

Calibration of Fourier domain short coherence interferometer for absolute distance measurements



Risto Montonen^{1,2}, Ivan Kassamakov^{1,2},
Edward Hæggström², and Kenneth Österberg^{1,2}

¹ Helsinki Institute of Physics, University of Helsinki

² Department of Physics, University of Helsinki

5 mm

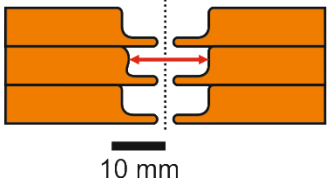
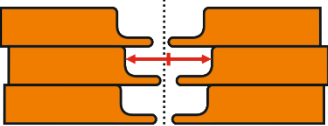
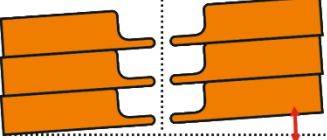
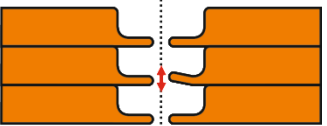




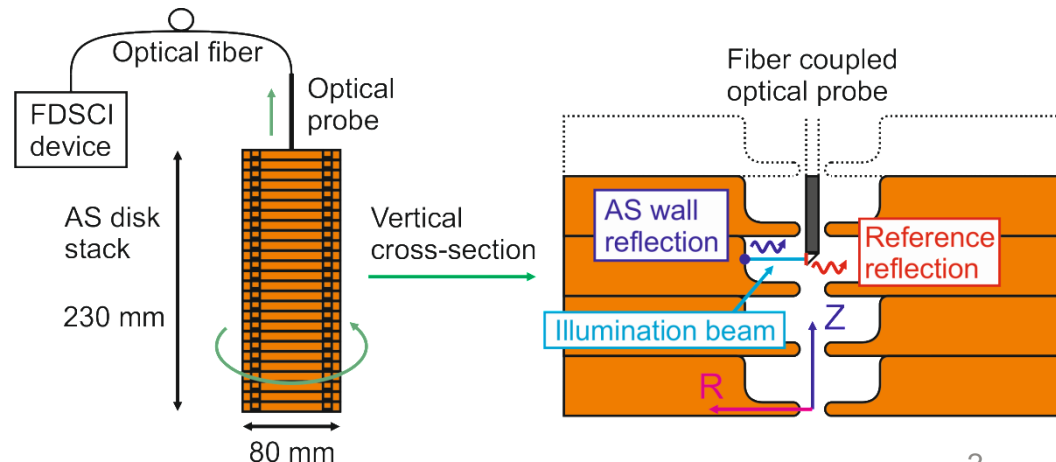
Introduction



- Accelerating Structures (AS) comprising OFE Cu disks undergo permanent thermo-mechanical deformations during assembly and RF operation.
- These deformations result in micron-level shape errors in AS.

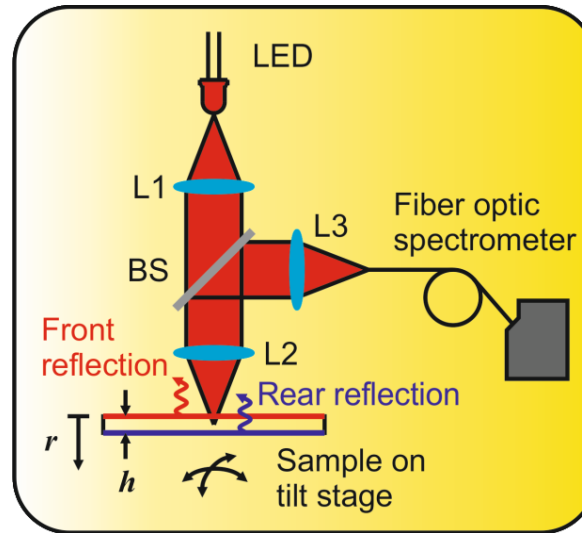
Shape error	Error in iris shape	Transversal offset	Tilt	Iris deformation
				
Tolerance	1 μm	5 μm	140 μrad	

- Sub-micron accuracy across 10 mm measurement range is required.
- Fourier Domain Short Coherence Interferometry (FDSCI) -technique





