

# Optical Beam Diagnostics: Transverse Phase Space Measurements

Ralph Fiorito

University of Liverpool, Cockcroft Institute  
Daresbury, UK

## Topics : use of beam based optical radiation to measure transverse beam properties

- size, space distribution  $(x, y)$  [OTR, OSR]
- divergence  $(x', y')$ , [OTR, ODR, OSR interferences]
- trajectory angle “
- rms emittance  $(e_x, e_y)$  “
- phase space mapping  $(x, x'), (y, y')$  “

Exclusions (will be talked about via other speakers)

- Laser wires
- Coherent optical radiation generated at optical wavelengths due to microbunching
- EO methods, Compton and Thomson scattering
- Longitudinal beam properties

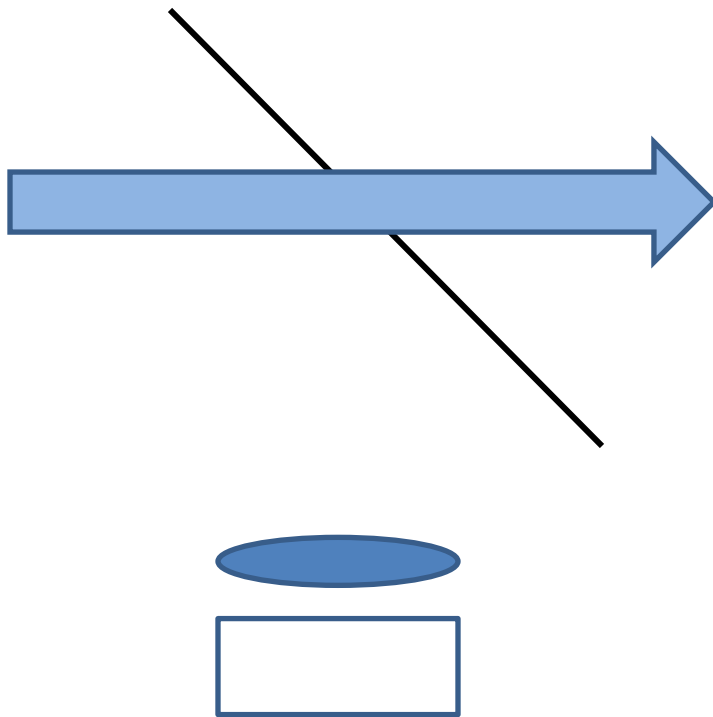
# I. Optical Beam Profiling Methods

Traditional Imaging: uses beam based radiations, e.g. OTR ,OSR, ODR, OCR, etc. or fluorescent screens, e.g. phosphors, YAG crystals, etc. (width of the PSF limits the resolution of these measurements- determined by the first few decades of intensity)

High Dynamic Range Imaging: HDR cameras (CMOS, CID), Segmented HDR imaging with spatial light modulators (e.g. DMD) (intensity distribution of the PSF limits these measurements)

Indirect Beam Size Measurement: Young's double slit interferometry - measures the degree of spatial coherence of optical radiation produced by the beam (depends on the size of the source; first used by Michelson to measure the size of stars).

# Optical Transition Radiation



OTR Beam PSF determines  
Resolution: 2-3 lens diffraction  
limit from point source

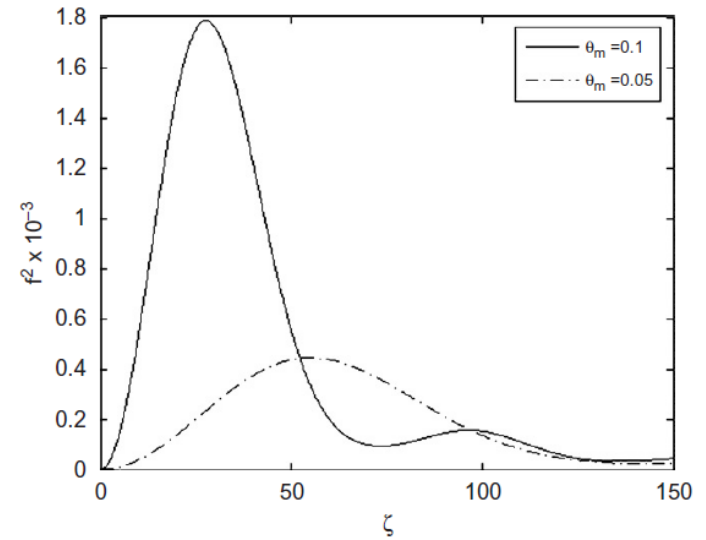


Fig. 2. PSF of a single electron for TR.  $\gamma = 1000$ .

# OTR vs inorganic scintillators at a glance

## OTR

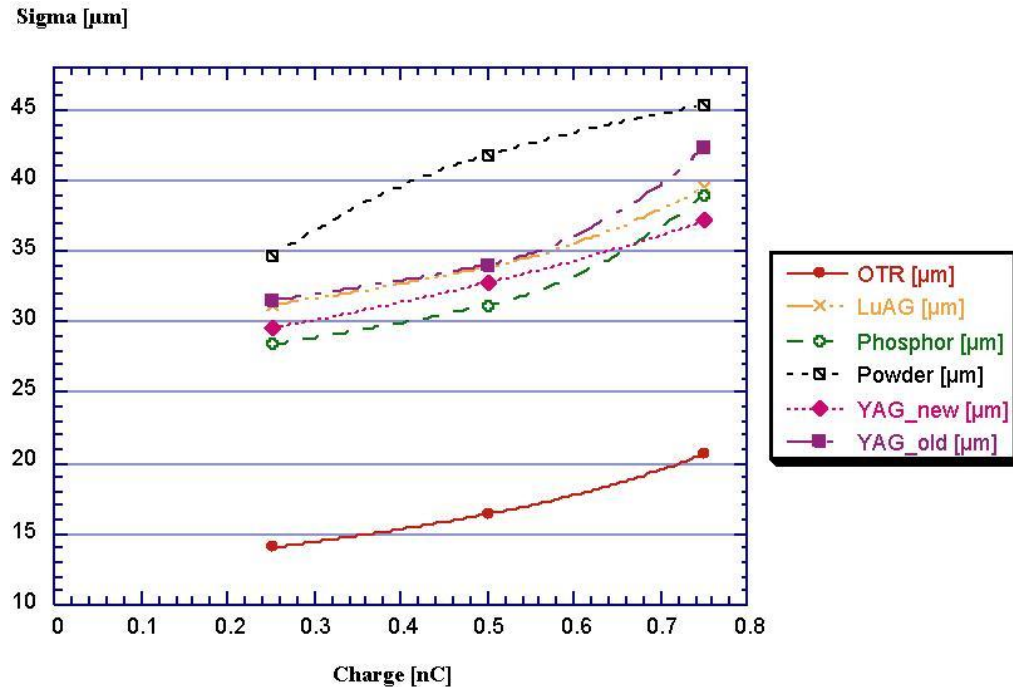
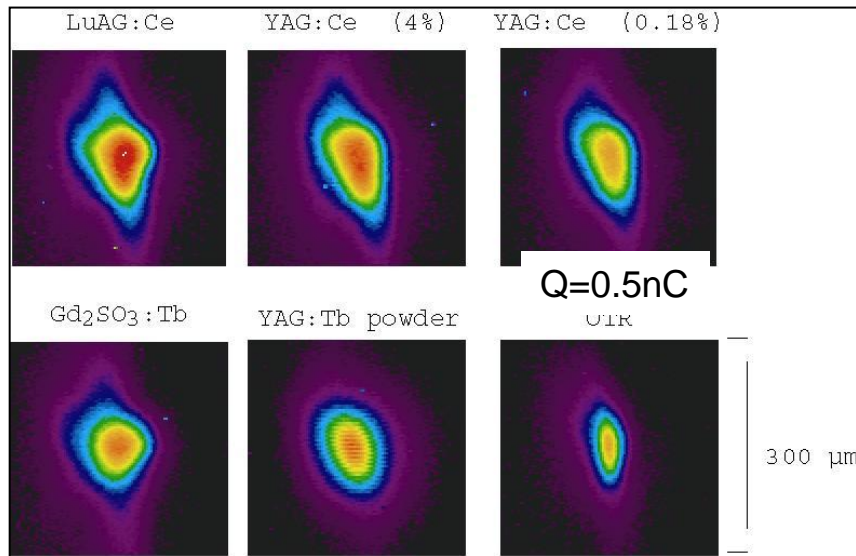
- Rapid (<fs) emission
- linearity (no saturation effects)
- high resolution (PSF  $\sim$  point source)
- surface effect: thickness doesn't matter
- small perturbation to the beam (small thickness)
- small radiation background (small thickness)
- can be used in a wide range of  $\gamma$
- relatively low photon yield (1 photon/137 electrons)

## Scintillators (YAG:Ce, YAP:Ce, oth.)

- high sensitivity +yield
- no grain structure
- time response  $\sim$  100ns
- conformance to HV
- radiation resistance
- bulk effect+space charge (cause saturation and limit resolution)

