



# Medium-Modified Fragmentation Functions

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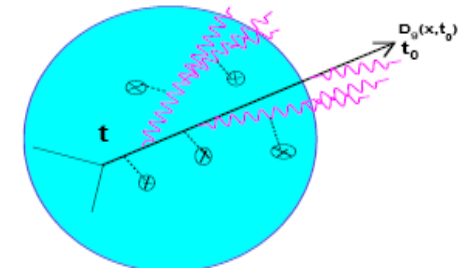


# Outline

- Medium induced gluon radiation
- Medium modified splitting functions
- Medium modified Sudakov form factor
- Medium modified fragmentation functions
- Nuclear modification factor
- Conclusions

# Medium induced gluon radiation

- A hard parton produced in the early stage of Heavy Ion Collisions travels through the hot and dense QCD matter. The scattering centers induce successive gluon radiations.
- The hard parton loses virtuality from the initial scale  $t$  to the final hadronization one  $t_0 \simeq \lambda_{QCD}^2$ . Hadronization happens outside the medium.
- Medium induced gluon radiation is the standard explanation for Jet Quenching observed at RHIC.



- The single inclusive distribution of medium induce gluons with energy  $\omega$  and transverse momentum  $k_t$  from a parent parton of energy E:

$$\omega \frac{dI}{d\omega dk_T} = \frac{\alpha_S C_R}{(2\pi)^2 \omega^2} 2 \text{Re} \int_0^\infty dy_l \int_{y_l}^\infty d\bar{y}_l du e^{-i_T u} e^{-\frac{1}{2} \int_{y_l}^\infty d\zeta n(\zeta) \sigma(u)}$$

$$\frac{\partial}{\partial y} \frac{\partial}{\partial u} \int_{y=0=r(y_l)}^{u=r(\bar{y}_l)} \mathcal{D}r e^{i \int_{y_l}^{\bar{y}_l} d\zeta \frac{\omega}{2} (r^2 - \frac{n(\zeta) \sigma(r)}{i\omega})}$$

- Two approximations

✓ Opacity expansion, in powers of  $n(\zeta) \sigma(\zeta)$  .

✓ multiple soft scattering:  $n(\zeta) \sigma(r) \simeq \frac{1}{2} \hat{q}(\zeta) r^2$  , **the path integral is one of a harmonic oscillator.**

■  $\hat{q}(\zeta)$  is the transport coefficient,  $\langle q_T^2 \rangle / \lambda$

■ The  $\omega \frac{dI}{d\omega dk_T} \longrightarrow F(\frac{\omega}{\omega_c}, \kappa^2)$ ,  $\omega_c = \frac{1}{2} \hat{q} L^2$ ,  $\kappa^2 = \frac{k_T^2}{\hat{q} L}$

# Previous MMFF calculations

- A Poissonian distribution of independent radiations was assumed by BDMPS

$$P_E(\epsilon) = \sum_{n=0}^{\infty} \frac{1}{n!} [\prod_{i=1}^n \int d\omega_i \frac{d((\omega_i))}{d\omega}] \delta(\epsilon - \sum_{i=1}^n \frac{\omega_i}{E}) e^{-\int d\omega \frac{dI}{d\omega}}$$

- The MMFF were calculated shifting the vacuum ones

$$D_{kh}^{(med)}(z, Q^2) = \int_0^1 d\epsilon P_E(\epsilon) \frac{1}{1-\epsilon} D_k(\frac{z}{1-\epsilon}, Q^2)$$

- Limitations

- ✓ The energy and momentum are not conserved
- ✓ There is no evolution in virtuality
- ✓ The medium and vacuum are treated differently

# Now Medium modified splitting functions

- The total medium-induced gluon radiation spectrum:

$$\omega \frac{dI}{d\omega dk_{\perp}} = \omega \frac{dI^{vac}}{d\omega dk_{\perp}} + \omega \frac{dI^{med}}{d\omega dk_{\perp}}$$

- The vacuum case  $\frac{dI^{vac}}{dz dk_T^2} = \frac{\alpha_s P(z)_{z \rightarrow 1}^{vac}}{2\pi k_T^2}$ ,  $P(z)_{z \rightarrow 1}^{vac} \simeq \frac{2C_R}{1-z}$ ,  $z = 1 - x$

- The ansatz is an extension of the former vacuum one to medium case:  
[Salgado and Polosa \(hep-ph/0607295\)](#)

$$\frac{dI^{MED}}{dz dk_T^2} = \frac{\alpha_s P(z)_{z \rightarrow 1}^{MED}}{2\pi k_T^2}, \quad P(z)_{z \rightarrow 1}^{med} = \frac{2\pi z t}{\hat{q}L} F\left(\frac{\omega}{\omega_c}, \kappa^2\right)$$

- The total splitting distribution is assumed to be the **vacuum+medium** ones:

$$P^{TOTAL}(z) = P^{VACUUM}(z) + P^{MEDIUM}(z)$$

# Sudakov form factor

- The sudakov factor

$$\Delta_a(t, t_0^a) = e^{-\sum_{a-cc'} \int_{t_0^a}^t \frac{dt'}{t'} \int_{z_{min}(t')}^{1-z_{min}(t')} dz \frac{\alpha_S(t', z)}{2\pi} P_{ca}(z)}$$

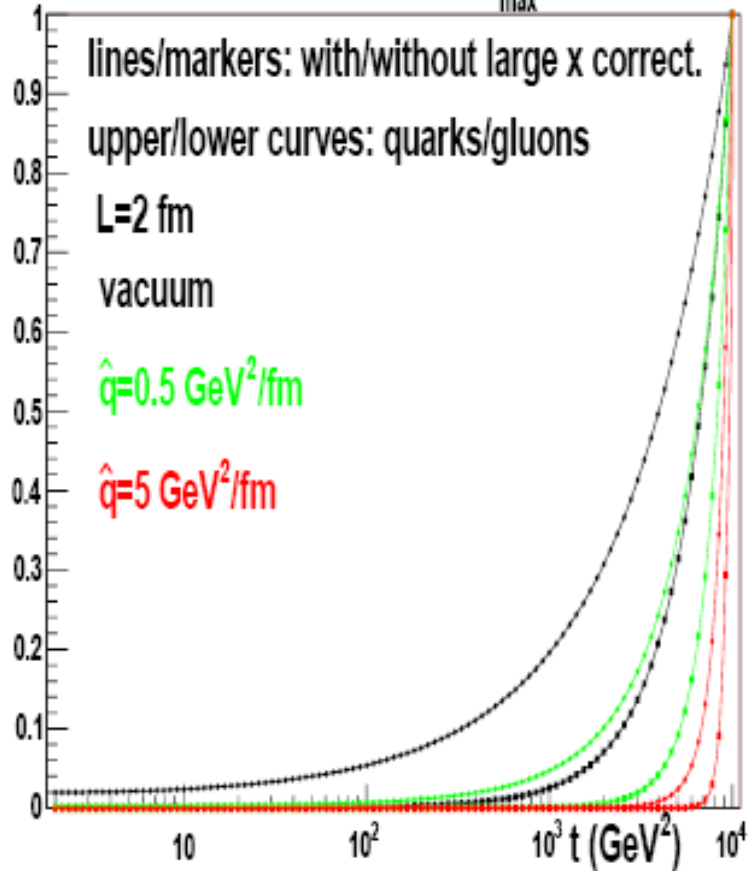
- $\Delta_a(t, t_0^a)$  means the probability for a parton not to branch while evolving from an initial virtuality  $t$  to a final scale  $t_0$

