

Introduction

- **Heavy quarks parton distribution function** play an important role in several SM and BSM processes
 - ▶ b plus jet, associated tW , tH^+
- Standard approach of PDF analysis:
 - ▶ **DGLAP**+ boundary condition
- Purely perturbative treatment: $m_c = 1.3$ GeV? $m_b = 4.5$ GeV?
 - ▶ **Light-cone** and **meson cloud** models predict a **non-perturbative** heavy quark component
- Global analysis for **IC** by CTEQ and Jimenez-Delgado et al.
⇒ set *significantly different limits*

Motivations

Our approach

- (II) Intrinsic heavy quark evolution can be **decoupled**
 - ▶ Quantify our approximation
- (III) Fill the gap by providing **IB(IC)** PDF
 - ▶ Well suited because the normalization can be **adjusted freely**
- (IV) Study the impact of IC and IB on parton-parton luminosities at the **LHC**
 - ▶ Assess the impact on **SM** and **NP** processes

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II) Evolution of intrinsic heavy quarks

III) Intrinsic bottom PDFs

IV) Parton-parton Luminosities and intrinsic heavy quarks at the LHC 14 TeV

V) Conclusion

Evolution equation

Definition

- $Q_1(x, \mu_0) := Q(x, \mu_0) - Q_0(x, \mu_0)$,
 - ▶ in $\overline{\text{MS}}$ (only NLO), $Q_0(x, \mu_0) = 0$ if $\mu_0 = m_Q$
- Any non-zero boundary condition $Q(x, m_Q) \neq 0$ can be attributed to intrinsic component
- Light quark q , heavy quark (c or b) Q , and gluon g

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$$\dot{g} = P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q,$$

$$\dot{q} = P_{qg} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q,$$

$$\dot{Q} = P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q.$$

- $Q = Q_0 + Q_1$
 - ▶ Q_0 is the usual radiatively generated extrinsic heavy quark
 - ▶ Q_1 is the **non-perturbative** intrinsic heavy quark

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$$\begin{aligned}
 \dot{g} &= P_{gg} \otimes g + P_{gq} \otimes q + P_{gQ} \otimes Q_0 + \cancel{P_{gQ} \otimes Q_1}, \\
 \dot{q} &= P_{qg} \otimes g + P_{qq} \otimes q + P_{qQ} \otimes Q_0 + \cancel{P_{qQ} \otimes Q_1}, \\
 \dot{Q}_0 + \dot{Q}_1 &= P_{Qg} \otimes g + P_{Qq} \otimes q + P_{QQ} \otimes Q_0 + P_{QQ} \otimes Q_1.
 \end{aligned}$$

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- $(q, g, Q_0) \Rightarrow$ usual DGLAP eq. without intrinsic
 - Q_1 Standalone **non-singlet** evolution equation
 - ▶ $\dot{Q}_1 = P_{QQ} \otimes Q_1$.

Sum rule

Full-fledge analysis:

- Modified **sum rule** in global analysis:

$$\int_0^1 dx \, x \left(g + \sum_i (q_i + \bar{q}_i) + Q_0 + \bar{Q}_0 + Q_1 + \bar{Q}_1 \right) = 1.$$

- Allowing for a small **violation** of the sum rule we can completely decouple the analysis of **intrinsic heavy quarks**

$$\Rightarrow \left\{ \begin{array}{l} \bullet \text{ Can take } \mathbf{\text{any PDF set}} \text{ for } (q, g, Q_0) \\ \bullet \text{ Add the standalone intrinsic heavy quark} \end{array} \right.$$

- Violation of the sum rule: $\int_0^1 dx \, x \, (Q_1 + \bar{Q}_1)$

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Different matching conditions

BHPS Intrinsic charm:

$$c_1(x) = \bar{c}_1(x) \propto x^2[6x(1+x)\ln x + (1-x)(1+10x+x^2)]$$

- **Normalization** and **precise energy scale** are not specified

- *b*-quark expected to be **very similar** with **normalization suppressed** $m_c^2/m_b^2 \simeq 0.1$

