

# Electroweak radiative corrections and $\alpha_{EM}(m_Z)$ determinations

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More material on <http://jadach.web.cern.ch/> and  
<http://wasm.web.cern.ch/wasm/>

# Role of $\alpha_{QED}(M_Z)$

Key input parameter precision of FCC-ee phenomenology:

$$\frac{\delta\alpha}{\alpha} \sim 3.6 \cdot 10^{-9}$$

$$\frac{\delta G_\mu}{G_\mu} \sim 8.6 \cdot 10^{-6}$$

$$\frac{\delta\alpha(M_Z)}{\alpha(M_Z)} \sim 1.6 \leftrightarrow 6.8 \cdot 10^{-4} \quad \frac{\delta M_Z}{M_Z} \sim 2.4 \cdot 10^{-5}$$

Clear: better control of  $\alpha(M_Z)$  is needed for precision physics.

In fact what is needed is precision of  $\alpha(Q)$ ;

It was this uncertainty contributing dominantly to 0.04% systematic error for luminosity measurement at LEP.

At this moment there is plenty of time for improvements from:

- better measurements of  $e^+e^- \rightarrow$  hadrons at low energies
- Lattice QCD calculations.
- Direct measurement of  $\alpha(Q)$  at FCC itself.

Important: how programs are going to use the input.

Resummations, Monte Carlo implementations, fitting programs.

In the following I want to concentrate on the issue:

0.01 % theoretical precision tag for realistic observable(s)

- I will not review existing programs and calculations, for reference see for example *Oct 28 meeting*:  
<https://indico.cern.ch/event/337673/other-view?view=standard>  
or talks of the present meeting.
- I will not review phenomenology possibilities, it is also presented elsewhere

I will recall experience of our KKMC Monte Carlo program of LEP time. Also BHLUMI as possible example/starting point.

It took decades to prepare phenomenology frame for LEP. Some of the calculations are at use and improve, but some other may be lost. Needed are stable devoted research groups.

# Precision of $\alpha_{QED}(M_Z)$ measurements

TH lumi precision:  $\sim 4 \cdot 10^{-4}$ , similar to  $\frac{\delta\alpha(M_Z)}{\alpha(M_Z)} \sim 1.6 \leftrightarrow 6.8 \cdot 10^{-4}$

Hint: useful, direct, measurement of  $\alpha(M_Z)$ ,  $\alpha(Q)$  from cross section measurement may be an option for FCC-ee.

Programs of LEP time useful, or better to start from scratch?  
In either case LEP experience can be helpful.

At this moment it seems that there is plenty of time for improvements.  
However every factor of 2 in systematic error is paid by enormous effort.  
Which need to be distributed among many people.

It took decades to prepare phenomenology frame for LEP.

- perturbative calculations of fixed higher orders, results from lattice QCD.
- Separation of results into QED (QED-like) parts, vacuum polarization parts, genuine weak corrections.
- Resummation techniques, such as exclusive exponentiation, or introduction of effective  $Z$  width.
- Specific programs: MC's for  $e^+e^- \rightarrow e^+e^-$ ,  $e^+e^- \rightarrow \bar{l}l$ , for fits, for electroweak corrections, vac. pol. etc.

# MC project useful for $\alpha_{QED}(M_Z)$ measurement.

## What is KKMC?

KKMC is the MC event generator for the process:

$$e^- e^+ \rightarrow f\bar{f} + n\gamma$$

$f = \mu, \tau, \nu, u, d, s, c, b, \quad n = 0, 1, 2 \dots \infty.$

Interfaced with TAUOLA+PHOTOS  
and with electroweak library DIZET.

Published version **4.13** (to be cited):

- Comput.Phys.Commun. 130(2000) 360, hep-ph/9912214, F77 code description and user guide (manual).
- Phys. Rev. D63 (2001) 113009, hep-ph/0006359 physics content, CEEEX exponentiation of QED corrs.

"Workhorse" in data analysis of all four LEP collaborations.

At present it is used extensively by Belle collaboration, also test for LHC

(FCC perspective: continuous improvements, checks with new compilers etc.)

