

Review of recent LHCb results

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laboratório de partículas elementares

Universidade Federal do Rio de Janeiro





Outline

- LHCb experiment
- Physics program
- Selected results
- Run II news and further prospects
- Summary

LHCb detector

**Forward single-arm spectrometer with warm magnet
(possibility to inverse polarity)**

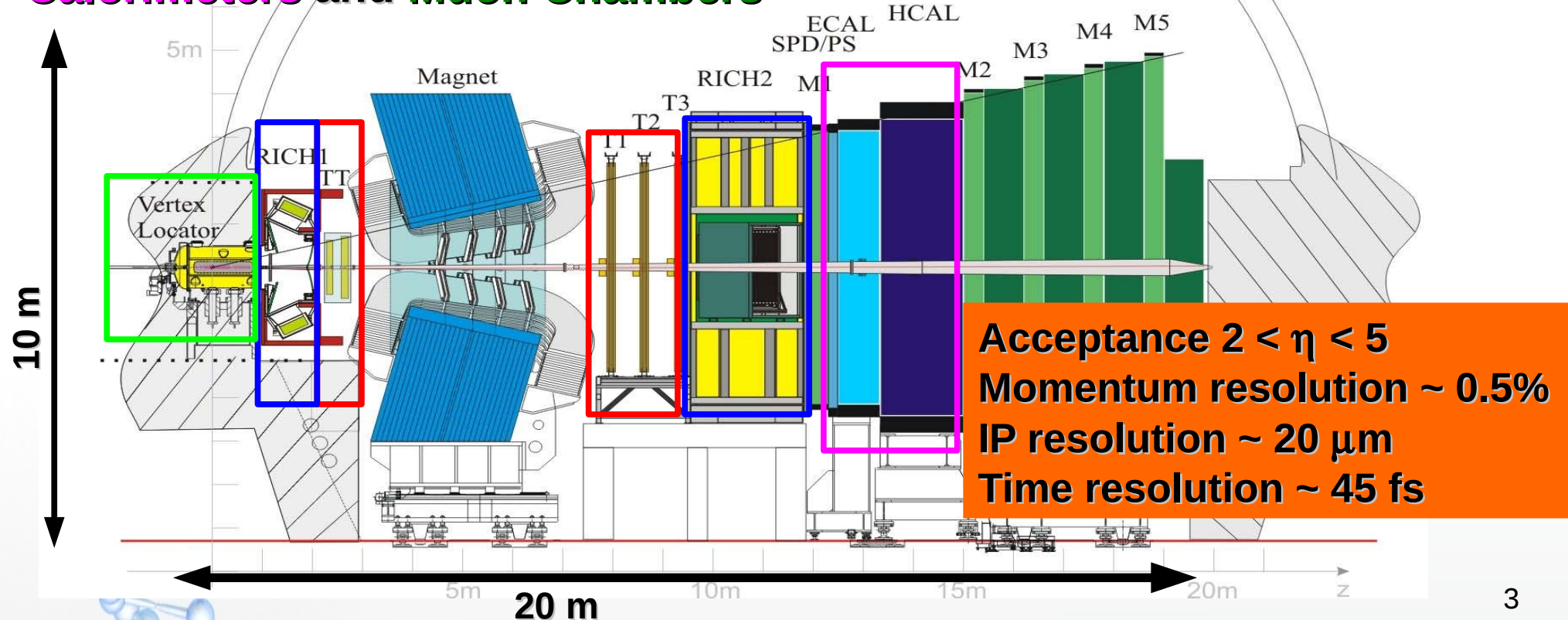
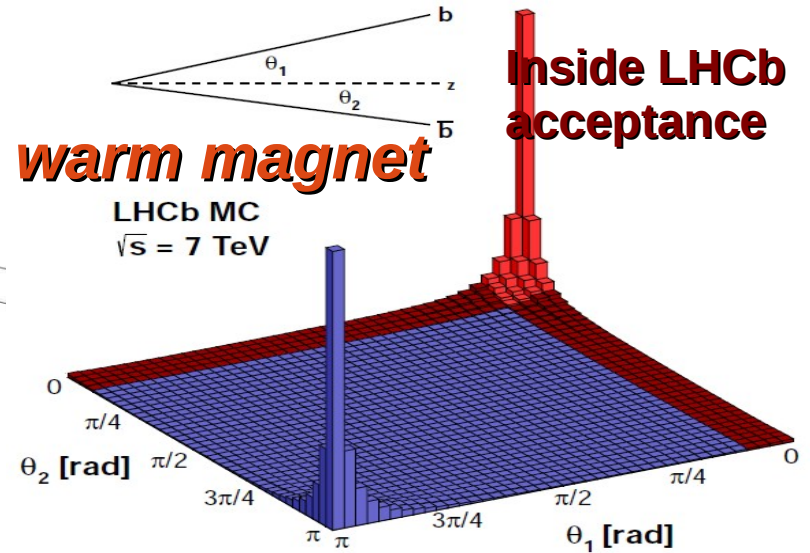
Optimize for b and c hadron studies

Vertexing

Tracking stations

Particle ID Ring Imaging Cherenkov

Calorimeters and Muon Chambers

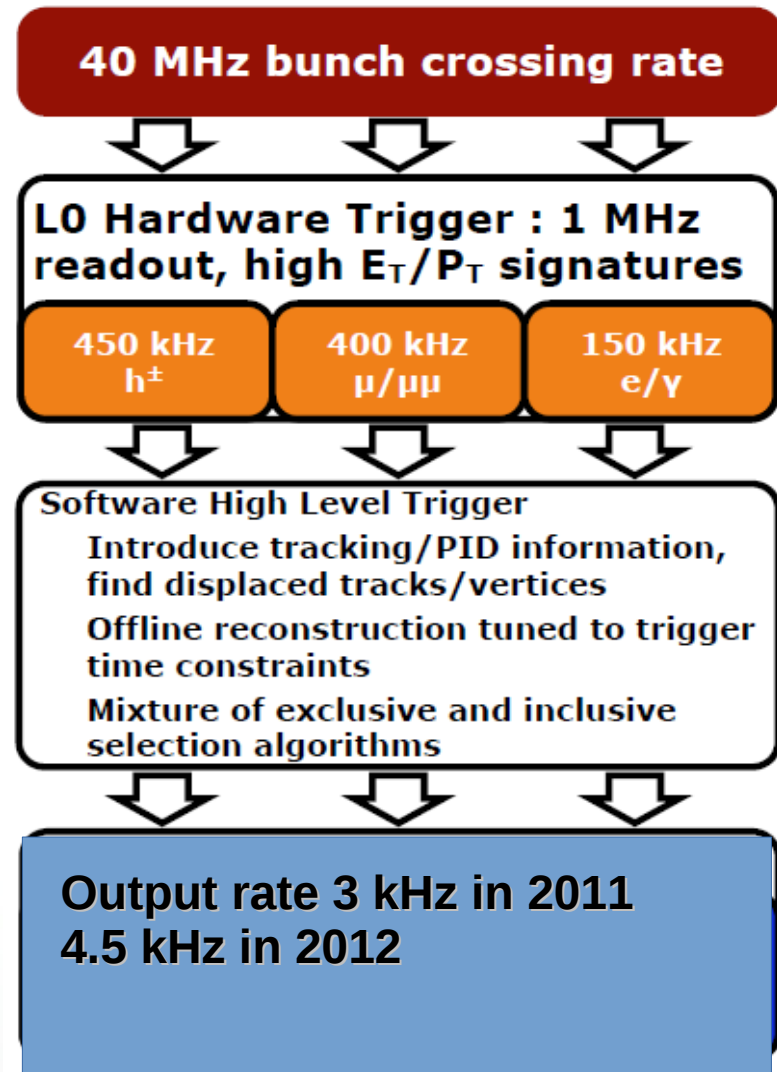
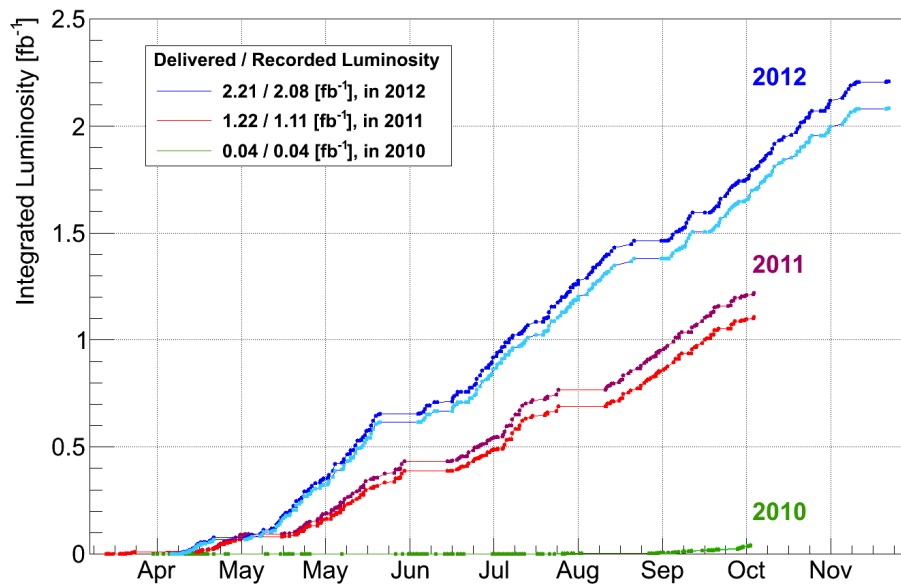


LHCb data for Run I (2011+2012)

10^{11} protons per bunch colliding at 7 (2011) and 8 (2012) TeV

Luminosity at IP8 (LHCb): $2\text{-}4 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
About 1500 charged particles produced at each pp collision

$\sigma(\text{bb}) \sim 75 \mu\text{b} @ 7 \text{ TeV}^*$ in LHCb acceptance
 $\sim 40\% \text{ B}^+$, $40\% \text{ B}^0$, $\sim 10\% \text{ B}_s$
Remaining b baryons, B_c , etc...



* *J. High Energy Phys.*08 (2013) 117



Physics program

- Rare decays, BSM and exotics
 - see J. Serrano (Fri 07/08) and X. Cid Vidal (Wed 05/08) for details
- CP violation
 - See B. Souza de Paula (Fri 07/08) for details
- Heavy flavours and spectroscopy
- Forward physics: QCD, EW and BSM in the forward region
 - See M. Rangel (later this afternoon) for details
 - See X. Cid Vidal (Wed 05/08) for direct searches on forward Higgs and BSM particles



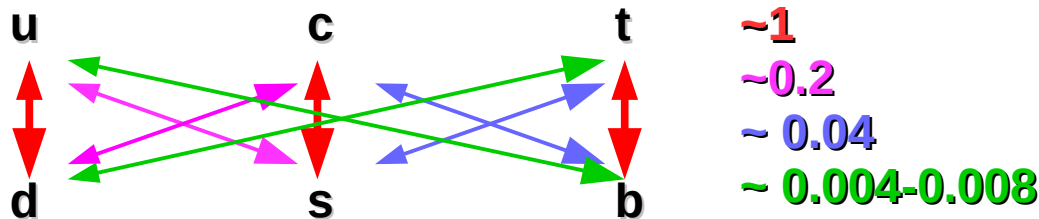
Selected results

- Rare $b \rightarrow s \ell^+ \ell^-$
 - New $B \rightarrow \pi \mu \mu$ results on $b \rightarrow d \ell^+ \ell^-$ imminently shown at DPF2015 meeting
- Semileptonic: $\Lambda_b \rightarrow p \mu \nu$, $B \rightarrow D^{(*)} \tau \nu$
- Top physics: first top measurement
- Spectroscopy: multiquark bound states
- Unitarity triangle: γ angle

CKM picture in brief

Weak interaction couples quarks through elements of the Cabibbo-Kobayashi-Maskawa (CKM) matrix

Weak eigenstates are different from mass eigenstates = CKM matrix is not diagonal and may relate quarks of different generation



- ~ 1
- ~ 0.2
- ~ 0.04
- $\sim 0.004-0.008$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Clear hierarchy in the couplings: the further from diagonal, the weaker

Unitarity imposes relations, among which $\sum_k V_{ik} V_{jk}^* = 0$

Elements forming sides (and angles) of 3 independent “unitarity” triangles, of which only a couple are of interest for heavy-flavour decays

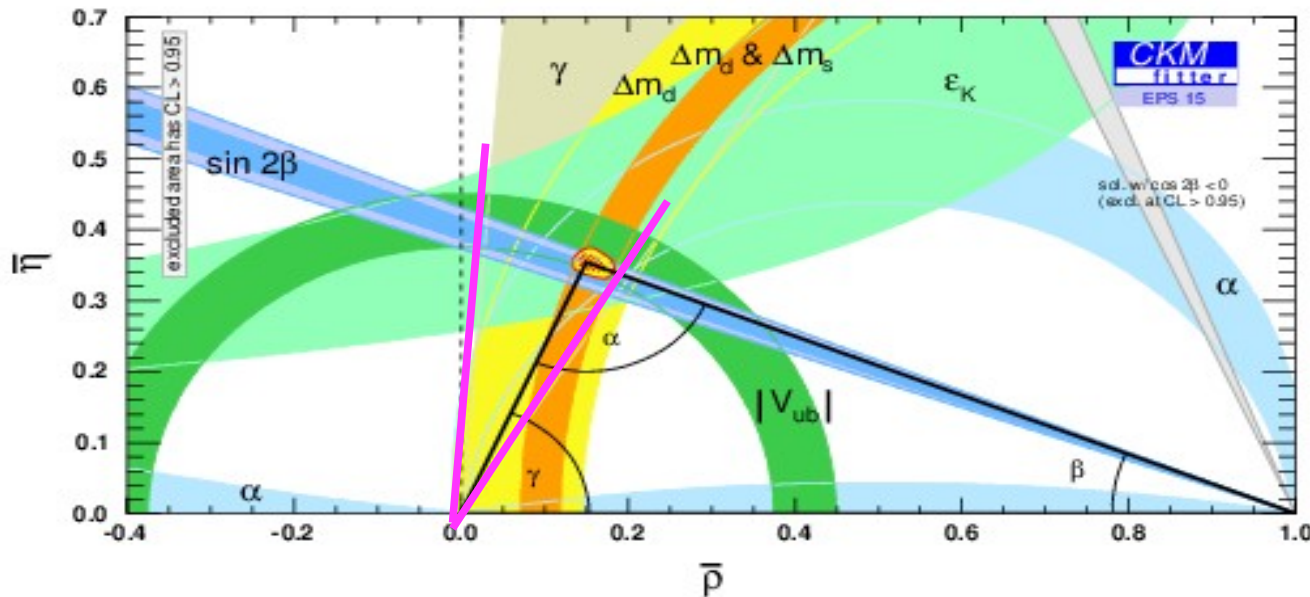
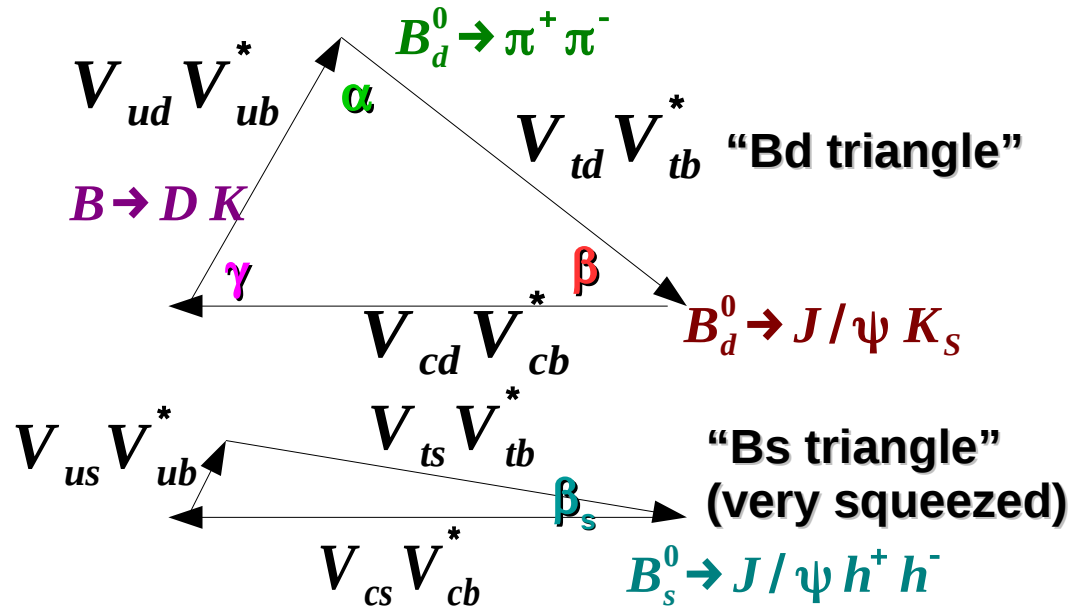
CKM and unitarity triangles

