

Beyond the Standard Model

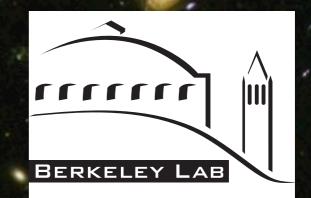
MATHEMATICS OF

Hitoshi Murayama (Berkeley, Kavli IPMU Tokyo) Invisibles School, June 17, 2015





BERKELEY CENTER FOR THEORETICAL PHYSICS

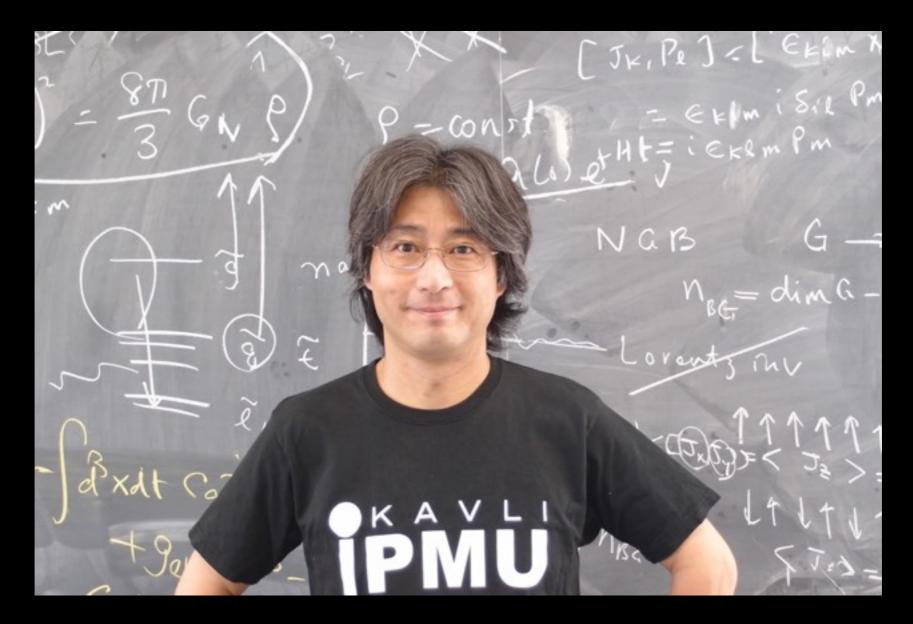




Director of the Kavli Institute for the Physics

and Mathematics of the Universe

A lot of responsibility!

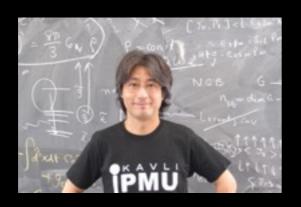


Director of the Universe

Not high enough authority

Voice of God





Director of the Universe



Beyond the Standard Model

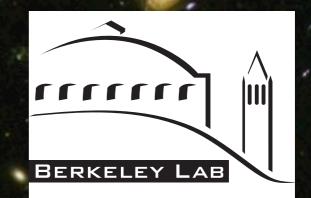
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2012.7.4 discovery of Higgs boson



Run: 204769 Event: 71902630 Date: 2012-06-10 Time: 13:24:31 CEST

http://atlas.ch

theory: 1964 design: 1984 construction: 1998

Higgsdependence Day July 4, 2012



Standard Model is extreeemely successful

- Take Particle Data Group "Reviews of Particle Physics" with 1676 pages
- With only a few exceptions, all numbers in the book are consistent with the Standard Model with suitably chosen 19 parameters
- add neutrinos: 5 more parameters
- Some of them tested at 10⁻⁹-10⁻¹² level
- Many at 10⁻³ level



Standard Model is extreeemely successful

- baryon and lepton number conserved (apart from anomaly $\propto e^{-8\pi^{2}/g^{2}}$)
- flavor approximately conserved (apart from small mixing in V_{CKM})
- especially flavor-changing neutral current small (e.g., s→d vanishes at tree-level, suppressed by m_c²/m_W² at one-loop)





Rare effects from high energies

• Effects of high-energy physics as effective operators added to the standard model

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda}\mathcal{L}_5 + \frac{1}{\Lambda^2}\mathcal{L}_6 + \cdots$$

can be classified systematically

 $\mathcal{L}_5 = (LH)(LH) \to \frac{1}{\Lambda} (L\langle H \rangle)(L\langle H \rangle) = m_{\nu} \nu \nu$

 $\mathcal{L}_{6} = QQQL, \bar{L}\sigma^{\mu\nu}W_{\mu\nu}Hl, \epsilon_{abc}W_{\nu}^{a\mu}W_{\lambda}^{b\nu}W_{\mu}^{c\lambda},$ $(H^{\dagger}D_{\mu}H)(H^{\dagger}D^{\mu}H), B_{\mu\nu}H^{\dagger}W^{\mu\nu}H, \cdots$

So, what's the problem?



Five empirical evidences for physics beyond SM

- Since 1998, it became clear that there are at least five missing pieces in the SM
 - non-baryonic dark matter
 - neutrino mass
 - accelerated expansion of the Universe
 - apparently acausal density fluctuations
 - baryon asymmetry

We don't really know their energy scales...

Physicists ask simple and profound questions

How did the Universe begin? What is its fate? What is it made of? What are its basic laws? Where do we come from?



Energy budget of Universe

- Stars and galaxies are only ~0.5%
- Neutrinos are ~0.1–0.5%
- Rest of ordinary matter (electrons, protons & neutrons) are 4.5%
- Dark Matter 27%
- Dark Energy 67%
- Anti-Matter 0%
- Higgs ~10⁶²%??

A C F LIFOR M

neutrinosdark matt

baryon

dark energy

Physicists ask simple and profound questions

How did the Universe begin? What is its fate? What is it made of? What are its basic laws? Where do we come from?





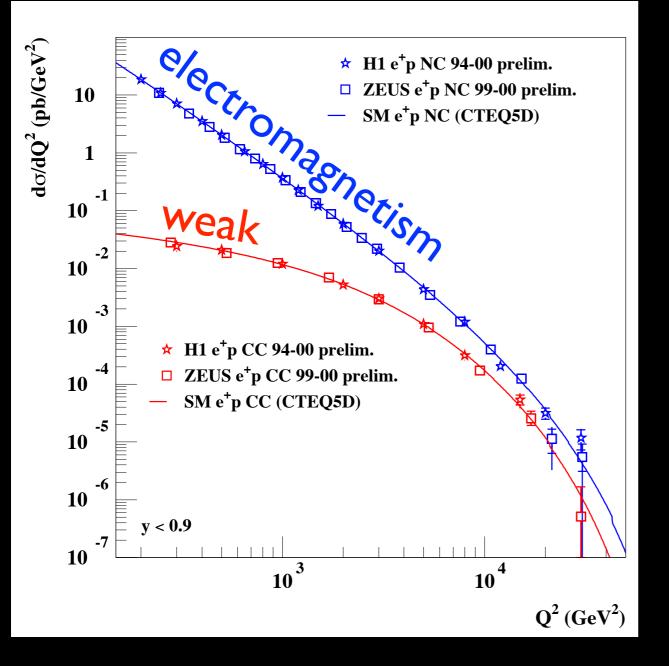
Einstein's Dream

- Is there an underlying simplicity behind vast phenomena in Nature?
- Einstein dreamed to come up with a unified description
- But he failed to unify electromagnetism and gravity (GR)



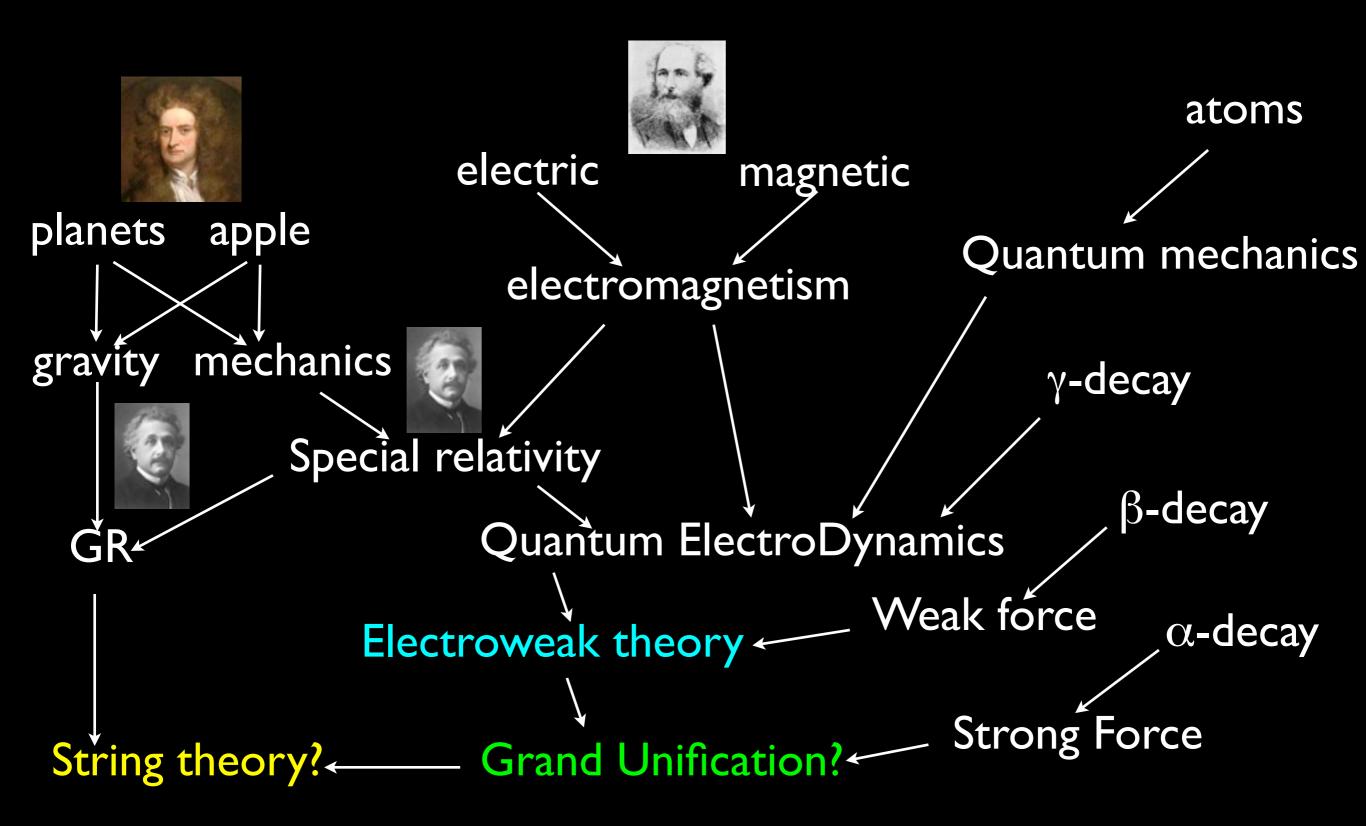
a new layer of unification

HERA ep collider



- Unification of electromagnetic and weak forces
- \Rightarrow electroweak theory
- Long-term goal since '60s
 We are finally getting there!
- If they are unified, what makes them so different?
- \Rightarrow Higgs boson!

