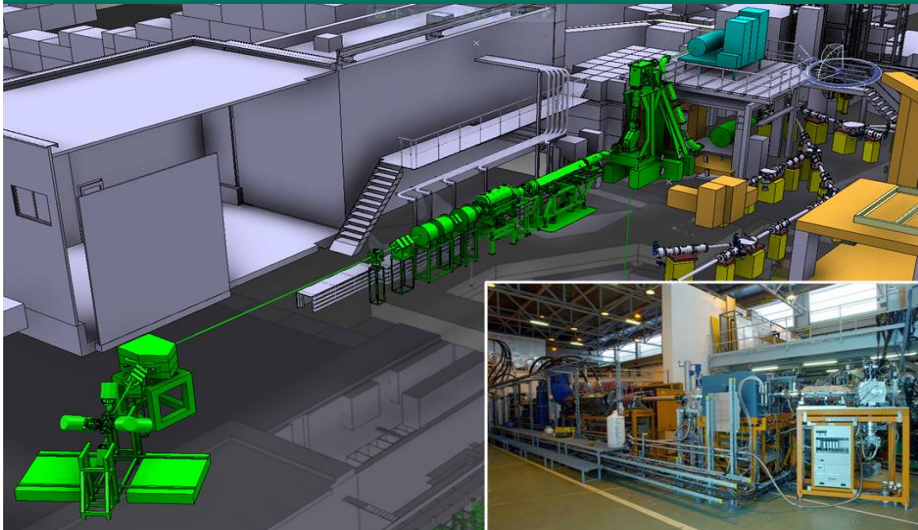


# Coulomb excitation of $^{138,140,142,144}\text{Xe}$

- IS411 campaign  
Corinna Henrich



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# Introduction - Area of interest

	136 Ba	137 Ba	138 Ba	139 Ba	140 Ba	141 Ba	142 Ba	143 Ba	144 Ba	145 Ba	146 Ba	147 Ba	148 Ba
	135 Cs	136 Cs	137 Cs	138 Cs	139 Cs	140 Cs	141 Cs	142 Cs	143 Cs	144 Cs	145 Cs	146 Cs	147 Cs
	134 Xe	135 Xe	136 Xe	137 Xe	138 Xe	139 Xe	140 Xe	141 Xe	142 Xe	143 Xe	144 Xe	145 Xe	146 Xe
	133 I	134 I	135 I	136 I	137 I	138 I	139 I	140 I	141 I	142 I	143 I	144 I	
	132 Te	133 Te	134 Te	135 Te	136 Te	137 Te	138 Te	139 Te	140 Te	141 Te	142 Te		
	131 Sb	132 Sb	133 Sb	134 Sb	135 Sb	136 Sb	137 Sb	138 Sb	139 Sb				
Z=50	130 Sn	131 Sn	132 Sn	133 Sn	134 Sn	135 Sn	136 Sn	137 Sn					
	129 In	130 In	131 In	132 In	133 In	134 In	135 In						
	128 Cd	129 Cd	130 Cd	131 Cd	132 Cd								

**N=82**

# Motivation - Evolution of the energy of the $2_1^+$ -state

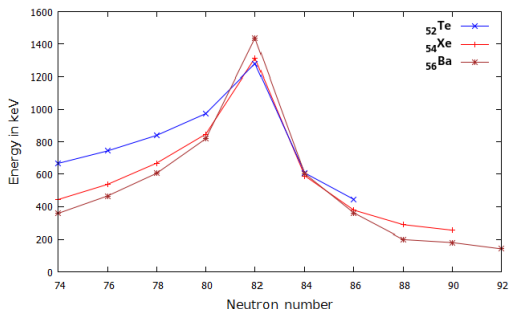
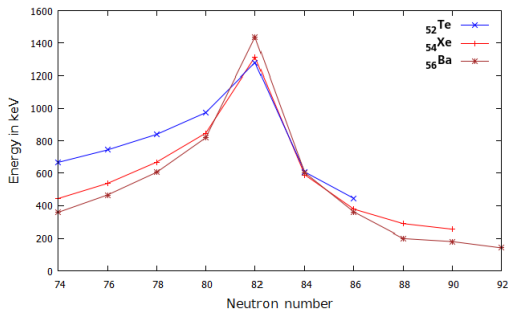