# More KKMC versions available since 2000

<http://jadach.web.cern.ch/jadach/KKindex.html>

- Production Version **4.16**, Oct. 2001,  
(KKMC-v.4.16d-export.tar.gz). Improved  $\nu\bar{\nu}$  matrix elm.  
RRes module for  $\gamma^* \rightarrow$  *narrow resonances* at LEP.
- Development Version **4.19**, Sept. 2002,  
(KKMC-v.4.19.b-export.tar.gz). C++ wrapper.  
Improved  $\nu\bar{\nu}$  matrix element and RRes for low energy colliders.  
ISR with complete NLO corrs, as in Phys.Rev. D65(2002)  
073030 by S.J., M.Melles, B.F.L.Ward and S.A. Yost.  
Collinear beamstrahlung for NLC/ILC.
- Development Version **4.22**, June 2013, (KKMC\_v4\_22.tgz).  
Tested  $\mu^- \mu^+$  and  $q\bar{q}$  beams (instead of  $e^- e^+$ ) at fixed energy.  
Optionaly, collinear PDFs for  $q\bar{q}$  beams instead of  
beamstrahlung, as a patch in the source code (temp. solution).
- The complete "algebraic" description of the NNLO formulas has been  
published in Phys.Rev. D73 (2006) 073001 (an extension of the work in  
Phys.Rev. D65 (2002) 073030), the code still not public.  
PHOKHARA MC is an alternative here for low energy colliders.

# Hidden treasures in KKMC

Can be useful for LHC?

KKMC is special because:

- Resummed (exponentiated) multiphoton effects at the AMPLITUDE level (CEEX).  $\sim 10$  man-years of work in QED.
- QED rad. corrections up to third LO and NLO, both in the initial and final state plus (exponentiated) initial-final interference.
- Complete spin effects, including transverse correlations, for incoming beams and outgoing fermions (needed for taus).

KKMC is useful in the LHC data analysis,

- Testing/calibrating for FSR in leptonic decays of Z/W,  $\phi_\eta^*$  observables
- Studies/estimations of ISR-FSR interferences in  $q\bar{q} \rightarrow Z \rightarrow l + \bar{l}$  data
- Electroweak+QCD corrections in the for Z production.cross section
- Spin correlations in  $Z \rightarrow \tau^- \tau^+$

# More on KKMC version 4.22 (2013)

## Technical points, important for project continuity

- Old benchmarks, Table III in Pys.Rev. D 63 (2001) and more, are reproduced under SLC5 and SLC6, after adjustments of flags in makefile's and minor corrections in f77 code.
- Unpublished (public) v.4.16,4.19 include varying subset of extra subdirectories, not included in v4.13. Also not in v.4.22.
- System of original interrelated custom *Makefile*'s is renamed *Makefile* → *KKMakefile* and preserved.
- *Automake/Autotools* are introduced (*makefile.am* etc.). Hence KKMC is more platform independent and can be easily put under *kdevelop3* or *eclipse*.
- Interface to C++ is provided. Main program (histogramming, etc) can be in C++, using optionally ROOT. (On request, or in v4.19)
- Scripts for running on PC-farms slightly upgraded and working.
- Still only old versions of PHOTOS and TAUOLA, straightforward to improve.



