

QCD to NNLO... and beyond!

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NORTHWESTERN
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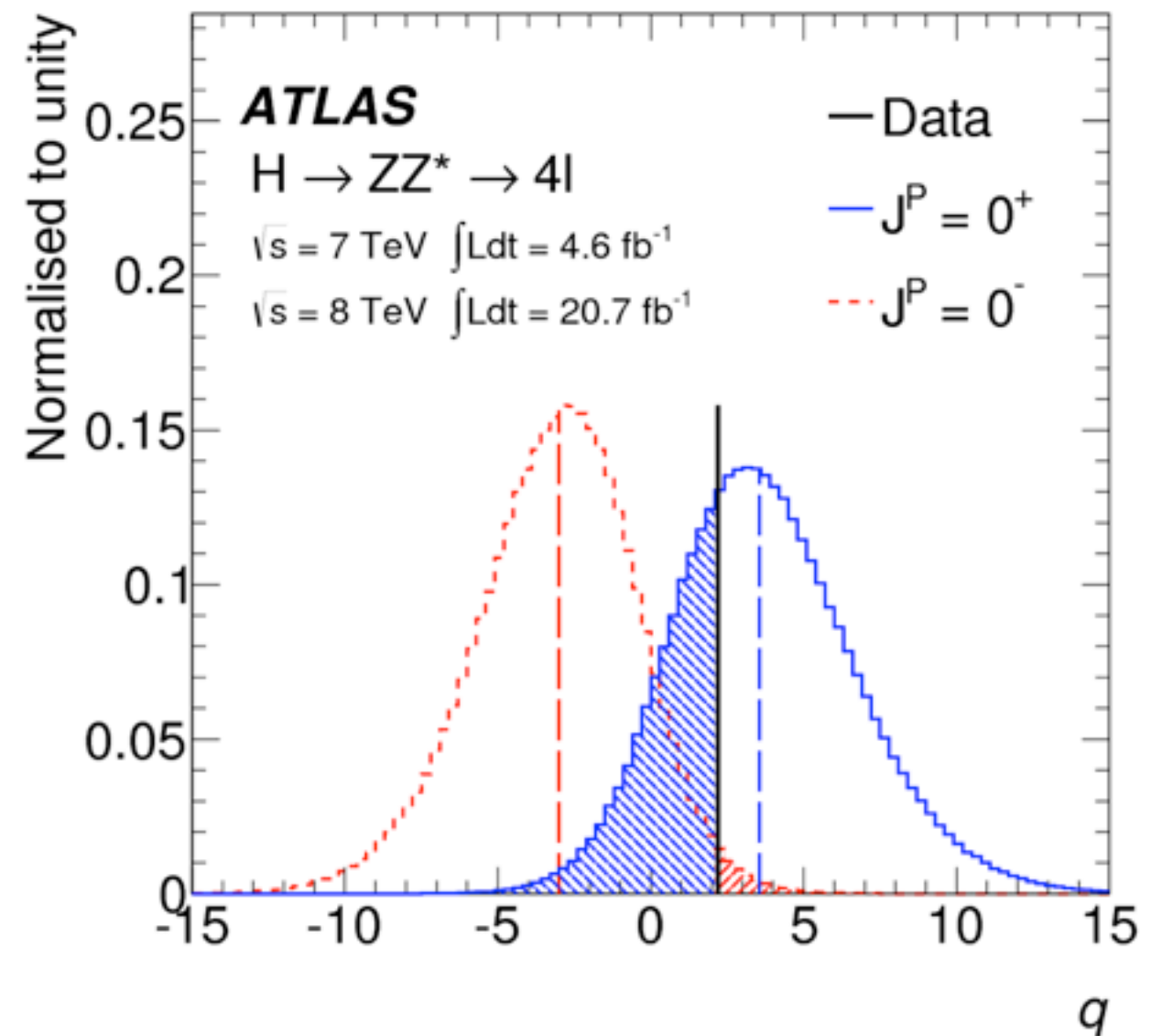
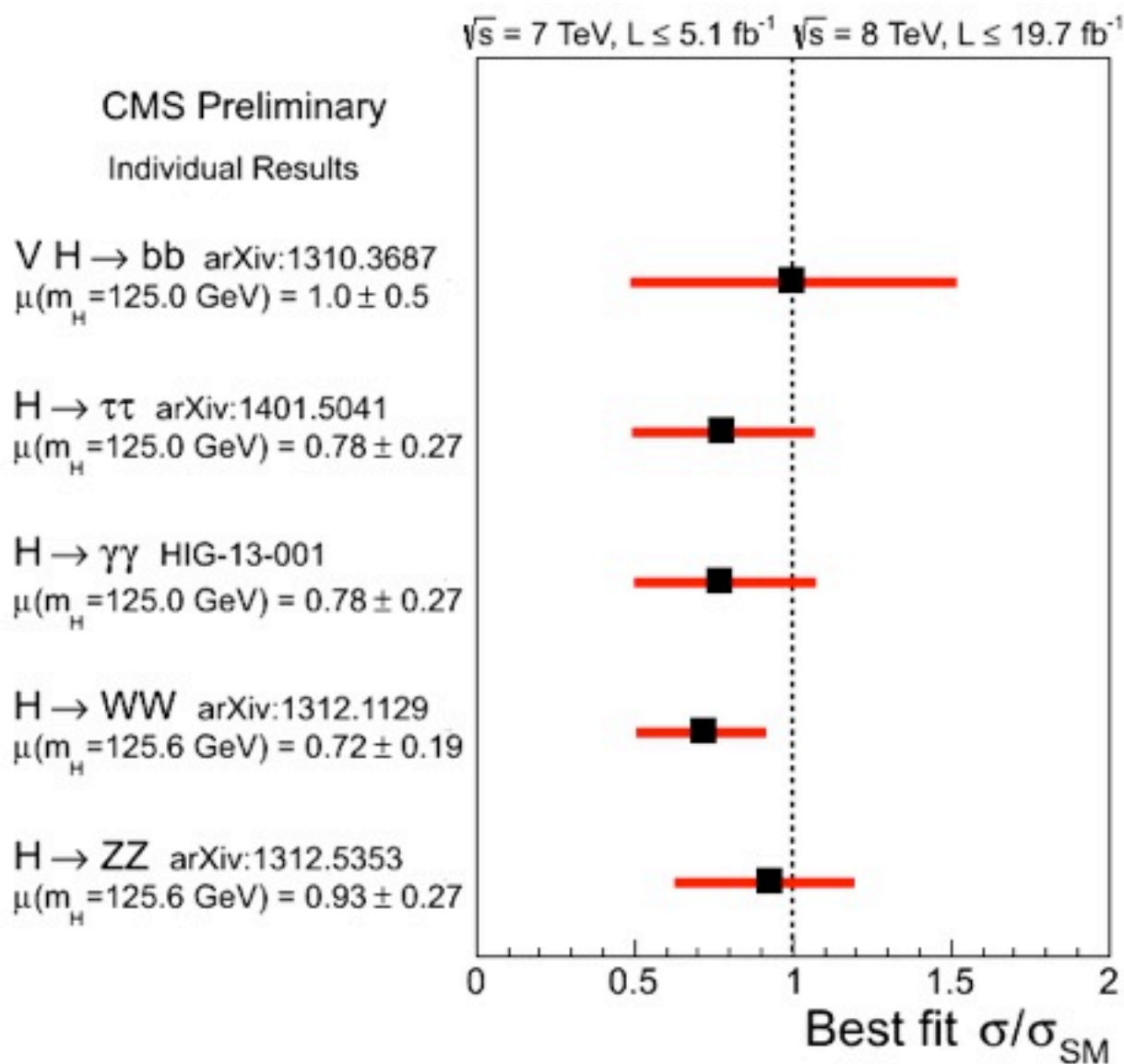


Outline

- Overview and the motivation for precision QCD
- QCD at NLO and W +many jets
- The role of NNLO QCD at the LHC
- Precision jet phenomenology
- Jet binning to all-orders and the Higgs
- The curious case of the Z +1-jet exclusive cross section

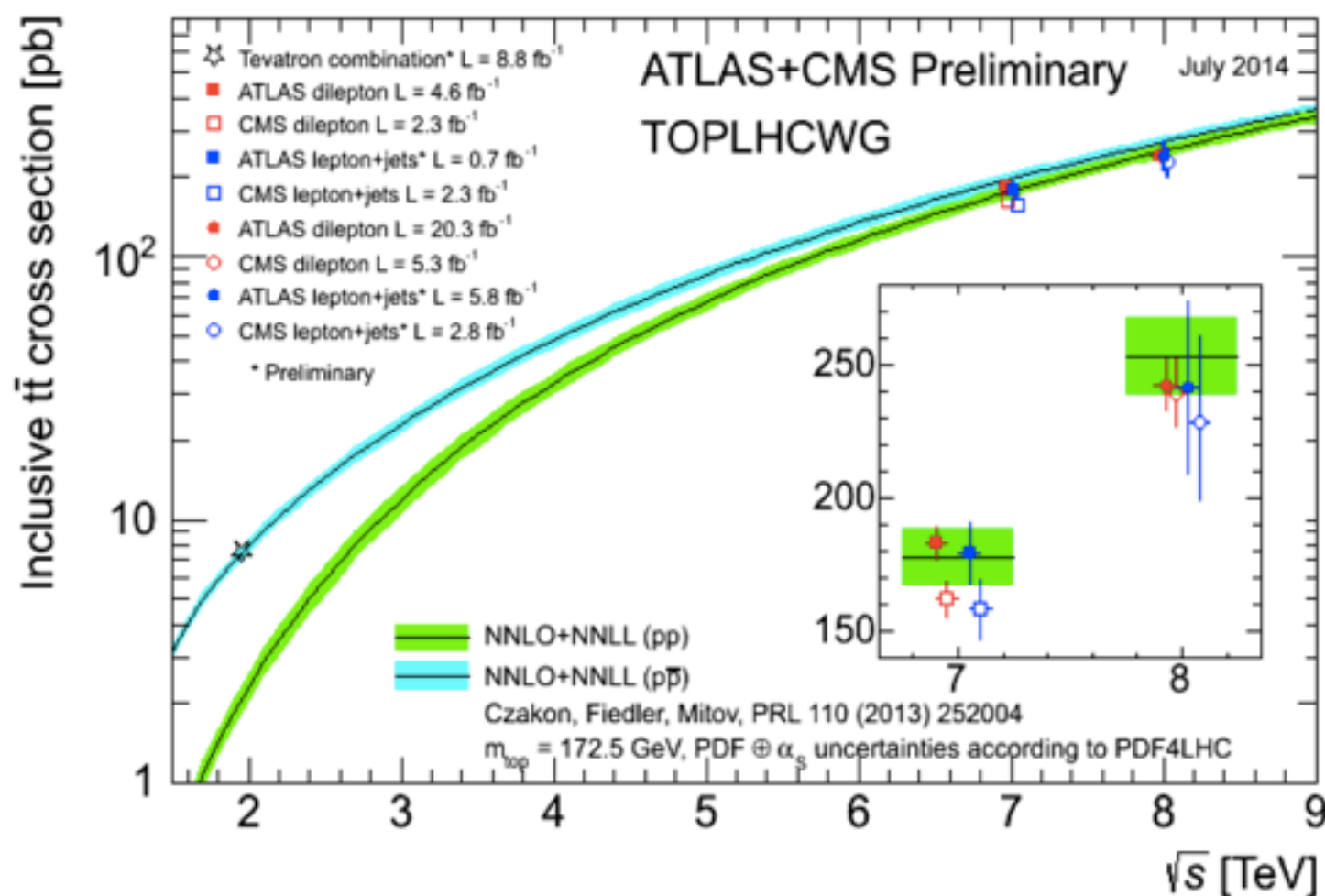
What have we learned from LHC Run I?

- We have a Higgs boson! It is a predominantly 0^+ state whose couplings agree roughly with SM predictions



What have we learned from LHC Run I?