Figure : Energy of the first  $2^+$ -state

# Motivation - Evolution of the energy of the $2_1^+$ -state



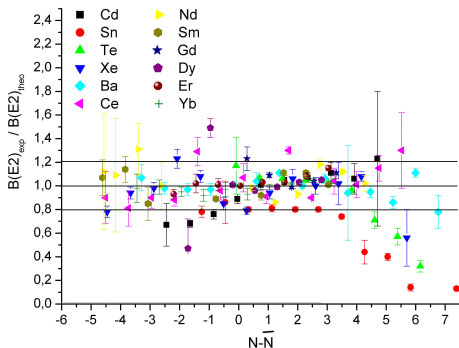
- Connection to  $B(E2; 0_{gs}^+ \rightarrow 2_1^+)$ : Empirical Grodzins' rule (1962):

$$E_{2_1^+}[\text{keV}] \cdot B(E2; 0_{gs}^+ \rightarrow 2_1^+)[e^2b^2] = 16.3 \cdot Z^2 \cdot A^{-1}$$

# Motivation - Empirical Grodzins' rule and B(E2)-values

- By S. Raman et al. (2001) and D. Habs et al. (2002) modified Grodzins' rule:

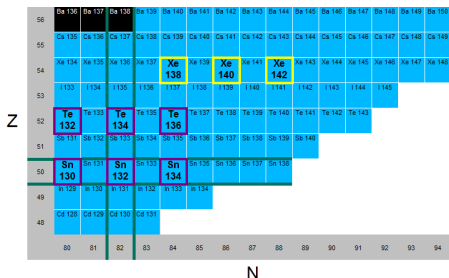
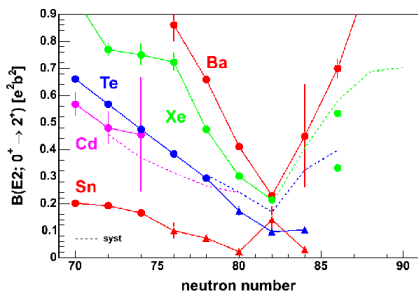
$$E_{2_1^+}[\text{keV}] \cdot B(E2; 0_{gs}^+ \rightarrow 2_1^+)[e^2b^2] = 3.242 \cdot Z^2 \cdot A^{-\frac{2}{3}}(1.000 - 0.0608(N - \bar{N}))$$



► 
$$\bar{N} = \frac{A}{2} \cdot \frac{1.0070 + 0.0128 \cdot A^{\frac{2}{3}}}{1 + 0.0064 \cdot A^{\frac{2}{3}}}$$

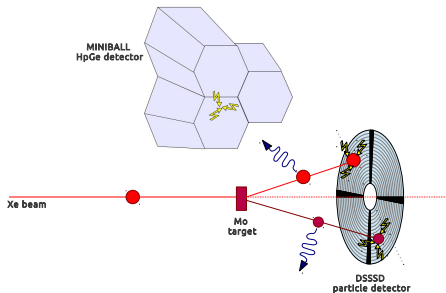
Data from: S. Raman, At. Data Nucl. Data Tables 78, 1 (2001)  
Figure taken from: D. Habs et al.: CERN-INTC-2002-015; INTC-P-156 (2002)

# Motivation - Former experimental results



Data measured at HRIBF (Oak Ridge): D. C. Radford et al., Phys. Rev. Lett. 88, 222501 (2002)  
R. L. Varner et al., Eur. Phys. J. A 25, s01, 391 (2005)  
D.C. Radford et al., Eur. Phys. J. A 25, 383 (2005)

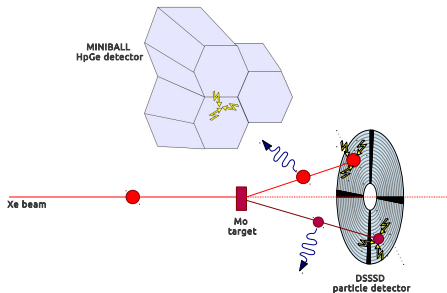
# Experiment - Coulex setup



## ► Projectile:

- **Xenon beam with 2.8 MeV/u**  
(85 % of max energy for Safe Coulex)
- Provided by REX-ISOLDE facility at CERN in 2005 and 2006
- Nuclides  $^{138,140,142,144}\text{Xe}$

