RF Cavity Design

- an introduction -



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Overview

Part 1:

- RF Cavity Design
 - Design Criteria
 - Figures of Merit
- Introduction to Superfish (2D)
- Examples:
 - Pill-box type cavity
 - DTL type cavity
 - Elliptical cavity
 - A ferrite loaded cavity

Part 2:

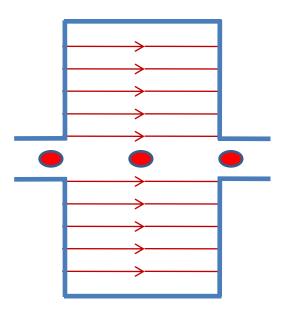
- CST MicroWave Studio Demo (3D)
- Surprise Cavity Model
- A Simple
 Measurement

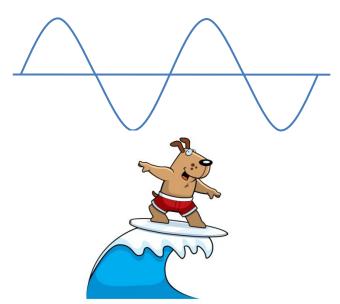




RF Cavity Design

- In most particle accelerators, the energy is delivered to the particle by means of a large variety of devices, normally know as cavity resonators.
- The ideal cavity: volume of perfect dielectric limited by infinitely conducting walls.
- Hollow cylindrical resonator excited by a radio transmitter -> standing wave -> accelerating fields (the pillbox cavity).



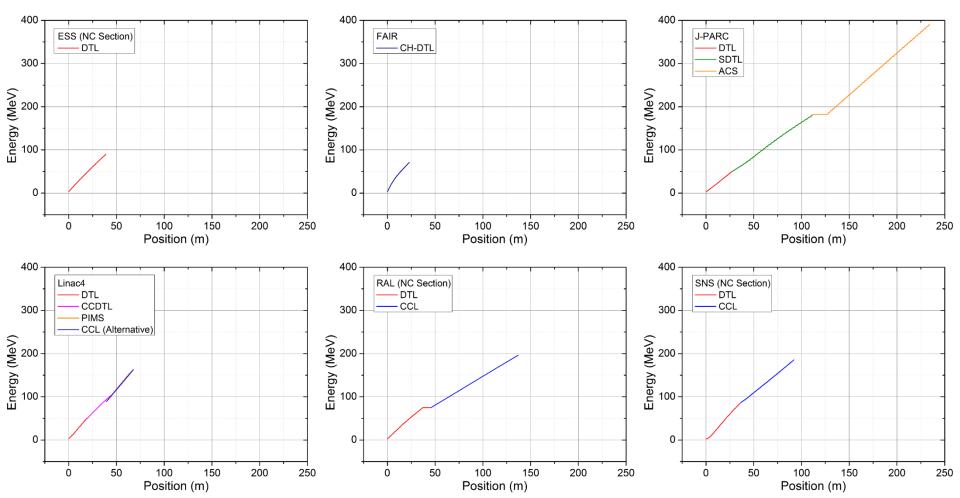






Why Cavity Design Is Important?

Acceleration Profile in Several Linacs







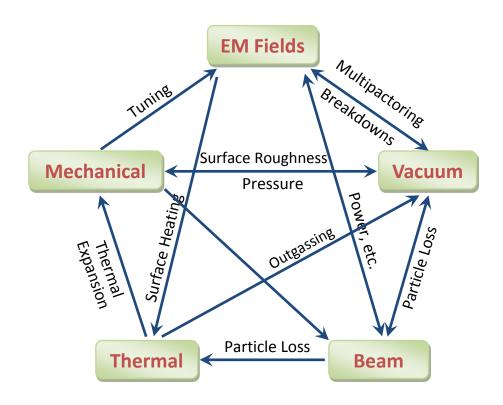
Design Criteria

- Define the requirements (intended application), RF frequency, NC/SC, voltage, tuning, etc.
- General design criteria:
 - Power Efficiency & RF Properties
 - Beam Dynamics considerations (control of loss and emittance growth, etc.) – especially true for linacs
 - Technologies and precisions involved
 - Tuning procedures (frequency, field profile, stability against perturbations)
 - Sensitivity to RF errors (phase and amplitude)
 - Etc.