# More on KKMC version 4.22 (2013)

## Table III in Pys.Rev. D 63 (2001) reproduced

$v_{\max}$	$\mathcal{K}\mathcal{K}\text{sem Refer.}$	$\mathcal{O}(\alpha^3)_{\text{EEX3}}$	$\mathcal{O}(\alpha^2)_{\text{CEEX intOFF}}$	$\mathcal{O}(\alpha^2)_{\text{CEEX}}$
	$\sigma(v_{\max})$ [pb]			
0.01	$1.6712 \pm 0.0000$	$1.6736 \pm 0.0018$	$1.6738 \pm 0.0018$	$1.7727 \pm 0.0021$
0.10	$2.5198 \pm 0.0000$	$2.5205 \pm 0.0020$	$2.5210 \pm 0.0020$	$2.6009 \pm 0.0024$
0.30	$3.0616 \pm 0.0000$	$3.0626 \pm 0.0022$	$3.0634 \pm 0.0022$	$3.1243 \pm 0.0026$
0.50	$3.3747 \pm 0.0000$	$3.3745 \pm 0.0022$	$3.3761 \pm 0.0022$	$3.4254 \pm 0.0026$
0.70	$3.7223 \pm 0.0000$	$3.7214 \pm 0.0022$	$3.7249 \pm 0.0022$	$3.7648 \pm 0.0027$
0.90	$7.1430 \pm 0.0000$	$7.1284 \pm 0.0022$	$7.1530 \pm 0.0022$	$7.1821 \pm 0.0026$
0.99	$7.6136 \pm 0.0000$	$7.5974 \pm 0.0021$	$7.6278 \pm 0.0021$	$7.6567 \pm 0.0026$
	$A_{\text{FB}}(v_{\max})$			
0.01	$0.5654 \pm 0.0000$	$0.5661 \pm 0.0012$	$0.5661 \pm 0.0012$	$0.6121 \pm 0.0014$
0.10	$0.5664 \pm 0.0000$	$0.5667 \pm 0.0009$	$0.5667 \pm 0.0009$	$0.5931 \pm 0.0011$
0.30	$0.5692 \pm 0.0000$	$0.5694 \pm 0.0008$	$0.5693 \pm 0.0008$	$0.5864 \pm 0.0010$
0.50	$0.5744 \pm 0.0000$	$0.5744 \pm 0.0008$	$0.5743 \pm 0.0008$	$0.5870 \pm 0.0009$
0.70	$0.5863 \pm 0.0000$	$0.5858 \pm 0.0007$	$0.5857 \pm 0.0007$	$0.5953 \pm 0.0008$
0.90	$0.3105 \pm 0.0000$	$0.3107 \pm 0.0004$	$0.3100 \pm 0.0004$	$0.3176 \pm 0.0004$
0.99	$0.2851 \pm 0.0000$	$0.2856 \pm 0.0003$	$0.2848 \pm 0.0003$	$0.2918 \pm 0.0004$

Energy cut-off study of total cross section  $\sigma$  and charge asymmetry  $A_{\text{FB}}$  for annihilation process  $e^-e^+ \rightarrow \mu^-\mu^+$ , at  $\sqrt{s} = 189\text{GeV}$ .

Energy cut:  $v < v_{\max}$ ,  $v = 1 - M_{\text{ff}}^2/s$ .

From <http://arxiv.org/abs/arXiv:1307.4037>

# More on KKMC version 4.22 (2013)

## Physics extensions, 1st step: lepton beams

Lepton beams  $\neq e^\pm$ , for instance  $\mu^- \mu^+$ ,  $q\bar{q}$ , etc.

Mainly the problem of transferring properly mass of beam leptons.

A few corrections, et voilà!  $\mu^- \mu^+ \rightarrow e^- e^+$  at 189GeV.

$v_{\max}$	KKsem Refer.	$\mathcal{O}(\alpha^3)_{\text{EEX3}}$	$\mathcal{O}(\alpha^2)_{\text{CEEX intOFF}}$	$\mathcal{O}(\alpha^2)_{\text{CEEX}}$
	$\sigma(v_{\max})$ [pb]			
0.01	$1.6703 \pm 0.0000$	$1.6716 \pm 0.0040$	$1.6718 \pm 0.0040$	$1.7721 \pm 0.0048$
0.10	$2.5076 \pm 0.0000$	$2.5119 \pm 0.0046$	$2.5123 \pm 0.0046$	$2.5946 \pm 0.0055$
0.30	$3.0153 \pm 0.0000$	$3.0192 \pm 0.0048$	$3.0203 \pm 0.0048$	$3.0813 \pm 0.0057$
0.50	$3.2808 \pm 0.0000$	$3.2839 \pm 0.0049$	$3.2867 \pm 0.0049$	$3.3348 \pm 0.0058$
0.70	$3.5252 \pm 0.0000$	$3.5277 \pm 0.0049$	$3.5338 \pm 0.0049$	$3.5712 \pm 0.0059$
0.90	$5.4288 \pm 0.0000$	$5.3946 \pm 0.0047$	$5.4412 \pm 0.0047$	$5.4699 \pm 0.0057$
0.99	$5.7248 \pm 0.0000$	$5.6824 \pm 0.0046$	$5.7414 \pm 0.0046$	$5.7697 \pm 0.0057$
	$A_{\text{FB}}(v_{\max})$			
0.01	$0.5654 \pm 0.0000$	$0.5664 \pm 0.0028$	$0.5664 \pm 0.0028$	$0.6132 \pm 0.0032$
0.10	$0.5659 \pm 0.0000$	$0.5666 \pm 0.0021$	$0.5666 \pm 0.0021$	$0.5934 \pm 0.0025$
0.30	$0.5675 \pm 0.0000$	$0.5684 \pm 0.0019$	$0.5684 \pm 0.0019$	$0.5855 \pm 0.0022$
0.50	$0.5705 \pm 0.0000$	$0.5710 \pm 0.0018$	$0.5710 \pm 0.0018$	$0.5835 \pm 0.0021$
0.70	$0.5774 \pm 0.0000$	$0.5776 \pm 0.0017$	$0.5777 \pm 0.0017$	$0.5870 \pm 0.0020$
0.90	$0.3844 \pm 0.0000$	$0.3873 \pm 0.0011$	$0.3848 \pm 0.0011$	$0.3921 \pm 0.0012$
0.99	$0.3613 \pm 0.0000$	$0.3652 \pm 0.0010$	$0.3622 \pm 0.0010$	$0.3683 \pm 0.0012$

