

$E + \Delta E$

$E - \Delta E$

Monochromatization for Higgs production

e^-

e^+

A. Faus-Golfe

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IFIC - LAL

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Outline

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 - Energy Resolution and Monochromatization
 - Monochromatization factor
 - Standard scheme
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Objectives

- The aim is to monochromatize the FCC-ee beams at $E_{\text{CM}} = 125.2$ GeV for the production of $e^+e^- \rightarrow H(125.2)$ in the s-channel, just like a muon collider, but with hopefully much higher luminosity -- and lower cross-section. The Higgs width is 4.2 MeV and the FCC-ee energy spread is about 5×10^{-4} at these energies, so one needs to gain a factor 10 in energy spread. We also need to keep the beams polarized to keep track of the beam energy precisely.
- From previous study we could conclude that there is no fundamental reason against monochomatization, but given the FCC-ee optics configuration (IP dispersion can be generated independently for the two beams since there are two separate e^+ / e^- channels) horizontal dispersion at the IP (opposite sign) is the more natural option. Based on this option and the related trade-off between horizontal focusing and horizontal dispersion, we have studied the impact on luminosity and the options to avoid losses.

Monochromatization principle Energy resolution and Monochromatization

Energy Resolution: $S_w = \sqrt{2E_0} S_e$

energy spread

$$\sigma_\varepsilon^2 = \frac{55\hbar c E_0^2}{32\sqrt{3}(mc^2)^3} \frac{I_3}{I_2} \frac{1}{J_\varepsilon}$$

↓

$$S_w \propto \frac{1}{\sqrt{rJ_e}}$$

To increase S_w

- $r \gg \gg$ bending radius
- $0.5 \leq J_e = 3 - J_x \leq 2.5$ longitudinal partition number

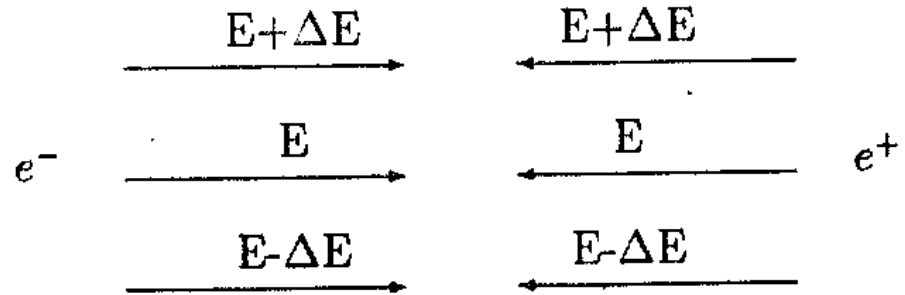
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Monochromatization [7]

Monochromatization principle Energy resolution and Monochromatization

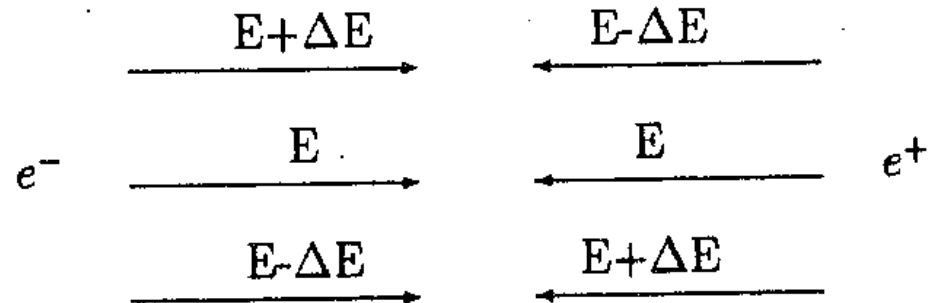
Standard collision:
dispersion has the same sign
in the IP

$$w = 2(E_0 + e)$$



Monochromatization:
dispersion has opposite sign in
the IP

$$w = 2E_0 + 0(e)^2$$



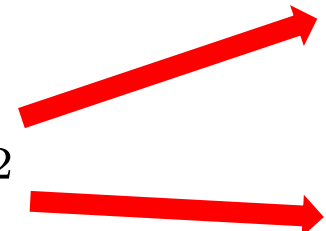
Enhancement of **energy resolution**, and sometimes increase of the relative frequency of the events at the centre of of the distribution.

