# Predictions & speculations related to $b \to c \, au ar{ u}$

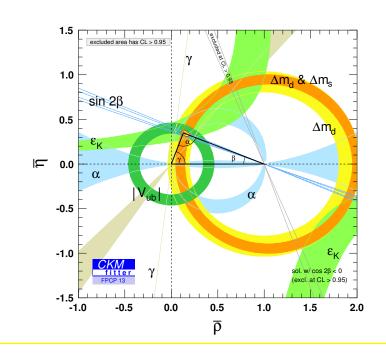
**Zoltan Ligeti** 

See: Freytsis, ZL, Ruderman, to appear

Naturalness @ Weizmann, November 13, 2014

#### **Snapshot of flavor physics**

- The level of agreement between the measurements is often misinterpreted
- Much larger allowed region if SM not assumed to hold, more parameters
- $\mathcal{O}(20\%)$  NP contributions to most FCNC (loop dominated) processes are still allowed



• Future:  $\frac{\text{(LHCb upgrade)}}{\text{(LHCb } 1\, fb^{-1})} \sim \frac{\text{(Belle II data set)}}{\text{(Belle data set)}} \sim \frac{\text{(BaBar data set)}}{\text{(CLEO data set)}} \sim 50$ 

Last 15 yrs: verify Kobayashi–Maskawa mechanism — Next 15 yrs: discover/study BSM signals?

• Increase in sensitivity to higher scales  $\sqrt[4]{50} \sim 2.5$ , similar to LHC8  $\rightarrow$  LHC14 Expect "unpredictable" progress, too — data usually motivate people to think hard...





The b o c auar
u data

## The $B o D^{(*)} au ar{ u}$ measurements

BaBar reported  $3.4\sigma$  deviation from SM in the ratios:  $R(X) = \frac{\Gamma(B \to X \tau \bar{\nu})}{\Gamma(B \to X \ell \bar{\nu})}$ 

	Belle	BABAR	SM
R(D)	$0.430 \pm 0.091$	$0.440 \pm 0.058 \pm 0.042$	$0.297 \pm 0.017$
$R(D^*)$	$0.405 \pm 0.047$	$0.332 \pm 0.024 \pm 0.018$	$0.252 \pm 0.003$
correlation	neglected	-0.27	-

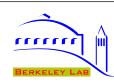
[Watanabe, FPCP 2014 — BaBar 1205.5442 + Belle private combination]

Public Belle result not yet available with full data, correlation neglected
 Combined significance would only be larger

[Naive combination, without correlations: R(D):  $2.4\sigma$ ,  $R(D^*)$ :  $3.8\sigma$ ,  $R(D^{(*)})$ :  $4.8\sigma$ ]

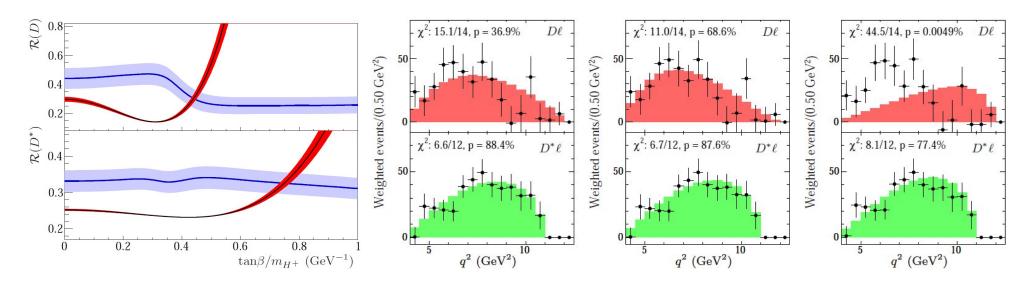
SM predictions fairly robust: heavy quark symmetry + lattice QCD





#### **BaBar statements on BSM models**

lacktriangle BaBar studied consistency of rates with 2HDM, and  ${
m d}\Gamma/{
m d}q^2$  with several models



[PRL 109 (2012) 101802, arXiv:1205.5442]

[PRD 88 (2013) 072012, arXiv:1303.0571]

• Found that type-II 2HDM gave nearly as bad fit to the data as the SM  ${
m d}\Gamma/{
m d}q^2$  clearly has additional discriminating power

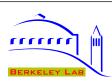




#### Reasons (not) to take the tension seriously

- ullet B factory measurements with au leptons are difficult
- Need a large tree-level contribution, SM suppression only by  $m_{\tau}$  NP expected to show up in FCNCs need fairly light NP here to fit the data
- Severe constraints on actual models from flavor physics, and from LHC
- Results from BaBar and Belle indicate consistent signal
- Even when BaBar and Belle disagreed in the past, averages often proved robust
- If Nature were as most theorist imagined (until a few years ago), then the LHC (Tevatron, LEP, DM searches) should have already discovered new physics





#### Tension with SM is model independent

- Use an OPE-based analysis to constrain SM allowed range as much as possible
- Learn more from inclusive =  $\sum$  exclusive

$$\mathcal{B}(B^- o X_c \ell \bar{
u}) = (10.92 \pm 0.16)\%$$
 and  $R(X_c) = 0.222 \pm 0.003$  [hep-ph/9401226, hep-ph/9811239]   
  $\Rightarrow \mathcal{B}(B^- o X_c \tau \bar{
u}) = (2.42 \pm 0.05)\%$ 

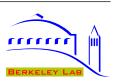
LEP average:  $\mathcal{B}(b \to X\tau^+\nu) = (2.41 \pm 0.23)\%$  [experimental concerns...]

