



Beyond the Standard Model

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Invisibles School, June 17, 2015



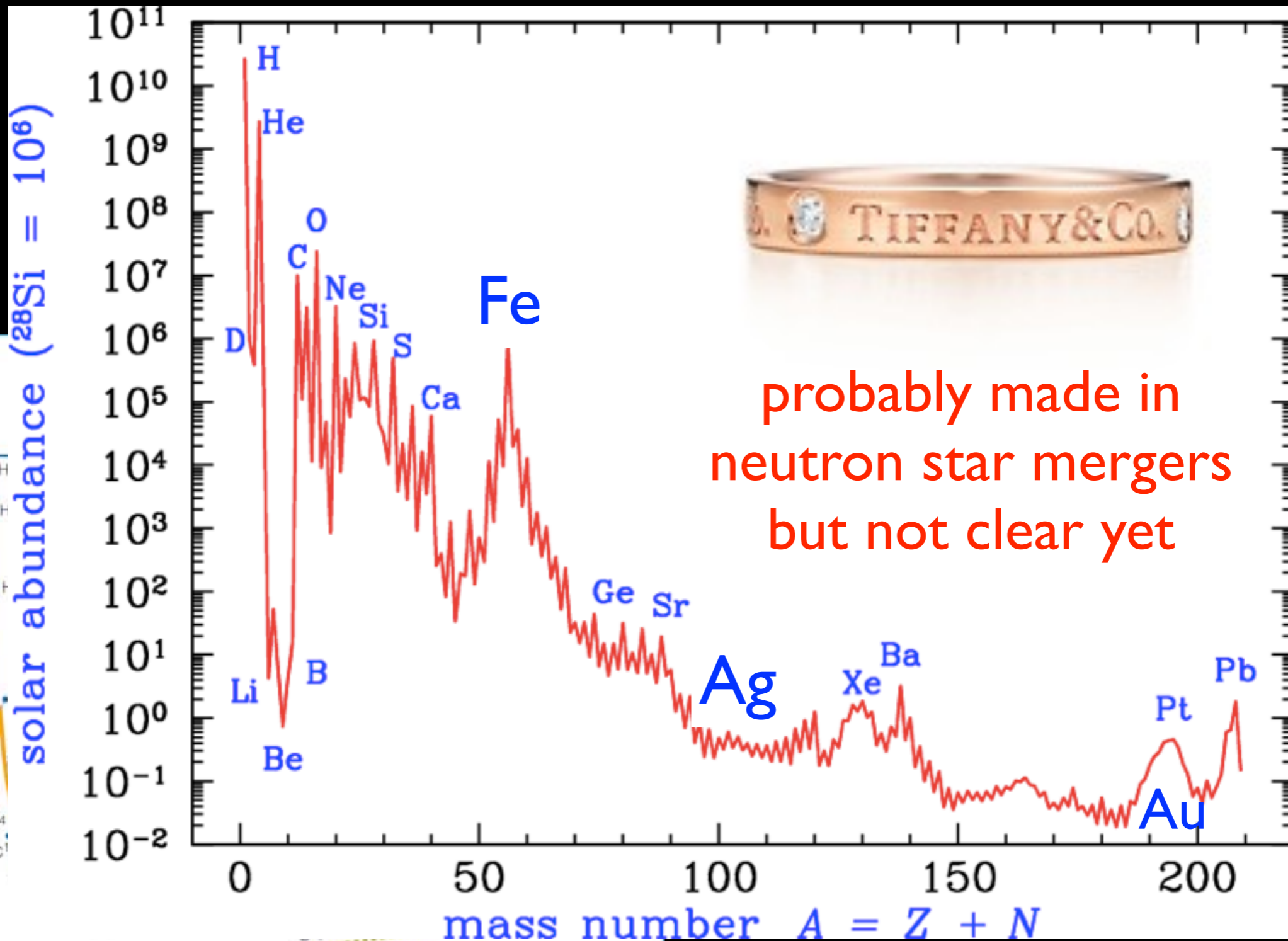
hydrogen
helium

carbon
nitrogen
oxygen
iron

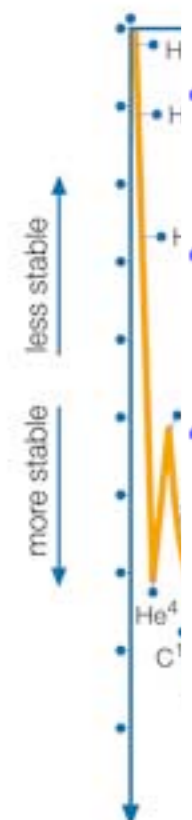


We are star dust

but only up to iron



Average binding energy per nucleon (MeV)

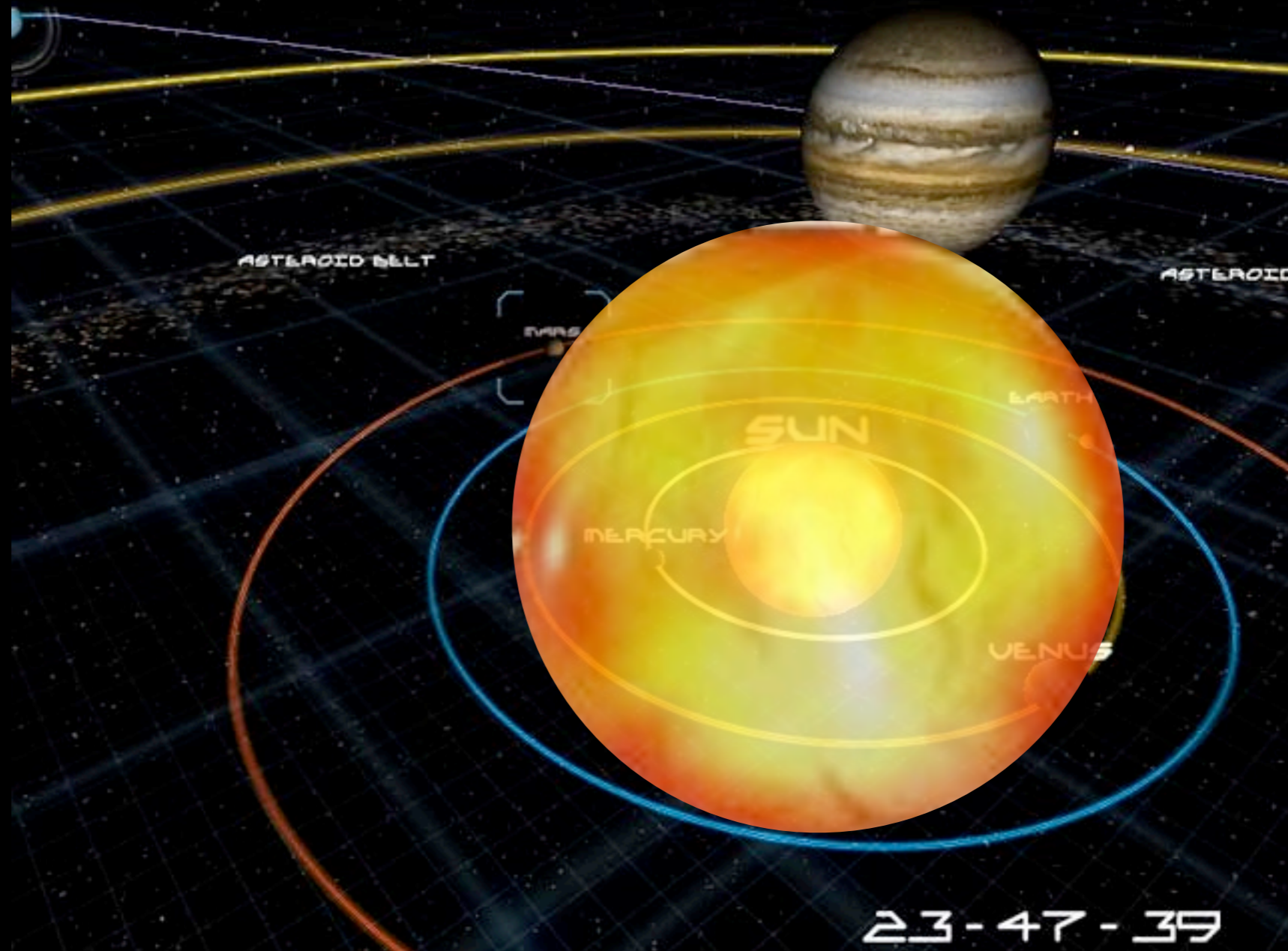


solar abundance ($^{28}\text{Si} = 10^6$)

probably made in
neutron star mergers
but not clear yet

mass number $A = Z + N$

fate of the Sun in 4.5 billion years

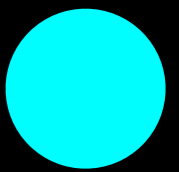
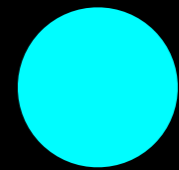
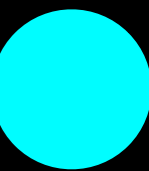
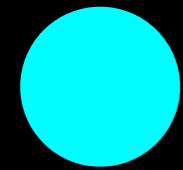
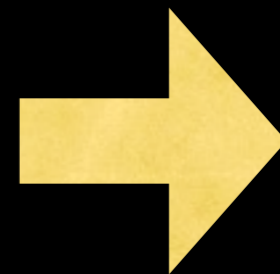
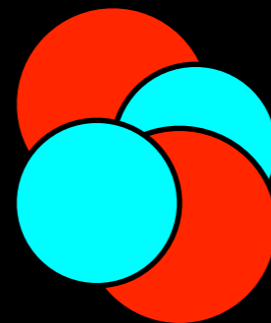
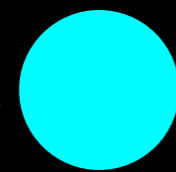
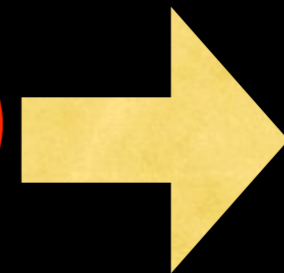
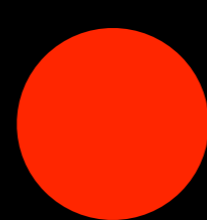
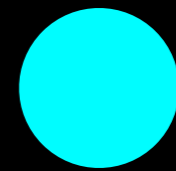
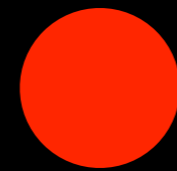




**STAR
WARS**
EPISODE II: ATTACK OF THE CLONES

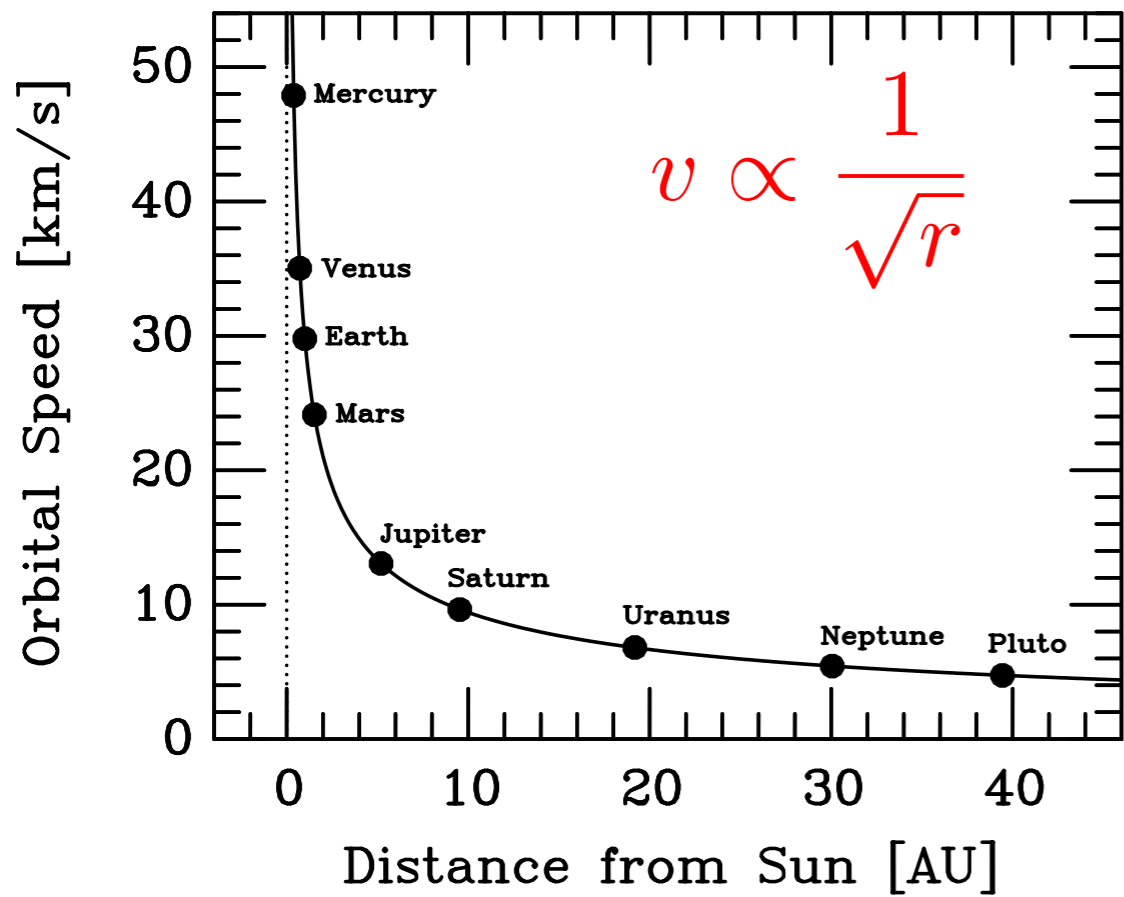
anthropic?

- protons and neutrons weigh very similar
- if v is bigger by 20, neutron is 20% heavier than proton, all neutrons decay into protons
- no nuclei possible!
- This is why $v \ll M_{PI}$? (Barr et al)

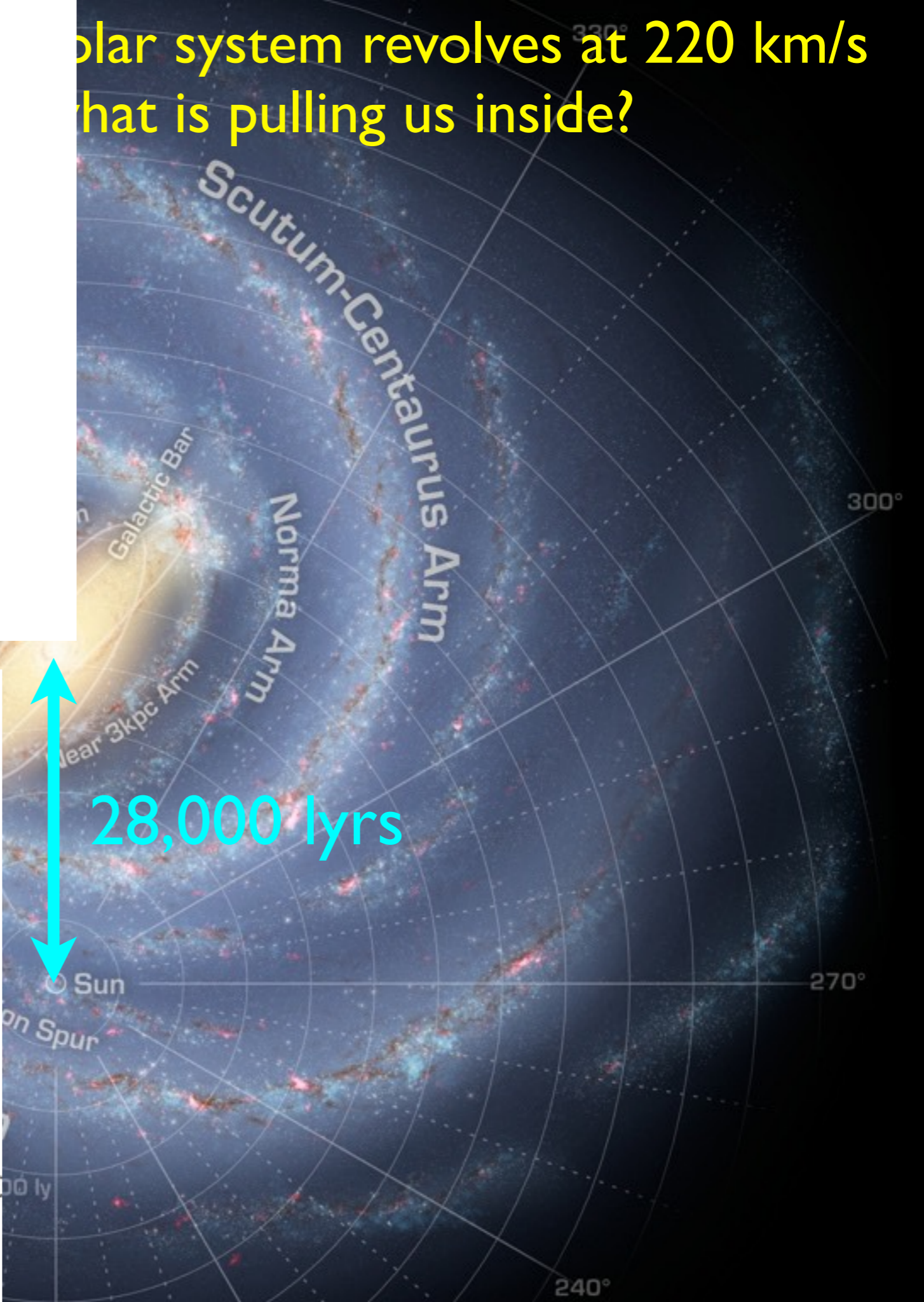
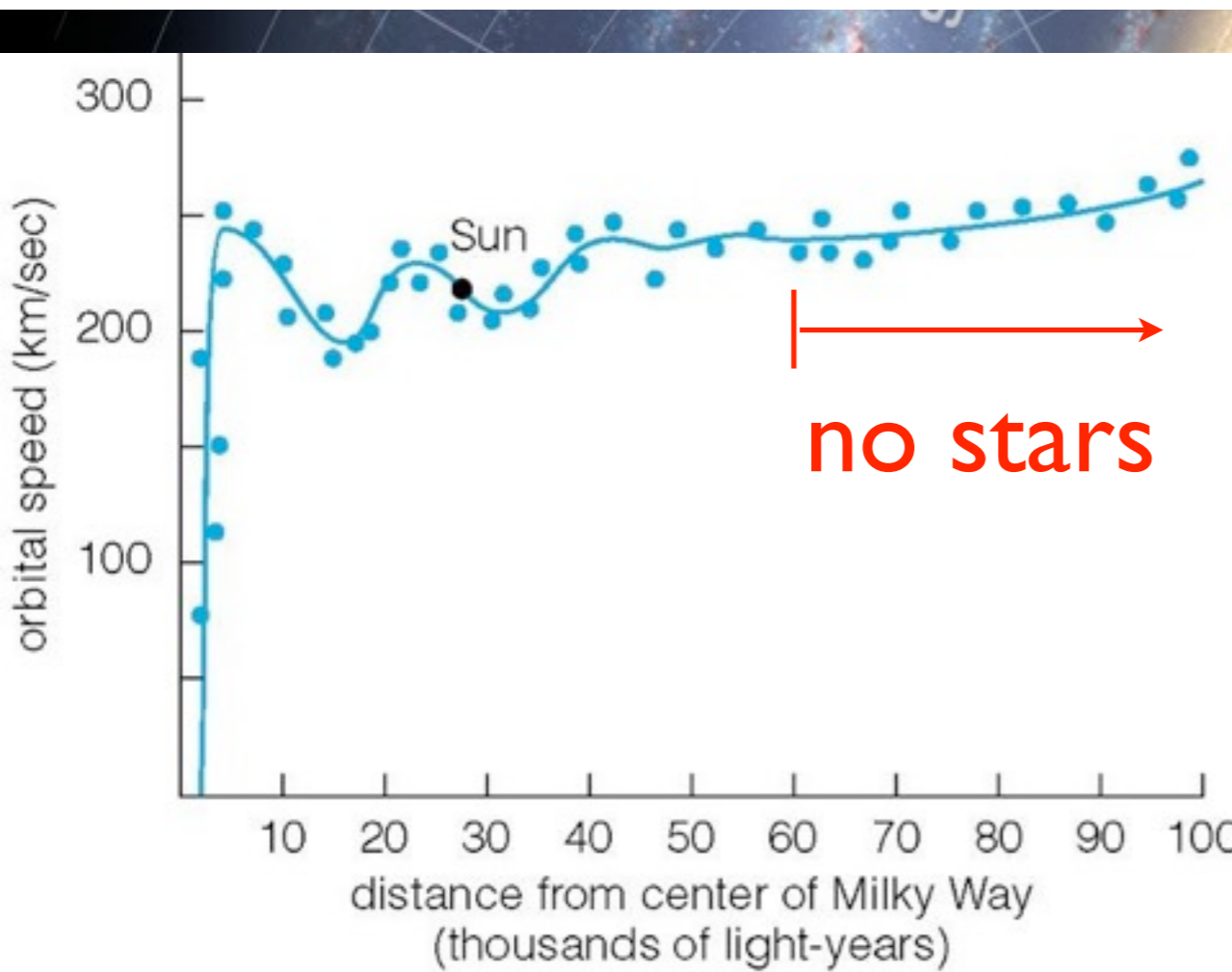


OK, atoms came from stars.
What about stars themselves?