- Matching scale is “unknown”:

$$\begin{aligned} \triangleright b_1(x, m_b) &= \frac{m_c^2}{m_b^2} c_1(x, m_c) \\ \triangleright b_1(x, m_c) &= \frac{m_c^2}{m_b^2} c_1(x, m_c) \Rightarrow \text{our ansatz} \end{aligned}$$

- **Remains valid** at all scales

- Note that **asymmetric boundary conditions**, $c_1(x) \neq \bar{c}_1(x), b_1(x) \neq \bar{b}_1(x)$ could be accommodated (like in meson cloud models)

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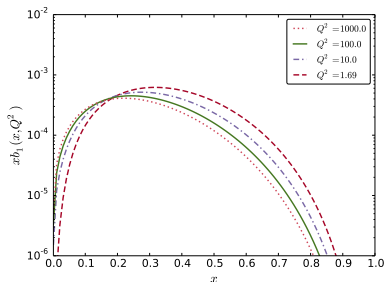
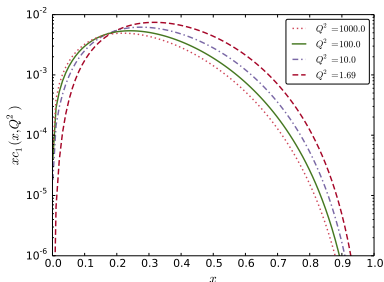
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$c_1(x)$, $b_1(x)$ @NLO

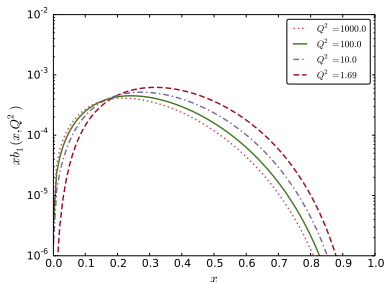
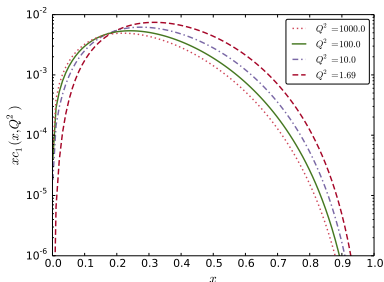
- $b_1(x, m_c) = \frac{m_c^2}{m_b^2} c_1(x, m_c)$, $\int_0^1 c_1(x) = 0.01$, $m_c = 1.3$ GeV,
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- The normalization can be changed by **simple rescaling**

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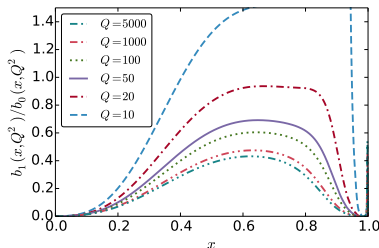
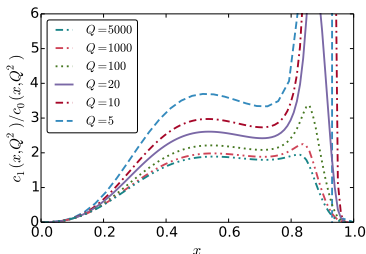
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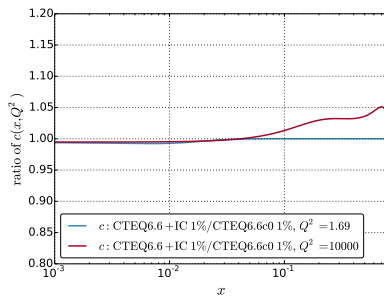
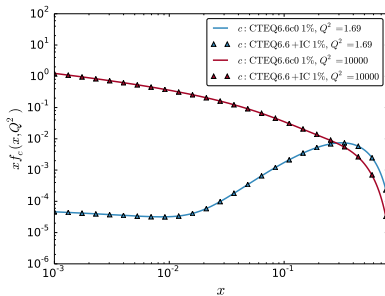
$c_1(x)$, $b_1(x)$ @NLO