Design A Setup



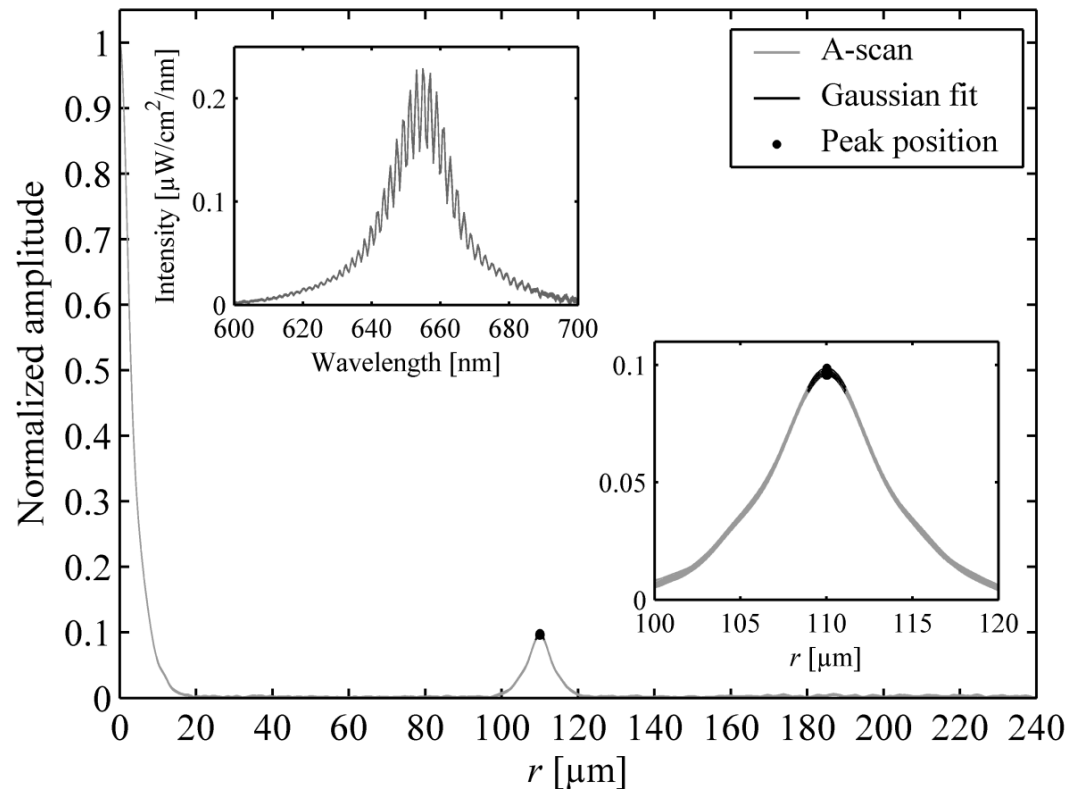
- Design A aims to verify micron accuracy of FDSCI method.
- LED light source (L-793SRC-E, Kingbright, $\lambda_0 = 655 \text{ nm}$, $\Delta\lambda = 22 \text{ nm}$)
- Visible range fiber optic spectrometer (HR2000, Ocean Optics, spectral resolution $\delta\lambda = 0.44 \text{ nm}$) captures a spectral interferogram.

$$\text{Measurement range } R_{max} = \frac{\lambda_0^2}{4n_{air}\delta\lambda}$$

- Expect $240 \text{ }\mu\text{m}$ measurement range R_{max} .



A-scan analysis



- Optical thickness (h) of the sample determined as the peak position of a Gaussian fit to the interference peak.
- In 100 A-scans, the repeatability better than $0.2 \mu\text{m}$ (2σ standard uncertainty)
- Axial resolution $0.002 \mu\text{m}$

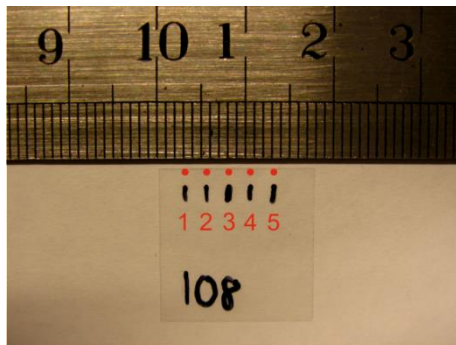


Calibration



- FDSCI setup calibrated by comparing the optical thickness of five individual calibration samples to the certified geometric thickness.