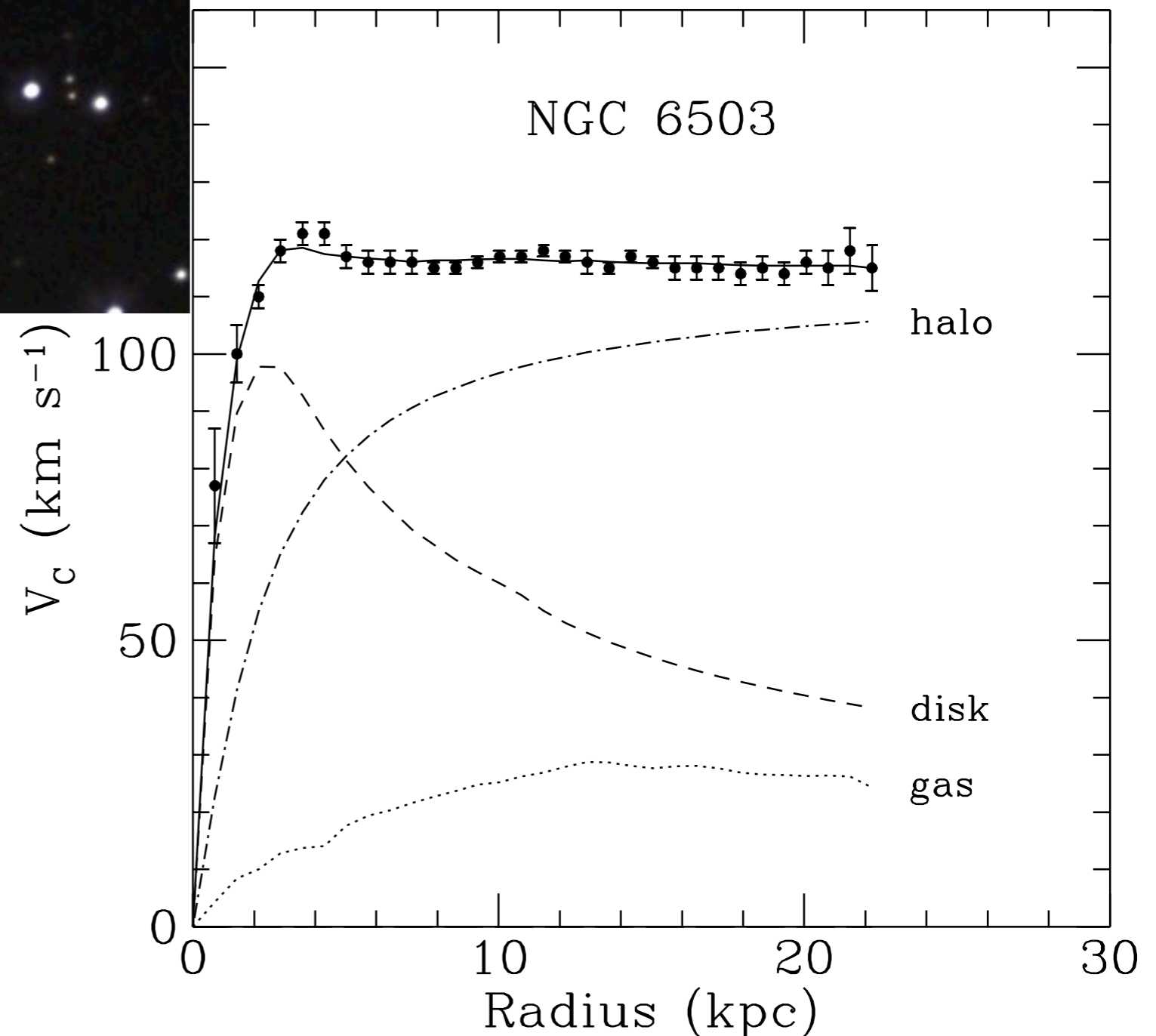
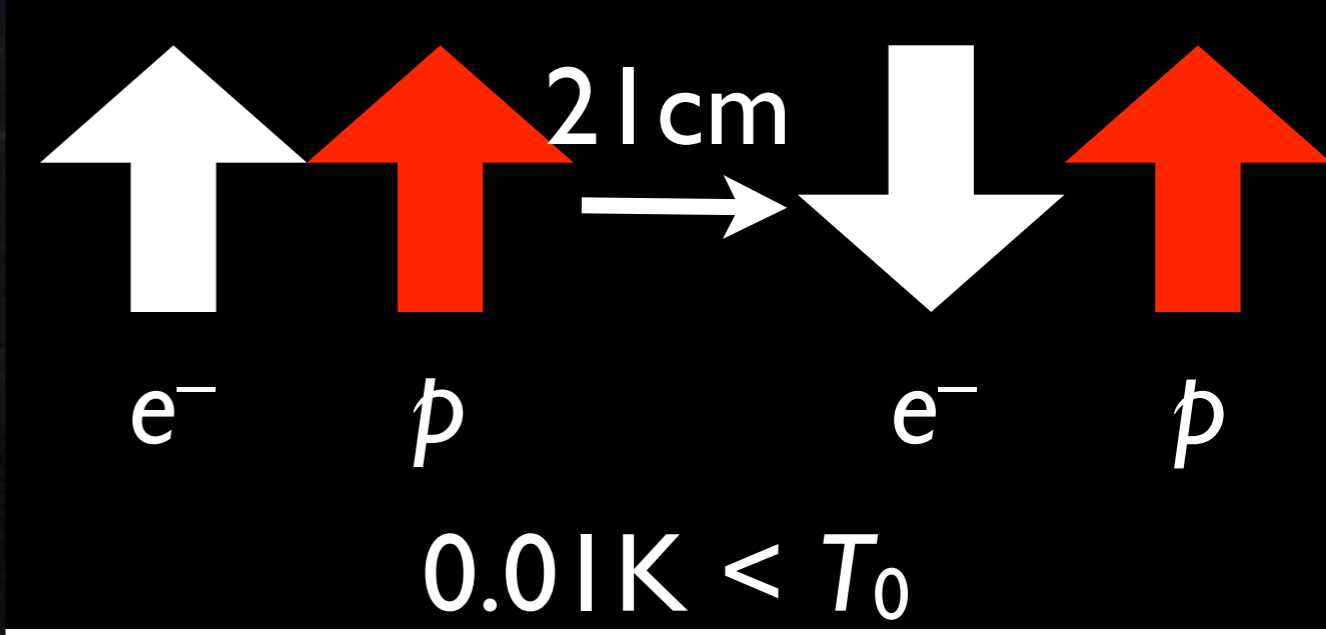
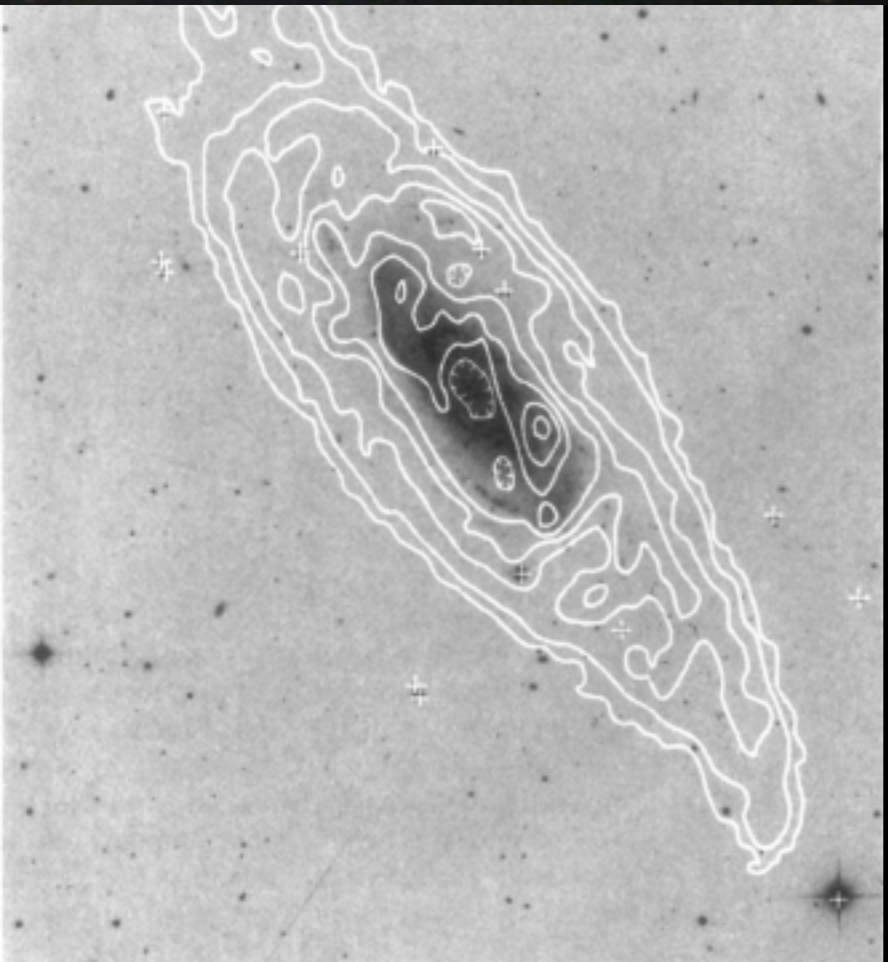
Dark Matter



Solar system revolves at 220 km/s
 what is pulling us inside?



28,000 yrs





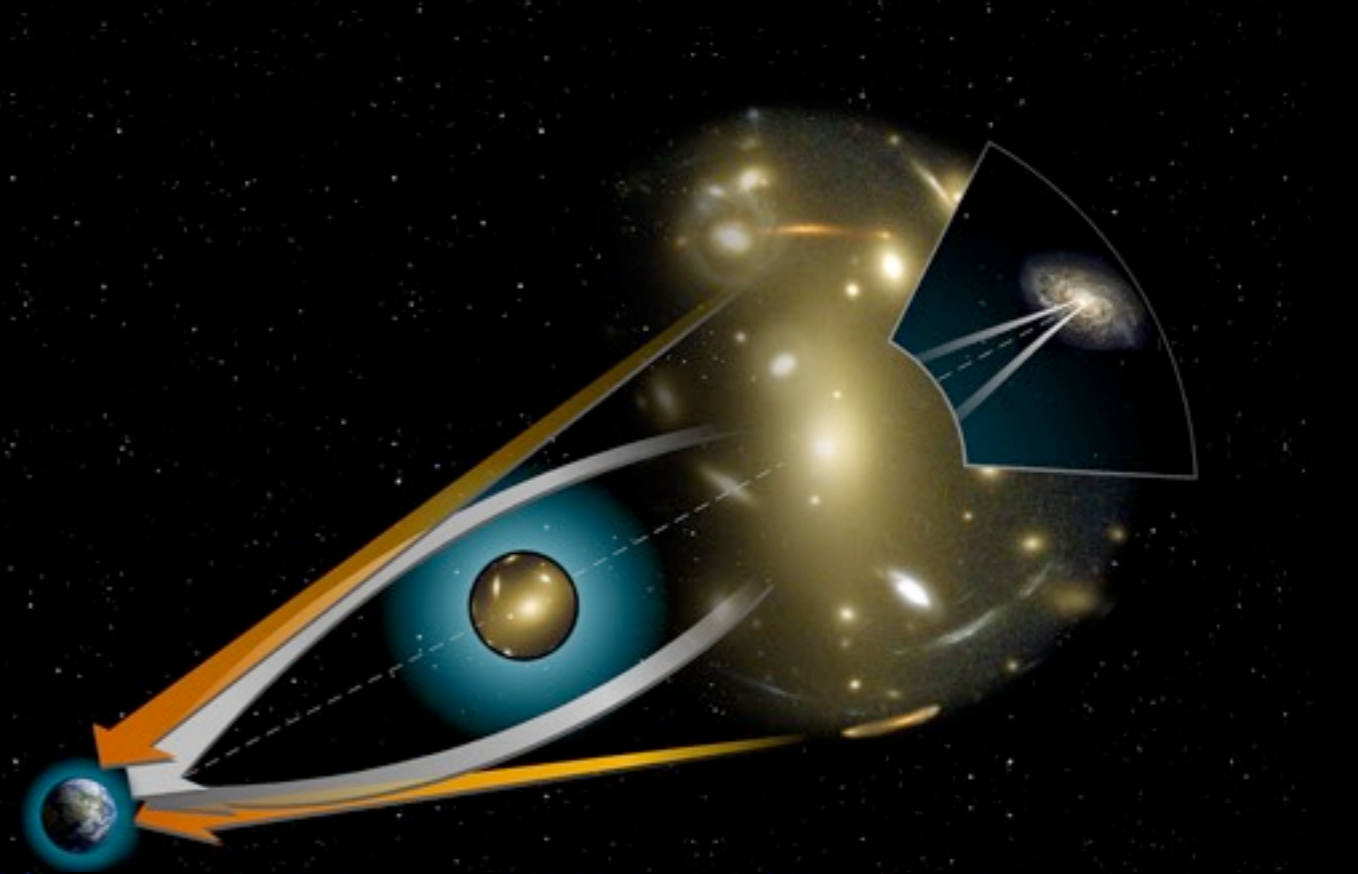
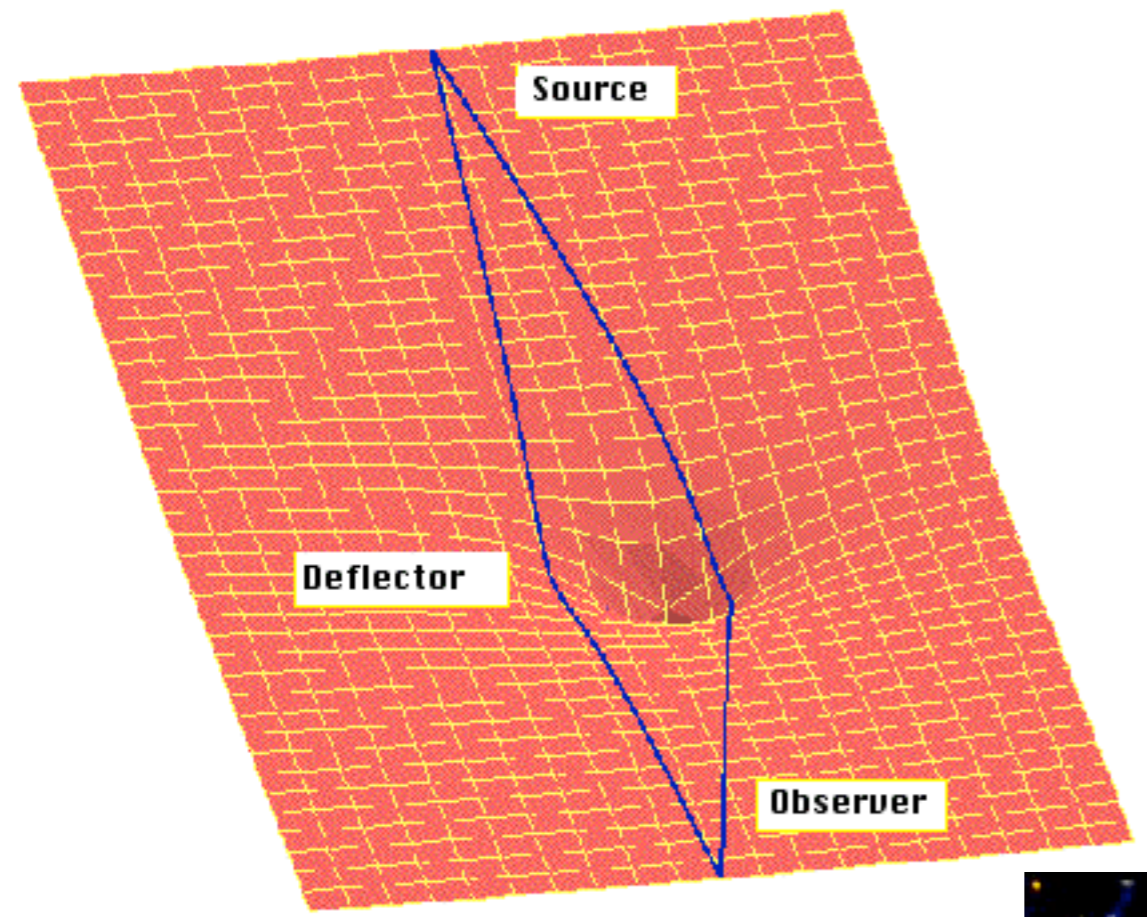
Vera
Rubin
1970's



cluster of galaxies
2.1 billion light years

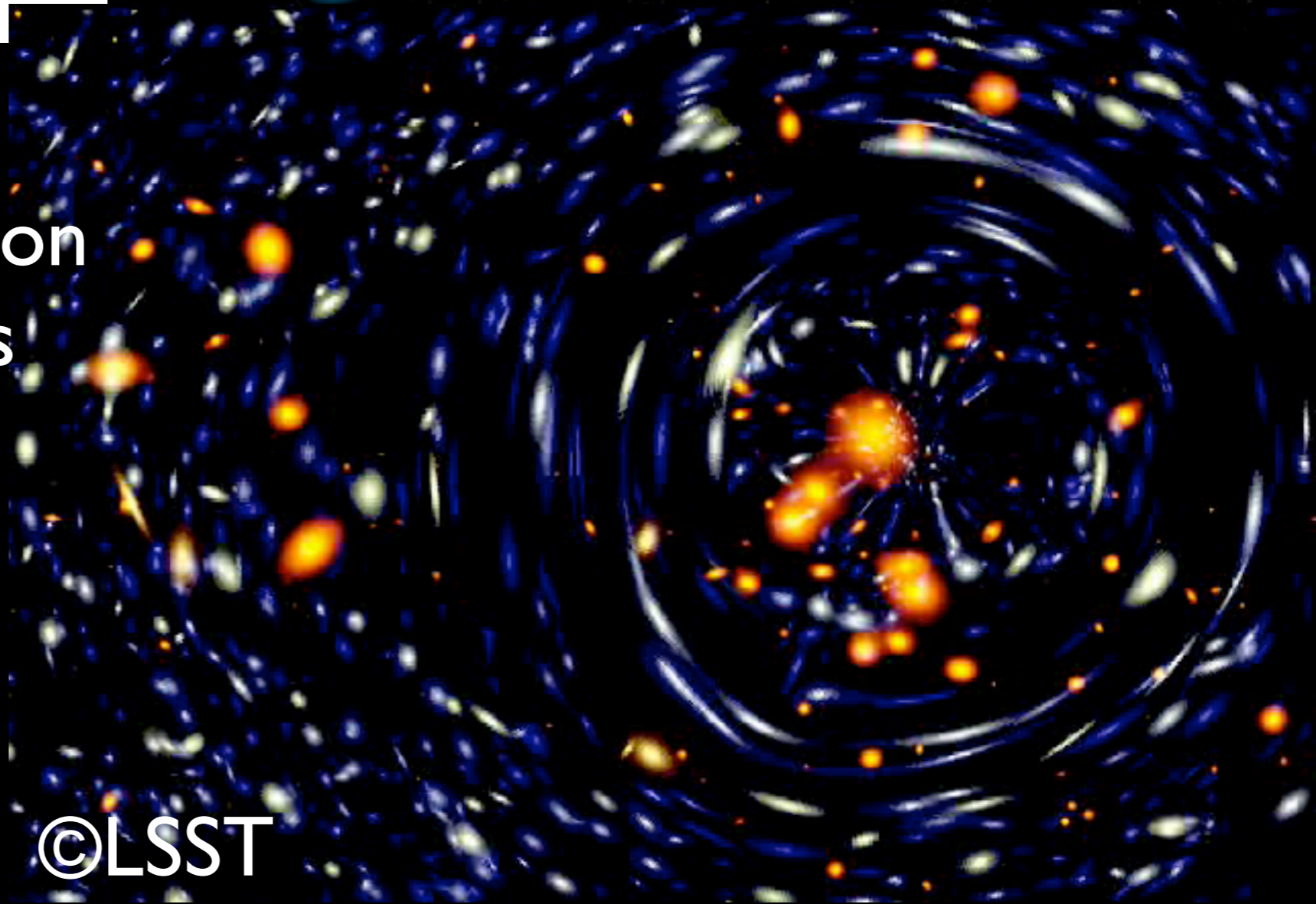
Abell 2218





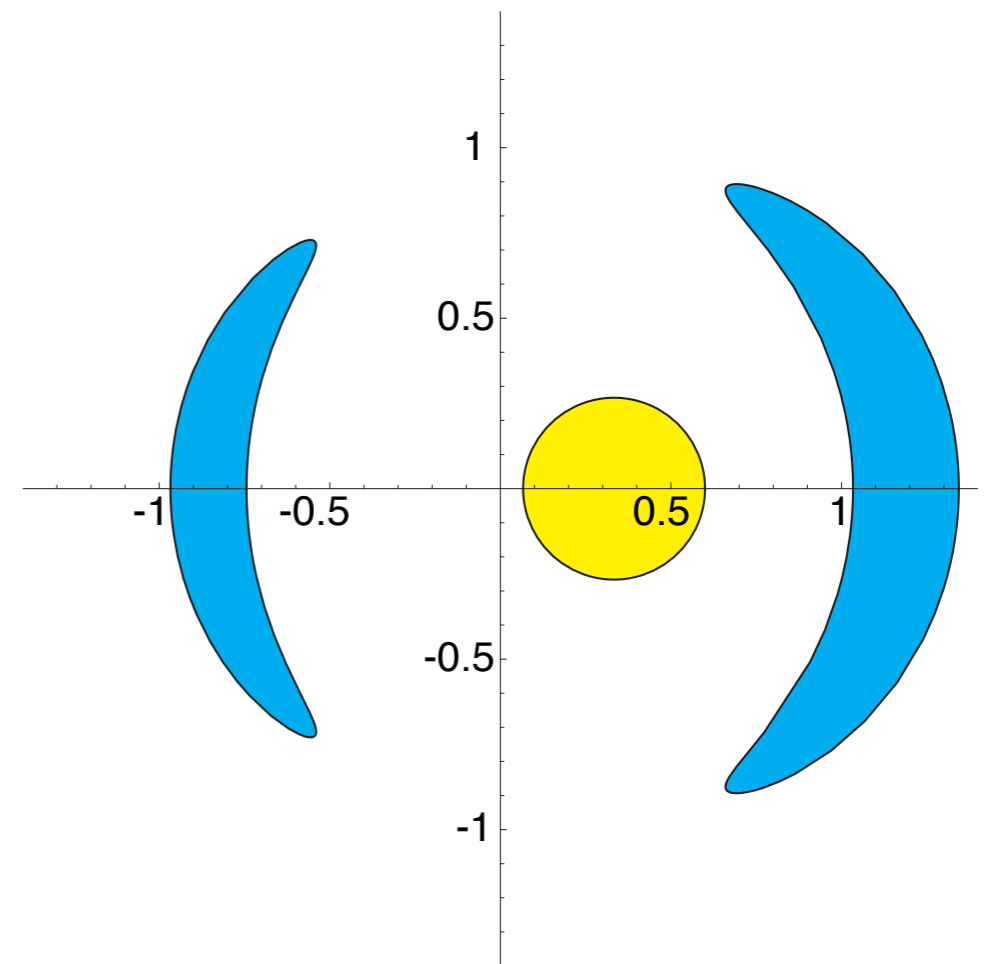
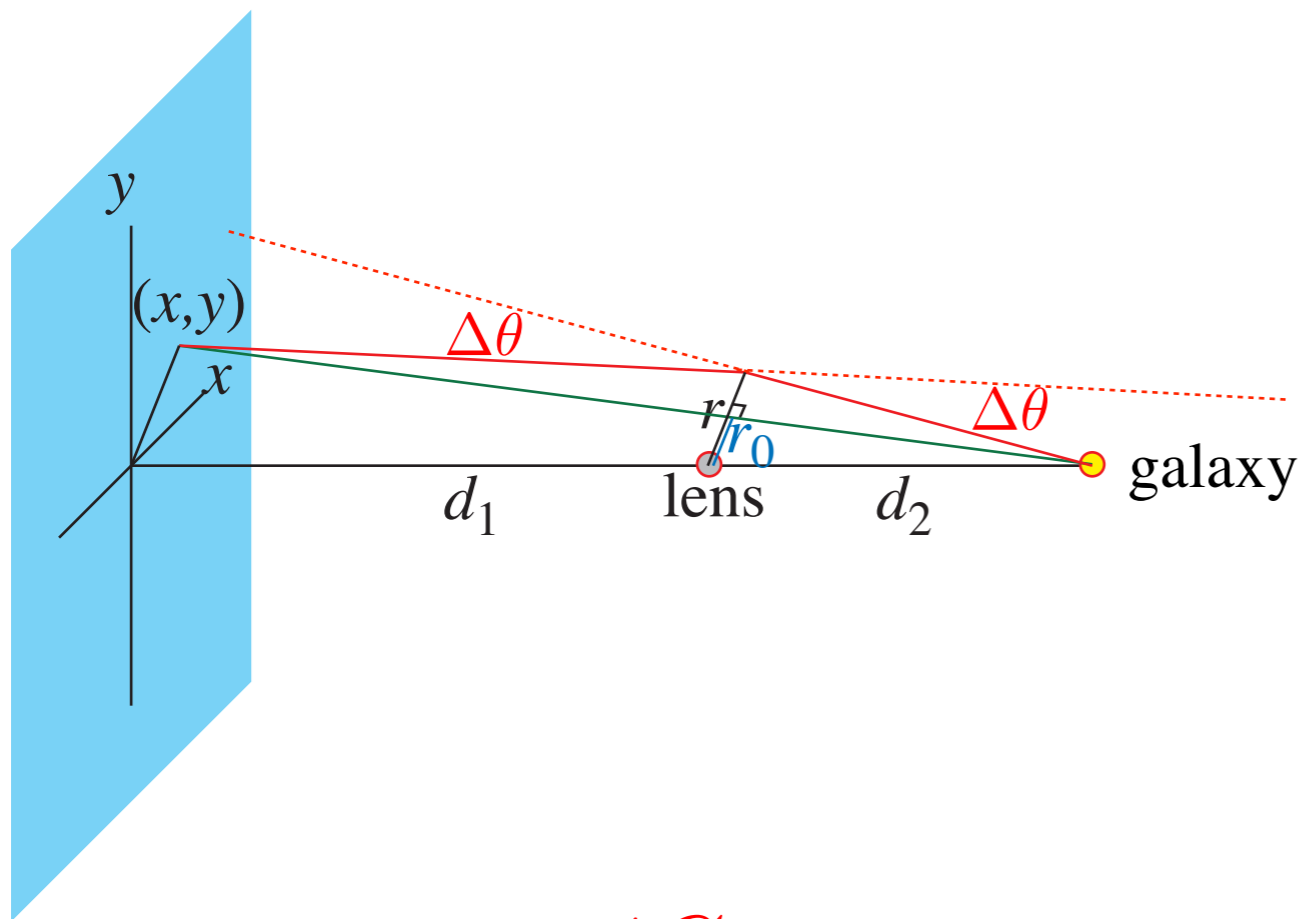
Homework
Work out the deflection
angle by a point lens