# Experiment - Coulex setup



## ► Projectile:

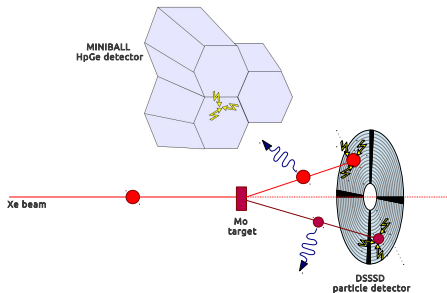
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## ► Target:

- $^{96}\text{Mo}$  target with thickness of  $1.7 \frac{\text{mg}}{\text{cm}^2}$
- Reasons for choice: sufficient information on nucleus, preparable as target, scattering kinematics



# Experiment - Coulex setup



- ▶ Projectile:
  - ▶ Xenon beam with 2.8 MeV/u  
(85 % of max energy for Safe Coulex)
  - ▶ Provided by REX-ISOLDE facility at CERN in 2005 and 2006
  - ▶ Nuclides  $^{138,140,142,144}\text{Xe}$
- ▶ Target:
  - ▶  $^{96}\text{Mo}$  target with thickness of  $1.7 \frac{\text{mg}}{\text{cm}^2}$
  - ▶ Reasons for choice: sufficient information on nucleus, preparable as target, scattering kinematics
- ▶ Inverse kinematics
- ▶ In-flight emission of  $\gamma$ -rays  
⇒ angles are of importance!

# Data analysis - Approach



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- ▶ Determine projectile Coulomb cross section  $\sigma_{Coul}^p$  relative to target  $\sigma_{Coul}^t$  using **CLX & DCY**

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$$\sigma_{Coul}^p = \frac{1}{P} \cdot \frac{N_{\gamma}^p}{\epsilon_{\gamma}^p} \cdot \frac{\epsilon_{\gamma}^t}{N_{\gamma}^t} \cdot \sigma_{Coul}^t$$

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$$\sigma_{Coul}^p = \frac{1}{P} \cdot \frac{N_{\gamma}^p}{\epsilon_{\gamma}^p} \cdot \frac{\epsilon_{\gamma}^t}{N_{\gamma}^t} \cdot \sigma_{Coul}^t$$

- ▶  $\sigma_{Coul}^t$ : CLX & DCY need matrix elements of target  $^{96}\text{Mo}$ :  $(M_{02}, M_{22})$  <sup>1</sup>
- ▶ Counts in efficiency corrected peak  $\frac{N_{\gamma}}{\epsilon_{\gamma}}$
- ▶ Beam purity  $P$ 
  - ▶ Cold plasma ion source used
  - ▶ Breeding time of REX-EBIS  $\Rightarrow$  beam purity

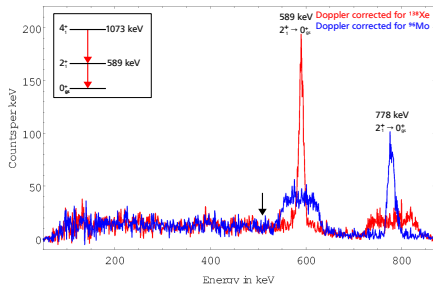
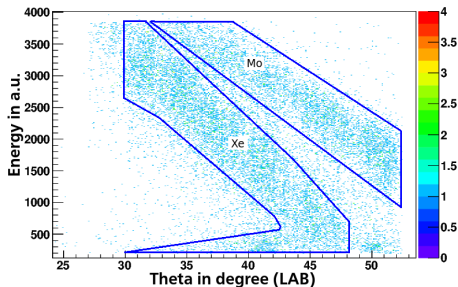


- ▶ Determine projectile Coulomb cross section  $\sigma_{Coul}^p$  relative to target  $\sigma_{Coul}^t$  using **CLX & DCY**

$$\sigma_{Coul}^p = \frac{1}{P} \cdot \frac{N_{\gamma}^p}{\epsilon_{\gamma}^p} \cdot \frac{\epsilon_{\gamma}^t}{N_{\gamma}^t} \cdot \sigma_{Coul}^t$$