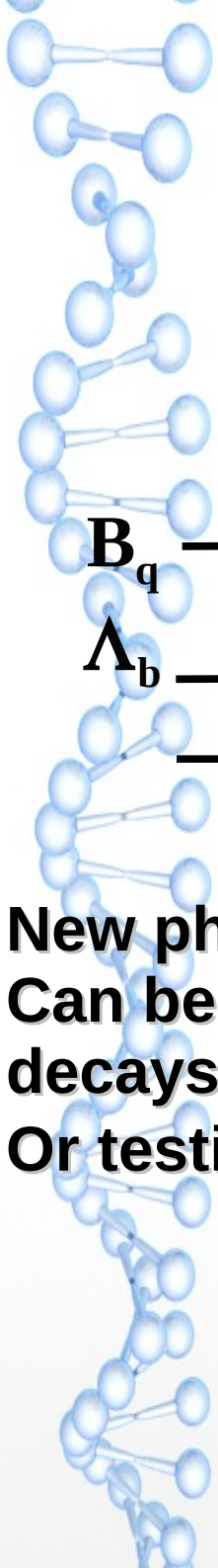
Most interesting relation:

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

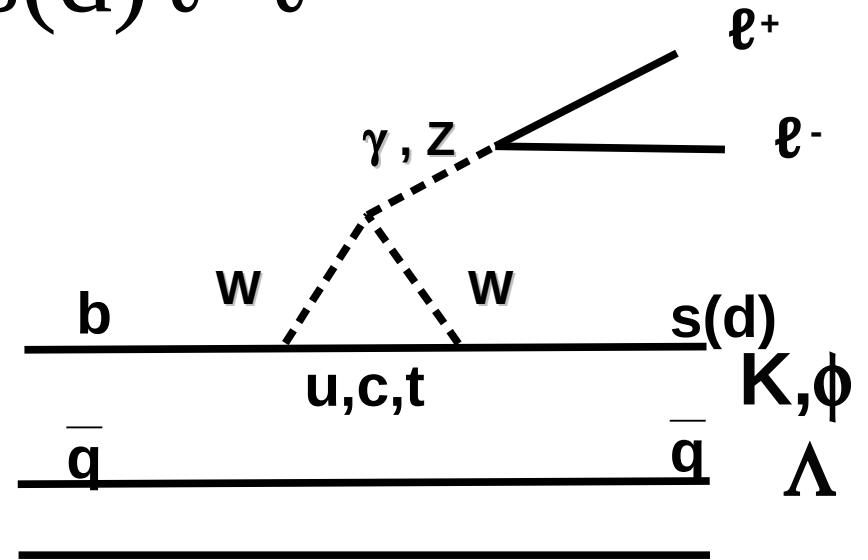
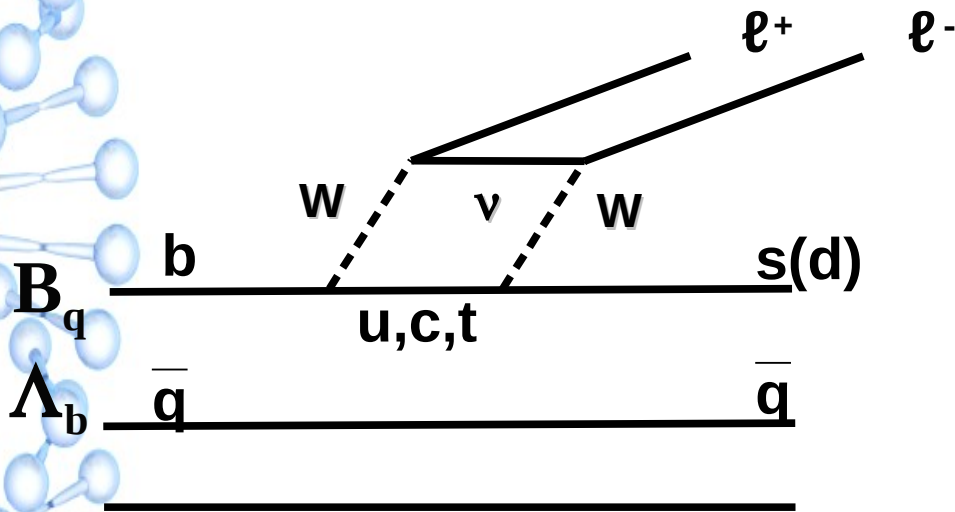
Sides usually measured in semileptonic decays and oscillation frequency, angles in CP asymmetries

$$V_{us} V_{ub}^* + V_{cs} V_{cb}^* + V_{ts} V_{tb}^* = 0$$





$$b \rightarrow s(d) \ell^+ \ell^-$$



New physics can intervene in the loops/boxes

Can be probed through the analysis of the dynamics of the decays

Or testing, e.g., lepton universality $b \rightarrow s e^+ e^- / b \rightarrow s \mu^+ \mu^-$

Dynamics for $B^0 \rightarrow K^{*0}\mu^+\mu^-$, $B_s \rightarrow \phi\mu^+\mu^-$

$$\frac{1}{d\Gamma/dq^2 d\cos\theta_l d\cos\theta_K d\Phi} \frac{d^3\Gamma}{dq^2 d\cos\theta_l d\cos\theta_K d\Phi} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l \right. \\ \left. + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\Phi + S_4 \sin 2\theta_K \sin 2\theta_l \cos \Phi \right. \\ \left. + A_5 \sin 2\theta_K \sin \theta_l \cos \Phi + A_6 \sin^2 \theta_K \cos \theta_l \right. \\ \left. + S_7 \sin 2\theta_K \sin \theta_l \sin \Phi + A_8 \sin 2\theta_K \sin 2\theta_l \sin \Phi \right. \\ \left. + A_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\Phi \right].$$

$q^2 = \mu^+\mu^-$ invariant mass squared

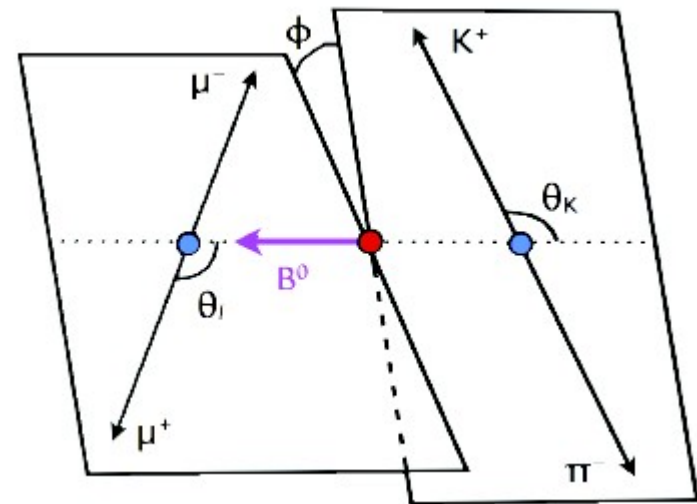
Formula slightly different between K^* (self-tagging) and ϕ

F_L : fraction of longitudinal polarization of K^*/ϕ

$A_6 \sim A_{FB}$ = forward-backward asymmetry of the dimuon system

$A_5 = S_5$ in the case of K^*

They depend on $B \rightarrow K^*/\phi$ form factors and Wilson Coefficients of the OPE



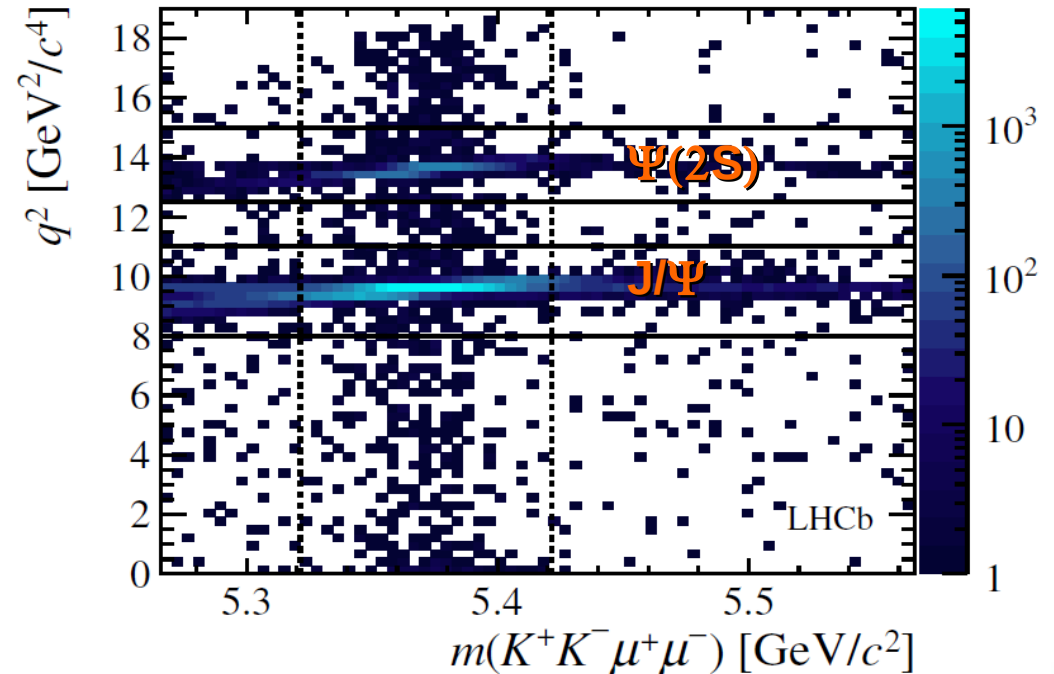
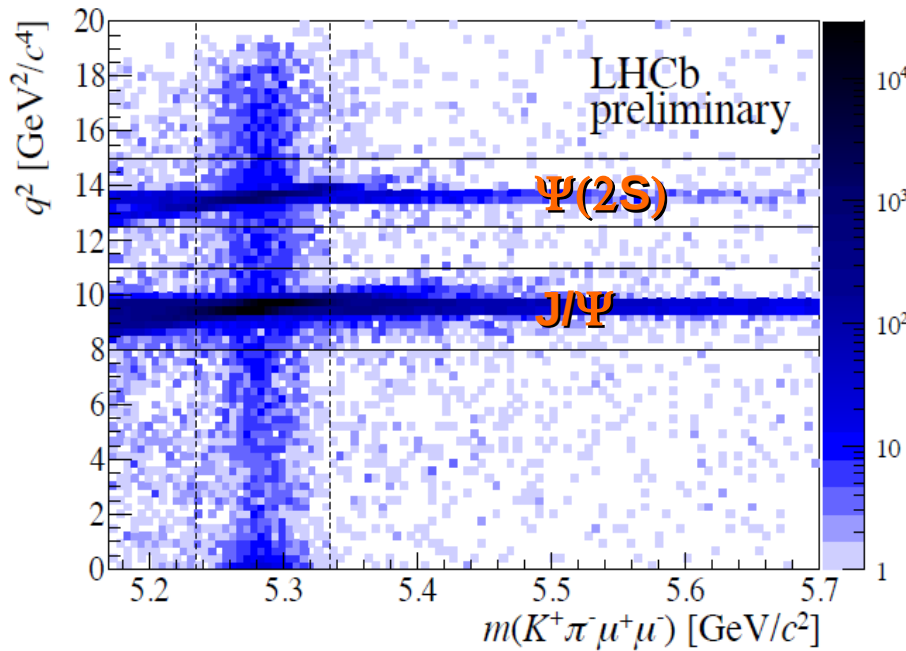
$B \rightarrow X \mu^+ \mu^-$ events distribution

LHCb-CONF-2015-002

$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$

LHCb-PAPER-2015-023

$$B_s \rightarrow \phi \mu^+ \mu^-$$

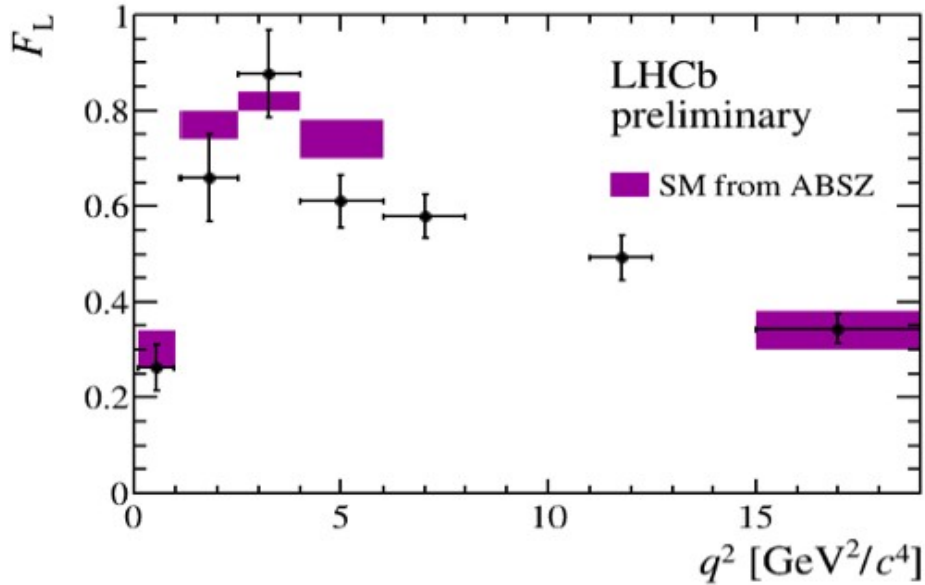


Signal yield excluding charmonia: 2.4 k evts

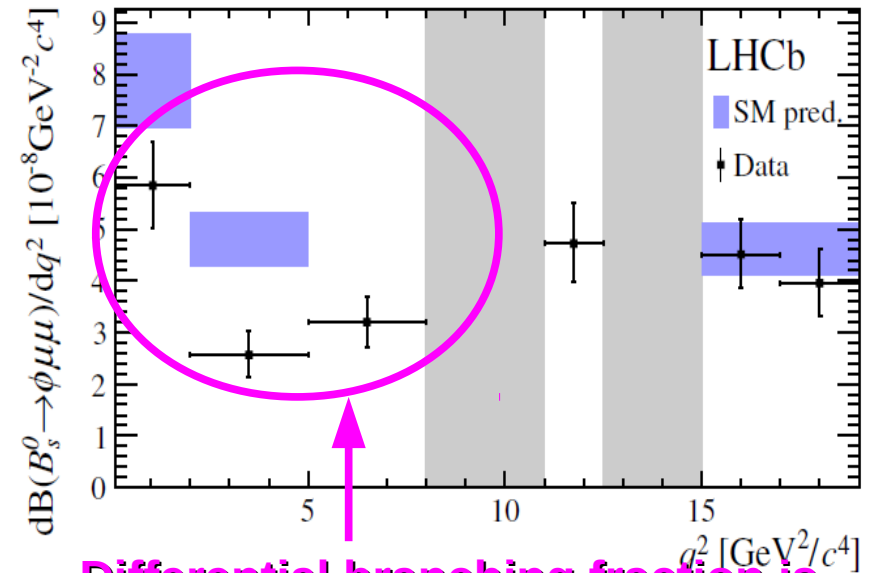
Signal Yield excluding charmonia: ~400 evts

B → X μ⁺μ⁻ results

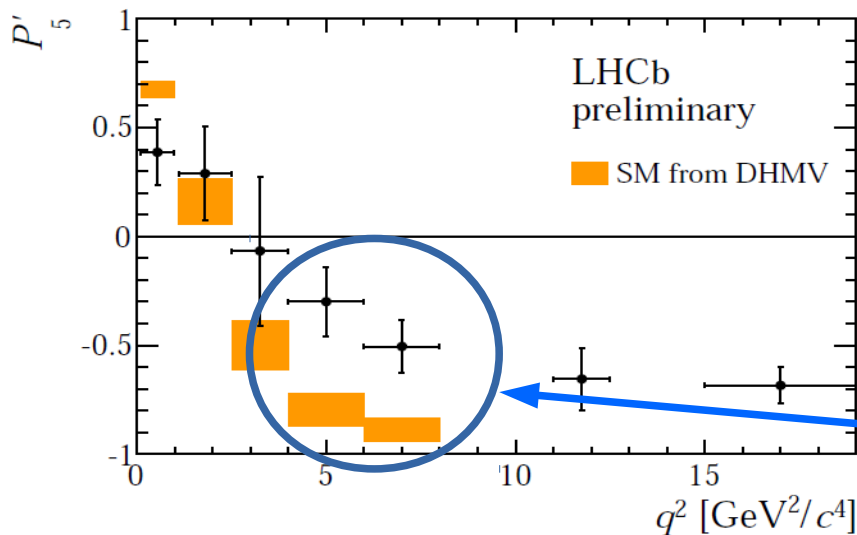
B⁰ → K^{*0}μ⁺μ⁻



B_s → φμ⁺μ⁻



Differential branching fraction is 3.5σ below SM prediction in the lower q^2 half, no discrepancy for the angular variables with this statistics