Monochromatization principle Monochomatization factor

1) Case with: $D_{x,y}^* = 0$ $L_0 = \frac{k_b f_r N_+ N_-}{4\pi \sigma_{x\beta}^* \sigma_{y\beta}^*}$

2) Case with: $D_{x+}^* = -D_{x-}^* = D_x^*$
 $D_{y+}^* = -D_{y-}^* = D_y^*$

Monochromatization factor

$$\lambda = \left(1 + \sigma_\varepsilon^2 \left(\frac{D_x^{*2}}{\sigma_{x\beta}^{*2}} + \frac{D_y^{*2}}{\sigma_{y\beta}^{*2}}\right)\right)^{1/2}$$


$$L = \frac{L_0}{\lambda}$$

$$\Sigma_w = \frac{\sqrt{2} E_0 \sigma_\varepsilon}{\lambda}$$

- Opposite dispersions at the IP enhance energy resolution without detriment of the differential luminosity while dispersion which have the same sign degrade both differential and total luminosity
- When $\sigma_y^* \ll \sigma_x^*$ is more efficient to produce dispersion in the vertical plane trying to keep it zero horizontally

Monochromatization principle “Standard” Scheme

$$\sigma_y^* \ll \ll \sigma_x^* \quad \longrightarrow \quad \begin{aligned} D_{x+}^* &= D_{x-}^* = 0 \\ D_{y+}^* &= -D_{y-}^* = D_y^* \end{aligned}$$

Implementations historical Studies:

- VEPP4: one ring, electrostatic quads [3] [12]
- SPEAR: one ring, electrostatic quads, $\lambda \sim 8$ [9]
- LEP: one ring, electrostatic quads (limited strength) and alternative RF magnetic quads, $\lambda \sim 3$ (optics limitations) [2] [10]
- Superconducting RF resonators [33]
- Tau-Charm factory: two rings, vertical dipoles, , $\lambda \sim 7.5$ [3] [4] [6] [8] [11] [13] [32]

Never tested experimentally !!!!!

Higgs factory:

$$E_0 = 120 \text{ GeV}$$

$$N_b = 0.46 \cdot 10^{11}$$

$$I = 30 \text{ mA}$$

$$\epsilon_x = 0.94 \text{ nm}$$

$$\epsilon_y = 1.9 \text{ pm}$$

$$\beta_x^* = 0.5 \text{ m}$$

$$\beta_y^* = 1.0 \text{ mm}$$

$$\sigma_x^* = 22 \text{ } \mu\text{m}$$

$$\sigma_y^* = 0.044 \text{ } \mu\text{m}$$

$$\sigma_\epsilon = 0.001$$

$$\sigma_b = 1.17 \text{ mm}$$

$$L_0 = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

choosing

$$D_x^* = 0.1 \text{ m}$$

$$D_y^* = 0.0$$



Monochromatization factor

$$\lambda = \left(1 + \sigma_\epsilon^2 \frac{D_x^{*2}}{\sigma_{x\beta}^{*2}}\right)^{1/2} = 4.65$$

Luminosity

$$L = \frac{L_0}{\lambda} = 1.29 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

Standard deviation of w

$$\Sigma_w = \frac{\sqrt{2} E_0 \sigma_\epsilon}{\lambda} = \frac{0.17}{4.65} = 0.036 \text{ GeV}$$

Monochromatization principle “Optimized” Scheme

Optimizing the beam parameters we could **gain** in **energy resolution** keeping the **luminosity** constant and the beam-beam in the standard limits !!!!!