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- ▶ Beam purity  $P$ 
  - ▶ Cold plasma ion source used
  - ▶ Breeding time of REX-EBIS  $\Rightarrow$  beam purity
- ▶  $\sigma_{Coul}^p = \text{CLX/DCY}(M_{02}, M_{22}, ..) \Rightarrow M_{02} \Rightarrow \text{B}(E2; 0_{gs}^+ \rightarrow 2_1^+)$

# Analysis of $^{138}\text{Xe}$ - Kinematics and Doppler-corrected spectra



- ▶ High count rates ( $10^5$  part./s)
  - ⇒ Inner four rings covered
  - ⇒ Only small angular range on DSSSD available!

# Analysis of $^{138}\text{Xe}$ - Lifetime measurements

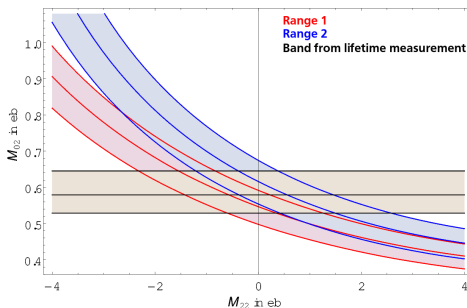


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- ▶  $\Rightarrow$  Not enough information to determine  $B(E2)$ -value and quadrupole moment with reasonable confidence intervals
- ▶  $\Rightarrow$  Additional information by direct lifetime measurements:  
 $\tau(2_1^+) = (17.3 \pm 3.4) \text{ ps}^{-1}$

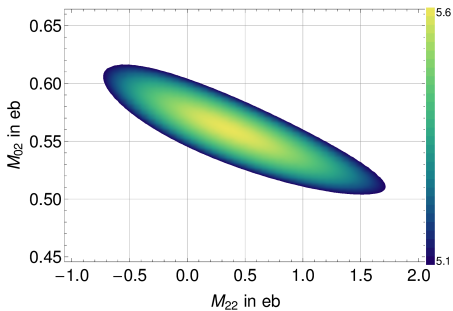
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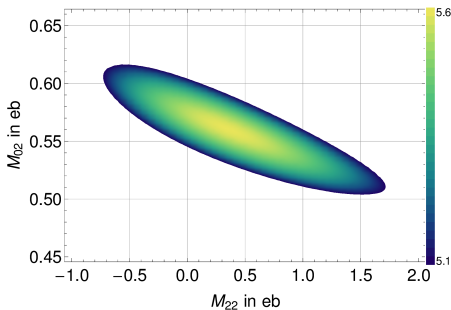




# Preliminary results for $^{138}\text{Xe}$ - $1\sigma$ -contour plot



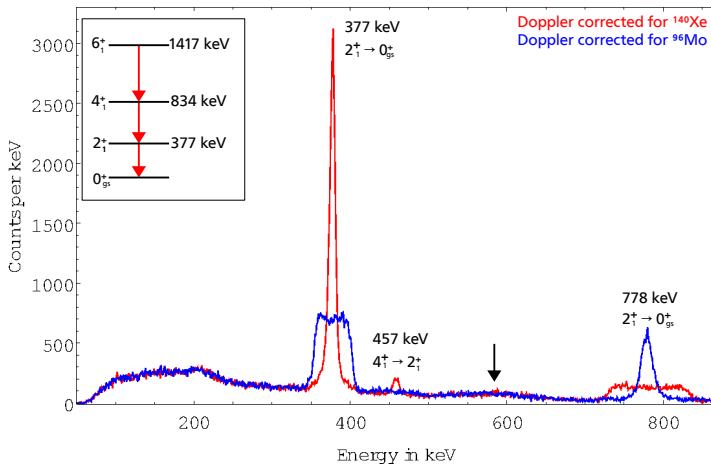
# Preliminary results for $^{138}\text{Xe}$ - 1 $\sigma$ -contour plot