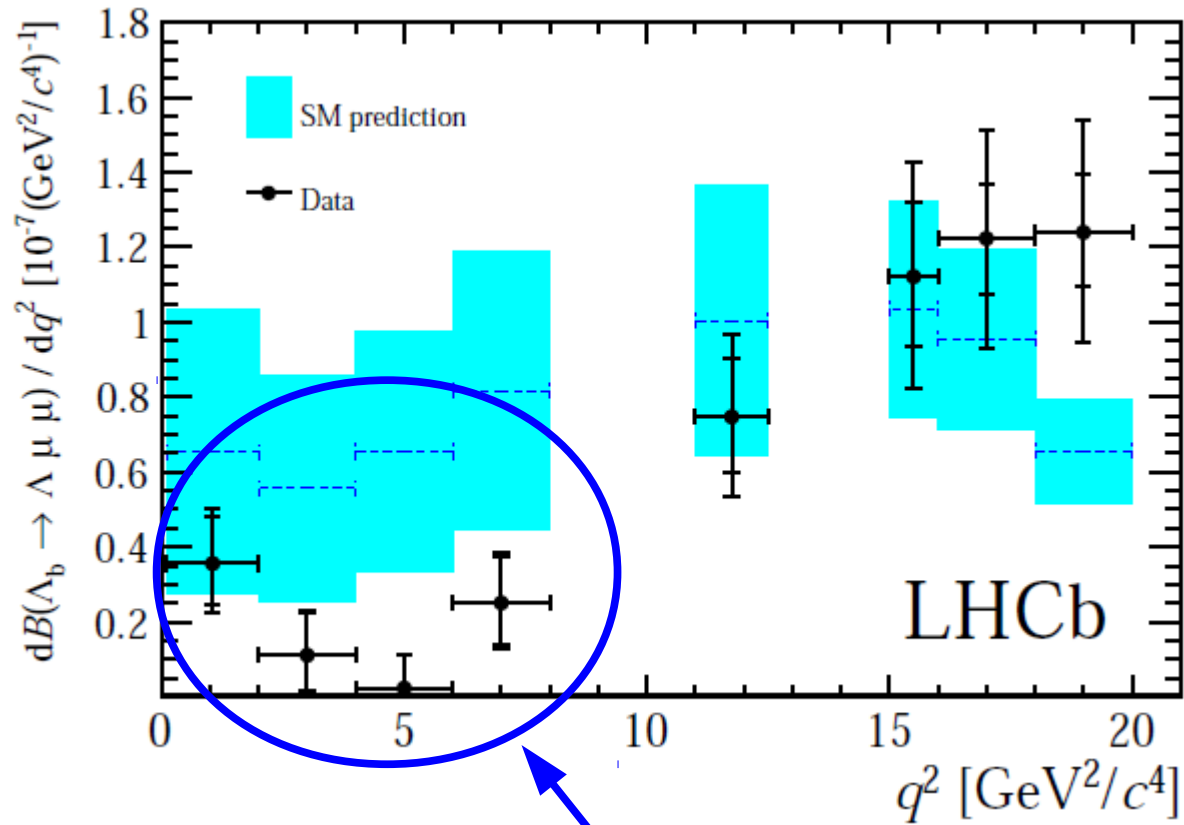
$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$$

Form-factor independent

3.7σ combined difference with SM

$$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$$

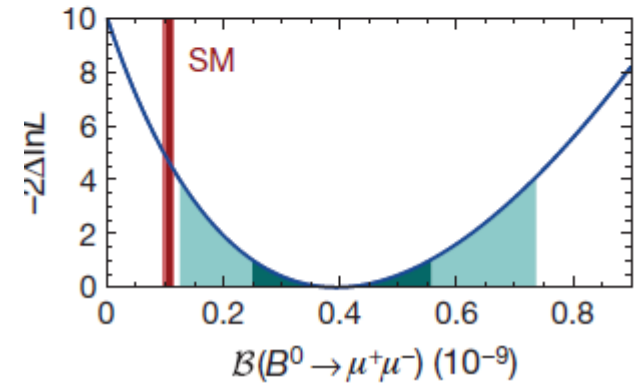
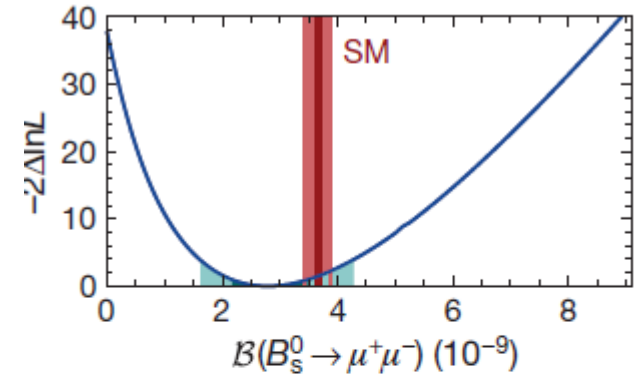
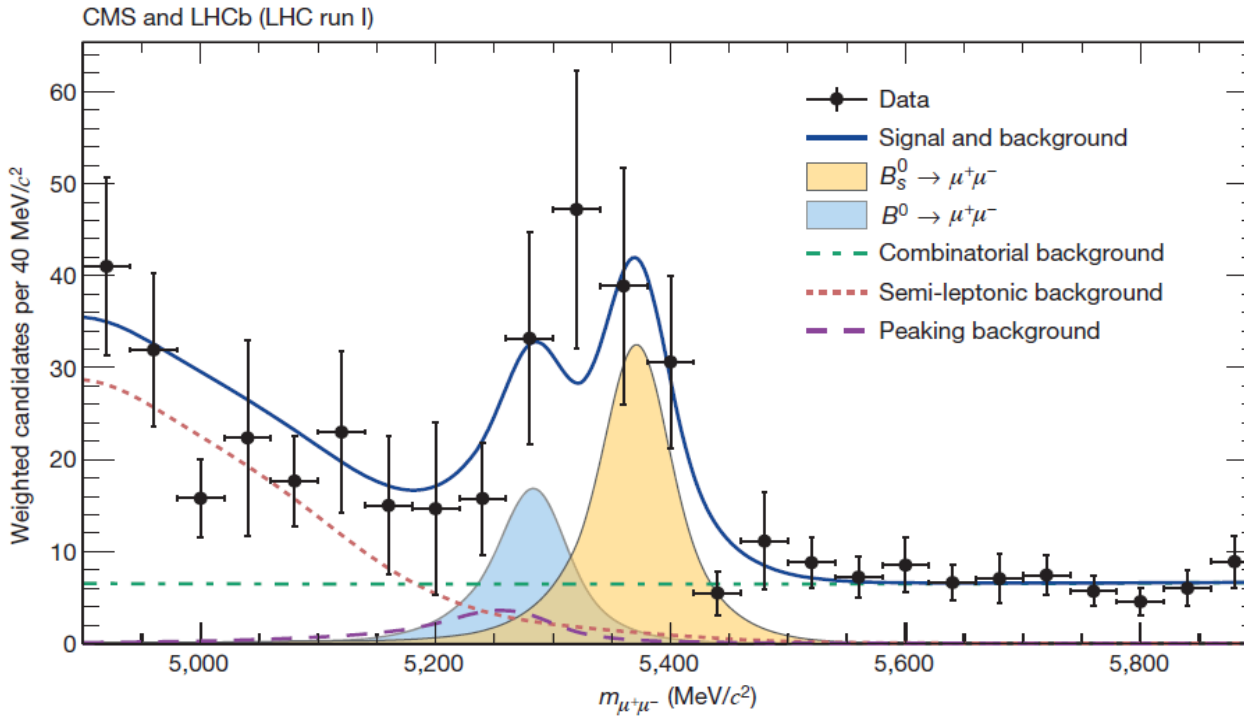
LHCb-PAPER-2015-009, arXiv:1503.07138



Similar as in $B_s \rightarrow \phi \mu^+ \mu^-$!

$B_{s,d} \rightarrow \mu\mu$

Nature 522, 68-72 (04 June 2015)



No significant deviation from SM yet (ratio of B_d/B_s is still $2,1\sigma$ within SM)

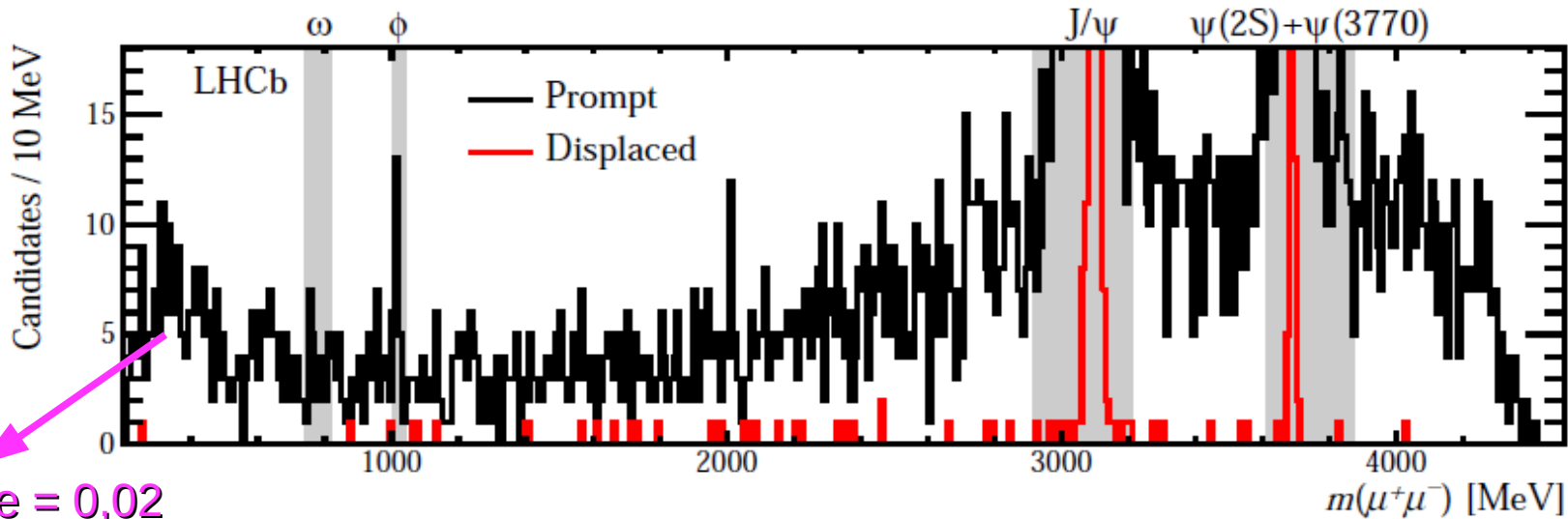
Hidden sector bosons $B^0 \rightarrow K^* \chi (\rightarrow \mu^+ \mu^-)$

LHCb-PAPER-2015-036 in preparation

Theoretical models predicting new particle to couple to SM particle through mixing with Z, H, γ, ν

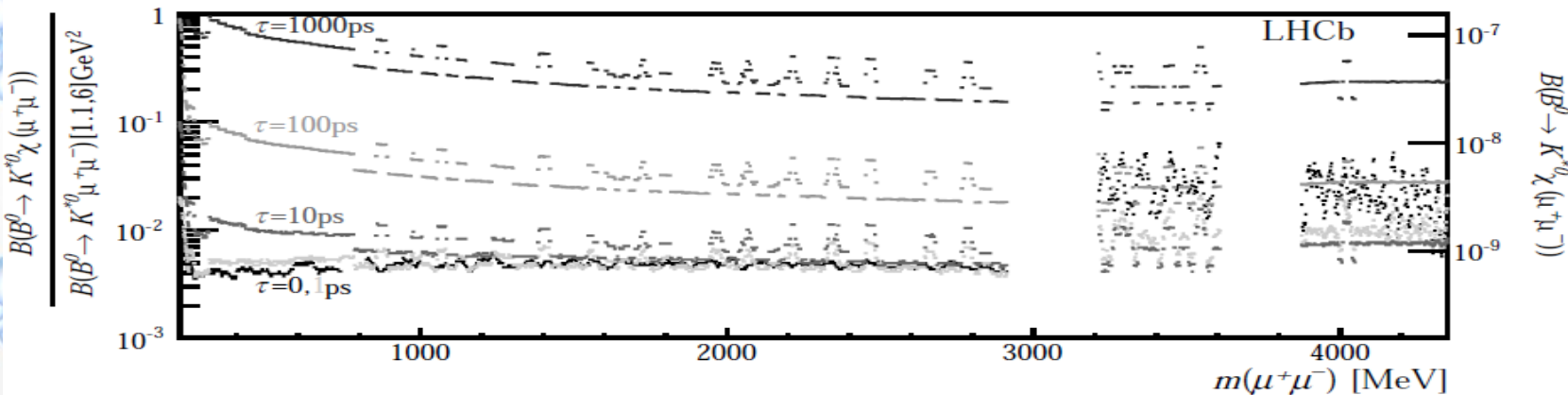
Short (axion-like PRD81(2010)034001, DM mediator PLB727(2013)) vs long (inflaton JHEP1005(2010)010) lifetime predictions

Typical mass $< O(1 \text{ GeV})$ and lifetime coverage up to 10^{-8} s

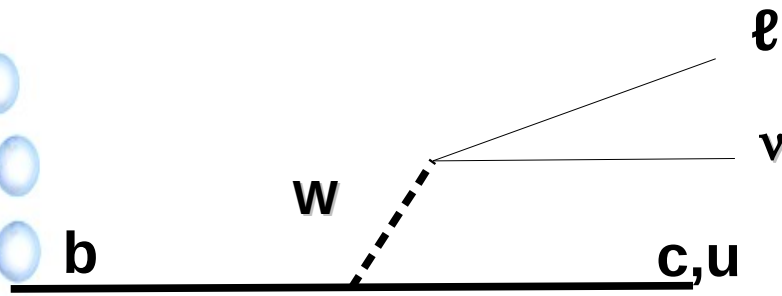
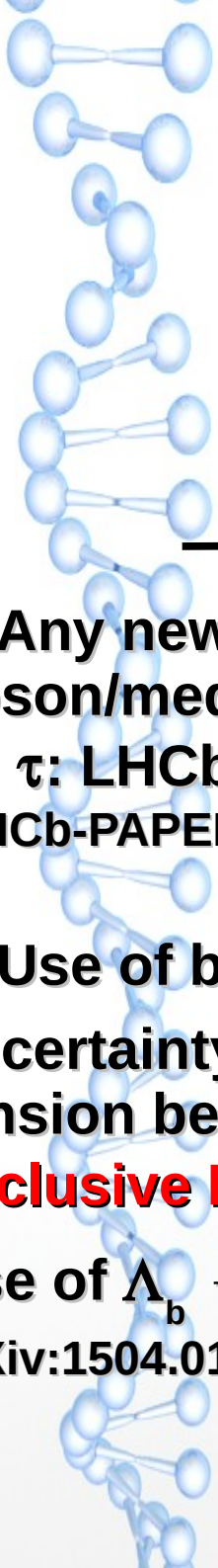


p-value = 0,02

No hint of signal, set upper limit vs lifetime and mass:



Semileptonics



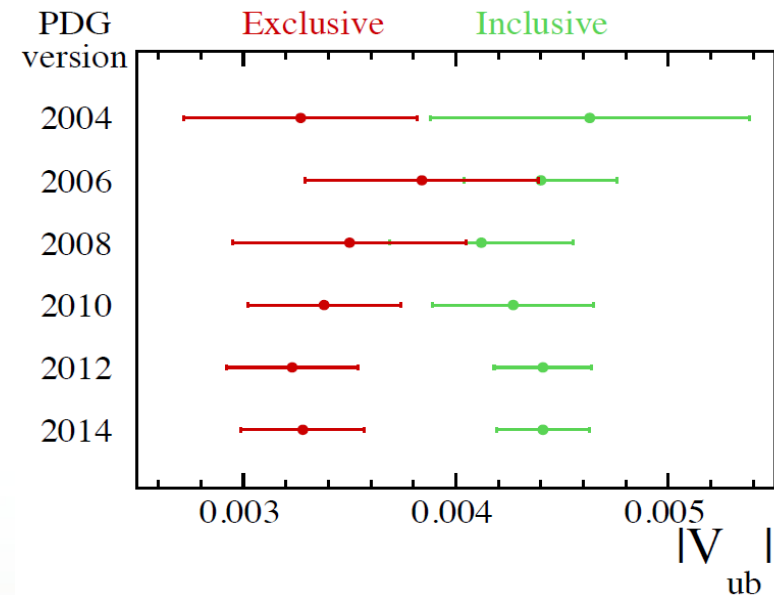
Theoretically well-understood in the SM
 Decays to light leptons well-measured by B factories