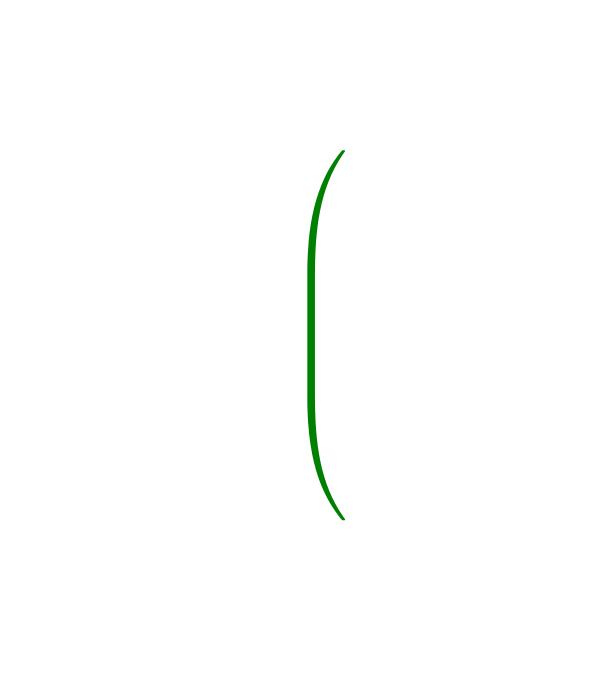
• The  $R(D^{(*)})$  data imply:

$$\mathcal{B}(\bar{B} \to D^* \tau \bar{\nu}) + \mathcal{B}(\bar{B} \to D \tau \bar{\nu}) = (2.78 \pm 0.25)\%$$

- Estimate  $\mathcal{B}(B \to D^{**}\tau\bar{\nu}) \gtrsim 0.2\%$  in the SM (the four 1P states)
- Thus, tension  $\geq 2\sigma$ , independent of SM calculation of  $R(D^{(*)})$
- Belle II: Expect reduction of uncertainties by factor 8-10

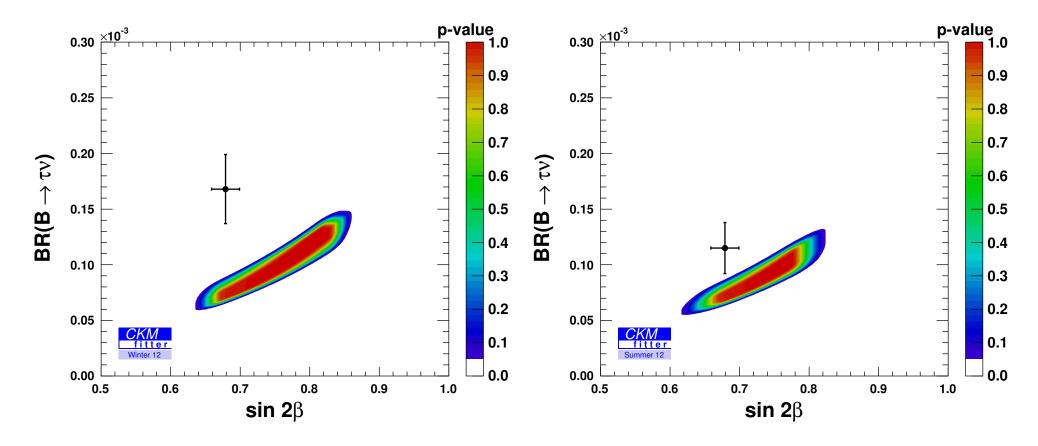






#### Past tension in B o auar u decay

• Until 2012 there was a  $\sim 2.5\sigma$  tension between  $\mathcal{B}(B \to \tau \bar{\nu})$  and the CKM fit