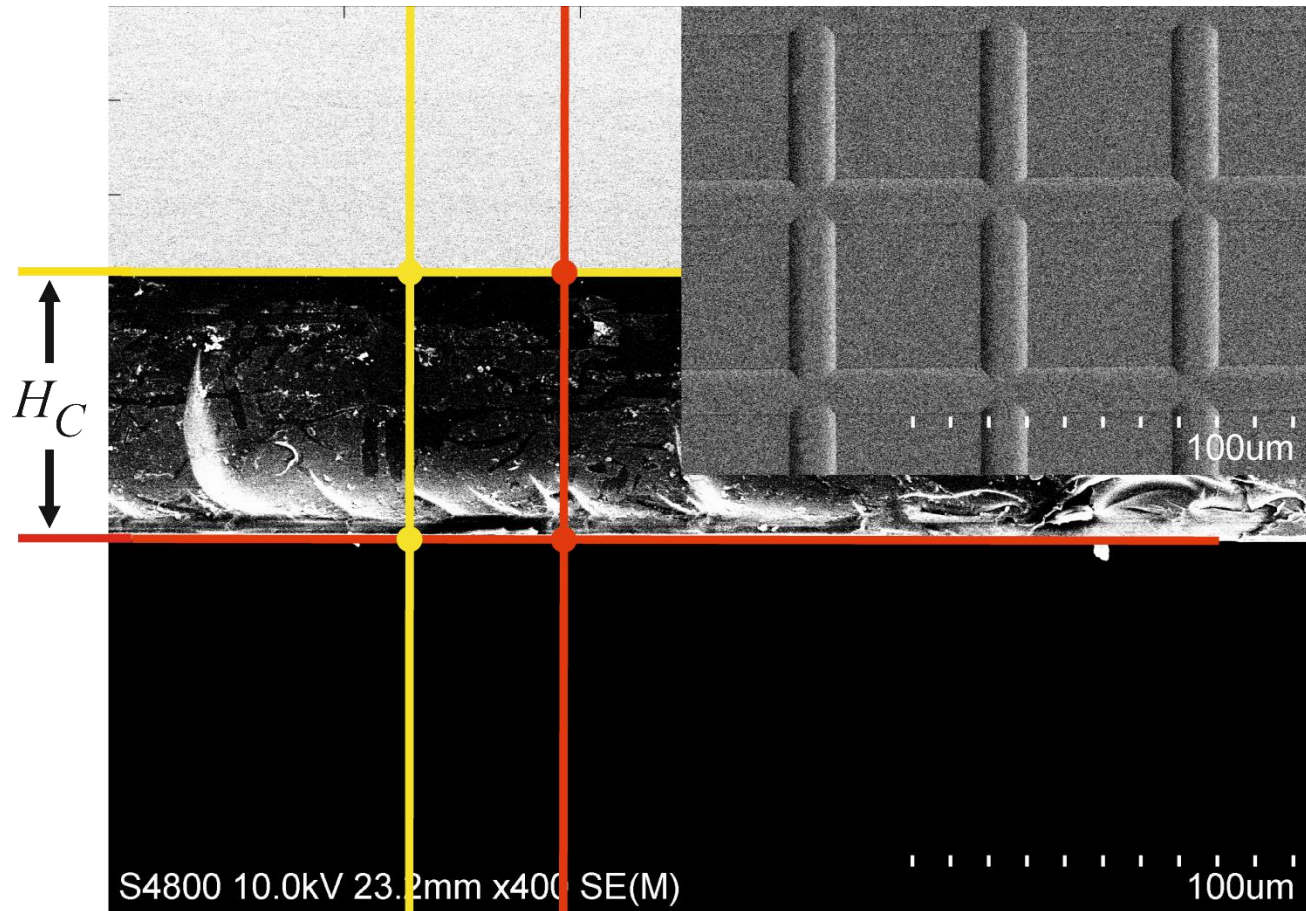
- Two plastic thickness standards (Check Line, CPS-100)
 - #11441: $(11 \pm 1) \mu\text{m}$
 - #11442: $(23 \pm 1) \mu\text{m}$



- Three standard thickness cover slips (Schott, D 263 M)
 - #00, #0, and #1
- Complementary refractive indices measured using polarometer (Horiba Jobin-Yvon, UVISEL-VASE).