Rewriting some formulas:

$$\sigma_y^* \ll \sigma_x^* \quad \longrightarrow \quad \begin{matrix} D_{y+}^* = D_{y-}^* = 0 \\ D_{x+}^* = -D_{x-}^* = D_x^* \end{matrix} \quad \frac{\sigma_\varepsilon^2 D_x^{*2}}{\sigma_{x\beta}^{*2}} \gg 1$$

$$\Sigma_w \simeq \sqrt{2} E_0 \sqrt{\frac{\epsilon_x}{H_x^*}} \quad \text{with} \quad H_x^* = \frac{D_x^{*2}}{\beta_x^*} \quad \text{horizontal invariant dispersion}$$

$$\xi_{xy} = \frac{N_b r_e \beta_{xy}^*}{2\pi \gamma \sigma_{xy}^* (\sigma_x^* + \sigma_y^*)} \quad \longrightarrow \quad L = \frac{I \gamma}{2e r_e} \left(\frac{\xi_x}{\beta_x^*} + \frac{\xi_y}{\beta_y^*} \right)$$

$$\xi_x \ll \xi_y \simeq \xi_{max}$$

$$\text{with } \sigma_x^* \simeq \sigma_\varepsilon D_x^* \quad \longrightarrow \quad \frac{\xi_y}{\beta_y^*} \quad \text{dominant term}$$

Monochromatization principle “Optimized” Scheme

The new condition for an **optimized scheme** with:

$$\beta_y^* \ll \beta_x^* \quad \sigma_y^* \ll \sigma_x^* \quad \xi_x < \xi_y$$

$$L \simeq \frac{I\gamma}{2er_e} \frac{\xi_y}{\beta_y^*} \quad \frac{2\pi\gamma}{N_b r_e} \epsilon_y \xi_y \frac{\beta_x^*}{\beta_y^*} \leq 1$$

The beam-beam parameter could be maximized in the plane where dispersion is zero, keeping lower value in the plane where dispersion is different from zero

Higgs factory:

$$E_0 = 120 \text{ GeV}$$

$$\sigma_\varepsilon = 0.001$$

$$\sigma_b = 1.17 \text{ mm}$$

choosing

$$D_x^* = 0.1 \text{ m}$$

$$\beta_y^* = 0.001, 0.005, 0.05, 0.01 \text{ m}$$

$$\beta_x^* = 0.5, 0.1, 0.05, 0.01 \text{ m}$$

keeping

$$L_0 = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\xi_y = 0.09$$



Monochromatization principle “Optimized” Scheme for FCC-ee

$L = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1} \quad \xi_y = 0.09$				
$\beta_y^* [m]$	0.001	0.005	0.01	0.05
N_b	$3.8 \cdot 10^{10}$	$1.95 \cdot 10^{11}$	$3.8 \cdot 10^{11}$	$1.95 \cdot 10^{12}$
$\beta_x^* [m]$	0.5	0.5	0.5	0.5
$\epsilon_y [m \text{ rad}]$	$1.6 \cdot 10^{-12}$	$4.1 \cdot 10^{-12}$	$1.6 \cdot 10^{-10}$	$4.1 \cdot 10^{-9}$
$\sigma_y^* [m]$	$4.0 \cdot 10^{-8}$	$1.4 \cdot 10^{-7}$	$1.3 \cdot 10^{-6}$	$1.4 \cdot 10^{-5}$
$\sigma_x^* [m]$	$1.02 \cdot 10^{-4}$	$1.02 \cdot 10^{-4}$	$1.02 \cdot 10^{-4}$	$1.02 \cdot 10^{-4}$
ξ_x	0.007	0.018	0.069	0.151