- The $t\bar{t}$ cross section is known at NNLO (Czakon, Fiedler, Mitov I303.6254) and is in good agreement with data; the error on the mass is below a GeV



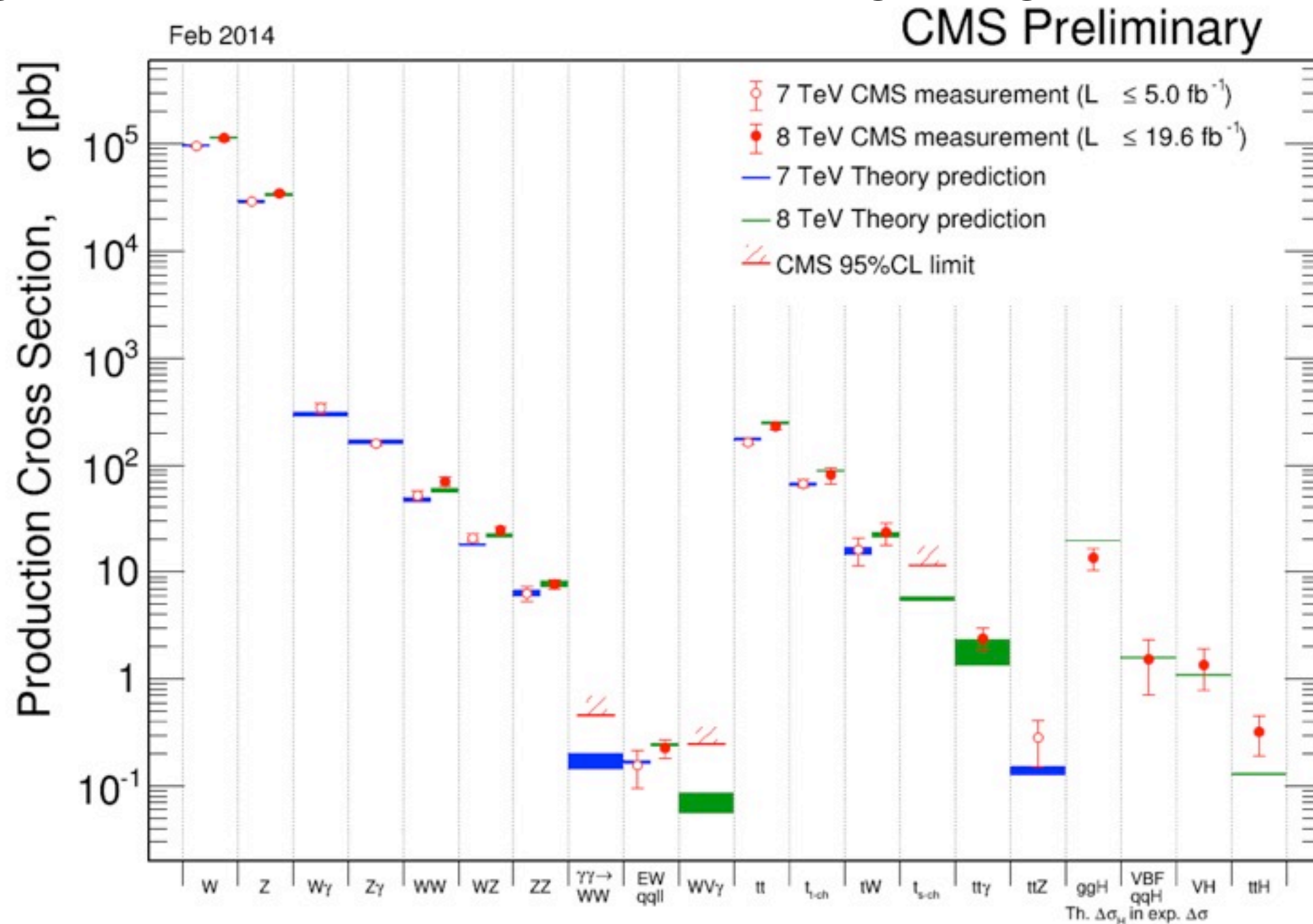
| | Tevatron | | LHC 8 TeV | |
|-----------|----------|------|-----------|------|
| Precision | D0 | CDF | ATLAS | CMS |
| total | 7.8% | 6.5% | 4.3% | 5.5% |
| stat | 2.6% | 4.0% | 0.7% | 0.8% |
| syst | 4.3% | 4.7% | 2.3% | 4.7% |
| lumi | 6.1% | 2.0% | 3.1 % | 2.6% |

$$m_{\text{top}} = 173.34 \pm 0.27 \text{ (stat)} \pm 0.24 \text{ (iJES)} \pm 0.67 \text{ (syst) GeV}$$

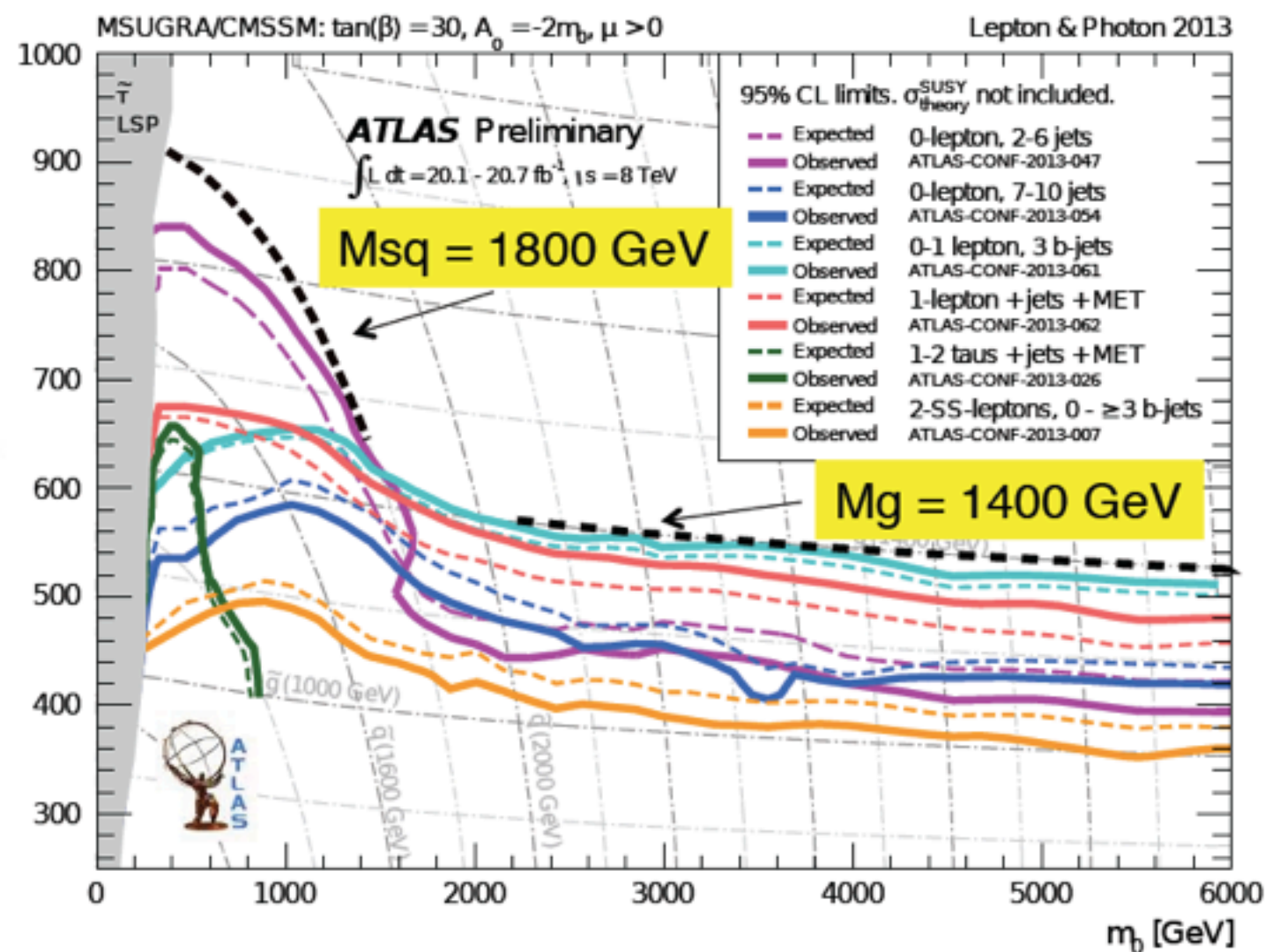
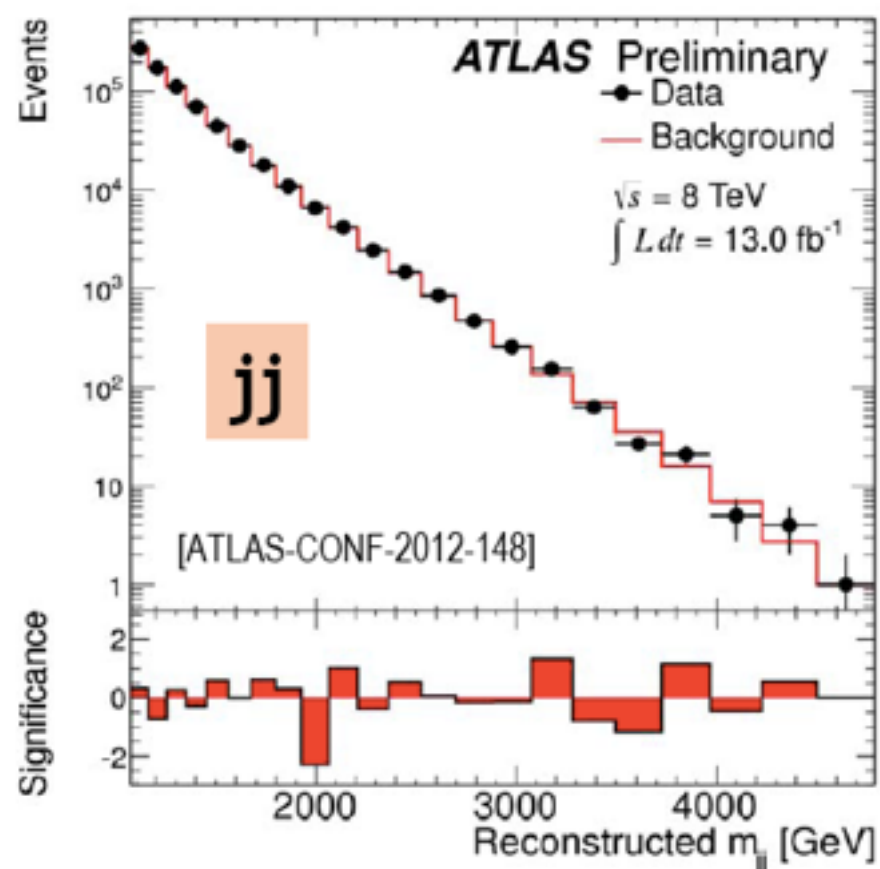
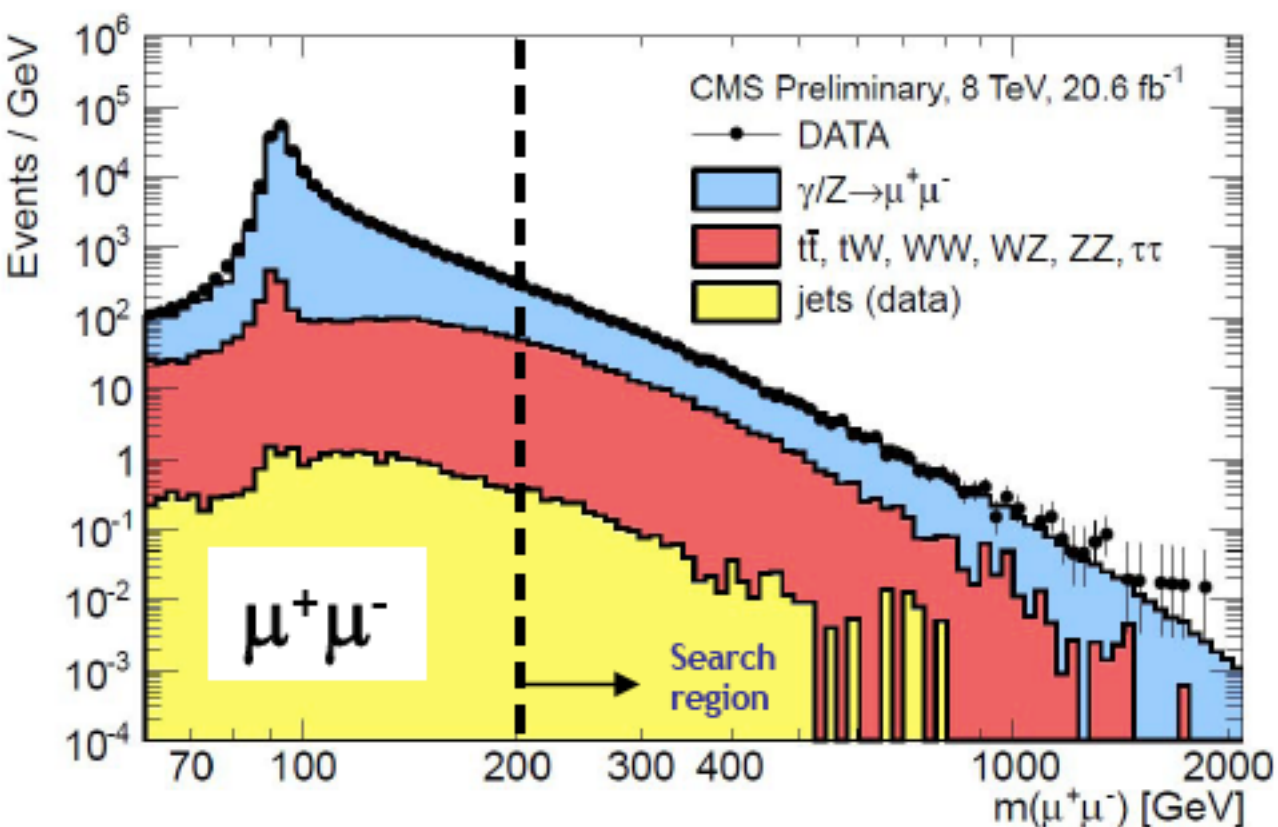
Combination from I403.4427

What have we learned from LHC Run I?

- EW gauge boson production cross sections spanning six orders of magnitude have been measured, and are in good agreement with theory



Global summary of high- p_T Run I results



- Nothing found besides the Higgs; limits reaching multi-TeV in some channels

A photograph of a desert landscape featuring rolling sand dunes. The dunes are covered in fine, wavy ripples of sand. The sky is a clear, vibrant blue with a few wispy white clouds. The lighting suggests a bright, sunny day, with shadows cast across the dunes.