History of Unification



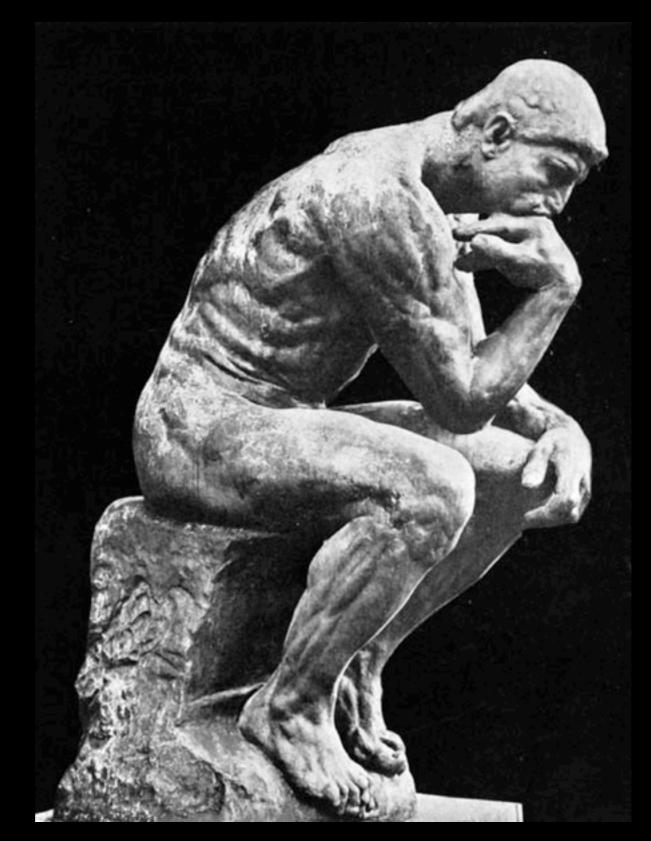
Physicists ask simple and profound questions

How did the Universe begin? What is its fate? What is it made of? What are its basic laws? Where do we come from?

Where do we come from?

Religions

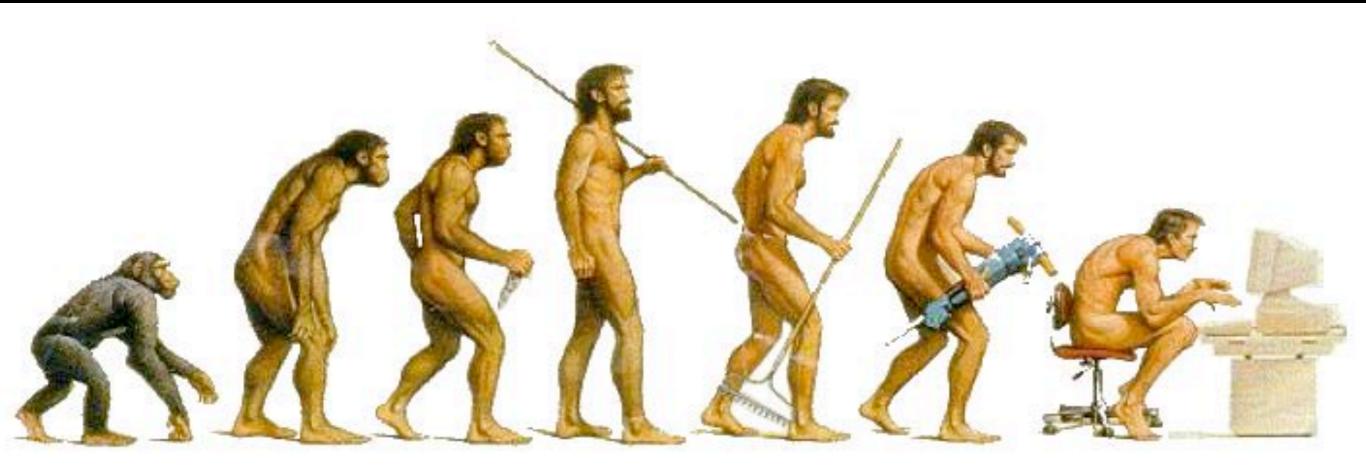
Where do we come from?

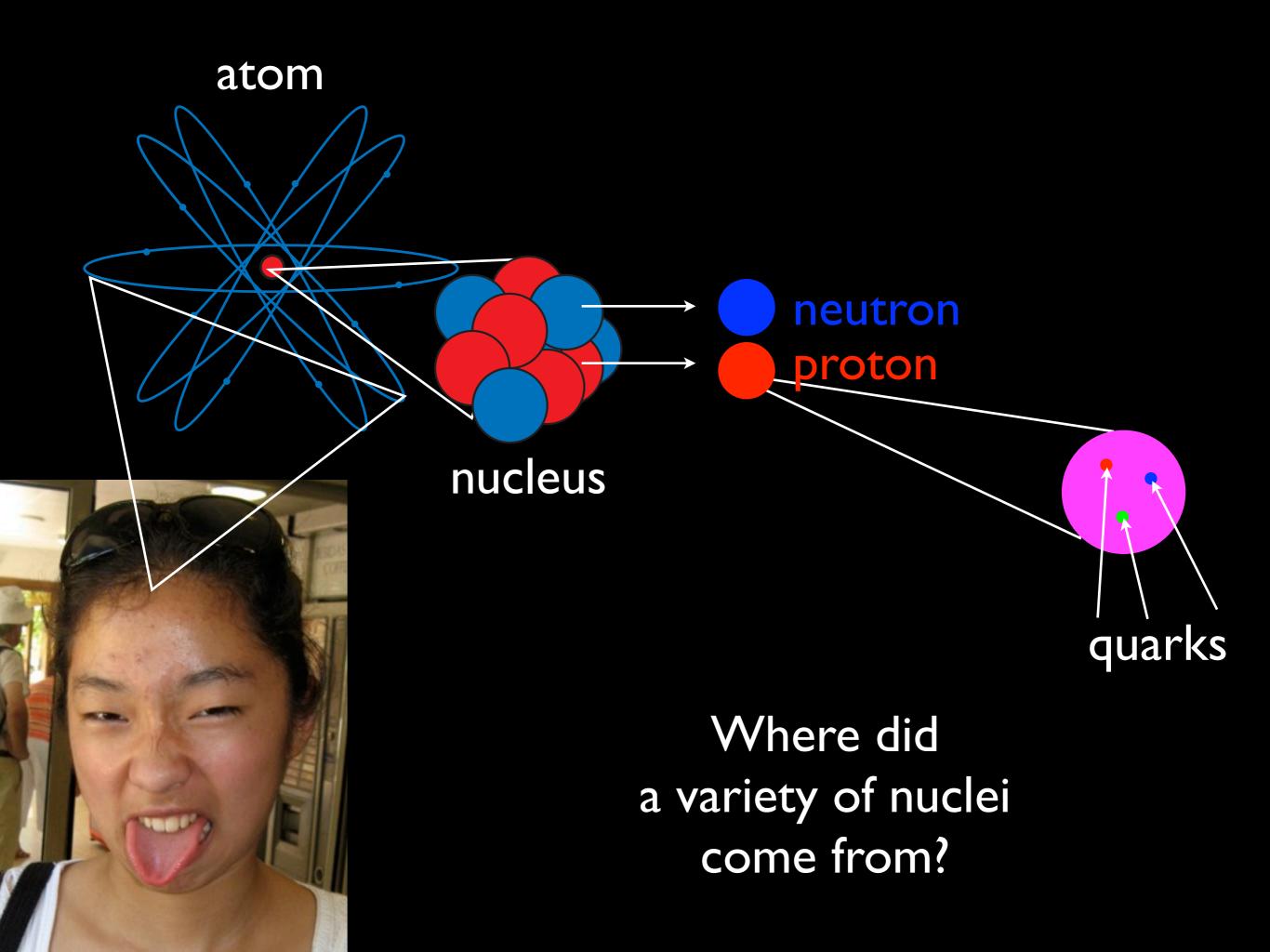


Philosophy

Where do we come from?

Evolutionary biology







Subaru 8.2m diameter mirror

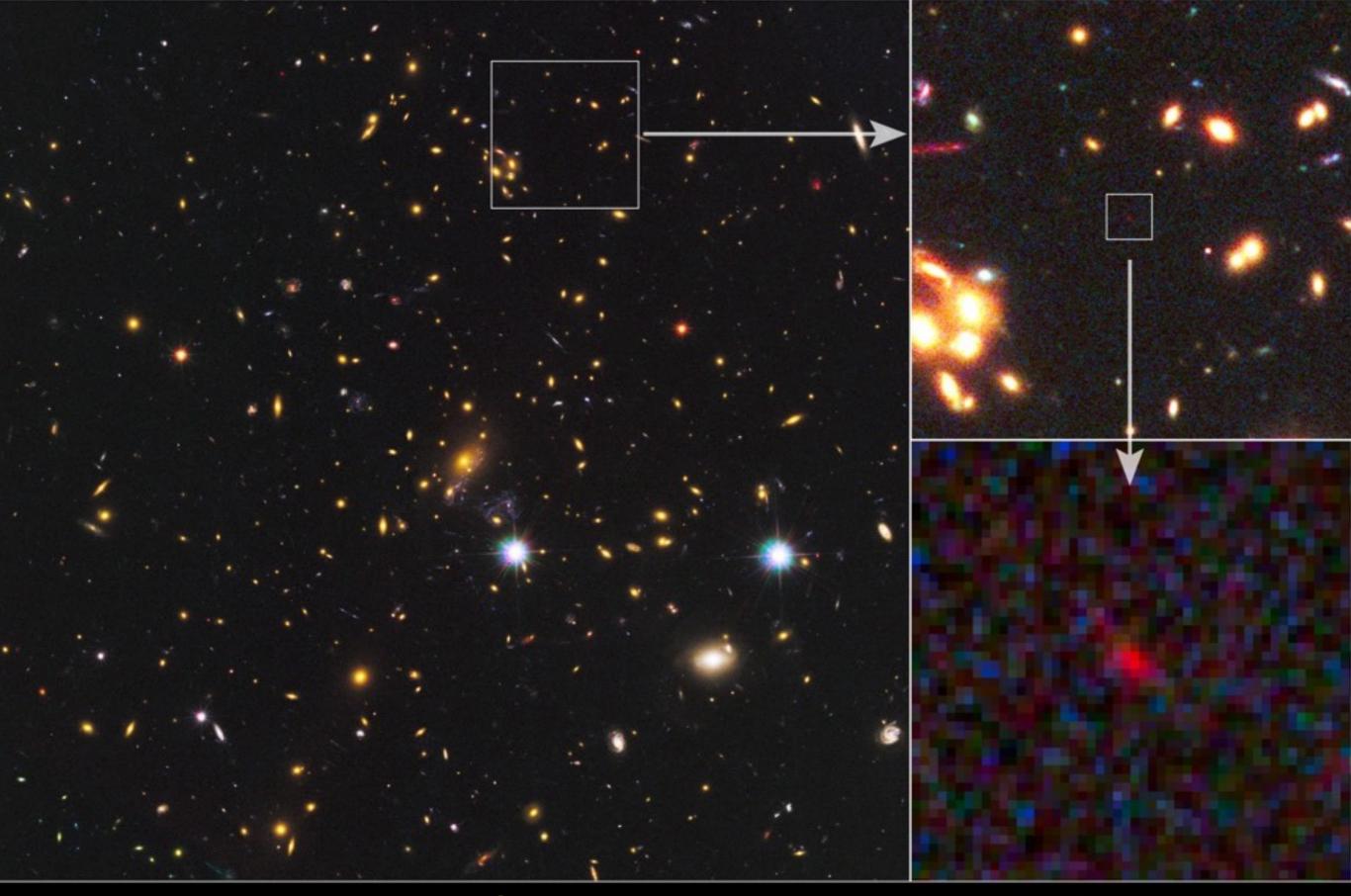
LHC 27km all around



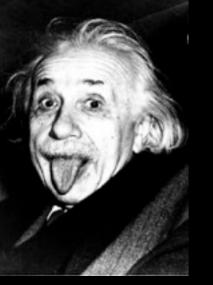
Andromeda 2.3 million light years

HSC team Subaru telescope cluster of galaxies 2.1 billion light years

Abell 2218



Galaxy Cluster MACS J1149+2223 galaxy @ 3.3 billion light years^{High-Redshift Galaxy MACS1149-JC A Distant Gravitationally-Lensed Galaxy at Redshift = 9.6 MASA / ESA / STScl/ J. Hora (Harvard-Smitsonian CfA)}