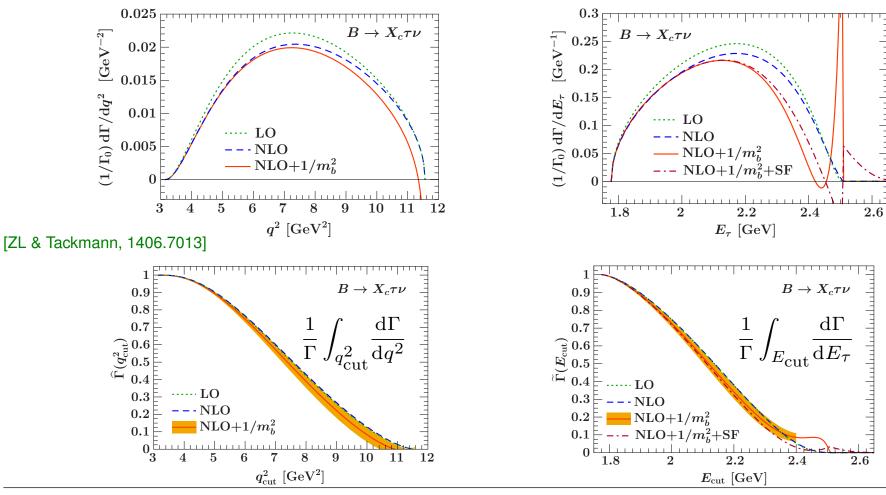
(Or, assuming the SM,  $\mathcal{B}(B \to \tau \bar{\nu})$  gave too large  $|V_{ub}|$ )





#### Precision $B o X_c au ar{ u}$ predictions

• No measurements since LEP, Belle analysis in progress (No theory work in  $\sim 15 \, \mathrm{yrs}$ ) Papers in '90s used pole mass, did not study spectra (experimentally needed) and uncertainties







#### $B o X_u auar u$ predictions

• Large interest in Belle II to study all decay modes with  $\tau$ -s

If LEP could measure  $B\to X_c\tau\bar{\nu}$  with a few  $\times 10^6~B-\overline{B}$  pairs, surely Belle II can measure  $B\to X_u\tau\bar{\nu}$  with  $5\times 10^{10}~B-\overline{B}$  pairs...

- Suppression of  $\tau$  mode smaller in  $b \to u$ :  $\Gamma(B \to X_u \ell \bar{\nu})/\Gamma(B \to X_u \tau \bar{\nu}) \simeq 3.0$  $\Gamma(B \to X_c \ell \bar{\nu})/\Gamma(B \to X_c \tau \bar{\nu}) \simeq 4.5$
- The inclusive calculation is unavailable for any distribution (except for total rate)

Calculated rates, figuring out subtleties with shape function... [ZL & Tackmann, to appear]





#### Tensions in $|V_{ub}|$ determinations

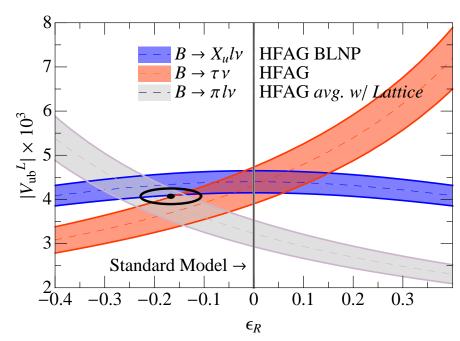
ullet  $\sim 3\,\sigma$  tension among  $|V_{ub}|$  measurements

Tim Gershon @ FPCP 2014: "Understanding this will involve a great deal of effort, but is essential for continued progress in the field"

- Too early to conclude:
  - Inclusive determination can improve
  - Exclusive measured better with full reco
  - Lattice QCD results will improve
- A BSM possibility:

$$\mathcal{L} = -\frac{4G_F}{\sqrt{2}} V_{ub}^L \left( \bar{u} \gamma_{\mu} P_L b + \epsilon_R \, \bar{u} \gamma_{\mu} P_R b \right) \left( \bar{\nu}_{\ell} \gamma^{\mu} P_L \ell \right)$$

Can we construct observables which give "more vertical" constraints?

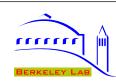


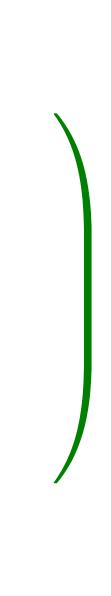
[Bernlochner, ZL, Turczyk, 1408.2516]

Decay	$ V_{ub}  \times 10^4$	adm.
$B \to \pi  \ell  \bar{\nu}_{\ell}$	$3.23 \pm 0.30$	$(1+\epsilon_R)$
$B \to X_u  \ell  \bar{\nu}_{\ell}$	$4.39 \pm 0.21$	$\sqrt{1+\epsilon_R^2}$
$B \to \tau  \bar{\nu}_{\tau}$	$4.32 \pm 0.42$	$(1-\epsilon_R)$

• NB: Cleanest  $|V_{ub}|$  I know, only isospin,  $\mathcal{B}(B_u \to \ell \bar{\nu})/\mathcal{B}(B_d \to \mu^+ \mu^-)$  — run LHCb @ 33 TeV