- a) Not as good for τ lepton
- b) Good way to extract V_{qb} CKM element

a) Any new (charged) intermediate boson/mediator would couple preferentially to τ : LHCb studied $B^0 \rightarrow D^{*+} \tau \nu / B^0 \rightarrow D^{*+} \mu \nu$ (LHCb-PAPER-2015-025, arXiv:1506.08614)

b) Use of $b \rightarrow u \mu \nu$ to improve $|V_{ub}|$ (relative uncertainty still $\sim 12-13\%$) + solve the tension between measurements from **exclusive $B \rightarrow \pi \mu \nu$** and **inclusive $B \rightarrow X_u \mu \nu$** :

Use of $\Lambda_b \rightarrow p \mu \nu$ (LHCb-PAPER-2015-013, arXiv:1504.01568)



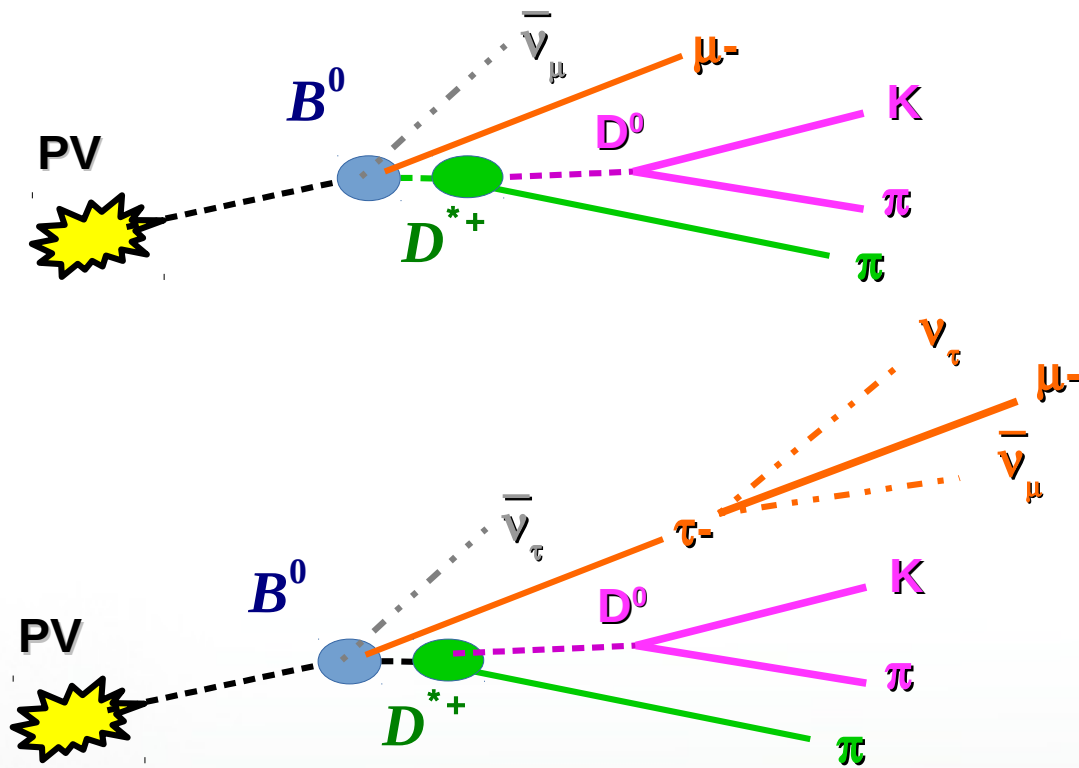
$$\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$$

Measure: $R(D^*) \equiv \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)}$

Using τ decay:

$$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$$

= 0.252 in SM (PRD 85094025 (2012)), with very good precision



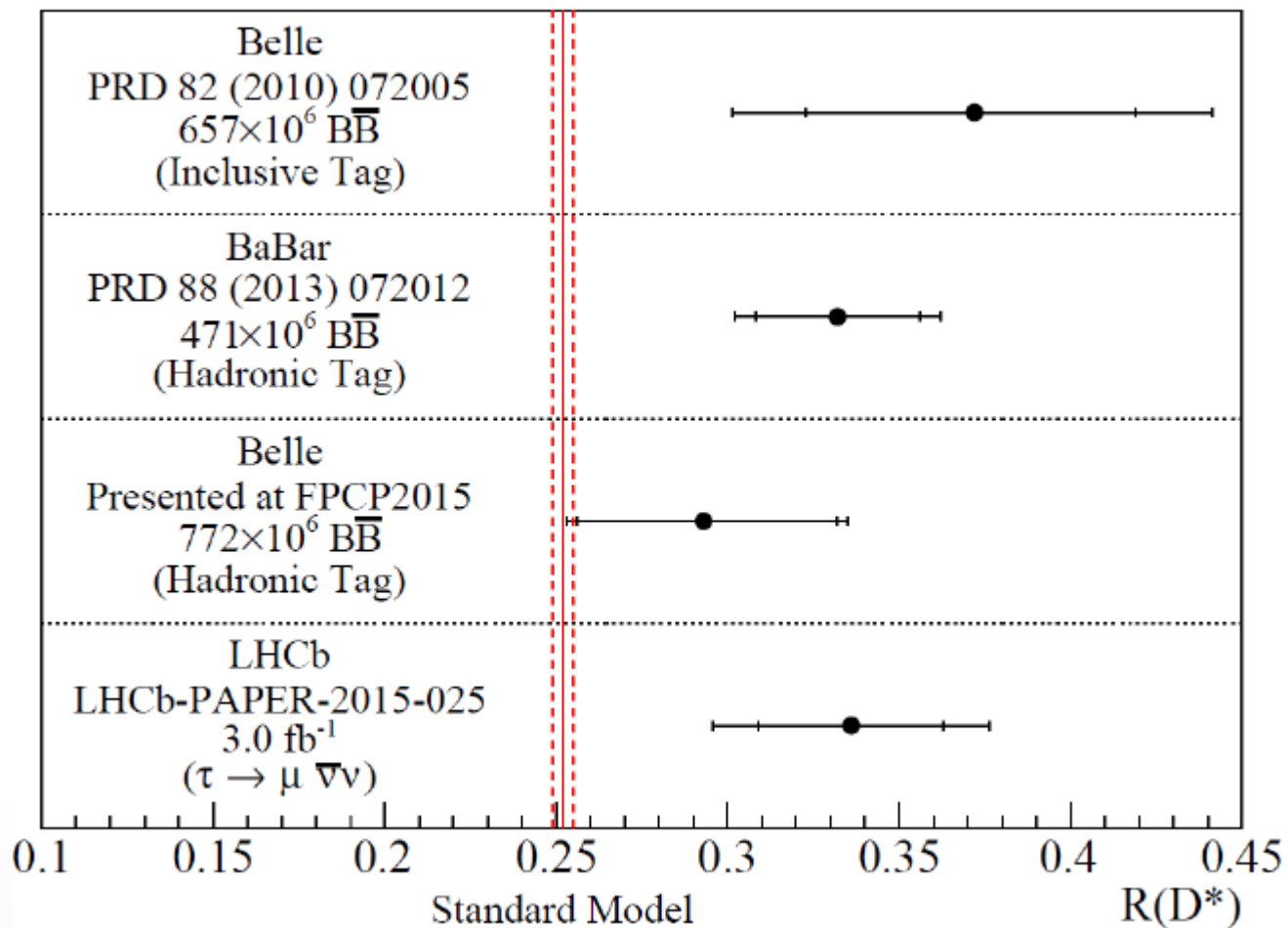
Very specific topologies
+ use of missing mass,
muon energy and
momentum transfer q

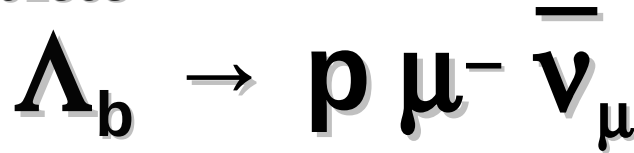
LHCb-PAPER-2015-025, arXiv:1506.08614

R(D*) result

$$R(D^*) = 0.336 \pm 0.027 \pm 0.030$$

Follows historical trend,
above SM prediction by ~
 2.1σ





Help clarify the debate on $|V_{ub}|$ and the tension between inclusive and exclusive measurements

Fit the ϵ_R dependence on additional left-handed V+A current

Experimentally:

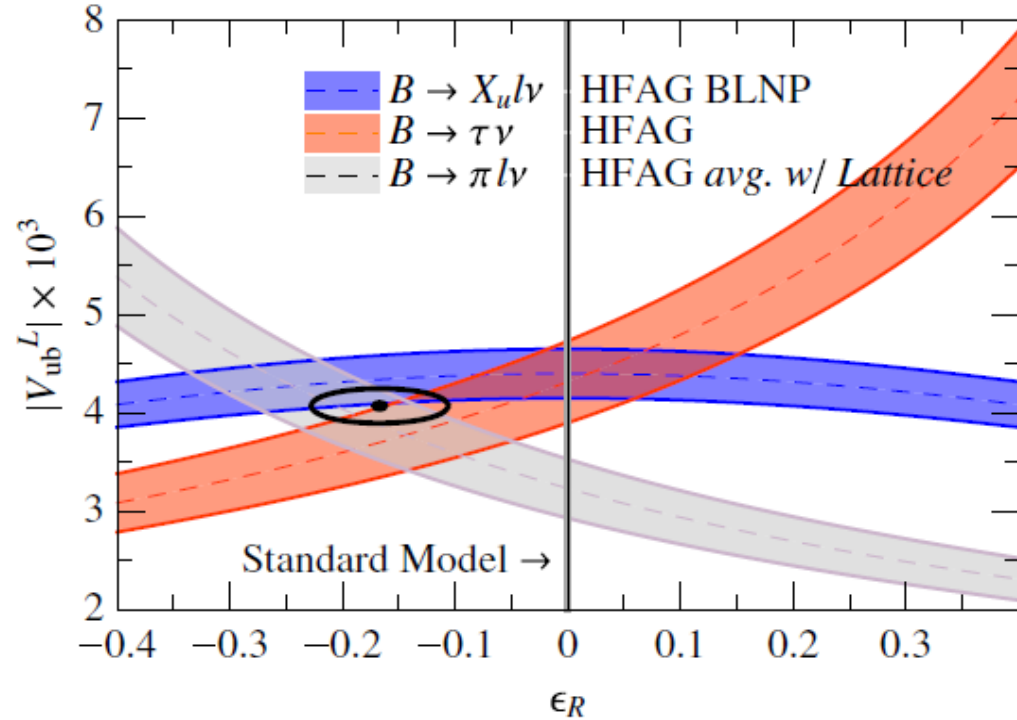
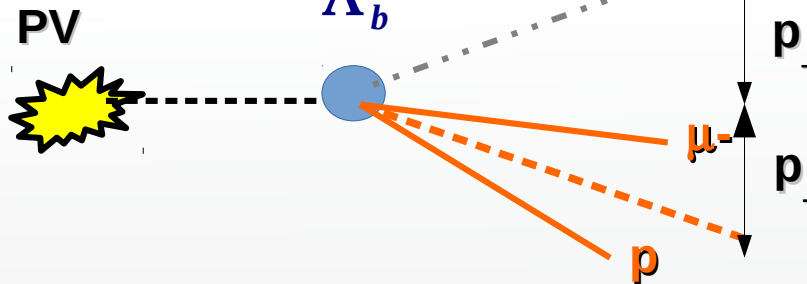
use $\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu$ as a normalization channel to minimize systematics

Derive $|V_{ub}|/|V_{cb}|$

Momentum transfer q and corrected mass as analysis variables

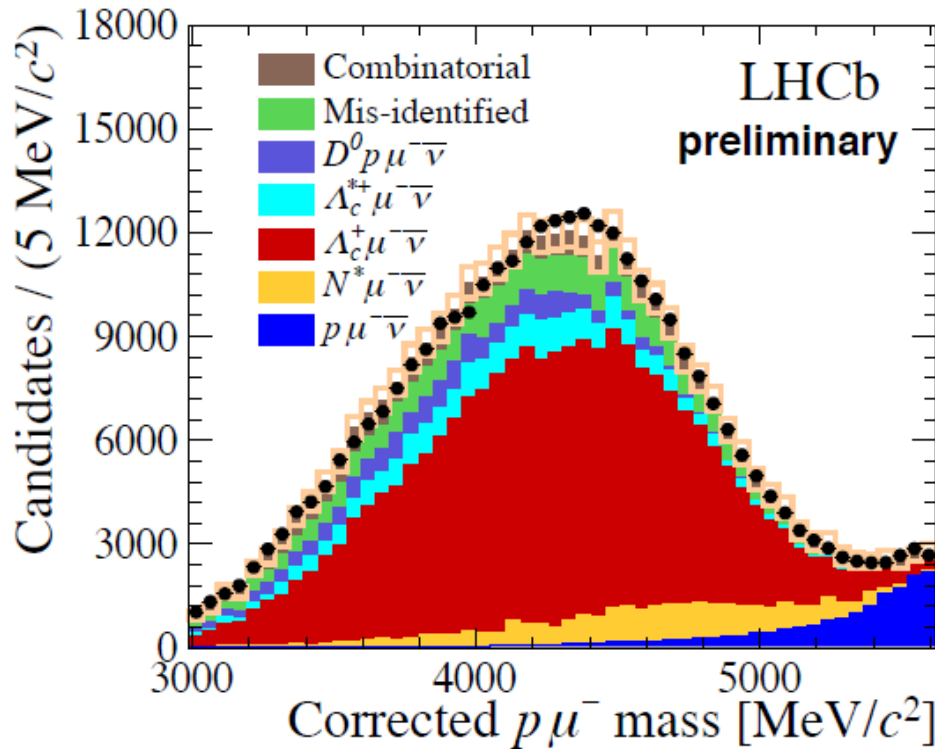
Fit corrected mass at high q^2 (better q determination)

$$M_{corr} = \sqrt{M_{p\mu}^2 + p_\perp^2 + p_\perp^2}$$

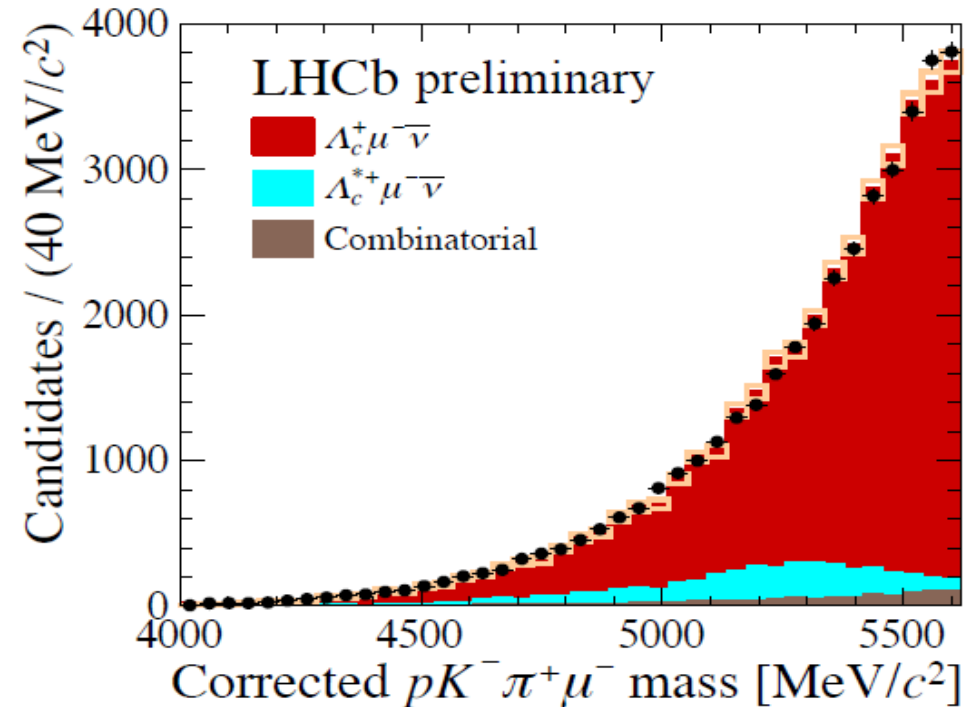


$\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu$ fits

Signal



Normalization channel $\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu$



First observation with the yield $N(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu) = 17687 \pm 733$