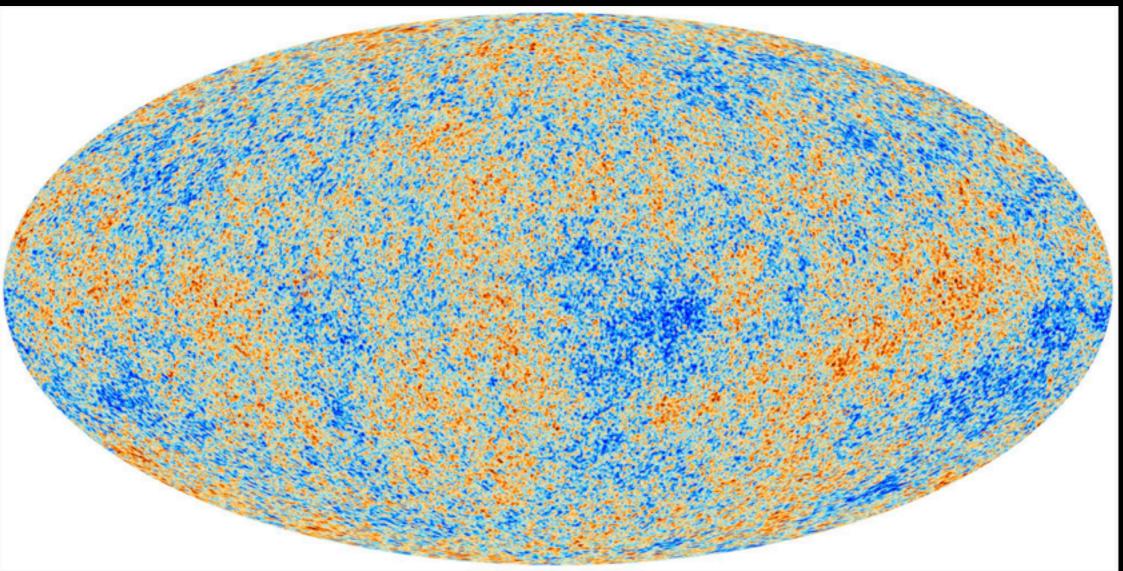


$E = h\nu = \frac{hc}{\lambda}$ expanding space

- Einstein: the universe is not just a box, actually *alive*
- the box can warp, twist, expand
- Universe as a whole is getting bigger
- at the same time it gets colder
- it was smaller, hotter in the past

Big Bang!

"Wall" @ 13.8 Blyrs



You can never "see" beyond this wall with a telescope

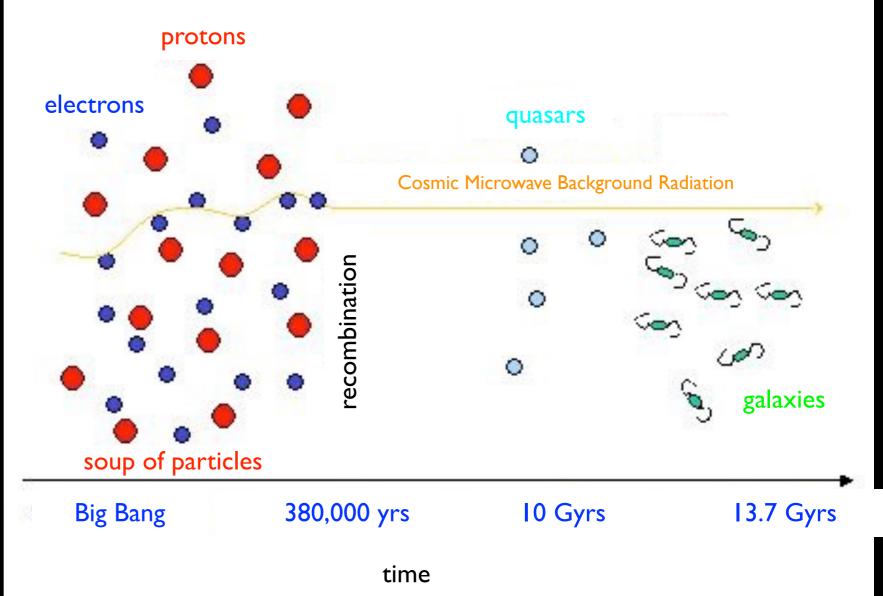


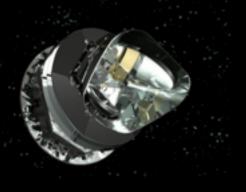




CMB

- before recombination, there was a fluid of protons, electrons, photons, dark matter (and neutrinos)
- photon pressure ⇒
 "sound waves"

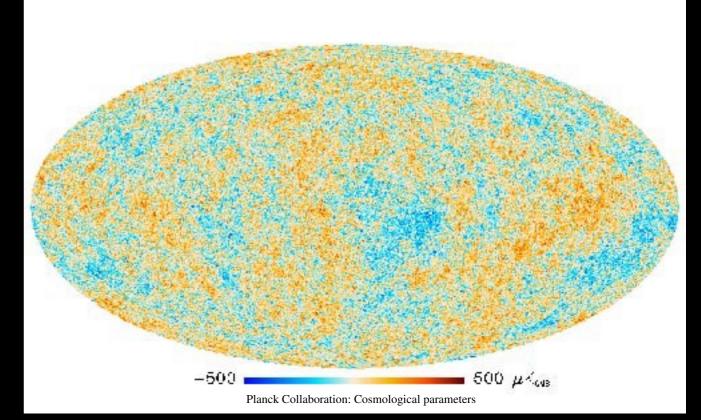


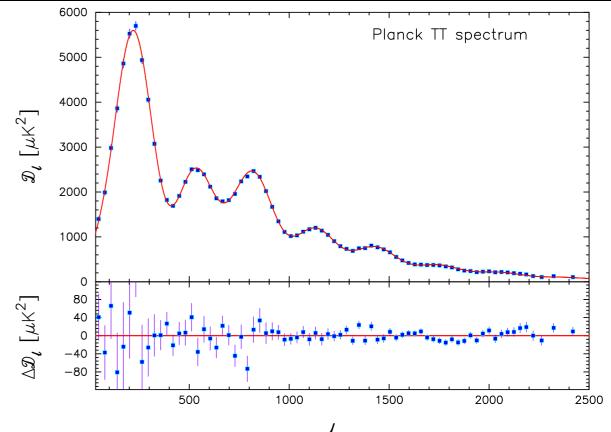


assumption



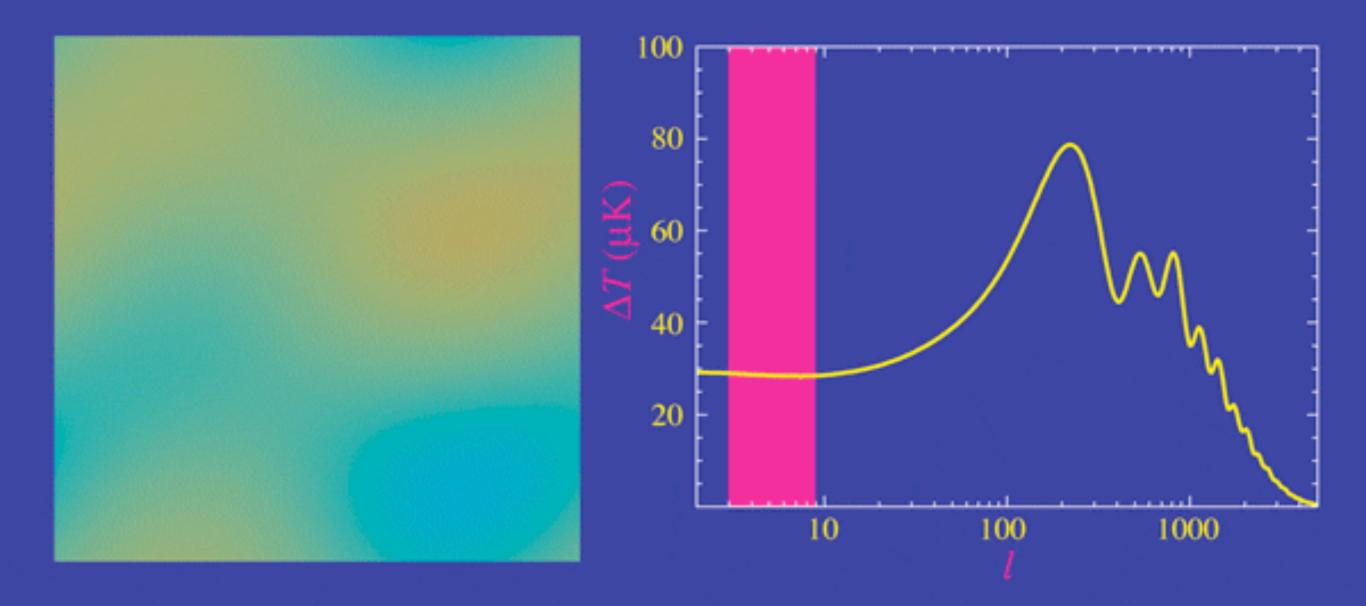
- a random density fluctuations $\sim O(10^{-5})$ more-or-less scale invariant $P(k) \propto k^{ns-1}$
- starts acoustic oscillation, amplified by gravitational attraction
- "knows" about everything between 0 < z < 1300 $\delta T/T = a_{lm} Y_{l}^{m}$ $(2l+1)c_{lm} = \sum_{m} a_{lm}^{*}a_{lm}$