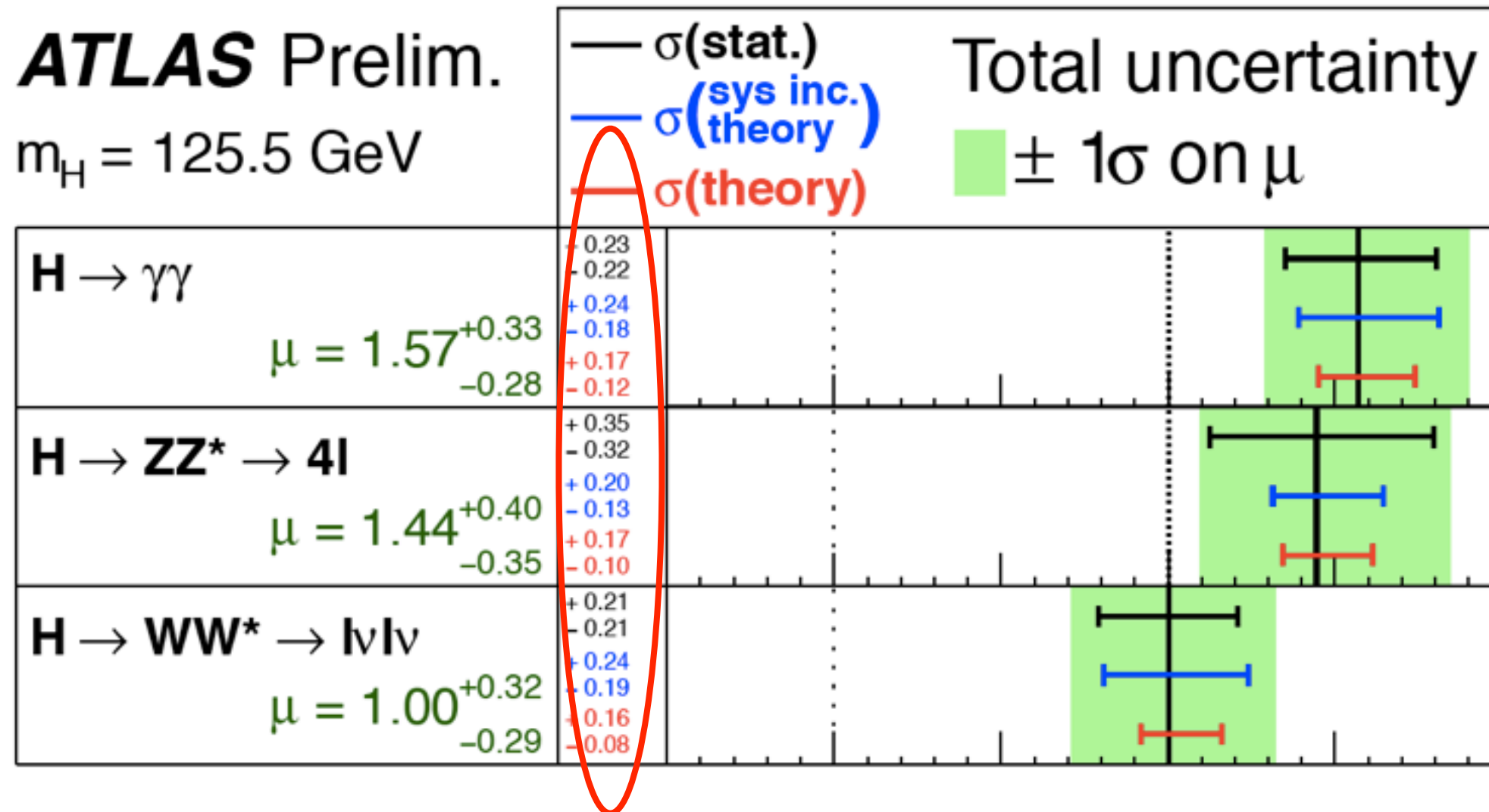
Everything we've measured so far is consistent with the following picture of fundamental physics at a few/tens of TeV



- There can be fascinating life hidden in a desert!
- We must be ready for the challenge if there is no obvious discovery at Run II
- There can be fascinating life hidden in a desert... but it can be rare and difficult to find

Precision physics may be the path to an oasis in the desert!

Precision and the Higgs



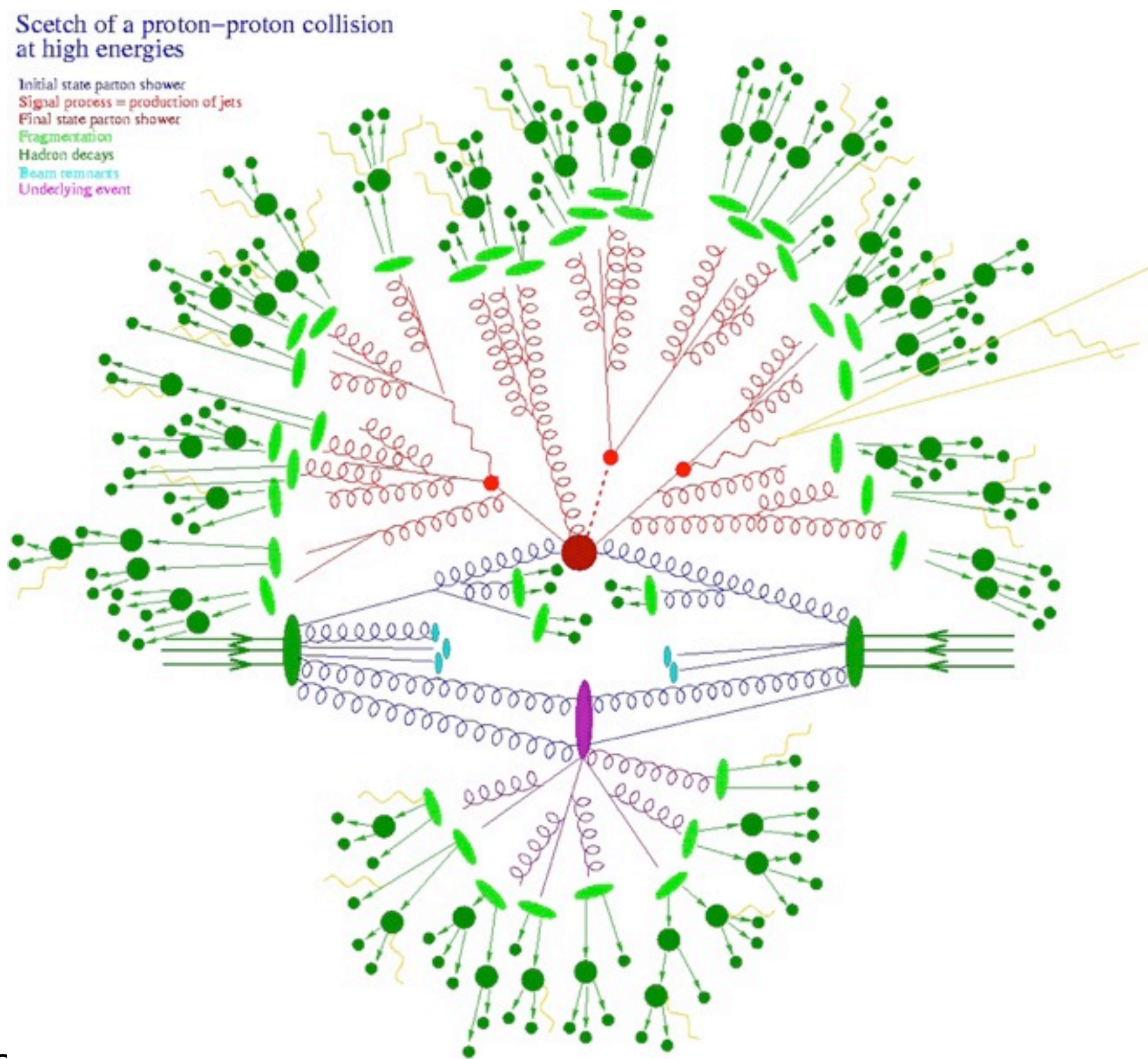
- The dominant component of the systematic error on the signal strength is theory.
- This will become a limiting factor in interpretation in Run II as statistical errors decrease.

Need better theory to sharpen our probes of BSM physics
 in the Higgs sector!

QCD at the LHC

Sketch of a proton-proton collision at high energies

Initial state parton shower
Signal process = production of jets
Final state parton shower
Fragmentation
Hadron decays
Beam remnants
Underlying event




- Theory at hadron colliders is driven by our understanding of **QCD**
- How does theory allows us to peer into the inner “hard-scattering” in this mess?


Factorization: divide and conquer

$$\sigma_{h_1 h_2 \rightarrow X} = \int dx_1 dx_2 \underbrace{f_{h_1/i}(x_1; \overbrace{\mu_F^2}^{\text{factorization scale}}) f_{h_2/j}(x_2; \mu_F^2)}_{PDFs} \underbrace{\sigma_{ij \rightarrow X}(x_1, x_2, \mu_F^2, \{q_k\})}_{\text{partonic cross section}} + \underbrace{\mathcal{O}\left(\frac{\Lambda_{QCD}}{Q}\right)^n}_{\text{power corrections}}$$

Collins, Soper, Sterman (1988)

Factorization: divide and conquer

How do we get a quark/gluon from the proton?
 Non-perturbative but *universal*; measure at
 HERA, Tevatron, etc.  Alberto Accardi's talk

factorization scale 

$$\sigma_{h_1 h_2 \rightarrow X} = \int dx_1 dx_2 \underbrace{f_{h_1/i}(x_1; \mu_F^2) f_{h_2/j}(x_2; \mu_F^2)}_{PDFs} \underbrace{\sigma_{ij \rightarrow X}(x_1, x_2, \mu_F^2, \{q_k\})}_{\text{partonic cross section}} + \underbrace{\mathcal{O}\left(\frac{\Lambda_{QCD}}{Q}\right)^n}_{\text{power corrections}}$$

Collins, Soper, Sterman (1988)

Calculate! $\sigma = \sigma^{(0)} + \frac{\alpha_s}{\pi} \sigma^{(1)} + \left(\frac{\alpha_s}{\pi}\right)^2 \sigma^{(2)}$

Leading-order (LO)

Next-to leading-order (NLO)

Next-to-next-to leading-order (NNLO)

+parton shower  Frank Siegert's talk

or even N³LO for Higgs!

 Stefano Forte's talk

Multi-jet QCD at NLO

QCD@NLO

- Well-honed techniques for calculating and combining real+virtual at NLO

Simple enough to integrate analytically so that $1/\epsilon$ poles can be cancelled against virtual corrections

$$d\sigma_{NLO} = \int_{d\Phi_{m+1}} (d\sigma_{NLO}^R - d\sigma_{NLO}^S) + \left[\int_{d\Phi_{m+1}} d\sigma_{NLO}^S + \int_{d\Phi_m} d\sigma_{NLO}^V \right]$$

Approximates real-emission matrix elements in all singular limits so this difference is numerically integrable

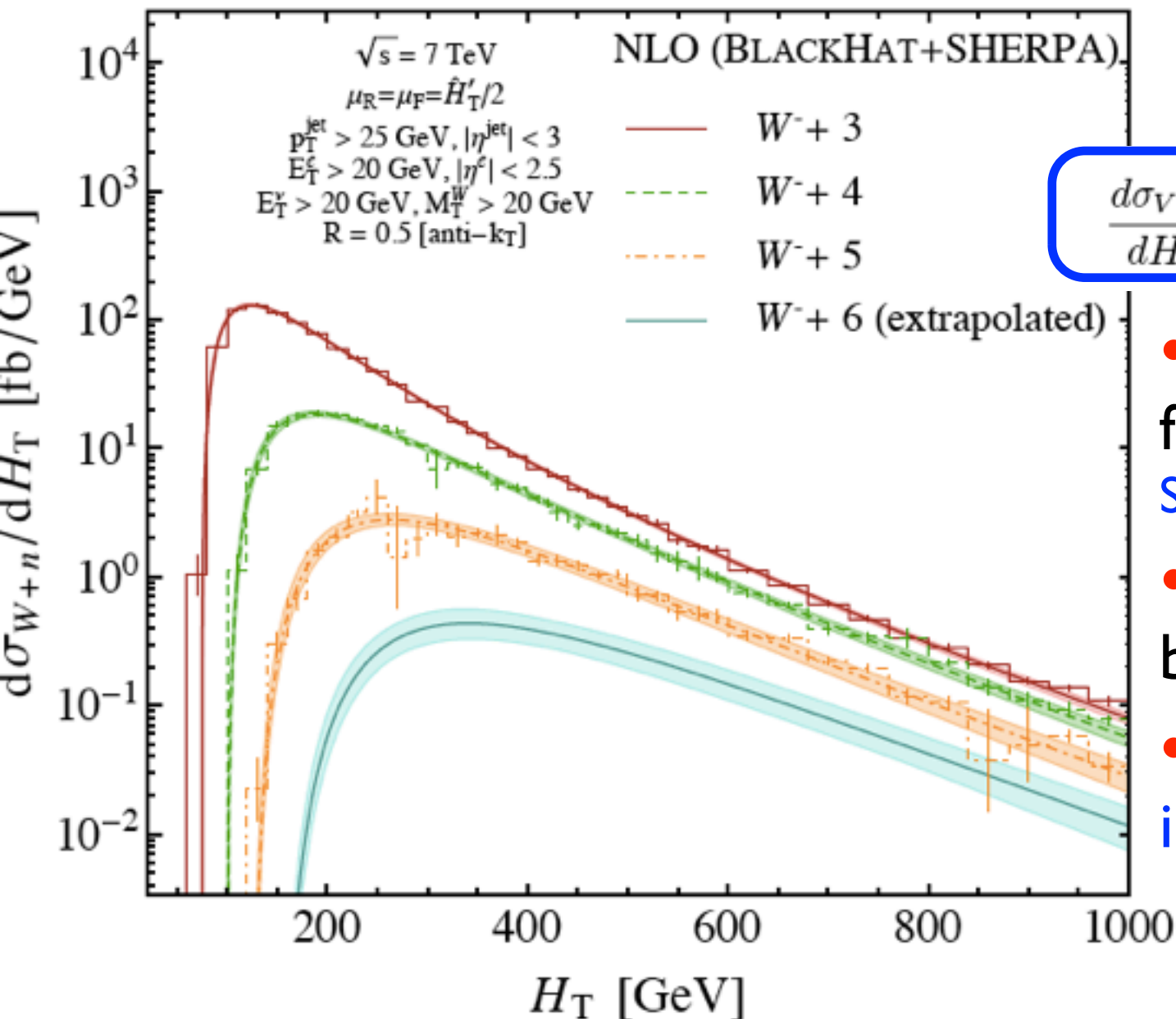
- Can use dipole subtraction ([Catani, Seymour 1996](#)); FKS subtraction ([Frixione, Kunszt, Signer 1996](#))
- Implemented in several dedicated codes [Autodipole](#), [Helac](#), [MadDipole](#), [MadFKS](#), [Sherpa](#), [TeVJet](#)
- Virtual corrections obtained as coefficients times 1-loop scalar integrals

$$A = \sum d_i \text{[box diagram]} + \sum c_i \text{[triangle diagram]} + \sum b_i \text{[bubble diagram]} + R$$