Yield ratio is then corrected for efficiency ratio to derive CKM elements

$$\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu - V_{ub}$$

Using result from lattice QCD calculations arXiv:1503.01421:

$$\frac{|V_{ub}|^2}{|V_{cb}|^2} = \frac{\int_{15 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu)}{dq^2} dq^2}{\int_{7 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu)}{dq^2} dq^2} (0.68 \pm 0.07)$$

One gets:

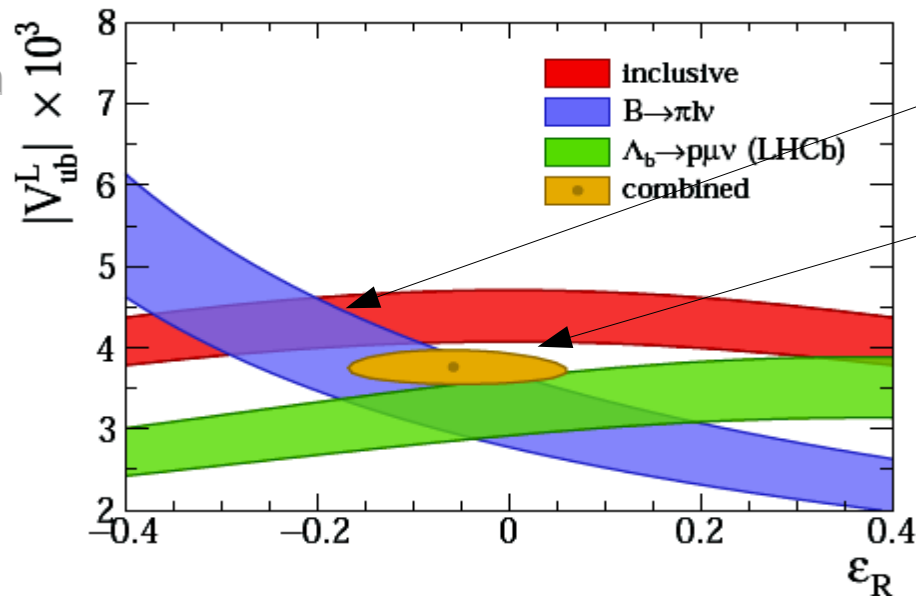
$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004(\text{expt}) \pm 0.004(\text{lattice})$$

and:

$$|V_{ub}| = (3.27 \pm 0.15(\text{exp}) \pm 0.17(\text{theory}) \pm 0.06(|V_{cb}|)) \times 10^{-3}$$

I) inclusive/exclusive mismatch confirmed

II) Fit to the fraction of right-handed current:
 $\rho_{\mu\nu}$ has different dependency from $\pi_{\mu\nu}$ due to proton spin.
 LHCb measurement does not support significant right-handed current

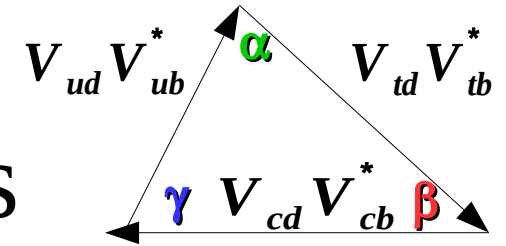


Initial overlap

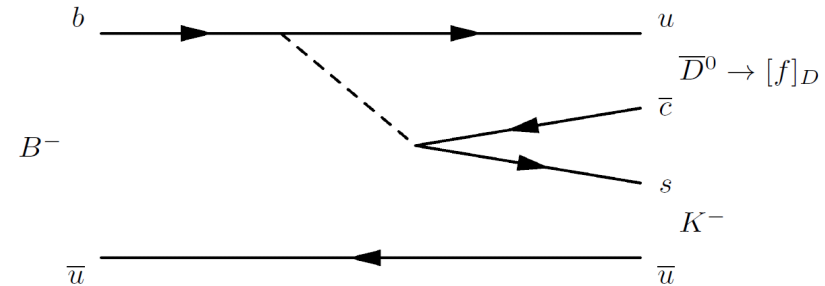
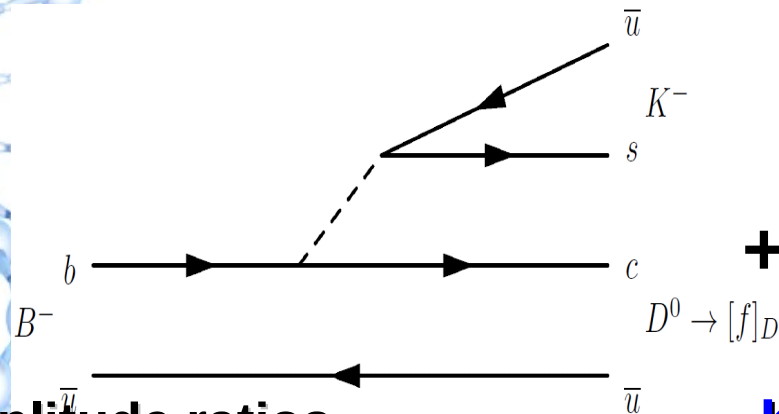
With LHCb measurement

$$\gamma = \arg\left(\frac{-V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}\right)$$

γ angle from trees

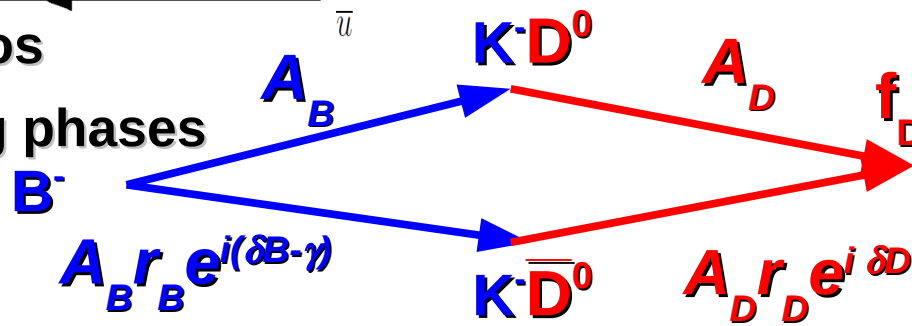


- Use interfering amplitudes in tree-level $B \rightarrow DK^{(*)}(h, hh)$ decays



r_i : amplitude ratios

δ_i : relative strong phases



In general: r_D and f_D used as external inputs (e.g. from CLEO-c data)

- Fits use ratios of allowed/suppressed BF + asymmetries
- For multibody D decays, dilution factor due to δ_D variation across phase space
- Compare to γ from loop diagrams: mismatch? BSM particles in the loop?
- Numerous LHCb analyses already published or on-going, several new channels adding up more information

We will see two recent examples of such novelties

Recently added decays modes for γ

$B^- \rightarrow D K^-$ with $D \rightarrow h^+ h^- \pi^0$ and $D \rightarrow K^+ \pi^- \pi^0$

Recent determination of CP-even contents F of $D \rightarrow h^+ h^- \pi^0$ CLEO-c, PLB740 (2015) 1

$[h^+ h^- \pi^0]K$ to $[h^+ h^- \pi^0]\pi$ ratio and $[h^+ h^- \pi^0]K$ CP asymmetries used to extract observables:

$$R(h^+ h^- \pi^0) = 1 + (r_B)^2 + (2F(h^+ h^- \pi^0) - 1) 2r_B \cos \delta_B \cos \gamma$$

$$A_{CP}(h^+ h^- \pi^0) = (2F(h^+ h^- \pi^0) - 1) 2r_B \sin \delta_B \sin \gamma / R(h^+ h^- \pi^0)$$

$B^- \rightarrow D K^- \pi \pi$ with $D \rightarrow h^+ h^-, h'^+ h^-$

Generalization of techniques from $B^- \rightarrow D K^-$ to $B^- \rightarrow D X_s$ states

$$\Gamma(B^- \rightarrow [h^- h^+]_D X_s^-) \propto 1 + r_B^2 + 2\kappa r_B \cos(\delta_B - \gamma)$$

$$\Gamma(B^+ \rightarrow [h^- h^+]_D X_s^+) \propto 1 + r_B^2 + 2\kappa r_B \cos(\delta_B + \gamma)$$

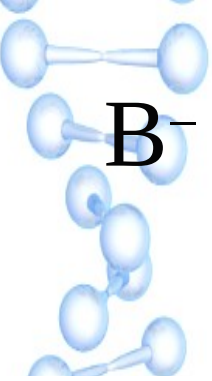
$$\Gamma(B^- \rightarrow [K^+ \pi^-]_D X_s^-) \propto r_B^2 + r_D^2 + 2\kappa r_B r_D \cos(\delta_B + \delta_D - \gamma)$$

$$\Gamma(B^+ \rightarrow [K^- \pi^+]_D X_s^+) \propto r_B^2 + r_D^2 + 2\kappa r_B r_D \cos(\delta_B + \delta_D + \gamma)$$

$$\Gamma(B^- \rightarrow [K^- \pi^+]_D X_s^-) \propto 1 + (r_B r_D)^2 + 2\kappa r_B r_D \cos(\delta_B - \delta_D - \gamma)$$

$$\Gamma(B^+ \rightarrow [K^+ \pi^-]_D X_s^+) \propto 1 + (r_B r_D)^2 + 2\kappa r_B r_D \cos(\delta_B - \delta_D + \gamma)$$

κ : dilution factor

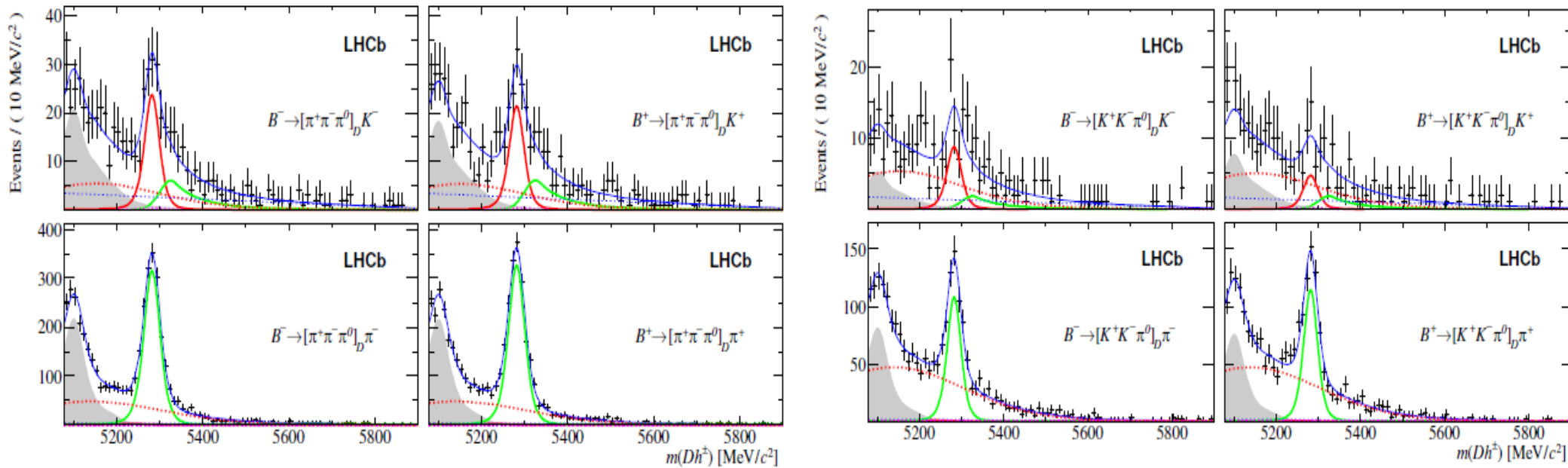


$B^- \rightarrow D K^-$ with $D \rightarrow h^+ h^- \pi^0$ and $D \rightarrow K^+ \pi^- \pi^0$

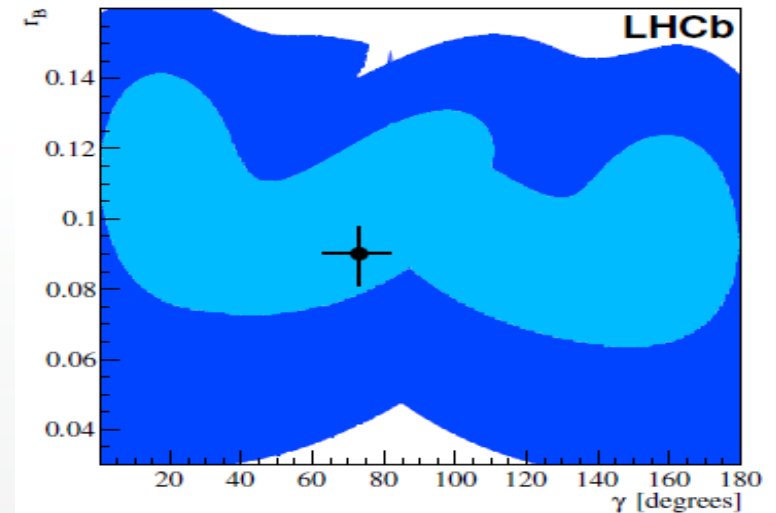
arXiv:1504.05442, PRD 91, 112014 (2015)

$D \rightarrow \pi^+ \pi^- \pi^0$

$D \rightarrow K^+ K^- \pi^0$



From CLEO-c DD data:
small dilution in $D \rightarrow K^+ \pi^- \pi^0$
High fraction of CP-even in $D \rightarrow h^+ h^- \pi^0$
Make them very adequate for γ measurement, particularly $D \rightarrow h^+ h^- \pi^0$
Final fit improves measurements obtained by B-factories



$B^- \rightarrow D K^- \pi \pi$ with $D \rightarrow h^+ h^-, h'^+ h'^-$

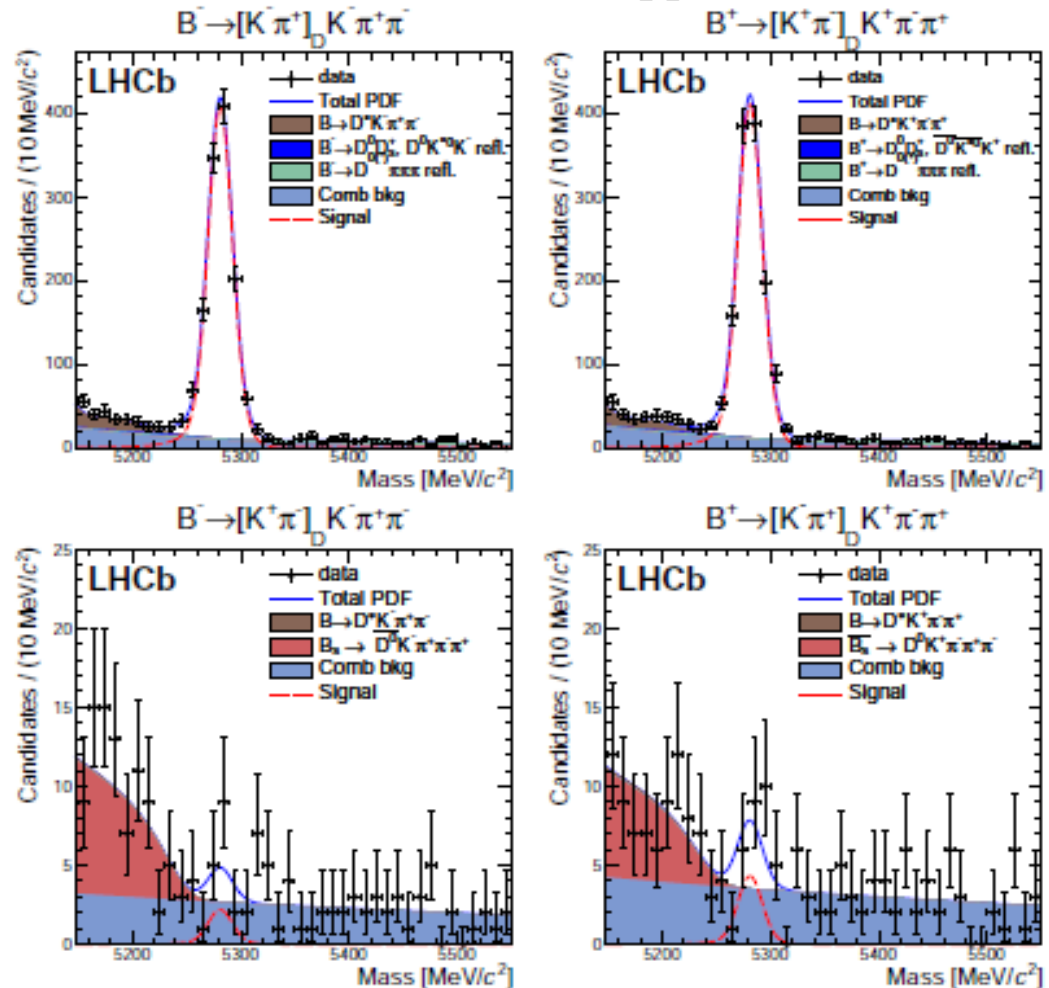
LHCb-PAPER-2015-020, arXiv:1505.07044

B^+/B^- invariant mass for the case $D \rightarrow K\pi$
 favored $K^- \pi^+$ vs suppressed $K^+ \pi^-$