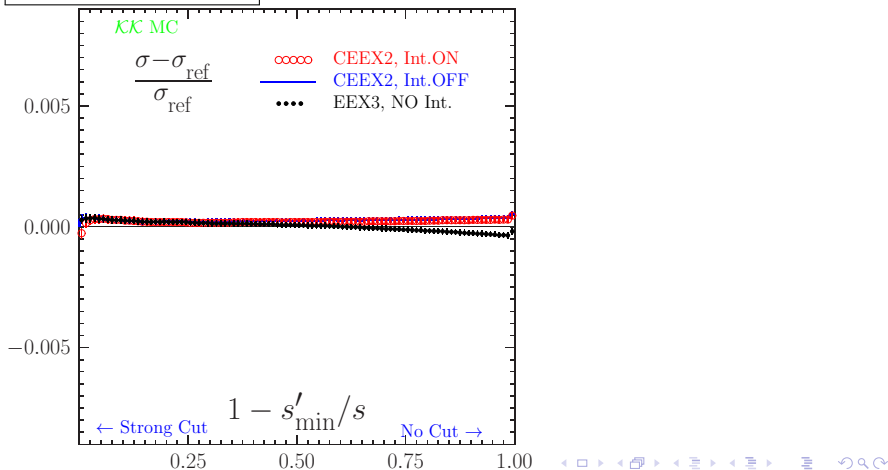
# More on KKMC version 4.22 (2013)

## Physics extensions, 2nd step: quark beams

Quark **beams** at fixed energy, for LHC, for continuity.

Mainly the problem of transferring properly weak isospin of beams.

$u\bar{u} \rightarrow e^-e^+ + n\gamma$  at  $\sqrt{s} = M_Z$ . Again KKMC vs. KKsem.



Quark **beams** at energies varying according to PDFs. From FCC-ee perspective it is important that program may go over evolution during LHC precision era. Also compatibility with FCC-pp applications.

Main problem in the code: variable  $\sqrt{s}$  from one MC event to another. Luckily already solved for beamstrahlung.

Test for  $u\bar{u} \rightarrow e^- e^+ + n\gamma$  at  $\sqrt{s} = M_Z$ .

KKMC vs. KKsem not available:(  
Only kinematics was tested, see event printout next slide.

# More on KKMC version 4.22 (2013)

## Physics extensions, 3rd step: PDFs for quark beam

```

*****
*                               KK Monte Carlo                               *
*                               4.22                               May 2013   *
*                               CMS energy average                 CMSene    a1 *
* 7000.000000000              Beam energy spread                 DelEne    a2 *
* 0.000000000                 Max. photon mult.                 npmax    a3 *
* 100                          wt-ed or wt=1 evt.                 KeyWgt   a4 *
* 0                             ISR switch                         KeyISR   a4 *
* 1                             FSR switch                         KeyFSR   a5 *
* 1                             ISR/FSR interferenc                KeyINT   a6 *
* 2                             New exponentiation                 KeyGPS   a7 *
* 1                             Hadroniz. switch                 KeyHad   a7 *
* 0                             Hadroniz. min. mass              HadMin   a9 *
* 0.200000000                 Maximum weight                     WTmax   a10 *
* 1.000000000                 Max. photon mult.                 npmax   a11 *
* 100                          Beam ident                         KFin    a12 *
* 2                             Manimum phot. ener.              Ene     a13 *
* 0.035000000                 Phot.mass, IR regul                MasPho  a14 *
* 0.100000000E-59            Phot. mult. enhanc.                Xenph   a15 *
* 1.250000000                 PolBeam1(1)                         Pol1x   a17 *
* 0.000000000                 PolBeam1(2)                         Pol1y   a18 *
* 0.000000000                 PolBeam1(3)                         Pol1z   a19 *
* 0.000000000                 PolBeam2(1)                         Pol2x   a20 *
* 0.000000000                 PolBeam2(2)                         Pol2y   a21 *
* 0.000000000                 PolBeam2(3)                         Pol2z   a22 *
*****