angular resolution

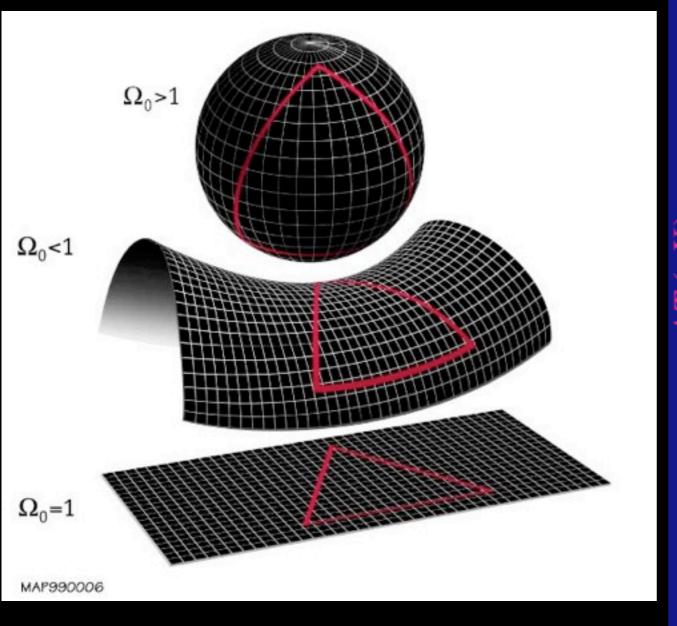


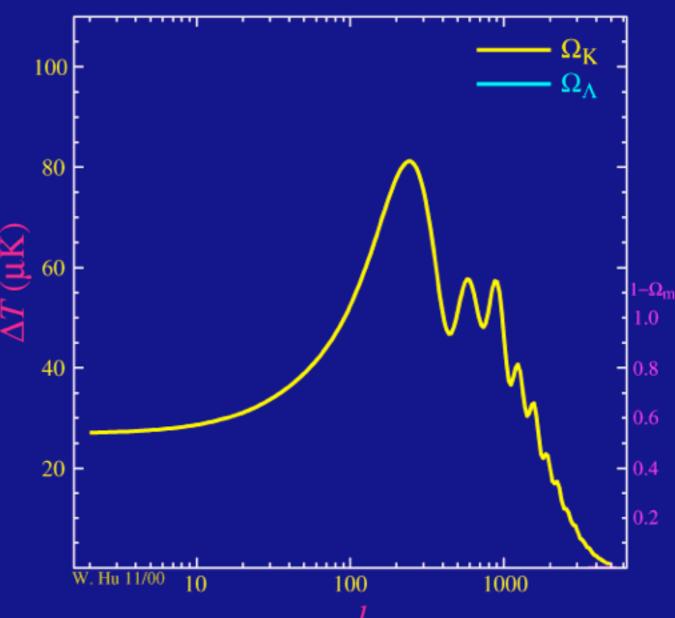
Wayne Hu

http://background.uchicago.edu/~whu/metaanim.html



spatial curvature



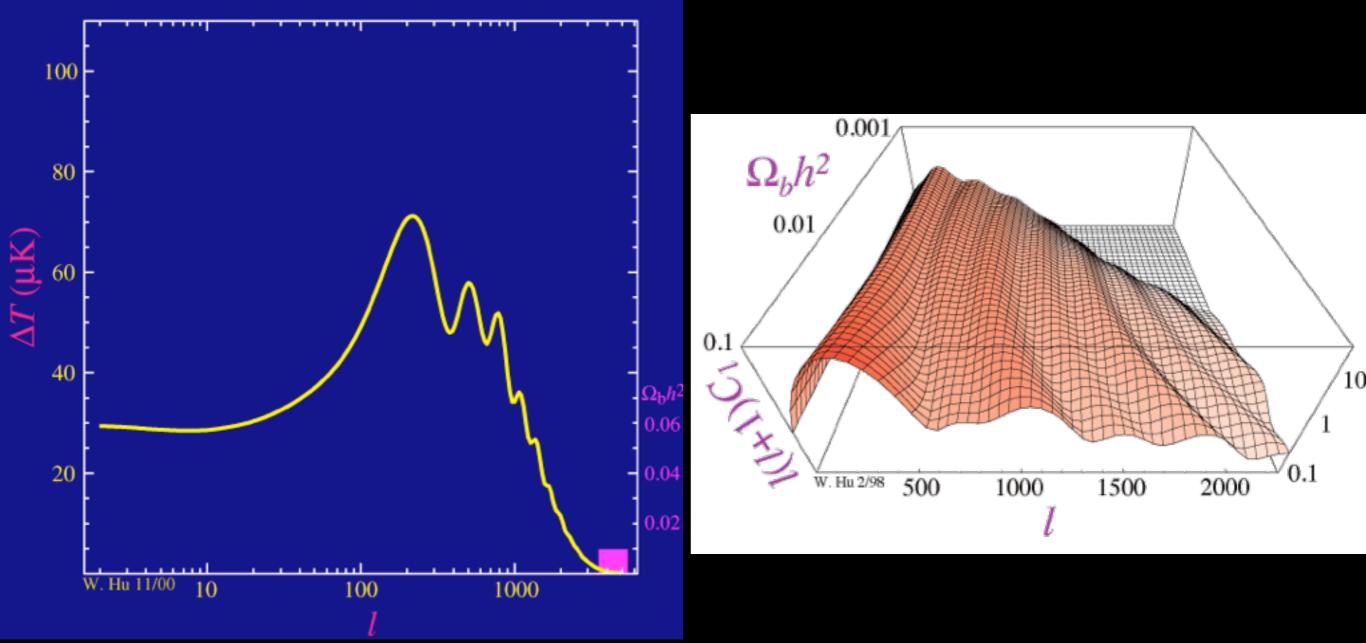


$$\label{eq:Ok} \begin{split} \Omega_k \mbox{ changes} \\ \mbox{the apparent angular size} \\ \mbox{ of the peak positions} \end{split}$$



atoms





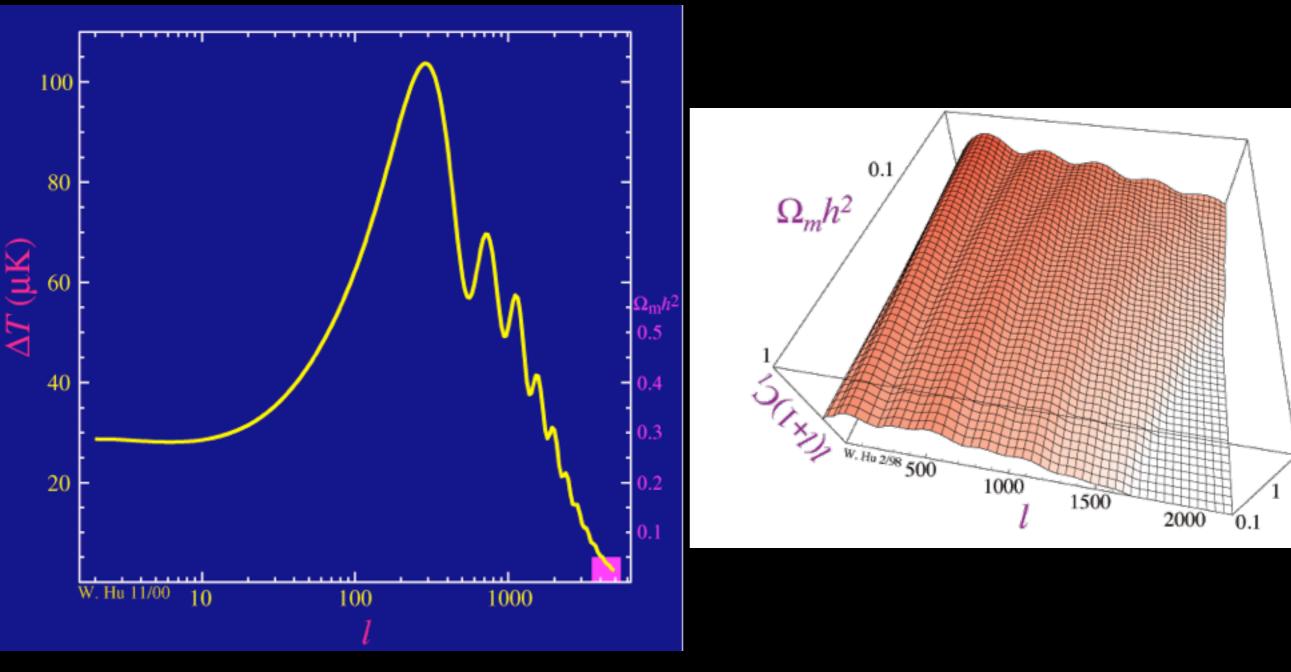
 Ω_b changes the relative size of even and odd peaks