# Operator analysis

#### **Four-fermion operators**

Parametrize new physics:

$${\cal H} = rac{4G_F}{\sqrt{2}} \, V_{cb} \, {\cal O}_{V_L} + rac{1}{\Lambda^2} \sum_i C_i^{(\prime,\prime\prime)} \, {\cal O}_i^{(\prime,\prime\prime)}$$

Consider redundant operators with different fermion ordering — simplifies understanding the mediators (which are integrated out)

Need substantial correction to SM tree-level process ⇒ forget about NP in loops

• Each ordering is convenient for a particular type of mediator Simplifies fits to all possible gauge invariant operators generating  $b \to c \tau \bar{\nu}$ 





#### **Operators convenient to consider**

Redundant set of operators, simplifies understanding of models:

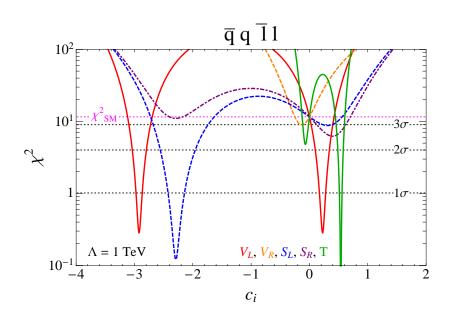
52	Operator		Fierz identity	Allowed Current	$\delta \mathcal{L}_{ ext{int}}$
$\mathcal{O}_{V_L}$	$(\bar{c}\gamma_{\mu}P_{L}b)(\bar{\tau}\gamma^{\mu}P_{L}\nu)$			$(1,3)_0$	$(g_q \bar{q}_L \boldsymbol{\tau} \gamma^{\mu} q_L + g_{\ell} \bar{\ell}_L \boldsymbol{\tau} \gamma^{\mu} \ell_L) W'_{\mu}$
$\mathcal{O}_{V_R}$ $\mathcal{O}_{S_R}$ $\mathcal{O}_{S_L}$ $\mathcal{O}_{T}$	$(\bar{c}P_Rb)(\bar{\tau}P_L\nu)$			$(1,2)_{1/2}$	$(\lambda_d ar{q}_L d_R \phi + \lambda_u ar{q}_L u_R i  au_2 \phi^\dagger + \lambda_\ell ar{\ell}_L e_R \phi)$
$\mathcal{O}'_{V_L}$	$(\bar{\tau}\gamma_{\mu}P_{L}b)(\bar{c}\gamma^{\mu}P_{L}\nu)$	$\longleftrightarrow$	$\mathcal{O}_{V_L}\Big\langle$	$(3,3)_{2/3}$	$\lambdaar{q}_Loldsymbol{ au}\gamma_\mu\ell_Loldsymbol{U}^\mu$
$\mathcal{O}'_{V_R}$	$(\bar{\tau}\gamma_{\mu}P_{R}b)(\bar{c}\gamma^{\mu}P_{L}\nu)$	$\longleftrightarrow$	$-2\mathcal{O}_{S_R}$	$(3,1)_{2/3}$	$(\lambda \bar{q}_L \gamma_\mu \ell_L + \tilde{\lambda} \bar{d}_R \gamma_\mu e_R) U^\mu$
$\mathcal{O}_{S_R}'$ $\mathcal{O}_{S_L}'$ $\mathcal{O}_T'$	$(\bar{\tau}P_Rb)(\bar{c}P_L\nu)$ $(\bar{\tau}P_Lb)(\bar{c}P_L\nu)$ $(\bar{\tau}\sigma^{\mu\nu}P_Lb)(\bar{c}\sigma_{\mu\nu}P_L\nu)$	$\longleftrightarrow$	2 2 0	$(3,2)_{7/6}$	$(\lambdaar{u}_R\ell_L+ ilde{\lambda}ar{q}_Li au_2e_R)R$
$\mathcal{O}_{V_L}''$ $\mathcal{O}_{V_R}''$ $\mathcal{O}_{S_R}''$ $\mathcal{O}_{S_L}''$ $\mathcal{O}_{T}''$	$(\bar{\tau}\gamma_{\mu}P_{L}c^{c})(\bar{b}^{c}\gamma^{\mu}P_{L}\nu)$ $(\bar{\tau}\gamma_{\mu}P_{R}c^{c})(\bar{b}^{c}\gamma^{\mu}P_{L}\nu)$ $(\bar{\tau}P_{R}c^{c})(\bar{b}^{c}P_{L}\nu)$ $(\bar{\tau}P_{L}c^{c})(\bar{b}^{c}P_{L}\nu)$ $(\bar{\tau}P_{L}c^{c})(\bar{b}^{c}P_{L}\nu)$ $(\bar{\tau}\sigma^{\mu\nu}P_{L}c^{c})(\bar{b}^{c}\sigma_{\mu\nu}P_{L}\nu)$	$\longleftrightarrow$ $\longleftrightarrow$ $\longleftrightarrow$	$-2\mathcal{O}_{S_R}$ $\frac{1}{2}\mathcal{O}_{V_L} \left\langle -\frac{1}{2}\mathcal{O}_{S_L} + \frac{1}{8}\mathcal{O}_T \right.$	$(\bar{3},2)_{5/3}$ $(\bar{3},3)_{1/3}$ $(\bar{3},1)_{1/3}$	$egin{aligned} (\lambdaar{d}_R^c\gamma_\mu\ell_L +  ilde{\lambda}ar{q}_L^c\gamma_\mu e_R)V^\mu \ \lambdaar{q}_L^ci au_2oldsymbol{ au}\ell_Loldsymbol{S} \end{aligned} \ (\lambdaar{q}_L^ci au_2\ell_L +  ilde{\lambda}ar{u}_R^ce_R)S \end{aligned}$