- Several semi-numerical codes exist for high-multiplicity final states ($2 \rightarrow 4$ or more) : [BlackHat](#), [GoSam](#), [HelacNLO](#), [MadLoop](#), [NJet](#), [OpenLoops](#), [Rocket](#)
- Programs with analytic representations of the amplitudes (such as MCFM) remain extremely important for speed/efficiency, and as input to NNLO

Recent NLO phenomenology

- W+2 through 5 jets known to NLO (higher-multiplicity process via BLACKHAT+SHERPA). Can these be used to predict even higher multiplicities?



$$\frac{d\sigma_{V+n}}{dH_T} = (2a_s(H_T/2))^n f^H(H_T) N_n^H \ln^{\tau_n^H} \rho_{H,n} (1 - H_T/H_T^{\text{max}})^{\gamma_n^H}$$

- Such universal behavior can be argued formally for some observables [Gerwick, Schichtel 1412.1806](#)
- Validate fit methodology on $n=2-5$ before extrapolation to six jets
- Will help control backgrounds to BSM in multi-jet final states

[Bern, Dixon, Febres Cordero, Hoeche, Kosower, Ita, Maitre 1412.4775](#)

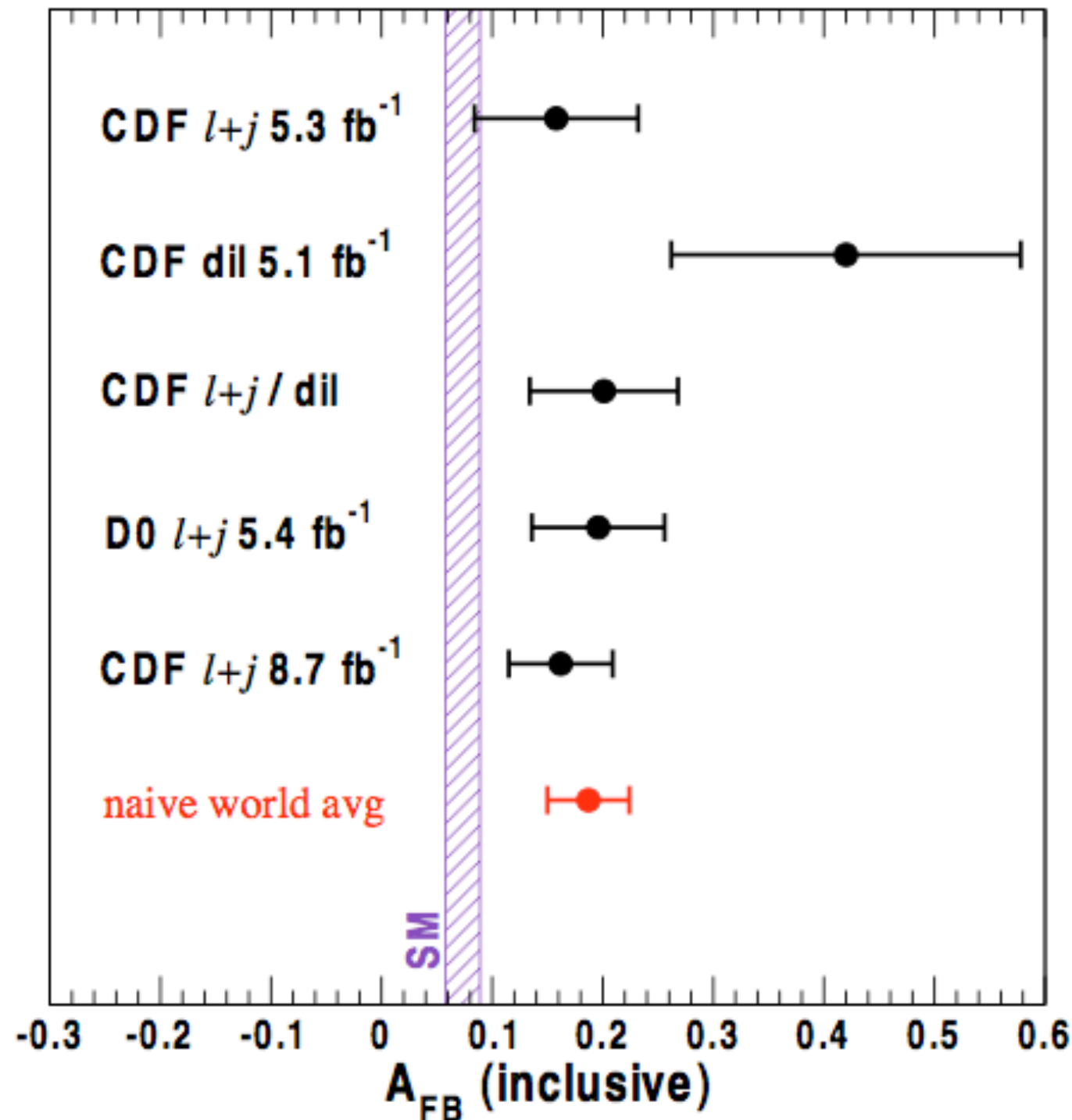
NNLO QCD at hadron colliders

- From Merriam-Webster:

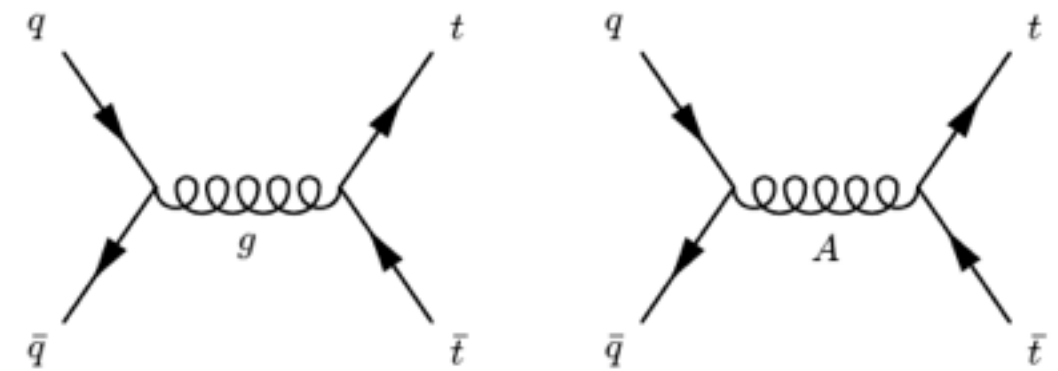
spoil·sport *noun* \ˈspɔɪ(-ə)l-,spɔrt\
: someone who spoils other people's fun or enjoyment

The $t\bar{t}$ asymmetry

- For several years the forward-backward asymmetry of top quarks measured at the Tevatron has differed from SM predictions



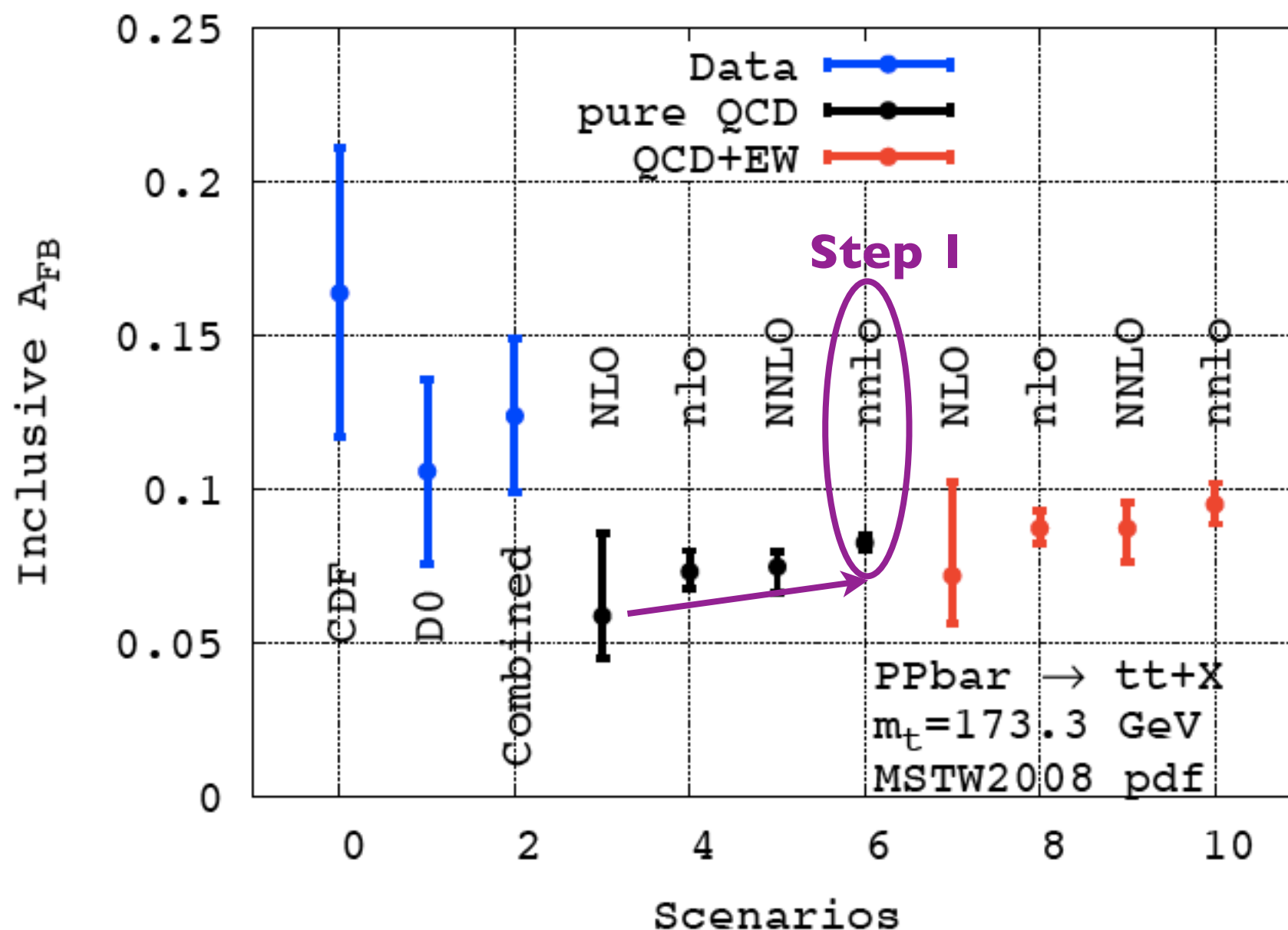
Could it be a light axigluon?



(many authors)

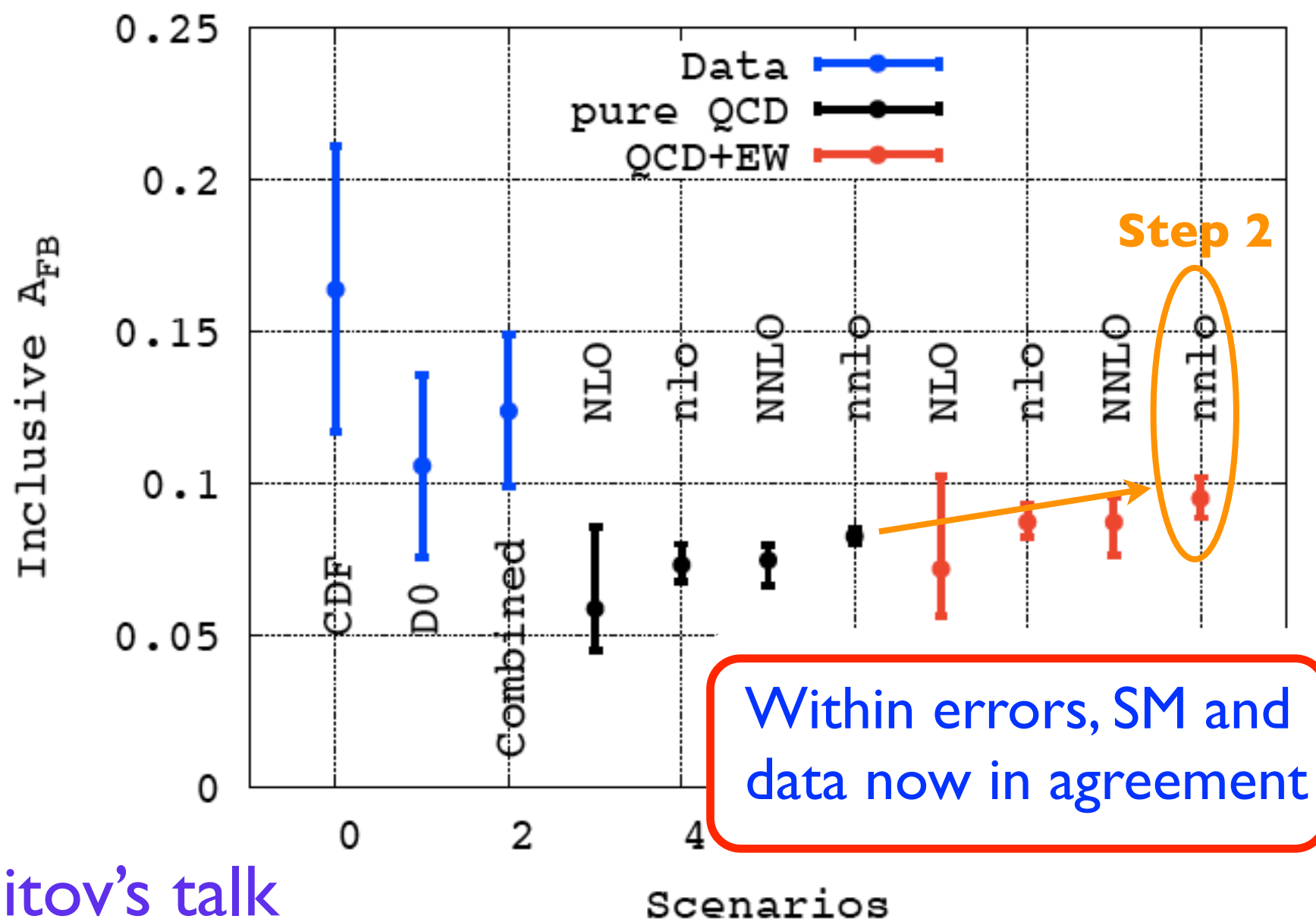
The $t\bar{t}$ asymmetry now

- Large NNLO QCD corrections! Not predicted by soft-gluon resummation, required a genuine NNLO prediction (Czakon, Fiedler, Mitov 1411.3007)