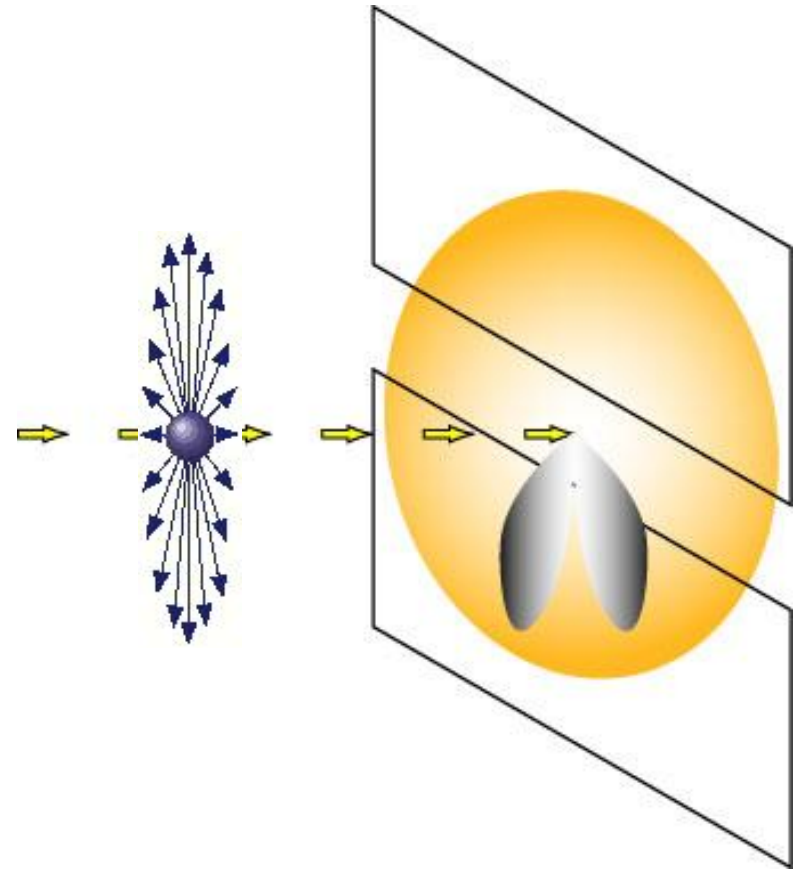
# OTR/Scintillator resolution

Experiments at BNL\* showed discrepancy in the beam size measurements compared to OTR and wire scans and is charge dependent.



# Diffraction radiation

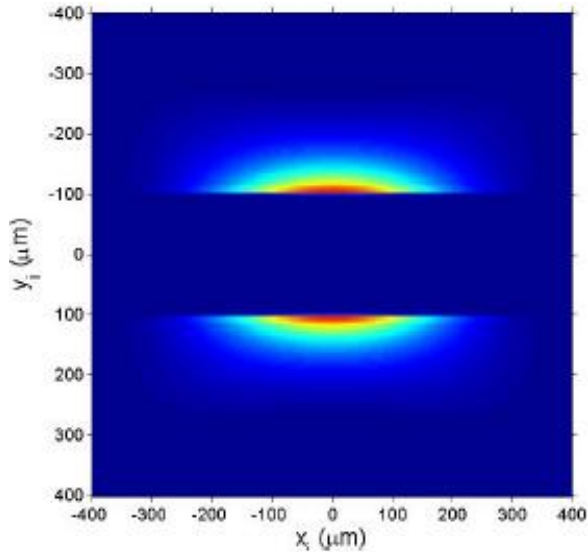
- **Diffraction radiation** is emitted when a particle passes in the proximity of optical discontinuities (apertures )
- **DR characteristics** depend on the ratio of the aperture size to the parameter  $\lambda\gamma$
- **DR intensity** strongly suppressed at wavelengths  $\lambda < a/\gamma$



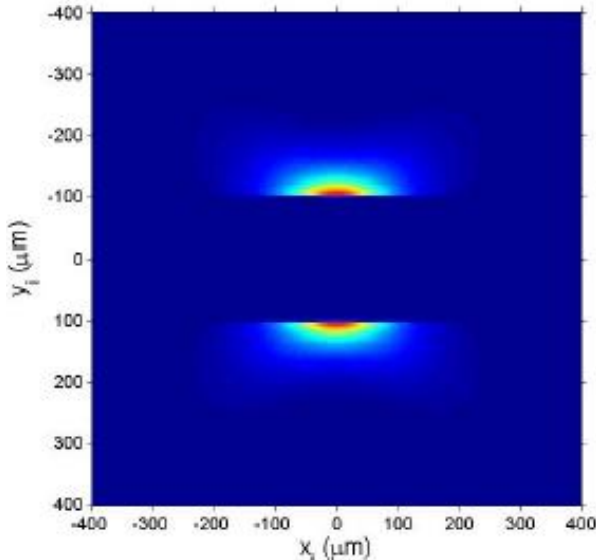
# Restoration of Beam Profile from Source Image of ODR\*

( example:  $\gamma = 2500$ ;  $\lambda = 0.5\text{m}$ ;  $\theta = 0.1$ )

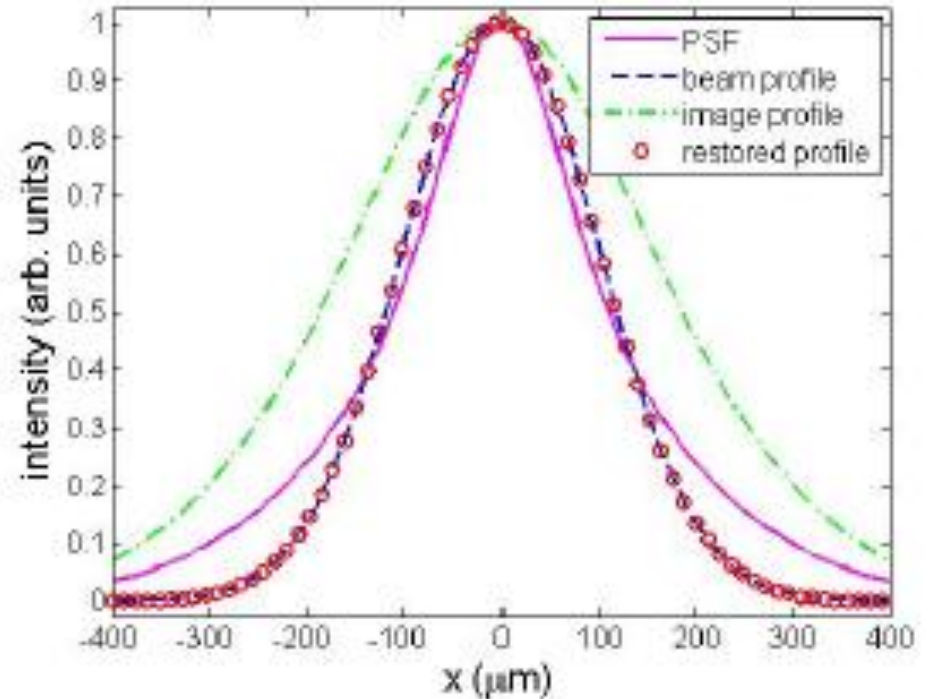
ODR  
Distribution  
from  
Gaussian  
Beam



PSF



Vertical Profiles

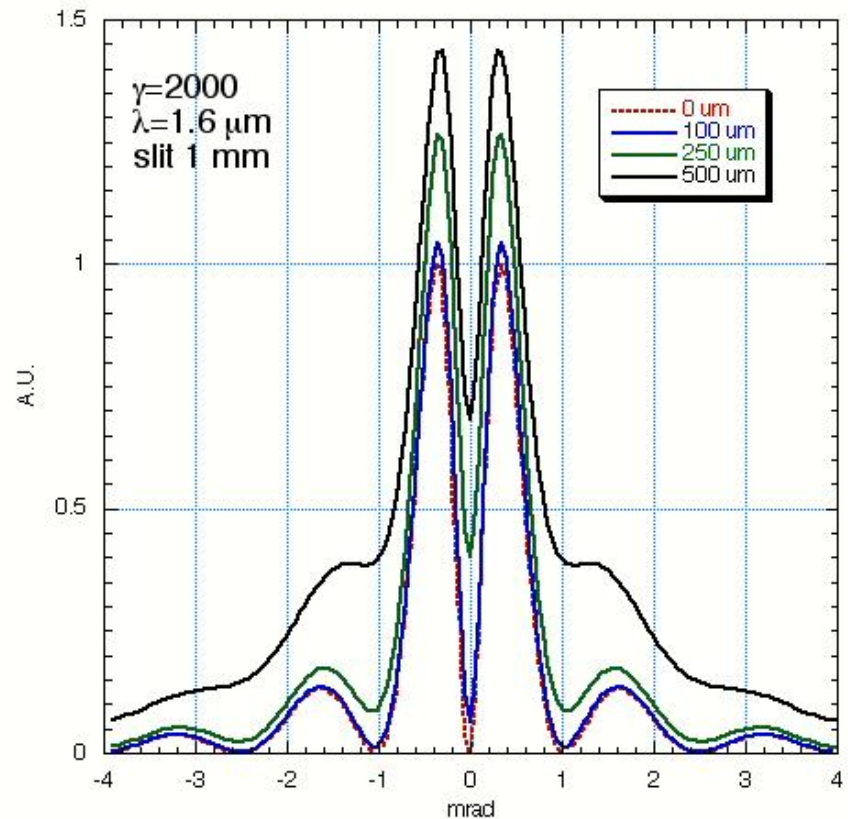


\*D.Xiang, et. al. PRSTAB 2007



# Effect of the beam size on Far Field ODR

- Angular distribution depends on the relative particle position with respect to the aperture and can be used to measure the beam size
- Energy and angular spread, detector bandwidth are interfering factors