⇒ B(E2)-value and quadrupole moment

- ▶  $B(E2; 0_{gs}^+ \rightarrow 2_1^+) = (0.31 \pm 0.07) e^2 b^2$
- ▶  $eQ_s(2_1^+) = (0.27 \begin{smallmatrix} +1.02 \\ -0.83 \end{smallmatrix}) eb$

# Analysis of $^{140}\text{Xe}$ - Doppler-corrected spectra using full statistics

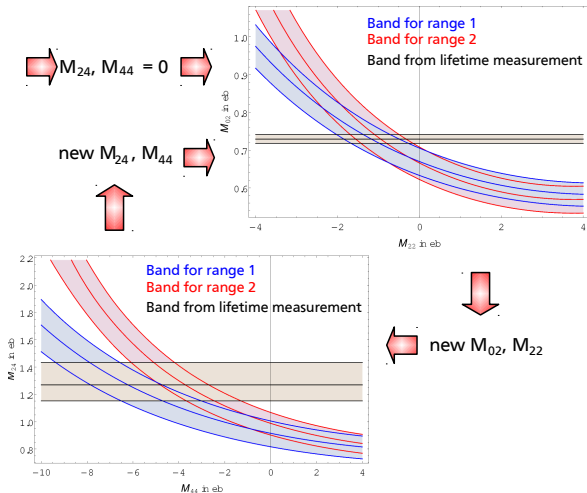


# Analysis of $^{140}\text{Xe}$ - Approach

- ▶ Relevant matrix elements:  $M_{02}$ ,  $M_{22}$ ,  $M_{24}$ , and  $M_{44}$
- ▶ Mean lifetime  
 $\tau(2_1^+) = (101.7 \pm 3.2) \text{ ps}^1$   
and  
 $\tau(4_1^+) = (22.8 \pm 4.9) \text{ ps}^1$

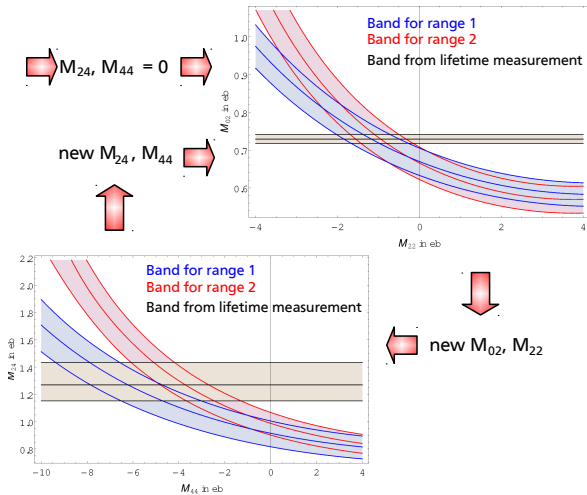
# Analysis of $^{140}\text{Xe}$ - Approach

- ▶ Relevant matrix elements:  $M_{02}$ ,  $M_{22}$ ,  $M_{24}$ , and  $M_{44}$
- ▶ Mean lifetime  $\tau(2_1^+) = (101.7 \pm 3.2) \text{ ps}^1$  and  $\tau(4_1^+) = (22.8 \pm 4.9) \text{ ps}^1$

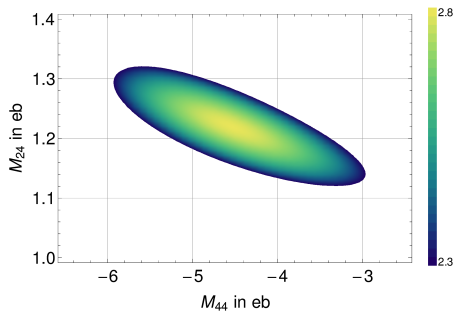
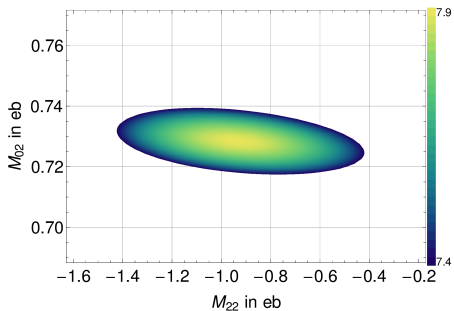


