

# FCC electron cloud studies and its future plan

K. Ohmi (KEK), L. Mether (CERN)

Mar. 23-27, 2015

FCC week at Washington DC

Thanks to R. Cimino, R. Kersevan, G. Iadarola,  
G. Rumolo, D. Schulte

# Formula for Single bunch instability

- Strong head-tail instability caused by electron cloud
- Threshold of electron density

$$\rho_{e,th} = \frac{2\gamma\nu_s\omega_e\sigma_z/c}{\sqrt{3}KQr_0\beta L}$$

$$K = \omega_e\sigma_z/c$$

$$Q = \min(\omega_e\sigma_z/c, 7)$$

$$\omega_e = \sqrt{\frac{\lambda_p r_e c^2}{\sigma_y(\sigma_x + \sigma_y)}}$$

Electron frequency in the beam field

$$\Delta\nu_{xy} = \frac{r_p}{\gamma}\rho_e\beta_{xy}L$$

Tune shift of the beam

# Beam parameter and electron cloud instability (3.3TeV-50TeV)

		25 ns inj	25ns top	5ns inj	5ns top
beam energy	E (TeV)	3.3	50	3.3	50
bunch population	$N_p$ ( $10^{10}$ )	10	10	2	2
emittance	$\varepsilon_{xy}$ (nm)	0.625	0.0413	0.125	0.00826
typical beta	$\beta_{xy}$ (m)	200	200	200	200
bunch length	$\sigma_z$ (cm)	8	8	8	8
synchrotron tune	$\nu_s$	0.002	0.002	0.002	0.002
electron freq.	$\omega_e/2\pi$ (GHz)	3.56	13.9	3.58	13.9
electron osc.	$\omega_e \sigma_z/c$	5.97	23.3	6.00	23.3
threshold density	$\rho_{e,th}$ ( $m^{-3}$ )	$4.4 \times 10^{10}$	$5.72 \times 10^{11}$	$4.4 \times 10^{10}$	$5.73 \times 10^{11}$
tune shift at thres.	$\Delta\nu(\rho_{e,th})$	0.00039	0.00033	0.00039	0.00033

Electron frequency in a bunch  $\omega_e = \sqrt{\frac{\lambda_p r_e c^2}{\sigma_y(\sigma_x + \sigma_y)}}$   
 The electron density is averaged over ring

# Synchrotron radiation

- Number of photon per meter, proton

$$N_{\gamma} = \frac{5\alpha}{2\sqrt{3}} \frac{\gamma}{\rho_{Bend}}$$

$$\rho_{bend} = 11.3 \text{ km}$$

$$N_{\gamma} = 0.0023/\text{p.m} \text{ (3.3 TeV)}$$
$$= 0.035/\text{p.m} \text{ (50 TeV)}$$

- Critical energy

$$E_c = \frac{3\hbar c}{2} \frac{\gamma^3}{\rho_{Bend}}$$

$$= 1.1 \text{ eV (3.3 TeV)}$$

$$= 3.96 \text{ keV (50 TeV)}$$

- Radiation power

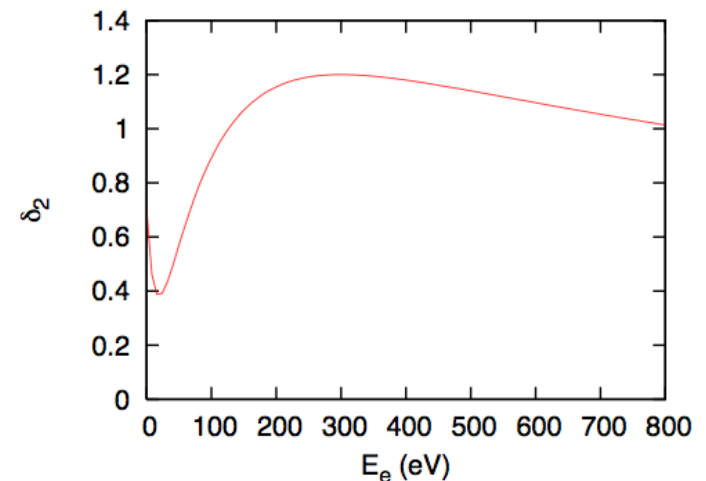
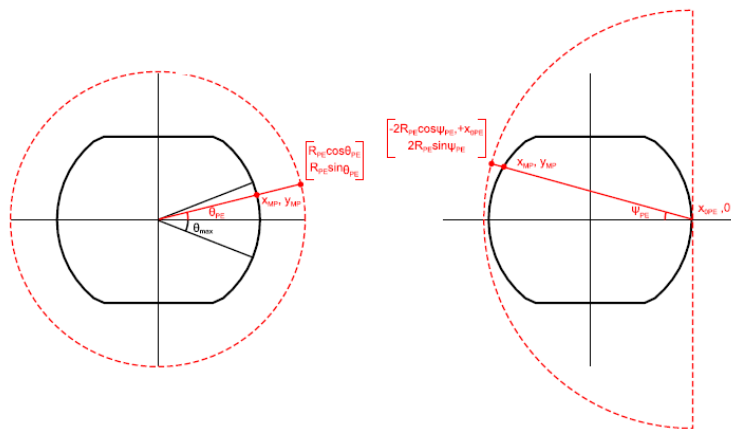
$$P_{SR} = N_p N_{\gamma} \frac{8E_c}{15\sqrt{3}} \frac{N_{bunch} f_0}{C}$$