- We modify the sudakov factor:

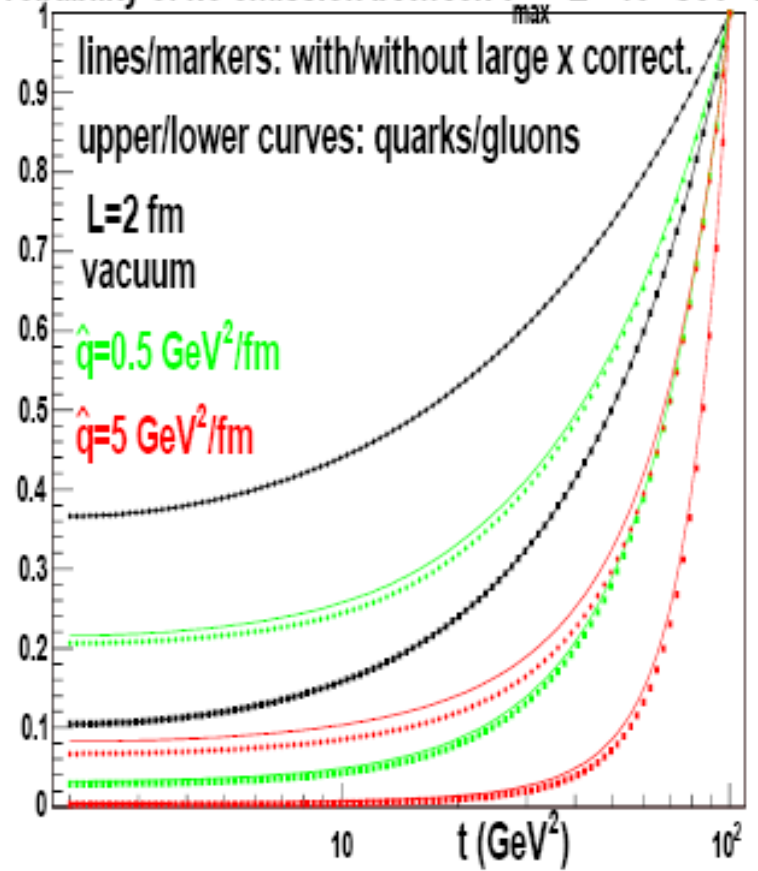
$$\Delta_a(t, t_0^a) = e^{-\sum_{a-cc'} \int_{t_0^a}^t \frac{dt'}{t'} \int_{z_{min}(t')}^{1-z_{min}(t')} dz \frac{\alpha_S(t', z)}{2\pi} (P_{ca}(z)^{vac} + P_{ca}(z)^{med})}$$

# Medium modified sudakov factor

Probability of no emission between  $t_{\text{min}} = E^2 = 10^4 \text{ GeV}^2$  and  $t_{\text{max}}$



Probability of no emission between  $t_{\text{min}} = E^2 = 10^2 \text{ GeV}^2$  and  $t_{\text{max}}$





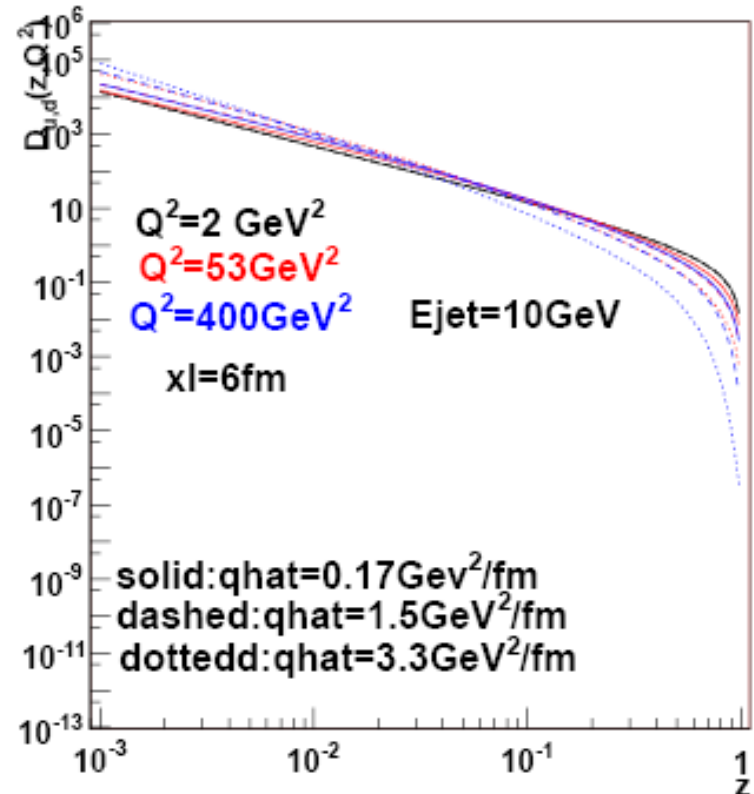
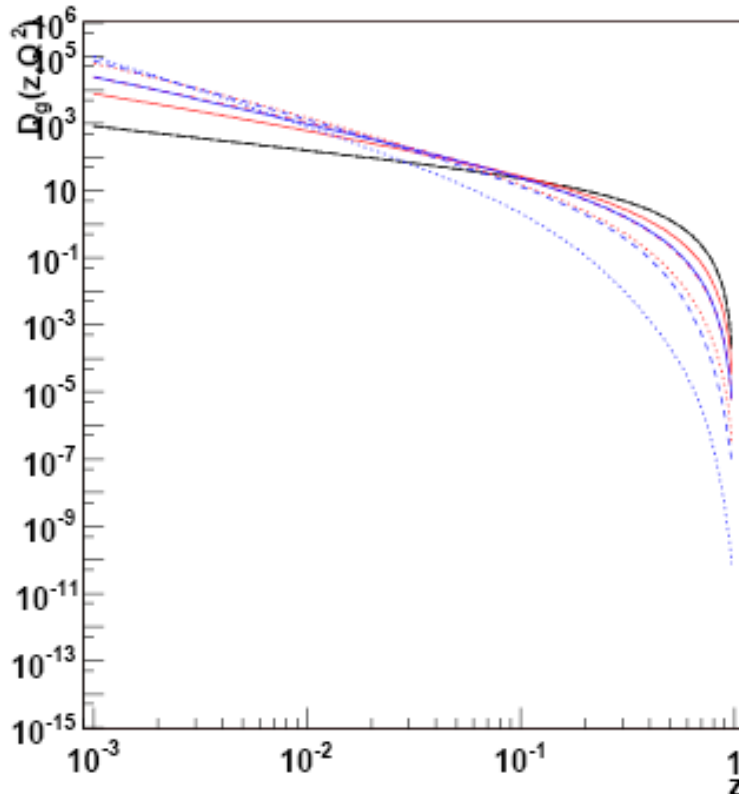
# Medium modified fragmentation functions