The $t\bar{t}b\bar{b}$ asymmetry now

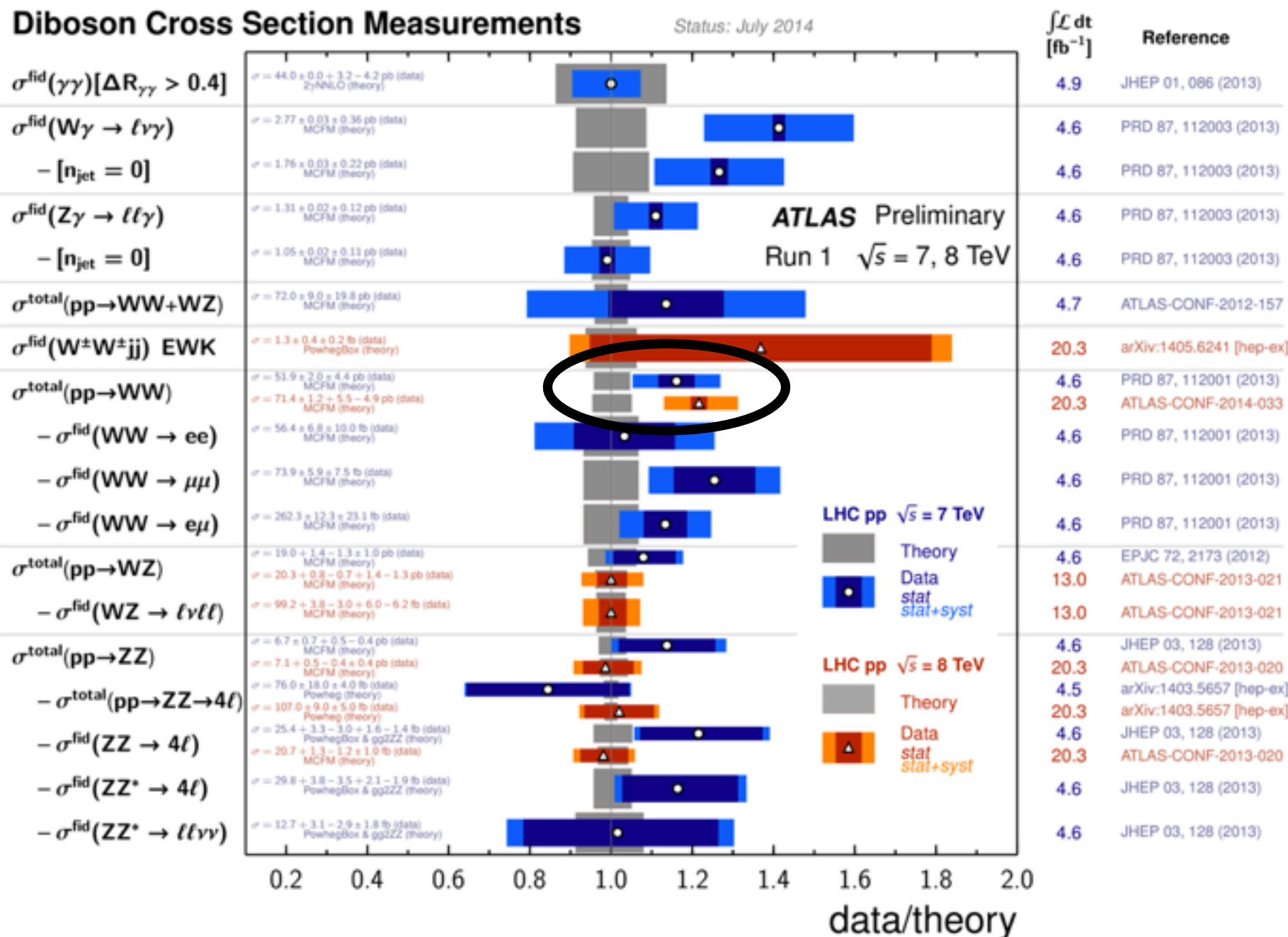
- **Large electroweak corrections!** QED generates an asymmetry via the same mechanism as QCD (Hollik, Pagani 1107.2606; Kuhn, Rodrigo 1109.6830)



see Alex Mitov's talk

The WW cross section

- Disagreement between the measured WW cross section and NLO theory seen by both ATLAS and CMS, at both 7 and 8 TeV

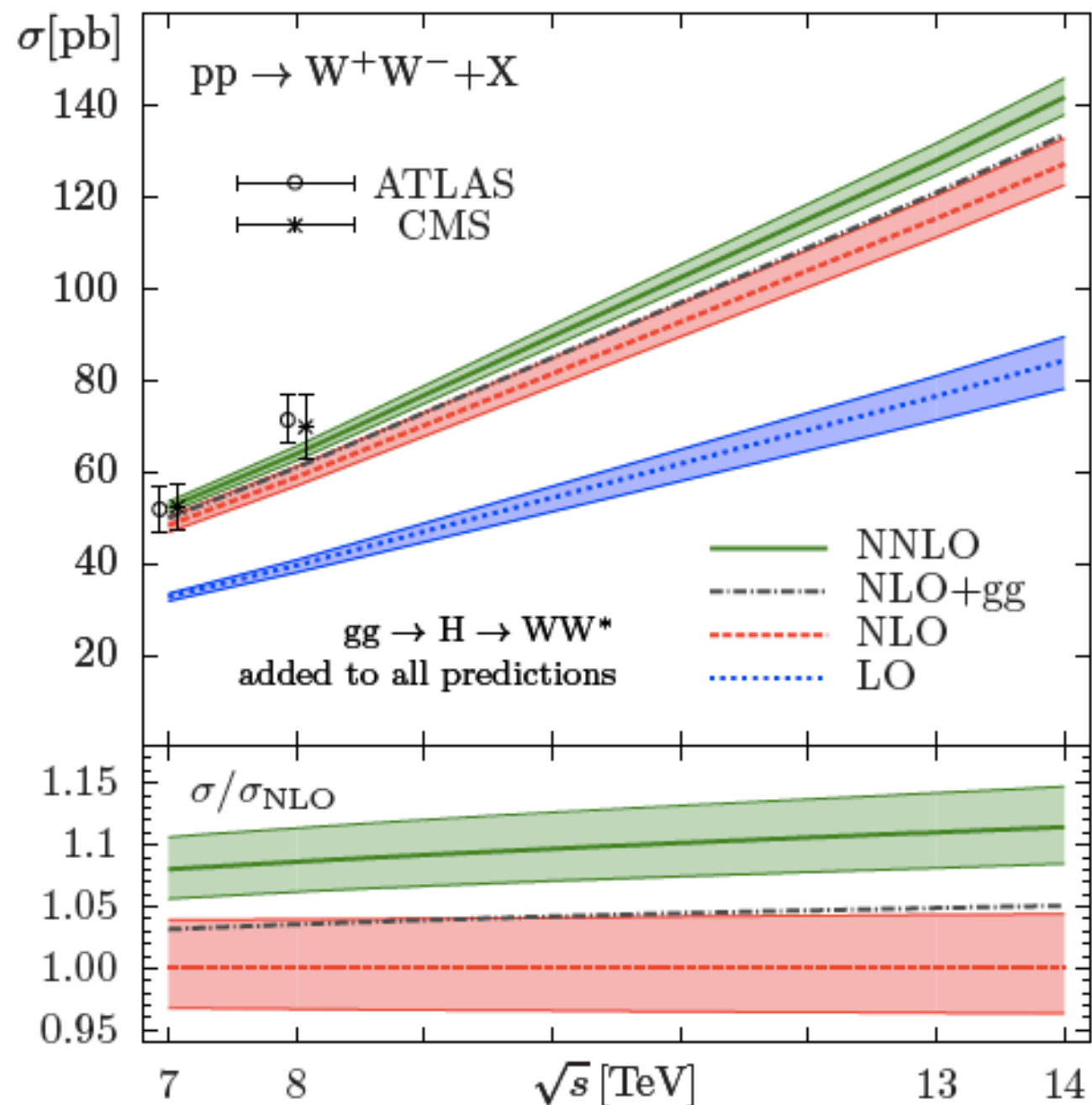


Could it be light charginos?
(Curtin, Jaiswal, Meade 1206.6888, and others)

The WW cross section now

- **Sizable NNLO QCD corrections!** Theory within 1σ agreement of ATLAS and CMS for both CM energies

Gehrmann, Grazzini, Kallweit, Maierhofer, von Manteuffel, Pozzorini, Rathlev, Tancredi 1408.5243

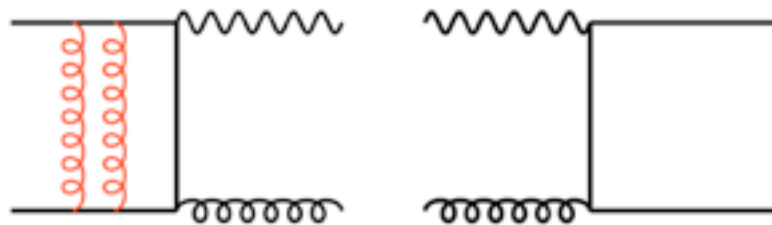


- Enhancement of theory is expected when the extrapolation from the fiducial region is properly modeled, further improving agreement

Monni, Zanderighi 1410.4745 (see also Jaiswal, Okui, 1407.4537; Curtin, Meade, Tien 1406.0848)

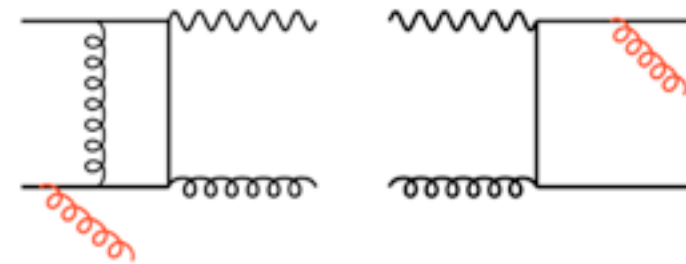
Ingredients at NNLO

2-loop matrix elements, m partons



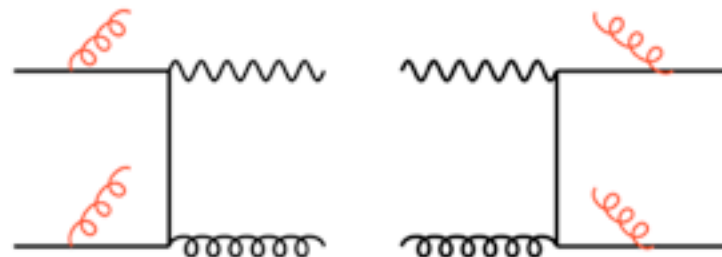
- **Explicit** IR poles from loop integrals

1-loop matrix elements, $m+1$ partons



- **Explicit** IR poles from loops
- **Implicit** IR poles from single unresolved radiation

Tree level matrix elements, $m+2$ partons



- **Implicit** IR poles from double unresolved radiation

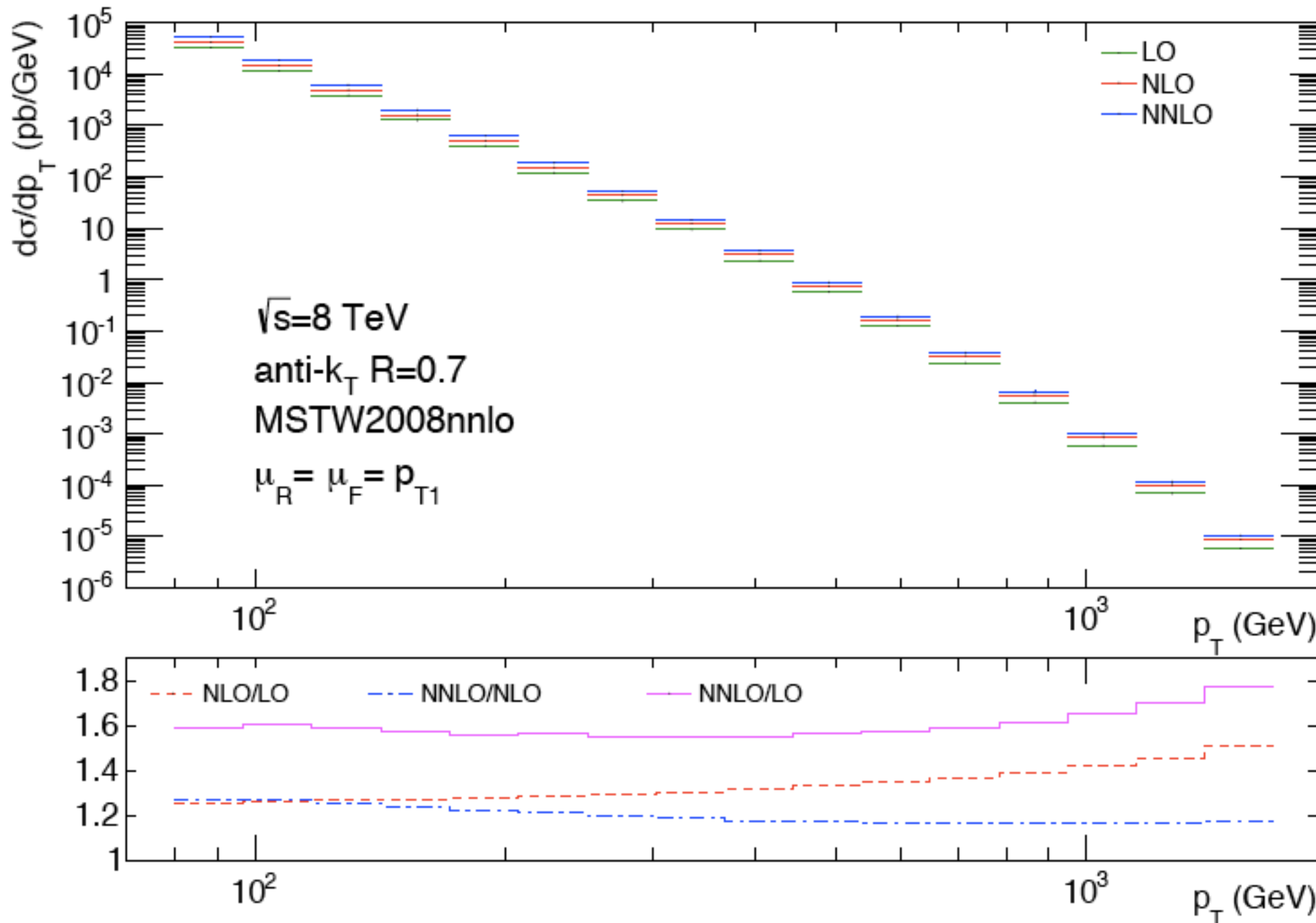
- Need a subtraction scheme to account for all singular configurations, like at NLO
- Understanding how to parameterize and integrate the subtraction terms much more difficult at NNLO