# Analysis of $^{140}\text{Xe}$ - Approach

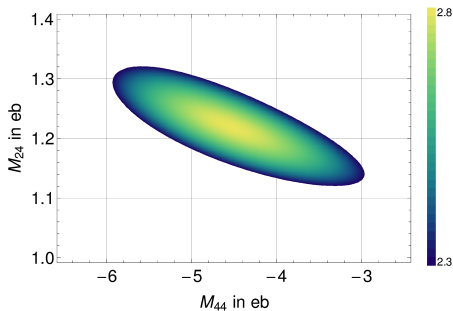
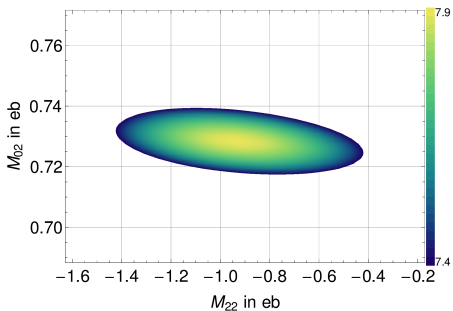
- ▶ Relevant matrix elements:  $M_{02}$ ,  $M_{22}$ ,  $M_{24}$ , and  $M_{44}$
- ▶ Mean lifetime  $\tau(2_1^+) = (101.7 \pm 3.2) \text{ ps}^1$  and  $\tau(4_1^+) = (22.8 \pm 4.9) \text{ ps}^1$
- ▶  $\Rightarrow$  Consistent set of matrix elements ( $M_{02}$ ,  $M_{22}$ ,  $M_{24}$ ,  $M_{44}$ )



# Preliminary results for $^{140}\text{Xe}$ - $1\sigma$ -contour plot



# Preliminary results for $^{140}\text{Xe}$ - 1 $\sigma$ -contour plot



⇒ B(E2)-values and quadrupole moments

▶  $B(E2; 0_{gs}^+ \rightarrow 2_1^+) = (0.53 \pm 0.01) e^2 b^2$

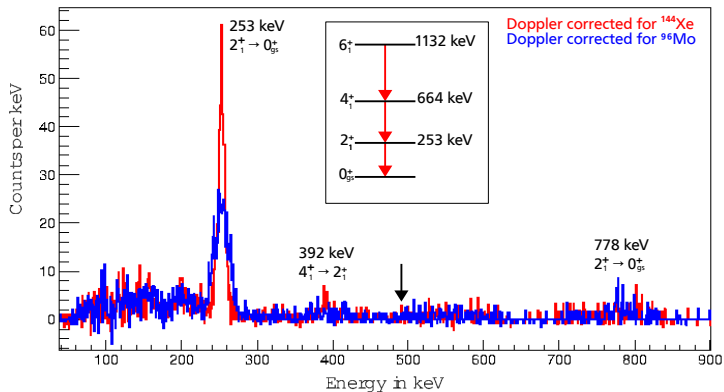
▶  $eQ_s(2_1^+) = (-0.71 \begin{smallmatrix} +0.39 \\ -0.36 \end{smallmatrix}) eb$

▶  $B(E2; 2_1^+ \rightarrow 4_1^+) = (0.30 \pm 0.05) e^2 b^2$

▶  $eQ_s(4_1^+) = (-2.56 \begin{smallmatrix} +0.88 \\ -0.79 \end{smallmatrix}) eb$