$$\Delta\theta = \frac{4G_N m}{c^2 r_c}$$

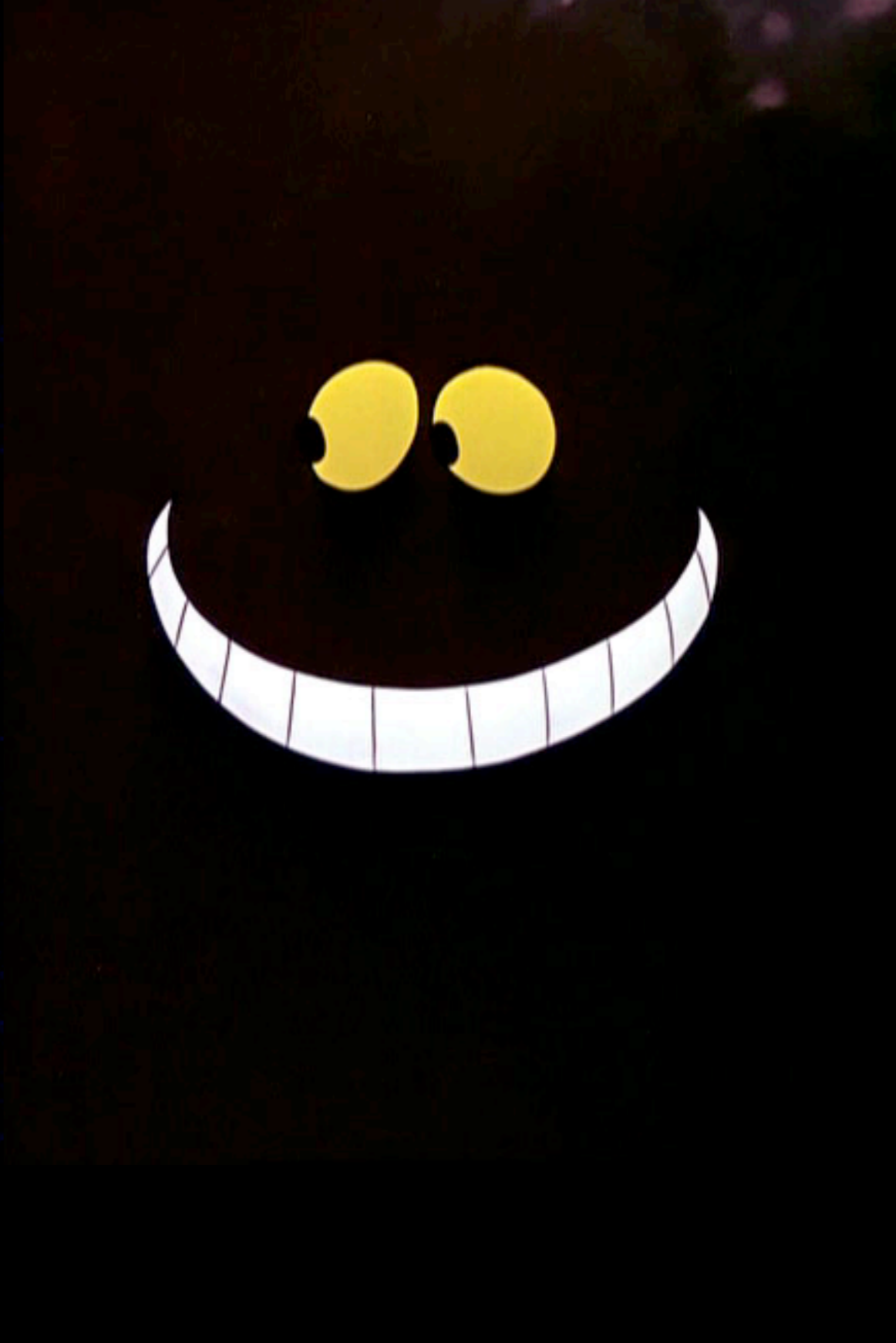


Homework

Show how images can be distorted like this

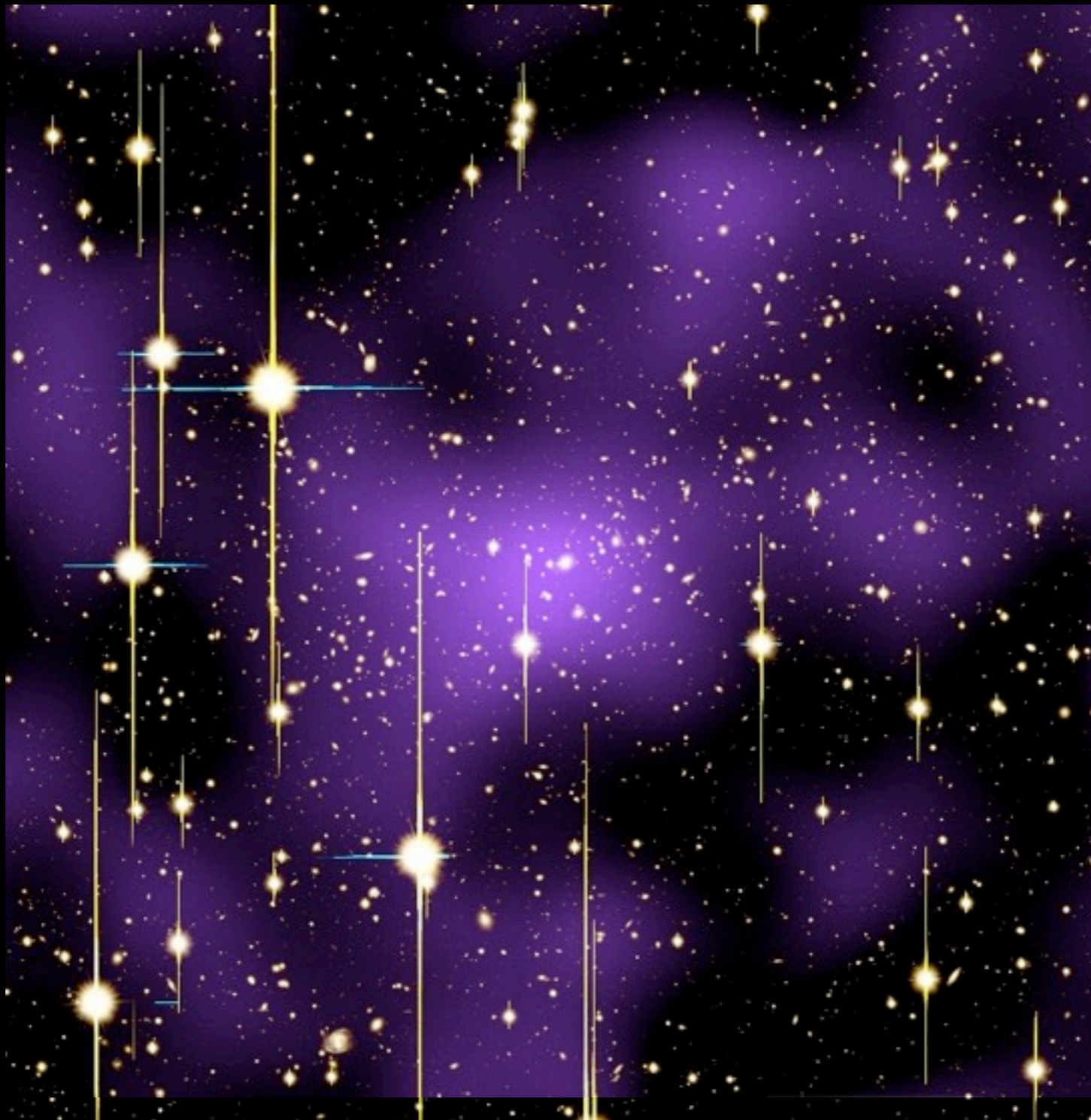


$$\Delta\theta = \frac{4G_N m}{c^2 r_c}$$



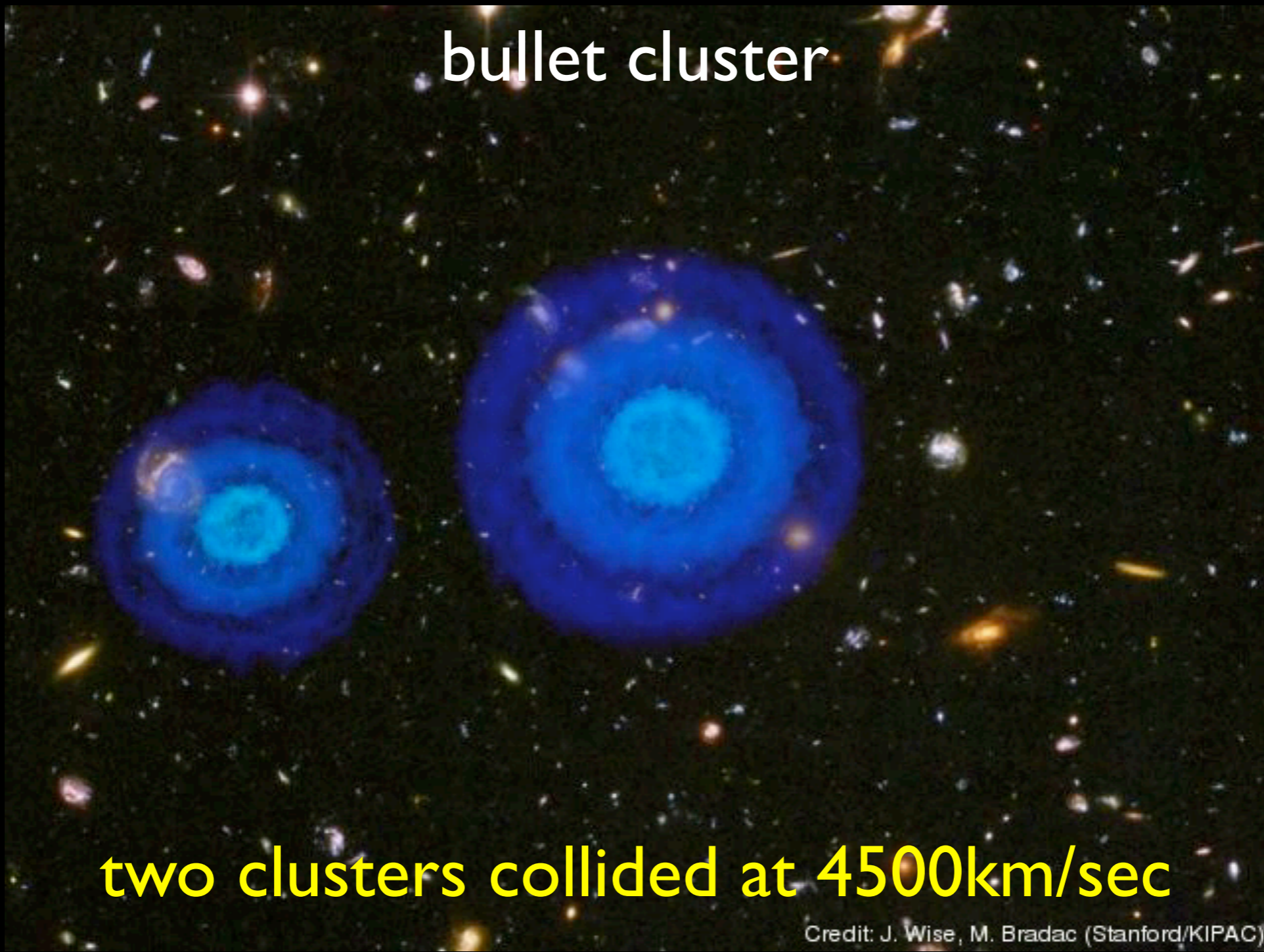
Cheshire cat

image invisible dark matter

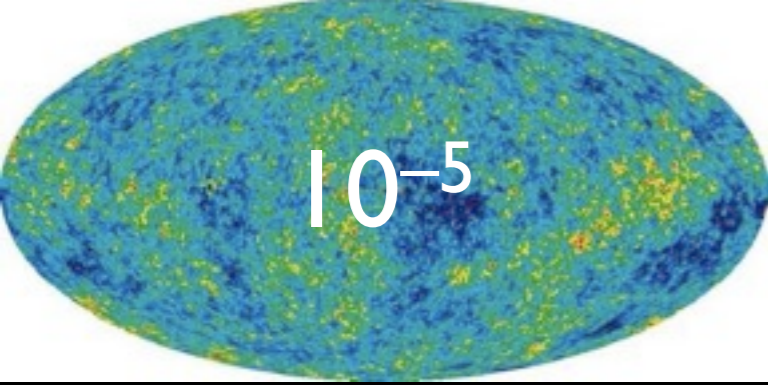


more than 80% of matter in the Universe is not atoms

$$\frac{\sigma_{\text{scatt}}}{m} \lesssim \frac{10^{-24} \text{cm}}{\text{GeV}}$$