- DGLAP evolution equation can be written in terms of the sudakovs:

$$t \frac{\partial}{\partial t} \left( \frac{D_a^h(x, t)}{\Delta_a(t, t_0^a)} \right) = \int_x^{1-z_{\min}(t)} \frac{dz}{z} \frac{\alpha_S(k_T^2, z)}{2\pi} P_{ba}(z) \frac{D_b^h(\frac{x}{z}, t)}{\Delta_a(t, t_0^a)}$$

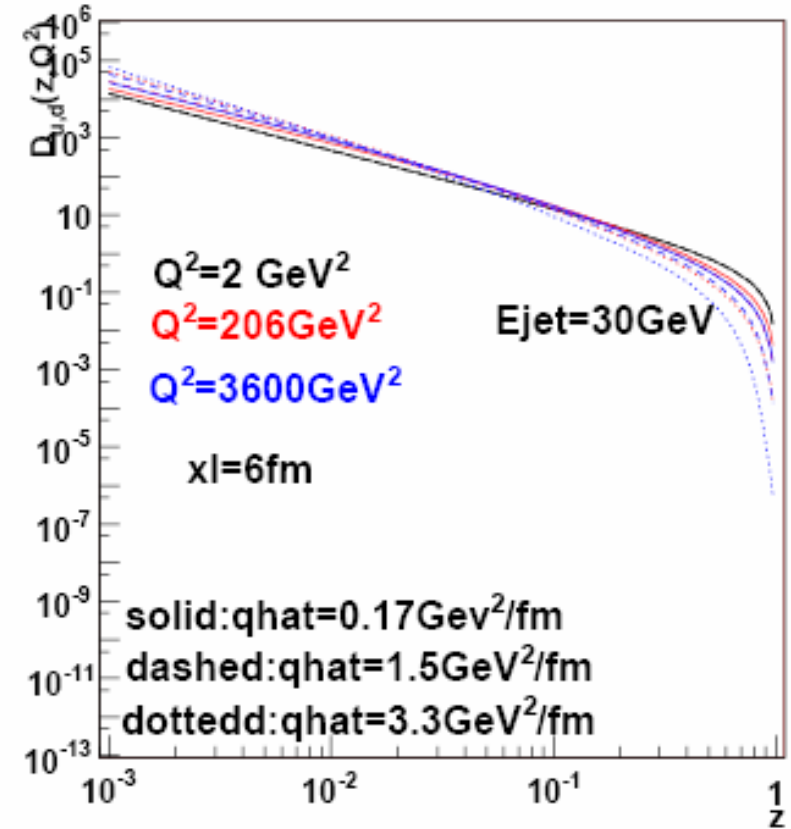
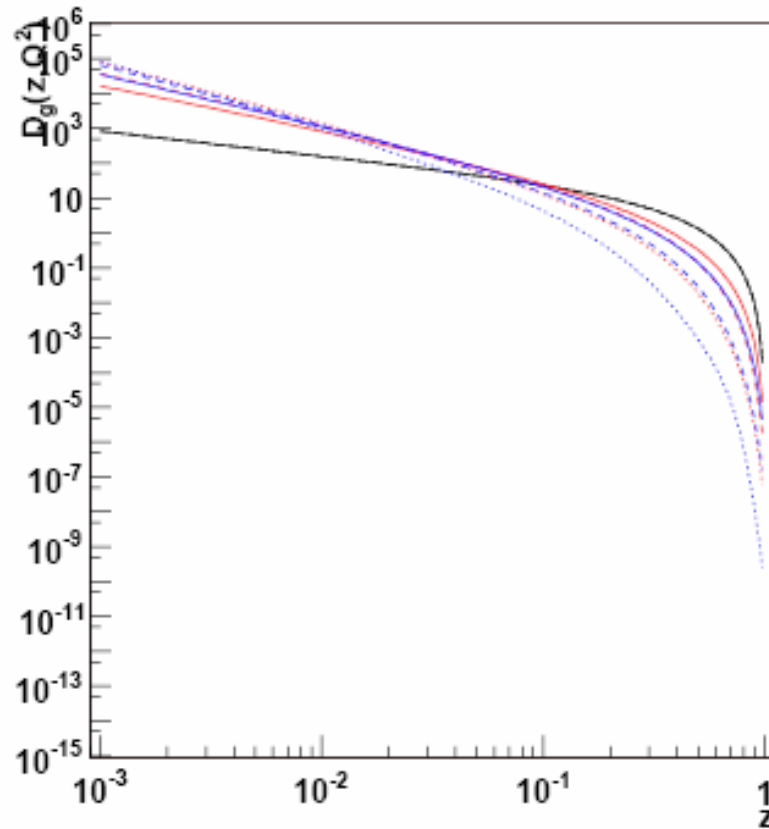
- The renormalization scale is  $t(1-z)z = k_T^2$
- The initial values for the FF we take the KKP ones at virtuality  $t$
- For each parton energy,  $t_0 = 2\text{GeV}^2$   $t_0 < t < 4E^2$  and  $t_0/t < z(t) < 1 - t_0/t$
- Our evolution depends on the initial parton energy through the scale range in the Sudakov.