$$= 0.1 \text{ mW/m (3.3 TeV)}$$

$$= 27.6 \text{ W/m (50 TeV)}$$

# Electron cloud build-up

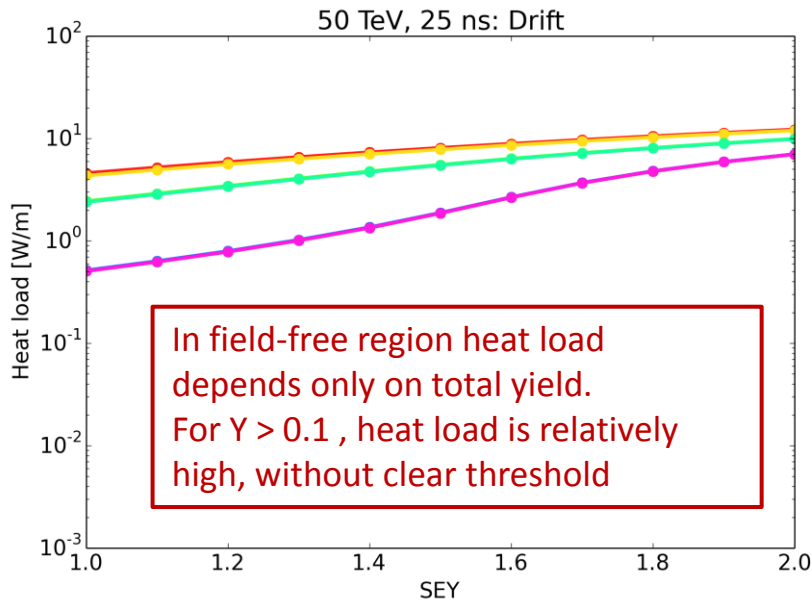
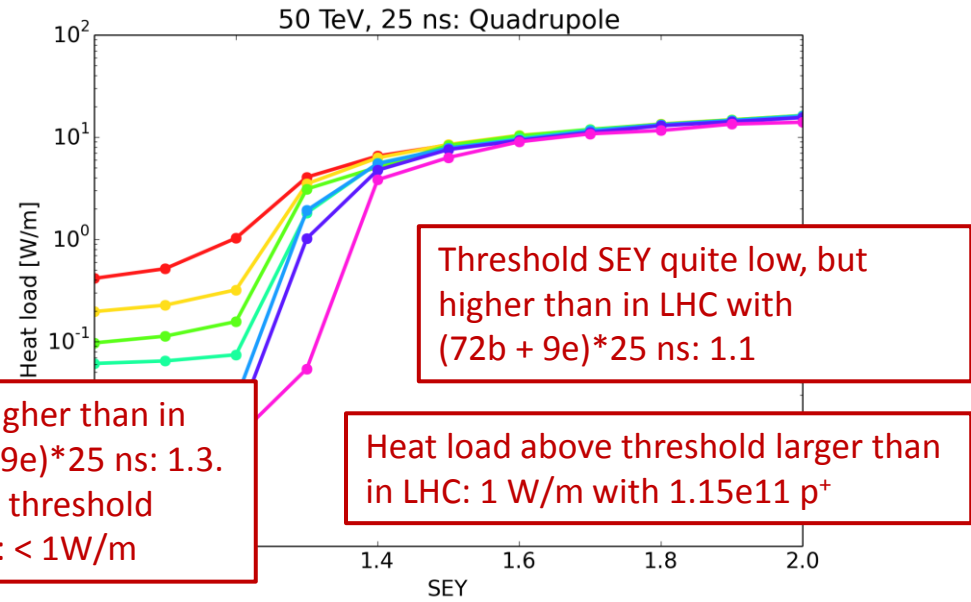
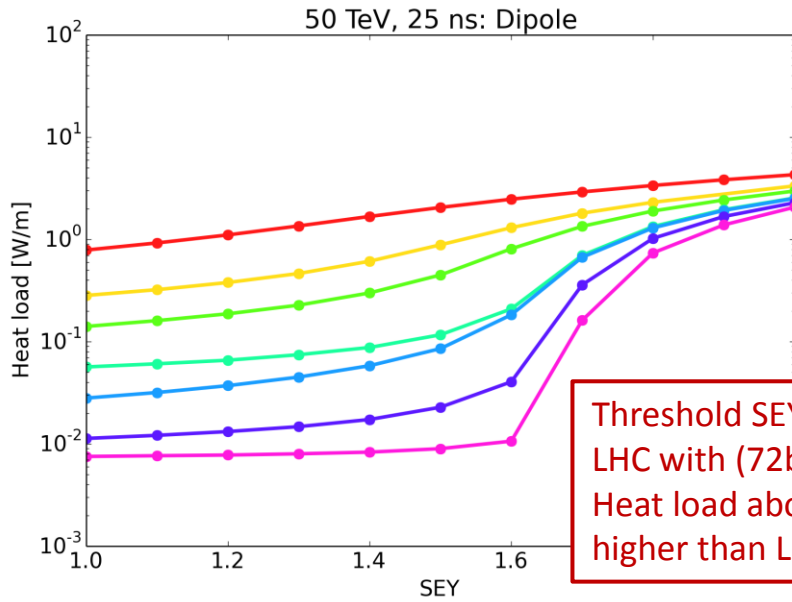
- Photoelectron
  - direct photon  $N_\gamma Y$  produced at illuminated position.
  - reflected photon  $N_\gamma Y R$  distribute  $\cos^2\theta$ .
- Secondary electron
  - production rate/electron  $\delta_2(E)$
  - characterized by  $E_{2,\max}$  and  $\delta_{2,\max}$



# Electron production

- $Y=0.2-0.3$  for smooth copper,  $0.02-0.05$  for saw-tooth copper.
- Electrons  $N_e = N_p N_\gamma Y = 10^9 - 10^8 \text{ m}^{-1}$  are produced by a bunch. The chamber cross section is  $10 \text{ cm}^2$ .
- Average density produced by a bunch,  $10^{11} - 10^{10} \text{ m}^{-3}$ , is already closed to the threshold.
- Most of electrons produced at illuminated position are protected by strong magnetic field of  $B$  and  $Q$ .
- Cure for Reflected photon and secondary emission are important.

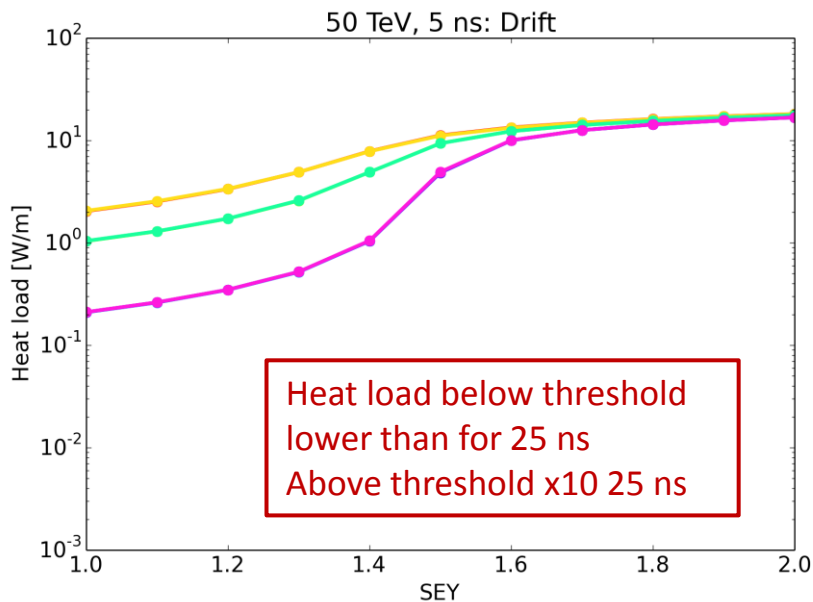
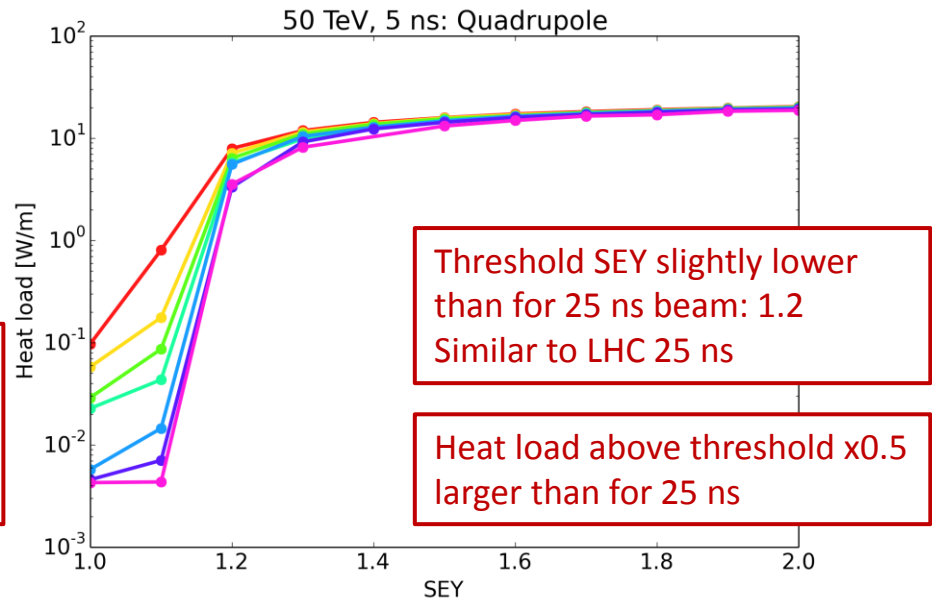
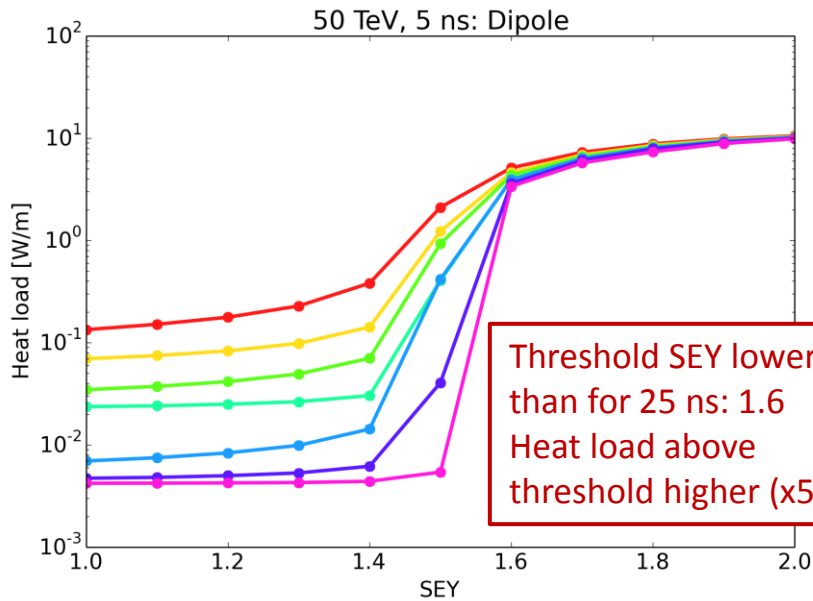
# Heat loads for 50 TeV, 25 ns beam in