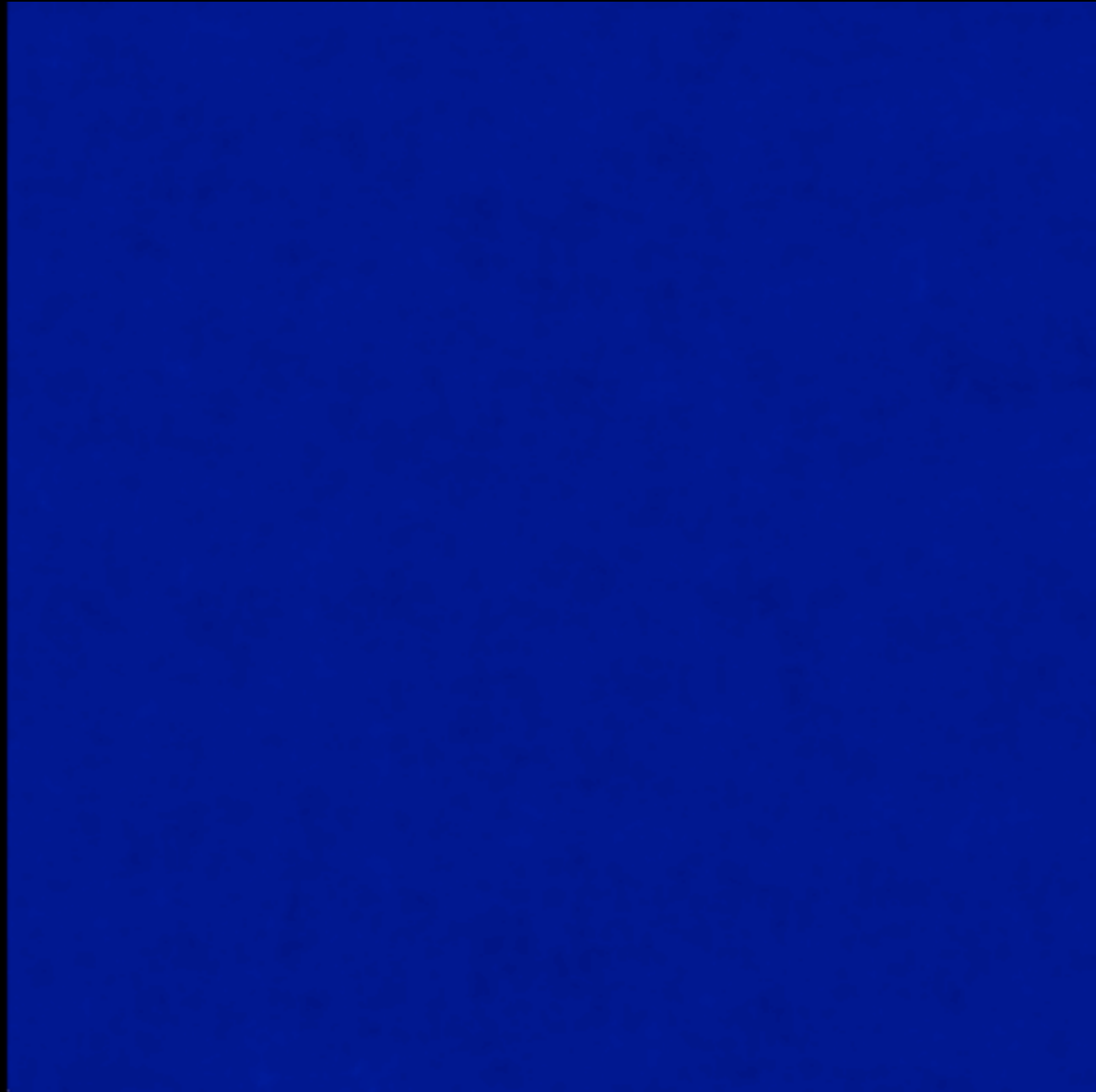
4B lyrs away



dark matter
is our mother



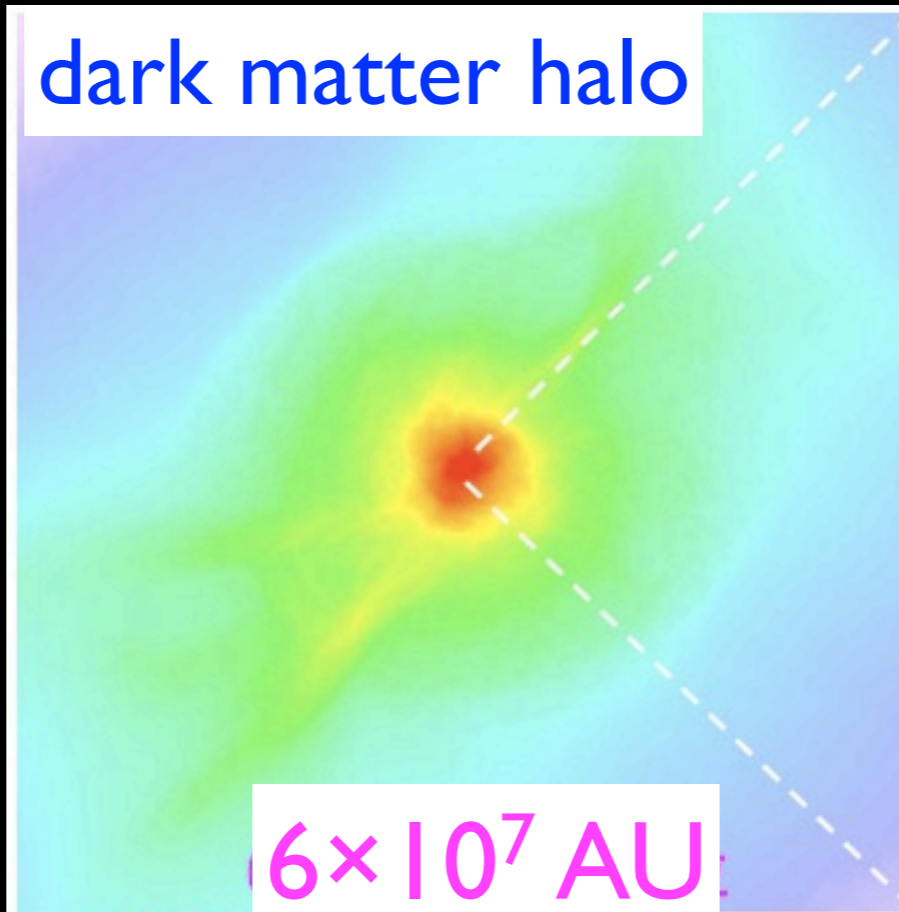
without dark matter



with dark matter

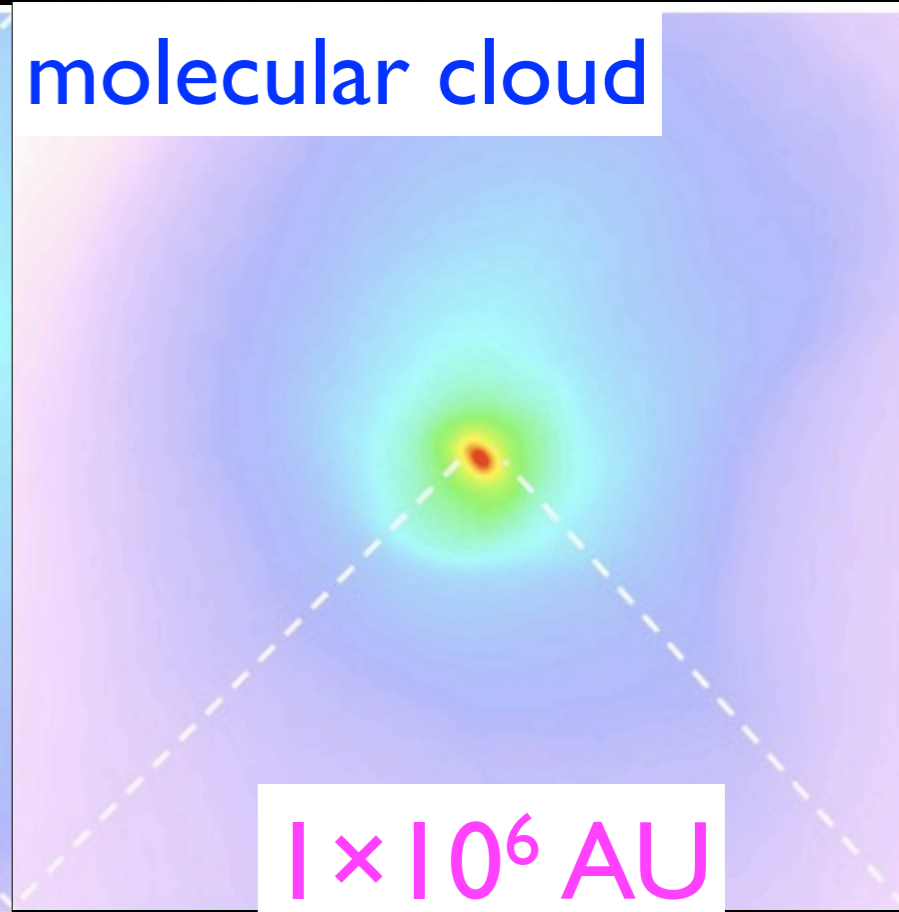
birth of a star

dark matter halo



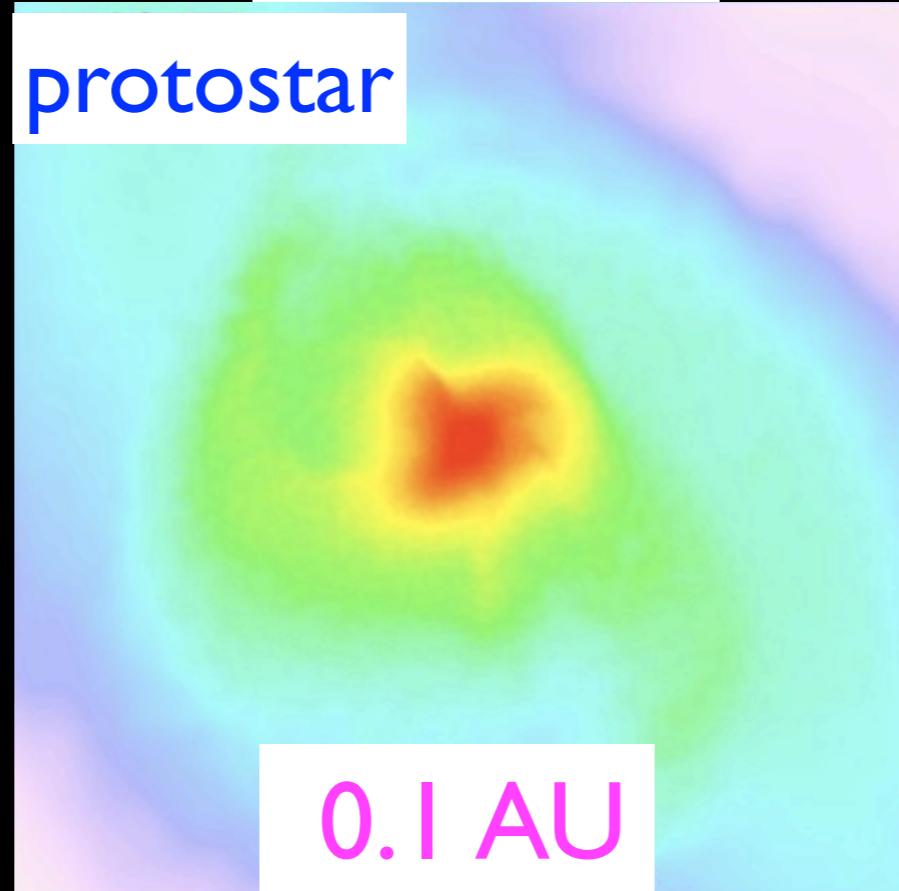
6×10^7 AU

molecular cloud



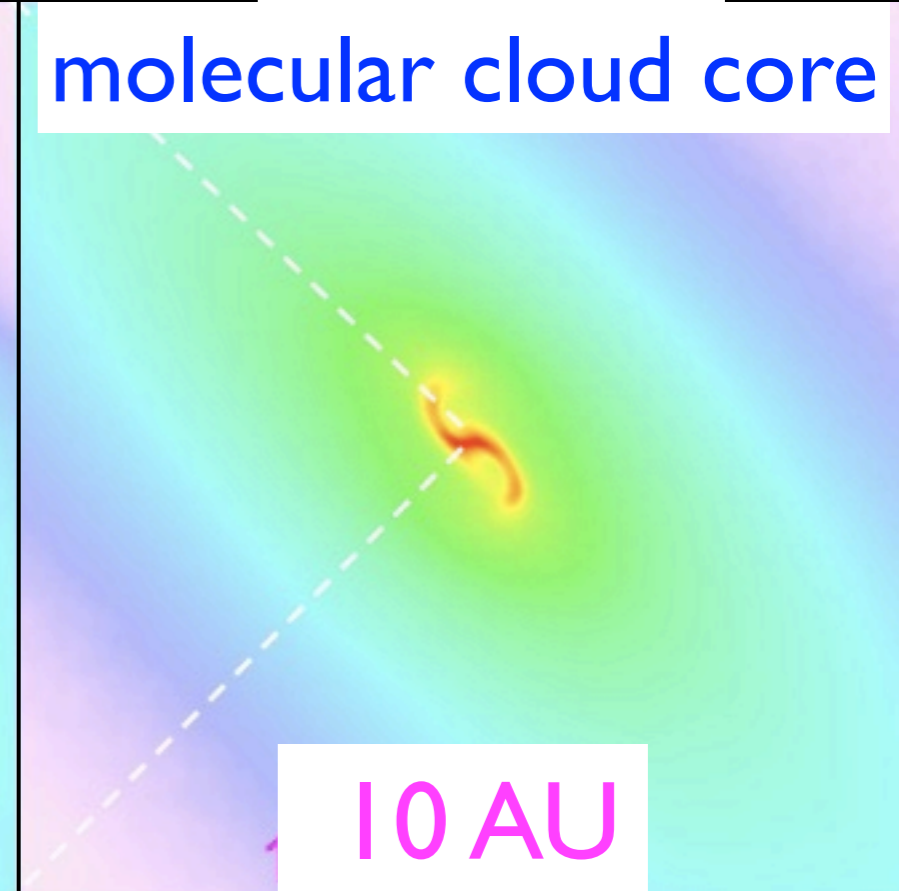
1×10^6 AU

protostar

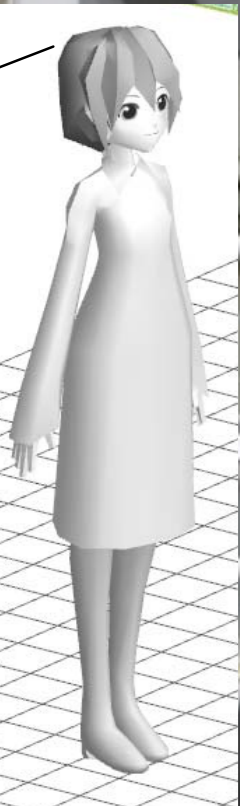
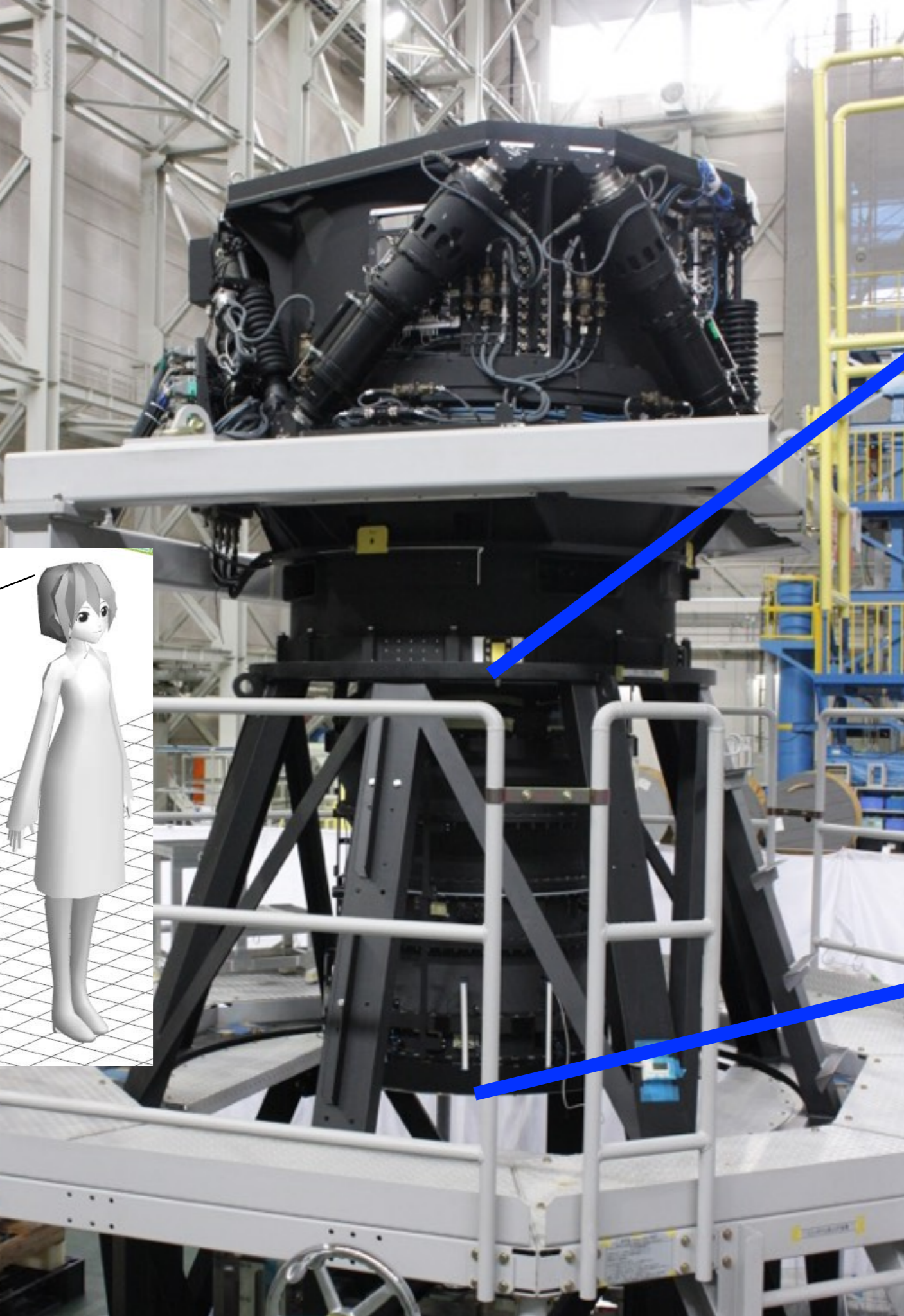


0.1 AU

molecular cloud core



10 AU



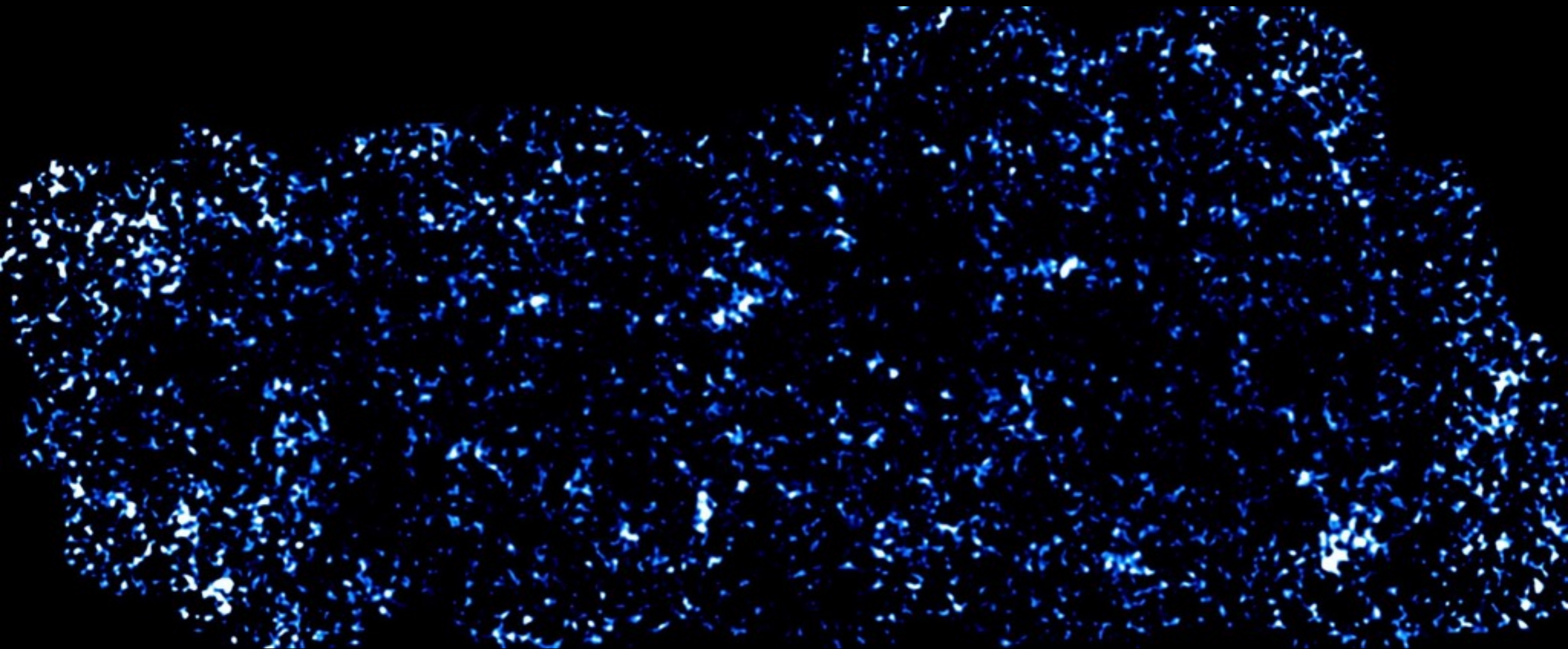
superb performance

HSC: 3 colors in 2.5hours

HST: 1 color in 500 hours



Weak lensing mass map for ~ 20 sq. degrees field (*2hrs data*)



What is dark matter?

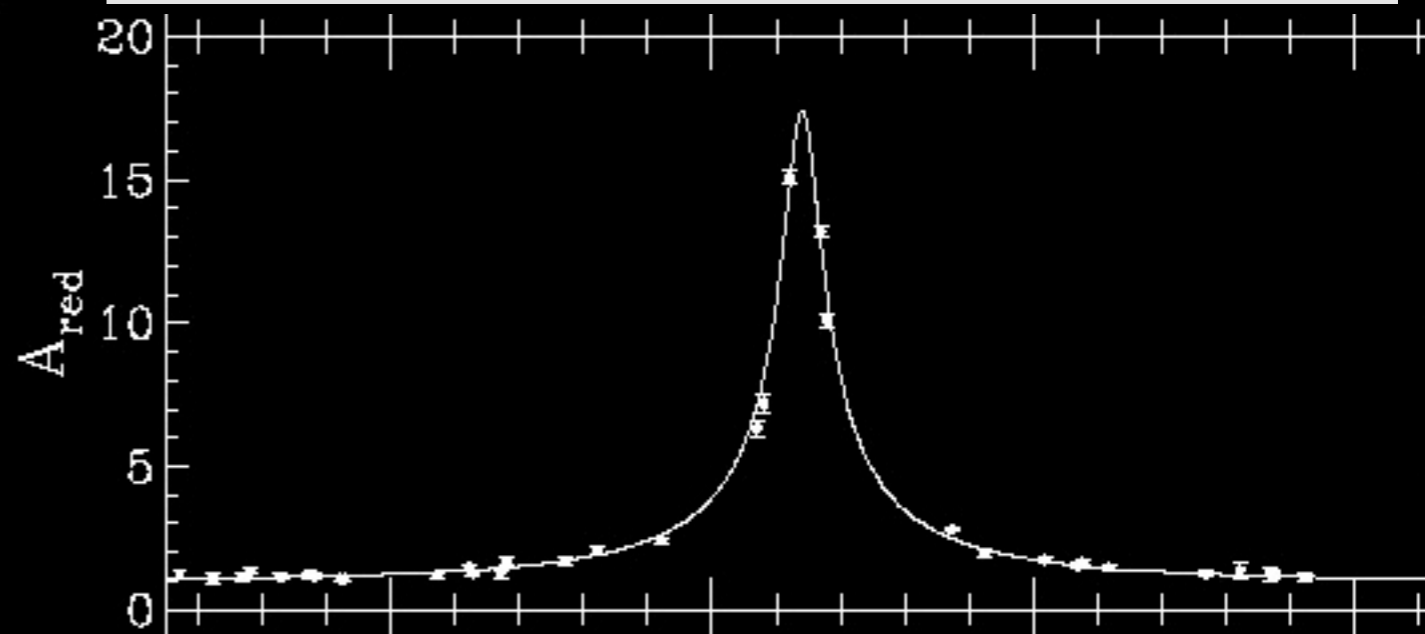
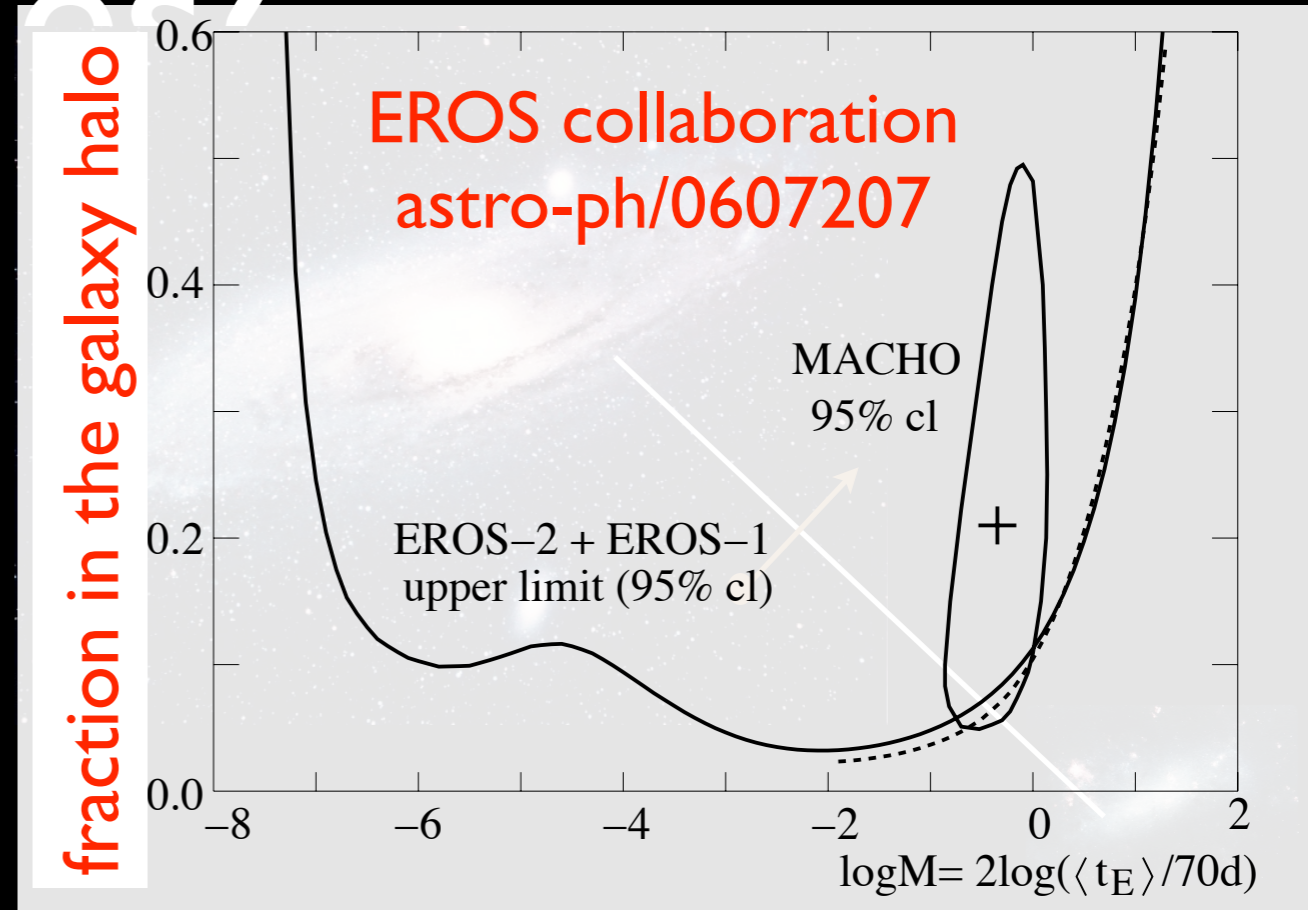
Dim Stars? Black

Holm?

Search for **MACHOs**
(Massive Compact Halo Objects)

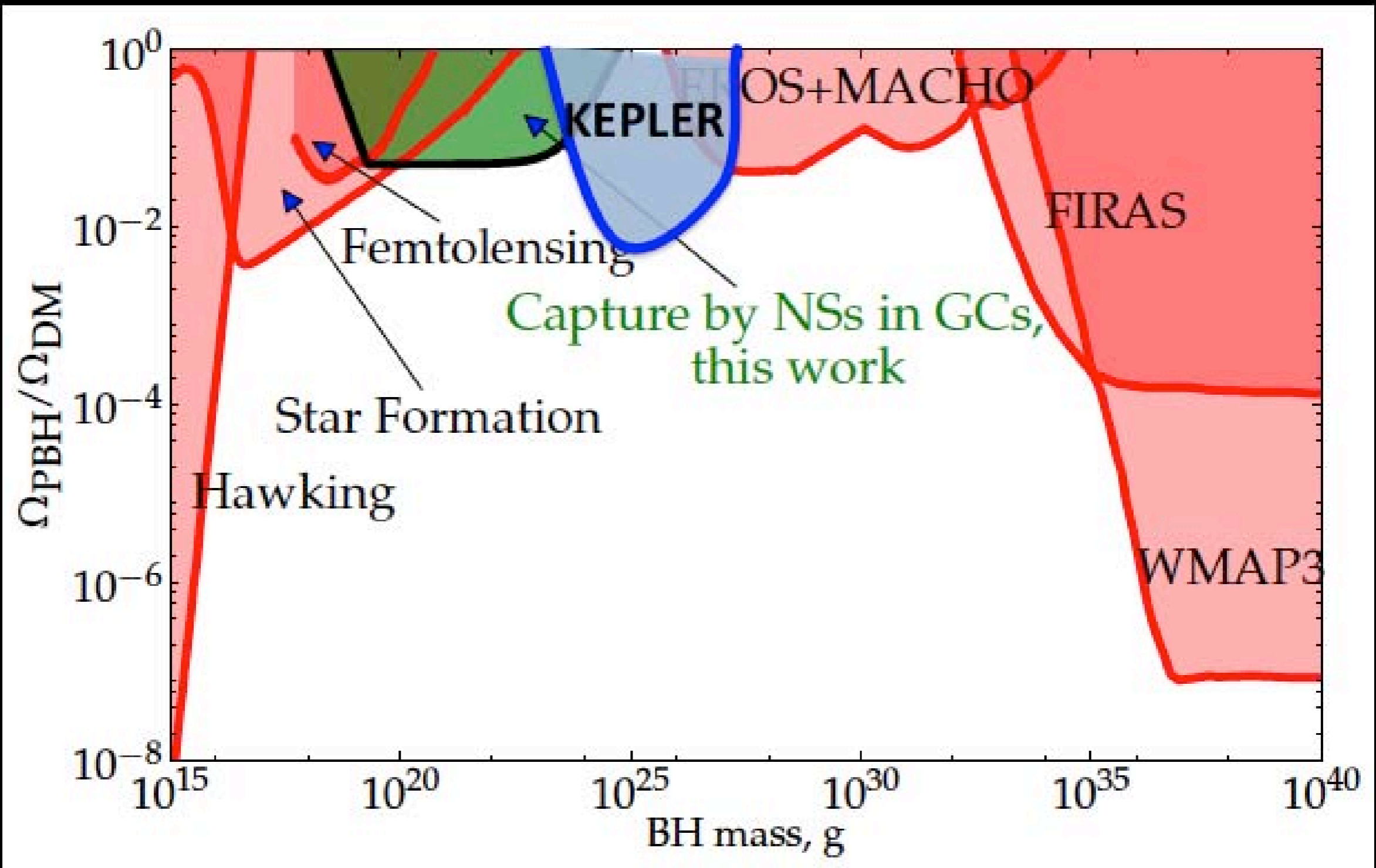


Large Magellanic Cloud



Not enough of them!

Closing the PBH as DM window



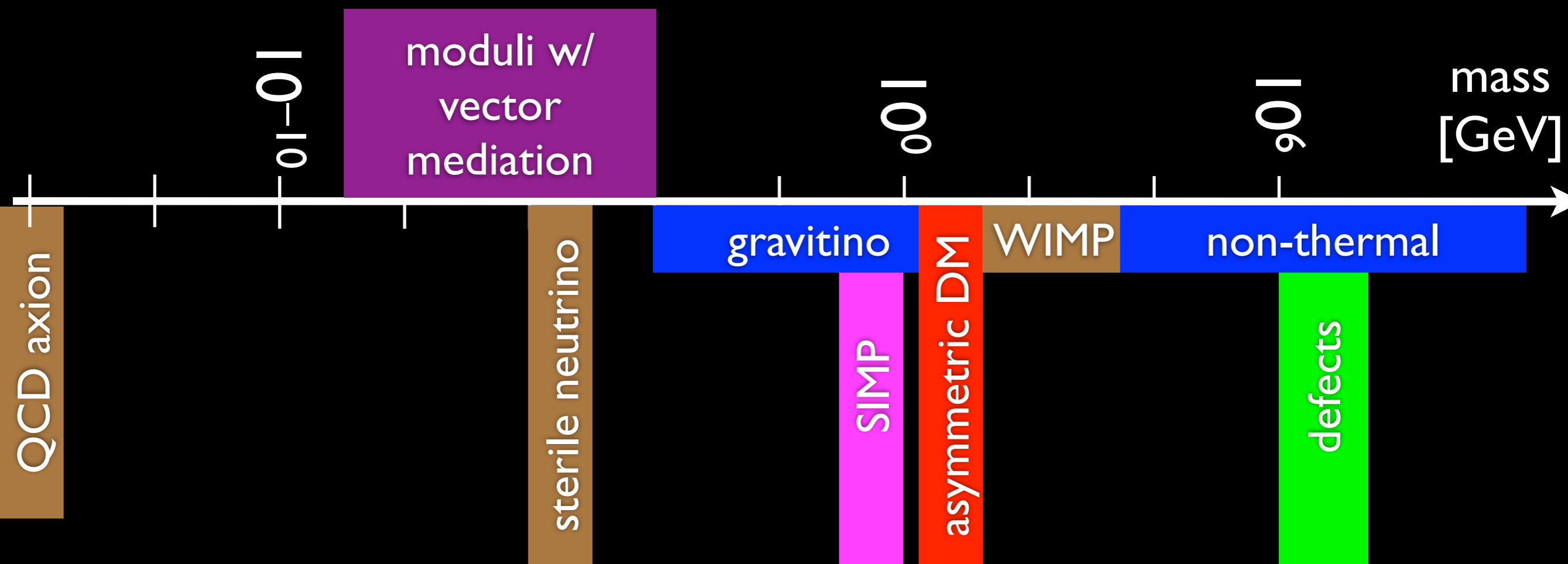
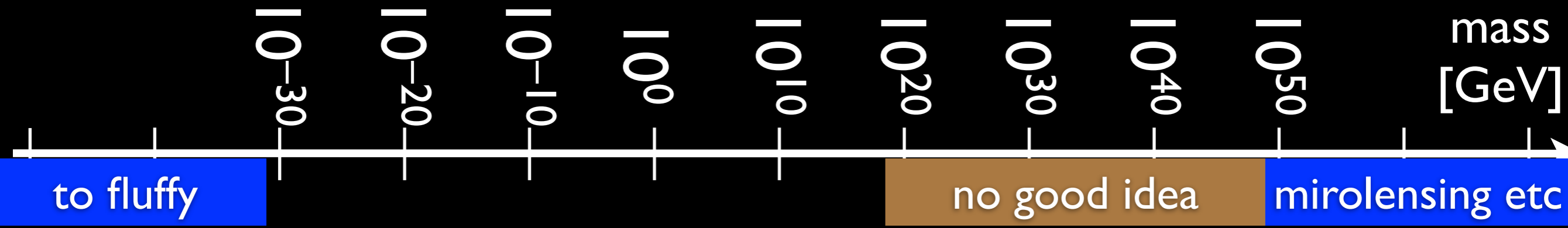
Capela, Pshirkov, & Tinyakov: arXiv:1301.4984



Mass Limits

“Uncertainty Principle”

- Clumps to form structure
- imagine $V = G_N \frac{Mm}{r}$
- “Bohr radius”: $r_B = \frac{\hbar^2}{G_N M m^2}$
- too small $m \Rightarrow$ won't “fit” in a galaxy!
- $m > 10^{-22}$ eV “uncertainty principle” bound
(modified from Hu, Barkana, Gruzinov, astro-ph/0003365)