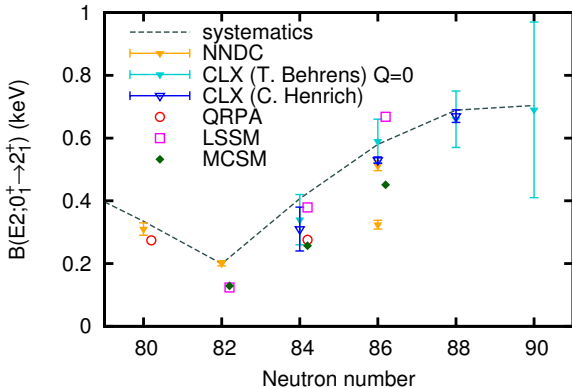


# Analysis of $^{144}\text{Xe}$ - Doppler-corrected spectra using full statistics



- Analysis ongoing. Challenging due to low statistics :(

# Preliminary results - Comparison to theory



systematics: modified Grodzins' systematics

NNDC: National Nuclear Data Center

T. Behrens, PhD thesis

QRPA: J. Terasaki et al., Phys. Rev. C 66 (2002) 054313

LSSM: D. Bianco et al., Phys. Rev. C 88 (2013) 024303

MCSM: N. Shimizu et al., J. Phys.: Conf. Ser. 49 (2006) 178

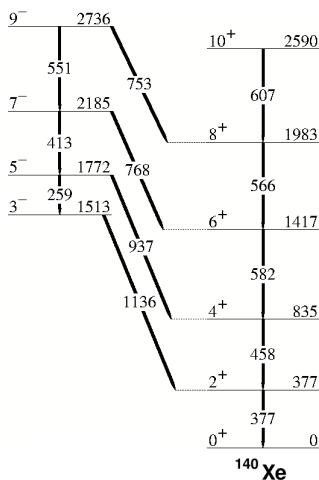
# Summary and outlook - Preliminary results

	Transition $I_i \rightarrow I_f$	$B(E2)_{\uparrow}$ in $e^2b^2$	$eQ_s(I_f)$ in eb
$^{138}\text{Xe}$	$0_{gs}^+ \rightarrow 2_1^+$	$0.31 \pm 0.07$	$0.27 \begin{smallmatrix} +1.02 \\ -0.83 \end{smallmatrix}$
$^{140}\text{Xe}$	$0_{gs}^+ \rightarrow 2_1^+$	$0.53 \pm 0.01$	$-0.71 \begin{smallmatrix} +0.39 \\ -0.36 \end{smallmatrix}$
	$2_1^+ \rightarrow 4_1^+$	$0.30 \pm 0.05$	$-2.56 \begin{smallmatrix} +0.88 \\ -0.79 \end{smallmatrix}$
$^{142}\text{Xe}$	$0_{gs}^+ \rightarrow 2_1^+$	$0.67 \pm 0.02$	$-1.02 \begin{smallmatrix} +0.64 \\ -0.60 \end{smallmatrix}$
	$2_1^+ \rightarrow 4_1^+$	$0.41 \begin{smallmatrix} +0.22 \\ -0.18 \end{smallmatrix}$	$-2.45 \begin{smallmatrix} +\infty \\ -1.88 \end{smallmatrix}$

# Summary and outlook - Preliminary results

	Transition $I_i \rightarrow I_f$	$B(E2)_{\uparrow}$ in $e^2b^2$	$eQ_s(I_f)$ in eb
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	$2_1^+ \rightarrow 4_1^+$	$0.41 \begin{smallmatrix} +0.22 \\ -0.18 \end{smallmatrix}$	$-2.45 \begin{smallmatrix} +\infty \\ -1.88 \end{smallmatrix}$

- ▶ HIE-ISOLDE: Influence of multiple Coulex increases (additional matrix elements)
- ▶ → Combined analysis of Coulex and lifetime measurements necessary



Level scheme taken from: W. Urban et al., Eur. Phys. J. A 16, 303307 (2003)