The "Magic Pentagon" of Cavity Design

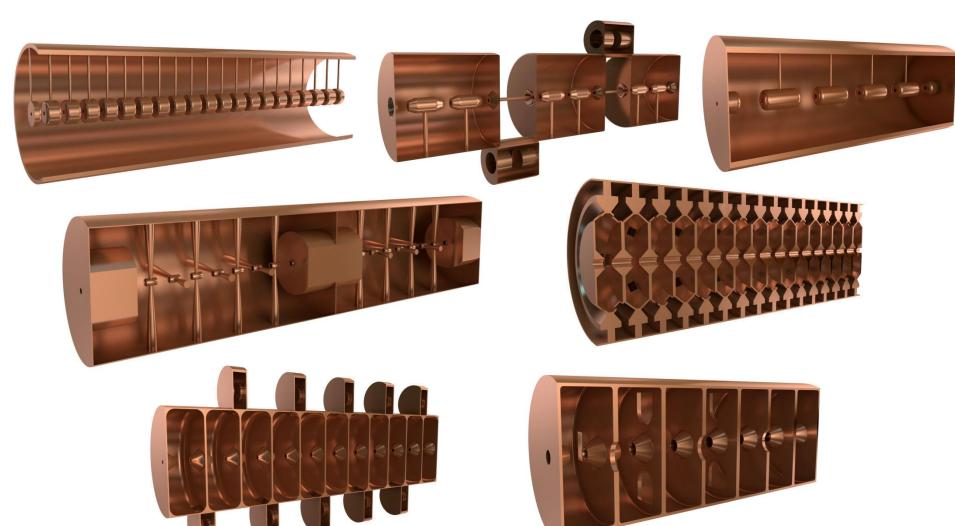


- The pentagon shows the importance of each design and manufacturing choice
- Technologies are interdependent





Cavity Zoo

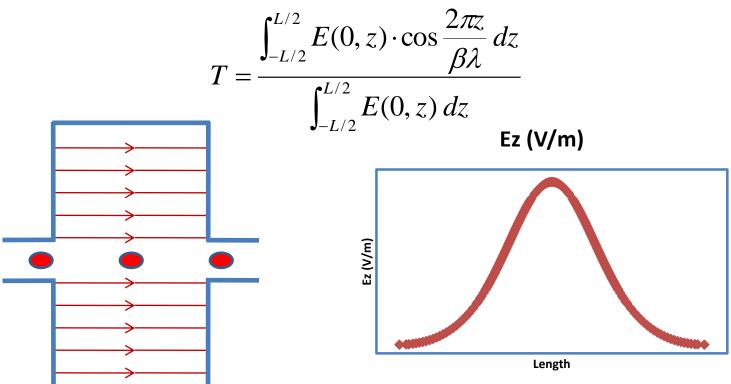






The Transit Time Factor, T

While the particle crosses the cavity, the field is also varying -> less acceleration ->
the particle sees only a fraction of the peak voltage -> T is a measure of the reduction
in energy gain cause by the sinusoidal time variation of the field in the cavity.







The Quality Factor, Q

$$Q_0 = \frac{2\pi \cdot stored\ energy}{energy\ consumed\ per\ period} = \frac{2\pi W}{TP_0} = \omega \frac{U}{P_0}$$

- To first order, the Q-value will depend on the conductivity of the wall material only
- High Q -> narrower bandwidth -> higher amplitudes
- But, more difficult to tune, more sensitive to mechanical tolerances (even a slight temperature variation can shift the resonance)
- Q is dimensionless and gives only the ratios of energies, and not the real amount of power needed to maintain a certain resonant mode
- For resonant frequencies in the range 100 to 1000 MHz, typical values are 10,000 to 50,000 for normal conducting copper cavities; 108 to 1010 for superconducting cavities.