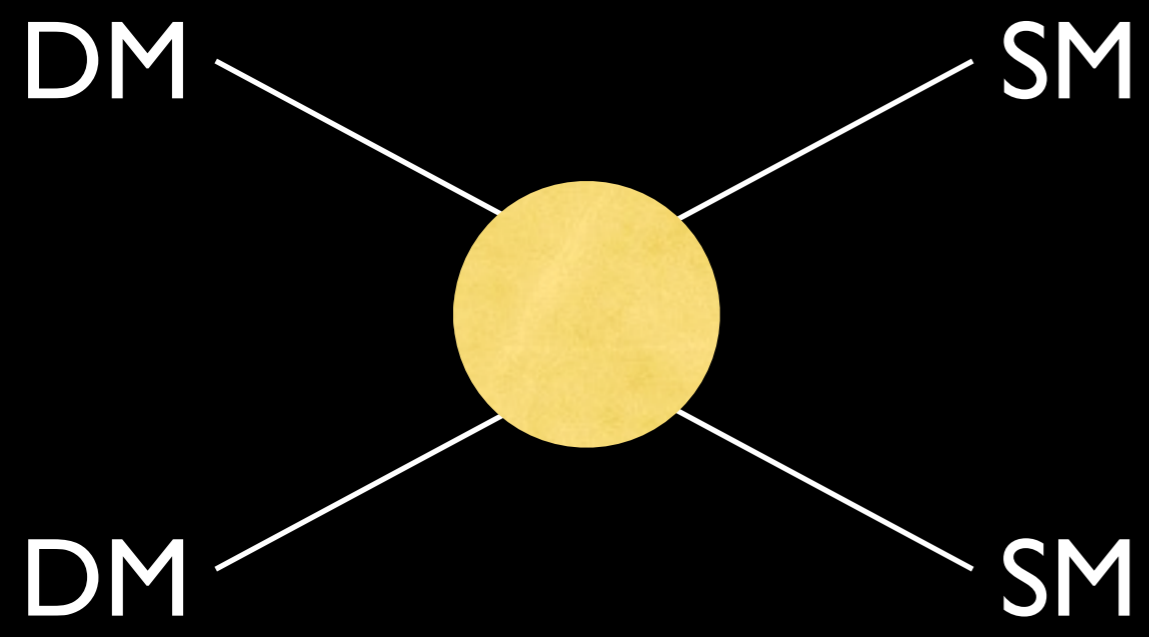


discuss various possibilities
 highly biased list
 most references are *mine*



$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

WIMP Miracle

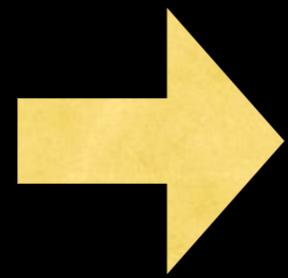


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

“weak” coupling
“weak” mass scale



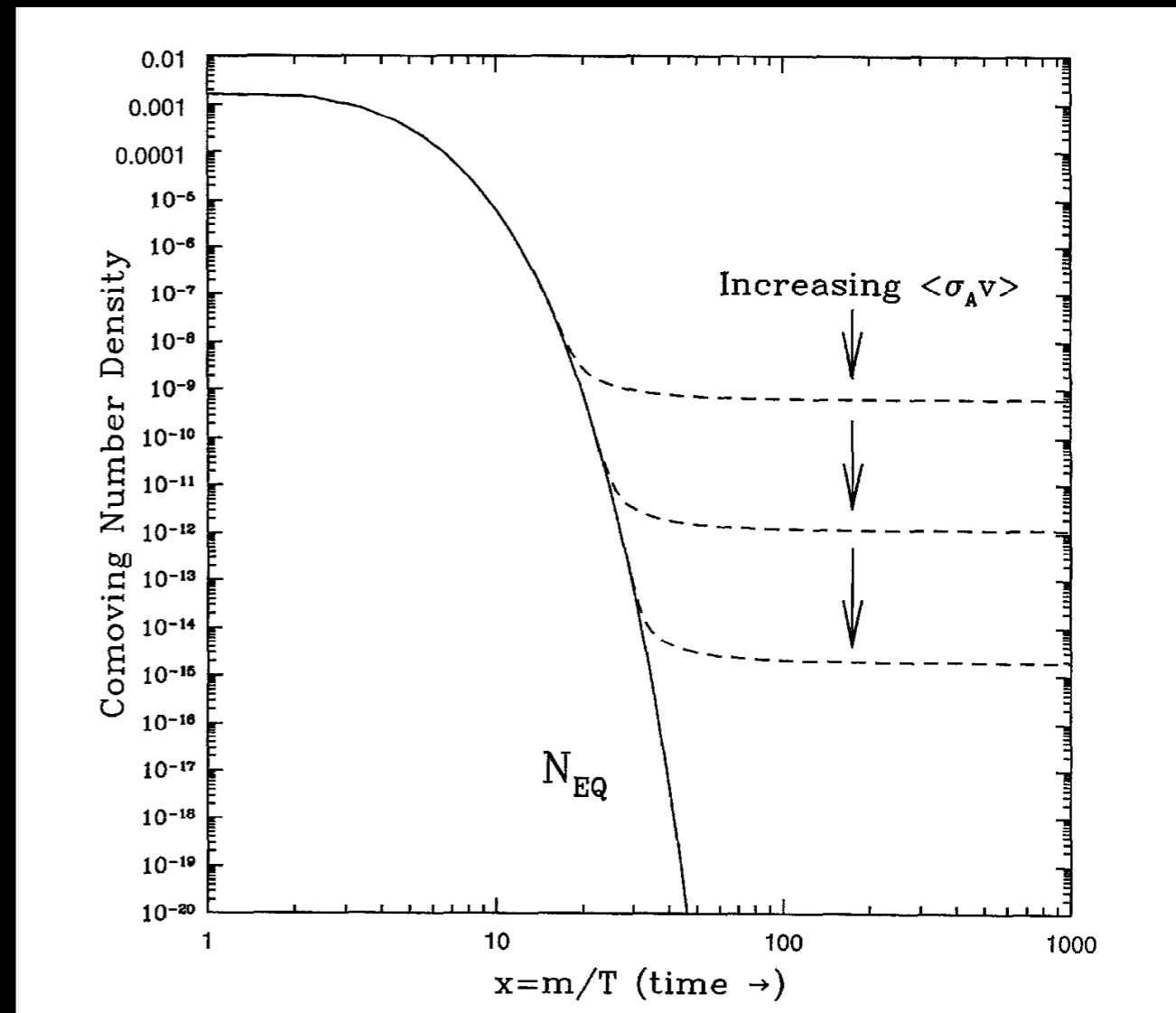
correct abundance

Miracle²



thermal relic

- thermal equilibrium when $T > m_\chi$
- Once $T < m_\chi$, no more χ created
- if stable, only way to lose them is annihilation
- but universe expands and χ get dilute
- at some point they can't find each other
- their number in comoving volume "frozen"



Freeze-out

- WIMP freezes out when the annihilation rate drops below the expansion rate
- Yield $Y=n/s$ constant under expansion
- stronger annihilation \Rightarrow less abundance

$$H \approx g_*^{1/2} \frac{T^2}{M_{Pl}}$$

$$\Gamma_{\text{ann}} \approx \langle \sigma_{\text{ann}} v \rangle n$$

$$H(T_f) = \Gamma_{\text{ann}}$$

$$n \approx g_*^{1/2} \frac{T_f^2}{M_{Pl} \langle \sigma_{\text{ann}} v \rangle}$$

$$s \approx g_* T^3$$

$$Y = \frac{n}{s} \approx g_*^{-1/2} \frac{1}{M_{Pl} T_f \langle \sigma_{\text{ann}} v \rangle}$$

$$\Omega_\chi = \frac{m_\chi Y s_0}{\rho_c}$$

$$\approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$

Order of magnitude

- “Known” $\Omega_\chi=0.23$ determines the WIMP annihilation cross section
- simple estimate of the annihilation cross section
- weak-scale mass!!!

$$\Omega_\chi \approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$

$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{1.12 \times 10^{-10} \text{GeV}^{-2} x_f}{g_*^{1/2} \Omega_\chi h^2}$$

$$\sim 10^{-9} \text{GeV}^{-2}$$

$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{\pi \alpha^2}{m_\chi^2}$$

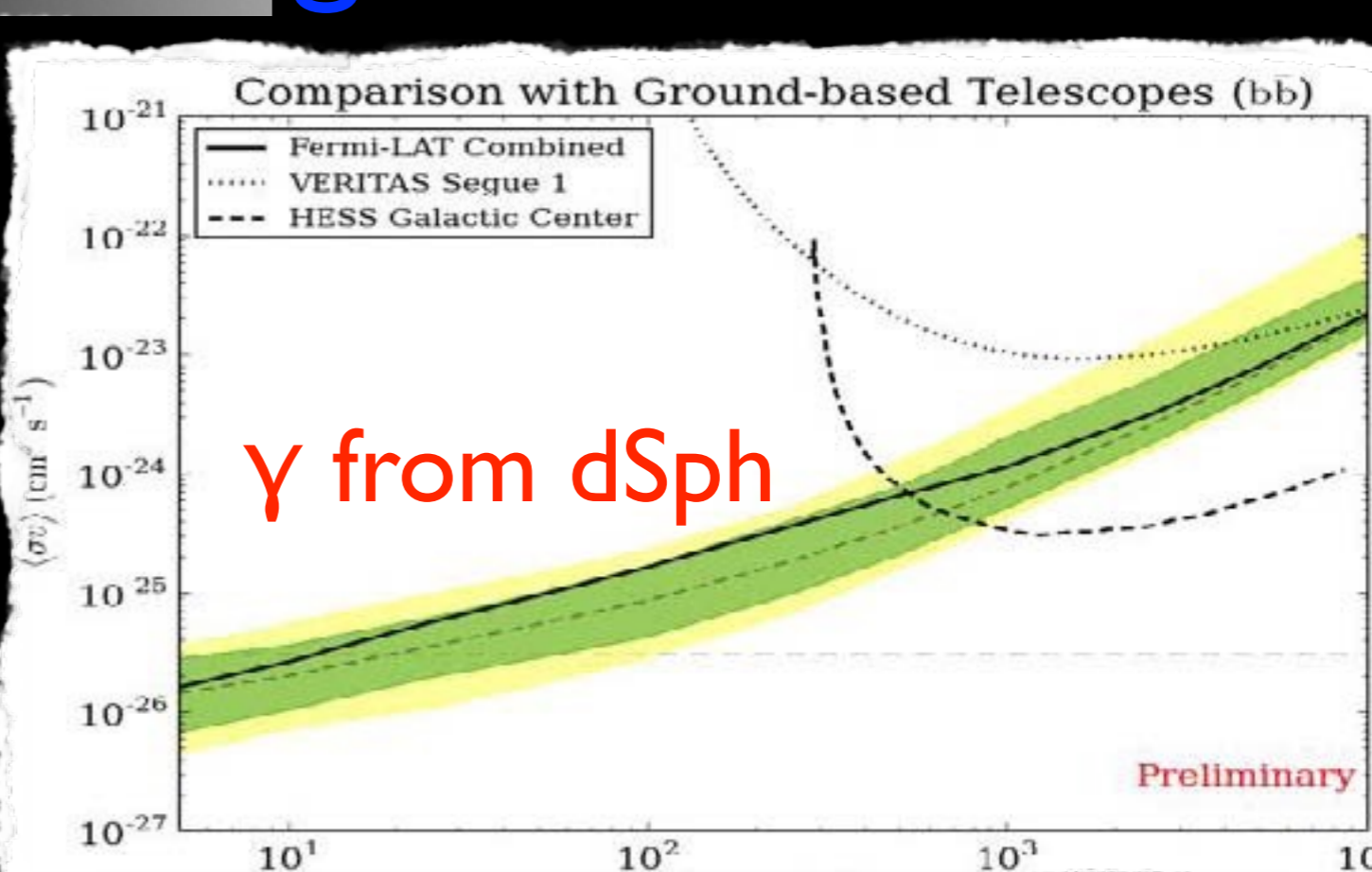
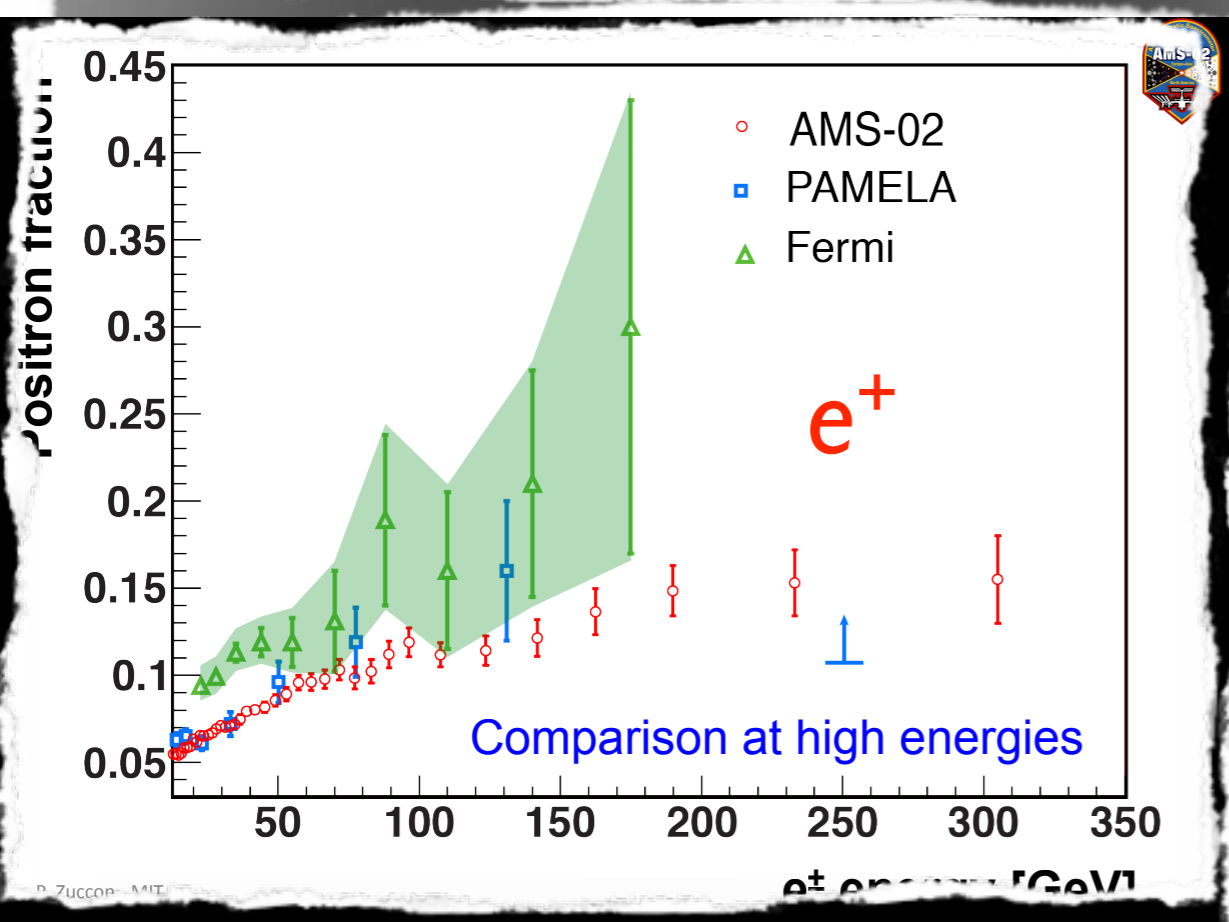
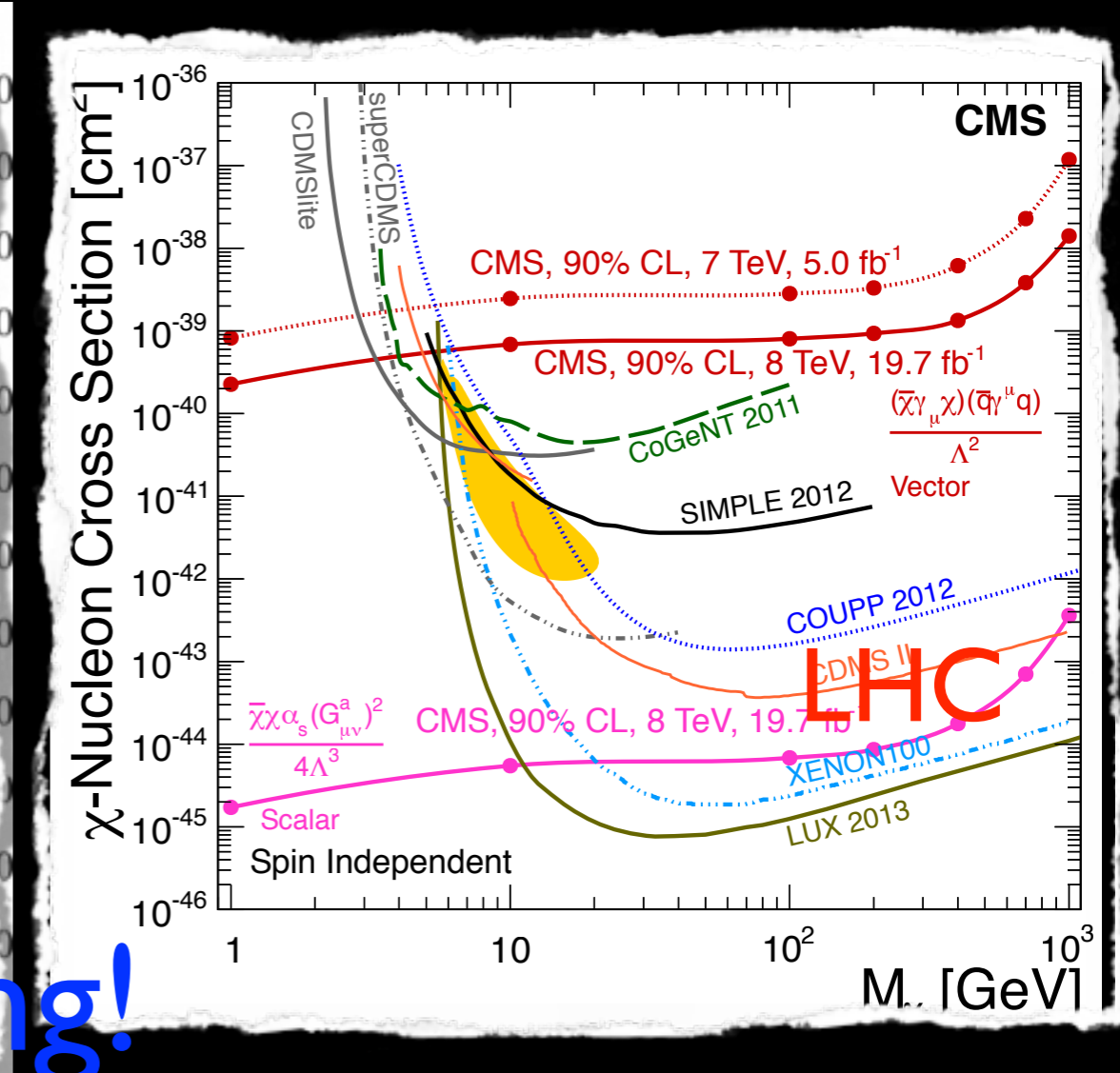
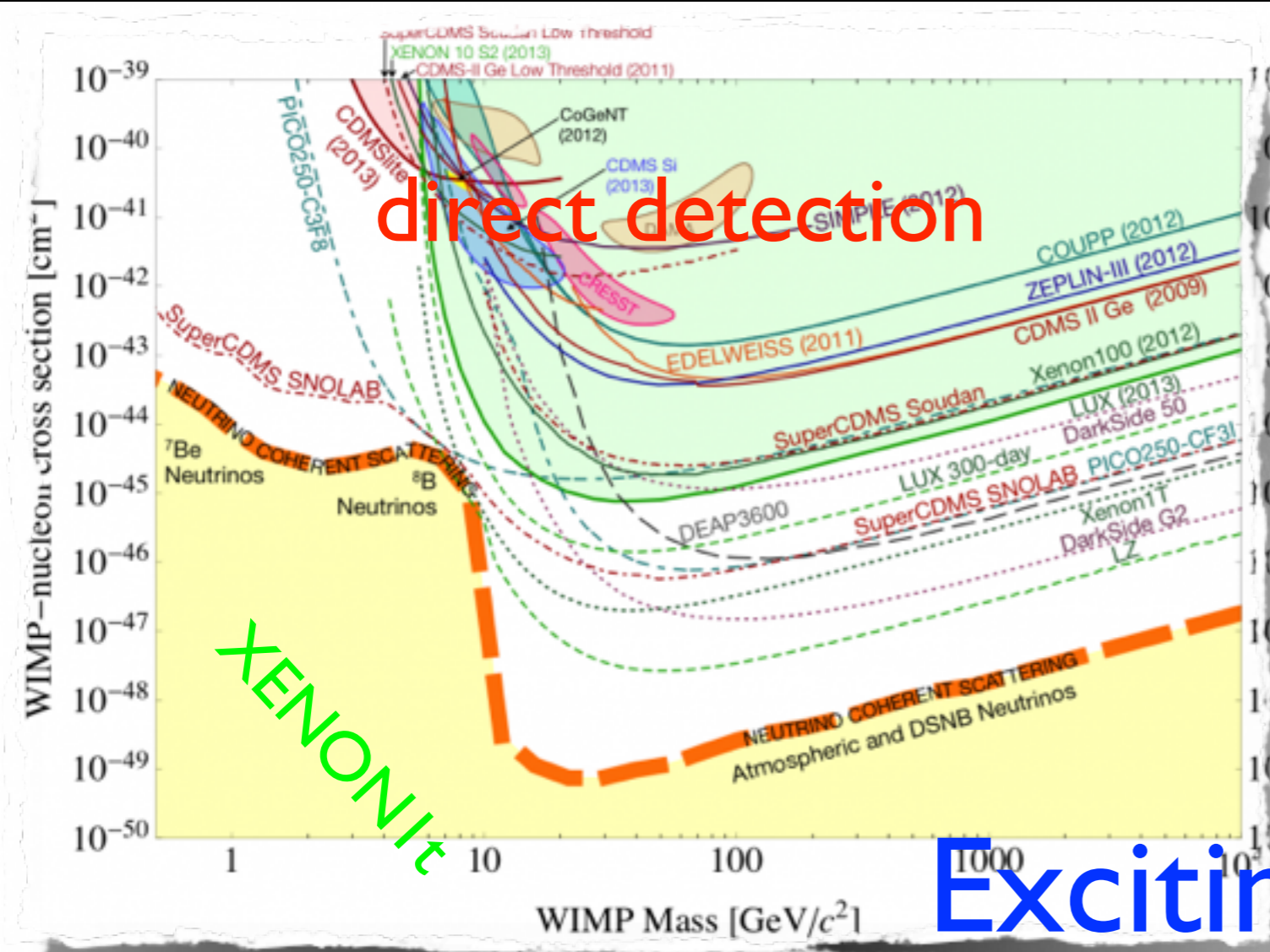
$$m_\chi \approx 300 \text{ GeV}$$

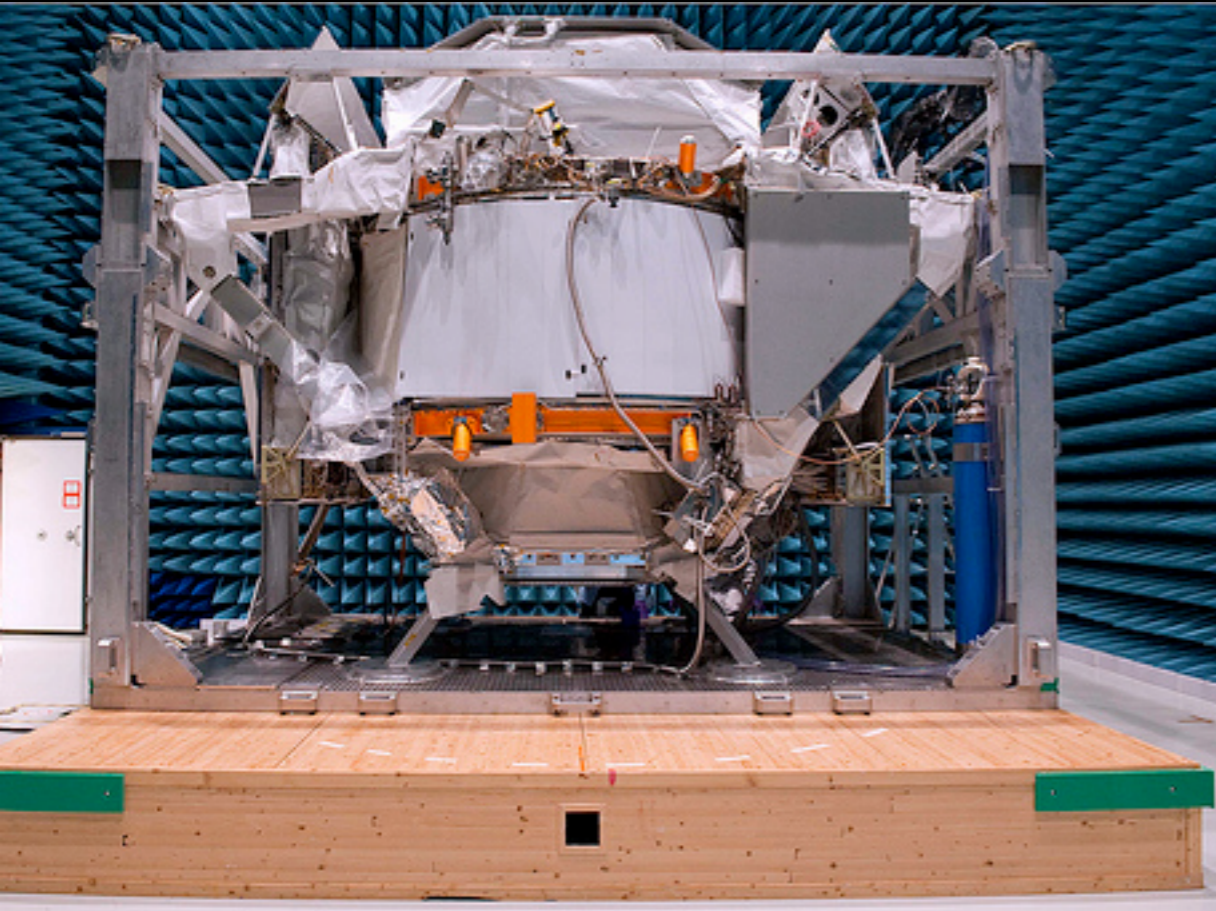
$$\langle \sigma_{\text{ann}} v \rangle \simeq 2.2 \times 10^{-26} \text{cm}^3/\text{sec}$$