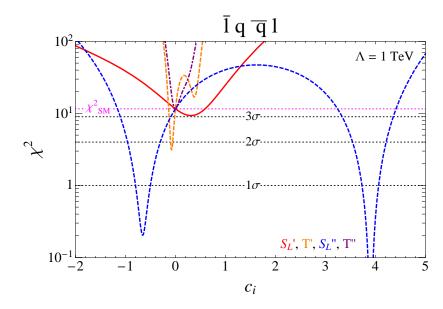
(Usually only the first 5 operators are considered)





## Fits for a single operator

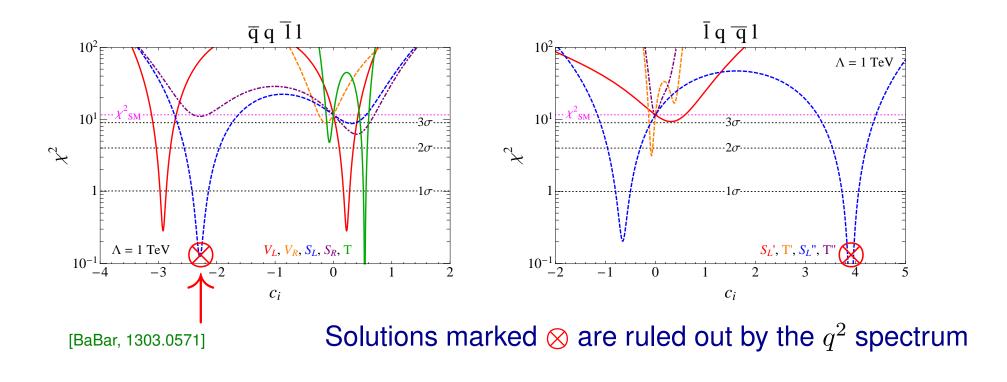








#### Fits for a single operator



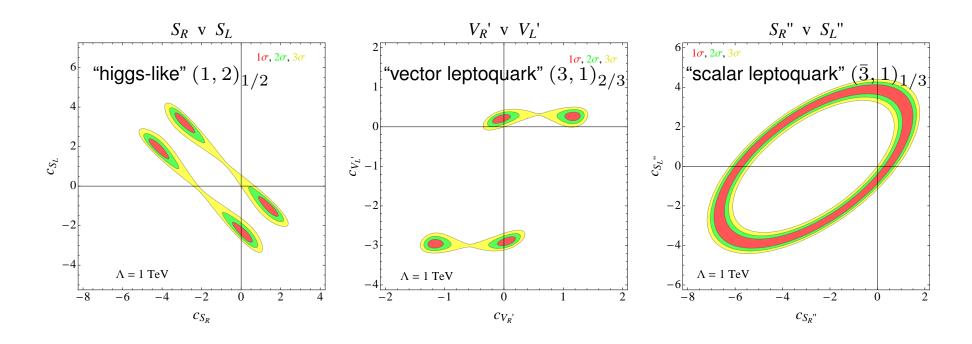
We rederived everything from scratch (beware of mis-Fierzing in some papers)

Agree (up to minor typos) with "classic" paper: Goldberger [hep-ph/9902311]