```

### Event listing (summary)

I	particle/jet	KS	KF	orig	p_x	p_y	p_z	E	m
1	!u!	21	2	0	0.000	0.000	22.668	22.668	0.005
2	!ubar!	21	-2	0	0.000	0.000	-245.458	245.458	0.005
3	(Z0)	11	23	1	23.016	18.370	-80.068	115.249	77.487
4	gamma	1	22	1	-30.989	-6.132	-128.905	132.719	0.000
5	gamma	1	22	1	0.000	0.000	0.031	0.031	0.000
6	gamma	1	22	1	7.973	-12.238	-13.848	20.127	0.000
7	gamma	1	22	1	0.000	0.000	3477.332	3477.332	0.000
8	gamma	1	22	1	0.000	0.000	-3254.542	3254.542	0.000
9	tau-	1	15	3	-24.701	21.657	-20.217	38.613	1.777
10	tau+	1	-15	3	47.716	-3.287	-59.851	76.635	1.777
	sum:		0.00		0.000	0.000	0.000	7000.000	7000.000

```

Event listing (summary)
I particle/jet KS   KF orig   p_x   p_y   p_z   E   m
1 !u!          21     2    0    0.000  0.000  271.908  271.908  0.005
2 !ubar!       21    -2    0    0.000  0.000   -6.542   6.542  0.005
3 (Z0)         11    23    1    0.047  1.133  244.401  257.454  80.928
4 gamma        1    22    1   -0.047  -1.133  20.965  20.996  0.000
5 gamma        1    22    1    0.000  0.000 3228.092 3228.092  0.000
6 gamma        1    22    1    0.000  0.000-3493.458 3493.458  0.000
7 mu-          1    13    3    0.601  14.537  2.005  14.687  0.106
8 mu+          1   -13    3   -0.554  -13.404 242.396 242.767  0.106
sum:          0.00  0.000  0.000  0.000  0.000 7000.000 7000.000

```

```

Event listing (summary)
I particle/jet KS   KF orig   p_x   p_y   p_z   E   m
1 !u!          21     2    0    0.000  0.000 1816.851 1816.851  0.005
2 !ubar!       21    -2    0    0.000  0.000   -1.137   1.137  0.005
3 (Z0)         11    23    1    0.011  0.003 1810.259 1812.532  90.760
4 gamma        1    22    1   -0.012  -0.002  5.371  5.371  0.000
5 gamma        1    22    1    0.000  0.000 1683.149 1683.149  0.000
6 gamma        1    22    1    0.000  0.000-3498.863 3498.863  0.000
7 mu-          1    13    3   12.468  -25.466 1612.743 1612.992  0.106
8 mu+          1   -13    3  -12.457  25.469 197.516 199.540  0.106
sum:          0.00  -0.001  0.001  -0.084 6999.916 6999.916

```

```

*****
*                               KK2f_Finalize printouts                               *
* 7000.00000000                 cms energy total                               cmsene   a0 *
*          5000                  total no of events                             nevgen   a1 *
* ** principal info on x-section **                                           *
* 233.95163953 +- 1.04896414  xs_tot MC R-units                               xsmc     a1 *
* 0.41468908                    xs_tot picob.                               xSecPb   a3 *
* 0.00185933                     x_err picob.                               xErrPb   a4 *
* 0.00448368                      relative error                               erel     a5 *
* 0.82048782                      WTsup, largest WT                          WTsup    a10 *
* ** some auxiliary info **                                                  *
* 0.00219522                      xs_born picobarns                             xborn    a11 *
* 0.73760000                      Raw phot. multipl.                          === *
* 5.00000000                      Highest phot. mult.                          === *
*                               End of KK2f_Finalize                               *
*****

```

# Pair emissions

KKMC was developed with 0.1% precision tag in mind.