# High Dynamic Range Beam/Halo Imaging

## OPTIONS

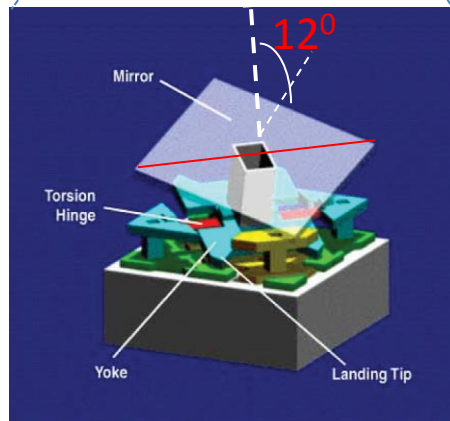
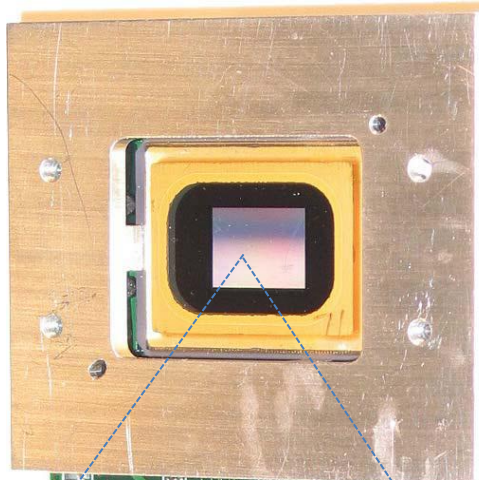
HDR CID or CMOS Cameras: expensive

Saturated/ Unsaturated sensors: cross talk possible in sensor; does not reduce scattering in optics from central beam core

Digital Micro-array Method: versatile programable masking  
reduces scattering of light in primary optics  
any type of camera can be used  
diffractive imaging possible

# DMD Technology

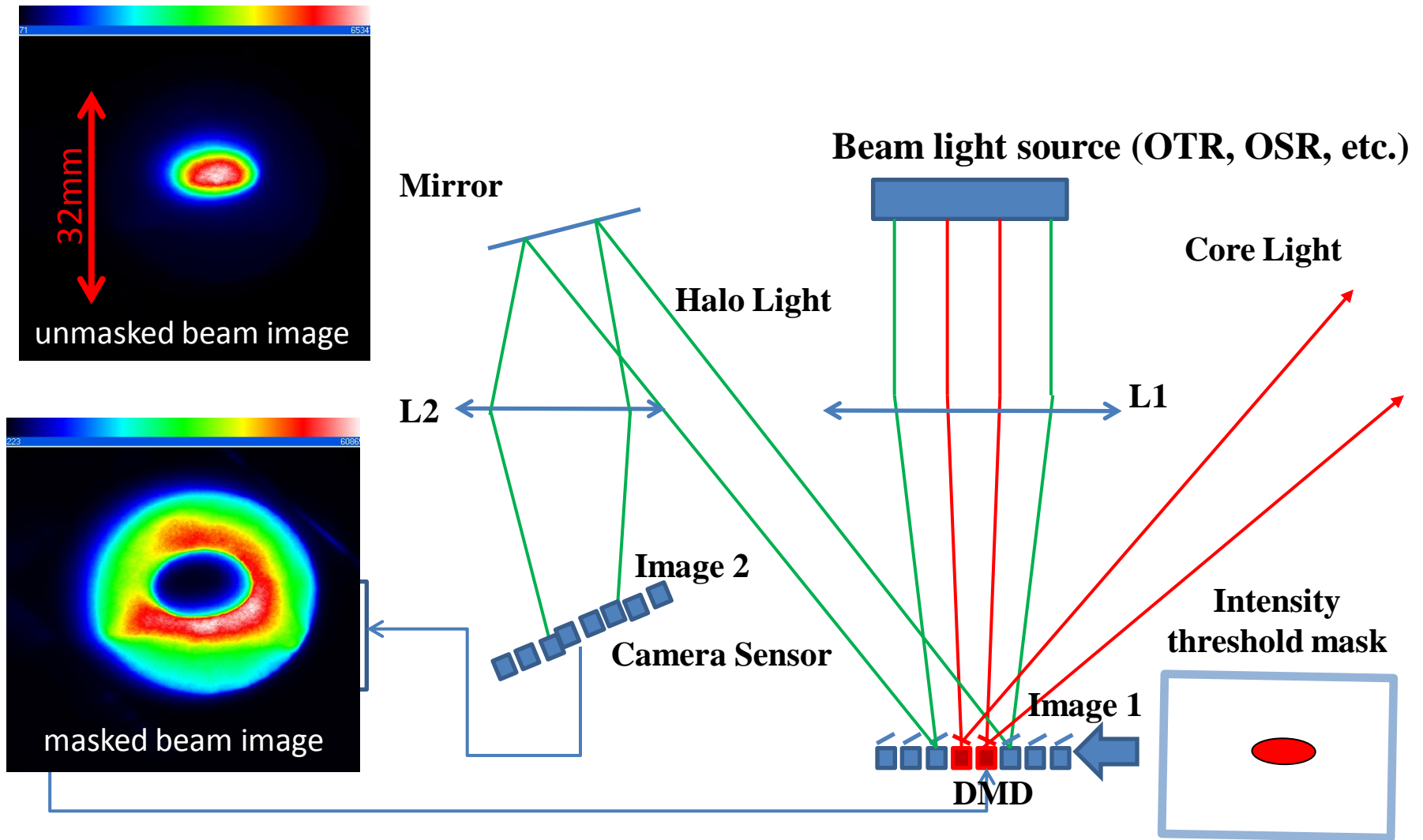
\*DLP™ Texas Instruments Inc.



Array dimensions: 14 x 10 mm  
Pixels: 1024 x 768,  
Pixel dimension: 14x14  $\mu$ m  
Switching rate: 9600-32000 fps  
Individual pixel addressable

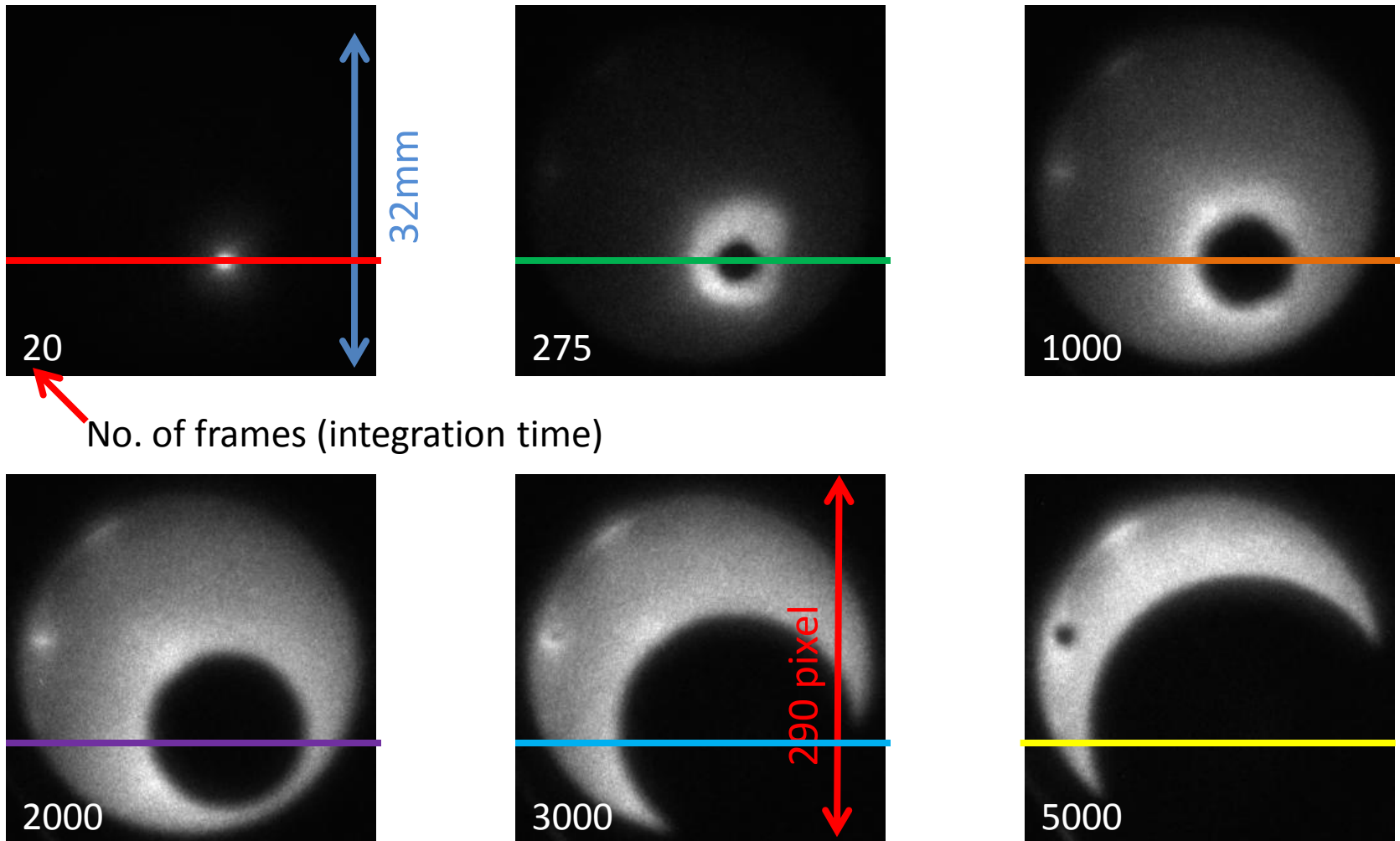
Uses: 1-Spatial light modulator  
2-Adaptive optical Mask