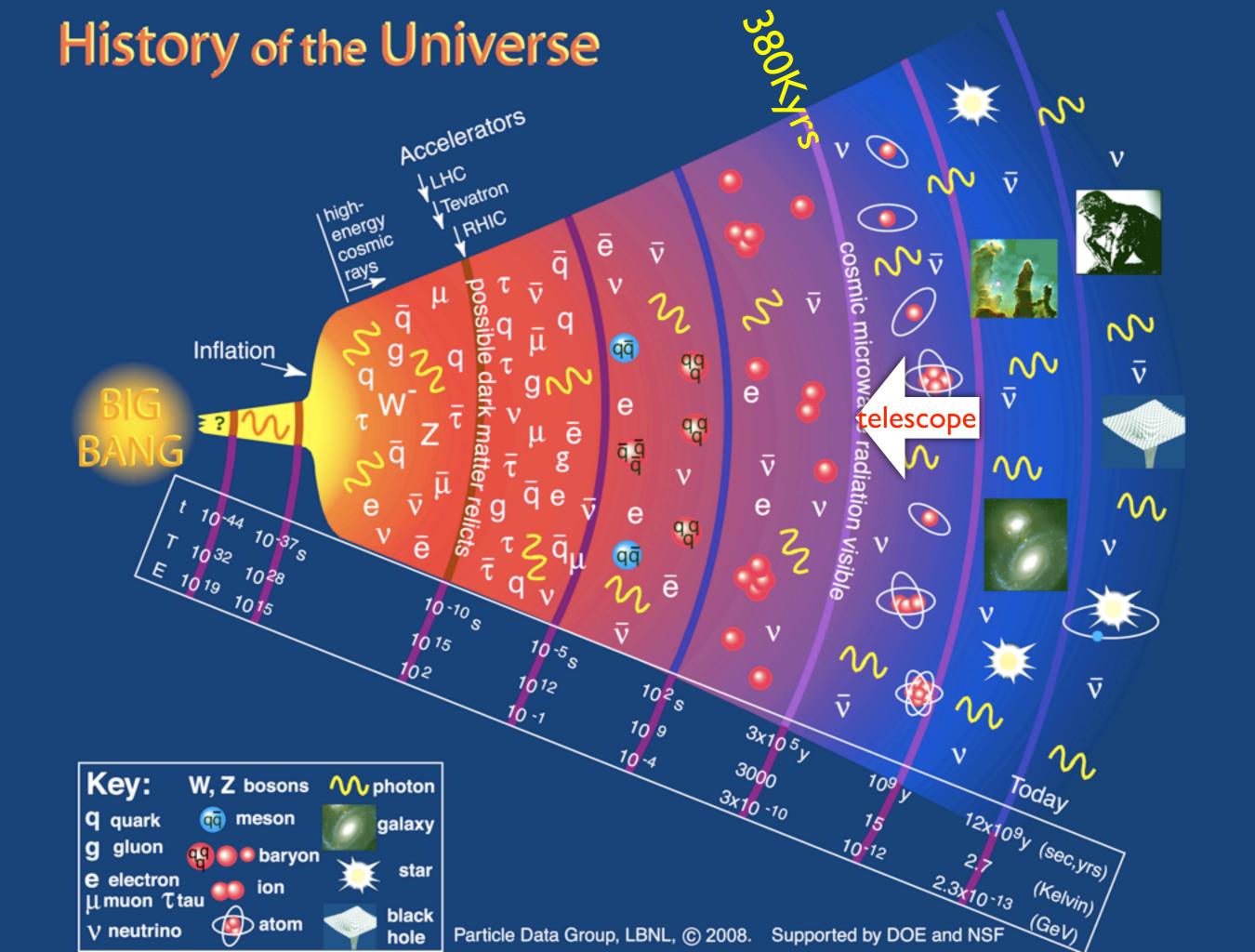
dark matter

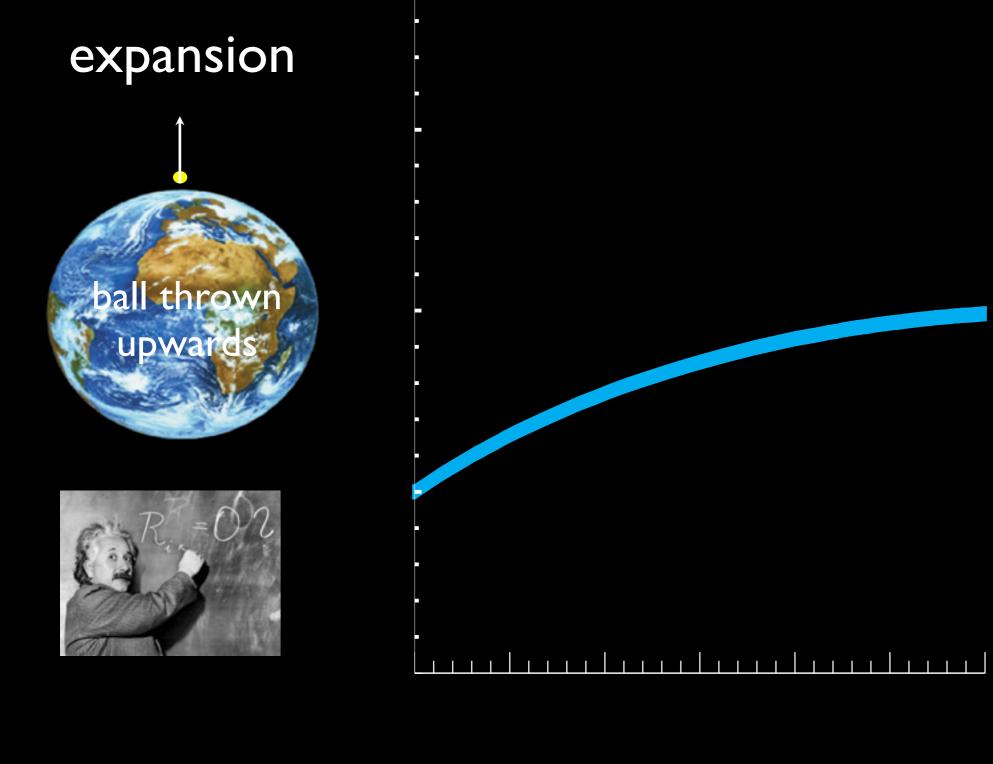


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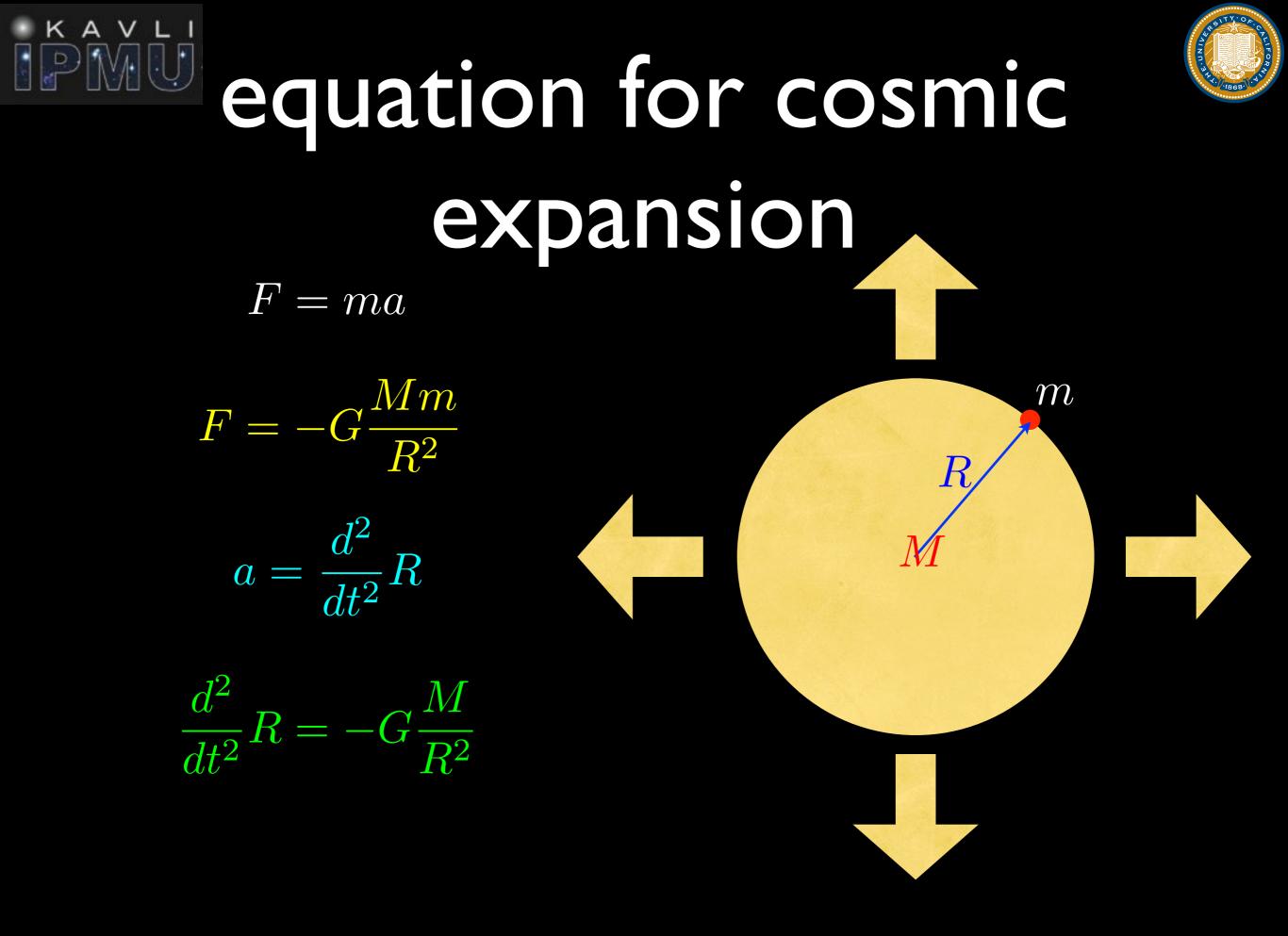


Ω_m changes overall power





should slow down







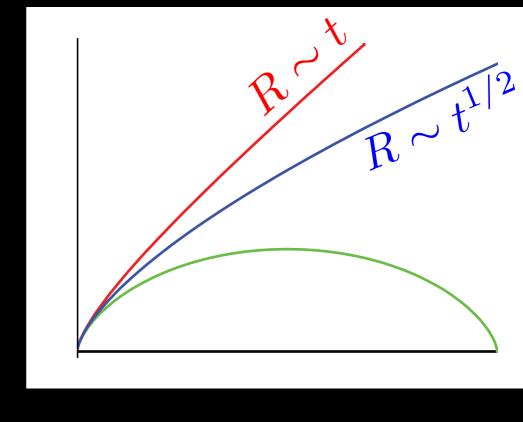
three possible fates

the same equation



- if enough matter, expansion slows and stops, starts to contract, Big Crunch
- if not enough matter, keeps expanding, eventually constant speed

size of the Universe

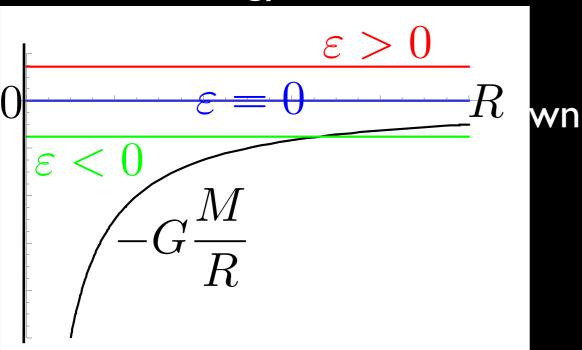


 $\frac{d^2}{dt^2}R$

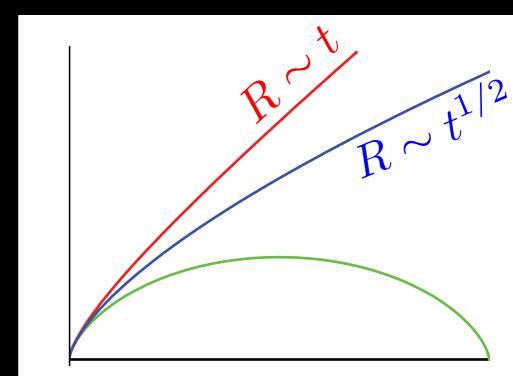
time

three possible fates $\frac{d^2}{dt^2}R = -G^2$

- This quantity is conserved (i.e. time-independent) $1 \left(\frac{dR}{2} \right)^2 M$
 - $\varepsilon = \frac{1}{2} \left(\frac{dR}{dt}\right)^2 G\frac{M}{R}$
- it has the interpretation of "total energy"



size of the Universe

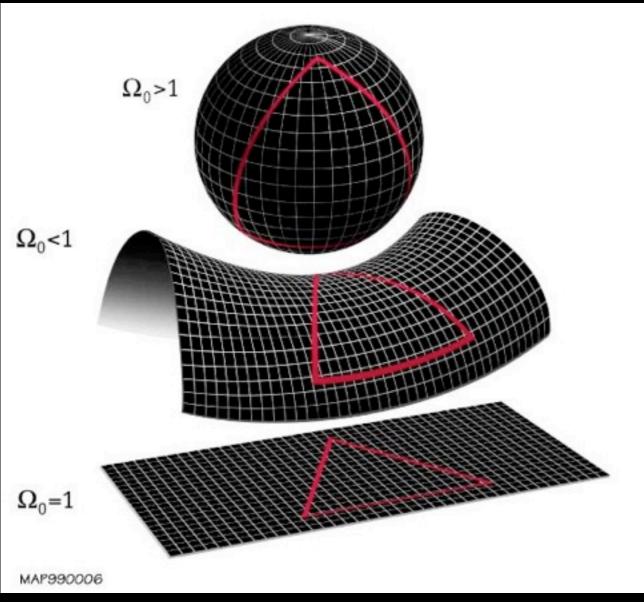


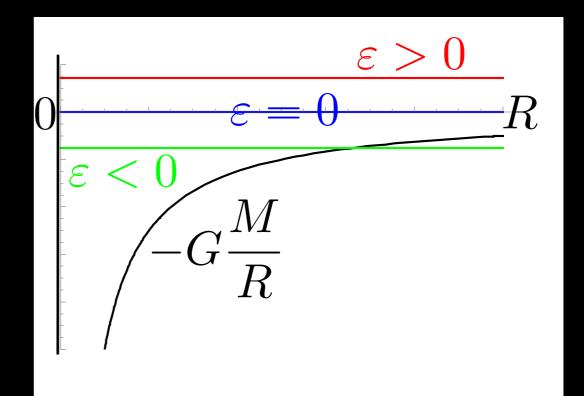
time





need GR for this





generalize

- so far assumed total mass is constant ("matter")
- if it changes as the Universe expands, generalize it
- Simplify the equation
- $\bullet \ \ \text{write} \ k=-2\varepsilon$

$$\varepsilon = \frac{1}{2} \left(\frac{dR}{dt}\right)^2 - G\frac{M}{R}$$

$$\varepsilon = \frac{1}{2} \left(\frac{dR}{dt}\right)^2 - G\frac{\rho}{R}\frac{4\pi}{3}R^3$$