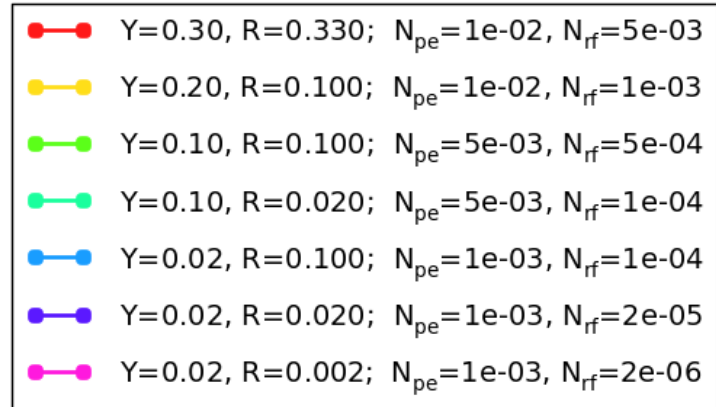
$$P_{SR} = 27.6 W/m$$

- Y=0.30, R=0.330;  $N_{pe}=1e-02$ ,  $N_{rf}=5e-03$
- Y=0.20, R=0.100;  $N_{pe}=1e-02$ ,  $N_{rf}=1e-03$
- Y=0.10, R=0.100;  $N_{pe}=5e-03$ ,  $N_{rf}=5e-04$
- Y=0.10, R=0.020;  $N_{pe}=5e-03$ ,  $N_{rf}=1e-04$
- Y=0.02, R=0.100;  $N_{pe}=1e-03$ ,  $N_{rf}=1e-04$
- Y=0.02, R=0.020;  $N_{pe}=1e-03$ ,  $N_{rf}=2e-05$
- Y=0.02, R=0.002;  $N_{pe}=1e-03$ ,  $N_{rf}=2e-06$

# Heat loads for 50 TeV, 5 ns beam in arc



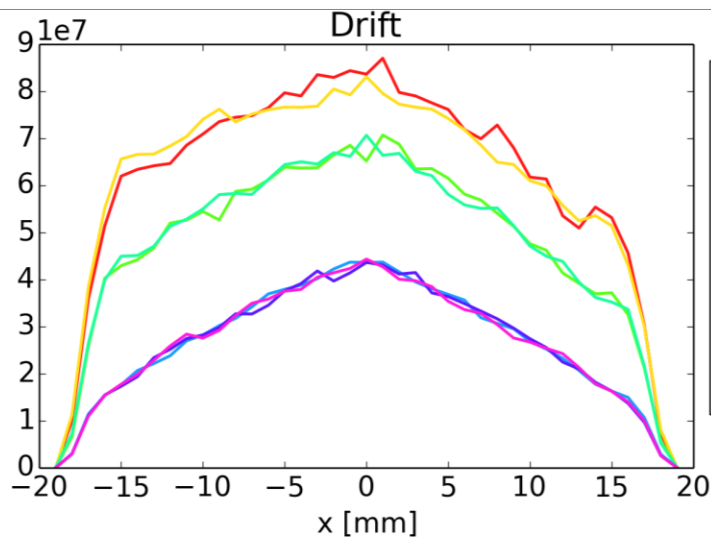
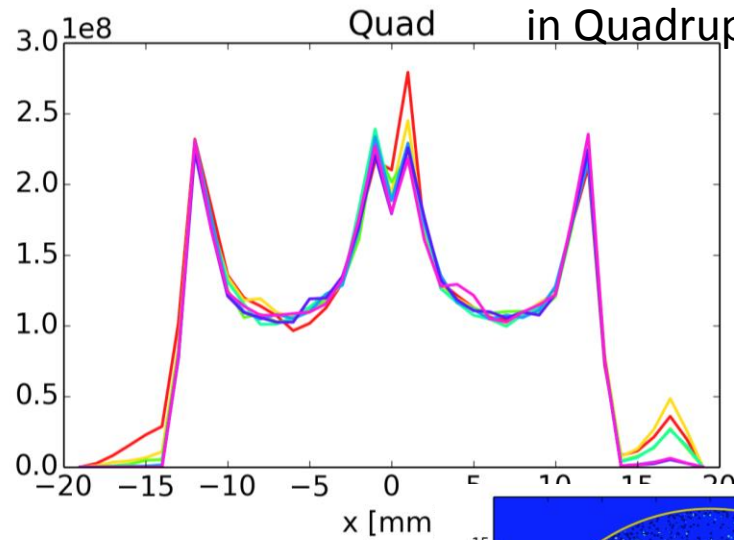
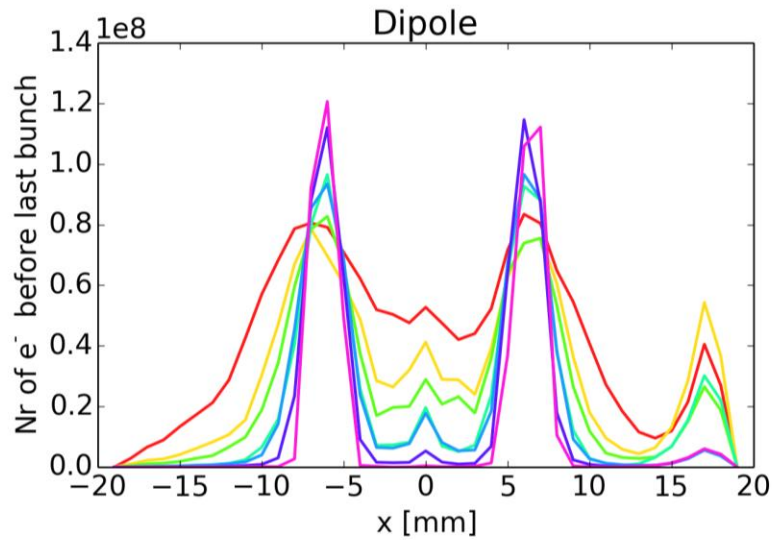
$$P_{SR} = 27.6 W/m$$



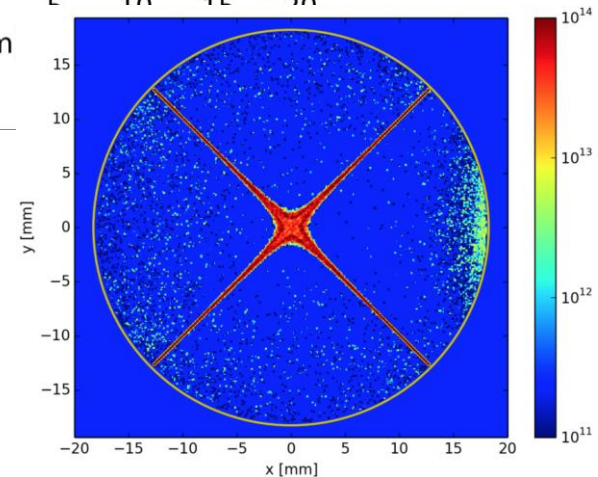


# x-distribution of electrons in chamber

Most electrons in centre  
in Quadrupole



- $Y = 0.30, R = 0.330$
- $Y = 0.20, R = 0.100$
- $Y = 0.10, R = 0.100$
- $Y = 0.10, R = 0.020$
- $Y = 0.02, R = 0.100$
- $Y = 0.02, R = 0.020$
- $Y = 0.02, R = 0.002$