# Optical Technique for DMD based Beam Halo Imaging\*

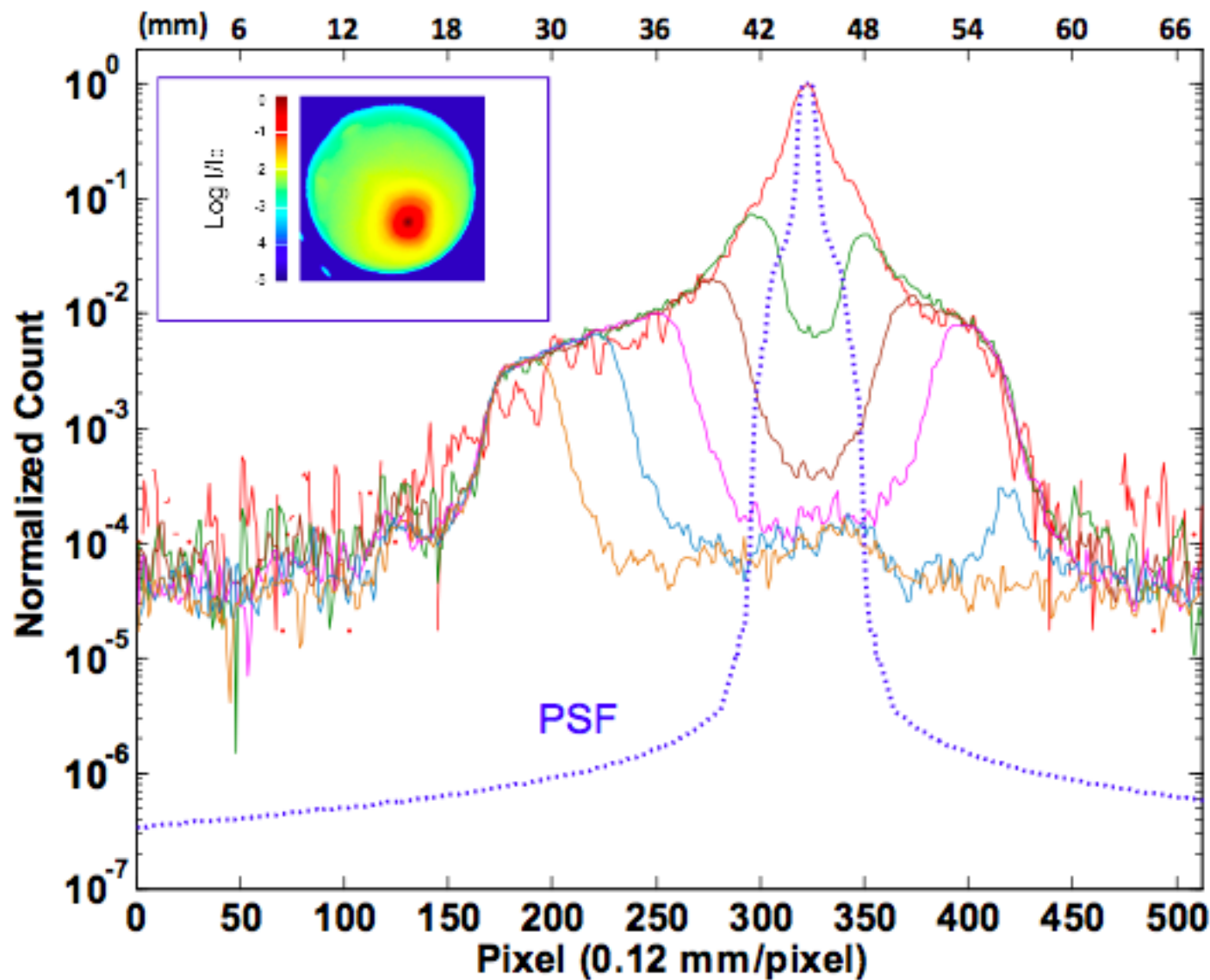


\*H. Zhang, et. al. Phys. Rev. ST Accel. and Beams (2012)

# Dynamic range measurement of imaging system using DMD as an optical mask with phosphor screen (21mA ebeam)



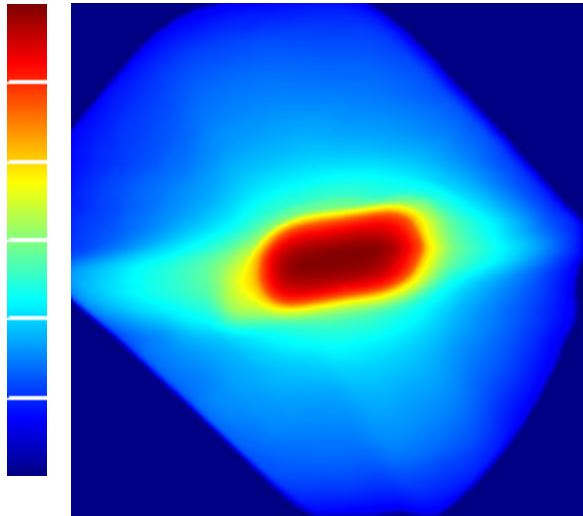
# Dynamic Range and Point Spread Function Measurements for UMER



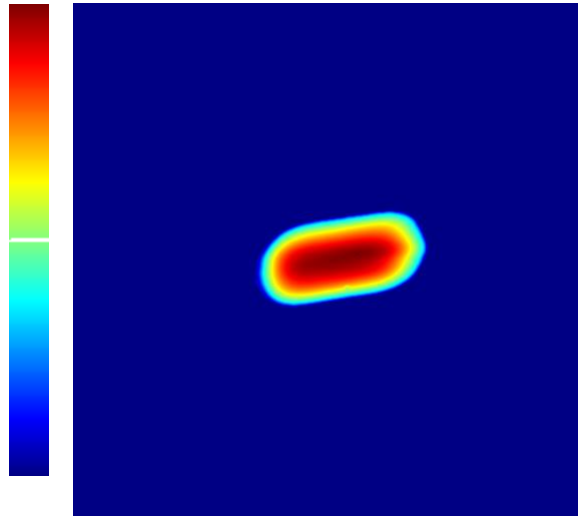
# Reconstructed intensity distribution $I(x,y)$ and calculated total radiant energy $E_{Total}$

Assume  $I(x,y) \sim J_{beam}(x,y) \Rightarrow E_{total} \sim Q_{beam}$

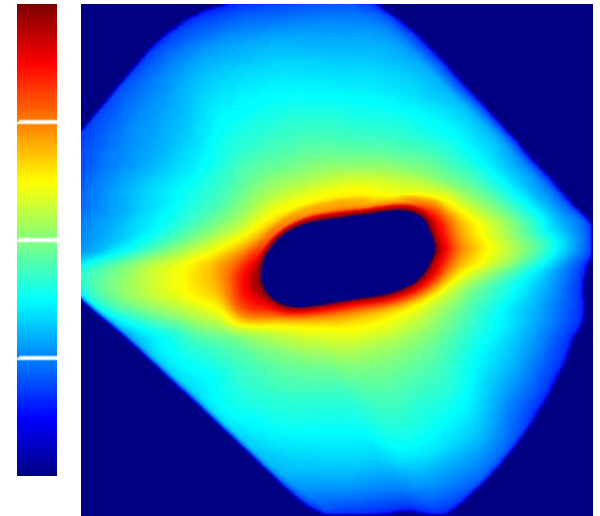
$(1 - 10^{-6}) I_{max}$



$(1 - 10^{-2}) I_{max}$



$(10^{-2} - 10^{-6}) I_{max}$



$$E_{Total} \equiv \int_S I(x, y) dx dy$$

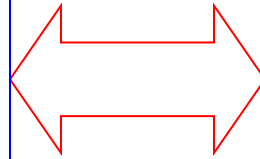
$$E \sim 0.99 E_{Total}$$

$$E \sim 0.01 E_{Total}$$

# RMS Emittance measurements

## Widely used techniques

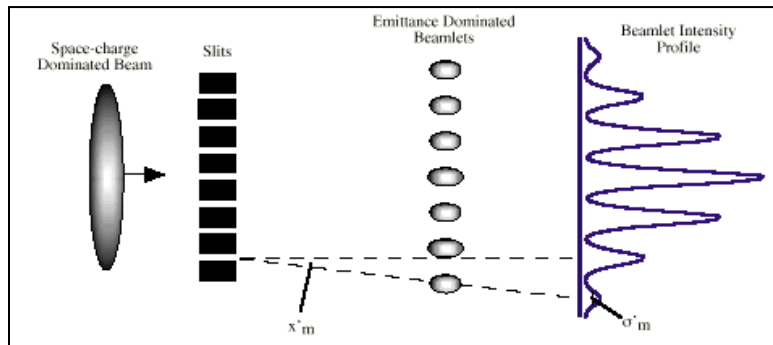
- Pepper-pot (multislit)
- Quadscan (beam size vs 1/f)
- 2 or more screens beam size



Space-charge forces

$$R = \frac{I\sigma^2}{2I_0\gamma\epsilon_n^2}$$

Measure of  
spaces-charge  
dominance





# Transverse rms Emittance using Angular and Spatial Distributions of OTR

1) Measurements at a beam waist:

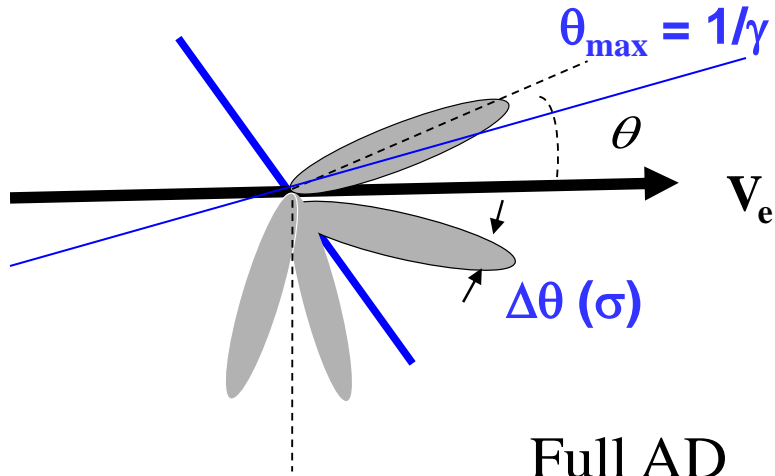
In addition to beam profile, measurement of beam divergence is required to construct

$$\left(\mathcal{E}_{r=x,y}^{rms}\right)^2 = \langle r^2 \rangle \langle r'^2 \rangle - \langle rr' \rangle^2$$

2) At beam minimum  $\langle rr' \rangle$  must be retrieved via an algorithm employing observables  $r_{rms}$  and  $r'_{rms}$ .

# OTR Angular Distribution Measures Divergence

*NOTE: far field OTR independent of beam size or position*



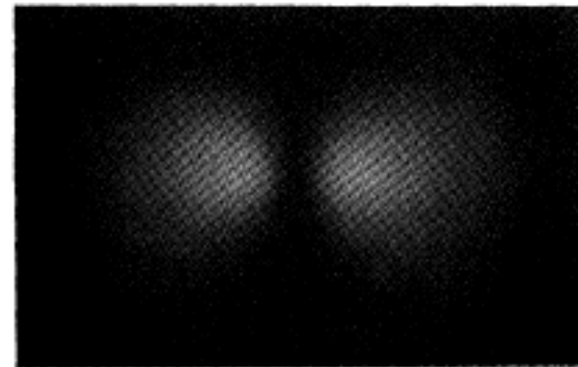
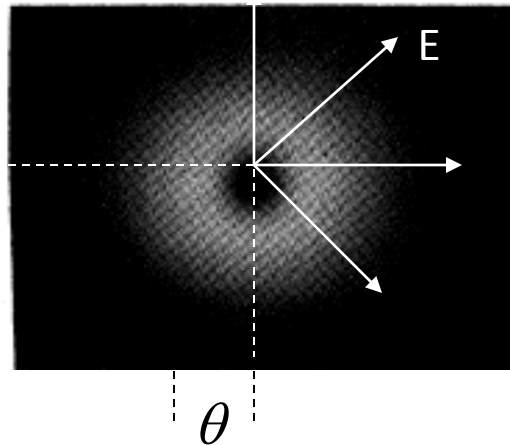
$$\frac{d^2 I^{(S)}}{d\omega d\Omega} = \frac{e^2}{c\pi^2} \frac{\theta^2}{(\gamma^{-2} + \theta^2)^2},$$

$$\theta \sim \gamma^{-1} \ll 1$$

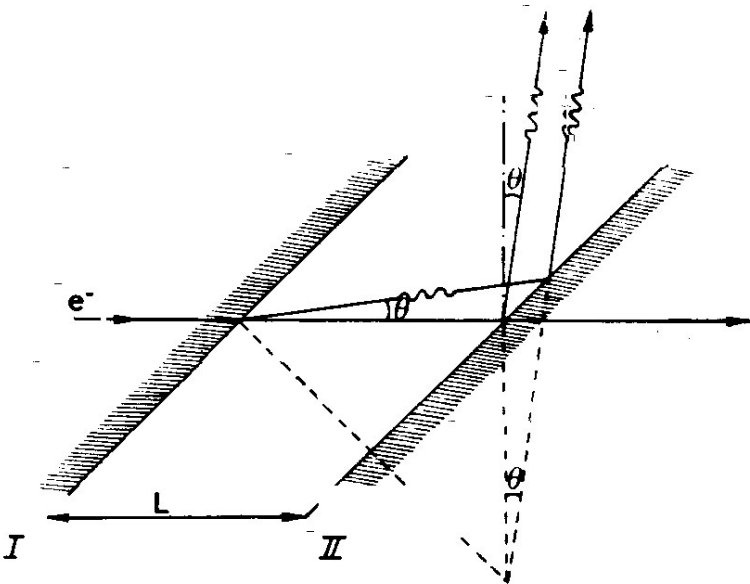
Full AD

Horizontally Polarized AD

Radially Polarized AD Pattern Centered on Direction of  $\mathbf{V}_e$



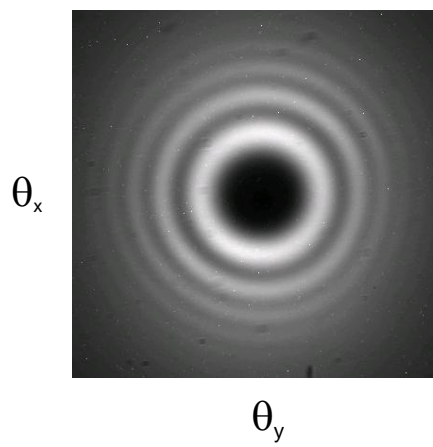
OTR Interferometry provides greater sensitivity to beam divergences  $x', y', E, \Delta E/E$



$$\frac{d^2 I_{TOT}}{d\omega d\Omega} = \left[ \frac{e^2}{c\pi^2} \frac{\theta^2}{(\gamma^{-2} + \theta^2)^2} \right] \left| 1 - e^{-i\phi} \right|^2,$$

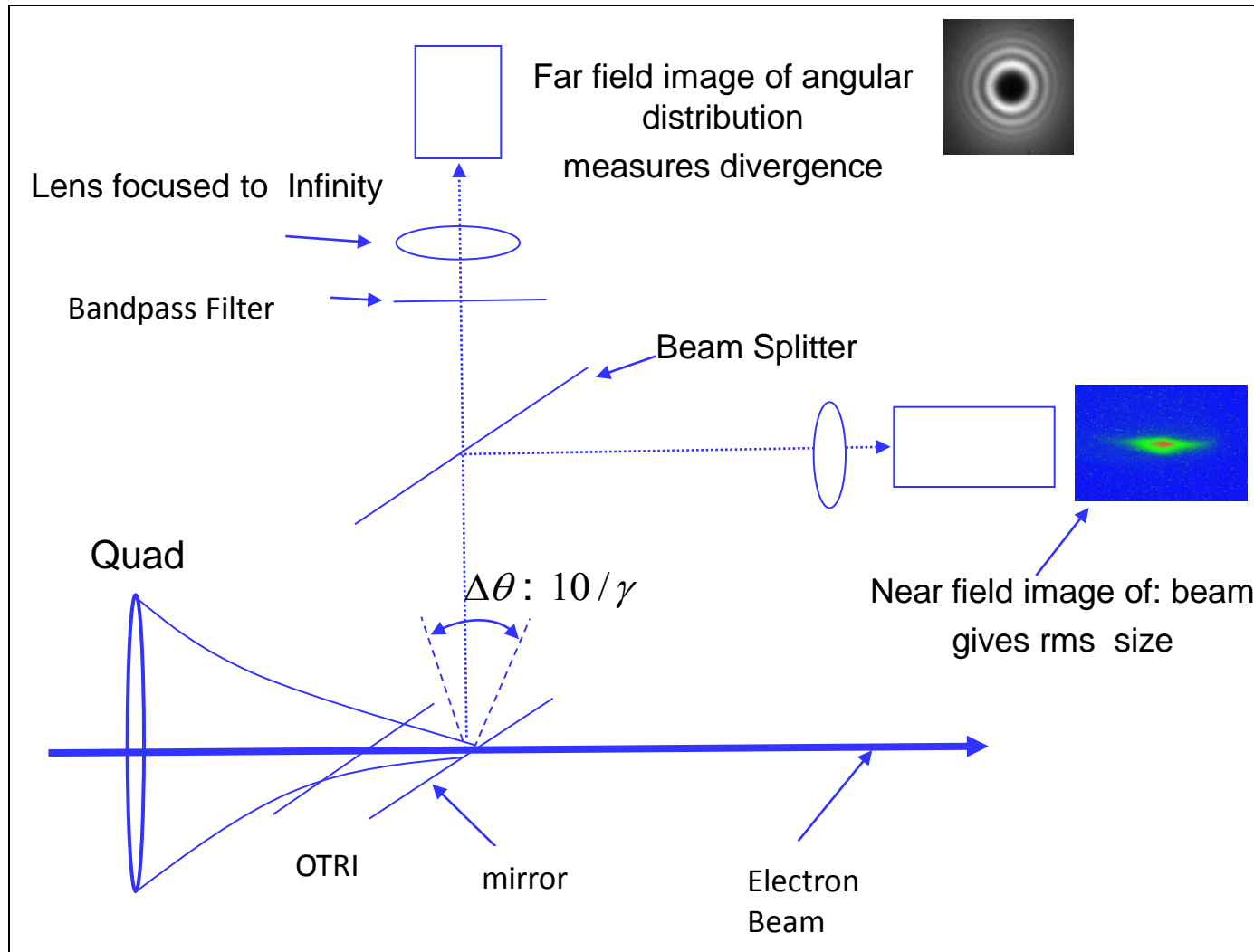
where:  $\phi = L/L_V$ ,  
(e-photon phase difference)

and:  $L_V = (\lambda/\pi)(\gamma^{-2} + \theta^2)^{-1}$   
(vacuum coherence length)