Global fit for all $D \rightarrow h^+ h^-$ modes gives:

$$\gamma = (74_{-18}^{+20})^\circ$$

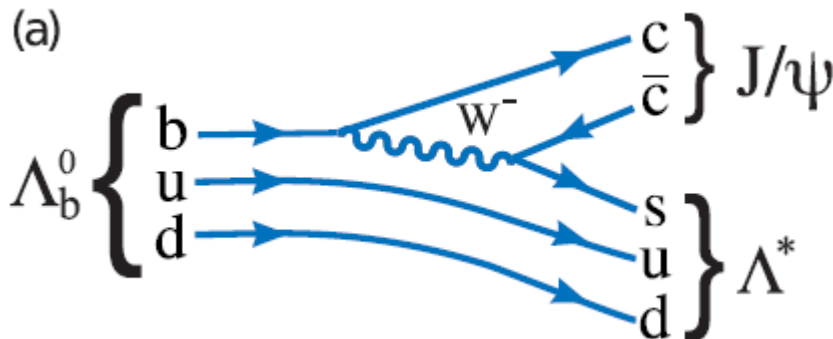
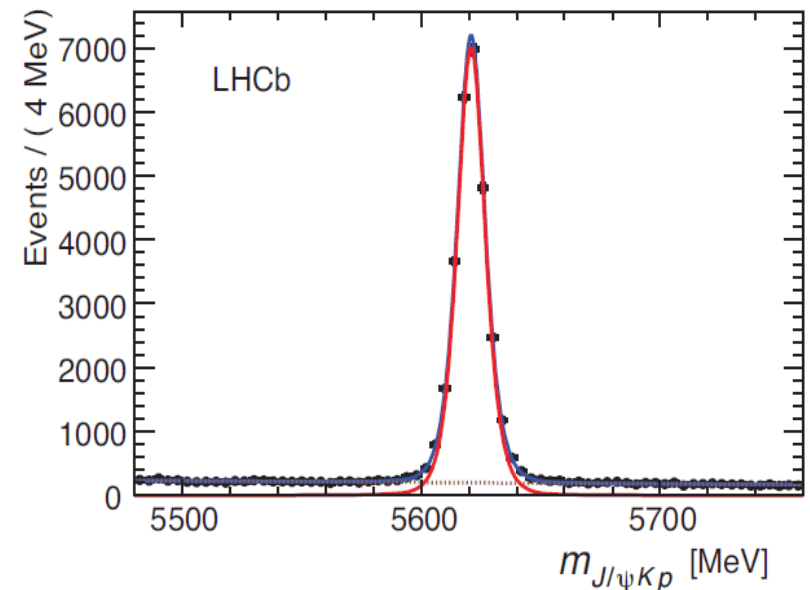
Which agrees with the global average published in LHCb-CONF-2014-004



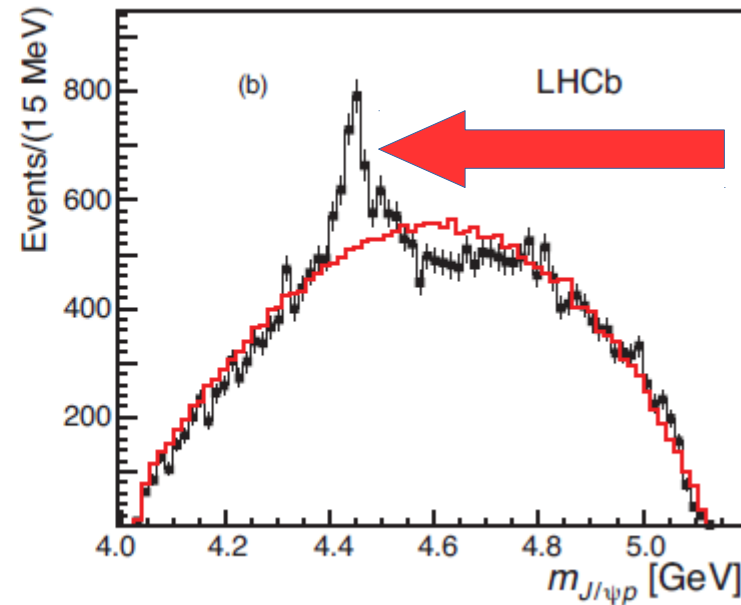
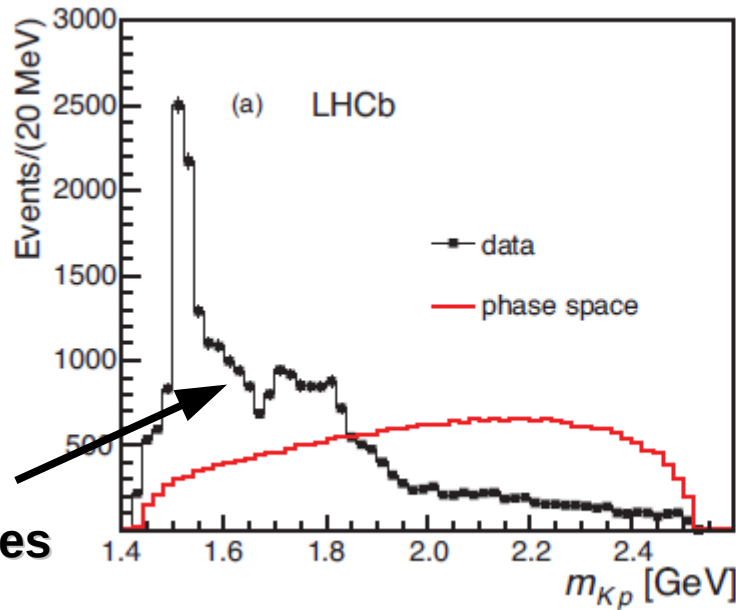
J/Ψ p pentaquark resonances in $\Lambda_b \rightarrow J/\Psi K^- p$

- Hypothesis of hadrons with more than three quarks raised 50 years ago (Gell-Mann, Phys. Lett. 8 (1964) 214 + later works of Jaffe, Strottman and Lipkin)
- A lot of past claims of pentaquark ended up not convincing (Eur. Phys. J.H37(2012) 1)
- One strong tetraquark candidate: Z(4430)⁺ observed in $\bar{B}^0 \rightarrow \Psi' K^- \pi^+$ decays (Belle, then LHCb)
- A priori $\Lambda_b \rightarrow J/\Psi(\mu\mu) K^- p$ are expected to proceed dominantly through $\Lambda_b \rightarrow J/\Psi(\mu\mu) \Lambda^*$

$\Lambda_b \rightarrow J/\Psi K^- p$ signal in data



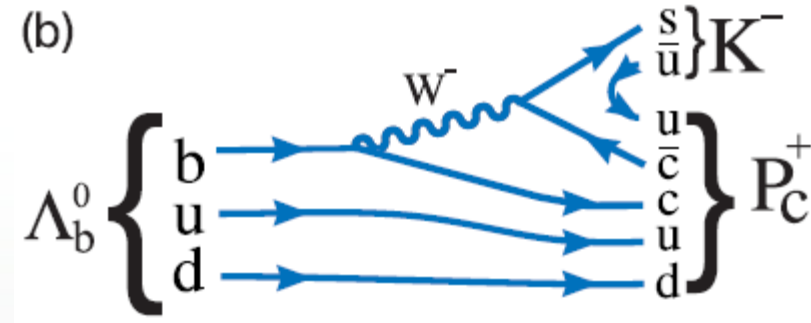
Looking at invariant masses in $\Lambda_b \rightarrow J/\Psi K^- p$



Λ and Σ resonances

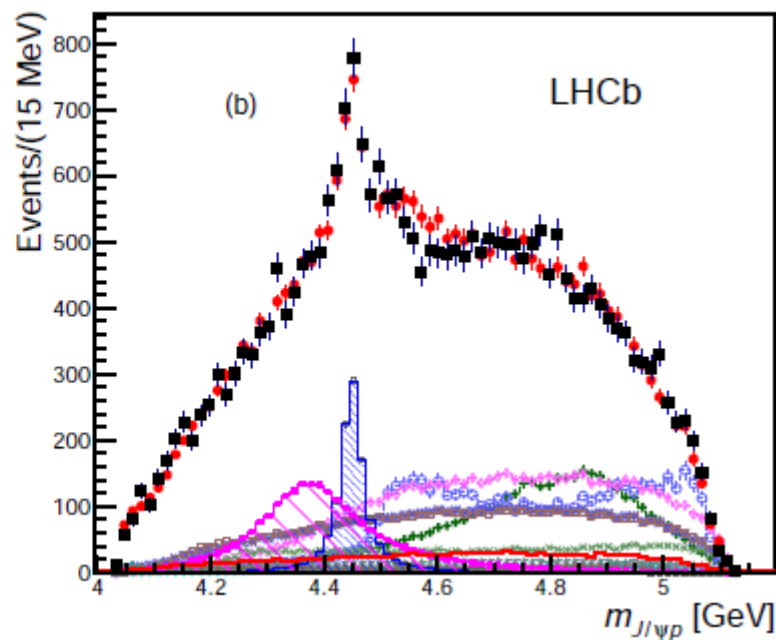
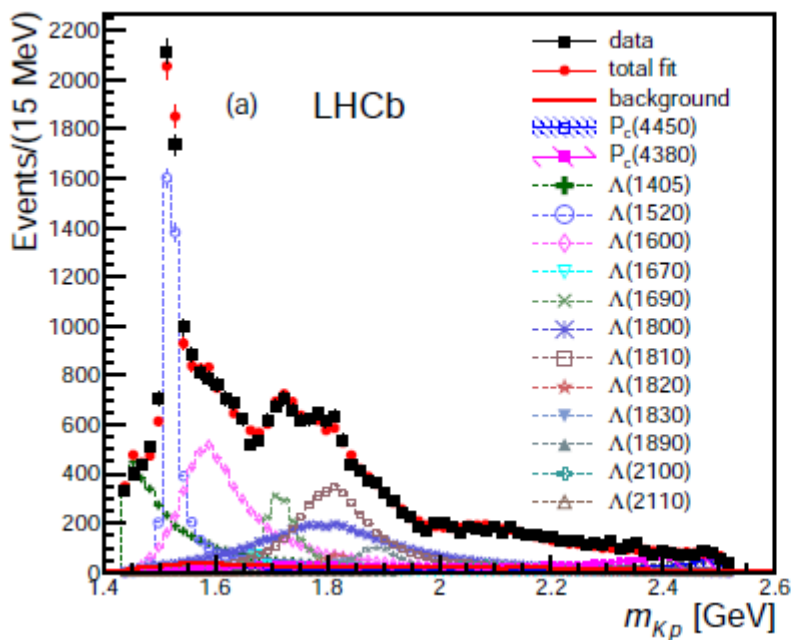
$J/\Psi p$ resonances should have a minimal quark content of $c\bar{c}uud$, i.e. charmonium pentaquark, labelled as P_c^+

Full amplitude analysis performed to check that these are not reflections from Λ^*



Amplitudes in $\Lambda_b \rightarrow J/\Psi K^- p$

Full fit includes 2 invariant masses and 5 decay angles!



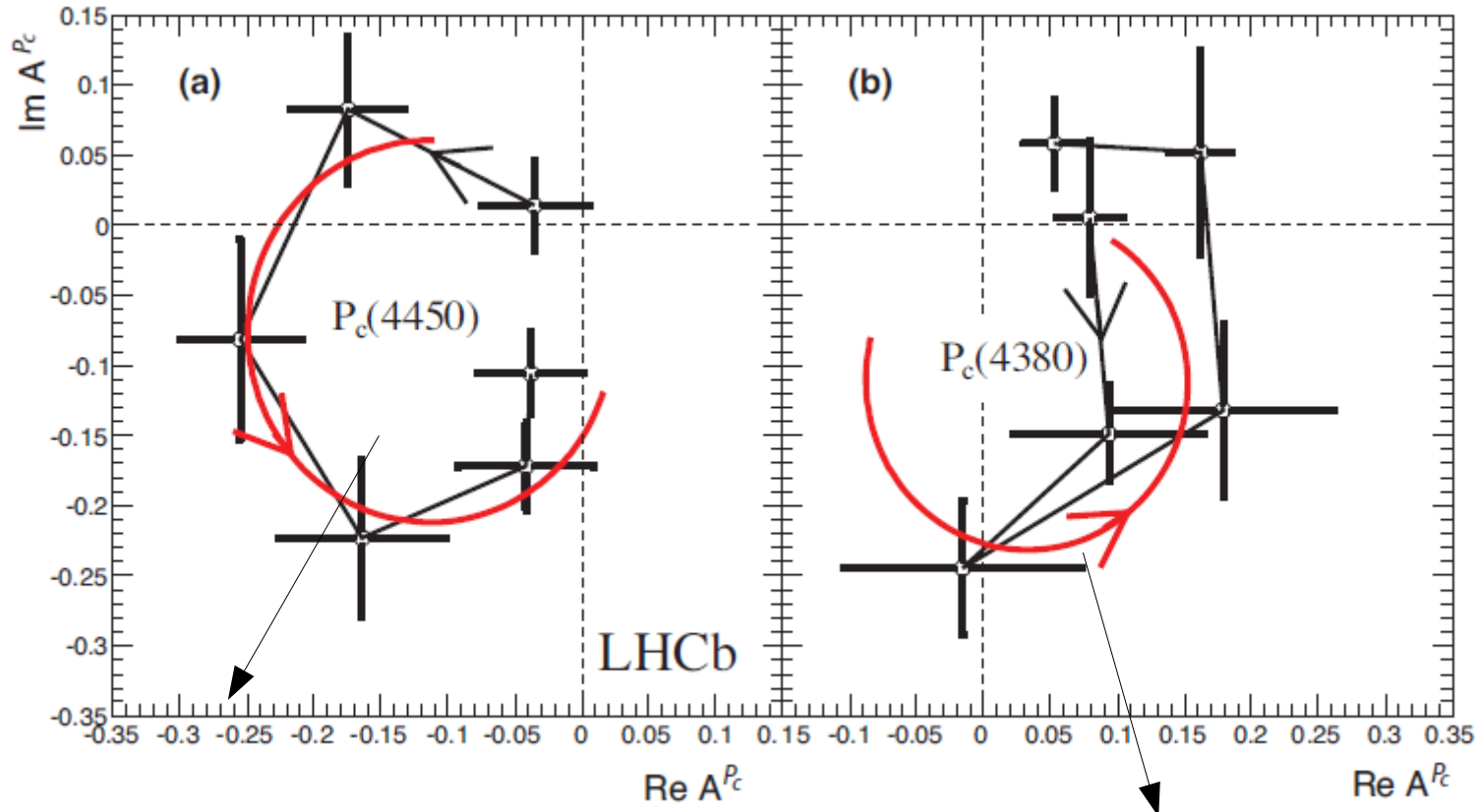
Minimal content for correct convergence/quality found to be 14 Λ^* states + 2 P_c^+ resonances, $P_c^+(4380)$ and $P_c^+(4450)$

Masses: $4380 \pm 8 \pm 29$ MeV and $4449.8 \pm 1.7 \pm 2.5$ MeV

Widths: $205 \pm 18 \pm 86$ MeV and $39 \pm 5 \pm 19$ MeV

Spin-parity: best fit gives $(3/2^-, 5/2^+)$ but $(3/2^+, 5/2^-)$ and $(5/2^+, 3/2^-)$ also acceptable solutions

P_c^+ argand diagrams

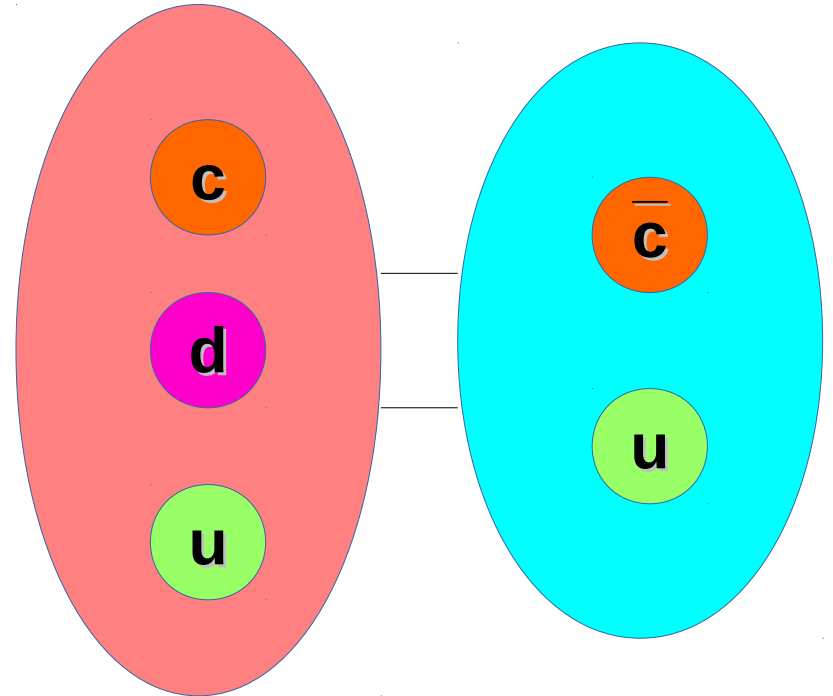
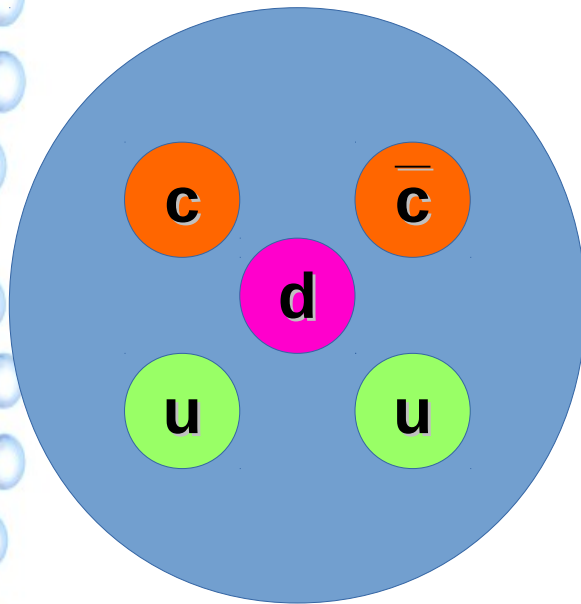


Very conclusive!