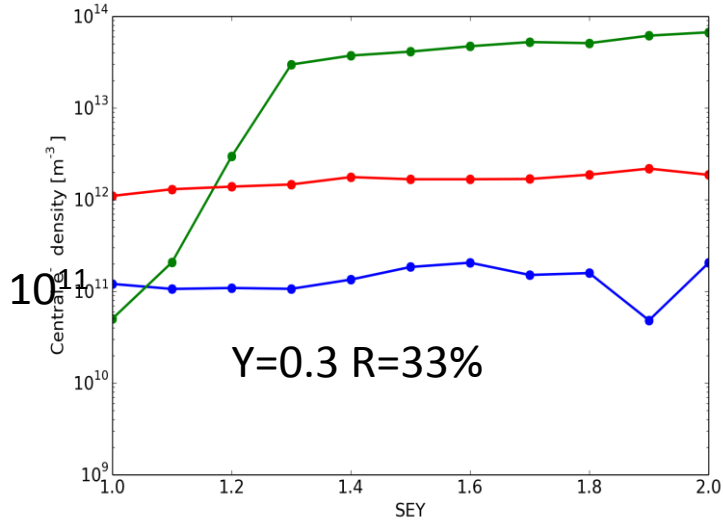


Electrons localize in  
Quad extremely.

# Electron density in centre of chamber

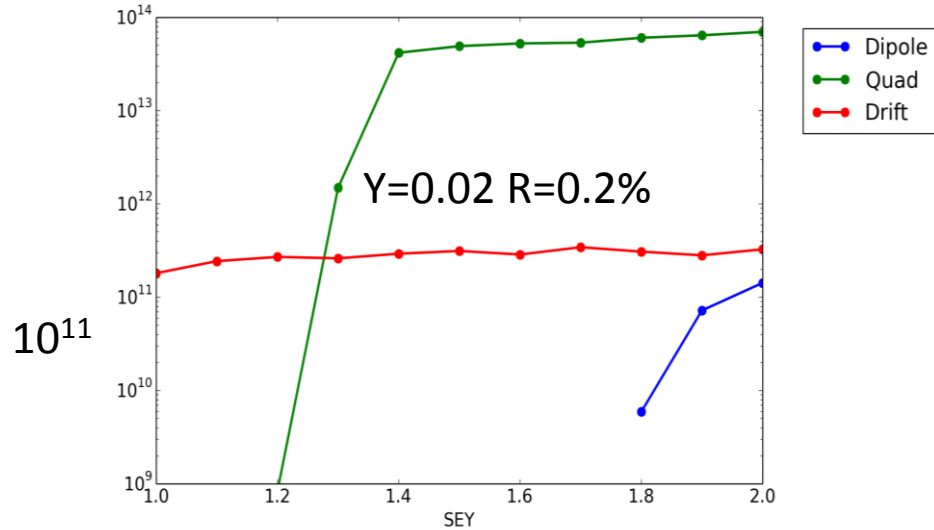
## Highest Yield and Reflectivity

$Y = 0.30, R = 33.0; N_{pe}=1.5e-02, N_{rf}=5.0e-03$



## Lowest Yield and Reflectivity

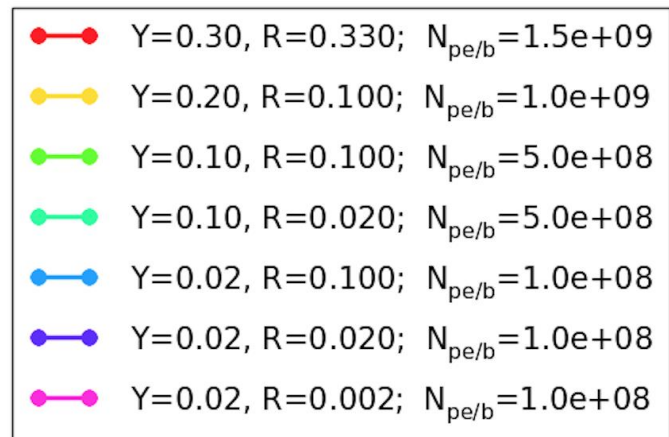
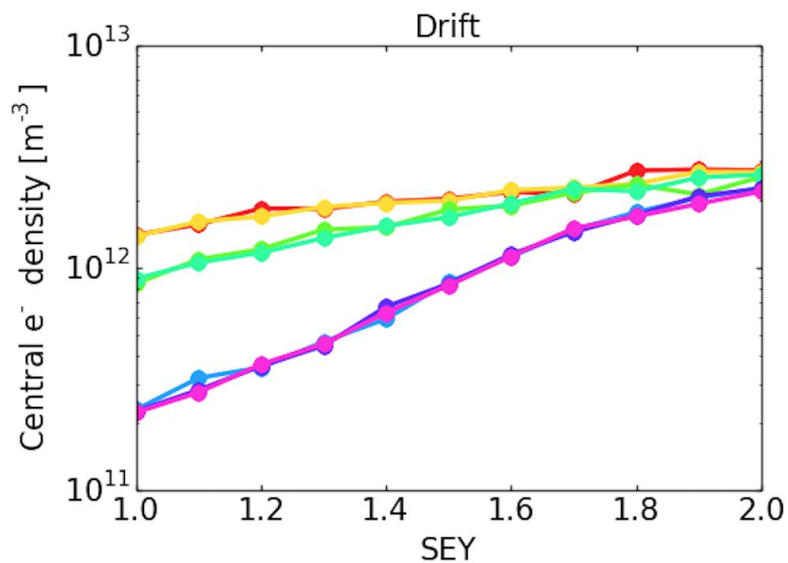
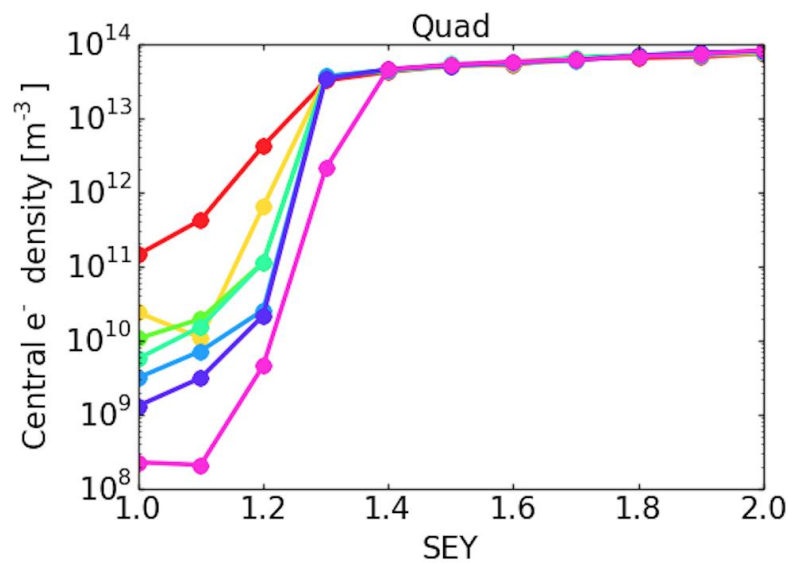
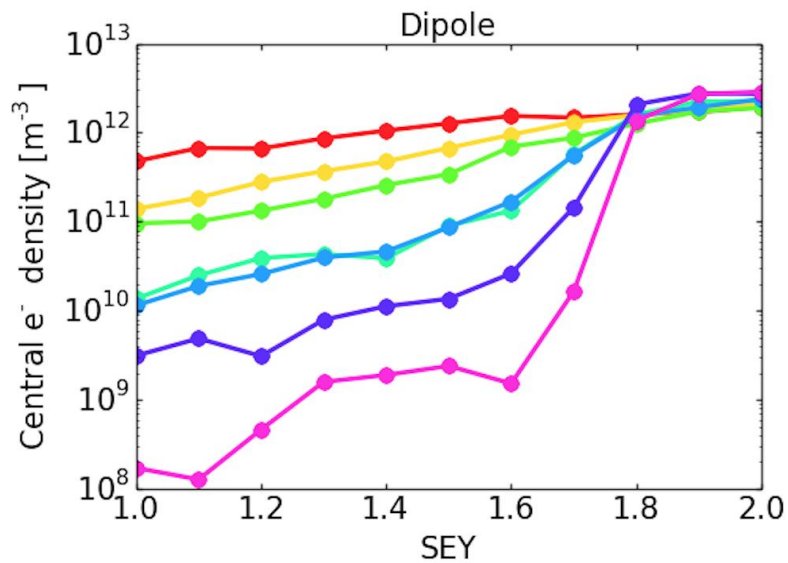
$Y = 0.02, R = 0.2; N_{pe}=1.0e-03, N_{rf}=2.0e-06$