The next frontier: NNLO for light jets

- Until recently, only colorless initial states or colorless (or massive, such as $t\bar{t}$) final states were known at the differential level to NNLO using available techniques
 - Sector decomposition: Anastasiou, Melnikov, FP
 - q_T -subtraction: Catani, Grazzini
- Three methods have been extended to allow for NNLO corrections to jets at hadron colliders:
 - Antennae subtraction: Gehrmann, Gehrmann-deRidder, Glover
 - Sector-improved subtraction: Czakon; Boughezal, Melnikov, FP
 - Jettiness subtraction: Boughezal, Focke, Liu, FP
- The past couple of years have seen the emergence of NNLO jet phenomenology, in time for Run II!

Inclusive jets at NNLO

- Important for high-x gluon; uses antennae subtraction, initial gluons only

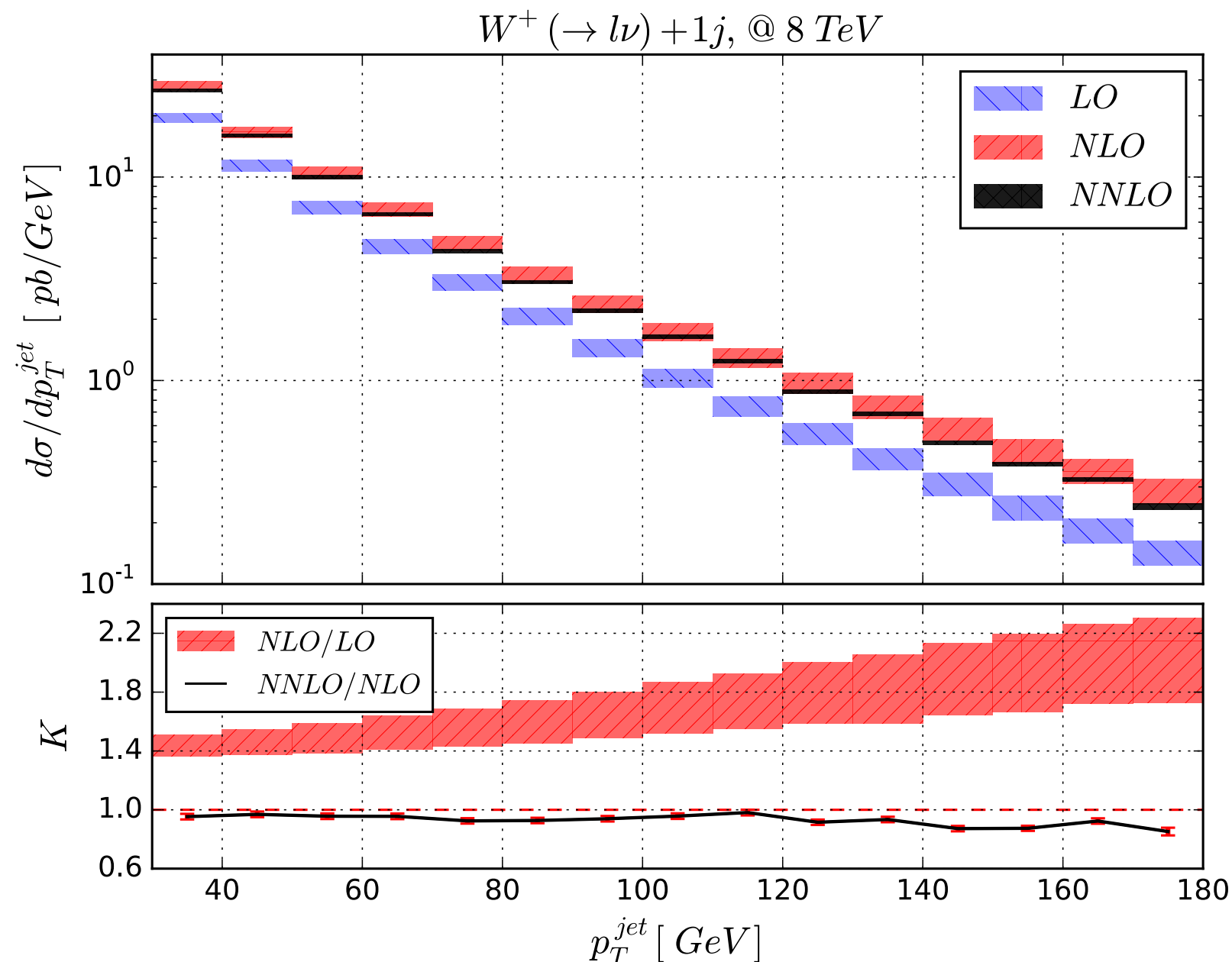


- 20% corrections beyond NLO, flat as a function of p_T
- Needed to control backgrounds to high-mass searches in Run II

Currie, Gehrmann-De Ridder, Glover, Pires
1310.3993

W+jet at NNLO

- **Jettiness subtraction**: resummation of jettiness allows a NNLO subtraction scheme to be constructed, similar to q_T -subtraction for colorless final states



$$\mathcal{T}_N = \sum_k \min_i \left\{ \frac{2p_i \cdot q_k}{Q_i} \right\}$$

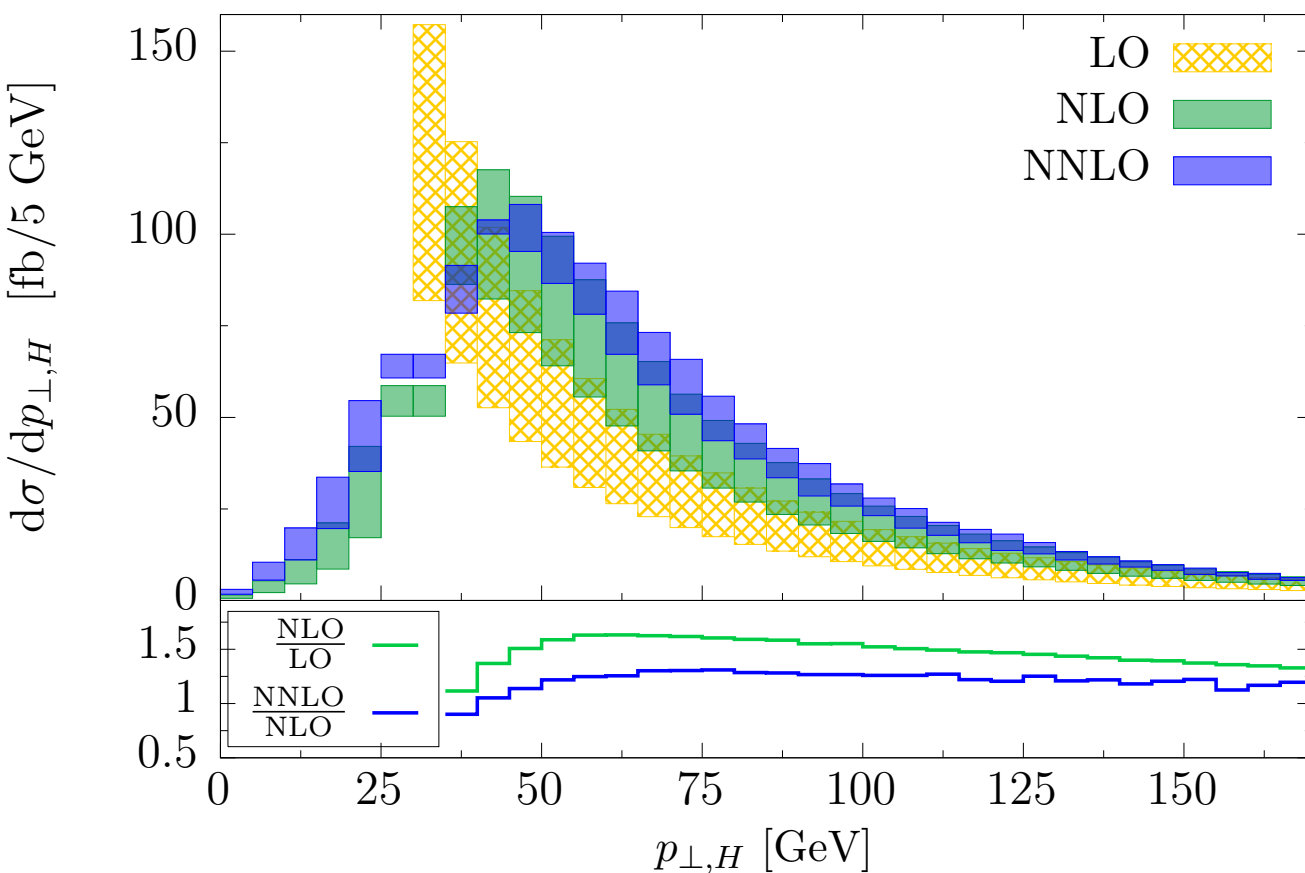
$$\sigma(\mathcal{T}_N < \mathcal{T}_N^{\text{cut}}) = \int H \otimes B \otimes B \otimes S \otimes \left[\prod_n^N J_n \right].$$

- Corrections of 2% which decrease NLO, flat with $p_{T,\text{jet}}$
- Ready for precision phenomenology in Run II!

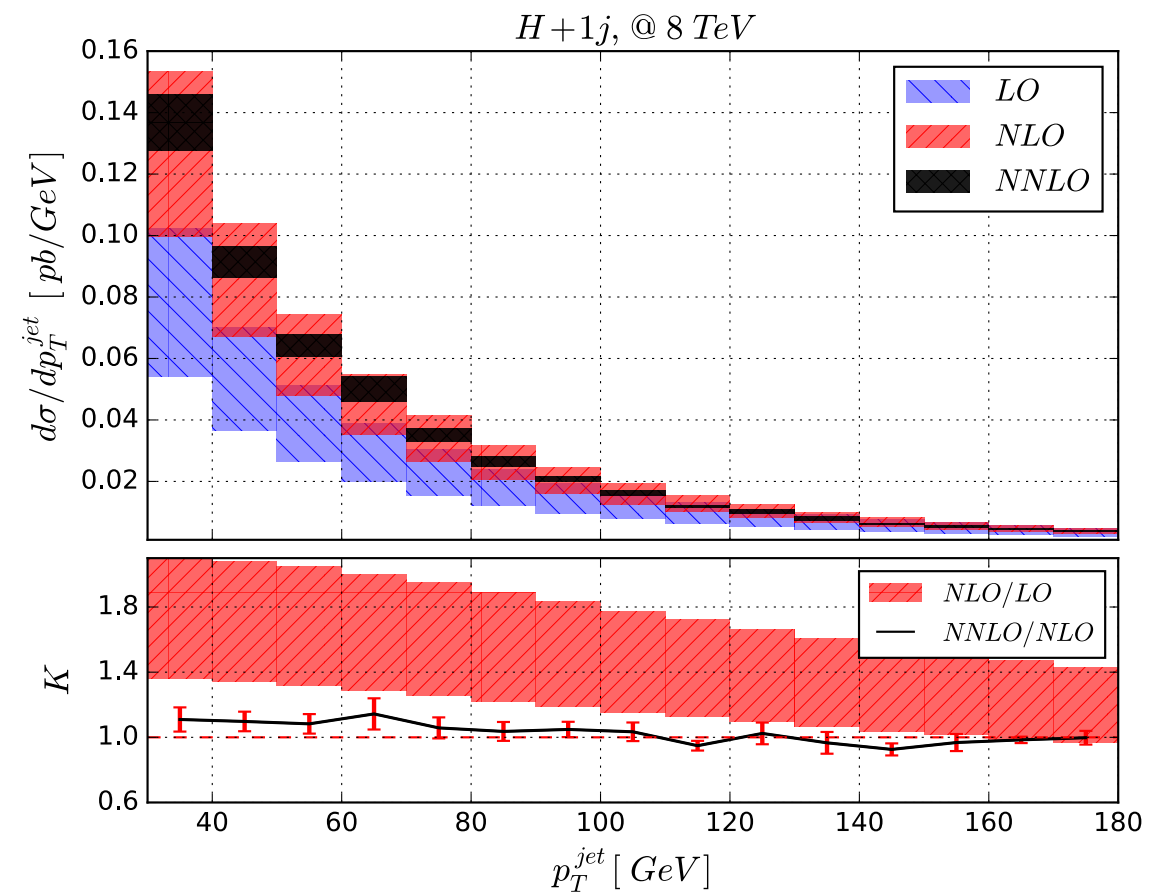
Boughezal, Focke, Liu, FP 1504.02131

H+jet at NNLO

- Needed for a description of Higgs p_T distribution; can help discriminate between BSM effects (Banfi, Martin, Sanz [1308.4771](#); Azatov, Paul [1309.5273](#))
- Calculations based on sector-improved subtraction (Boughezal, Caola, Melnikov, FP, Schulze) and jettiness subtraction (Boughezal, Focke, Liu, FP); gluons-only results with antennae subtraction (Chen, Gehrmann, Glover, Jaquier)