Because of wider state, amplitude is more sensitive to the details of modeling of Λ^*

Although many tests have been performed to insure the robustness of the results, further work is being performed

P_c^+ detailed structure?



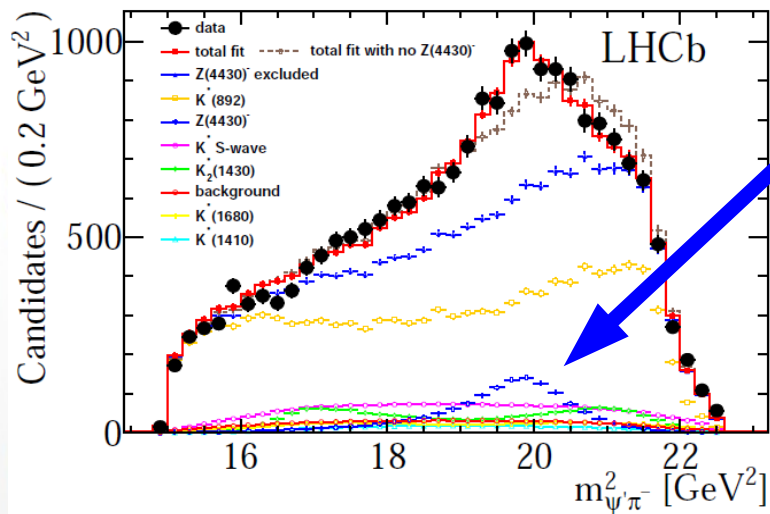
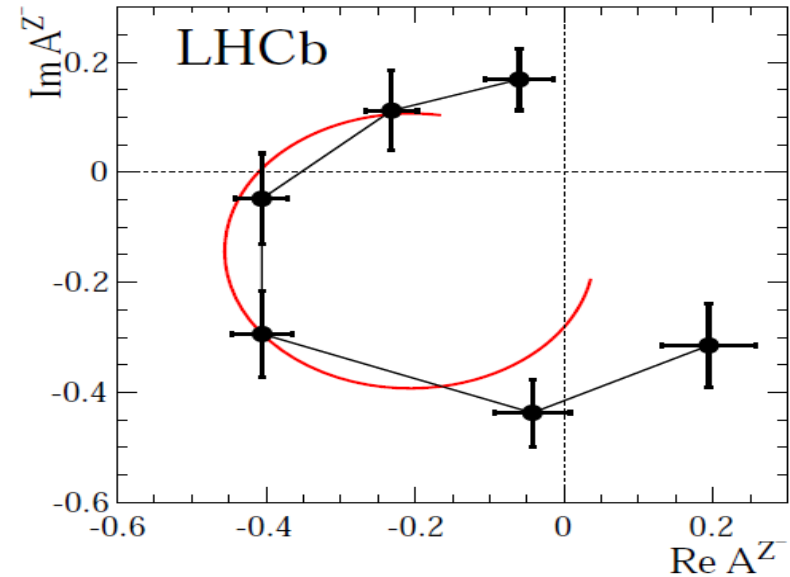
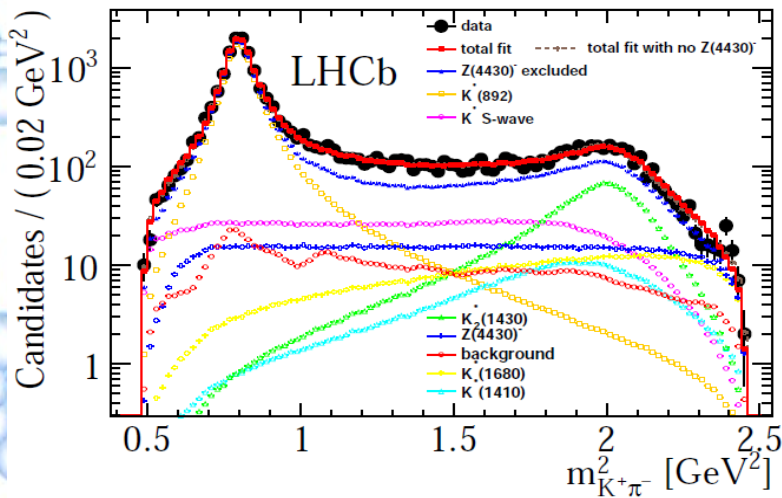
Tight bounds? Molecular?

Tetraquark $Z(4430)^-$ in $B^0 \rightarrow \Psi' \pi^- K^+$

Already observed by Belle, resonant character was not established

4D amplitude analysis converge to $J^P = 1^+$

LHCb uses a sample of 25k signal events (vs 2k for B-factories)



Z(4430)

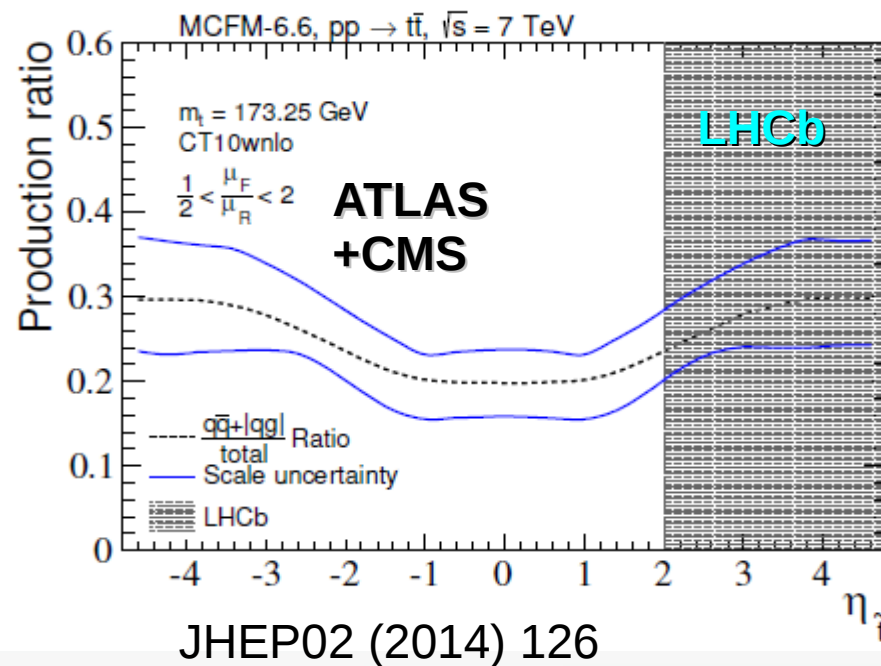
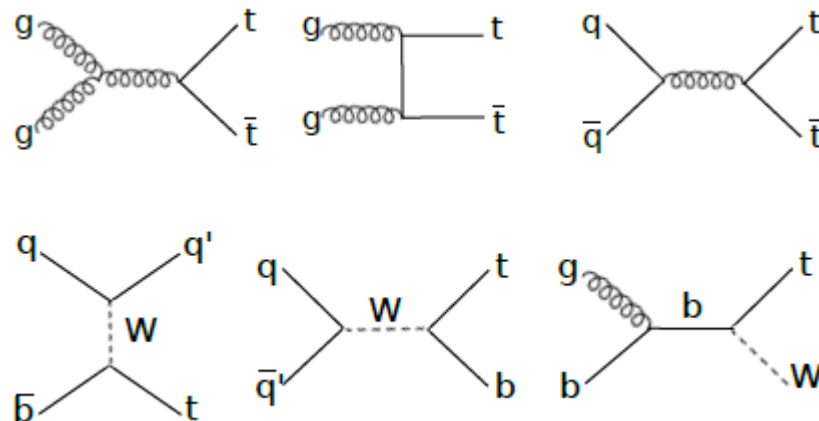
Mass: $4475 \pm 7^{+15}_{-25}$ MeV

Width: $172 \pm 13^{+37}_{-34}$ MeV

Remark: both P_c and Z contain charmonium

Top quark

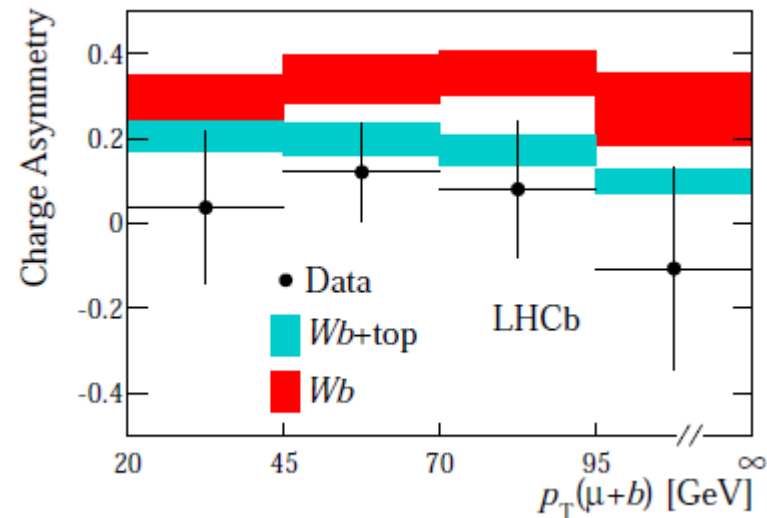
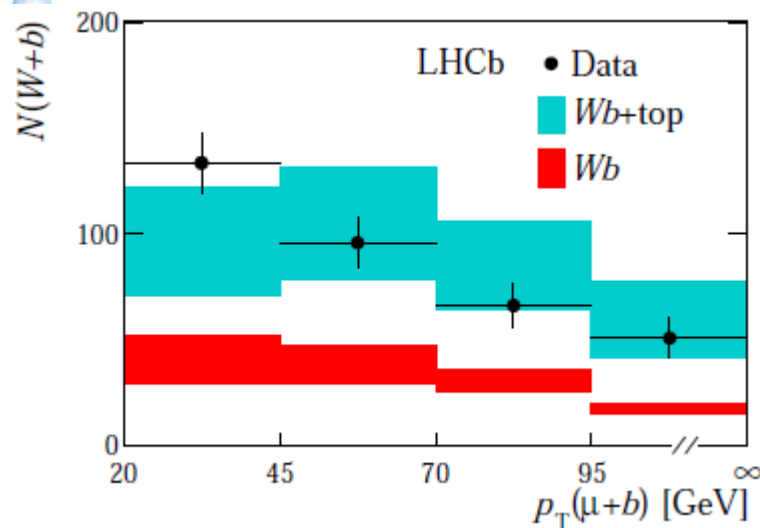
- $t\bar{t}$ and single top physics extensively explored by ATLAS and CMS in the central region
- LHCb will complete the knowledge at high pseudorapidities



Top in LHCb (LHCb-PAPER-2015-022)

arXiv:1506.00903

- Searched for in W(left) + b-jet events
- Use W + j-jet events as normalization
- MVA discrimination to discard light + c jets
- Compare W+b yield and asymmetry with expectations with and without top



5.4 σ (first) observation of top production in the forward region

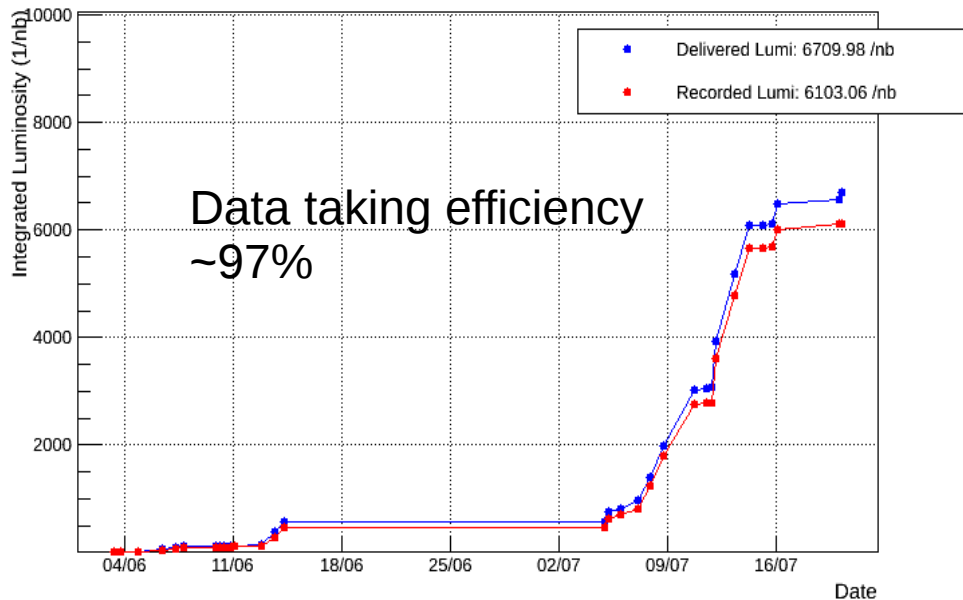
$$\sigma(\text{top})[7 \text{ TeV}] = 239 \pm 53 (\text{stat}) \pm 38 (\text{syst}) \text{ fb}$$

$$\sigma(\text{top})[8 \text{ TeV}] = 289 \pm 43 (\text{stat}) \pm 46 (\text{syst}) \text{ fb}$$

Current data taking (Run II)

Run II has begun!
Higher CM energy + small bunch spacing (25 ns) = data rate \uparrow
Finished 50 ns bunch spacing run

LHCb Integrated Luminosity at p-p 6.5 TeV in 2015



About $\sim 6 \text{ pb}^{-1}$ @ 13 TeV already taken,
25 ns data taking will start soon

New trigger flow: **calibrations**
performed between High
Level Triggers 1 and 2

LHCb 2015 Trigger Diagram

40 MHz bunch crossing rate

L0 Hardware Trigger : 1 MHz readout, high E_T/P_T signatures

450 kHz
 h^\pm

400 kHz
 $\mu/\mu\mu$

150 kHz
 e/γ

Software High Level Trigger

Partial event reconstruction, select displaced tracks/vertices and dimuons

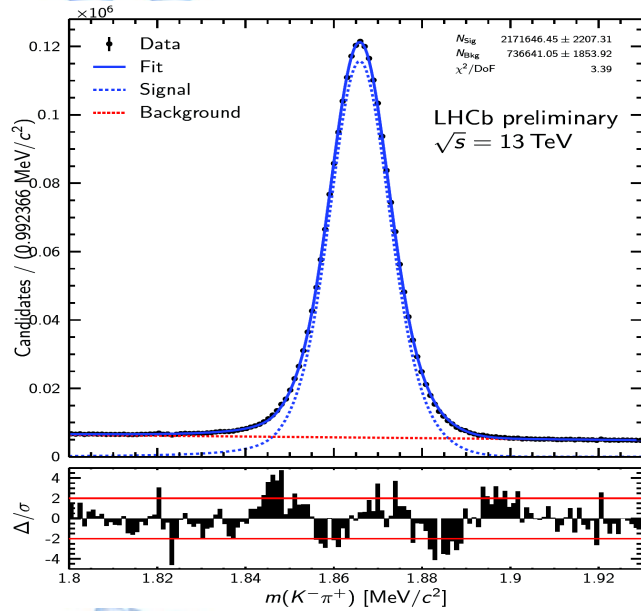
Buffer events to disk, perform online detector calibration and alignment