Shunt Impedance

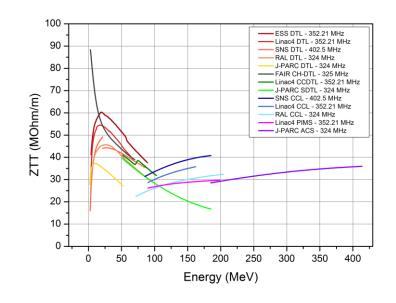
 A measure of the effectiveness of producing an axial voltage V₀ for a given power dissipated

$$r_s = \frac{V_0^2}{P_0}$$

Effective Shunt Impedance per unit length

$$ZT^2 = \frac{r}{L} = \frac{(E_0 T)^2}{P_0 / L}$$

– Typical values of ZT² for normal conducting linacs is 30 to 50 MΩ/m. The shunt impedance is not relevant for superconducting cavities.







r/Q

 measures the efficiency of acceleration per unit of stored energy at a given frequency

$$\frac{r}{Q} = \frac{(V_0 T)^2}{\omega U}$$

 It is a function only of the cavity geometry and is independent of the surface properties that determine the power losses.



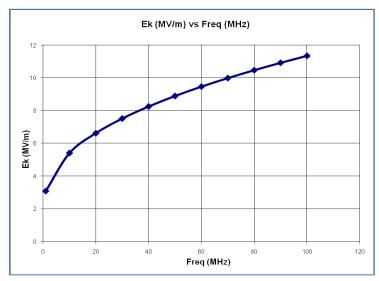


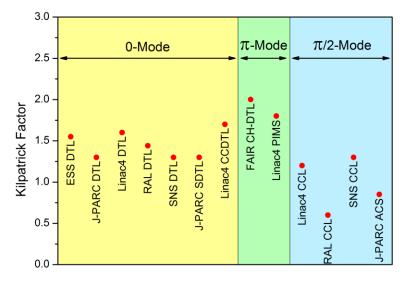
The Kilpatrick limit

- High Field -> Electric breakdown
- Maximum achievable field is limited

$$f = 1.64 E_k^2 e^{-8.5/E_k}$$





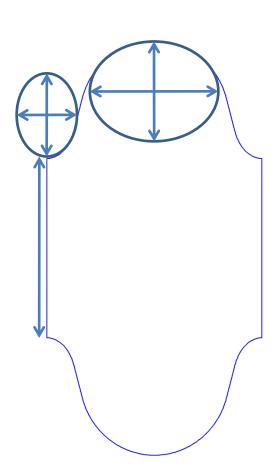






Superconducting Cavities (Slightly different story for):

- r/Q (characteristic impedance)
- G (Geometric Factor the measure of energy loss in the metal wall for a given surface resistance)
- Epeak/Eacc field emissions limit (Eacc limit)
- Bpeak/Eacc quench limit (sc breakdown)
- Higher Order Modes manage and suppress HOM (e.g.: dipole modes can degrade the beam -> suppression scheme using HOM couplers)
- Kcc Cell to cell coupling
- Multicell cavities: Field Flatness
- Optimise geometry to increase both r/Q and G resulting in less stored energy and less wall loss at a given gradient (low cryogenic losses)
- Optimise geometry to reduce Epeak/Eacc and Bpeak/Eacc
- Find optimum Kcc. (e.g.: a small aperture increases r/Q and G
 (!), but reduces Kcc. A small Kcc increases the sensitivity of the field profile to cell frequency errors.)