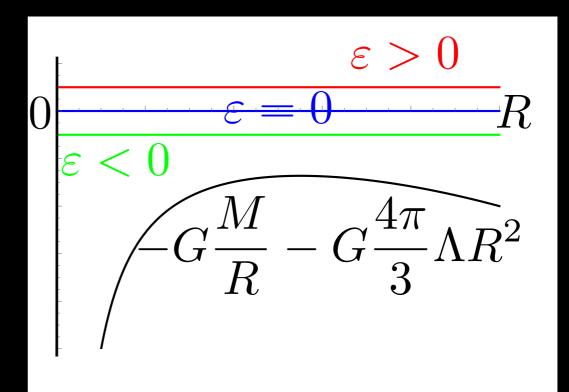
$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G\rho + \frac{2\varepsilon}{R^2}$$

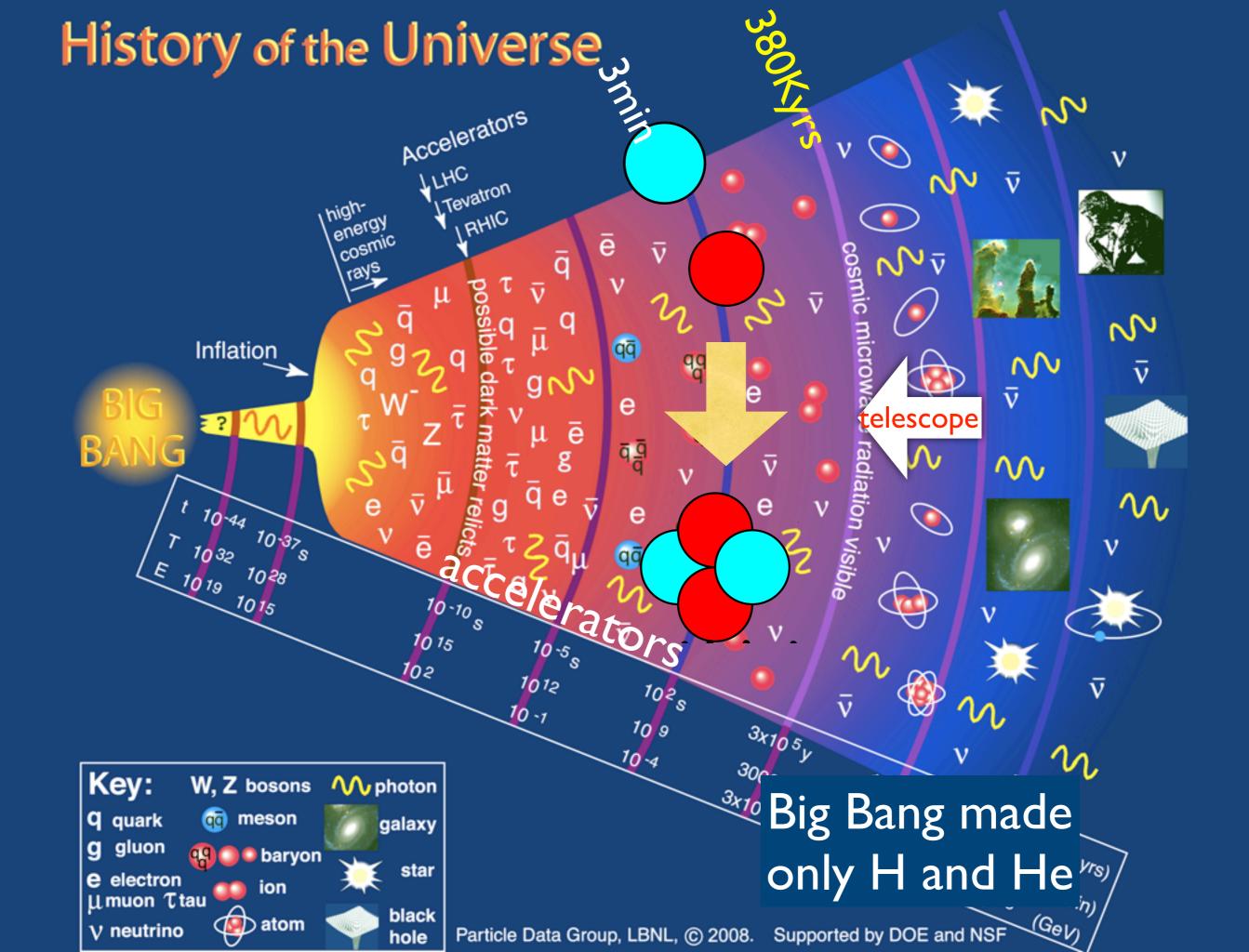
$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G\rho - \frac{k}{R^2}$$

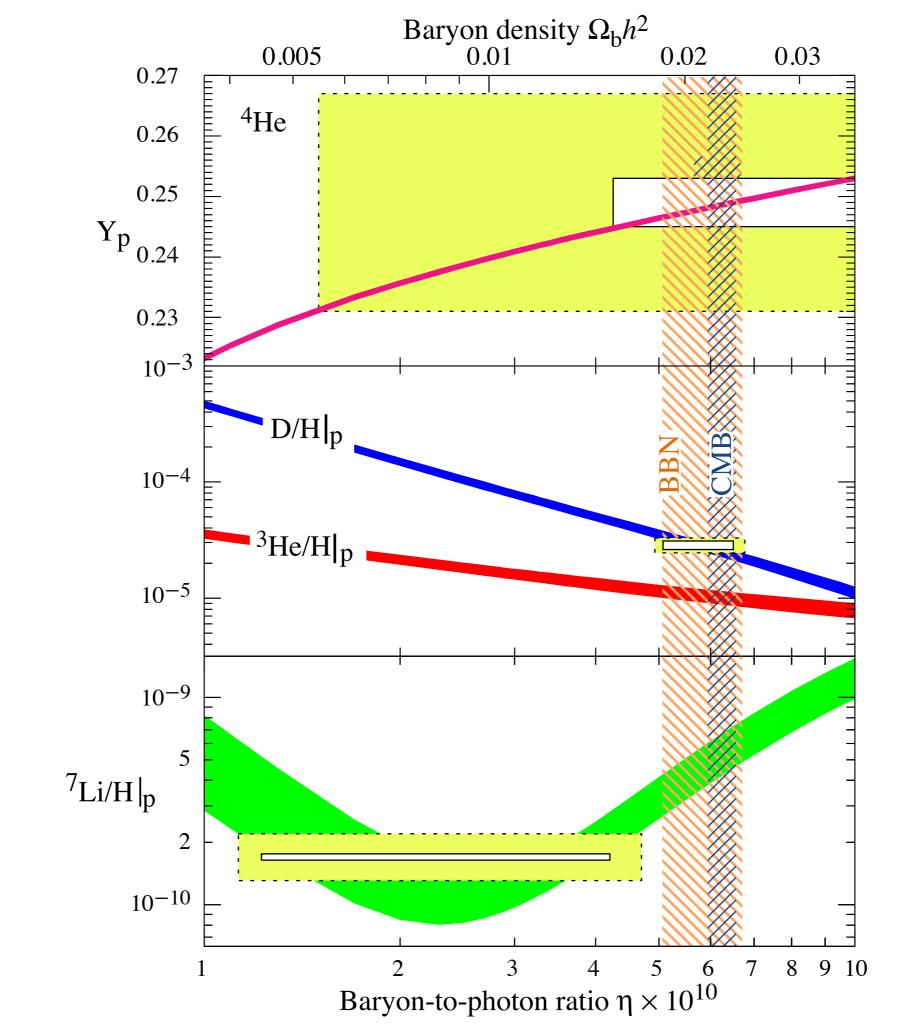
Homework

- we have at least three components
- radiation: $\rho \propto R^{-4}$
- matter: $\rho \propto R^{-3}$
- vacuum energy: $\rho \propto R^0$
- it appears k=0
- current value: H_0
- Solve this differential equation with Planck data to compute the age of the Universe

$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G\rho - \frac{k}{R^2}$$







PDG

deuterium abundance Kirkman, Tytler, Suzuki, O'Meara, Lubin

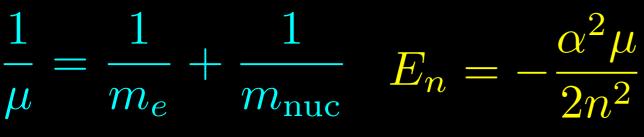
 $Å^{1}$)

cm⁻² ,

sec⁻¹

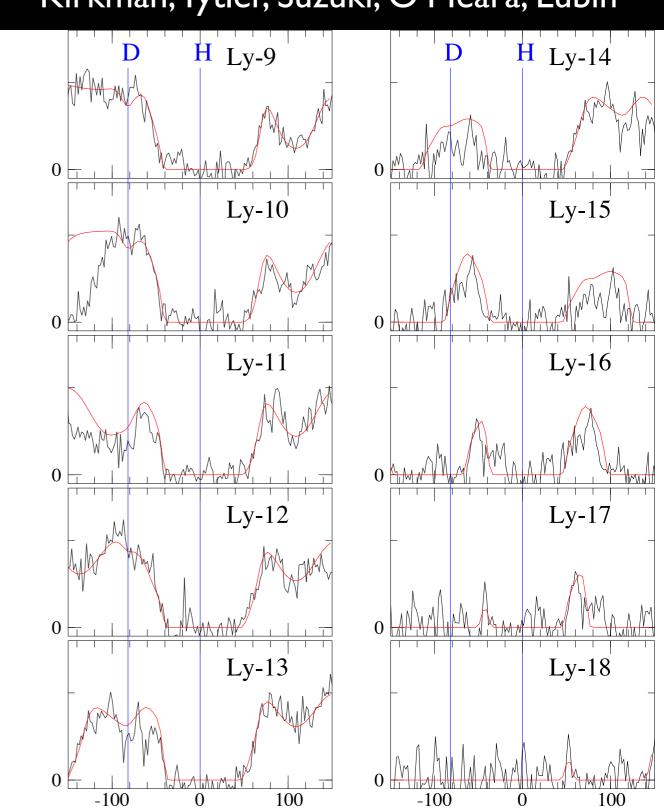
 $\times 10^{-16}$ (ergs

ц



- believed to be the most accurate, most primordial
- hydrogen backlit by quasar, Lyman absorption lines
- reduced mass different by I/4000 between H and D H gas