- Visibility of OTRI measures beam divergence (and/or  $\Delta E/E$ )
- Radial Polarization of OTRI can be used to separately measure  $x'$  and  $y'$  via polarizer
- Fringe position measures beam energy ( $E$ )

# Experimental Setup for OTR RMS Emittance Measurement



# New theory predicts correlation term ( $\langle r r' \rangle$ ) in terms of simple OTR observables $x_{rms}$ , $x'_{rms}$ , $y_{rms}$ , $y'_{rms}$

Emittance Dominated Beam

(C. Papadopolous, R. Fiorito PAC 09)

1) **true beam waist:**

difficult to achieve, i.e.

need to move screen along  $s$

$$\left. \frac{d(x(s, f))}{ds} \right|_{f=f_0} = \langle xx' \rangle = 0$$

2) **beam spot minimum:**

achievable with a usual quad scan, i.e. vary  $f$  and image beam with OTR

$$\left. \frac{d(x(s, f))}{df} \right|_{s=L} = 0 \rightarrow \langle xx' \rangle = \frac{1}{L} \langle x^2 \rangle$$

3) **divergence minimum:**

achievable by varying  $f$  and maximizing OTRI fringe visibility

$$\left. \frac{d(x'(s, f))}{df} \right|_{s=L} = 0 \rightarrow \langle xx' \rangle = L \langle x'^2 \rangle$$

# Theory predicts relative error in emittance measurements at beam size minimum

Example: JLAB 100 MeV, OTR measurement

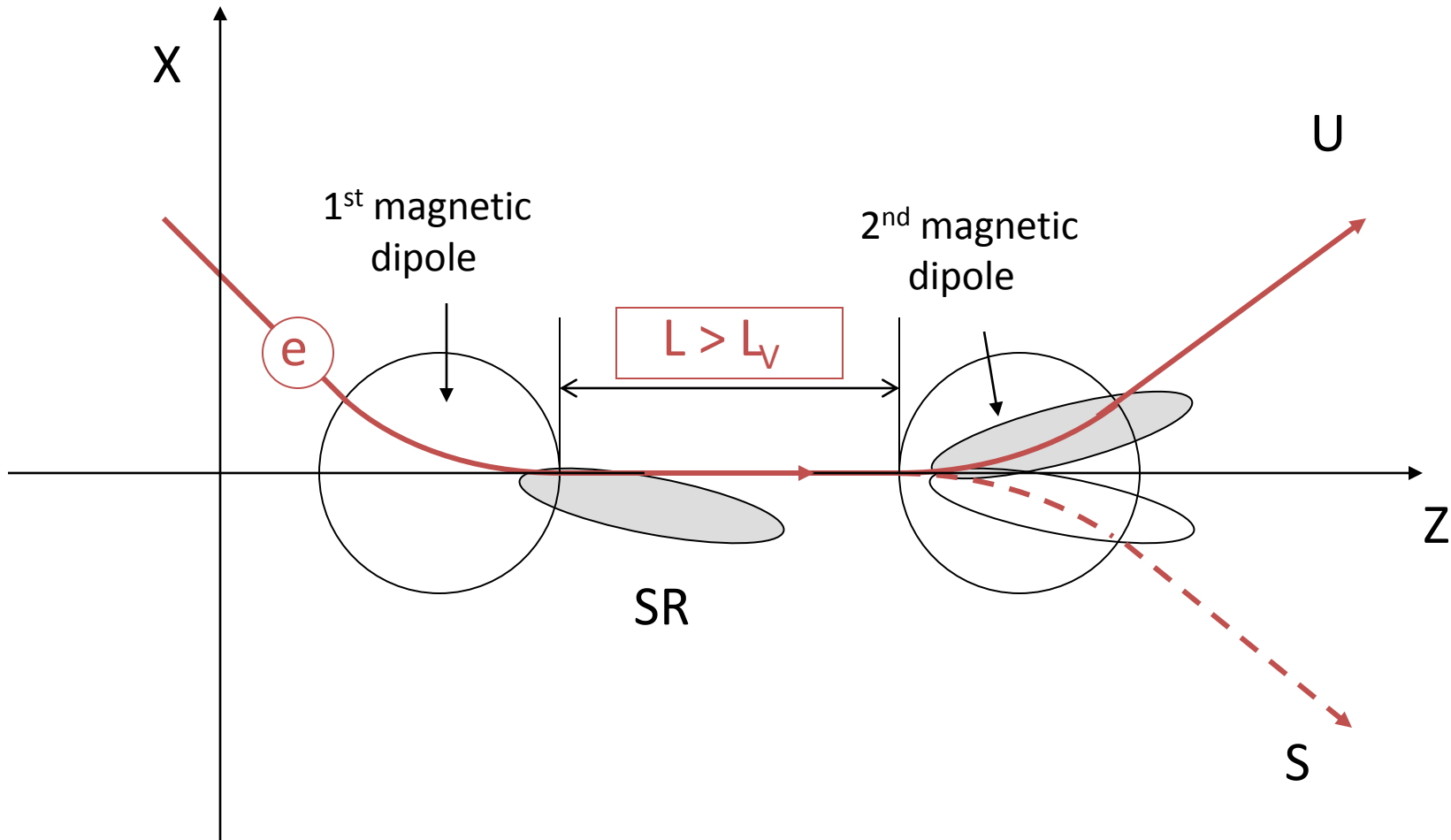
$$\frac{\Delta\varepsilon}{\varepsilon} = -\frac{1}{2} \frac{\langle yy' \rangle^2}{\langle y^2 \rangle \langle y'^2 \rangle} = -\frac{1}{2} \frac{\langle y^2 \rangle}{L^2 \langle y'^2 \rangle} \sim 4.4 \times 10^{-4}$$

- Caveats:
- 1) in general error may not be small
  - 2) space charge forces neglected in the analysis shown above  
recent new correlation term algorithm developed that computes correlation terms in the presence of space charge from two measurements of  $r$ ,  $r'$  and  $1/f$  \*

\*K. Poorrezaie, R. Fiorito, et. al. PRSTAB 20013

# Non Invasive Divergence Measurement using Optical Synchrotron Interferences (OSRI)

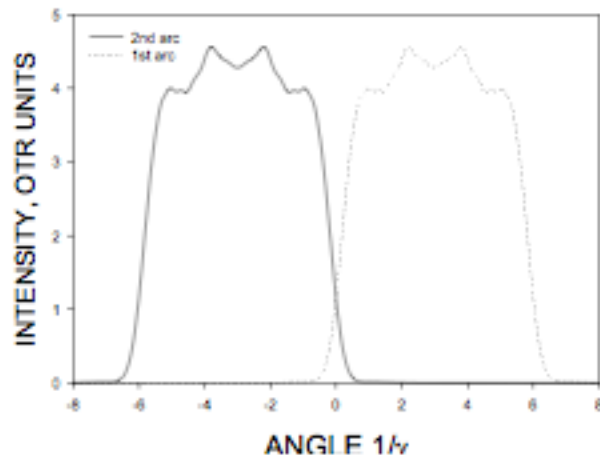
from two magnetic dipoles separated by a straight trajectory



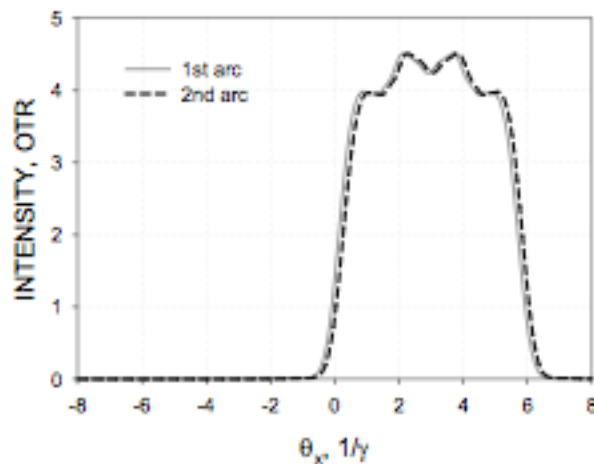
# Comparison of OSR from U and S Arcs For the 100 MeV JLAB ERL

(  $R = 1.09$  m,  $\lambda = 600$  nm,  $L = 46$  mm,  $\Delta\theta = 6/\gamma$ ,  $\theta_e = 0$  )