# Medium modified fragmentation functions



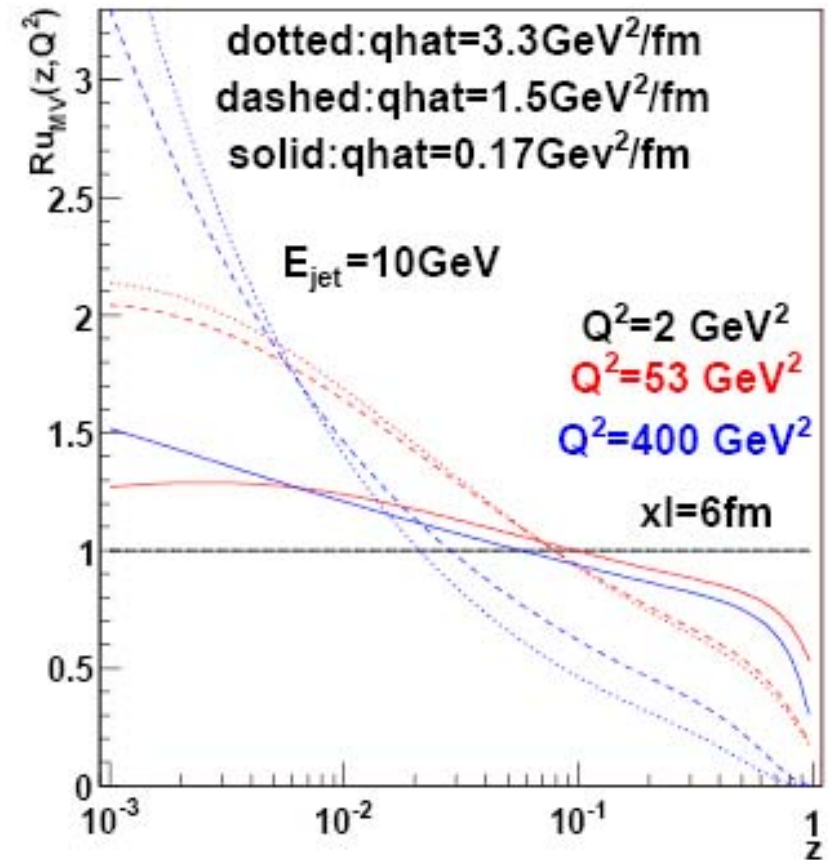
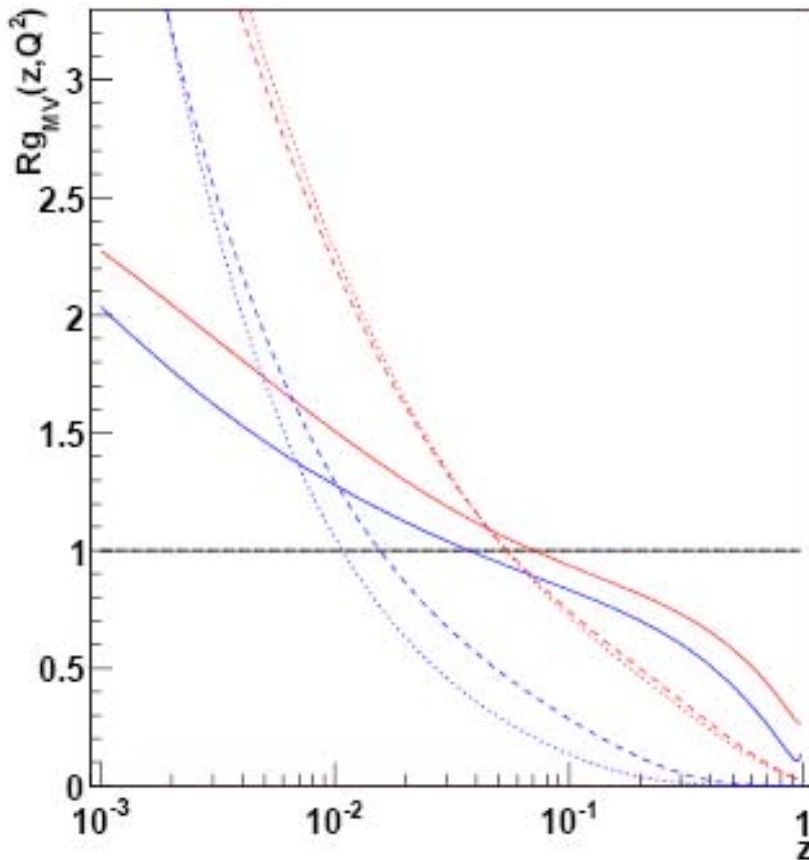
Fragmentation functions for different medium densities for  $E_{jet}=10 \text{ GeV}$