QSO



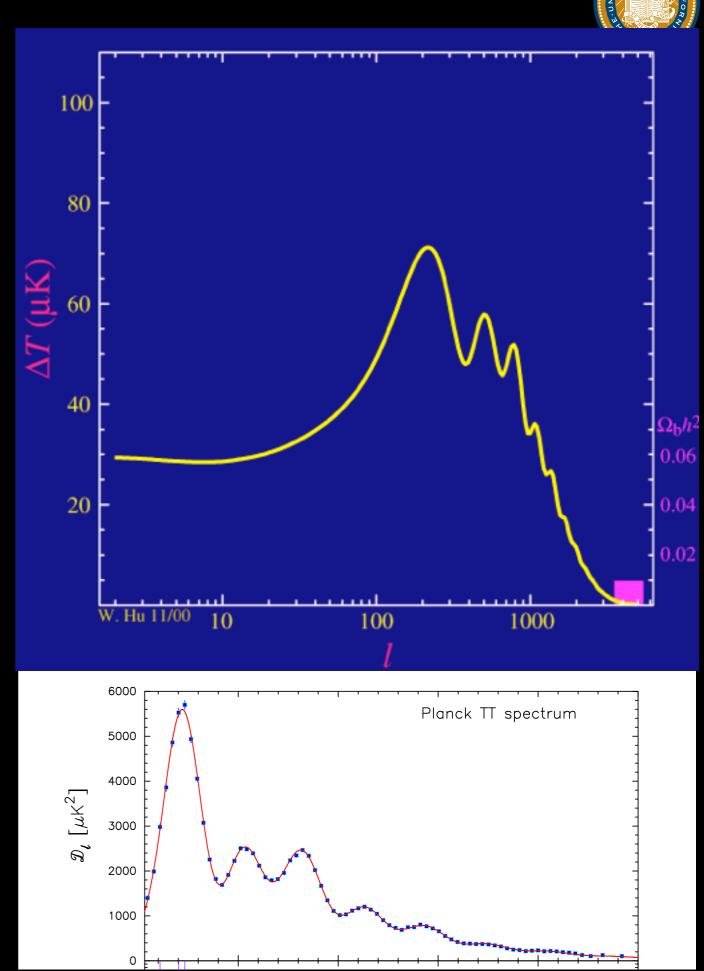
Velocity (km se \bar{c}^1)

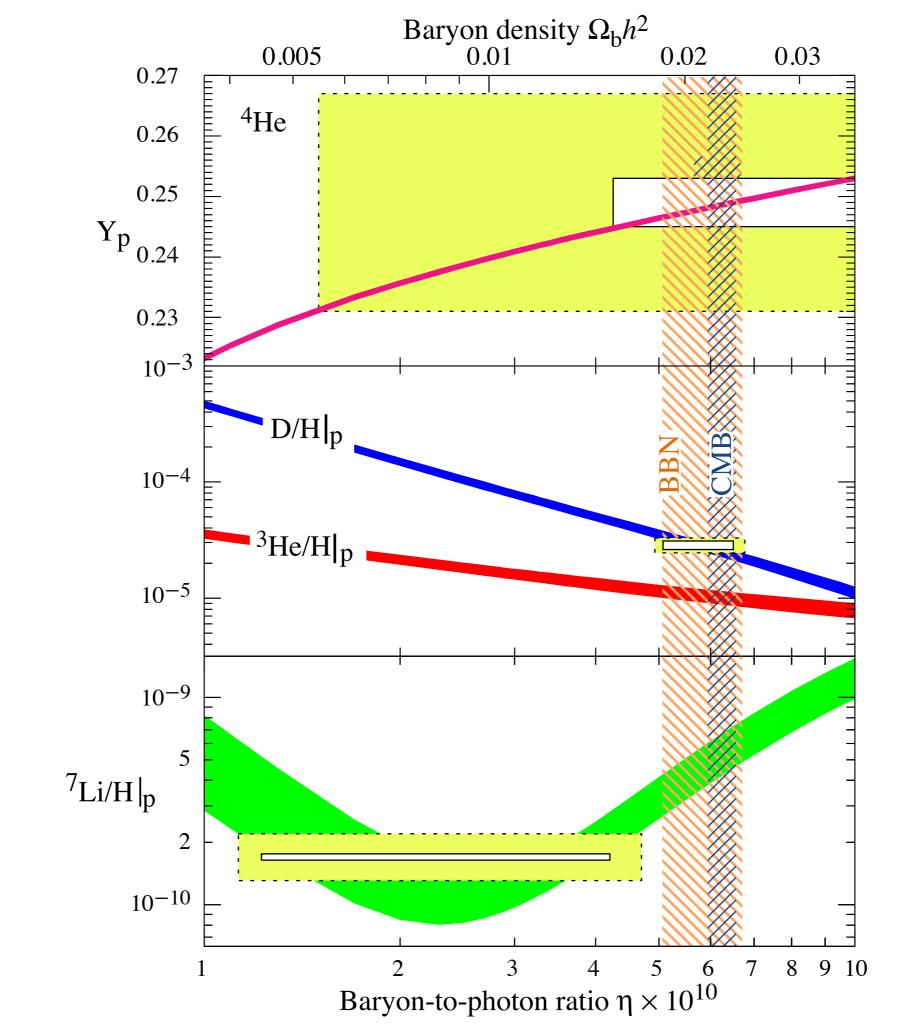


CMB

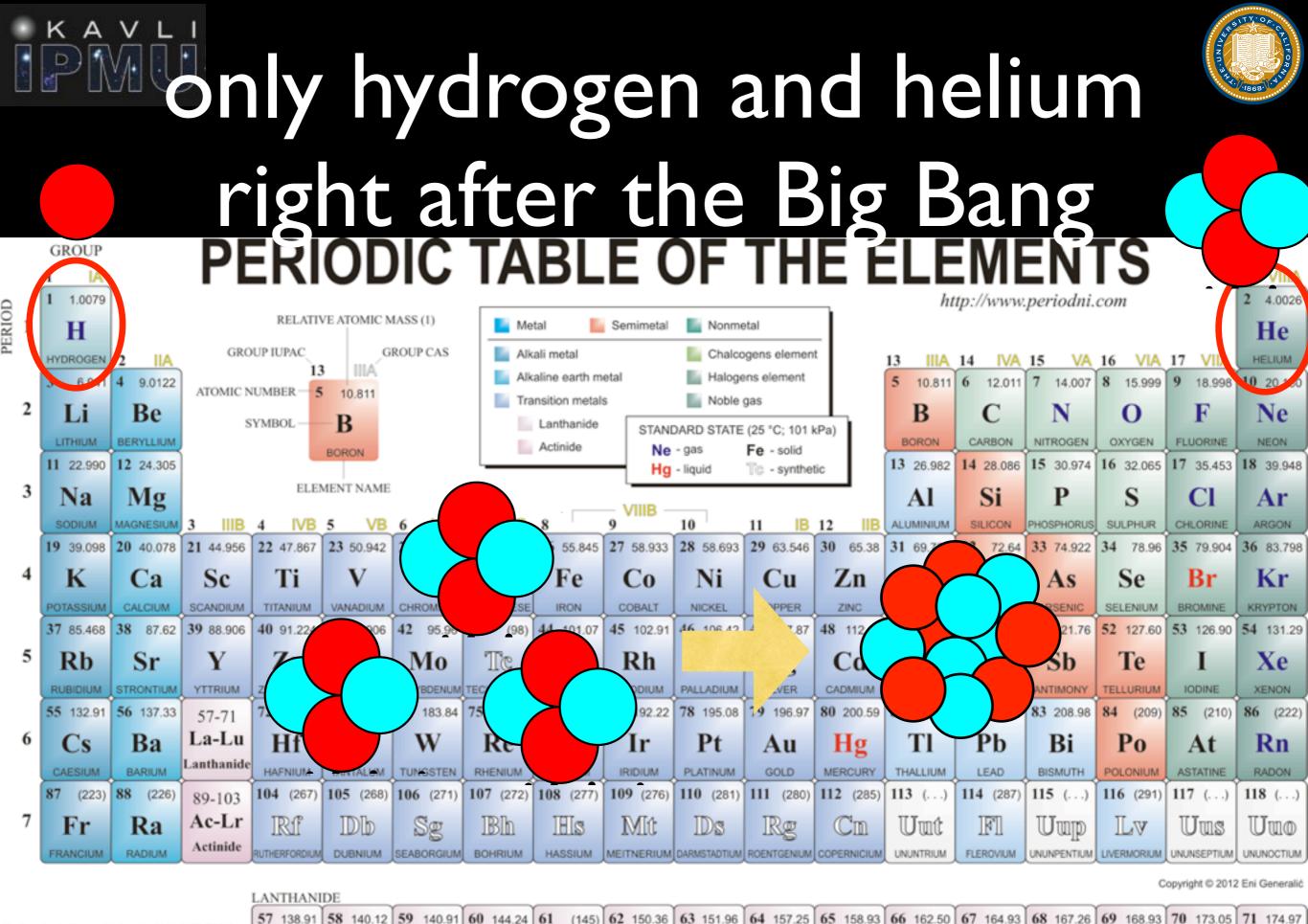
- acoustic peaks in the CMB anisotropy power spectrum are due to the sound waves (oscillations) in photonbaryon fluid at T~3000K
- amount of baryon particularly affects the ratio of even and odd peaks

$\Omega_b h^2 = 0.02207 \pm 0.00033$





PDG



(1)	Pure Appl. Chem., 81, No. 11, 2131-2156 (2009)					
	Relative	atomic	masses	are	expressed	with
	five significant figures. For elements that have					
	no stabl	e nuclia	des the	val	ue enclose	d in

La

Ce

Pr

Nd

IPm

Sm

Eu

Gd

Tb

Dv

Ho

HOLMIUM

Er

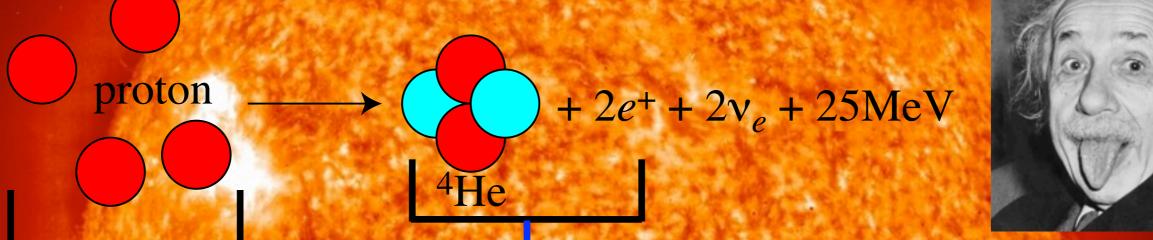
Tm

Yb

EDBILIN THUR VITEDBILIN LUTETILIN

Lu

Why does the Sun shine?





the Sun is getting lighter by 4 million tons every second

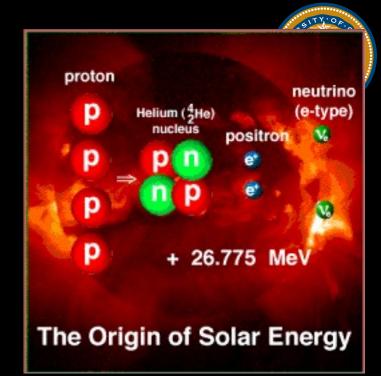
a hundred trillion neutrinos go through our body every second

Super-Kamiokande



evidence

burning atoms in the Sun produces neutrinos trillions through our body every second