Every factor of 2 improvement will be a challenge and we need to get to at least 0.01 % precision level.

One of such necessary elements is extra lepton pair emissions from final states.

Recently it became available with the help of PHOTOS C++ version <http://photospp.web.cern.ch/photospp/>, which is now 100% in C++ but has an interface to HEPEVT of F77 as well, thus can work with KKMC as well.

Pair emissions are not ready for precision simulation, but offer an option for detector response studies. Improvements will come over the next months.

# Pair emission

This example contains files and instructions on attaching Photos++ to KKMC v4.16d, easily adaptable to other KKMC versions.

```
=====
PHOTOS, Version: 3.58
Released at: 2/3/15
=====
```

Photos QED corrections in Particle Decays

Monte Carlo Program - by E. Barberio, B. van Eijk and Z. Was  
From version 2.09 - by P. Golonka and Z. Was  
From version 3.00 - by N. Davidson, T. Przedzinski and Z. Was

EVENT BEFORE Photos++ PROCESSING:

INFO from PHOTOS:

PhotosHEPEVTEvent

```
P:( 0)  11  3|  0.0000e+0  0.0000e+0  1.0000e+2  1.0000e+2|  5.1100e-4|M: -1 -1|D:  2  4
P:( 1) -11  3|  0.0000e+0  0.0000e+0 -1.0000e+2  1.0000e+2|  5.1100e-4|M: -1 -1|D:  2  4
P:( 2)  23  2| -2.3929e-2  3.5715e-2 -9.9410e+1  1.0059e+2|  1.5352e+1|M:  0  1|D:  5  6
P:( 3)  22  1|  2.3120e-2 -2.7186e-2  9.9379e+1  9.9379e+1|  0.0000e+0|M:  0  1|D: -1 -1
P:( 4)  22  1|  8.0862e-4 -8.5288e-3  3.0802e-2  3.1971e-2|  0.0000e+0|M:  0  1|D: -1 -1
P:( 5)  15  2|  7.2460e-1 -1.3170e+0 -9.7575e+1  9.7603e+1|  1.7770e+0|M:  2  2|D:  7  8
P:( 6) -15  2| -7.4853e-1  1.3527e+0 -1.8353e+0  2.9860e+0|  1.7770e+0|M:  2  2|D: 11 12
P:( 7)  16  1|  1.0911e+0 -5.8632e-1 -4.6120e+1  4.6137e+1|  9.9998e-3|M:  5  5|D: -1 -1
P:( 8) -213 2| -3.6653e-1 -7.3072e-1 -5.1455e+1  5.1466e+1|  6.9034e-1|M:  5  5|D:  9 10
P:( 9) -211 1| -3.2170e-1 -3.6679e-2 -1.4112e+1  1.4116e+1|  1.3957e-1|M:  8  8|D: -1 -1
P:(10) 111 1| -4.4830e-2 -6.9404e-1 -3.7343e+1  3.7350e+1|  1.3496e-1|M:  8  8|D: -1 -1
P:(11) -16  1| -2.8502e-1 -1.8574e-1  1.9563e-1  3.9257e-1|  9.9949e-3|M:  6  6|D: -1 -1
P:(12) 211 1| -4.6351e-1  1.5385e+0 -2.0309e+0  2.5935e+0|  1.3957e-1|M:  6  6|D: -1 -1
```



# Pair emissions, cont.

EVENT AFTER Photos++ PROCESSING:

INFO from PHOTOS:

PhotosHEPEVTEvent

```
P:( 0) 11 3| 0.0000e+0 0.0000e+0 1.0000e+2 1.0000e+2| 5.1100e-4|M: -1 -1|D: 2 4
P:( 1) -11 3| 0.0000e+0 0.0000e+0 -1.0000e+2 1.0000e+2| 5.1100e-4|M: -1 -1|D: 2 4
P:( 2) 23 2| -2.3929e-2 3.5715e-2 -9.9410e+1 1.0059e+2| 1.5352e+1|M: 0 1|D: 5 8
P:( 3) 22 1| 2.3120e-2 -2.7186e-2 9.9379e+1 9.9379e+1| 0.0000e+0|M: 0 1|D: -1 -1
P:( 4) 22 1| 8.0862e-4 -8.5288e-3 3.0802e-2 3.1971e-2| 0.0000e+0|M: 0 1|D: -1 -1
P:( 5) 15 2| 7.2412e-1 -1.3162e+0 -9.7512e+1 9.7540e+1| 1.7770e+0|M: 2 -1|D: 9 10
P:( 6) -15 2| -7.2159e-1 1.3580e+0 -1.8401e+0 2.9848e+0| 1.7770e+0|M: 2 -1|D: 13 14
P:( 7) 11 1| -9.3541e-3 -2.0009e-3 -2.1191e-2 2.3256e-2| 5.1100e-4|M: 2 -1|D: -1 -1
P:( 8) -11 1| -1.7109e-2 -4.1491e-3 -3.6517e-2 4.0542e-2| 5.1100e-4|M: 2 -1|D: -1 -1
P:( 9) 16 1| 1.0909e+0 -5.8590e-1 -4.6091e+1 4.6107e+1| 9.9998e-3|M: 5 -1|D: -1 -1
P:(10) -213 2| -3.6678e-1 -7.3026e-1 -5.1422e+1 5.1433e+1| 6.9034e-1|M: 5 -1|D: 9 10
P:(11) -211 1| -3.2170e-1 -3.6679e-2 -1.4112e+1 1.4116e+1| 1.3957e-1|M: 8 -1|D: -1 -1
P:(12) 111 1| -4.4830e-2 -6.9404e-1 -3.7343e+1 3.7350e+1| 1.3496e-1|M: 8 8|D: -1 -1
P:(13) -16 1| -2.7704e-1 -1.8577e-1 1.9630e-1 3.8716e-1| 9.9949e-3|M: 6 -1|D: -1 -1
P:(14) 211 1| -4.4455e-1 1.5438e+0 -2.0364e+0 2.5976e+0| 1.3957e-1|M: 6 6|D: -1 -1
```

Photos++ test: successfully added at least 1 particle. Exiting.

make[1]: Leaving directory `/tmp/KK-all/ffbench/Tau'

# Possible extensions for LHC use.

Could one include/improve QCD correction for the incoming beams?  
Yes, for example classic NLO corrs, Powheg style etc.

In this case the upper level of KKMC would be replaced by C++ code, which is already in place in some simple form.

The extension to  $q\bar{q} \rightarrow W \rightarrow l + \nu$  is thinkable, but would require update of the QED matrix element (also new EW corrs.)

NB. t-channel  $W$  exchange with h.o. QED is already there for  $\nu\bar{\nu}$  channel and could be exploited as a starting point.

The bottom line:

The existing KKMC can be exploited for LHC and for Belle applications, ensuring that it is living project !!!

# Summary

- KKMC alive, useful for on-going experiments, but has to find **new contributors** within next 10 years, if is to remain available for later decenies!
- Precision tag improvement  $0.1 \rightarrow 0.01$  % is a challenge but may be feasible.
- This requires effort of many peoples (groups) of distinct interest and over many years. It is not going to be easy.
- But it may be done. Note that BHLUMI precision tag of 0.04 % for LEP luminosity observables was reached years ago.

# Summary, cont.

- For KKMC QED component, path for improvements toward 0.01 % precision is clear. It requires effort, also in training of new people. No unexpected difficulties?
- Electroweak corrections up to two loops and in a form suitable for separation into: QED, line shape and genuine weak parts more difficult. We keep scientific links e.g. with people of former DIZET team having this challenge in mind.
- QED part need to be separated, because its higher orders have to be resummed in an exclusive manner.
- If  $\alpha_{QED}(M_Z)$  (and consequently  $\alpha_{QED}(Q)$ ) is to be obtained from direct measurements at high energies then it may simplify theoretical tasks. Less complications of dispersion relations resulting from use of low energy  $e^+e^- \rightarrow \text{hadrons}$  data.
- Semi-analytical calculations for tests and fitting programs (like ZFITTER) will be needed.
- **All this look challenging, but do-able.**