# Medium modified fragmentation functions



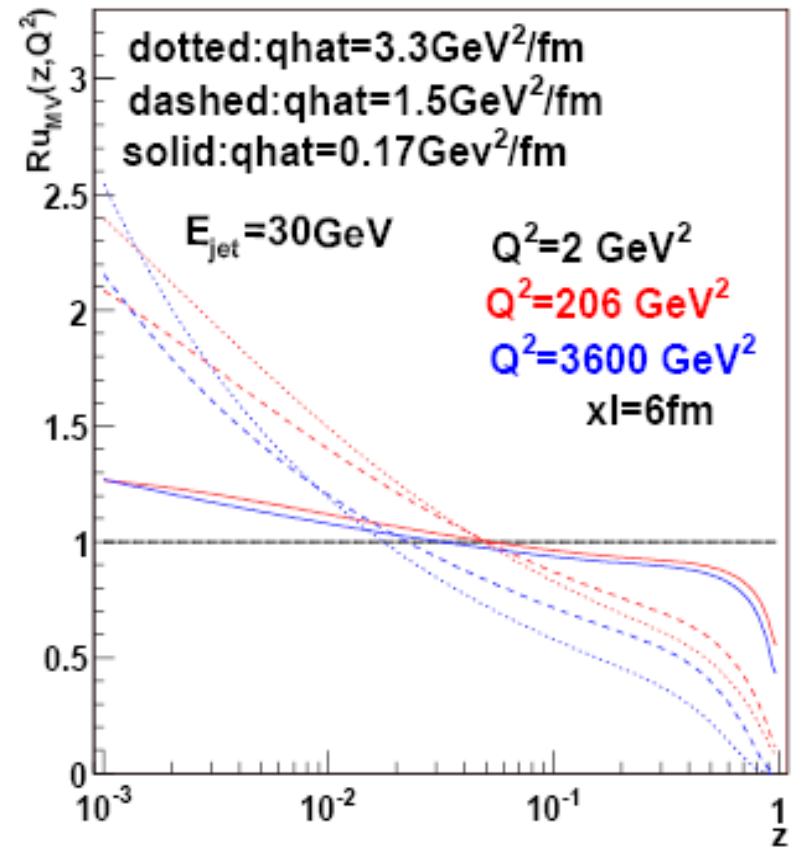
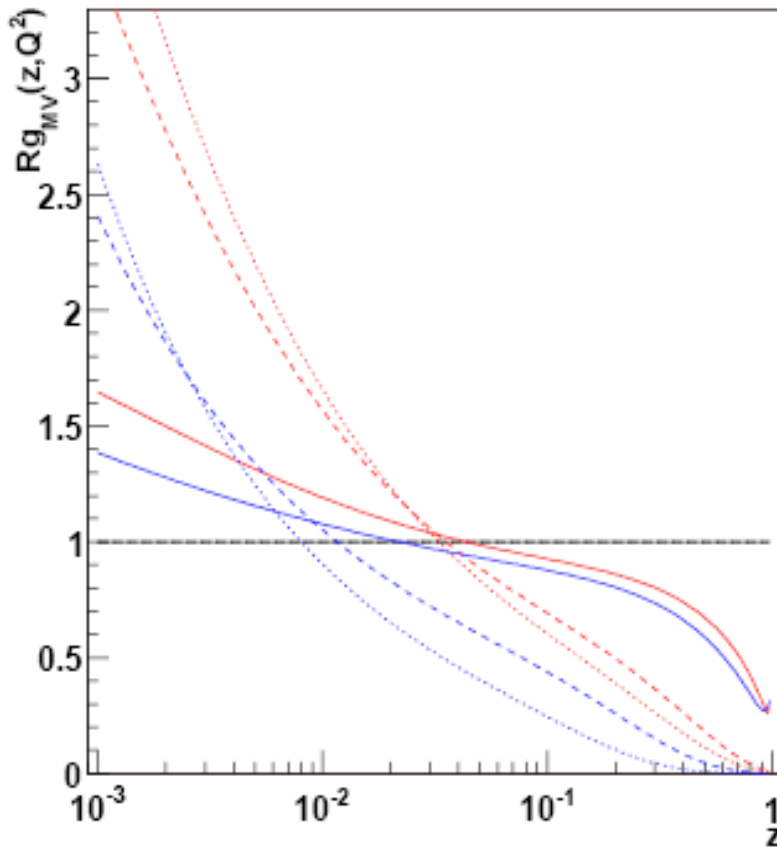
Fragmentation functions for different medium densities for  $E_{\text{jet}} = 30 \text{ GeV}$

# Medium modified fragmentation functions



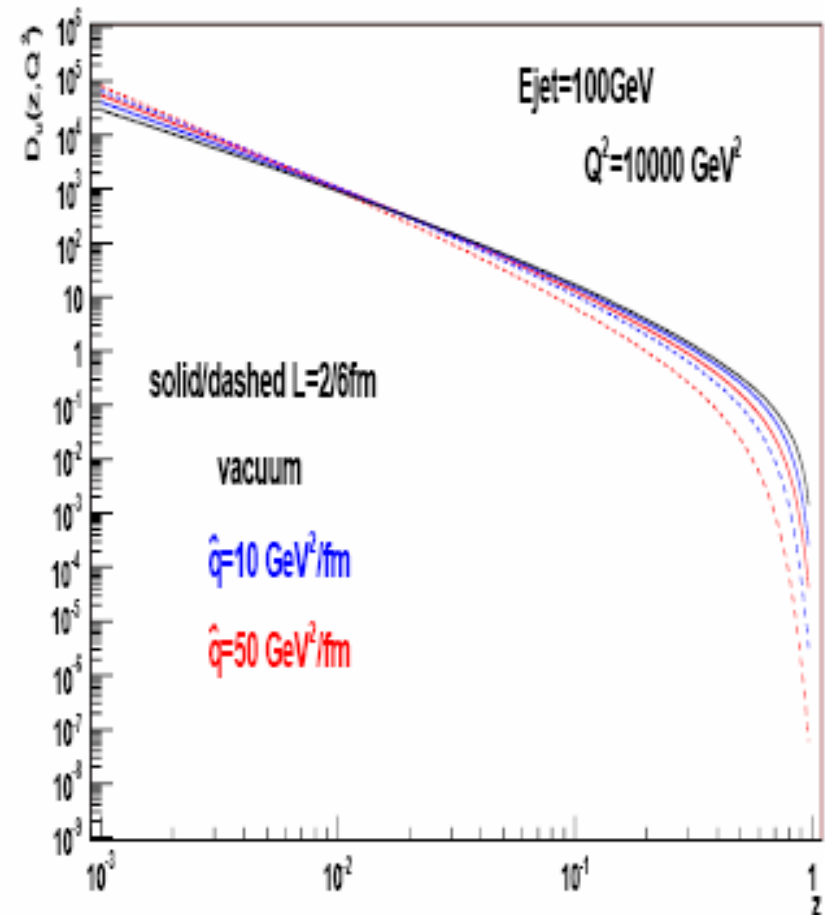
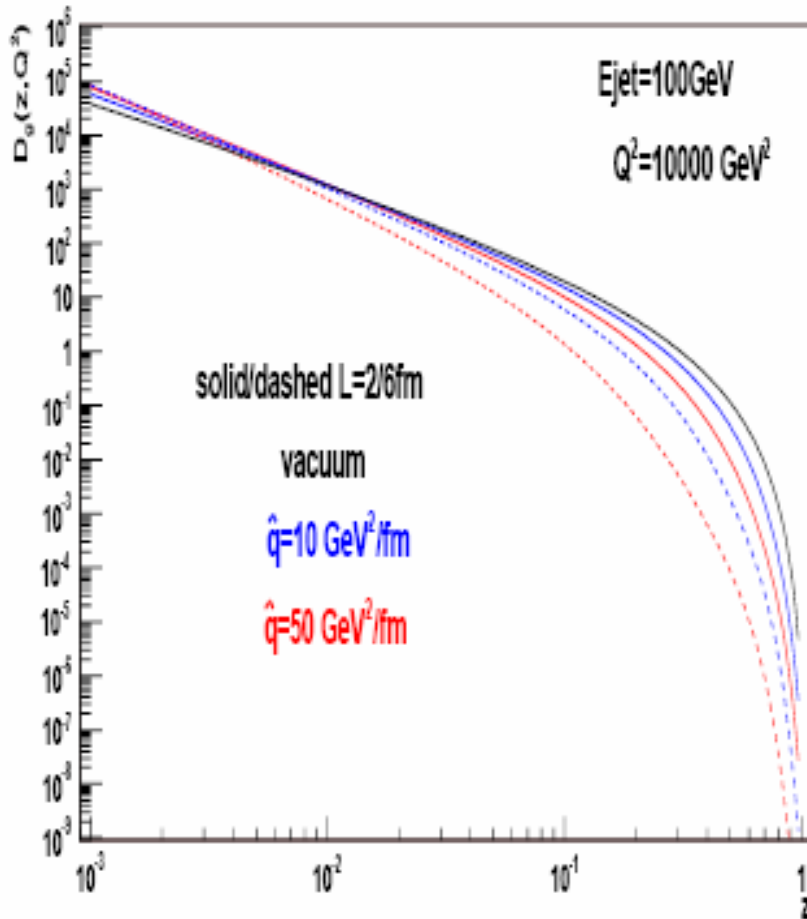
Ratio Medium/Vacuum of the fragmentation functions for  $E_{jet}=10$  GeV