Geometric thickness of cover slips



- Scanning Electron Microscope (SEM) Hitachi S4800
- SIRA SEM S170 calibration specimen (19.7 lines/mm, 1% accuracy)



Measurement bias and uncertainty budget

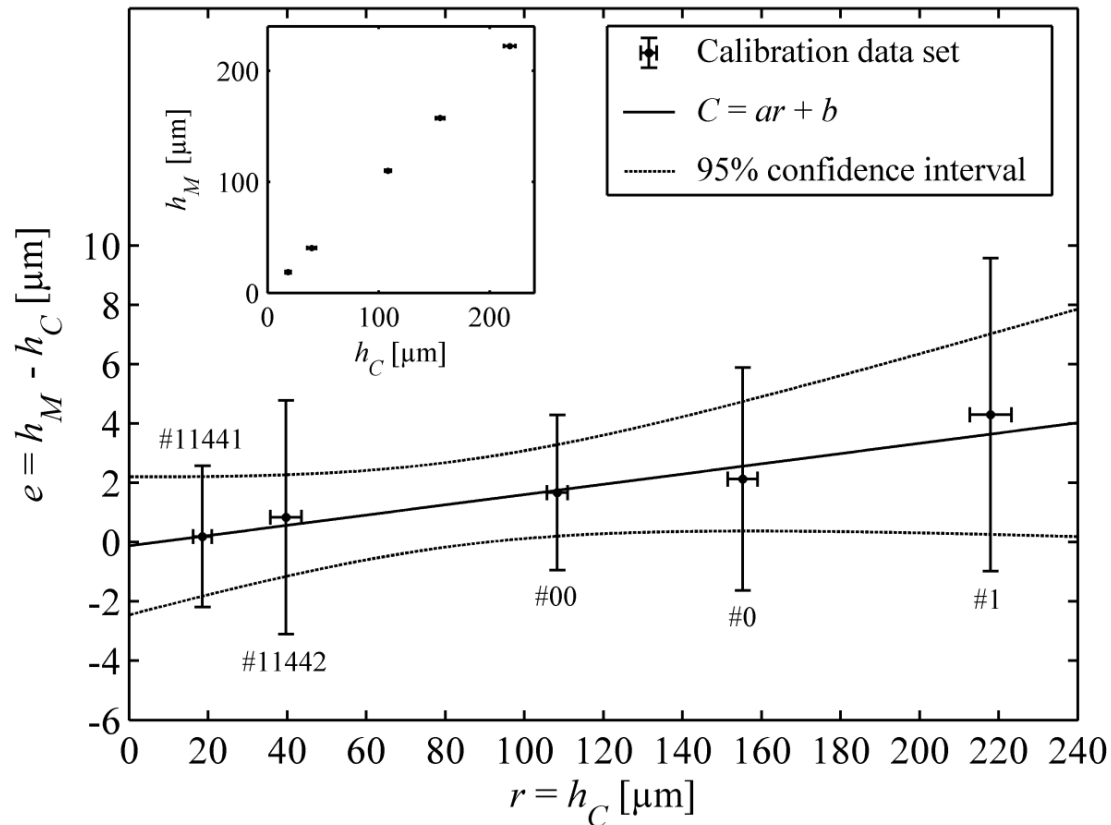
- Measurement bias: $e = h_M - h_C = h(1 + \theta_h^2/2) - H_C n(1 + \theta_H^2/2)(1 + \alpha\Delta T)$

Uncertainty budget for #00 cover slip sample.