- For  $Y \times R < 0.1 \times 2\%$ ,  $SEY < 1.6$ , the density in bend is lower than the threshold.
- Central density in quadrupole 2-3 orders of magnitude higher than in dipole..
- The integrated density in quad dominates compare than bend.
- $10^{14}$  at quad is serious. SEY should be less than 1.2

FODO cell: 208.14 m, Dipole 170.40 m,  
 Quad: 10.34 m, Drift: 26.40 m

# Central Density

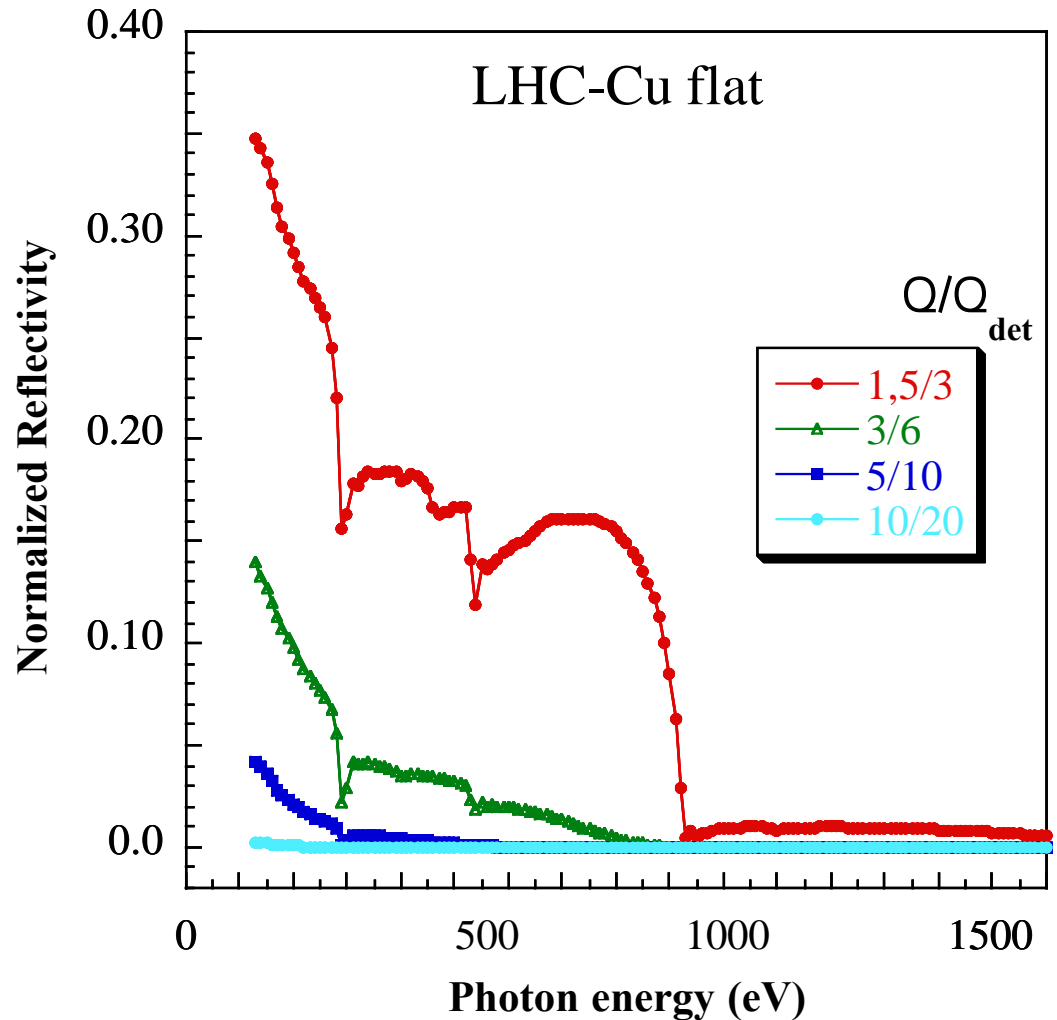


# Measurement of R

Courtesy of R. Cimino

R has been measured!

Reflectivity of LHC- Cu sample representative of the flat part of the beam screen, as function of photon energy for various incidence angles  $\theta$  and emission angle  $2\theta$ .

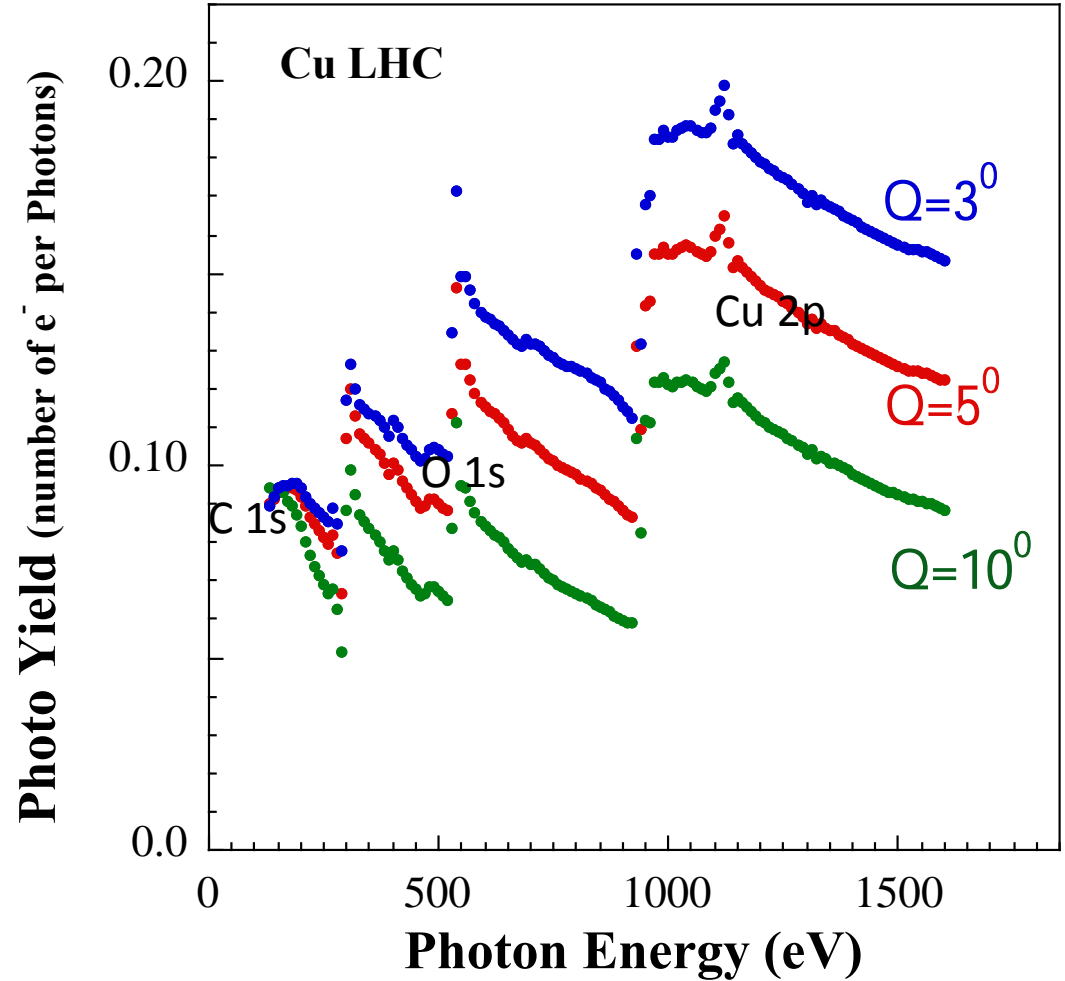


# Measurement of $\gamma$

Courtesy of R. Cimino

PY can be and has been measured!