# Medium modified fragmentation functions

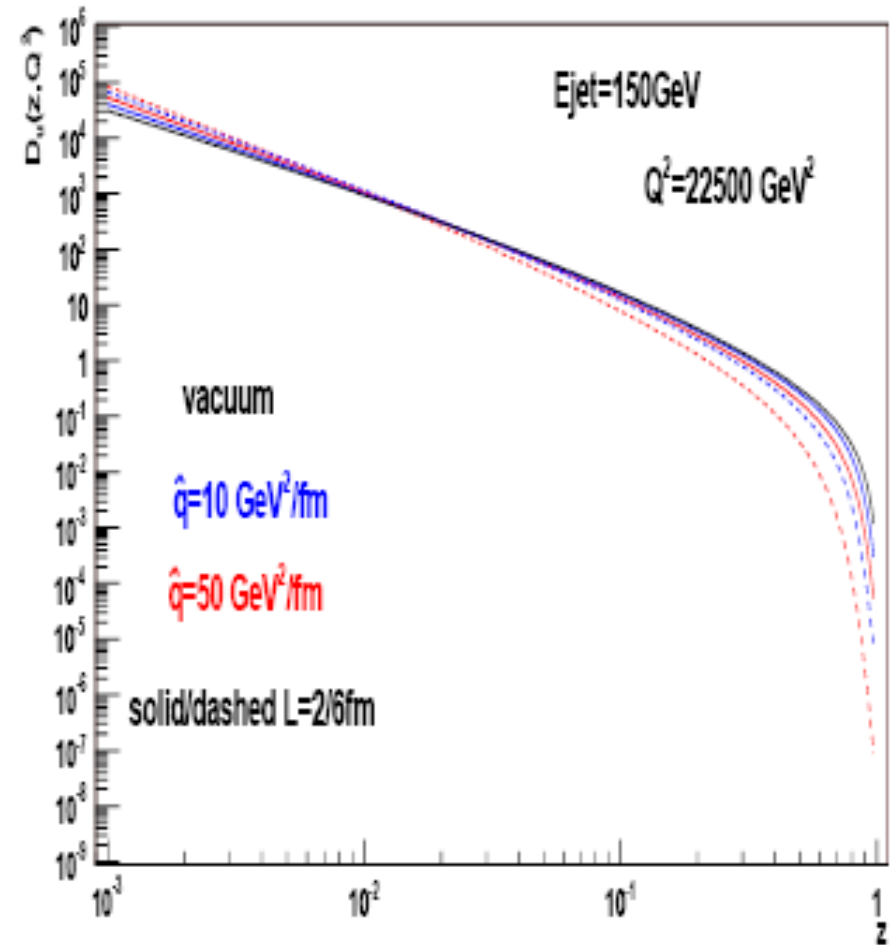
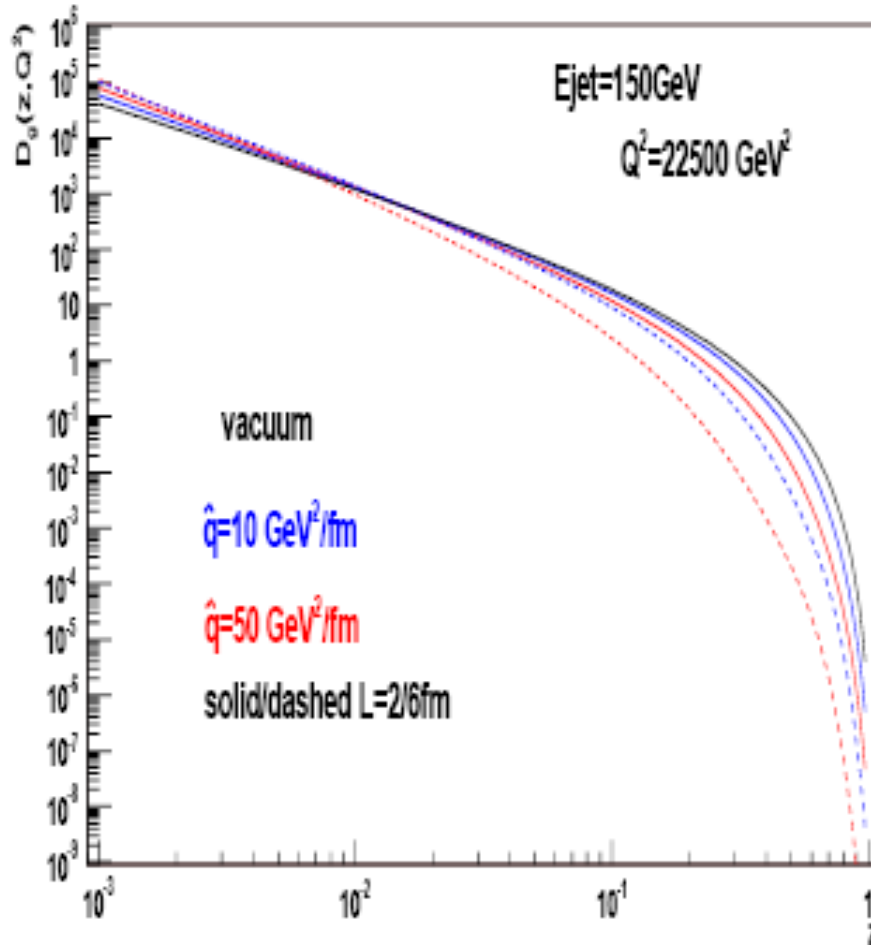