# Thank you for your attention!

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**ISOLDE**

and the IS411-MINIBALL  
Collaboration



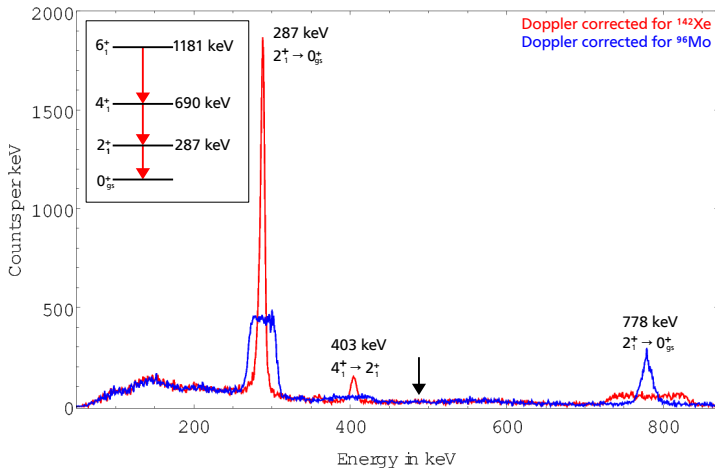




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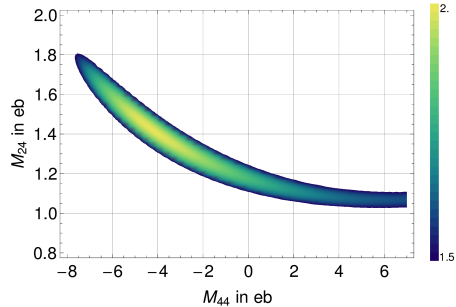
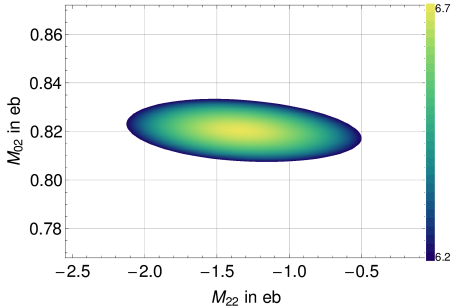


# Backup - Analysis of $^{142}\text{Xe}$ - Doppler-corrected spectra using full statistics



# Backup -

## Preliminary results for $^{142}\text{Xe}$ - 1 $\sigma$ -contour plot



⇒ B(E2)-values and quadrupole moments

▶  $B(E2; 0_{gs}^+ \rightarrow 2_1^+) = (0.67 \pm 0.02) e^2 b^2$

▶  $eQ_s(2_1^+) = (-1.02 \begin{smallmatrix} +0.64 \\ -0.60 \end{smallmatrix}) eb$

▶  $B(E2; 2_1^+ \rightarrow 4_1^+) = (0.41 \begin{smallmatrix} +0.22 \\ -0.18 \end{smallmatrix}) e^2 b^2$

▶  $eQ_s(4_1^+) = (-2.45 \begin{smallmatrix} +\infty \\ -1.88 \end{smallmatrix}) eb$

Used mean lifetime  $\tau(2_1^+) = (270 \pm 10)$  ps; S. Ilieva, preliminary value; EXILL-FATIMA campaign at ILL in 2013

# Backup - Matrix elements

- ▶ B(E2)-values are dependent on off-diagonal matrix elements

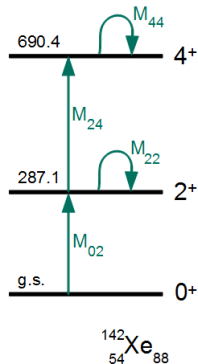
$$B(E2; I_i \rightarrow I_f) = \frac{1}{2I_i + 1} |M_{if}|^2$$

- ▶ Connection of the mean lifetime  $\tau$  to B(E2)-values

$$\frac{1}{\tau(I_f)} \propto E_\gamma^5 \cdot B(E2; I_i \rightarrow I_f)$$

- ▶ Quadrupole moments are dependent on diagonal matrix elements

$$M_{22} = \sqrt{\frac{7}{2\pi} \frac{5}{4}} eQ_s$$
$$M_{44} = \frac{1}{2} \sqrt{\frac{275}{7\pi}} eQ_s$$

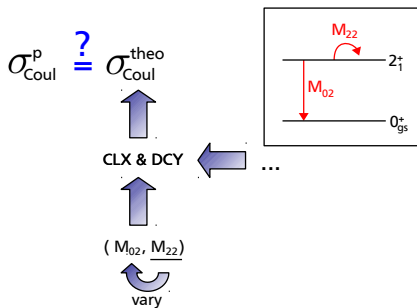


# Backup - Analysis of $^{138}\text{Xe}$ - Approach

$$\sigma_{Coul}^p = P \cdot \frac{N_\gamma^p}{\epsilon_\gamma^p} \cdot \frac{\epsilon_\gamma^t}{N_\gamma^t} \cdot \sigma_{Coul}^t$$

- Determine all observables on right side  $\Rightarrow$  experimental projectile cross section  $\sigma_{Coul}^p$

- $\Rightarrow (M_{02}, M_{22})$ -pairs determined from experimental projectile cross section



# Backup - Grodzins' rule