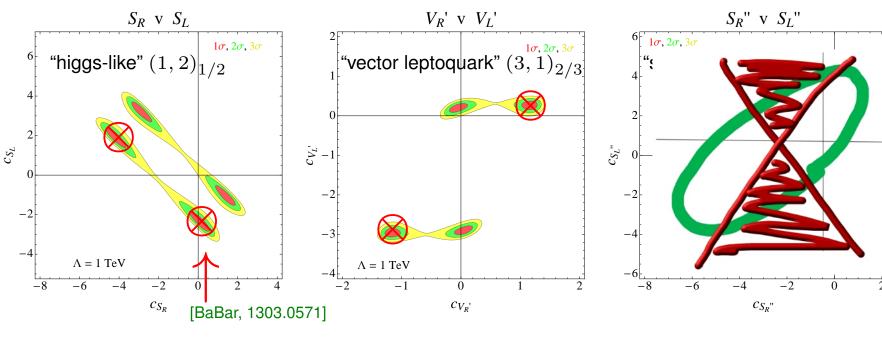
#### Fits for two operators





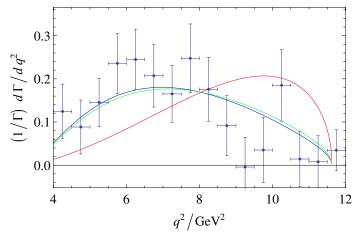


#### Fits for two operators



#### Operator coefficients

$$C'_{V_L} = 0.2$$
  $C'_{V_R} = 1.2$   $C'_{V_L} = 0.2$   $C'_{V_R} = -0.02$   $C''_{S_R} = 0.27$   $C''_{S_L} = -0.27$ 

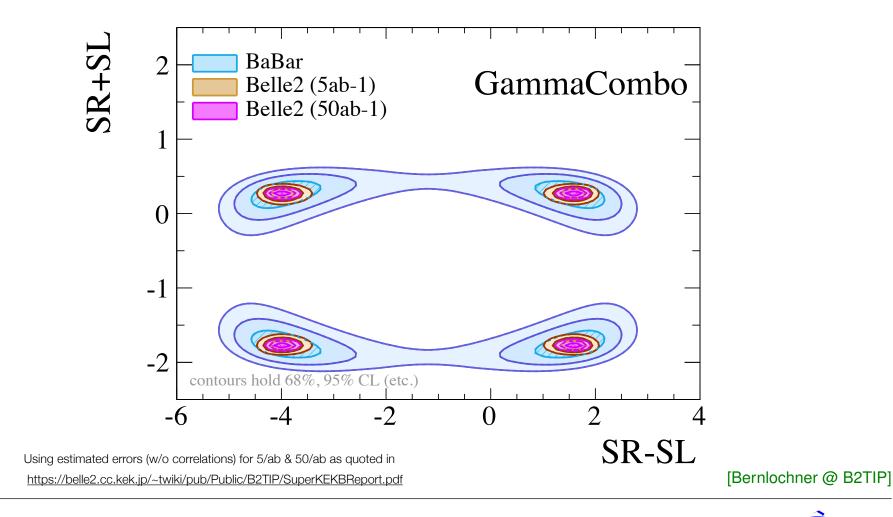






#### Future sensitivity — a rough estimate

#### Belle2 with 5/ab & 50/ab







# Flavor symmetries for $b ightarrow c au ar{ u}$

#### **Viable mediators**

• Good fits for several mediators: scalar, "Higgs-like"  $(1,2)_{1/2}$  vector, "W'-like"  $(1,3)_0$  "scalar leptoquark"  $(\bar{3},1)_{1/3}$  or  $(\bar{3},3)_{1/3}$  "vector leptoquark"  $(3,1)_{2/3}$  or  $(3,3)_{2/3}$ 

• Surprising if only BSM operator had  $(\overline{b}c)(\overline{ au}
u)$  flavor structure

Consider MFV and  $U(2)^3$  models / scenarios

[Fajfer, Kamenik, Nisandzic, Zupan, 1206.1872]

- Focus on quark flavor, assume only coupling to  $\tau$  This is an assumption in the MFV case, more natural in  $U(2)^3$  models
- Bounds:  $b \to s\nu\bar{\nu}$ ,  $D^0$  &  $K^0$  mixing,  $Z \to \tau^+\tau^-$ , LHC contact int.,  $pp \to \tau^+\tau^-$ , etc.
- Enough to eliminate some scenarios





#### Eliminating "W'-like" and "Higgs-like" models

- ullet A vector mediator with W' quantum numbers has to be a flavor singlet to couple to both quark and lepton pairs
  - ⇒ Couplings to lighter generations cannot be suppressed
  - ⇒ Collider limits exclude such models by orders of magnitude
- ullet Similar to the W', a scalar must be a flavor singlet to have all necessary couplings
  - ⇒ Must have coupling ratios to different flavors like a (charged) Higgs
  - $\Rightarrow D \overline{D}$  mixing data excludes observed  $B \to D^{(*)} \tau \bar{\nu}$  excess
- Left with models with leptoquark quantum numbers





#### **MFV** leptoquarks

Assign charges under:

$$U(3)_Q \times U(3)_u \times U(3)_d$$

Possible choices:

scalars:  $S \sim (\overline{\bf 3}, {\bf 1}, {\bf 1}), ({\bf 1}, \overline{\bf 3}, {\bf 1}), ({\bf 1}, {\bf 1}, \overline{\bf 3})$ 

vectors:  $U_{\mu} \sim (\mathbf{3}, \mathbf{1}, \mathbf{1})$ ,  $(\mathbf{1}, \mathbf{3}, \mathbf{1})$ ,  $(\mathbf{1}, \mathbf{1}, \mathbf{3})$ 