Photo yield (number of electrons emitted per incident photon) from a Cu Technical surface of LHC beam screen, as function of photon energy at different incidence angles.



# SR screen design study

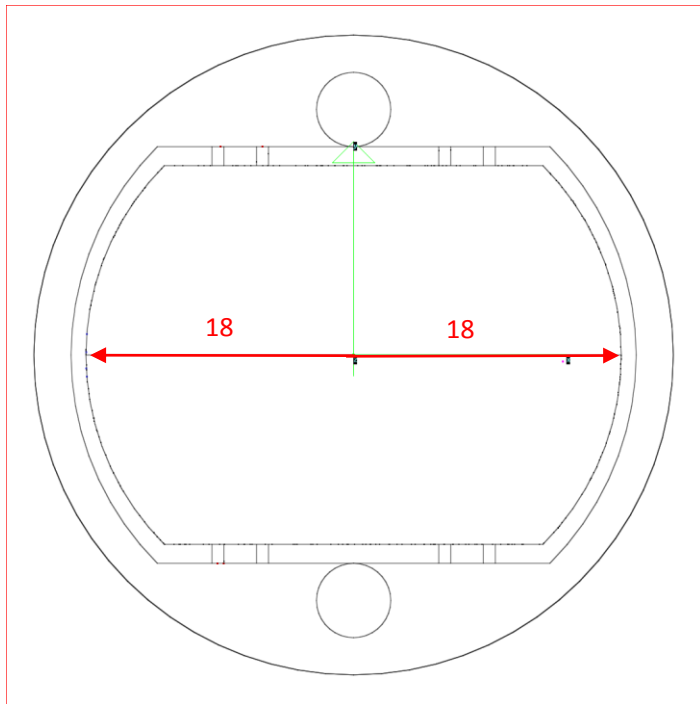
Courtesy of R. Kersevan



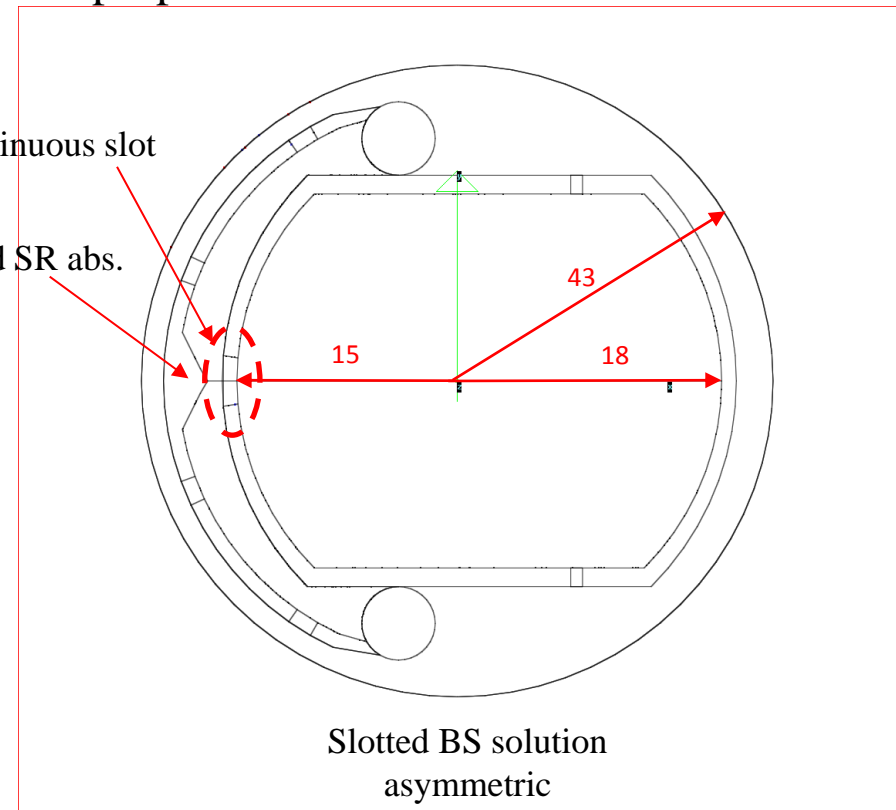
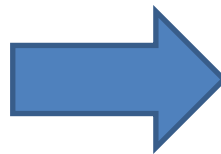
## FCC:

### Configuration:

A combined BS, made up of a LHC-like BS with a continuous slot and an “external” SR power absorber is proposed here.



LHC-like BS solution



Slotted BS solution  
asymmetric

Courtesy of R. Kersevan

# SR ray trace

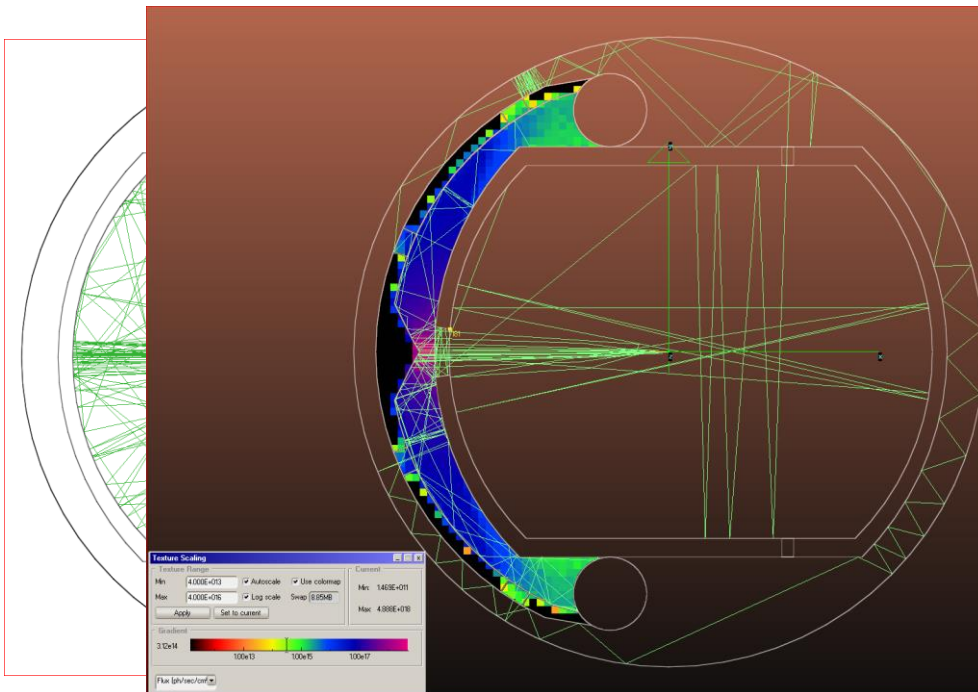
Courtesy of R. Kersevan



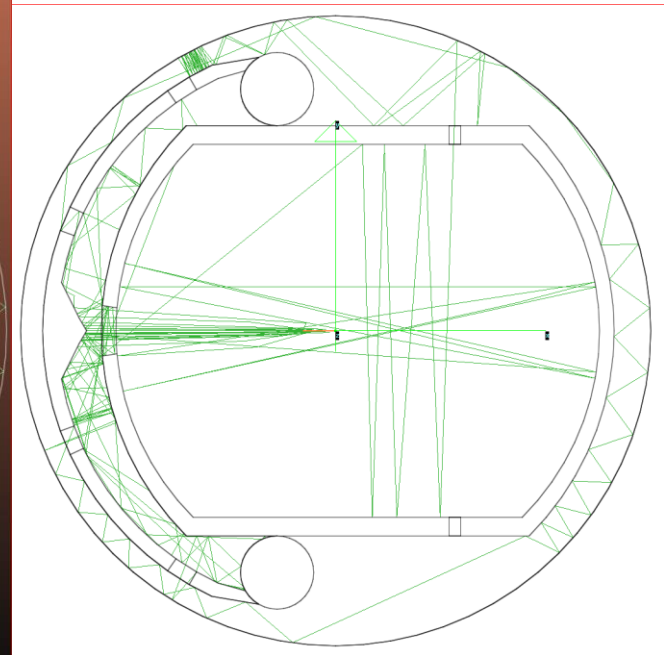
## FCC:

## SR Ray-Tracing (Synrad+):

The high-energy small vertical angle opening of the primary SR fan passes almost unscathed inside of the 2x 1.57 mm-high continuous slot



All SR-induced gas load may interact with the beam



Only a fraction of the SR-induced gas load may interact with the beam

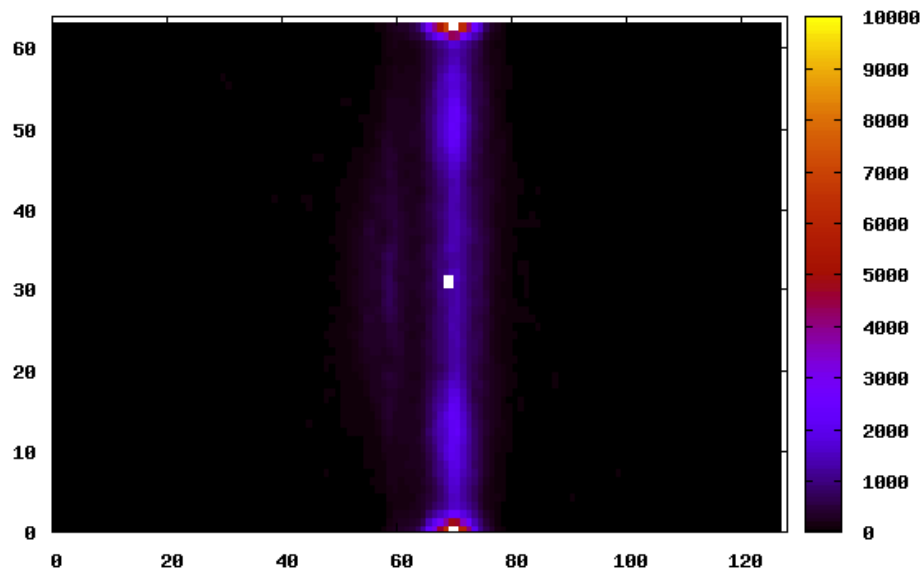
# Other beam phenomena due to electron cloud

- Coupled bunch instability
- Incoherent Emittance growth



# Coupled bunch instability

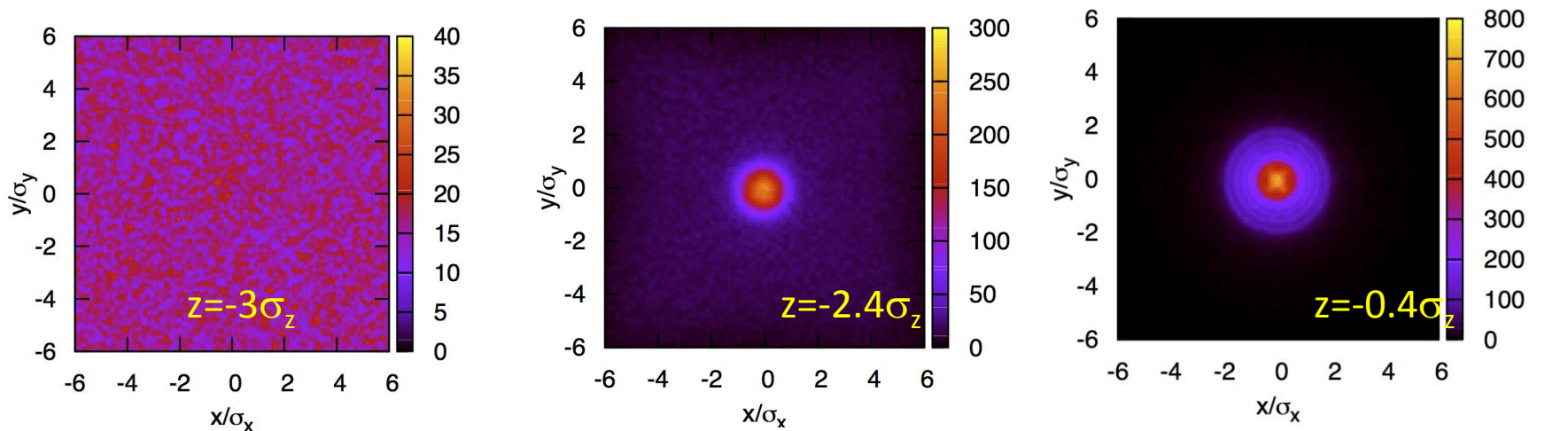
- Corrective motion between beam and electron cloud.
- Instability due to electron cloud in bending magnet in **DAFNE** (rectangular chamber).



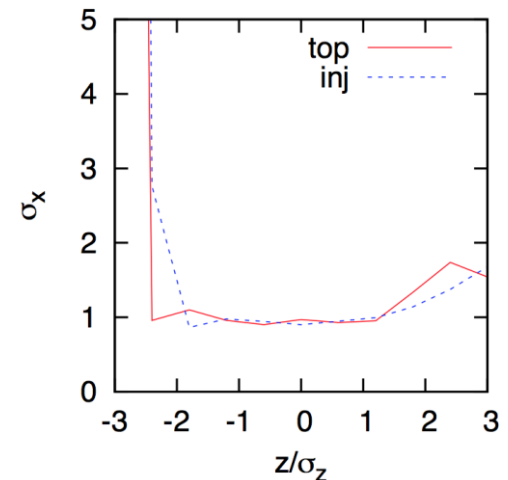
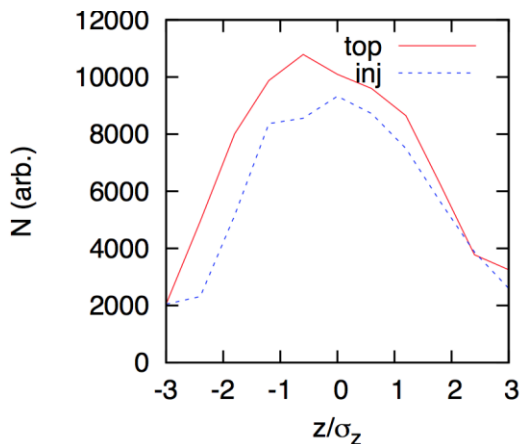
White : beam center  
Violet: electron cloud