Monochromatization principle “Optimized” Scheme for FCC-ee

$L = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1} \quad \xi_y = 0.09$				
$\beta_y^* [m]$	0.001	0.005	0.01	0.05
N_b	$3.8 \cdot 10^{10}$	$1.95 \cdot 10^{11}$	$3.8 \cdot 10^{11}$	$1.95 \cdot 10^{12}$
$\beta_x^* [m]$	0.1	0.1	0.1	0.1
$\epsilon_y [m \text{ rad}]$	$8.1 \cdot 10^{-12}$	$2.1 \cdot 10^{-11}$	$8.1 \cdot 10^{-10}$	$2.1 \cdot 10^{-10}$
$\sigma_y^* [m]$	$9.0 \cdot 10^{-8}$	$3.2 \cdot 10^{-7}$	$2.8 \cdot 10^{-6}$	$3.2 \cdot 10^{-5}$
$\sigma_x^* [m]$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$
ξ_x	0.0007	0.0037	0.007	0.028

Monochromatization principle “Optimized” Scheme for FCC-ee

$L = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1} \quad \xi_y = 0.09$				
$\beta_y^* [m]$	0.001	0.005	0.01	0.05
N_b	$3.8 \cdot 10^{10}$	$1.95 \cdot 10^{11}$	$3.8 \cdot 10^{11}$	$1.95 \cdot 10^{12}$
$\beta_x^* [m]$	0.05	0.05	0.05	0.05
$\epsilon_y [m \text{ rad}]$	$1.6 \cdot 10^{-11}$	$4.1 \cdot 10^{-11}$	$1.6 \cdot 10^{-9}$	$4.1 \cdot 10^{-8}$
$\sigma_y^* [m]$	$1.3 \cdot 10^{-7}$	$4.5 \cdot 10^{-7}$	$4.0 \cdot 10^{-6}$	$4.5 \cdot 10^{-5}$
$\sigma_x^* [m]$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$
ξ_x	0.0004	0.0019	0.004	0.012

Monochromatization principle “Optimized” Scheme for FCC-ee

$L = 6.0 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1} \quad \xi_y = 0.09$				
$\beta_y^* [m]$	0.001	0.005	0.01	0.05
N_b	$3.8 \cdot 10^{10}$	$1.95 \cdot 10^{11}$	$3.8 \cdot 10^{11}$	$1.95 \cdot 10^{12}$
$\beta_x^* [m]$	0.01	0.01	0.01	0.01
$\epsilon_y [m \text{ rad}]$	$8.1 \cdot 10^{-11}$	$2.1 \cdot 10^{-10}$	$8.1 \cdot 10^{-9}$	$2.1 \cdot 10^{-7}$
$\sigma_y^* [m]$	$2.8 \cdot 10^{-7}$	$1.0 \cdot 10^{-6}$	$9.0 \cdot 10^{-6}$	$1.0 \cdot 10^{-4}$
$\sigma_x^* [m]$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$	$1.0 \cdot 10^{-4}$
ξ_x	0.00007	0.0004	0.0007	0.002

Conclusions

- There is no fundamental reason against monochomatization.
- Implementation of a “standard” and even an “optimized” scheme seems not so difficult.
- But monochomatization has never been tested experimentally these means a flexible lattice with two modes of operation with/without is mandatory.

Drawbacks:

- D_x^* gives rise quantum excitation which increase horizontal emittance
- Residual coupling
- Aperture limitation
- Dynamic Aperture reduction
- Beam-Beam including parasitic crossings
- Estimations of the broad band and the narrow band impedances and the current limits
- Touschek lifetime
- Polarization ring
- Background and masking