Ratio Medium/Vacuum of the fragmentation functions for  $E_{\text{jet}}=30 \text{ GeV}$

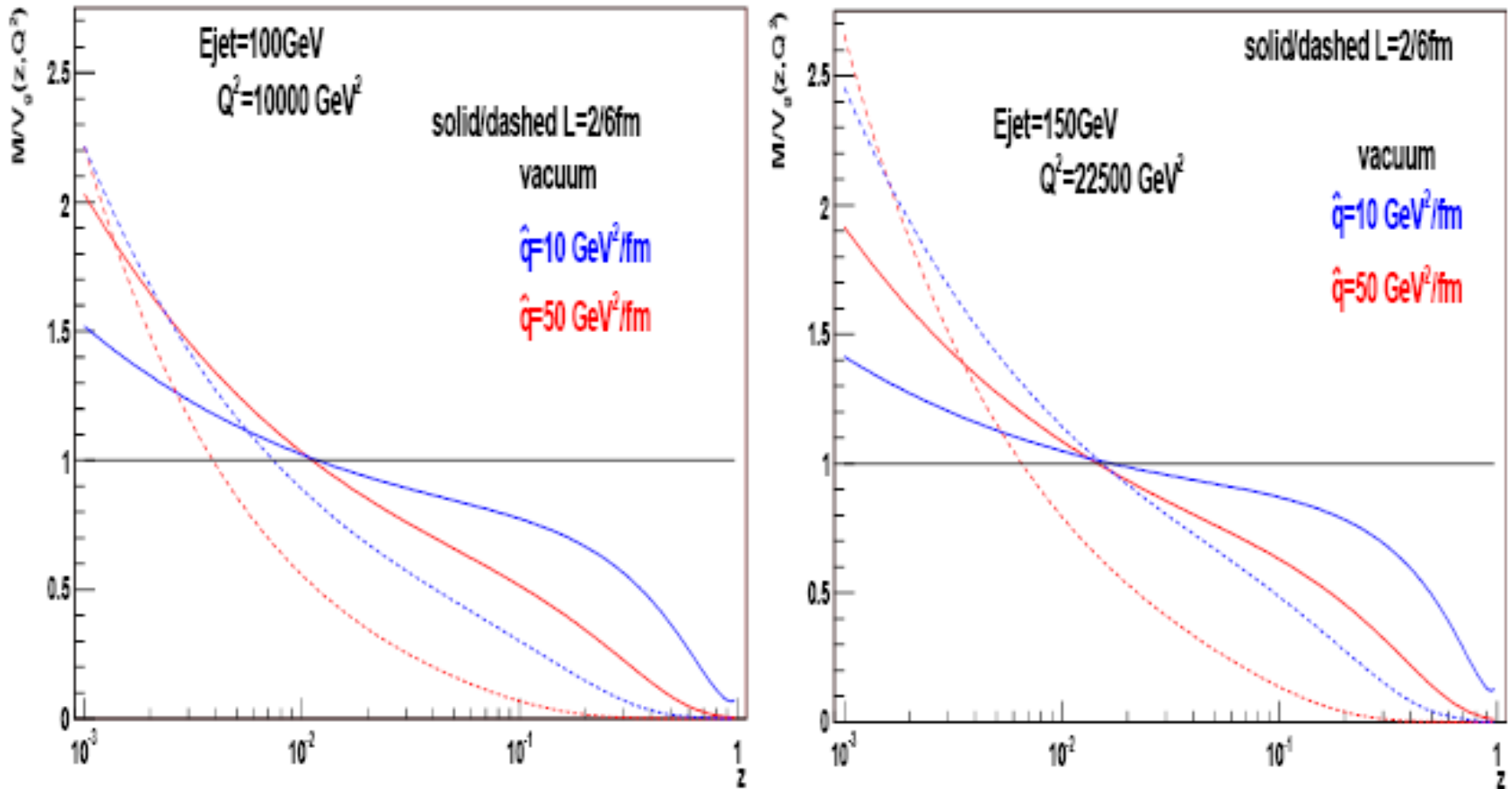
# Medium modified fragmentation functions: LHC energy



# Medium modified fragmentation functions: LHC energy



# Medium modified fragmentation functions: LHC energy





# Particle production

- A typical hard cross section can be written in the form:

$$\sigma^{ABh} = f_A(x_1, Q^2) f_B(x_2, Q^2) \otimes \sigma(x_1, x_2, Q^2) \otimes D_{i \rightarrow h}(z, Q^2)$$