Full offline-like event selection, mixture of inclusive and exclusive triggers

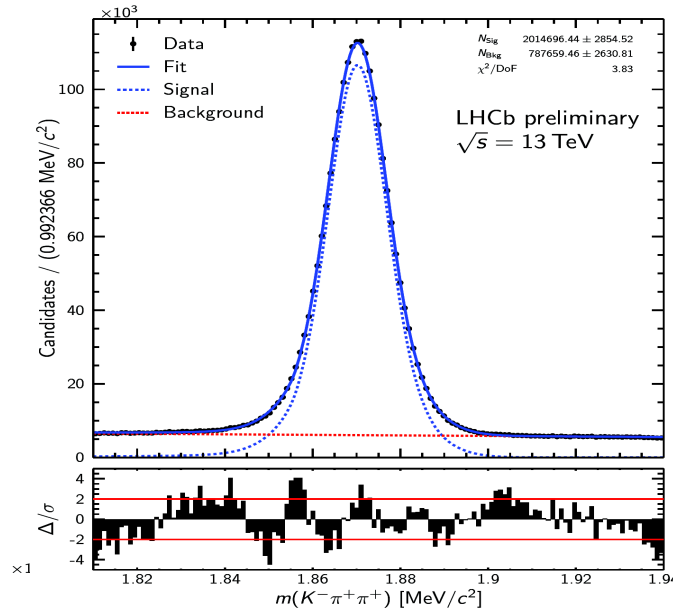
12.5 kHz Rate to storage

Early signals from first Run II data

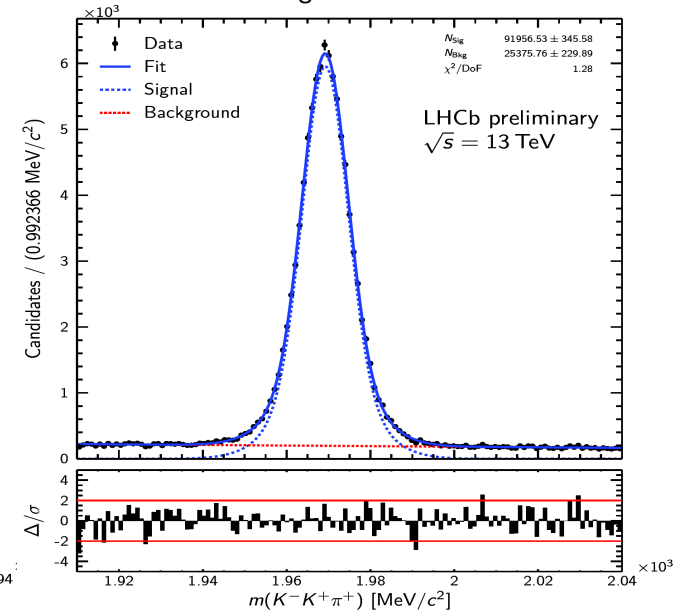
$D^0 \rightarrow K\pi$



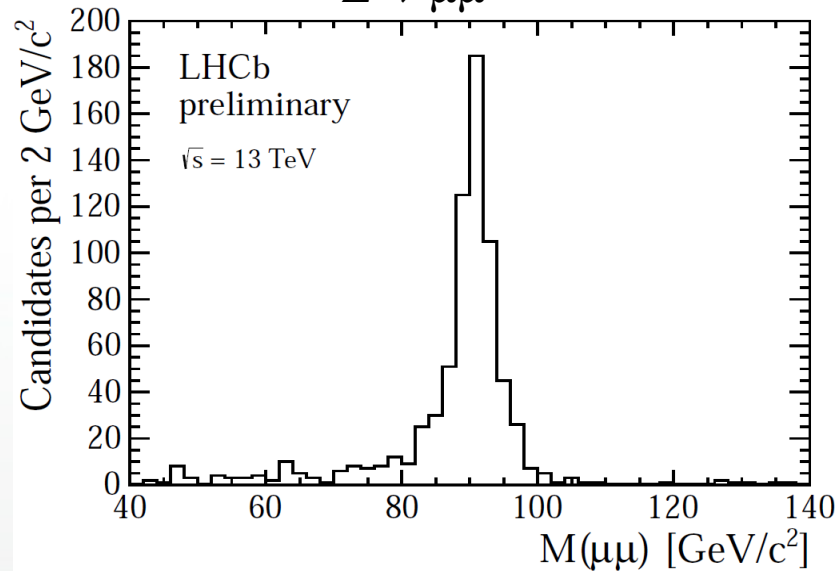
$D^+ \rightarrow K\pi\pi$



$D_s \rightarrow KK\pi$



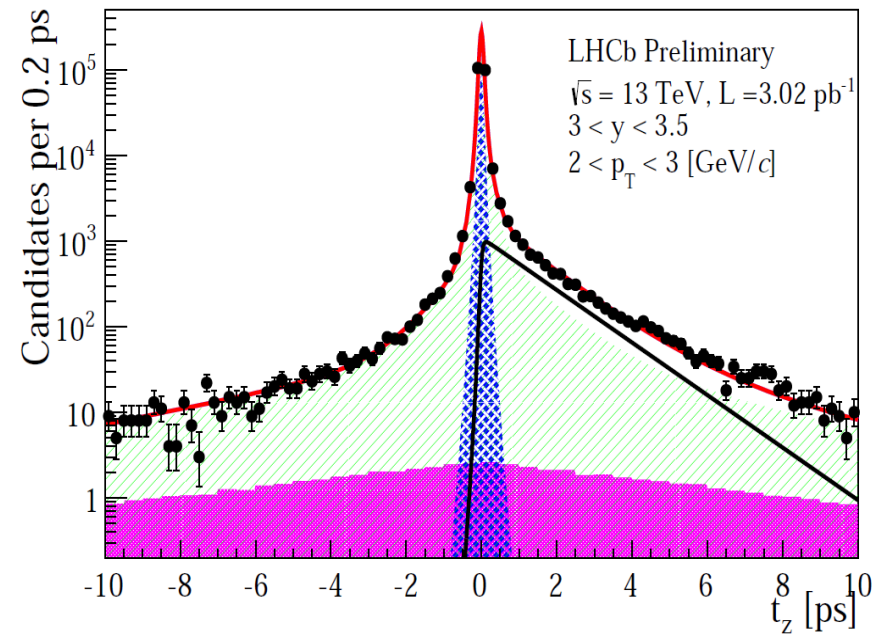
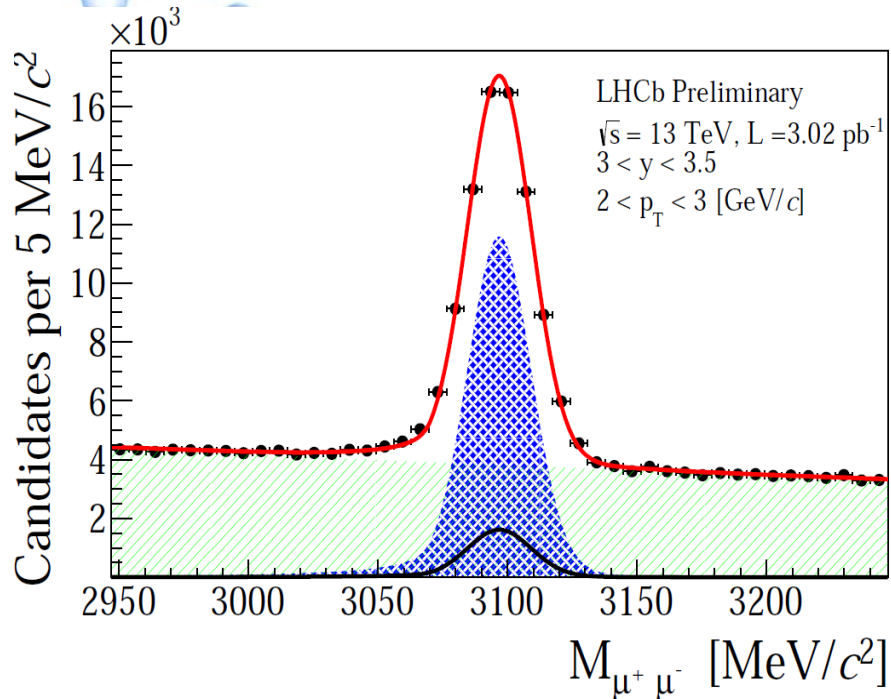
$Z \rightarrow \mu\mu$



Early measurements from first Run II data

LHCb-PAPER-2015-037

J/Ψ cross-sections @ $\sqrt{s} = 13$ TeV
 Measured prompt + component from b decays



J/Ψ from b, **prompt J/Ψ** , **background**, **wrong PV association (tails)**

$$\sigma(\text{prompt } J/\psi) = 15.35 \pm 0.03 \text{ (stat)} \pm 0.85 \text{ (syst)} \mu\text{b}$$

$$\sigma(J/\psi \text{ from } b) = 2.36 \pm 0.01 \text{ (stat)} \pm 0.13 \text{ (syst)} \mu\text{b.}$$

In LHCb acceptance

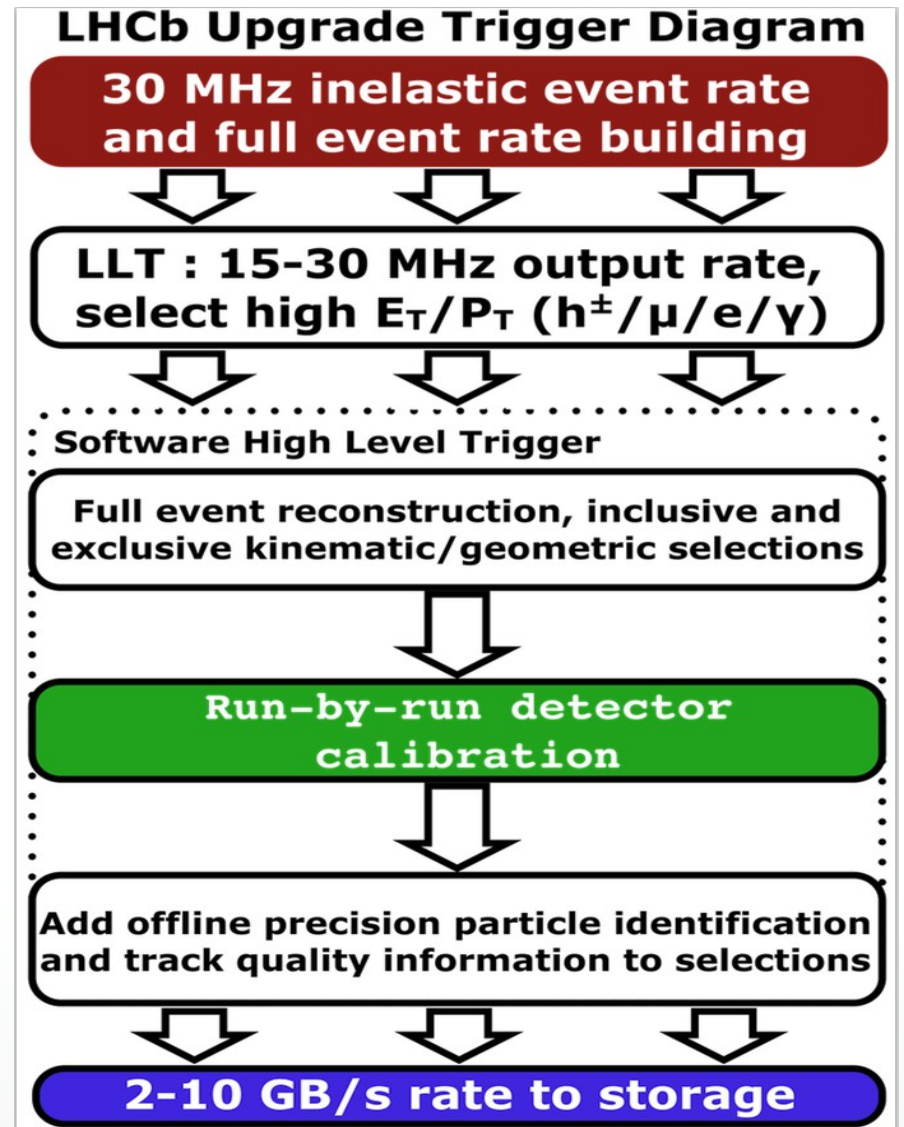
Using acceptance rescaling from Pythia + $b \rightarrow J/\Psi X$ BF from PDG:

$$\sigma(pp \rightarrow b\bar{b}X) = 518 \pm 2 \text{ (stat)} \pm 53 \text{ (syst)} \mu\text{b}$$

Upgrade

(see A.Schopper Wed 05/08)

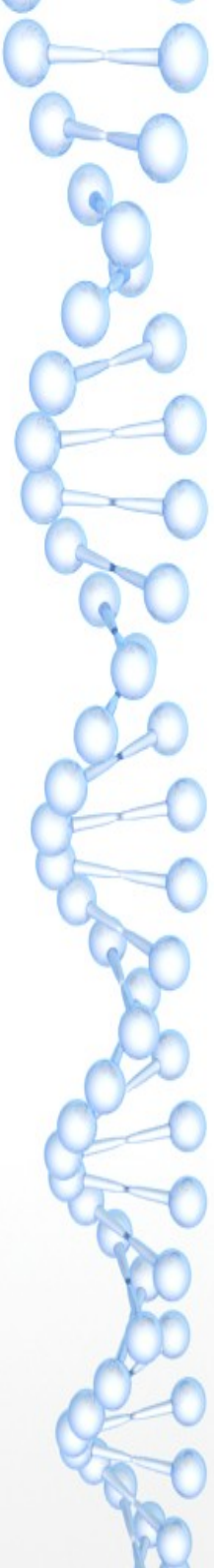
- Planned during LS2 (2019-2020)
 - Prepare for acquisition of 50 fb^{-1}
- Detectors:
 - full upgrade of the tracking system
 - new RICH (Particle ID) detectors
 - Calorimeters and muon system: new electronics, more shielding, etc...
- Triggering: full software trigger
 - This removes the limitation of the L0 Hardware trigger (1 MHz)





Summary

- **A big variety of results released in all aspects of the physics program**
 - **Pushing the SM further in the corners and hunt for intervention of NP: e.g., persisting discrepancies in some observables of rare decays**
 - **New quark bound states**
 - **Direct searches are now ramping up as part of forward physics studies**
- **Very promising first Run II data taking: the detector is running Ok, fast and efficient data acquisition and analysis with the new streaming model**
 - **First paper draft ready almost immediately after data taking**
 - **Very exciting prospects ahead for the coming 25 ns running**
- **Preparation for upgrade is well advanced and most of the R&D phases are now achieved**



Backup



γ from $B \rightarrow DK$, different techniques

- $f_D =$ CP eigenstates, $D^0 \rightarrow K^+K^-, \pi^+\pi^-, K_S\pi^0$
 - Gronau, London, Wyler (GLW) 1991
- $f_D =$ flavour states: $D^0 \rightarrow K^+\pi^-, K^-\pi^+$
 - Atwood, Dunietz, Soni (ADS) 1997
- $f_D =$ multibody final states (variation of δ_D over phase space)
 - $K_S h^+ h^-$ Giri, Grossman, Soffer, Zupan 2003; Poluektov 2004 (GGSZ-P)
 - $K^\pm \pi^{-/+} \pi^+ \pi^-$, multibody ADS
 - $K_S K^\pm \pi^{-/+}$, GLS
- Some variants involving neutrals, B^0 and B_s

Observables: charge asymmetries and BF ratios of suppressed/favoured D decays (applies for self-tagging decays)

γ from trees

Case of $D^0 \rightarrow K\pi^+$ (Cabibbo Allowed), $D^0 \rightarrow K\pi^-$ (double Cabibbo Suppressed)

$$R_h^\pm = \frac{\Gamma(B^\pm \rightarrow D_{DCS} h^\pm)}{\Gamma(B^\pm \rightarrow D_{CA} h^\pm)} = \frac{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D \pm \gamma)}{1 + (r_B r_D)^2 + 2r_B r_D \cos(\delta_B - \delta_D \pm \gamma)}$$

For multibody decays, must take into account the interference term between the two amplitudes in the D meson phase space, using a coherence factor κ_D

PRD68 (2003) 033003, arXiv:hep-ph/0304085

$$2r_B r_D \cos(\delta_B + \delta_D \pm \gamma) \rightarrow 2r_B r_D \kappa_D \cos(\delta_B + \delta_D \pm \gamma)$$