Uncertainty component	Unit	Nominal value	Standard uncertainty $u(x_i)$	Sensitivity coefficient $ c_i = \left \frac{\partial f}{\partial x_i} \right $	Uncertainty contribution $u_i(y) = c_i u(x_i)$ [μm]
Optical thickness	h μm	110.01	0.14	$1 + \theta_h^2 / 2$	0.14
Angular error in h	θ_h mrad	7.0	4.0	$h\theta_h$	3.1×10^{-3}
Calibrated geometric thickness	H_C μm	71.49	0.42	$n(1 + \theta_H^2 / 2)(1 + \alpha\Delta T)$	0.64
Angular error in H_C	θ_H mrad	1.7	1.0	$H_C n\theta_H (1 + \alpha\Delta T)$	1.9×10^{-4}
Refractive index	n -	1.516	0.016	$H_C(1 + \theta_H^2 / 2)(1 + \alpha\Delta T)$	1.1
Coefficient of thermal expansion	α 10 ⁻⁶ K ⁻¹	7.2	0.4	$H_C n(1 + \theta_H^2 / 2)\Delta T$	2.7×10^{-5}
Temperature between h and H_C	ΔT °C	-0.6	0.8	$H_C n(1 + \theta_H^2 / 2)\alpha$	6.4×10^{-4}
Calculated quantity	Function	Nominal value [μm]	Standard uncertainty $u_c(y) = (\sum_{i=1}^N u_i^2(y))^{1/2}$ [μm]	Expanded uncertainty $U = 2u_c(y)$ [μm]	
Measured optical thickness	h_M $h(1 + \theta_h^2 / 2)$	110.01	0.15	0.30	
Calibrated optical thickness	h_C $H_C n(1 + \theta_H^2 / 2)(1 + \alpha\Delta T)$	108.3	1.4	2.8	
Bias	e $h_M - h_C$	1.7	1.4	2.8	



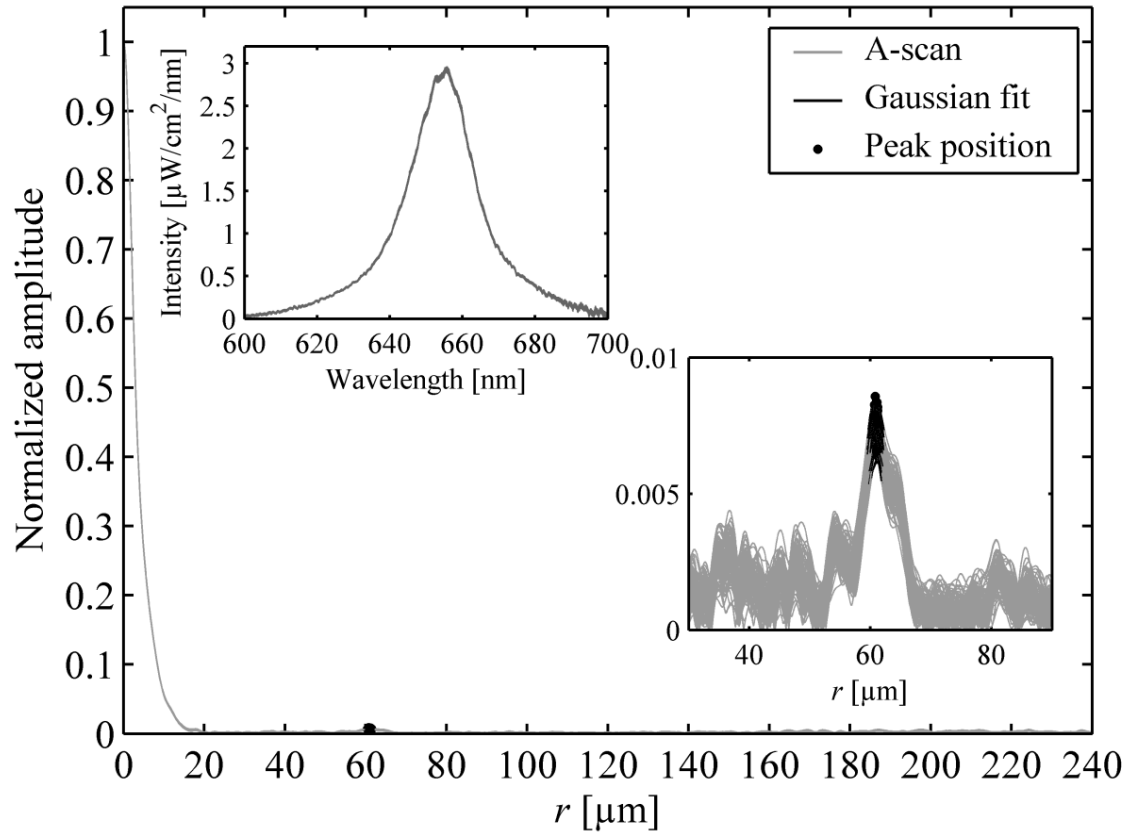
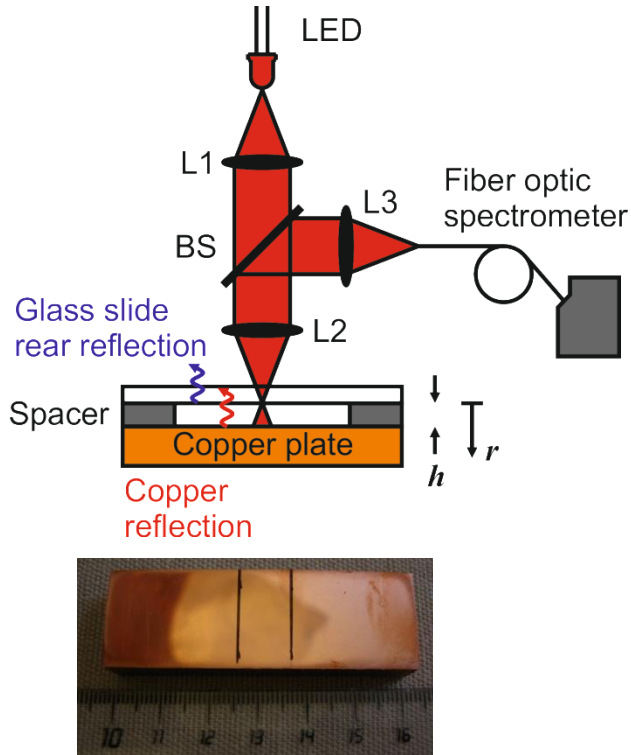
Calibration function and 95% confidence level system uncertainty