- $S(\overline{\bf 3},{f 1},{f 1})$  and  $U_{\mu}({f 3},{f 1},{f 1})$  give large  $pp o au^+ au^-$ , excluded by Z' searches
- $S({f 1},{f ar 3},{f 1})$  and  $U_{\mu}({f 1},{f 3},{f 1})$  give  $y_c$  suppressed  $B o D^{(*)} au ar 
  u$  contributions  $\Rightarrow$  too large couplings or too light leptoquarks
- Possibly viable:  $S(\mathbf{1},\mathbf{1},\overline{\mathbf{3}})$  and  $U_{\mu}(\mathbf{1},\mathbf{1},\mathbf{3})\Rightarrow$  consider in more detail Both can be electroweak singlets or triplets





## The $S(1,1,\bar{3})$ Lagrangians

Interactions terms for electroweak singlet:

$$\mathcal{L} = S(\lambda Y_d^{\dagger} \bar{q}_L^c i \tau_2 \ell_L + \tilde{\lambda} Y_d^{\dagger} Y_u \bar{u}_R^c e_R)$$

$$= S_i(\lambda y_{d_i} V_{ji}^* \bar{u}_{Lj}^c e_L - \lambda y_{d_i} \bar{d}_{Li}^c \nu_L + \tilde{\lambda} y_{d_i} y_{u_j} V_{ji}^* \bar{u}_{Rj}^c e_R)$$

Integrating out S, contribution to  $R(X_c)$  via:  $(m_{S_3} \neq m_{S_1} = m_{S_2})$ 

$$-rac{V_{cb}^*}{m_{S_3}^2}\Big(\lambda^2y_b^2\,{\cal O}_{S_R}^{\prime\prime}+\lambda ilde{\lambda}y_cy_b^2\,{\cal O}_{S_L}^{\prime\prime}\Big)$$

[electroweak triplet has no  $\tilde{\lambda}$  term]

• Can fit  $R(D^{(*)})$  data iff  $y_b = \mathcal{O}(1)$ 





## The $U_{\mu}(1,1,3)$ Lagrangians

Interactions terms for electroweak singlet:

$$\mathcal{L} = (\lambda \, \bar{q}_L Y_d \gamma_\mu \ell_L + \tilde{\lambda} \, \bar{d}_R \gamma_\mu e_R) \, U^\mu$$
$$= (\lambda y_{d_i} V_{ji} \, \bar{u}_{Lj} \gamma_\mu \nu_L + \lambda y_{d_i} \bar{d}_{Li} \gamma_\mu \tau_L + \tilde{\lambda} \bar{d}_{Ri} \gamma_\mu \tau_R) \, U_i^\mu$$

As before, contribution to  $R(X_c)$  via:  $(m_{U_3} \neq m_{U_1} = m_{U_2})$ 

$$rac{V_{cb}}{m_{U_3}^2} \Big( \lambda^2 y_b^2 \, {\cal O}_{V_L}^\prime + \lambda ilde{\lambda} y_b \, {\cal O}_{V_R}^\prime \Big)$$

[Again, electroweak triplet has no  $\tilde{\lambda}$  term]

• Can fit  $R(D^{(*)})$  data iff  $y_b = \mathcal{O}(1)$ 

[NB: vector leptoquarks are hard to make sense of as a low energy effective theory, without knowing the UV completion — divergences]





#### Constraints from $b o s u ar{ u}$

With three Yukawa spurion insertions, can write:

$$\lambda' S Y_d^{\dagger} Y_u Y_u^{\dagger} \, \bar{q}_L^c i \tau_2 \ell_L$$

Leads to operators of the form:

$$rac{V_{tb}^{st}V_{ts}}{2m_{S_3}^2}\,y_t^2y_b^2\,\lambda^\prime\lambda\,(ar{b}_L\gamma^\mu s_L\,ar{
u}_L\gamma_\mu
u_L)$$

• Current limits from  $B \to K \nu \bar{\nu}$  require:

$$\lambda'/\lambda \lesssim 0.07$$

• A vector singlet is the only one of the four leptoquarks without such a constraint (E.g., vector triplet has  $\lambda' \bar{q}_L Y_u Y_u^\dagger Y_d \boldsymbol{\tau} \gamma_\mu \ell_L \boldsymbol{U}^\mu$  term)