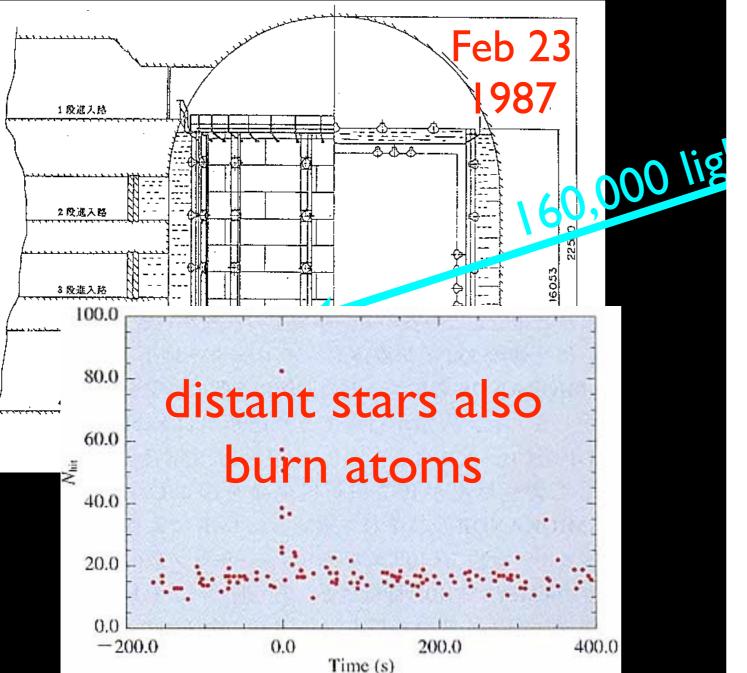


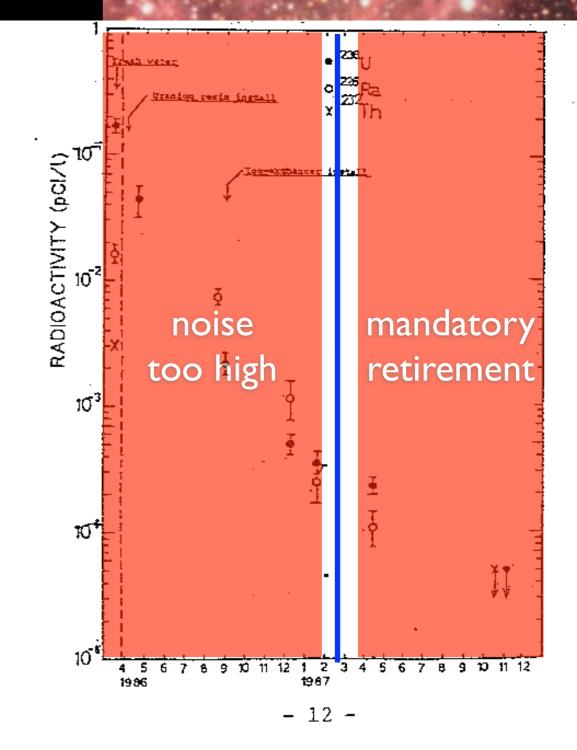


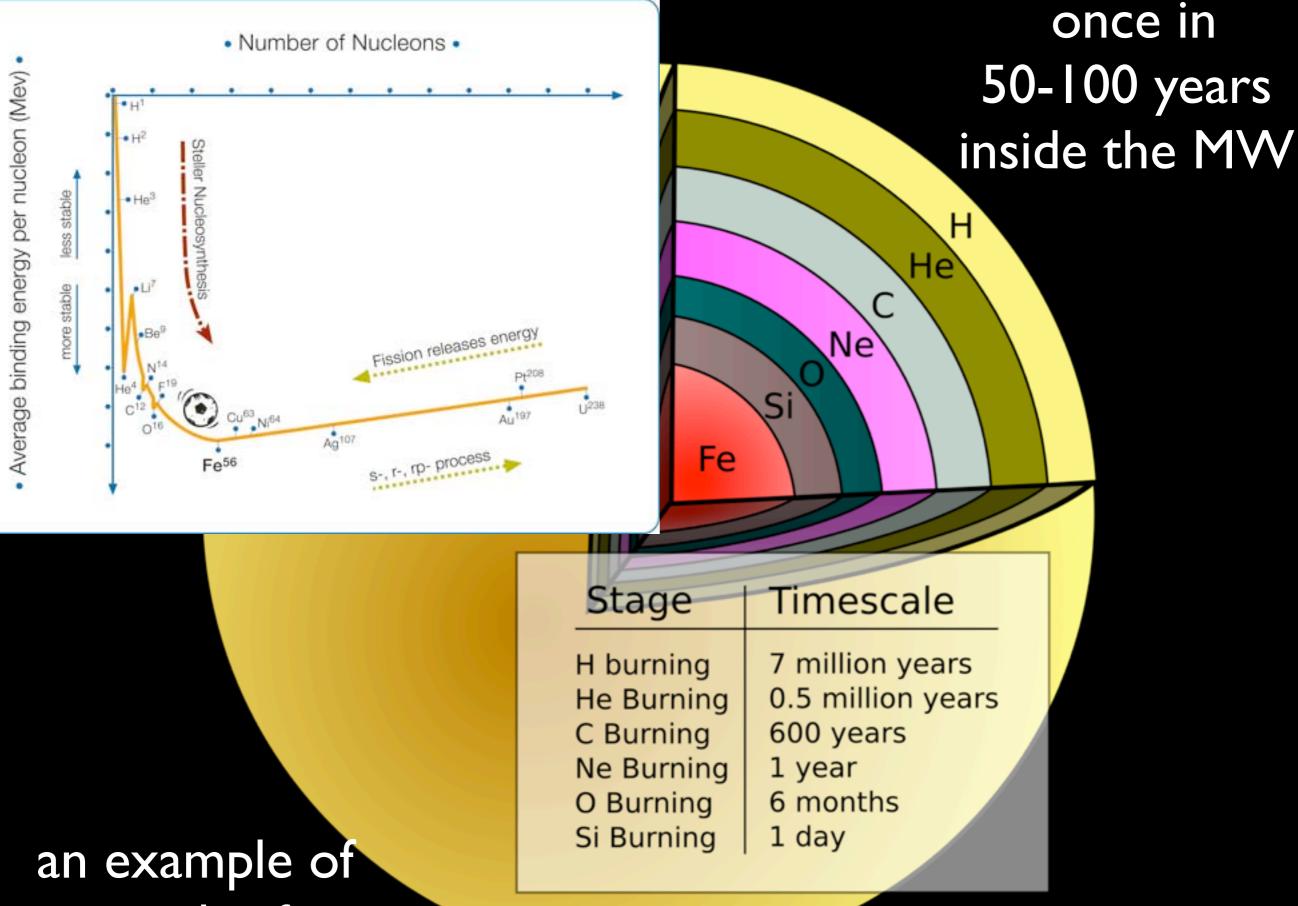
in pitch darkness 1000m underground



Fremendous luck







an example of time scales for a quite massive star hydrogen helium

carbon nitrogen oxygen iron

We are star dust

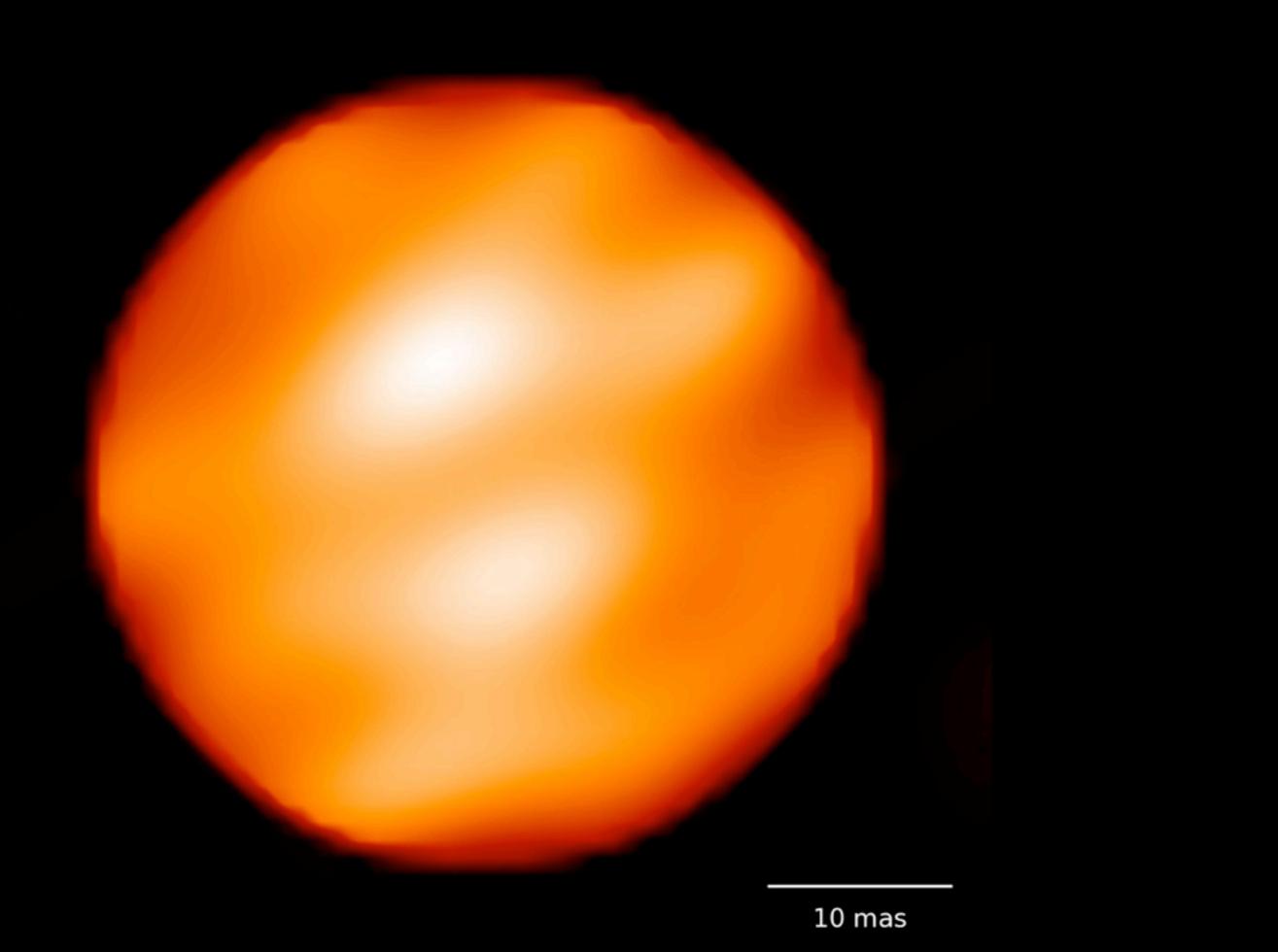
E CIROS

© Anglo-Australi



Betelgeuse 20M⊙

Constellation Orion



PROTOSTAR BLUE SUPERGIANT

PROTOSTAR BLUE SUPERGIANT

BLUE SUPERGIANT PROTOSTAR

PROTOSTAR BLUE SUPERGIANT

SUN-LIKE STAR PROTOSTAR

PROTOSTAR RED DWARF

BROWN

DWARF

PROTOSTAR

PAIR-INSTABILITY

BLACK HOLE

TYPE II SUPERNOVA

BLUE GIANT

RED GIANT TYPE II SUPERNOVA

RED GIANT

PLANETARY NEBULA

BROWN DWARF

NURSERY

STELLAR

SUPERSHELL

NEUTRON STAR

TYPE IA SUPERNOVA

WHITE DWARF

WHITE DWARF

RED DWARF

BLACK HOLE

hydrogen helium

carbon nitrogen oxygen iron

We are star dust

E CINOS

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