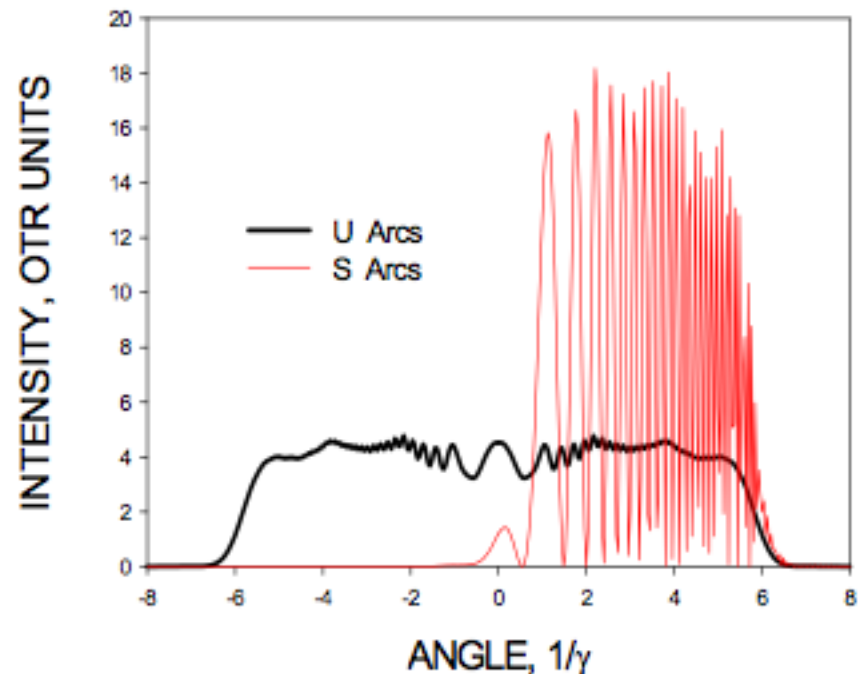
U  
arcs



S  
arcs



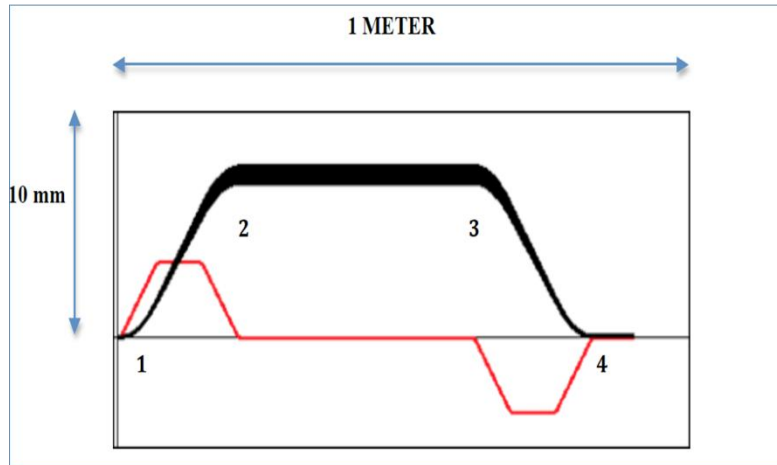
Interferences of OSR





# Non Invasive Emittance and Energy Spread Monitor using OSR Interferences

## Diagnostic Mini chicane Design with (1,2) 'S' and (2,3) 'U' Interferometers



### Properties of Chicane:

$B$  (100MeV) = 0.12 Tesla

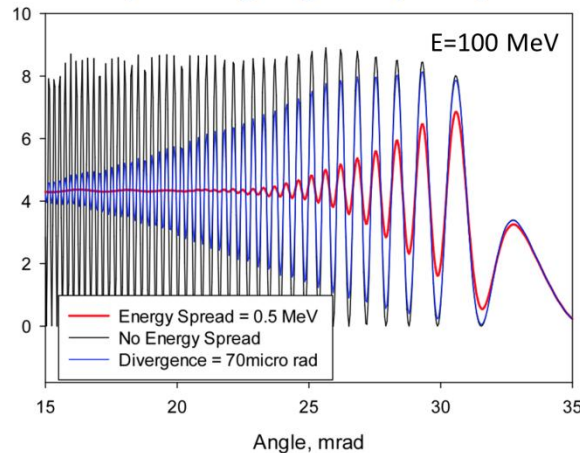
$B$ (285 MeV) = 0.35 Tesla

$L$  @magnet = 100 mm

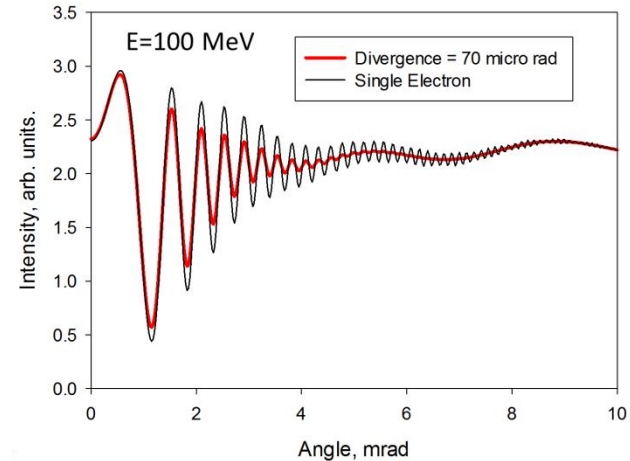
$L$  (2,3) = 600 mm

Angle deflection = 35 mrad

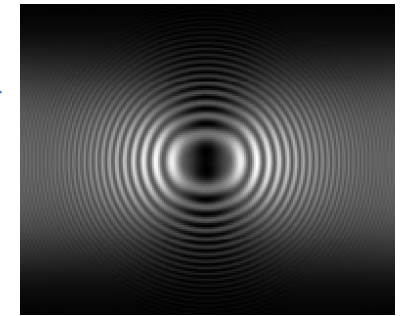
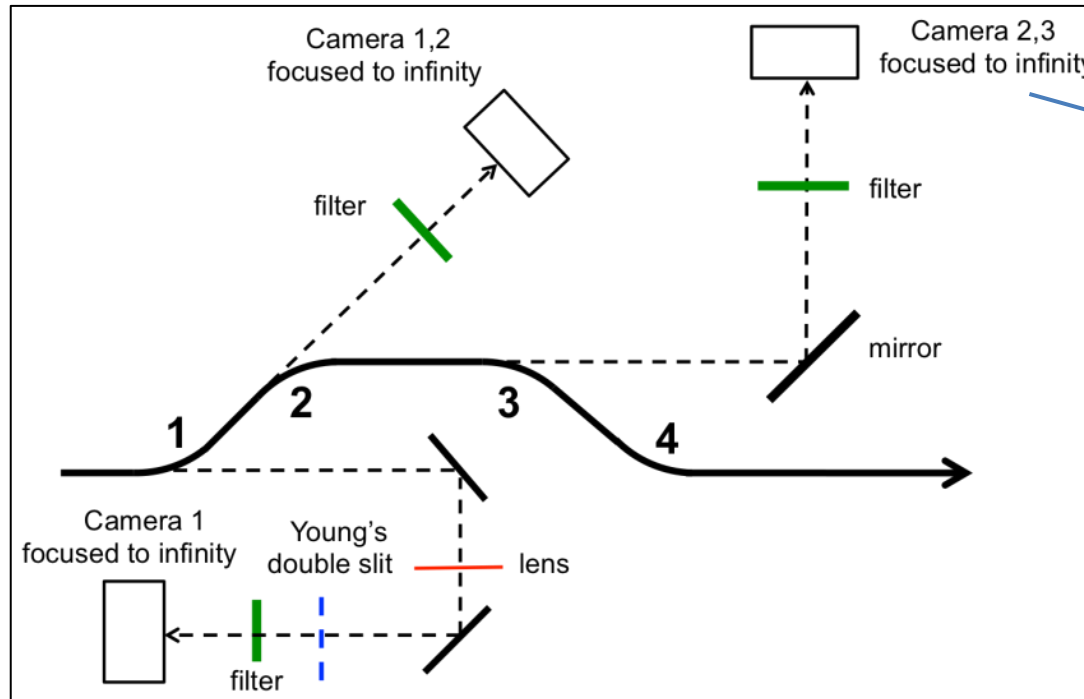
### OSR Interferences from (1,2) shows sensitivity to $dE/E$ (due to large angular dispersion)



### OSR Interferences from (2,3) shows sensitivity to divergence (and essentially no sensitivity to $dE/E$ )



# Optics to Observe Beam Size and Divergence using Optical Synchrotron Radiation Interferences



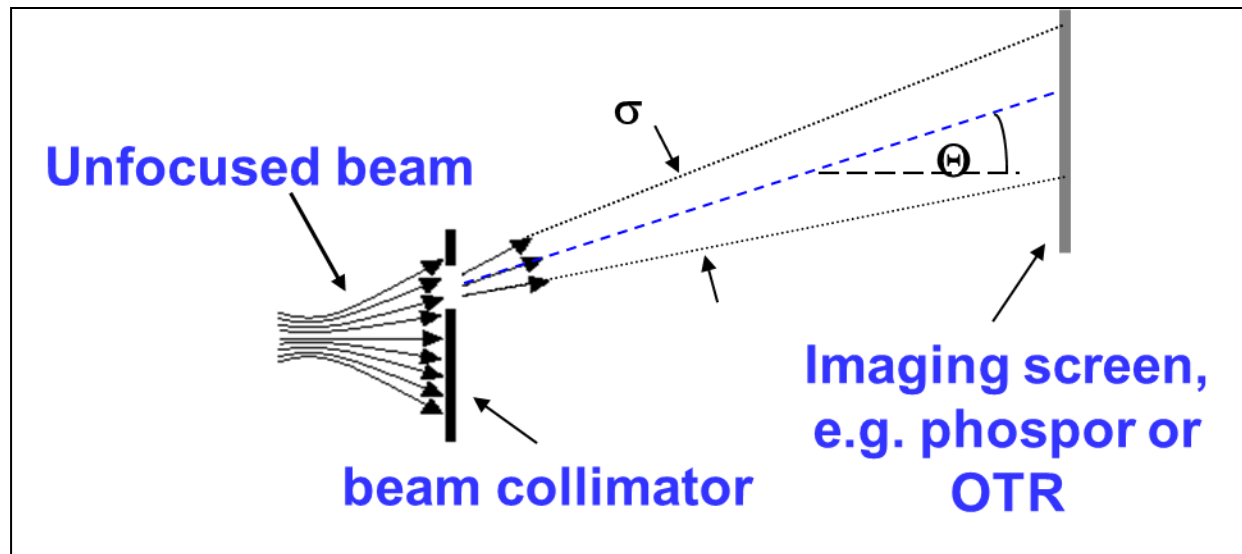
$\theta_y$

$\theta_x$

# Optical phase space mapping (OPSM)\* - the optical equivalent of the pepper pot technique

**Conventional PSM:** uses collimator (slits or pinholes) to segment the beam into beamlets, whose angular trajectories and angular spreads are measured as a function of position within the beam to make a PSM