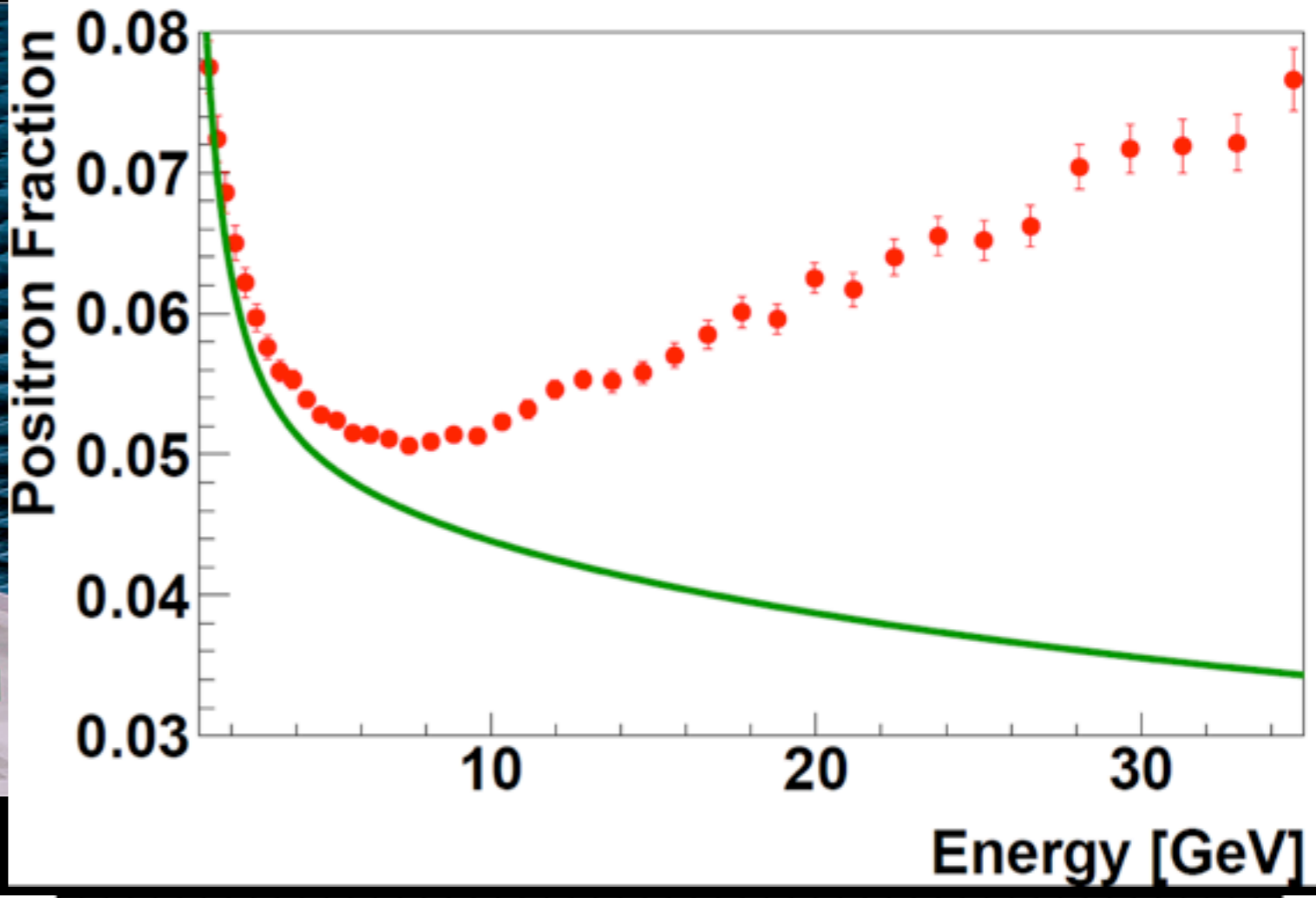
“WIMP Miracle”

- A stable particle at the weak scale with “EM-strength” coupling naturally gives the correct abundance
- This is where we expect new particles because of the hierarchy problem $m_W \ll M_{Pl}$
- Many candidates of this type: supersymmetry, little Higgs with T-parity, Universal Extra Dimensions, etc
- If so, we may even create dark matter at accelerators

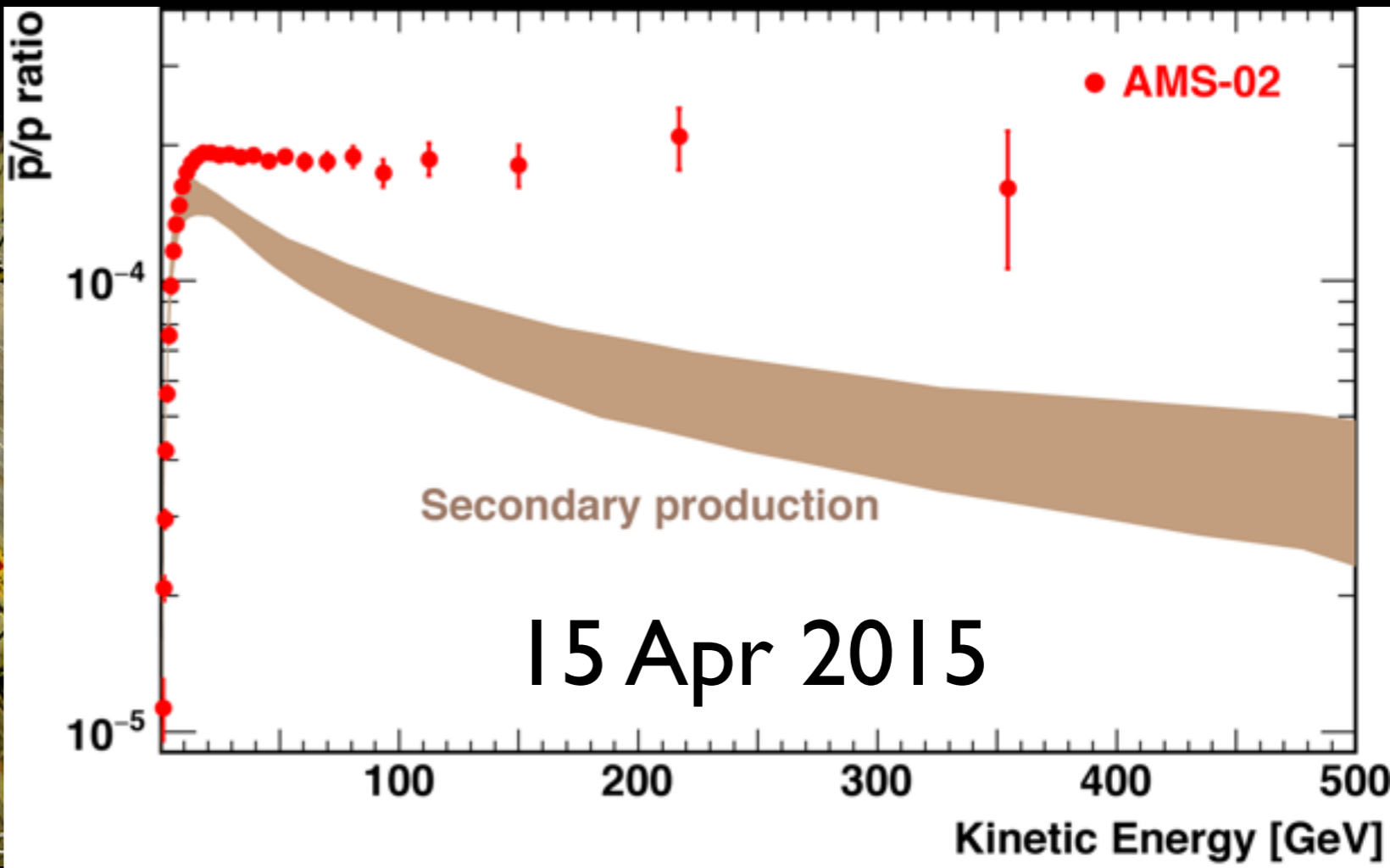




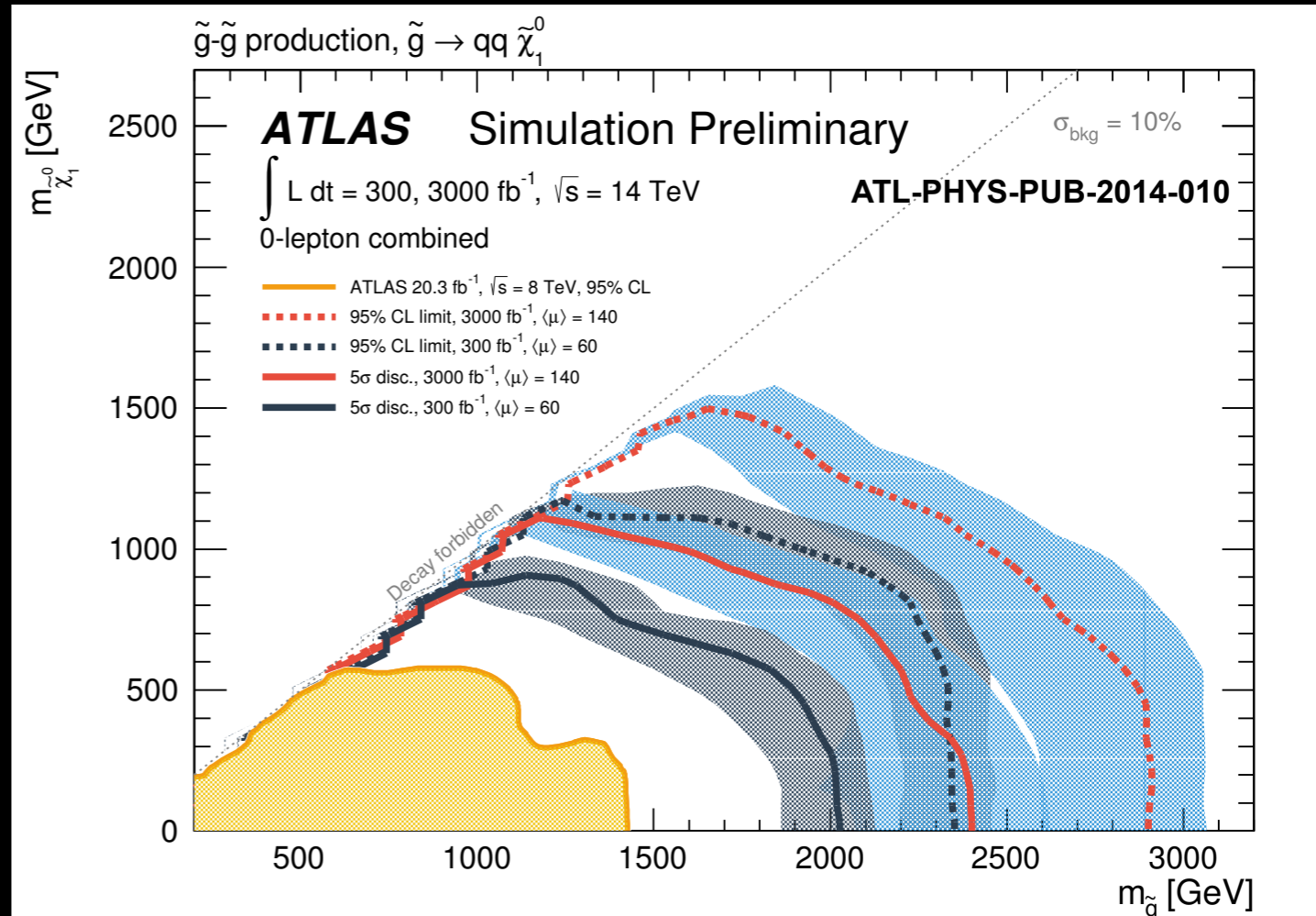
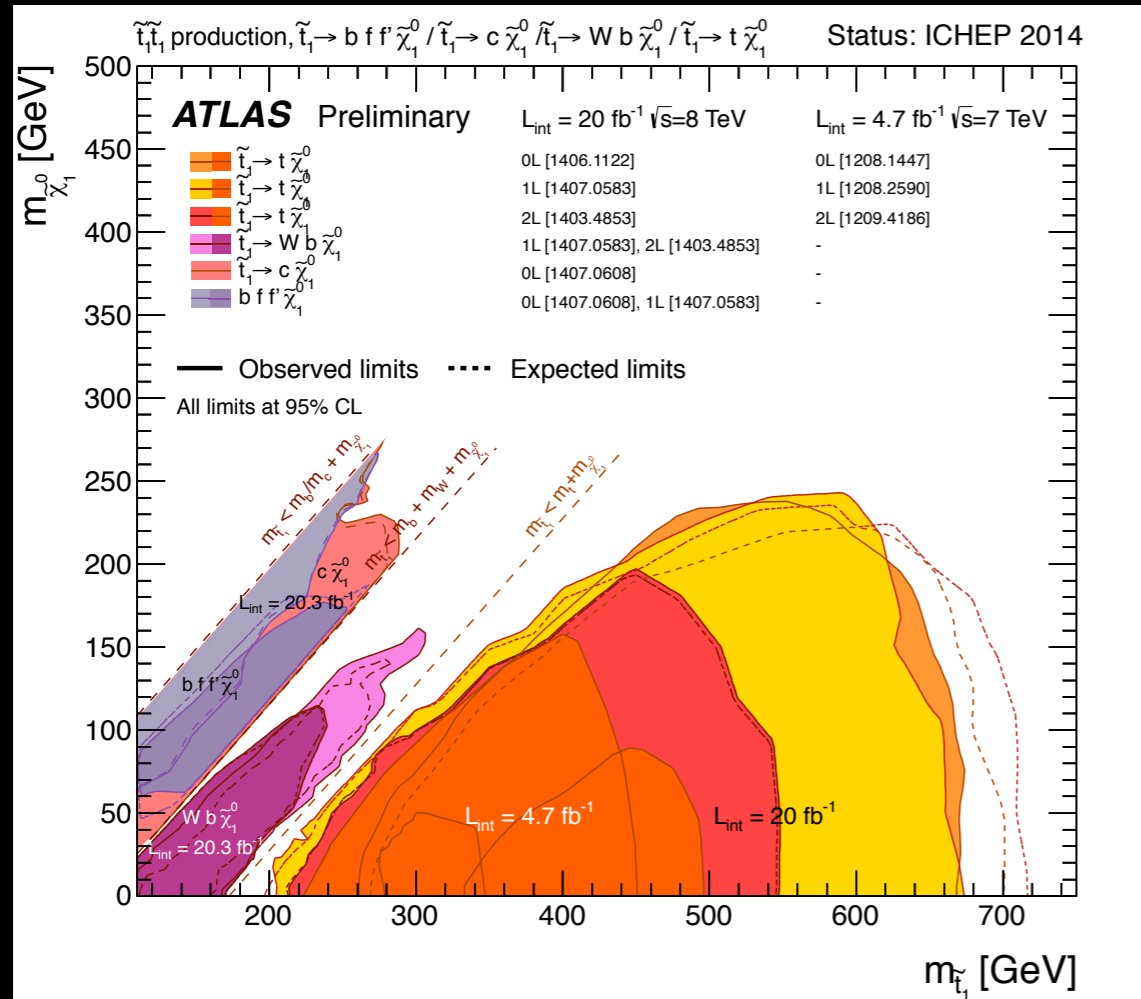
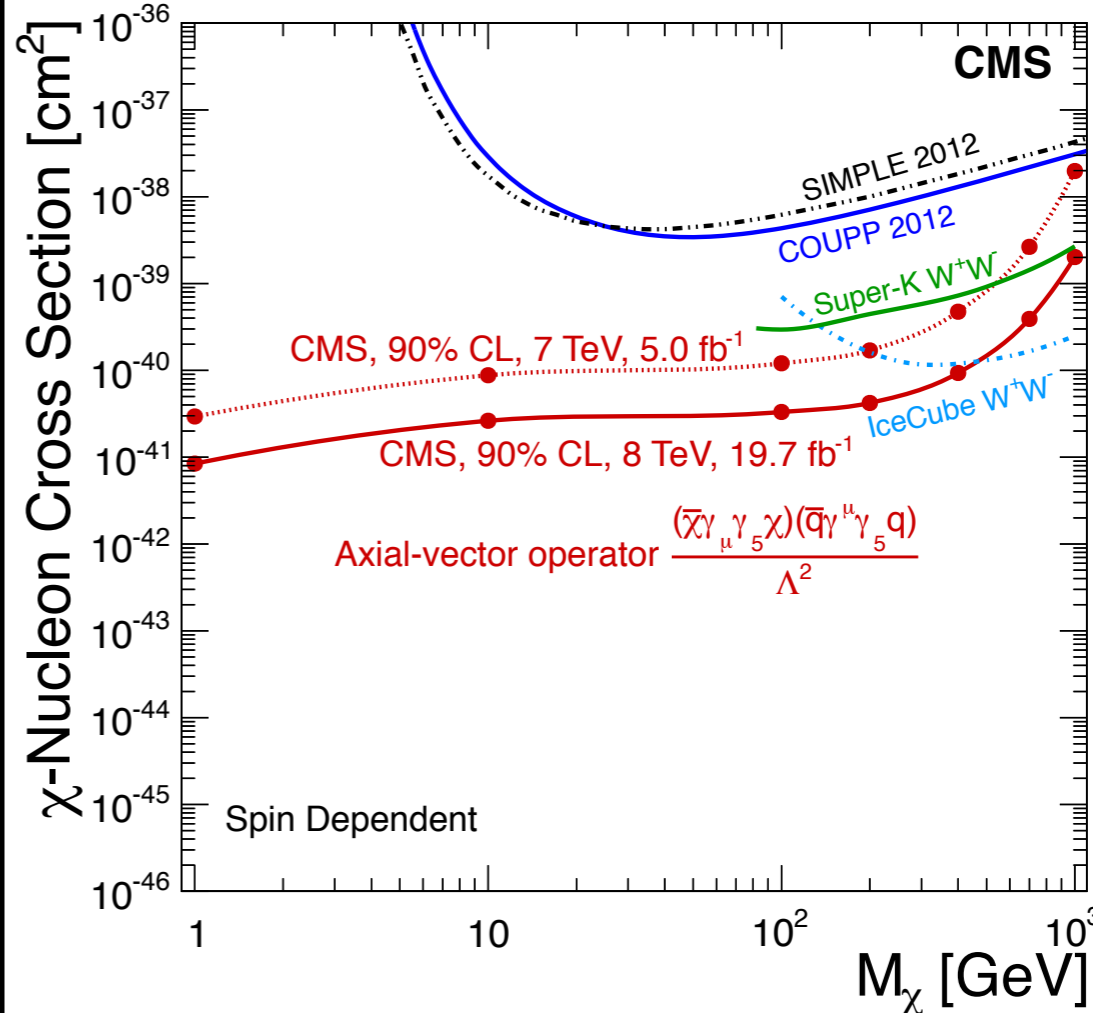
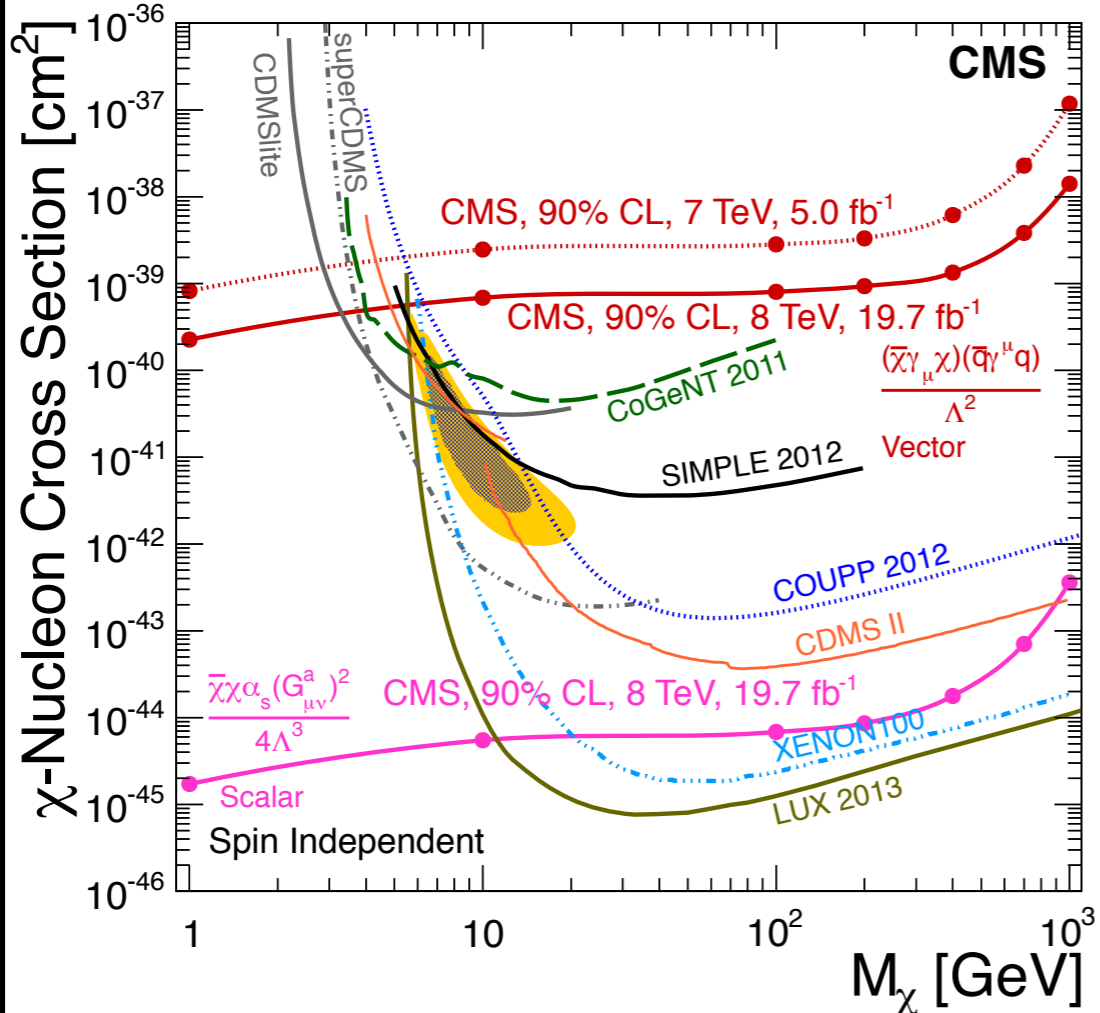
AMS