Introduction to Poisson Superfish

- You will need a laptop running Windows. If you have Linux/MacOS install VMWare/Wine.
- Please download and install Poisson Superfish. To do this go to the following address and follow the instructions: http://laacg1.lanl.gov/laacg/services/download_sf.phtml
- Please download the example files to your computer from the JAI website.
- An extensive documentation can be found in the Superfish home directory (usually C:/LANL).
 - Have a look at the SFCODES.DOC file. Table VI-4 explains how the object geometry is defined in Superfish (page 157).
 - For a list of Superfish variables, see SFINTRO.doc, Table III-3 (page 76)
- For any questions, email Emmanuel (<u>emmanuel.tsesmelis@cern.ch</u>) or Ciprian (<u>ciprian.plostinar@stfc.ac.uk</u>). Good luck!





Introduction to Poisson Superfish

- Poisson and Superfish are the main solver programs in a collection of programs from LANL for calculating static magnetic and electric fields and radio-frequency electromagnetic fields in either 2-D Cartesian coordinates or axially symmetric cylindrical coordinates.
- Finite Element Method



Solvers:

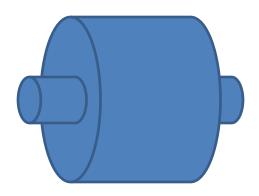
- Automesh generates the mesh (always the first program to run)
- Fish RF solver
- Cfish version of Fish that uses complex variables for the rf fields, permittivity, and permeability.
- Poisson magnetostatic and electrostatic field solver
- Pandira another static field solver (can handle permanent magnets)
- SFO, SF7 postprocessing
- Autofish combines Automesh, Fish and SFO
- DTLfish, DTLCells, CCLfish, CCLcells, CDTfish, ELLfish, ELLCAV, MDTfish, RFQfish, SCCfish for tuning specific cavity types.
- Kilpat, Force, WSFPlot, etc.





A Pillbox Cavity

The simplest RF cavity



For the accelerating mode (TM_{010}), the resonant wavelength is:

$$\lambda = \frac{\pi D}{x_1}$$
$$x_1 = 2.40483$$

 x_1 - first root of the zero-th order Bessel function J_0 (x)

- -> Resonant frequency independent of the cell length
- -> Example: a 40 MHz cavity (PS2) would have a diameter of ~ 5.7 m
- -> In the picture, CERN 88 MHz