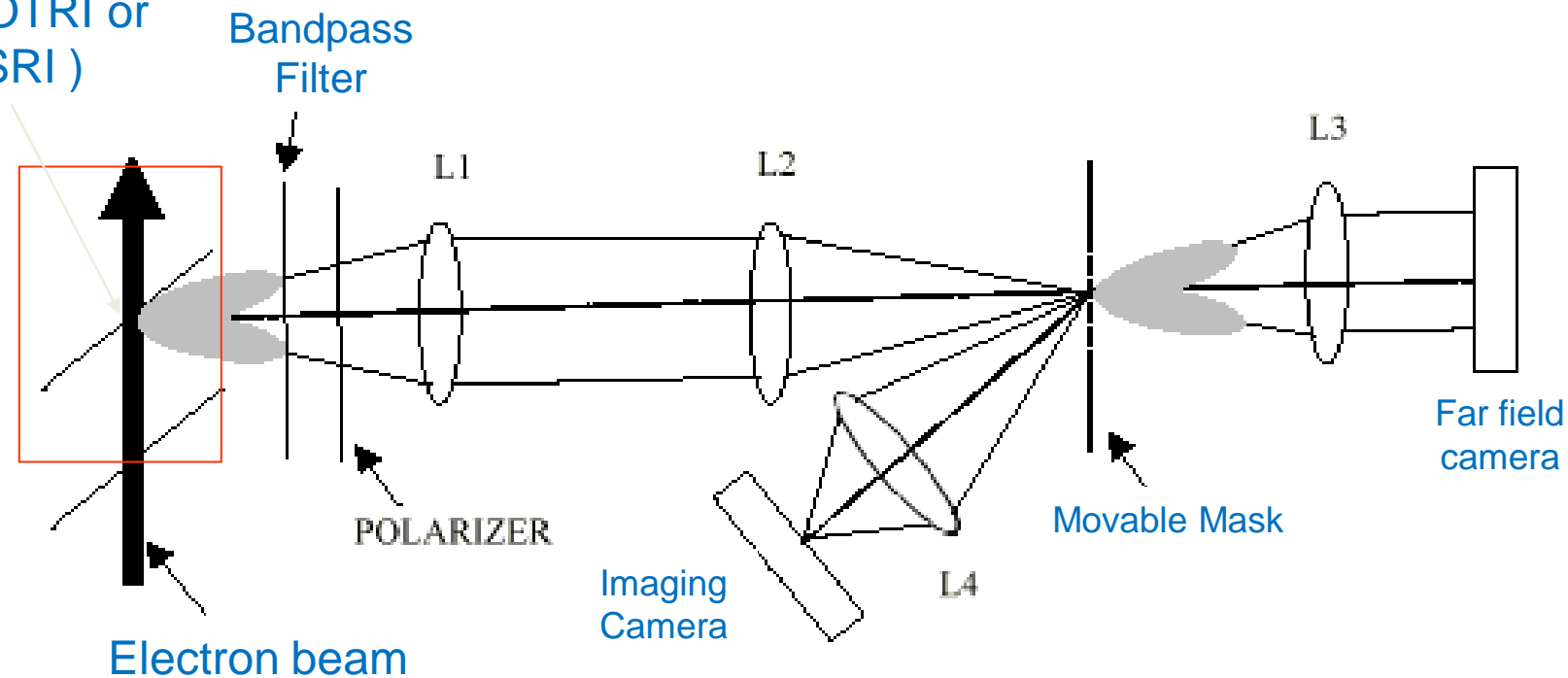
**Problems:** *Not practical for high energy beams - collimation doesn't work - beams too small; requires drift space and imaging screens in the beam line.*



\* R.B. Fiorito, A.G. Shkvarunets, and P.G. O'Shea, AIP Conf. Proc. No. 648, (2002).

**OPSM:** uses optical mask to segment beam associated radiation to measured beam divergence and trajectory angle measurements as a function of position within the beam image at one position in space \*

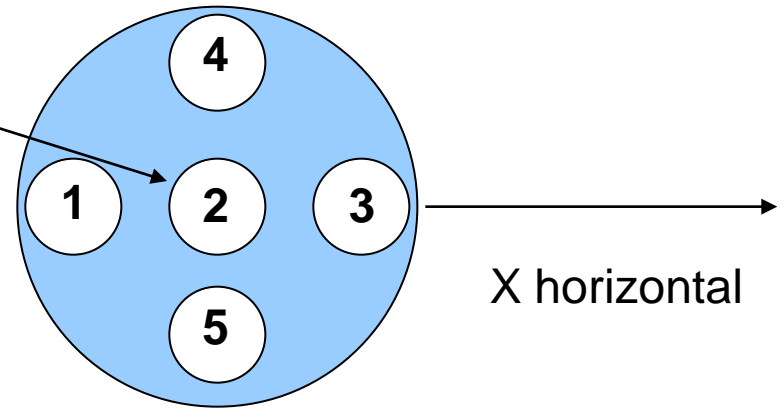
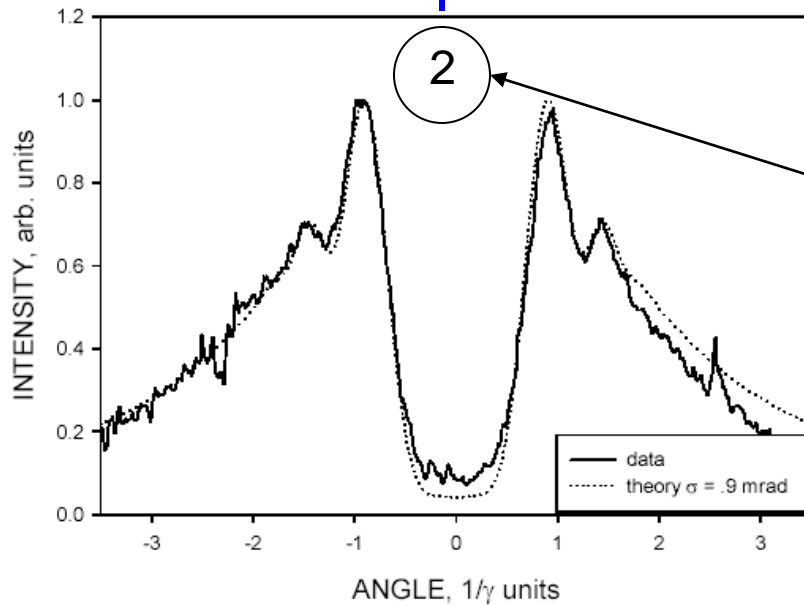
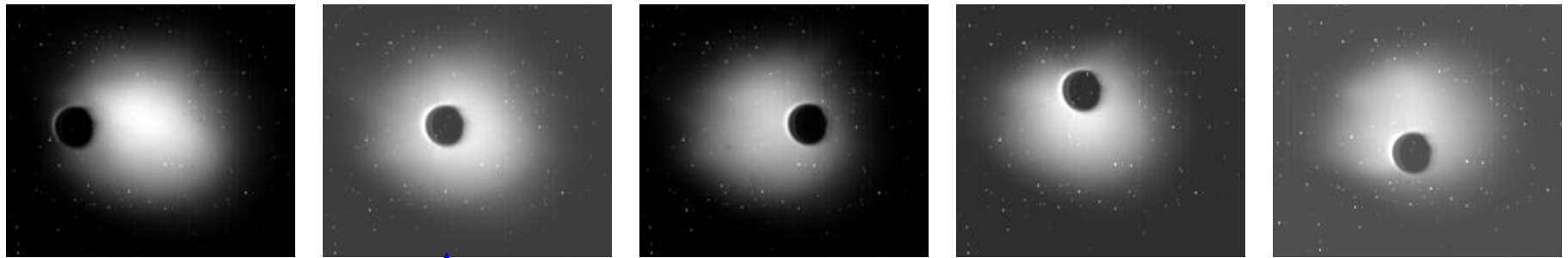
Optical Radiation  
(e.g. OTRI or OSRI)



- Applications:
- 1) separate out core and halo emittance
  - 2) create phase (trace) space map of beam

# Proof of principle experiment using OTR and a scanning pinhole mask

Done at 95 MeV linac at NPS- Monterrey CA\*



R. Fiorito, et. AIP Conf. Proc. 648, (2002)

The End: Thanks for your  
attention.