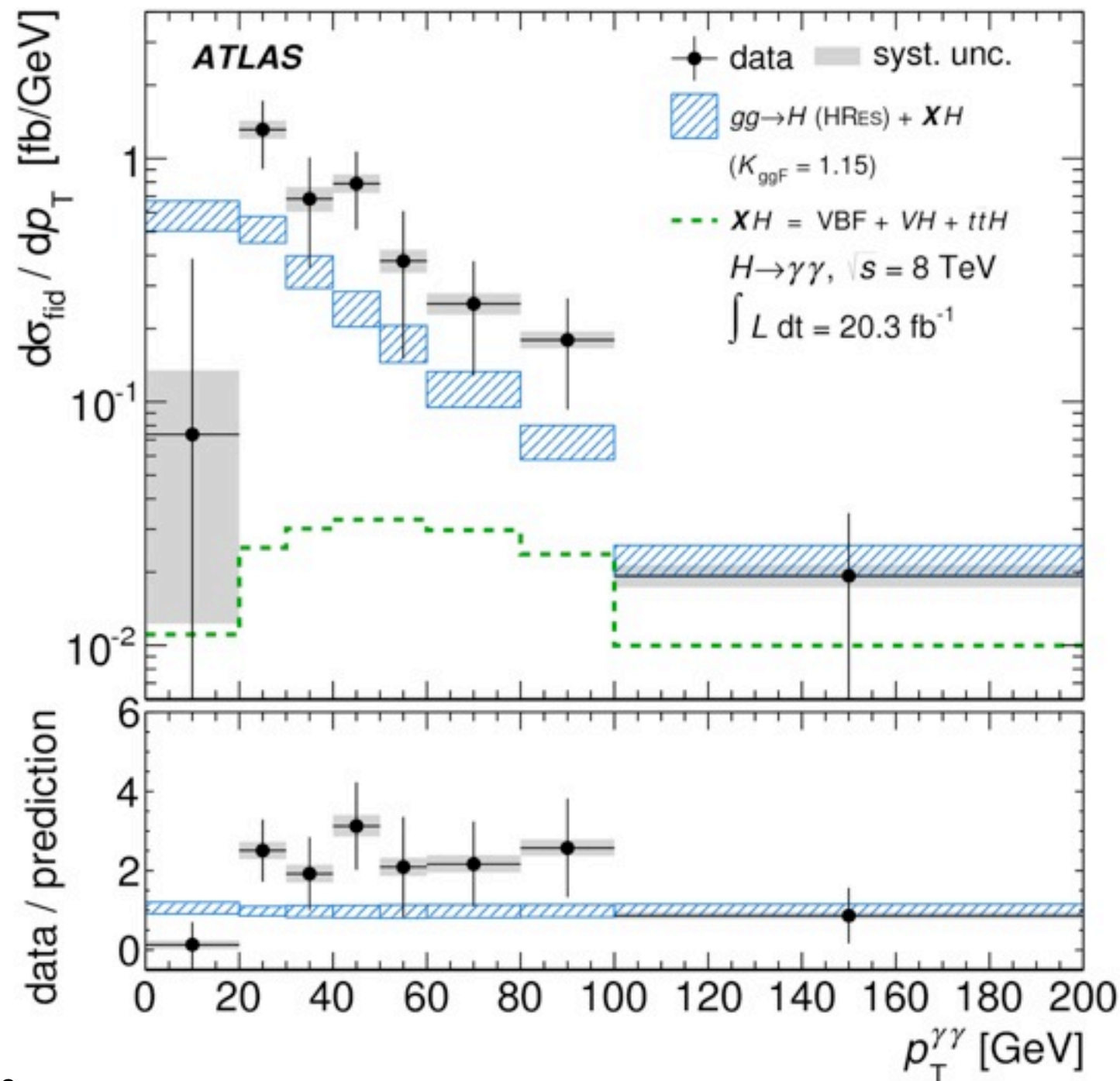
Boughezal, Caola, Melnikov, FP, Schulze,
[1302.6216](#) and to appear



Boughezal, Focke, Liu FP, to appear

H+jet at NNLO

- Needed for a description of Higgs p_T distribution; can help discriminate between BSM effects ([Banfi, Martin, Sanz |308.477|](#); [Azatov, Paul |309.5273|](#))

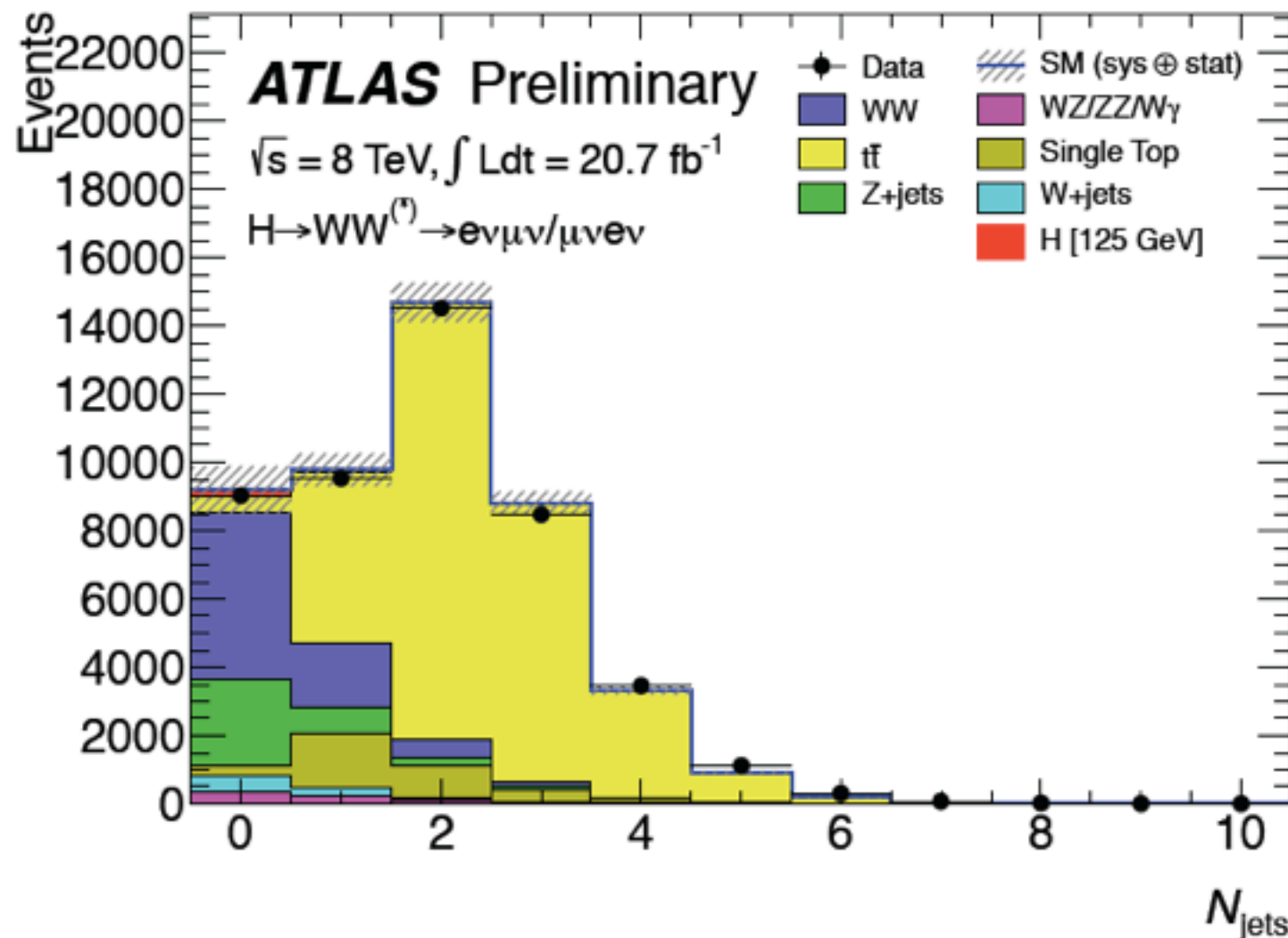


- Waiting for the next measurements from Run II!

Jet binning and all-orders resummation

Jet binning

- No mass peak in WW; theory especially crucial for search and interpretation
- A major issue in this channel is the division into exclusive jet bins

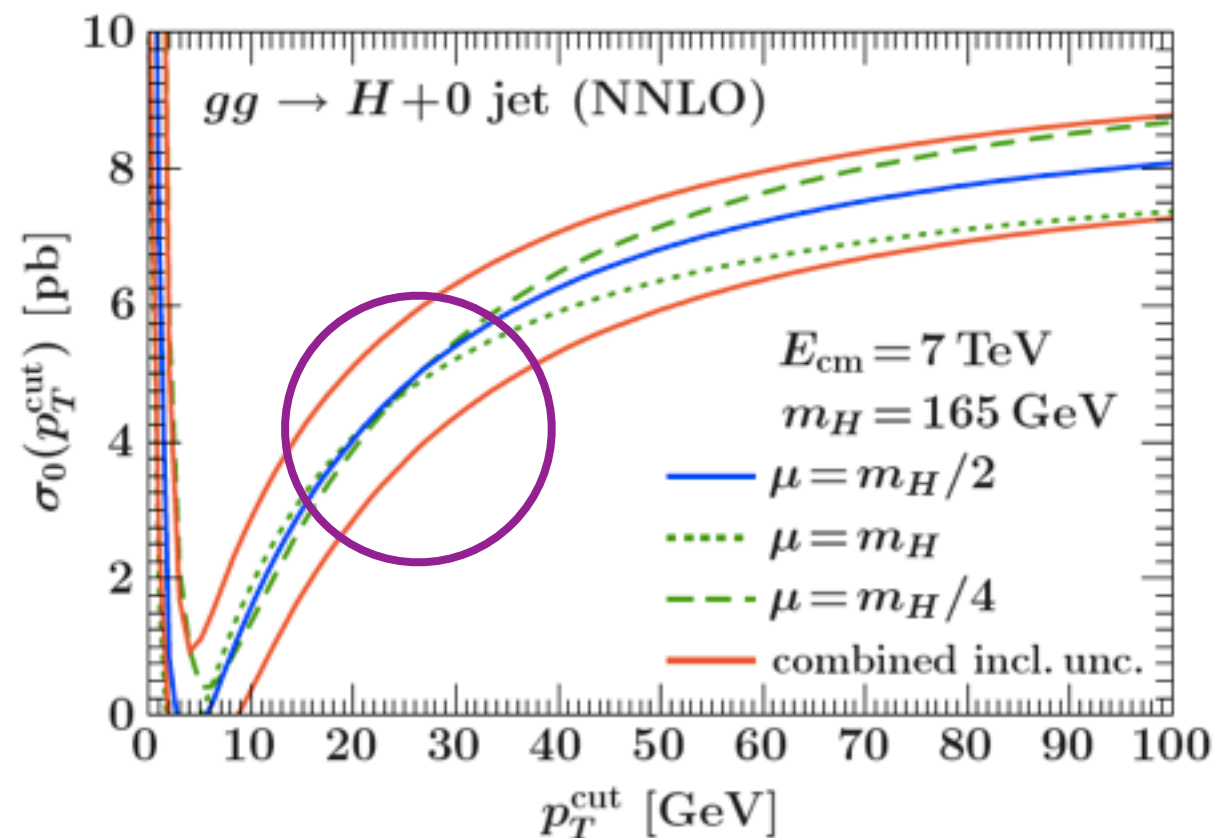


- Required by background composition
- Large logs from soft/collinear radiation
- Typical parameters: $p_{T,\text{veto}} \sim 25\text{-}30 \text{ GeV} \ll M_H$
- Relevant term for gluon-fusion Higgs: $2C_A(\alpha_s/\pi)\ln^2(M_H/p_{T,\text{veto}}) \sim 1/2$

Effects of the jet binning

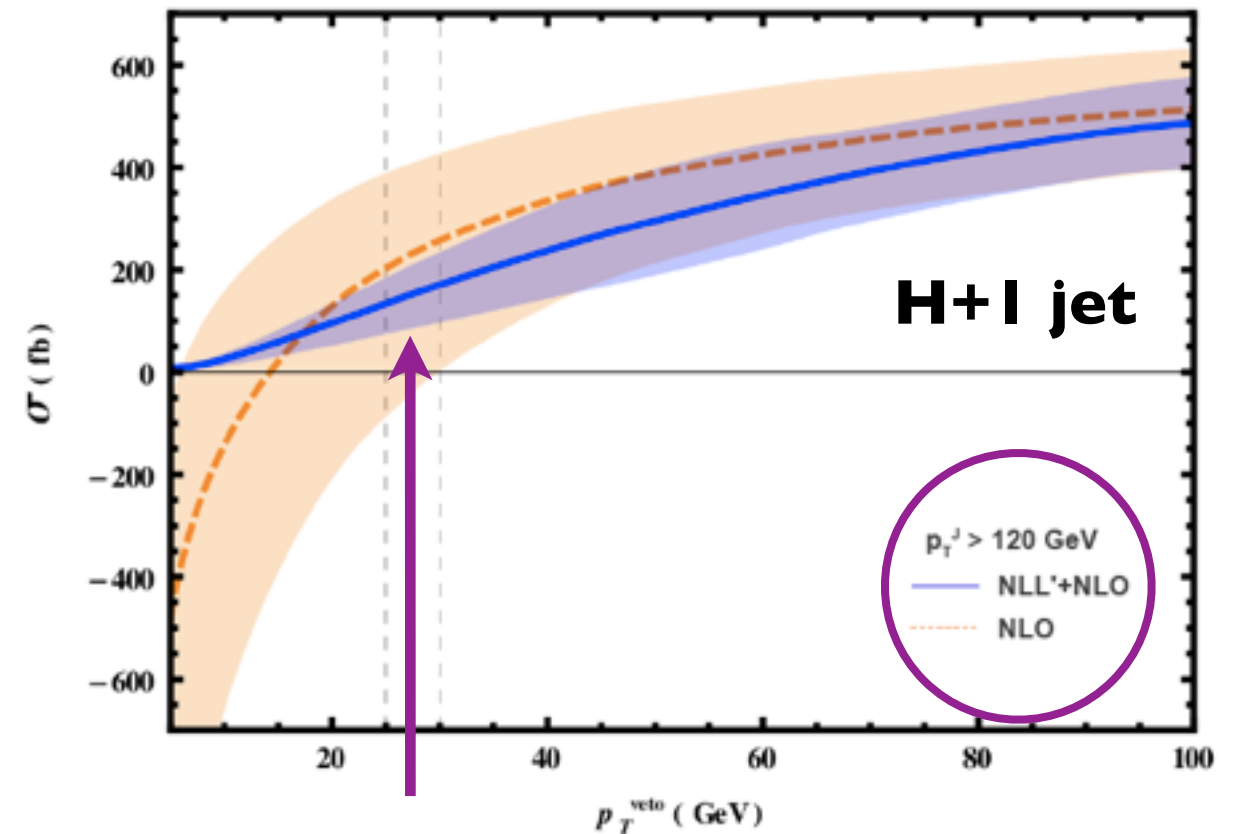
- These large logarithms induce several problems in the theory predictions