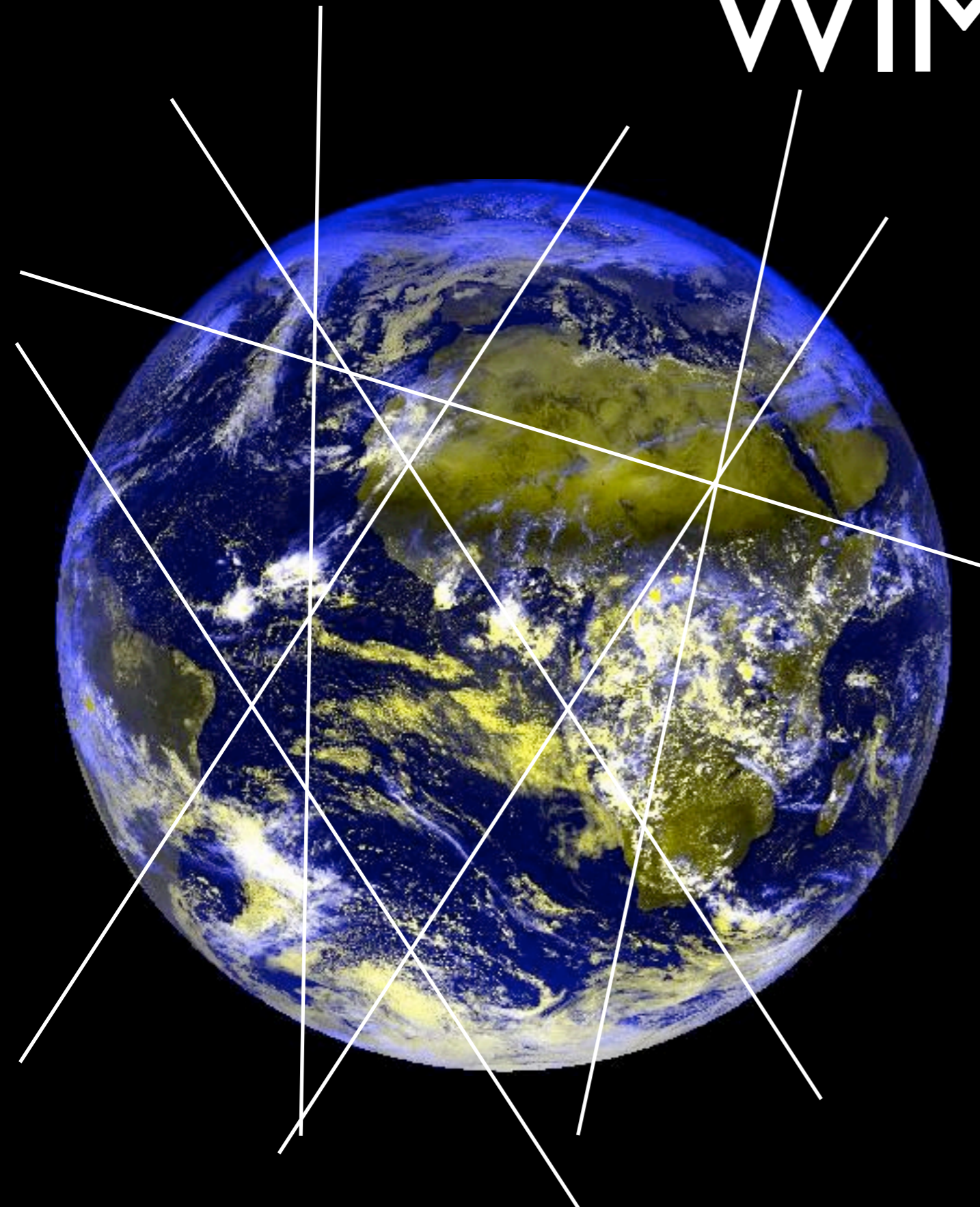
© Michele Famiglietti / AMS C



15 Apr 2015



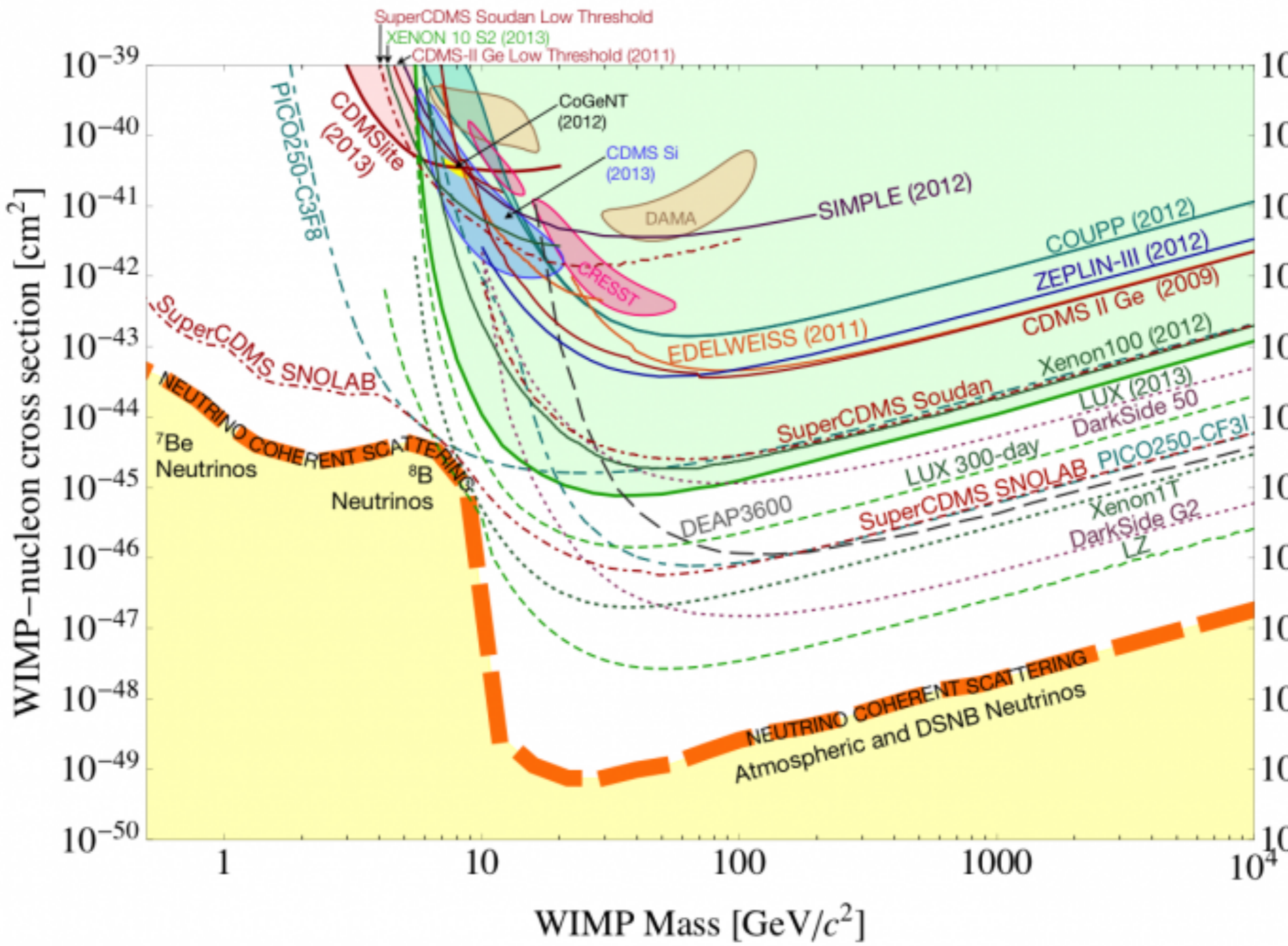
WIMPs



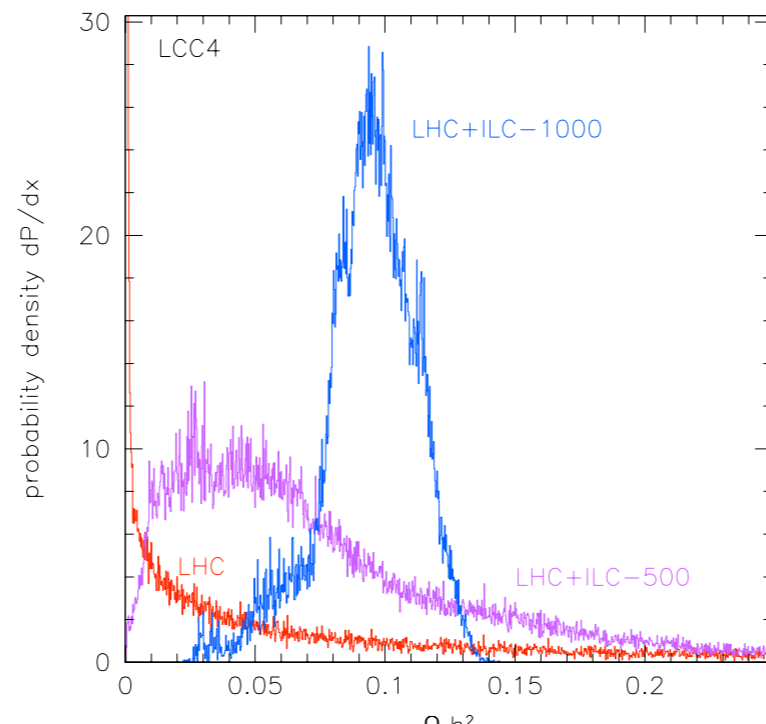
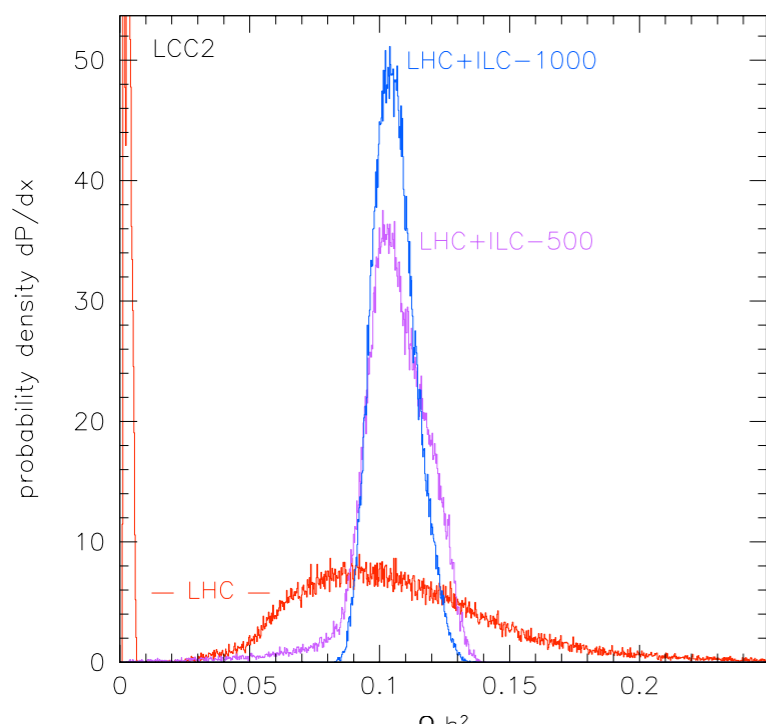
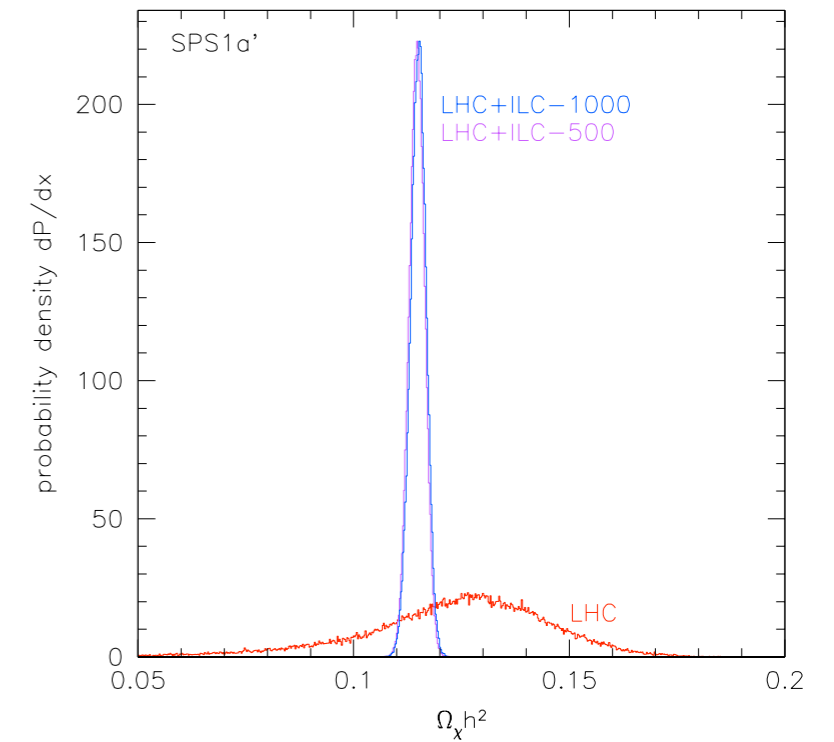
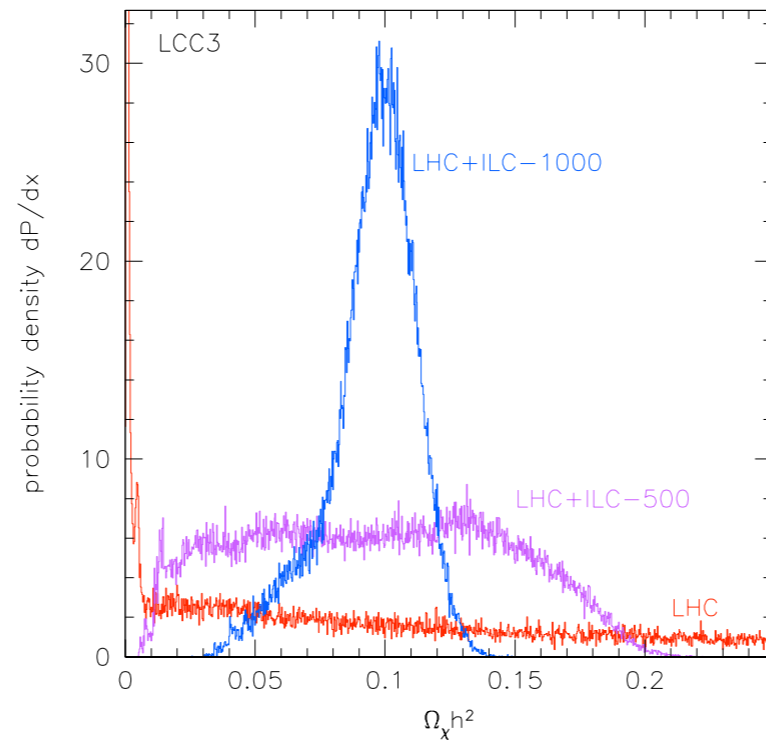
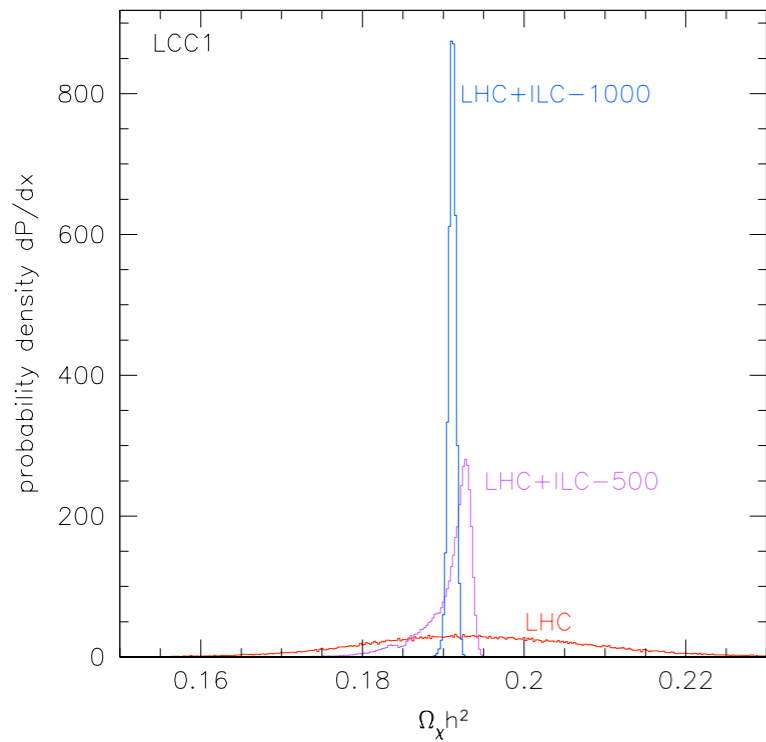
- It is probably **WIMP** (Weakly Interacting Massive Particle)
- Stable heavy particle produced in early Universe, **left-over from near-complete annihilation**
- **millions of them** go through your body every second

avoid noise on the surface
go to quiet underground





Omega from colliders



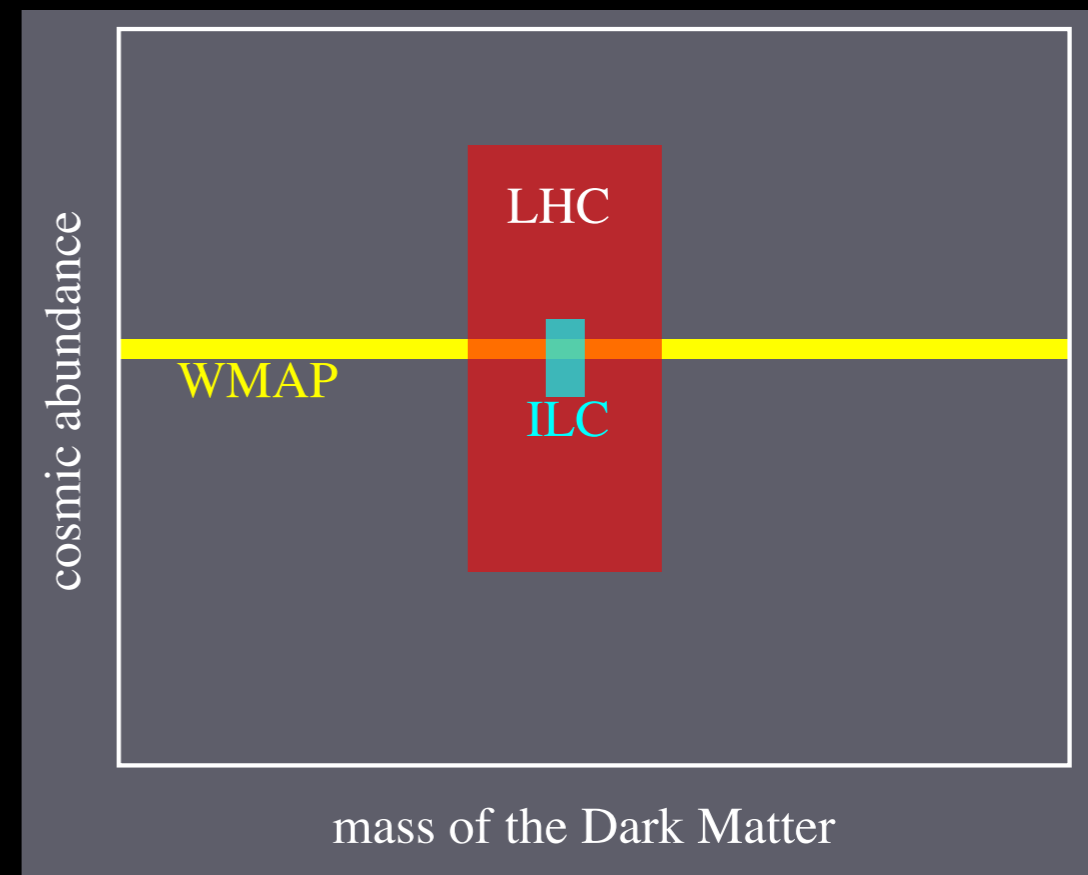
SUSY case study
Baltz, Battaglia, Peskin,
Wizansky hep-ph/0602187

program

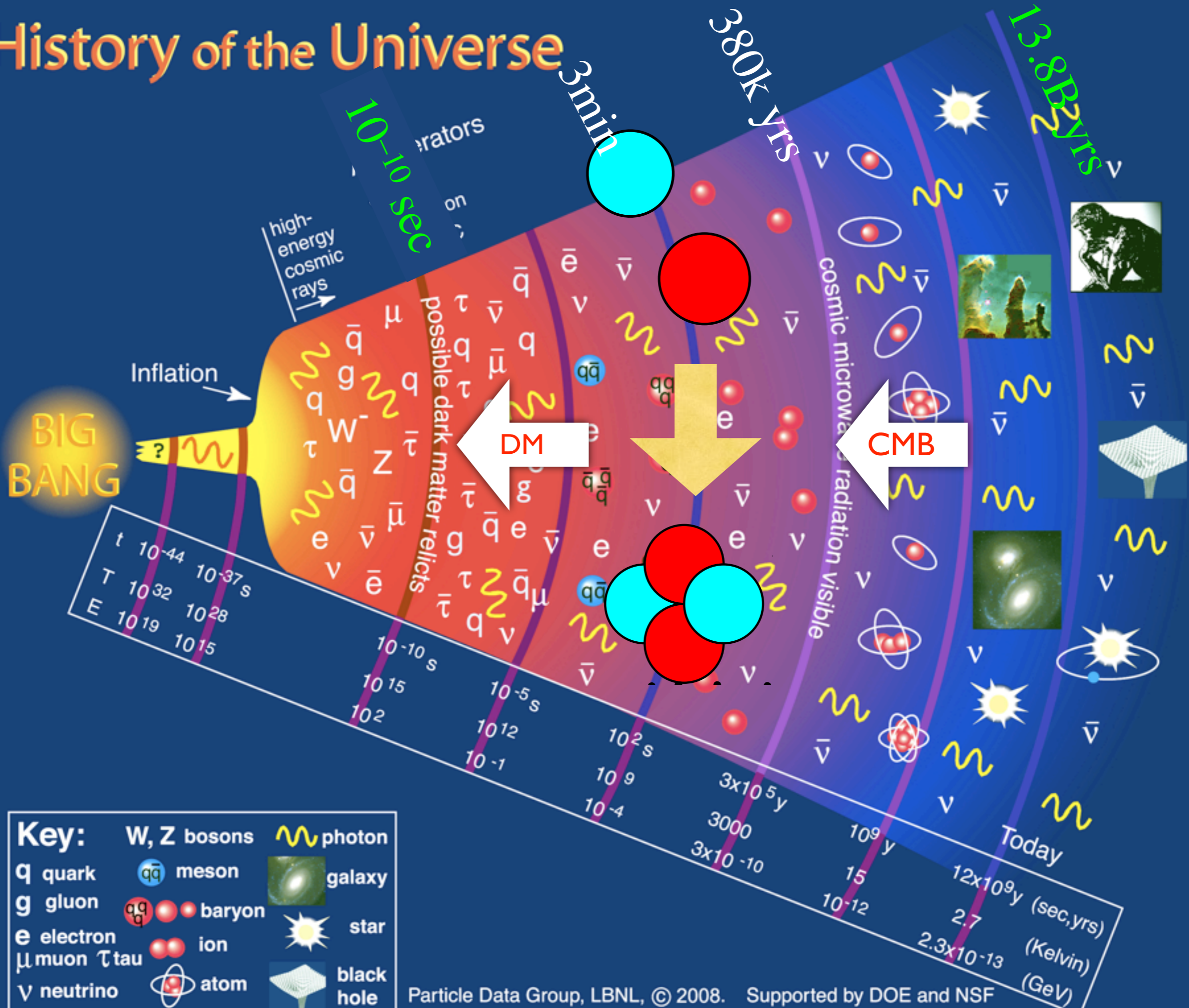
- telescope measurement of dark matter
- underground detection experiments
- production with accelerators
- If they agree with each other:

⇒ Will know *what Dark Matter is*

⇒ Will understand universe back to $t \sim 10^{-10}$ sec



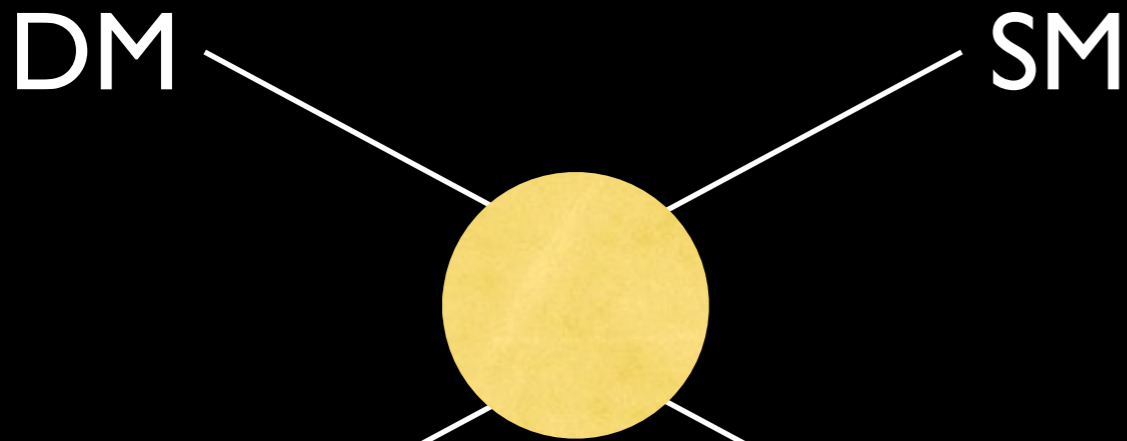
History of the Universe





$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

Miracles

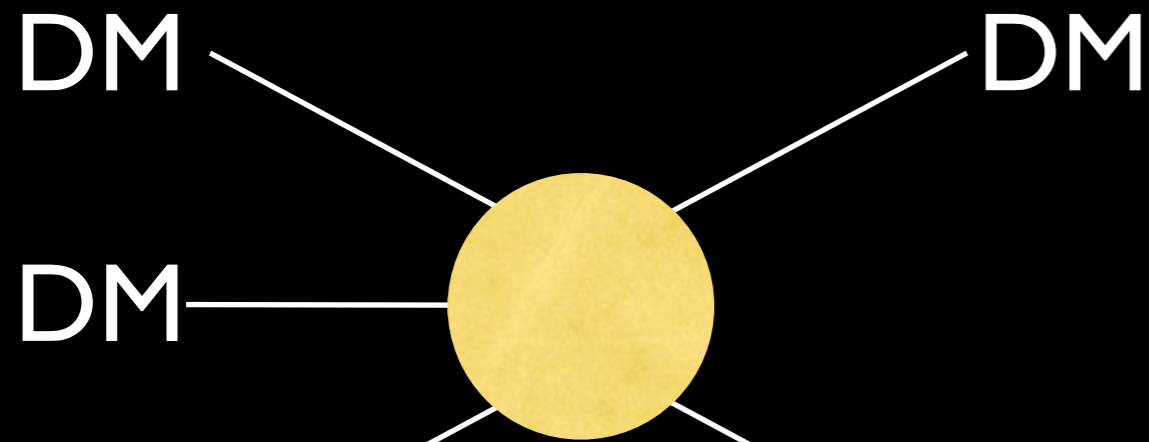
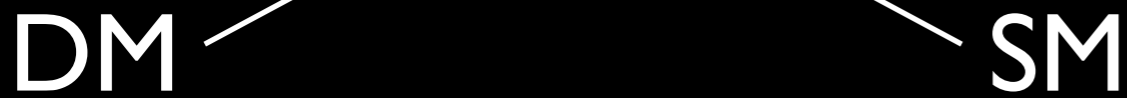


$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

WIMP miracle!