# Electron density during interaction with beam

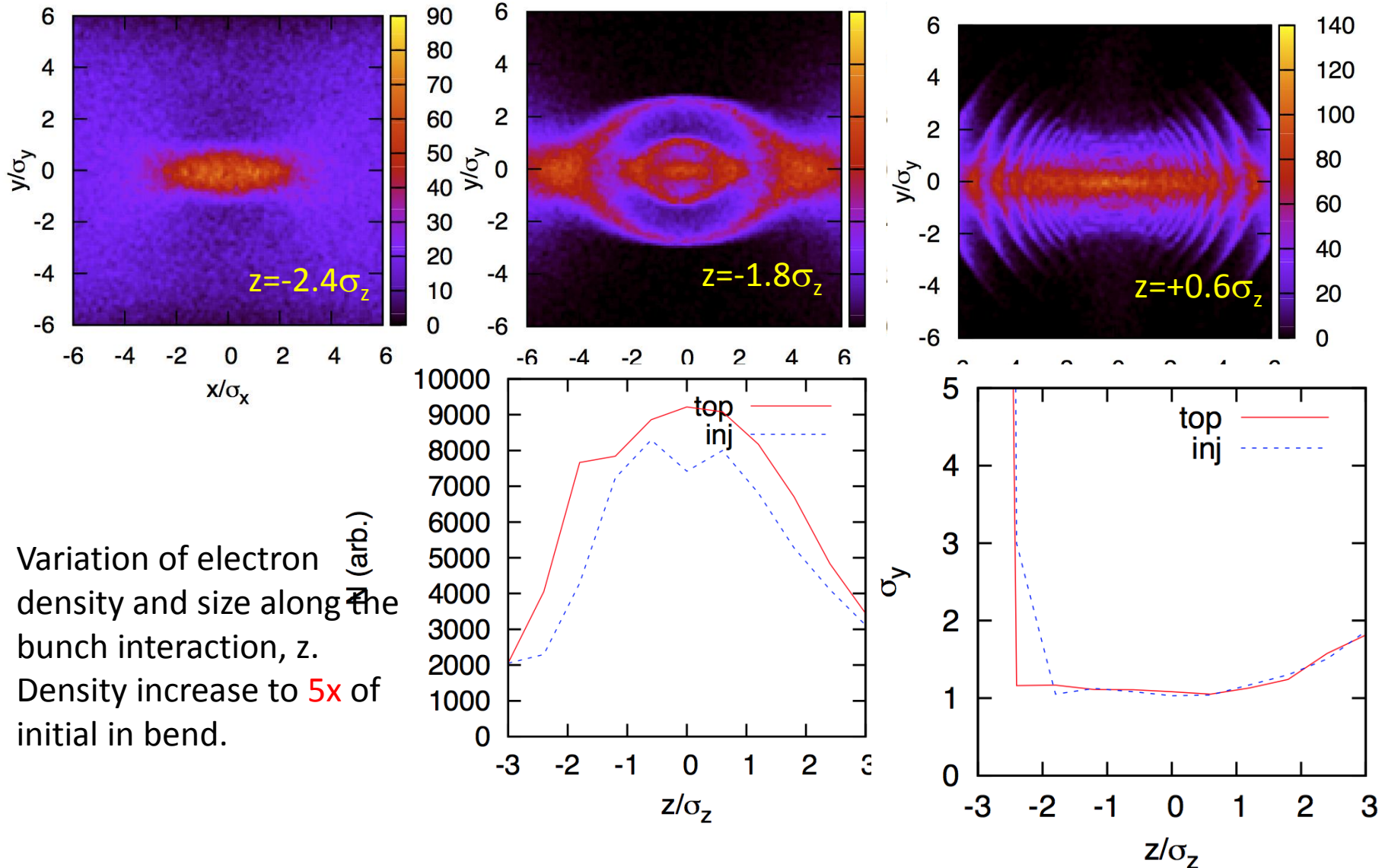
- Transverse electron profile along  $z$ . (drift space)
- Electron initial energy  $v_0=10^6$  m/s (3eV) is assumed.



- Variation of electron density and size along the bunch interaction,  $z$ .
- Density increase to **25x** of initial.
- **The increase is the same in Quad.**



- In strong Bending magnet



- Variation of electron density and size along the bunch interaction,  $z$ .
- Density increase to **5x** of initial in bend.

# Emittance growth caused by electron cloud

- Electron cloud potential induces tune spread and resonances.

$$\Delta\nu_{xy} = \frac{r_p}{\gamma} \rho_e \beta_{xy} L$$

- The strength of the resonances are characterized by the width in amplitude space,  $\Delta J$ .
- Modulation of the resonances due to synchrotron motion etc. results in emittance growth.

# Electron cloud induced tune spread and resonance term

- $U(x,y)$ : integrated effective potential due to electron cloud
- Resonance driving term is Fourier component of  $U$ .

$$U(x, p_x, y, p_y, s) = \oint e^{iH_0 s} U(x, y, s') e^{-iH_0 s} ds'$$

$H_0$ : lattice transformation of  $s'$  to  $s$

$$U(J_x, \phi_x, J_y, \phi_y) = \sum_{m_x, m_y} U_{m_x, m_y} \cos(m_x \phi_x + m_y \phi_y)$$

$$U_{m_x, m_y}(J_x, J_y) = \frac{\lambda_p r_p}{\beta^2 \gamma^3} \oint ds \int_0^\infty \frac{du}{\sqrt{2\sigma_x^2 + u} \sqrt{2\sigma_y^2 + u}} \quad \text{Tune spread is given by } U_{00}.$$

$$\left[ \delta_{m_x 0} \delta_{m_y 0} - \exp(w_x - w_y) (-1)^{(m_x + m_y)/2} I_{m_x/2}(w_x) I_{m_y/2}(w_y) e^{-im_x \phi_x - im_y \phi_y} \right].$$

$$w_x = \frac{\beta_x J_x}{2\sigma_x^2 + u}$$

# Summary

- The threshold of single bunch instability is  $\rho_e = 5 \times 10^{10}(\text{inj}) - 5 \times 10^{11} \text{ m}^{-3}(\text{top})$ .
- For  $Y \times R < 0.1 \times 2\%$ , the density in **Bend** is lower than  $\rho_e$ .  $SEY < 1.2$  is required for the threshold in **Quad**.
- The numbers should be refined by detailed studies.
  - Measurement of Y,R,SEY
  - Beam screen design
  - Cross check of electron buildup codes, PyECLOUD and PEI.

# Beam dynamics studies

- Evaluate coupled bunch instability growth rate. Requirement for feedback damper.
- Evaluate unstable Modes in quadrupole to check which magnet is dominant for electron cloud.
- Tune shift is very small,  $\Delta\nu=0.0003$ , even at the threshold of coherent instability.
- The tune shift can be x25 (in quad) higher due to pinching,  $\Delta\nu=+0.008$ . Not very large.
- IR Q located at high beta will be studied.
- Evaluate Resonance width and simulation using resonance model to study emittance growth.





# Tune shift and slope due to Gaussian electron cloud

- Tune shift

$$2\pi\Delta\nu_x = -\frac{\lambda_p r_p}{\beta^2 \gamma^3} \oint ds \frac{\beta_x}{\sigma_x^2} \int_0^\infty \frac{d\eta}{(2+\eta)^{3/2} (2r_{yx} + \eta)^{1/2}} \left[ e^{-w_x - w_y} (I_0(w_x) - I_1(w_x)) I_0(w_y) \right]$$

$$2\pi\Delta\nu_y = -\frac{\lambda_p r_p}{\beta^2 \gamma^3} \oint ds \frac{\beta_x}{\sigma_x^2} \int_0^\infty \frac{d\eta}{(2+\eta)^{1/2} (2r_{yx} + \eta)^{3/2}} \left[ e^{-w_x - w_y} I_0(w_x) (I_0(w_y) - I_1(w_y)) \right]$$

- Tune slope

$$\begin{aligned} \frac{\partial^2 U_{00}}{\partial J_x^2} &= -2\pi \frac{\partial \nu_x}{\partial J_x} \\ &= \frac{\lambda_p r_p}{\beta^2 \gamma^3} \oint ds \frac{\beta_x^2}{\sigma_x^4} \int_0^\infty \frac{d\eta}{(2+\eta)^{5/2} (2r_{yx} + \eta)^{1/2}} \left[ e^{-w_x - w_y} \left\{ \frac{3}{2} I_0(w_x) - 2I_1(w_x) + \frac{1}{2} I_2(w_x) \right\} I_0(w_y) \right] \end{aligned}$$

$$r_{yx} = \sigma_y^2 / \sigma_x^2$$

$$w_x = \frac{\beta_x J_x / \sigma_x^2}{2 + \eta}$$

$$w_y = \frac{\beta_y J_y / \sigma_y^2}{2 + \eta / r_{yx}}$$