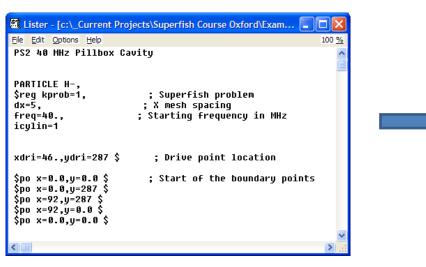


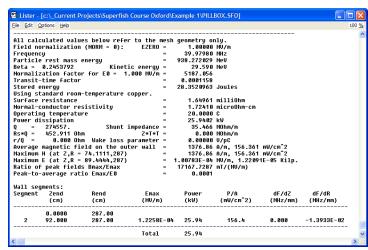


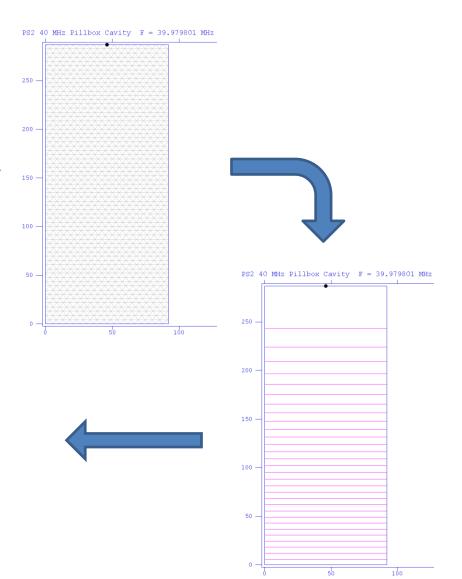


A Pillbox Cavity

Superfish input file





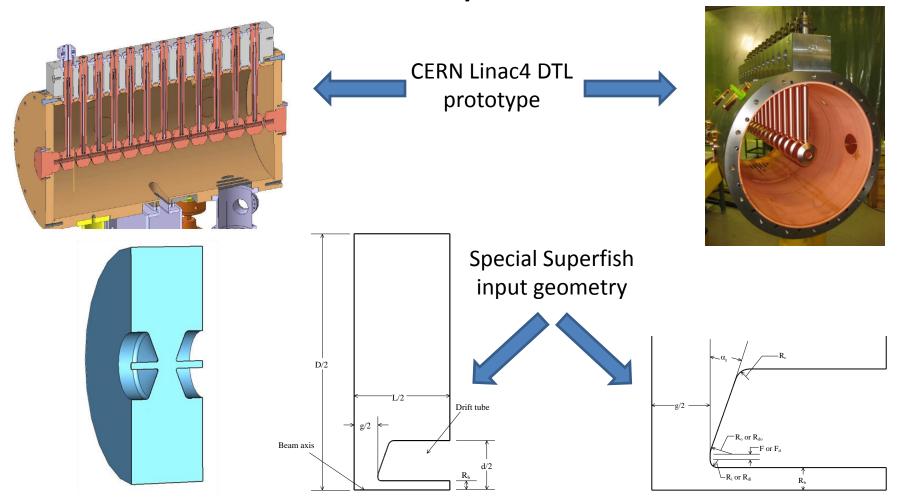






A DTL-type Cavity

Drift Tube Linac Cavity

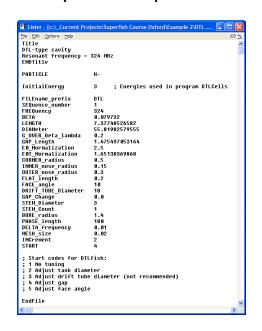




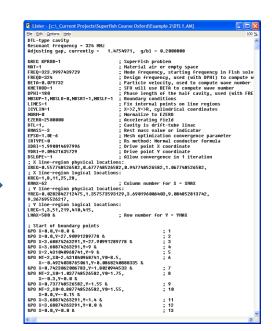


A DTL-type Cavity

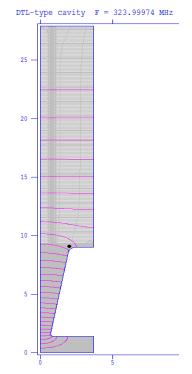
Superfish input file



Geometry file



Solution









An Elliptical Cavity

Often used in superconducting applications

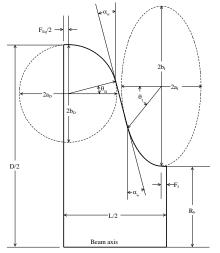


INFN & CEA 704 MHz elliptical SC cavities



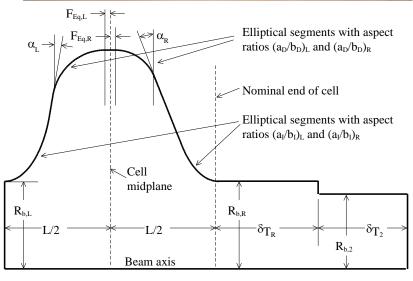






Special Superfish input geometry



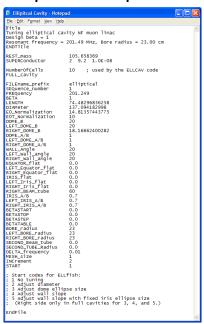






An Elliptical Cavity

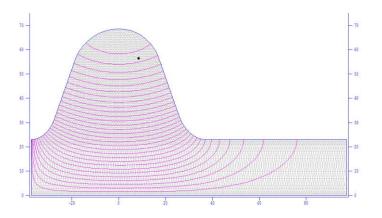
Superfish input file

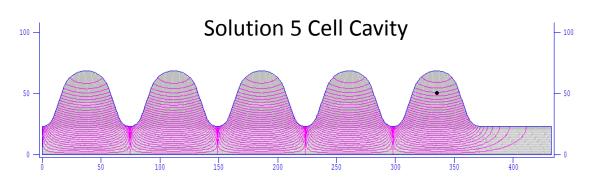


Geometry file



Solution 1 Cell







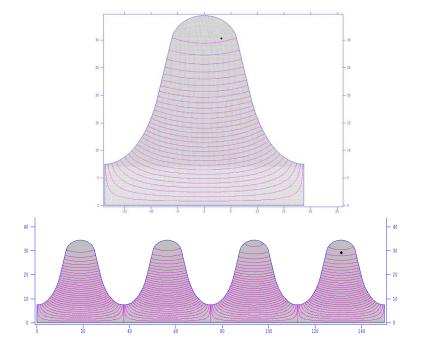


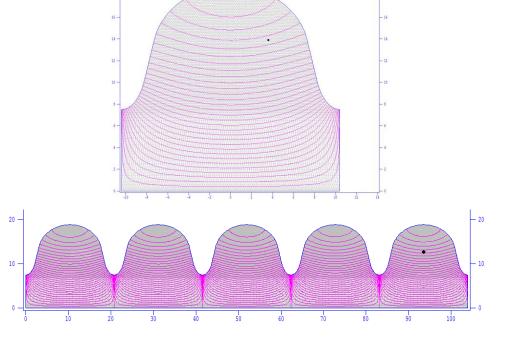


An Elliptical Cavity

- Example 1: 400 MHz