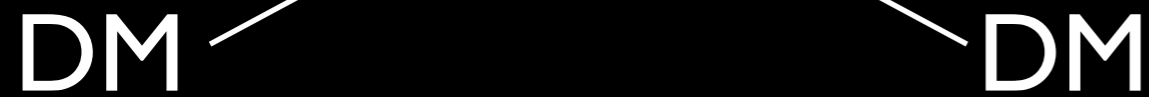
$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

Hochberg, Kuflik,
Volansky, Wacker

$$m \approx 300 \text{ MeV} \text{ arXiv:1402.5143}$$

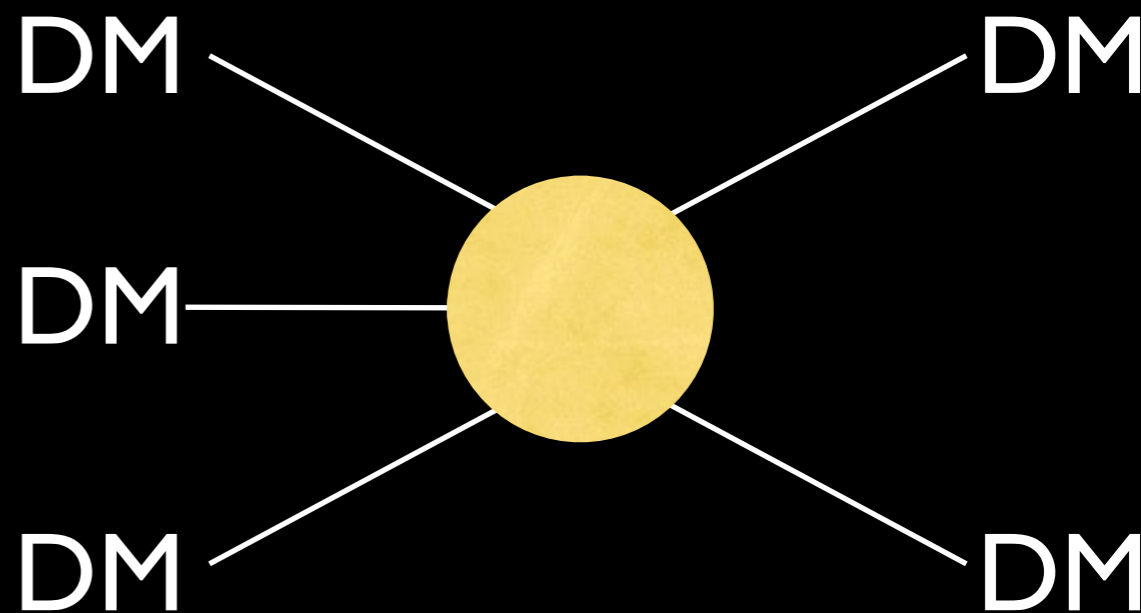
SIMP miracle!





SIMPlEst Miracle

- Not only the mass scale is similar to QCD
- dynamics itself can be QCD! Miracle³
- DM = pions
- e.g. $SU(4)/Sp(4) = S^5$



$$\mathcal{L}_{\text{chiral}} = \frac{1}{16f_{\pi}^2} \text{Tr} \partial^{\mu} U^{\dagger} \partial_{\mu} U$$

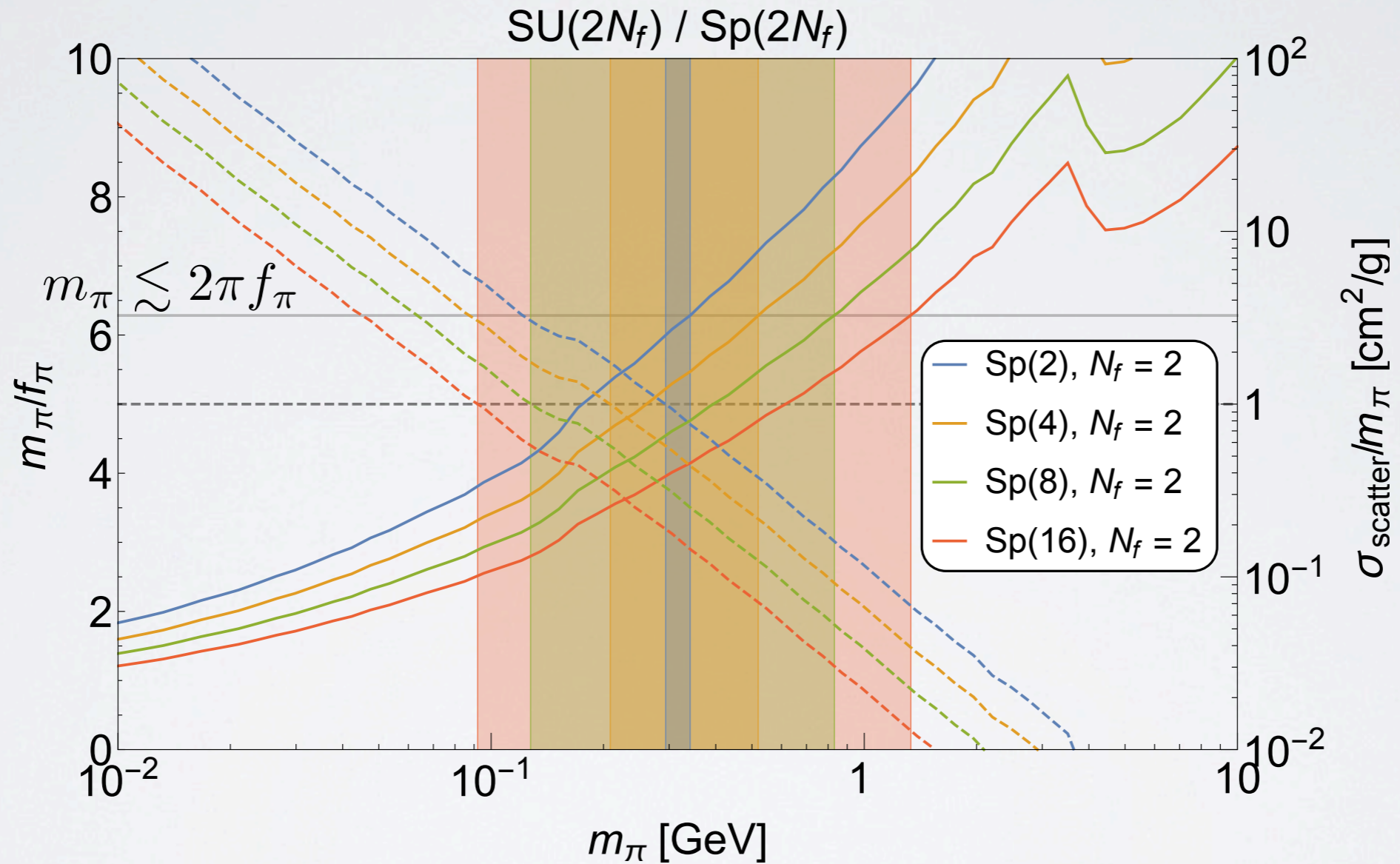
+HM

arXiv:1411.3727

$$\mathcal{L}_{\text{WZW}} = \frac{8N_c}{15\pi^2 f_{\pi}^5} \epsilon_{abcde} \epsilon^{\mu\nu\rho\sigma} \pi^a \partial_{\mu} \pi^b \partial_{\nu} \pi^c \partial_{\rho} \pi^d \partial_{\sigma} \pi^e + O(\pi^7)$$

$$\pi_5(G/H) \neq 0$$

THE RESULTS



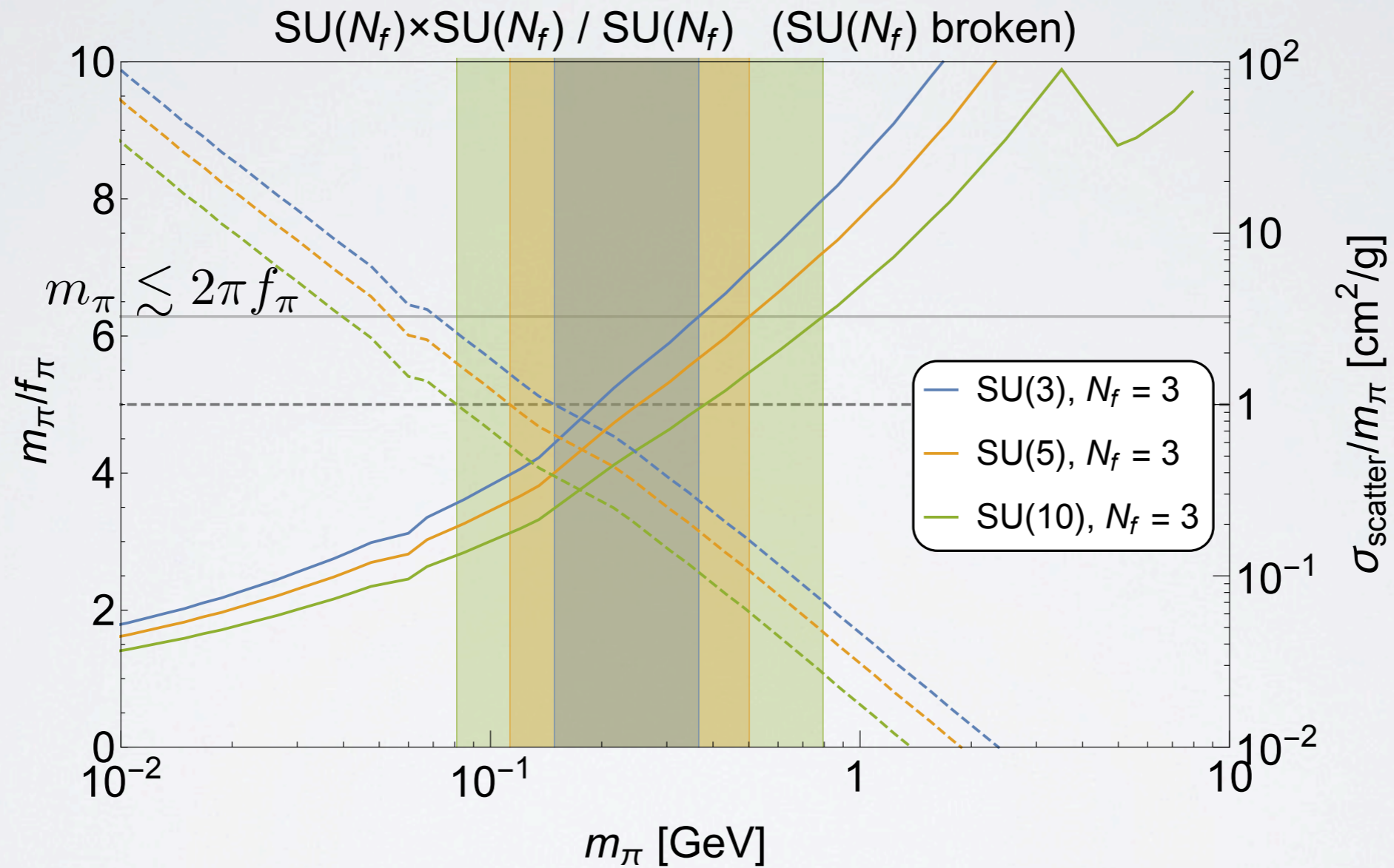
Solid curves: solution to Boltzmann eq.

Dashed curves: along that solution

$$\frac{m_\pi}{f_\pi} \propto m_\pi^{3/10}$$

$$\frac{\sigma_{\text{scatter}}}{m_\pi} \propto m_\pi^{-9/5}$$

THE RESULTS



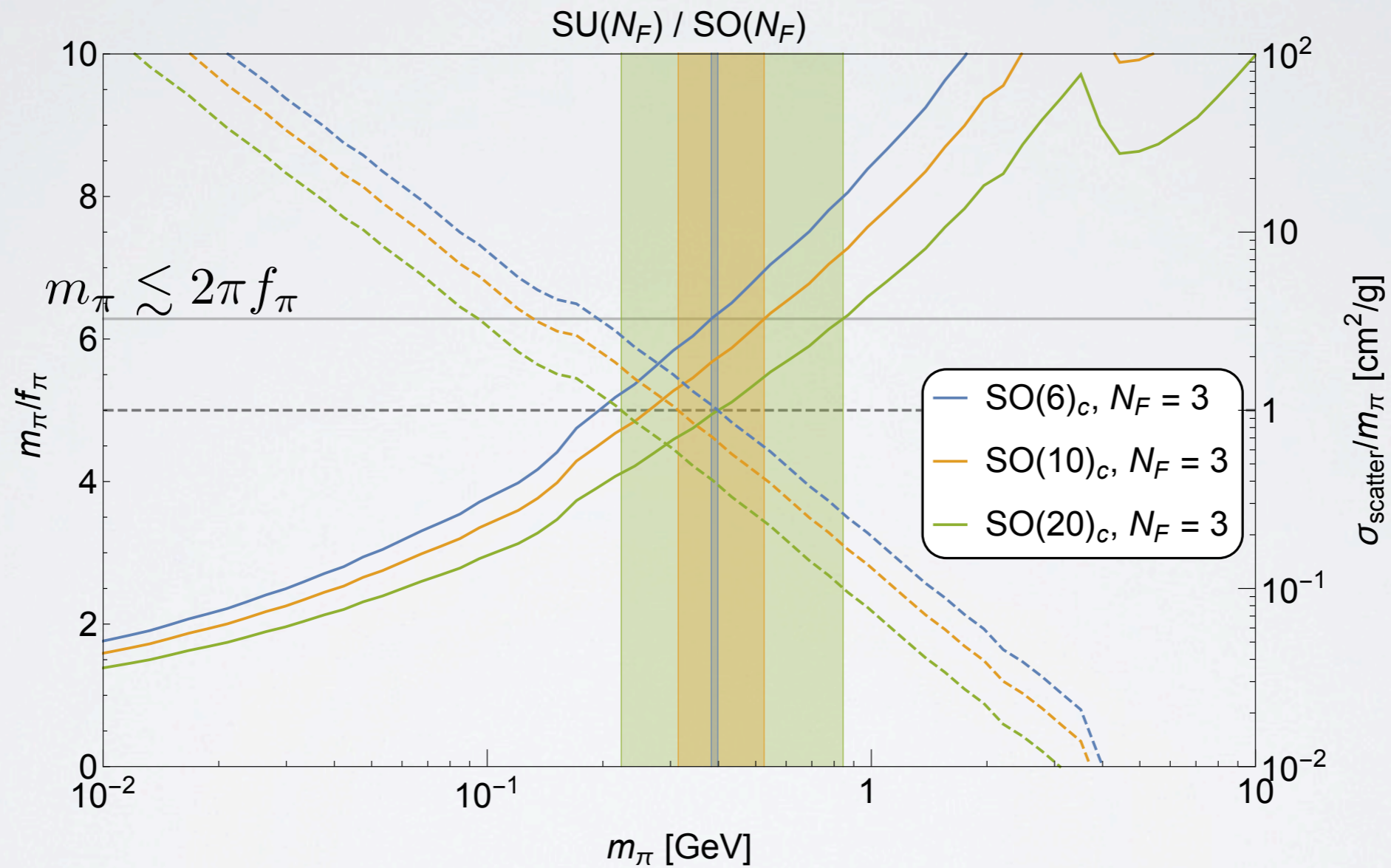
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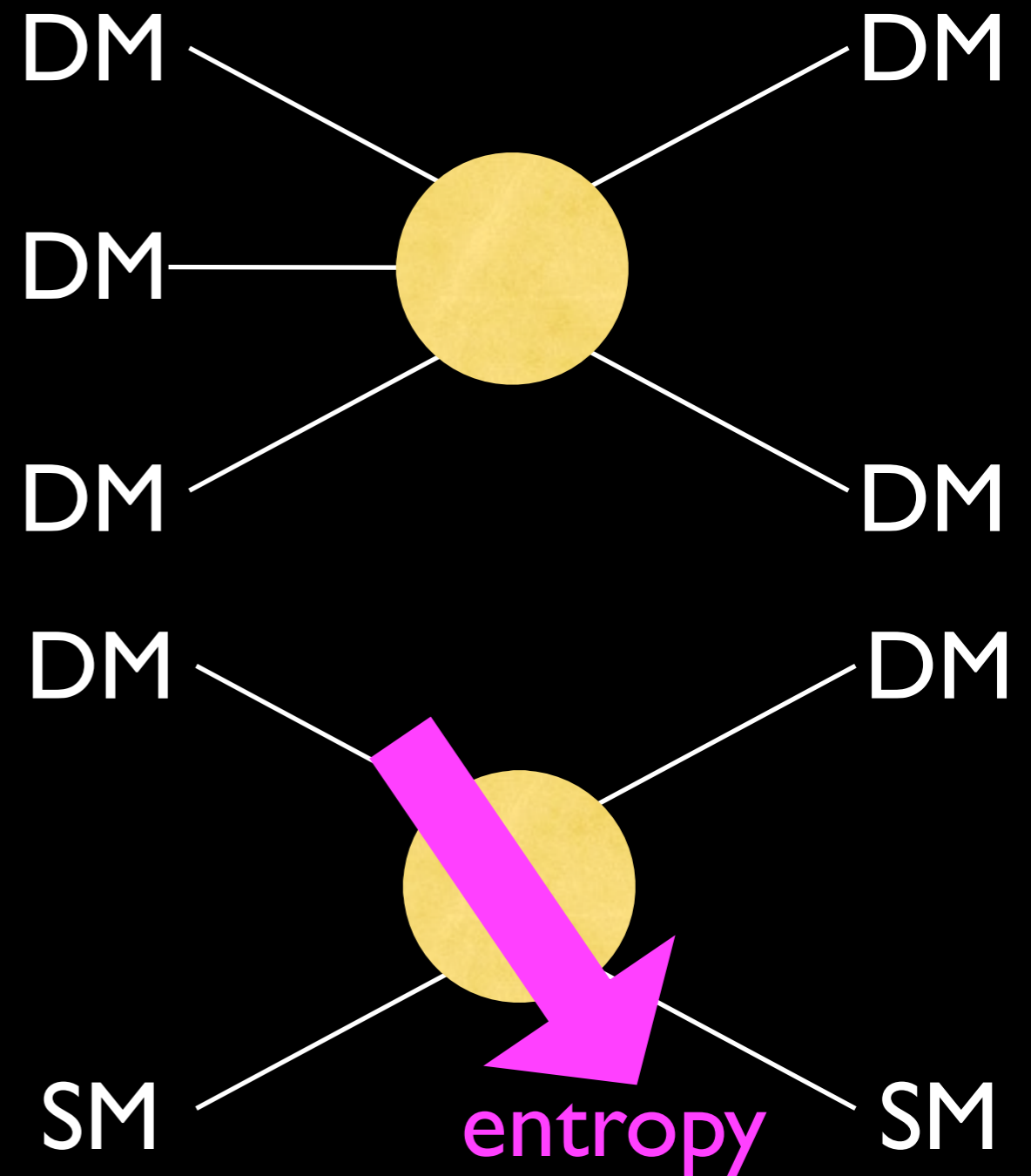
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communication

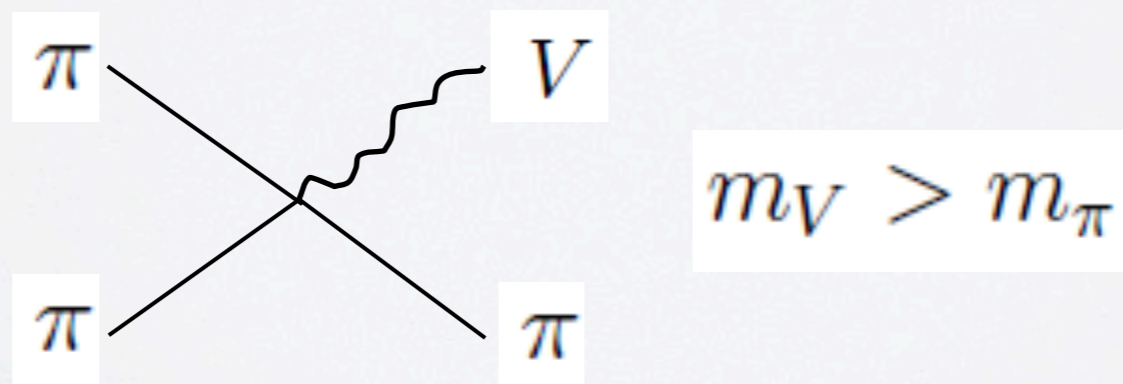
- 3 to 2 annihilation
- excess entropy *must* be transferred to e^\pm, γ
- need communication at some level
- leads to experimental signal



VECTOR PORTAL

- Gauge a $U(1)$ subgroup of the flavor symmetry
- New gauge-boson kinetically mixed with the hyper charge gauge boson

Avoid semi-annihilation:



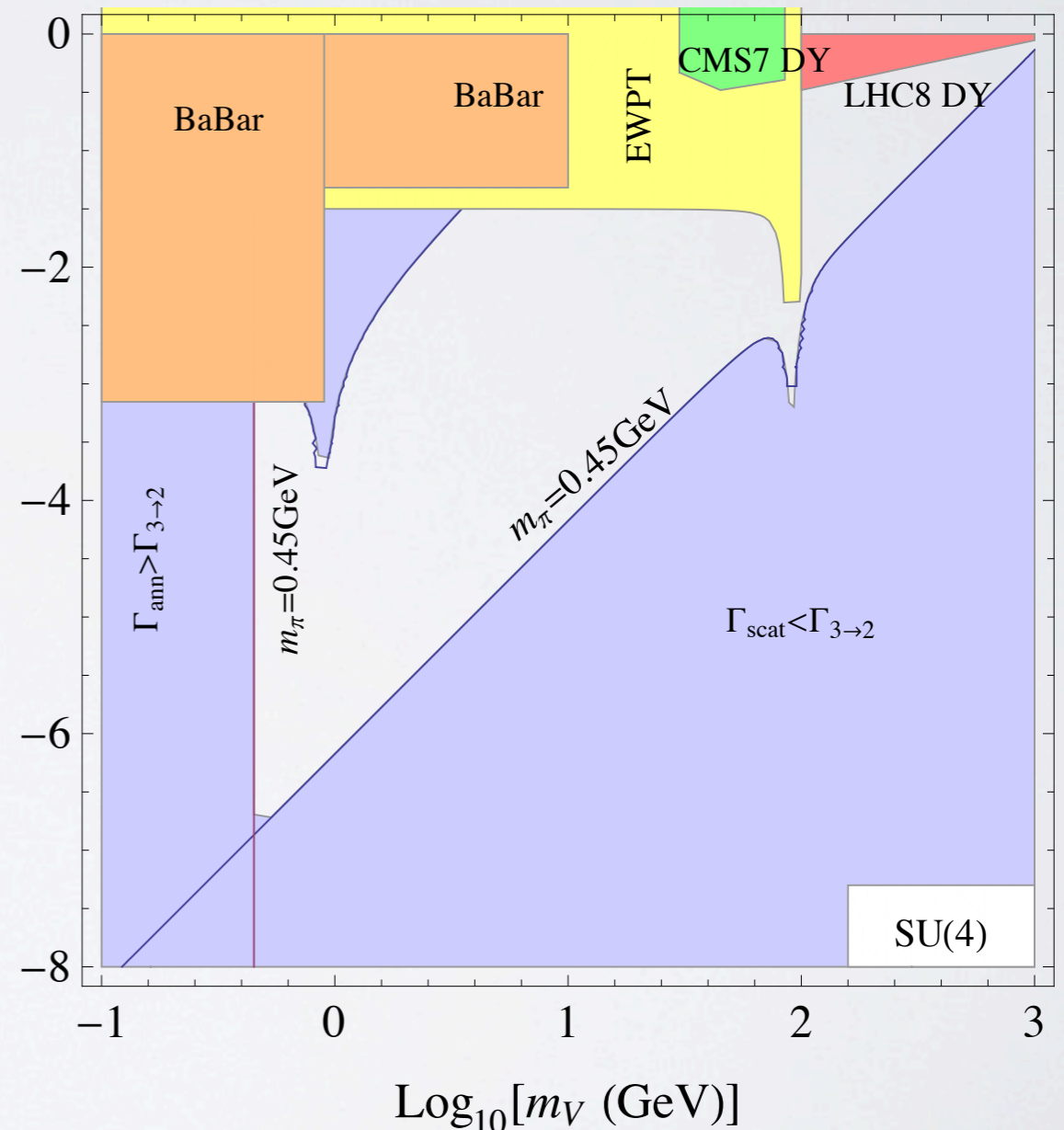
KINETICALLY MIXED U(1)

- e.g., SU(4) gauge group with Nf=3

- gauged U(1): $\begin{pmatrix} 1 & & \\ & -1 & \\ & & -1 \end{pmatrix} \text{Log}_{10}[\epsilon_\gamma]$

- kinetic mixing induced by:

$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$



[Lee, Seo 1504.00745]

AXION PORTAL

- e.g., SU(2) gauge group with 2 flavors and coupling to photons

$$\mathcal{L}_{\text{axion}} = -\frac{1}{2}m_q e^{ia/f_a} J^{ij} q_i q_j + \frac{1}{f_{a\gamma}} a F_{\mu\nu} \tilde{F}^{\mu\nu}$$



$$m_a^2 = \frac{m_\pi^2 f_\pi^2}{f_a^2}$$

AXION PORTAL

Axion portal $L = \lambda_1 a^2 \pi^2$, $\lambda_1 = \frac{m_\pi^2}{4 f_{a,\text{SIMP}}^2}$