- Calibration function $C = (0.017r - 0.1) \mu\text{m}$
- 95% confidence level system uncertainty $(6.3 \times 10^{-3}r + 2.4) \mu\text{m}$ (enveloped)
- Article on calibration in preparation.



Example copper measurement

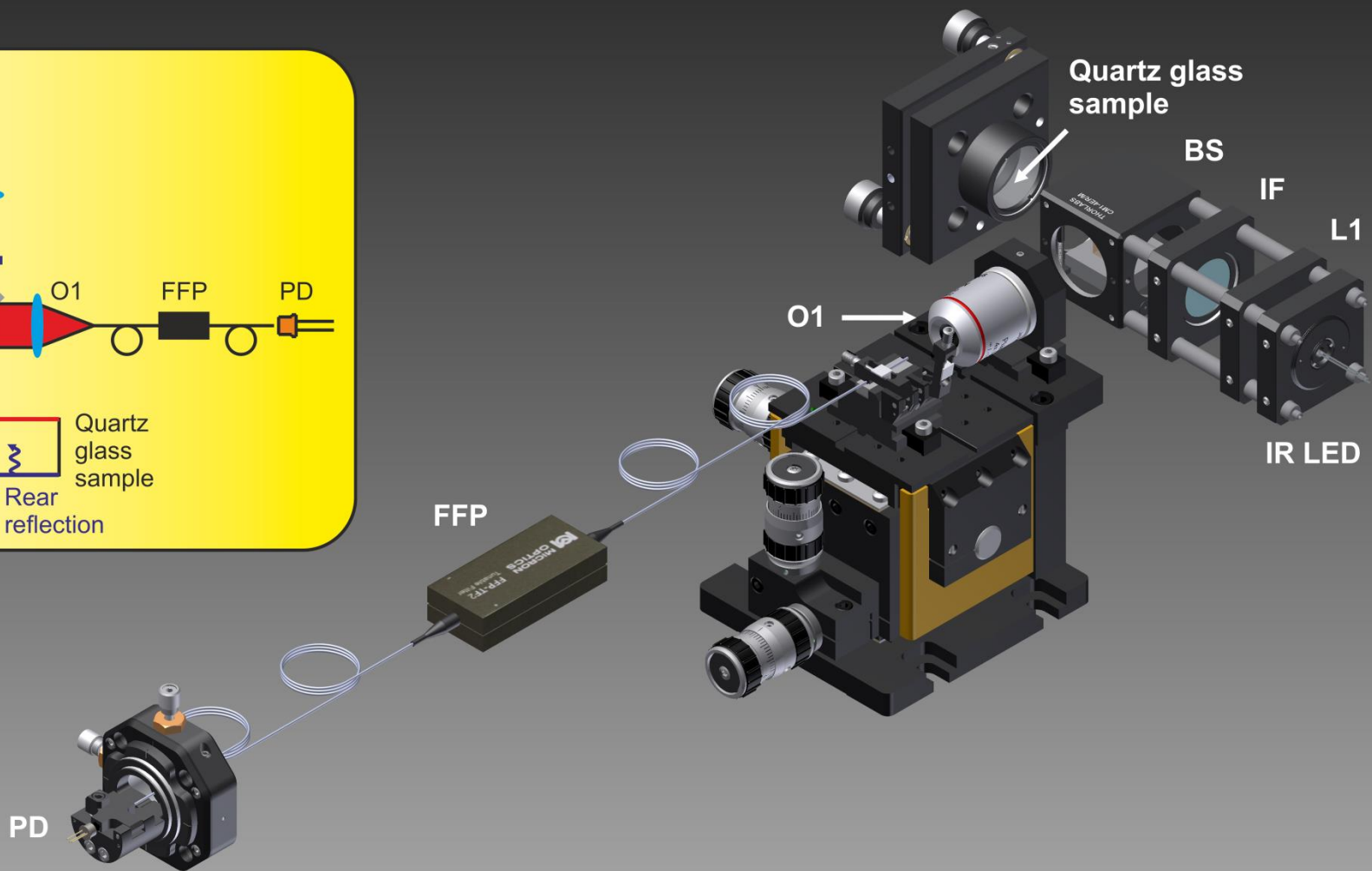
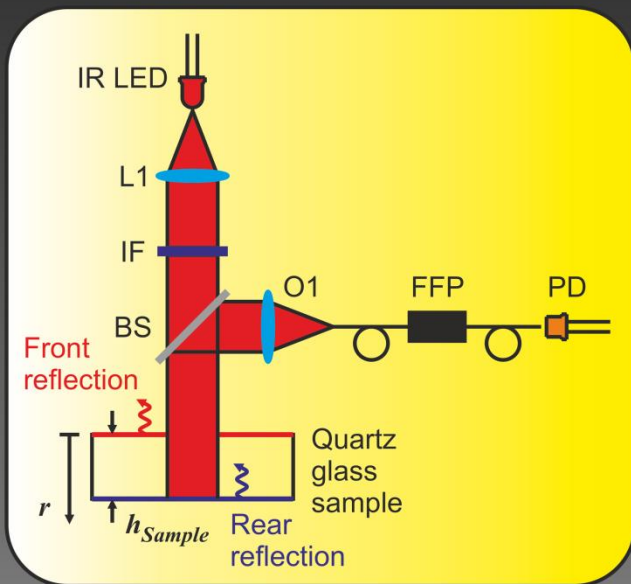


- Optical distance between glass slide rear surface and copper surface $h = (60.927 \pm 0.021) \mu\text{m}$. $T = (20.7 \pm 0.6) ^\circ\text{C}$, $H_R = (32.5 \pm 1.7)\%$.
- Calibrated optical distance: $h_C = h - C(h) = (60.0 \pm 2.8) \mu\text{m}$ with 95% confidence level



Design B setup

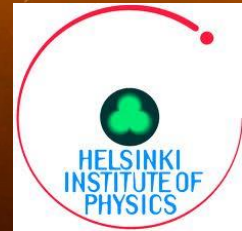
Fiber Fabry-Perot spectrometer to reach 10 mm measurement range





Conclusions

- FDSCI calibrated for micron accuracy absolute distance measurements.
 - Accuracy could be enhanced using $< 1\%$ uncertainty dimension standards.
- FDSCI can be used to measure copper.
 - Coherence could be increased tuning the sample tilt.
 - Next the FDSCI will be tested to determine height of ultra-precisely machined steps on an OFE Cu disc.
- To reach the required 10 mm measurement range we will upgrade our setup with a fiber Fabry-Perot spectrometer.



Thank You



Calibration data set

Calibration data set. Uncertainties reported represent 1σ standard uncertainties.