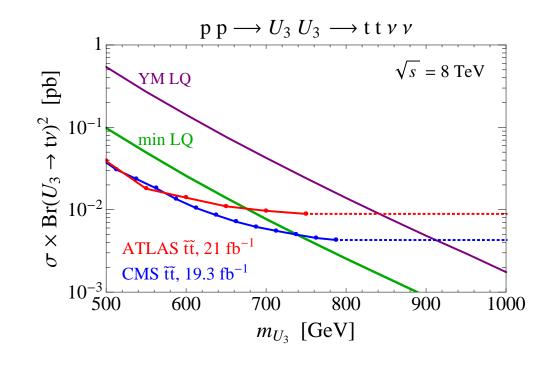
## $U_{\mu}(1,1,3)$ — LHC constraints

- The  $\tilde{\lambda}$  term for electroweak singlet vector leptoquark gives unsuppressed coupling to 1st generation
  - $\Rightarrow$  constraints from t-channel exchange in  $pp \to \tau^+ \tau^- \ \Rightarrow \ \tilde{\lambda} \lesssim 0.15 \, \lambda$
- Limits on  $m_{U_3}$  from direct leptoquark search ( $b\tau$ ) or recasting stop ( $t\nu$ ) searches:

Ambiguities related to possible "dipole" term:  $-ig_s\kappa~U_{\mu}^{i\dagger}t_{ij}^aU_{\nu}^j~G_a^{\mu\nu}$ 

Find:  $m_{U_3} \gtrsim 750 \, \text{GeV}$ 

ullet For S, CMS search for third generation scalar LQ decaying to t au gives  $m_{S_3} \gtrsim 500\,{
m GeV}$  [CMS-PAS-EXO-13-010]







#### **Additional constraints**

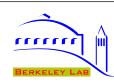
• Main constraints from loop processes: (i) meson mixings, and (ii) electroweak precision corrections to  $R(Z \to \tau^+\tau^-)$  and  $A(Z \to \tau^+\tau^-)$ 

Scalar LQ calculable, for vector LQ need prescription for UV divergence of loops

[Jure et al. (1206.1872) dismissed scalar due to PEW constraints, we think there is marginal room]

Bounds are satisfied, although some constraints are tight





# Final comments

#### Several possible tests & consequences

- LHC: several extensions to current searches would be interesting:
  - Searches for  $t\tau$  and  $b\tau$  resonances
  - Extensions of stop/sbottom searches to higher prod. cross sections ( $t\nu$  and  $b\nu$ )
  - Searches for states appearing on-shell in t- but not in s-channel in pp collisions
  - Enhanced  $h \to \tau^+ \tau^-$  rate (and  $t \to c \tau^+ \tau^-$  [tough])
- Low energy probes:
  - Firm up  $B \to D^{(*)} \tau \bar{\nu}$  rate and kinematic distributions; Cross checks w/ inclusive
  - Smaller theor. error in  $[d\Gamma(B \to D^{(*)}\tau\bar{\nu})/dq^2]/[d\Gamma(B \to D^{(*)}l\bar{\nu})/dq^2]$  at same  $q^2$
  - Improve bounds on  $\mathcal{B}(B \to K^{(*)} \nu \bar{\nu}$
  - $\mathcal{B}(D \to \pi \nu \bar{\nu}) \sim 10^{-5}$  possible, maybe observable at BES III
  - $\mathcal{B}(B_s \to \tau^+\tau^-) \sim 10^{-3}$  possible





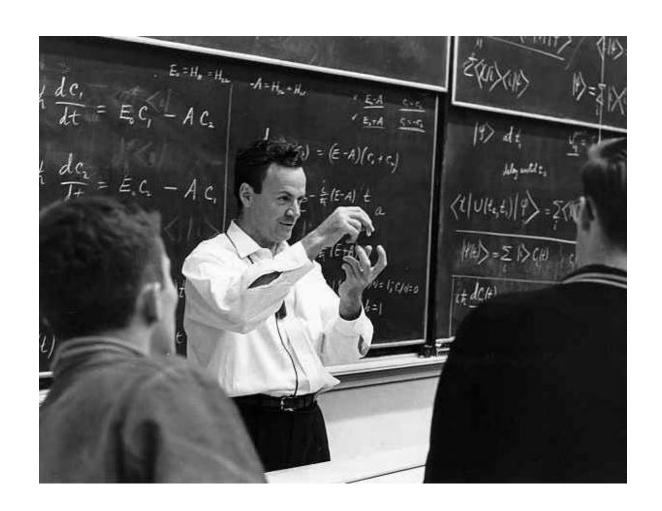
#### **Conclusions**

- Amusing if NP shows up in an operator w/o much CKM and loop suppression
- Despite statements in the literature, possible to write down (somewhat) sensible models for  $B \to D^{(*)} \tau \bar{\nu}$  excesses, with extensions to other flavors
- Several simple extensions to current LHC searches could cover much of this parameter space (see anomalies or rule out models)
- Measurements of  $b \to c \tau \bar{\nu}$  will improve in the next decade by order of magnitude (Even if central values change, plenty of room for significant deviations from SM)





#### Ultimately, data will tell



"It doesn't matter how beautiful your theory is, it doesn't matter how smart you are. If it doesn't agree with experiment, it's wrong."

[Feynman]