 - Like the LHC 400 MHz RF
 - 4-cell cavity, 4 cavities/Cryomodule

- Example2: 721.4 MHz
 - SPL-like cavities
 - 5-cell cavity









Ferrite Loaded Cavities

- Used when variable resonance is needed
- The torus of the ferrite encircles the beam path
- Ferrite properties are important (limit the cavity capabilities)
- Bias current -> Variable magnetic field -> Variable magnetic permeability of the ferrite -> Frequency change
- The structure can be thought of as a resonant transformer in which the beam constitutes a one-turn secondary winding.
- Frequencies domain: 100 kHz and 60 MHz

Beam

- Typical gap voltage of up tens of kV
- Different requirements (large frequency ranges, rapid swings, space, etc) -> various designs. $\bar{1}$

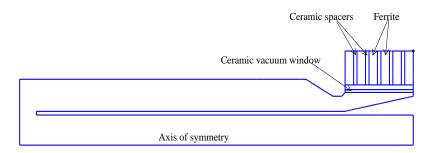


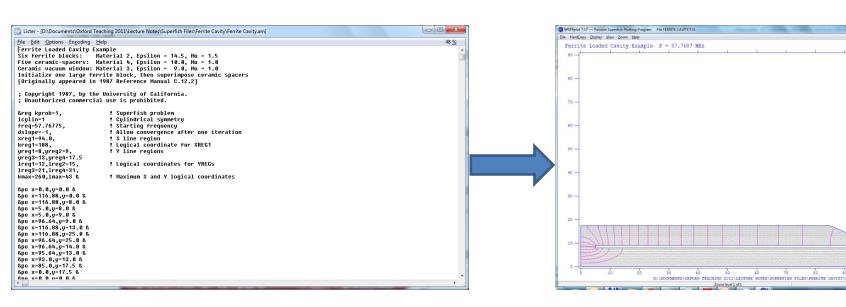


Ferrite Loaded Cavities

Six ferrite blocks: Epsilon = 14.5, Mu = 1.5 Five ceramic-spacers: Epsilon = 10.0, Mu = 1.0 Ceramic vacuum window: Epsilon = 9.0, Mu = 1.0

> Cavity length: 116 cm Number of gaps: 1









Now, use your imagination!