Calibration sample		Optical thickness h [μm]	Angular error in h θ_h [mrad]	Calibrated geometric thickness H_C [μm]	Angular error in H_C θ_H [mrad]	Refractive index n [-]	Coefficient of thermal expansion α [10^{-6} K^{-1}]	Temperature between h and H_C ΔT [$^{\circ}\text{C}$]
Check Line CPS-100	#11441	$18.765 \pm 0.078^*$	$7.0 \pm 4.0^{**}$	$11.0 \pm 0.6^{**}$	-	$1.689 \pm 0.061^*$	- ⁺	$1.5 \pm 1.3^{**}$
	#11442	$40.53 \pm 0.19^*$	$7.0 \pm 4.0^{**}$	$23.0 \pm 0.6^{**}$	-	$1.726 \pm 0.074^*$	- ⁺	$1.4 \pm 1.3^{**}$
Schott D 263 M	#00	$110.01 \pm 0.14^*$	$7.0 \pm 4.0^{**}$	$71.49 \pm 0.42^*$	$1.7 \pm 1.0^{**}$	$1.516 \pm 0.016^*$	$7.2 \pm 0.4^{**}, ++$	$-0.6 \pm 0.8^{**}$
	#0	$157.38 \pm 0.13^*$	$7.0 \pm 4.0^{**}$	$101.77 \pm 0.61^*$	$1.7 \pm 1.0^{**}$	$1.526 \pm 0.016^*$	$7.2 \pm 0.4^{**}, ++$	$-3.2 \pm 0.8^{**}$
	#1	$222.26 \pm 0.19^*$	$7.0 \pm 4.0^{**}$	$144.15 \pm 0.87^*$	$1.7 \pm 1.0^{**}$	$1.512 \pm 0.016^*$	$7.2 \pm 0.4^{**}, ++$	$-0.9 \pm 0.8^{**}$

*Type A uncertainty evaluation (ISO Guide to the expression of uncertainty in measurement).

**Type B uncertainty evaluation, uniform distribution assumed (ISO Guide to the expression of uncertainty in measurement).

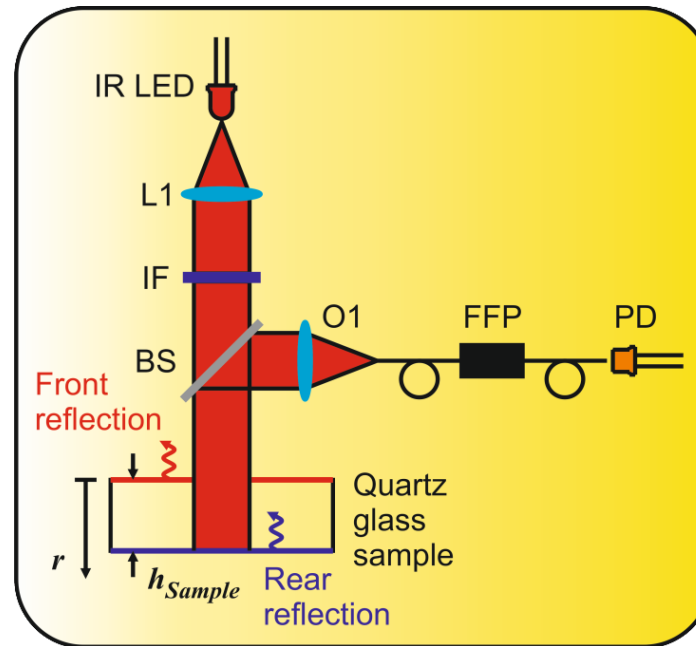
⁺The specification of Check Line CPS-100 includes the thickness variation due to thermal expansion within temperature $(21 \pm 2) ^{\circ}\text{C}$.

⁺⁺ α from the datasheet of Schott D 263 M, 10% maximum variation assumed.



Design B

Goal to reach 10 mm measurement range



- NIR LED (LED1550-35K42, Roithner Lasertechnik) + interference filter (IF) (NIR01-1550/3-25, Semrock) $\Rightarrow \Delta\lambda = 8.8 \text{ nm}$ centered at $\lambda_0 = 1550 \text{ nm}$
- Tunable fiber Fabry-Perot (FFP) filter (FFP-TF2, Micron Optics) combined with photodetector (PD) (PT511-2, Roithner Lasertechnik) captures the spectral interferogram.
 - 23.2 nm free spectral range (FSR) at $\lambda_0 = 1550 \text{ nm}$, $\delta\lambda = 0.025 \text{ nm}$
- Expect 20 mm axial depth range r_{max} in air.
- 1 – 10 mm quartz glass samples