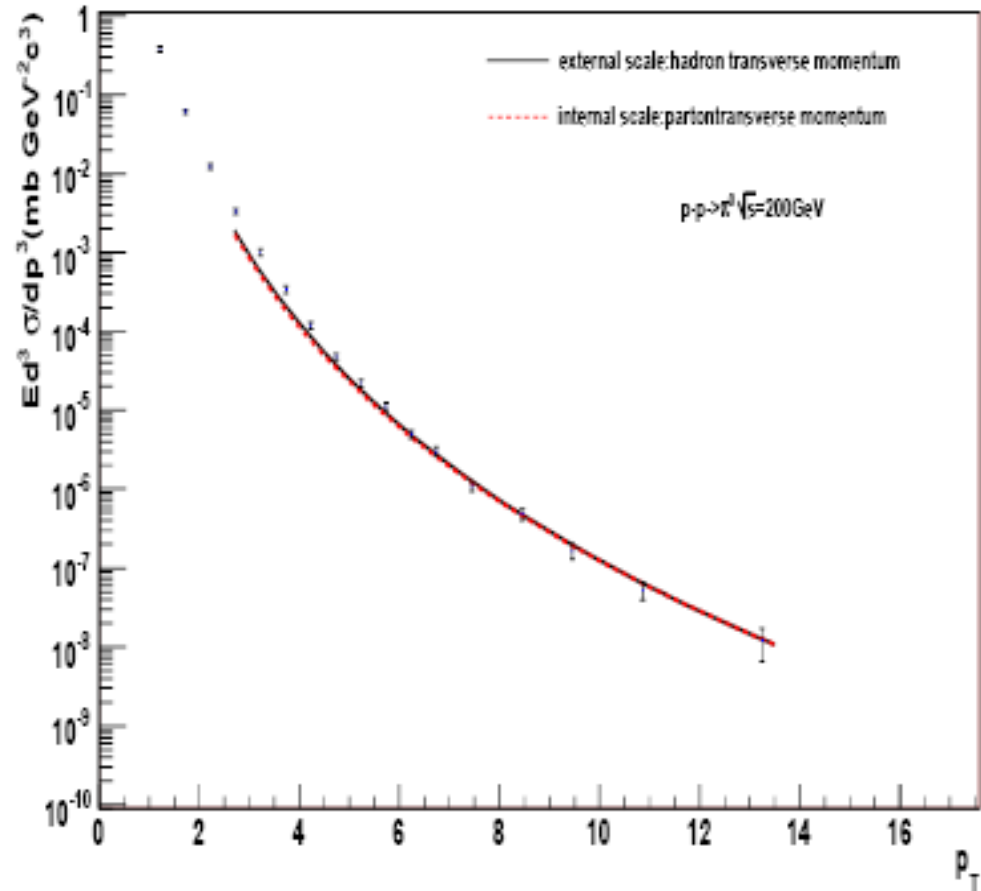
- We define the nuclear modification factor as:

$$R_{AA} = \frac{\frac{d\sigma}{dydq_T^2}(\text{pdflib} + EKS + MMFF)}{\frac{d\sigma}{dydq_T^2}(\text{pdflib} + EKS + VACFF)}$$

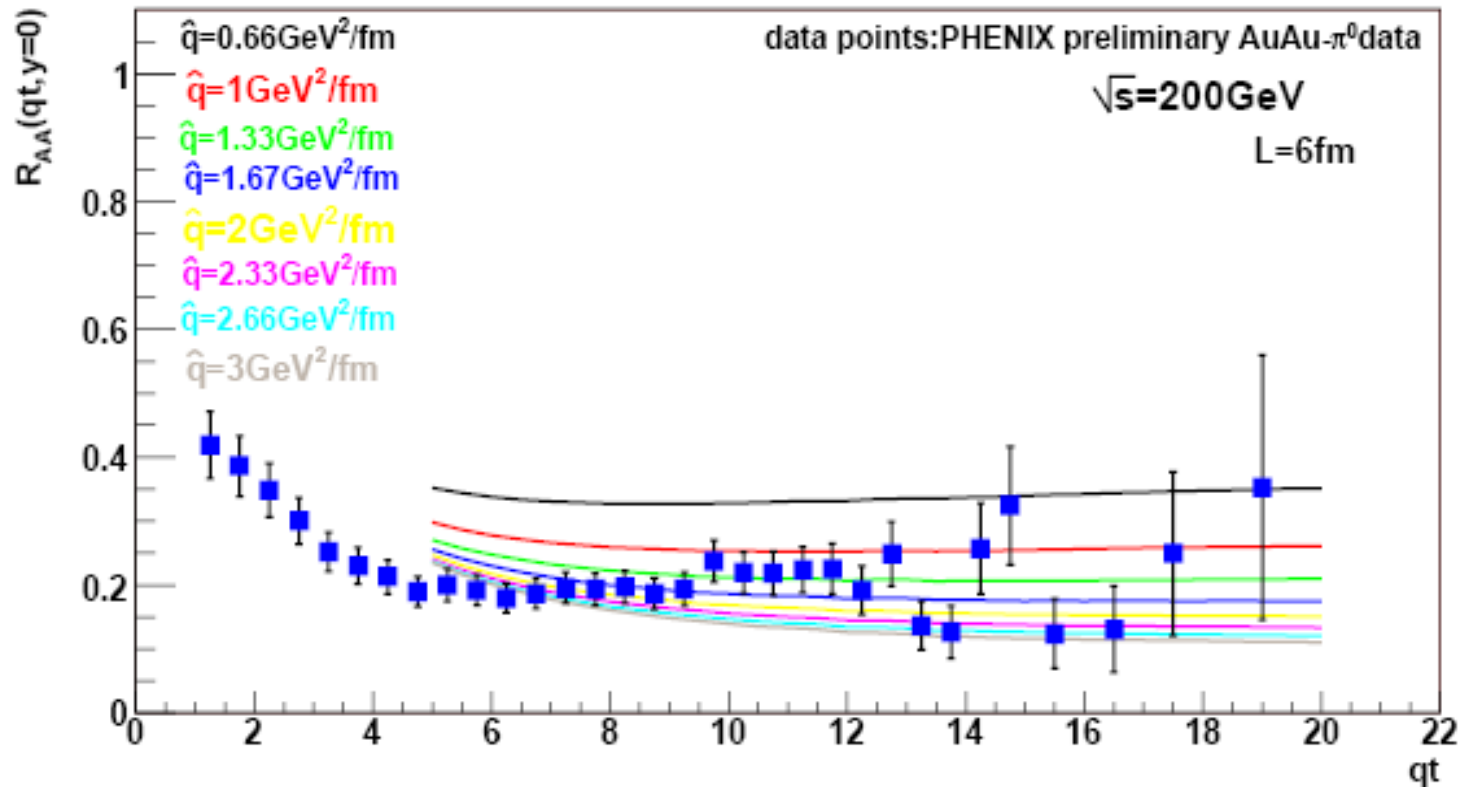
# PP reference

✓ Vacuum pp spectra as a reference.

✓ CTEQ 4L pdf 's LO.



# Nuclear modification factor



The fragmentation scale is the internal parton momentum

# conclusions

- Vacuum splitting functions  $\longrightarrow$  medium splitting functions
- Sudakov form factors in medium
- Medium modified DGLAP evolution via Sudakov factor
- Medium modified Fragmentation Functions  $\longrightarrow$  A code will be soon publish available.
- Some phenomenological applications:
  - ✓ Perturbative convolution  $\longrightarrow$  particle distributions
  - ✓ Comparison to experimental data: Nuclear modification factor  
we determine the value of the transport coefficient for a fixed pass length  $L=6$  fm

$$\longrightarrow \hat{q} \simeq 1 \text{ GeV}^2 / \text{fm}$$