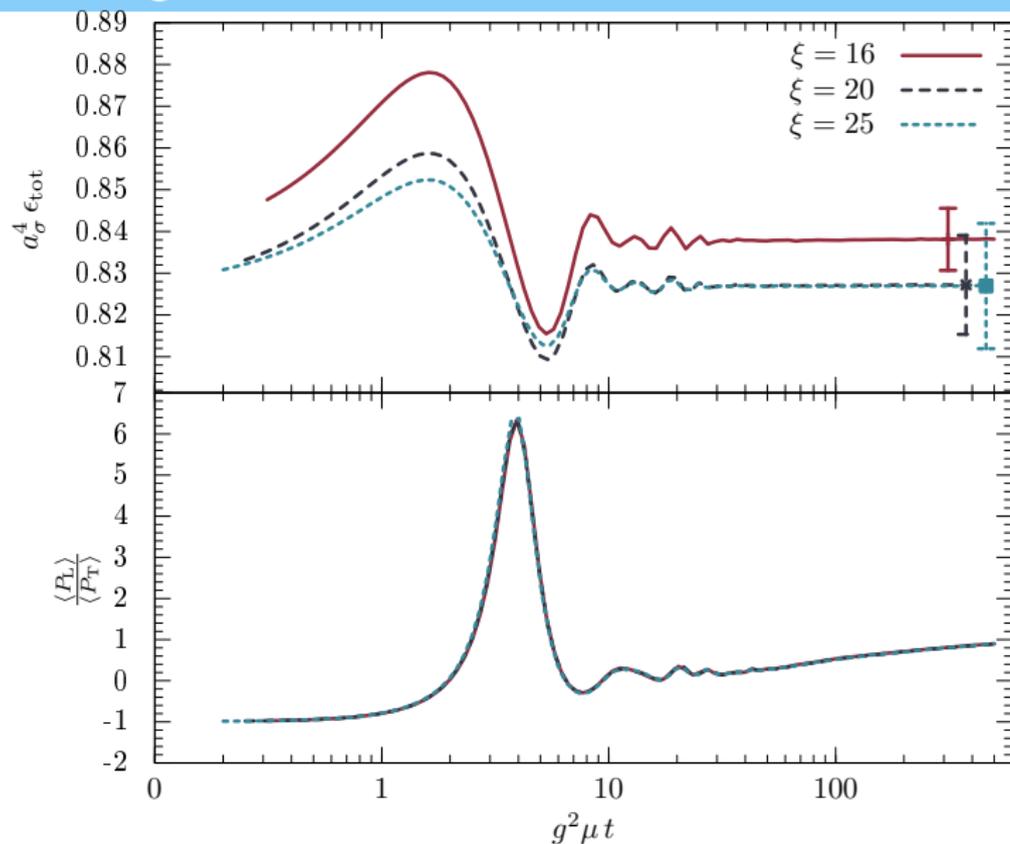
SU(2) [Fukushima 2013]



SU(3) [MA, Philipsen, Schäfer 2014]



Check for volume effects [MA, Philipsen, Schäfer 2014]



Check for anisotropy effects [MA, Philipsen, Schäfer 2014]