References

- [1] R. Eichler et al., Proposal for an electron-positron collider for heavy flavor particle physics and synchrotron radiation (PSI PR 88-09, 1988).
- [2] J.M. Jowett, CERN LEP-TH 87-56 (1987).
- [3] A.A. Zholents, CERN SL/AP 92-27 (1992).
- [4] P.F. Beloshitsky, A magnet lattice for a Tau-Charm factory suitable for both standard scheme and monochromatization scheme (LAL-RT 92-09, July 1992).
- [5] SLAC linear collider conceptual design report, SLAC report 229 (1980).
- [6] J. Gonichon, J. Le Duff, B. Mouton and C. Travier, Preliminary study of a high luminosity e^+e^- storage ring at a CM energy of 5 GeV (LAL-RT 90-02, January 1990).
- [7] A Renieri, Possibility of achieving very high energy resolution in e^+e^- storage rings, Frascati Preprint INF/75/6(R) (1975).
- [8] A.A. Advienko et al., The project of modernization of the VEPP-4 storage ring for monochromatic experiments in the energy range of Ψ and Y mesons, Proc. 12th Int. Conf. on High Energy Accelerators, Batavia (1983).
- [9] K. Wille and A.W. Chao, SLAC/AP-32 (1984).
- [10] M. Bassetti and J.M. Jowett, Proc. IEEE Part. Accel. Conf., Washington (1987) p. 115 and CERN/LEP-TH/87-09 (1987).
- [11] A. Faus-Golfe and J. Le Duff, A versatile lattice for a tau-charm factory that includes a monochromatization scheme (LAL-RT 92-01, February 1992).
- [12] A.L. Gerasimov and A.A. Zholents, Proc. 13th Int. Conf. on High Energy Accelerators, Novosibirsk (1986) and Preprint INP 86-85, Novosibirsk (1986).
- [13] A.L. Gerasimov, D.N. Shatilov and A.A. Zholents, Nucl. Instr. and Meth. A 305 (1991) 25.
- [14] DESY Storage Ring Group, Proc. 9th Int. Conf. on High Energy Accelerators, Stanford (1974) p. 43.
- [15] A.L. Gerasimov, D.N. Shatilov and A.A. Zholents, Proc. 9th Int. Conf. on High Energy Accelerators, Stanford (1974).
- [16] K.W. Robinson, Phys. Rev. 111 (2) (1958) 373.
- [17] A. Hoffman, LEP Note 192, October 1979.
- [18] Workshop 4th Generation Light Sources SSRL 92/02 (1992).
- [19] M. Sommer, Optimization of the emittance of electron-positrons storage rings, LAL-RT 83-15, November 1983.
- [20] G. Wüstefeld, The minimization of the natural emittance in the Triple Bend Achromat, Technischer Bericht BESSY TB 108-87 (1987).
- [21] A Jackson, A comparison of the Chasman-Green and Triple Bend Achromat, LBL 21279 (1986).
- [22] H. Kung, C. Travier and C.C. Kuo, Emittance calculation for a TBA storage ring, SRRC/BD 87-04 (1987).
- [23] L. Farvacque, J.L. Laclare and A. Ropert, BETA User's Guide, ESRF-SR LAT-88-08, Grenoble, March 1987, revised in February 1989.
- [24] H. Grote and F. Christoph Iselin, CERN SL/AP 90-13 (Rev. 3) (1993).

References

- [25] M. Donald and D. Schofield, A User's guide to the HAR-MON program, LEP Note 420 (1982).
- [26] F. Iazzourene, C.J. Bocchetta, R. Nagaoka, L. Tosi and A. Wrulich, RACE-TRACK User's guide Version 4.01, ST/M 92-7, July 1992.
- [27] R.P. Walker, Proc. IEEE Part. Accel. Conf., Washington, vol. 1 (1987) p. 491.
- [28] U. Völkel, Particle Loss by Touschek Effect in a Storage Ring, DESY 67-5 (1967).
- [29] J. Haissinski, Rapport technique 52.63 bis Rubriques: Problèmes Théoriques généraux (1963).
- [30] Y. Alexahin, Calculation of the Touschek lifetime JINR Dubna, private communication.
- [31] J. Haissinski, RT 5-64 Anneaux de stockage, Laboratoire de l'Accélérateur Linéaire, Orsay (1964).
- [32] A. Faus-Golfe and J. Le Duff, *Versatile DBA and TBA lattices for a Tau-Charm Factory with and without beam Monochromatization*. NIM A 372 (1996) 6-18.
- [33] A. Zholents, *Shopisticated Accelerator Techniques for Colliding Beam Experiments*. NIM A 265 (1988) 179-185.

Thanks for your attention

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E

E

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e^-

e^+