- Modifications in **BHPS** models are essentially at **large- x**
- IB effects less **pronounced**:
 - ▶ Still, observables dominated by b initiated processes could be enhanced by a factor up to ~ 1.6
 - ▶ For constraining intrinsic bottom \Rightarrow low Q and high- x e.g. AFTER@LHC



Goodness of the approximation

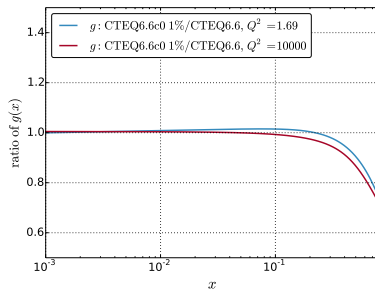
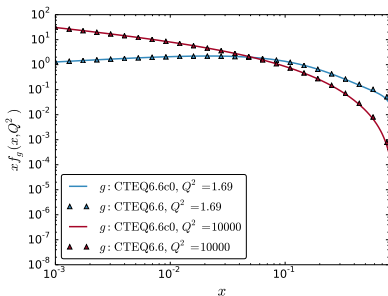
- Comparison of $c_1(x) + \text{CTEQ6.6}$ and $c(x)$ of CTEQ6.6c0 with the **same normalization**
 - ▶ $\int_0^1 dx c(x) = 0.01$
 - ▶ $\int_0^1 dx x [c(x) + \bar{c}(x)] = 0.0057$
- **Charm-quark** with 1% normalization



- The error is under control and reaches at worst 5%.

Goodness of the approximation

- Comparison of $g(x)$ of CTEQ6.6 and $g(x)$ of CTEQ6.6c0 with 1% normalization



- The error is larger at high x but the gluon is very small and the uncertainties large in this region.

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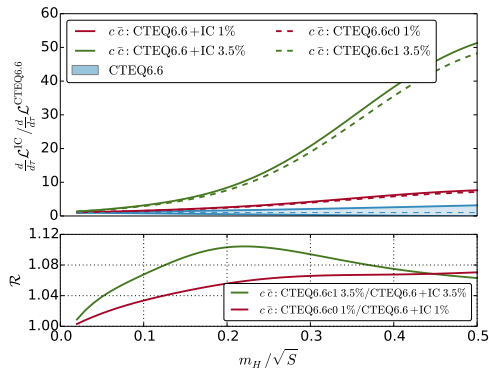
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Definition

$$\frac{d\mathcal{L}_{ij}}{d\tau}(\tau, \mu) = \frac{1}{1+\delta_{ij}} \int_{\tau}^1 \frac{dx}{x} \left[f_i(x, \mu) f_j(\tau/x, \mu) + (i \leftrightarrow j) \right]$$

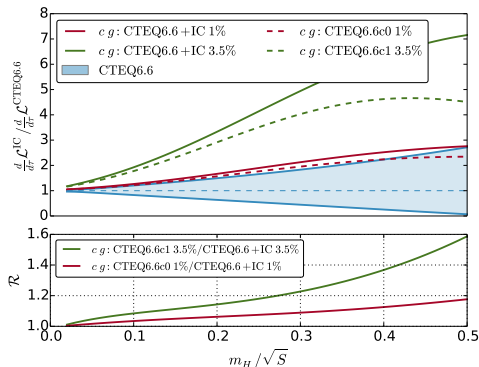
- Validity of the approximation on the Luminosities:



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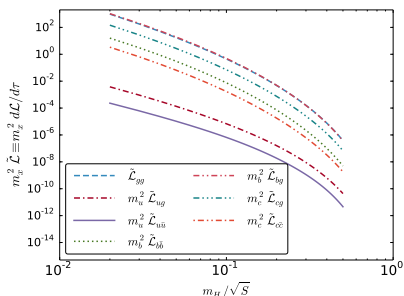
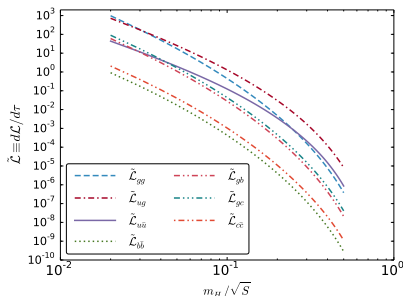


- Note that for the intrinsic bottom the error is **smaller**

Luminosities @ the LHC14 TeV

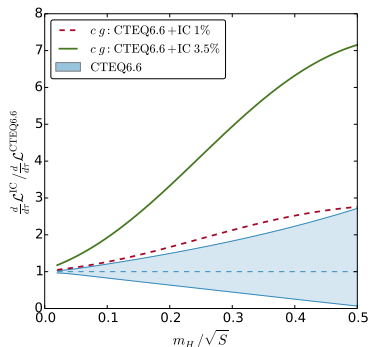
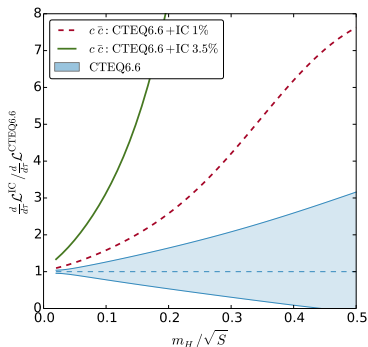
Production of a heavy state

$$\sigma_{pp \rightarrow H+X} = \sum_{ij} \int_{\tau}^1 d\tau \frac{d\mathcal{L}_{ij}}{d\tau} \hat{\sigma}_{ij}(s), \quad \sqrt{\tau} = m_H/\sqrt{S}$$

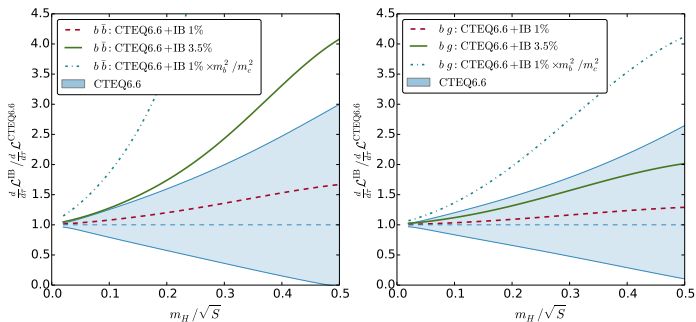


- E.g. a **heavy scalar** with couplings proportional to the **fermion mass**: m_c^2/m_b^2 factor compensated

■ $\sqrt{\tau} = m_H/\sqrt{S}$



- The impact of the intrinsic charm is clearly visible and outside the uncertainty band from PDF for both $c\bar{c}$ and cg .



- Also include an *extreme* scenario with the **first moment** of IB at 1%.
- Effects smaller than for IC as expected
- 3.5% normalization is distinguishable

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- Intrinsic heavy quarks can be decoupled \Rightarrow **non-singlet** evolution
 - ▶ Can generate matched **IC/IB** distributions for any PDF set **without** re-doing a global analysis
 - ▶ The normalization can be chosen **freely**
- The Approximation holds to a **very good** level for all relevant applications:
 - ▶ For **IB**, it is very good
 - ▶ For **IC**:
 - (i) 1-2% normalization \Rightarrow error smaller than **PDF uncertainty** at large- x
 - (ii) For **larger norms**, the error **grows** but the effect also such that it can easily be separated from the *without IC case*.
- Need a low Q large- x machine to constrain IB
 - ▶ Electron Ion Collider (EIC)
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- the c PDF of CTEQ66.c0 goes negative at large- x small Q