Stewart, Tackmann 1107.2117



- Scale variation no longer estimates theory uncertainties (green band); use the ST prescription to get the much larger red band

Liu, FP 1303.4405

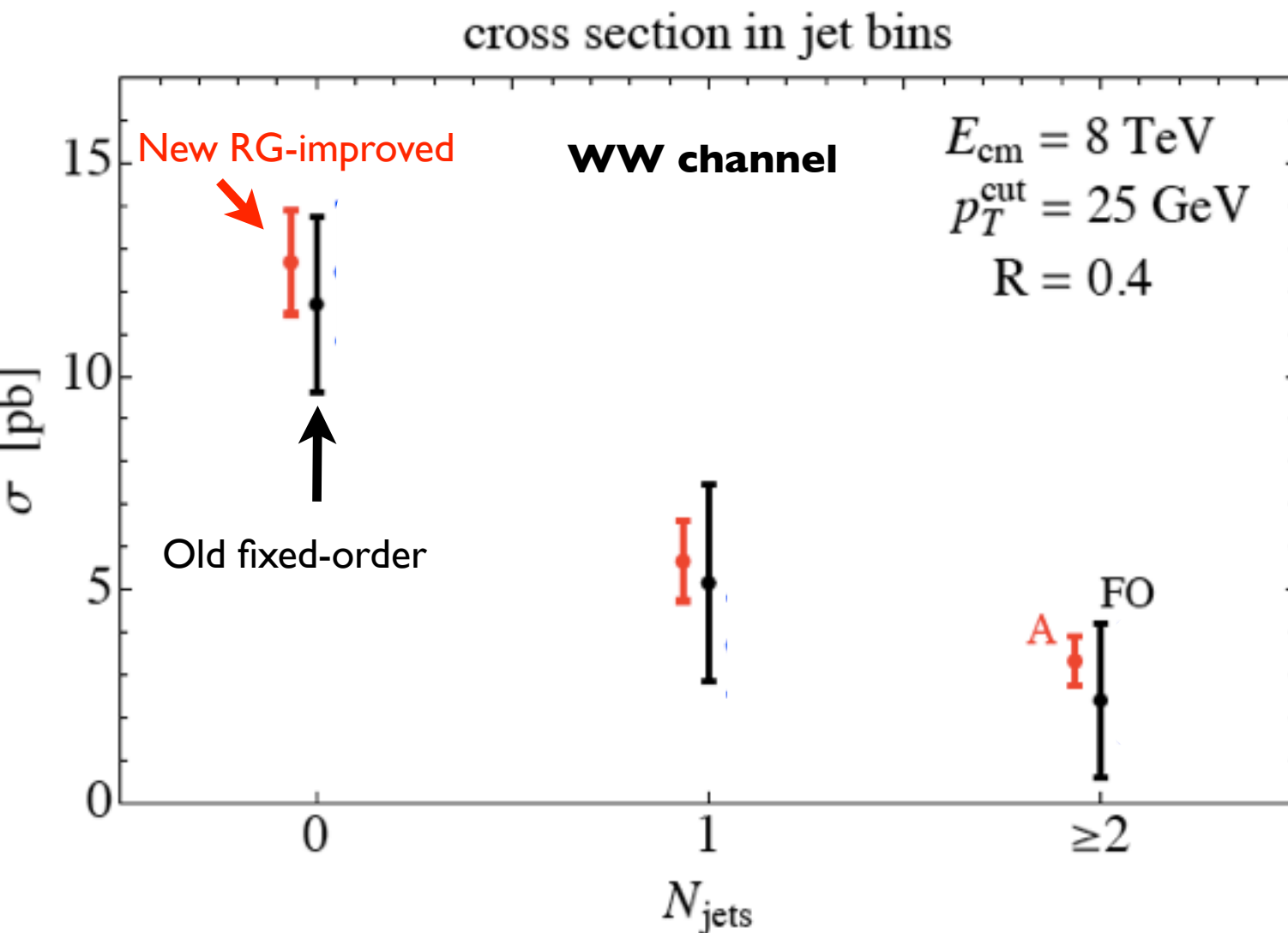


- Deviations from fixed-order, especially in new kinematic regions that will be first probed in Run II

Very active area! Banfi, Monni, Salam, Zanderighi; Becher, Neubert;
 Liu, FP; Stewart, Tackmann, Walsh, Zuberi; Li, Liu

Numerical results for the LHC

- **The goal:** completely replace fixed-order perturbation theory with renormalization-group improvement that resums the large jet-veto logs



Boughezal, Liu, Petriello, Tackmann, Walsh 1312.4535

- Can accomplish this using SCET framework for all jet bins
- Improved signal-strength error:

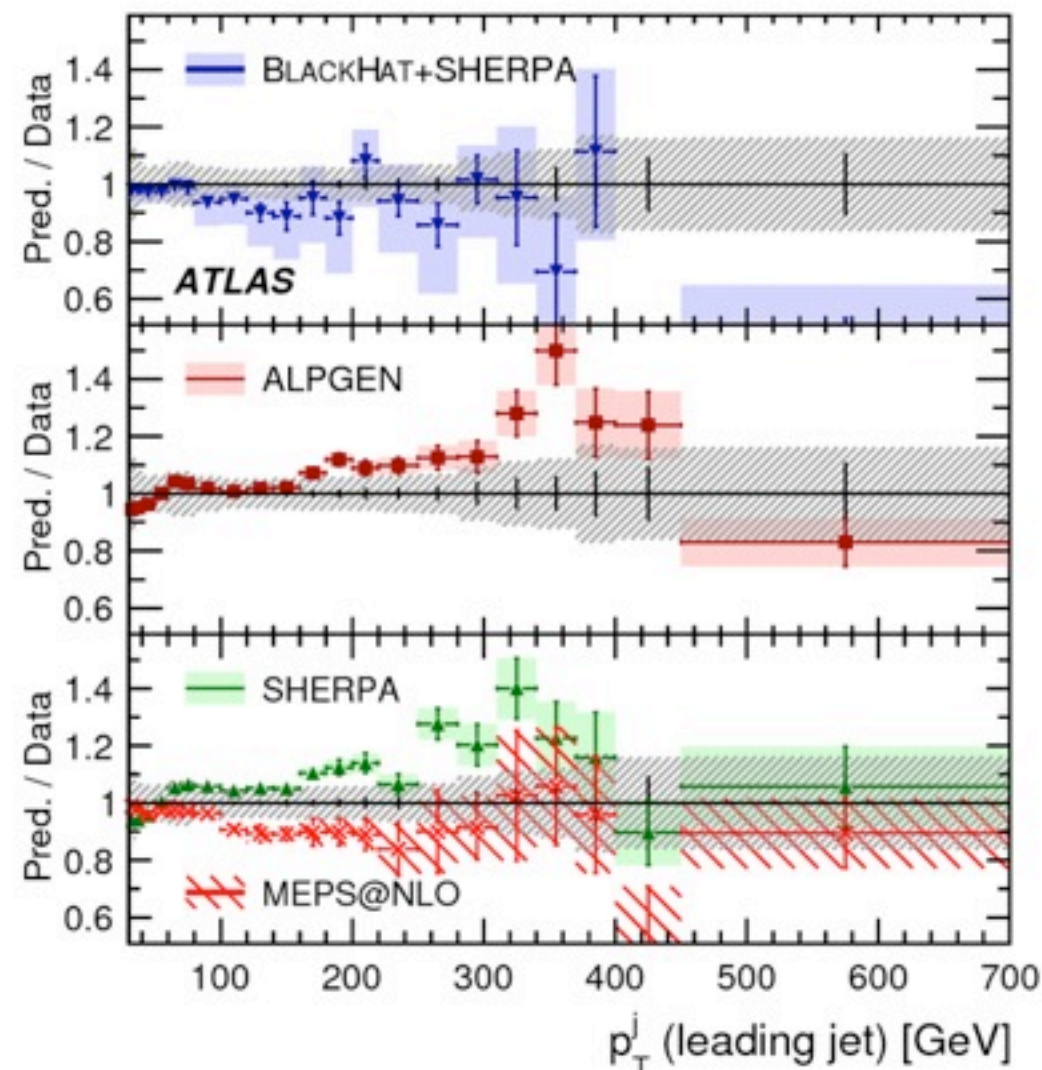
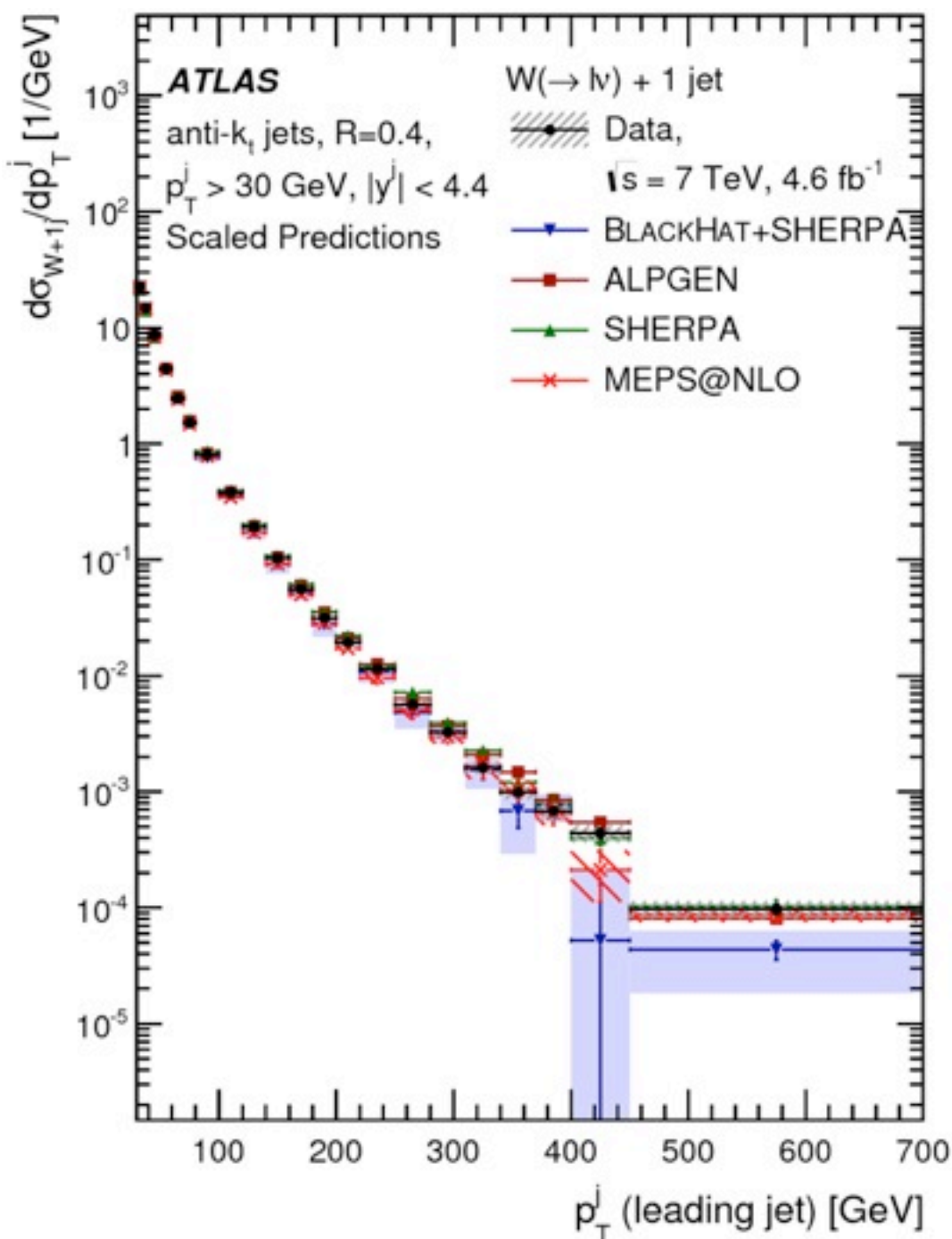
$$(\Delta\mu/\mu)_{\text{FO}} = 13.3\%$$

$$(\Delta\mu/\mu)_{\text{RG}} = 6.9\%$$

- **WW** theory uncertainty down by nearly a factor of 2!
- ATLAS finds agreement between this framework and their $\gamma\gamma$, $\gamma\gamma$ + ZZ data: 1407.4222, 1504.05833

The exclusive Z+1-jet puzzle

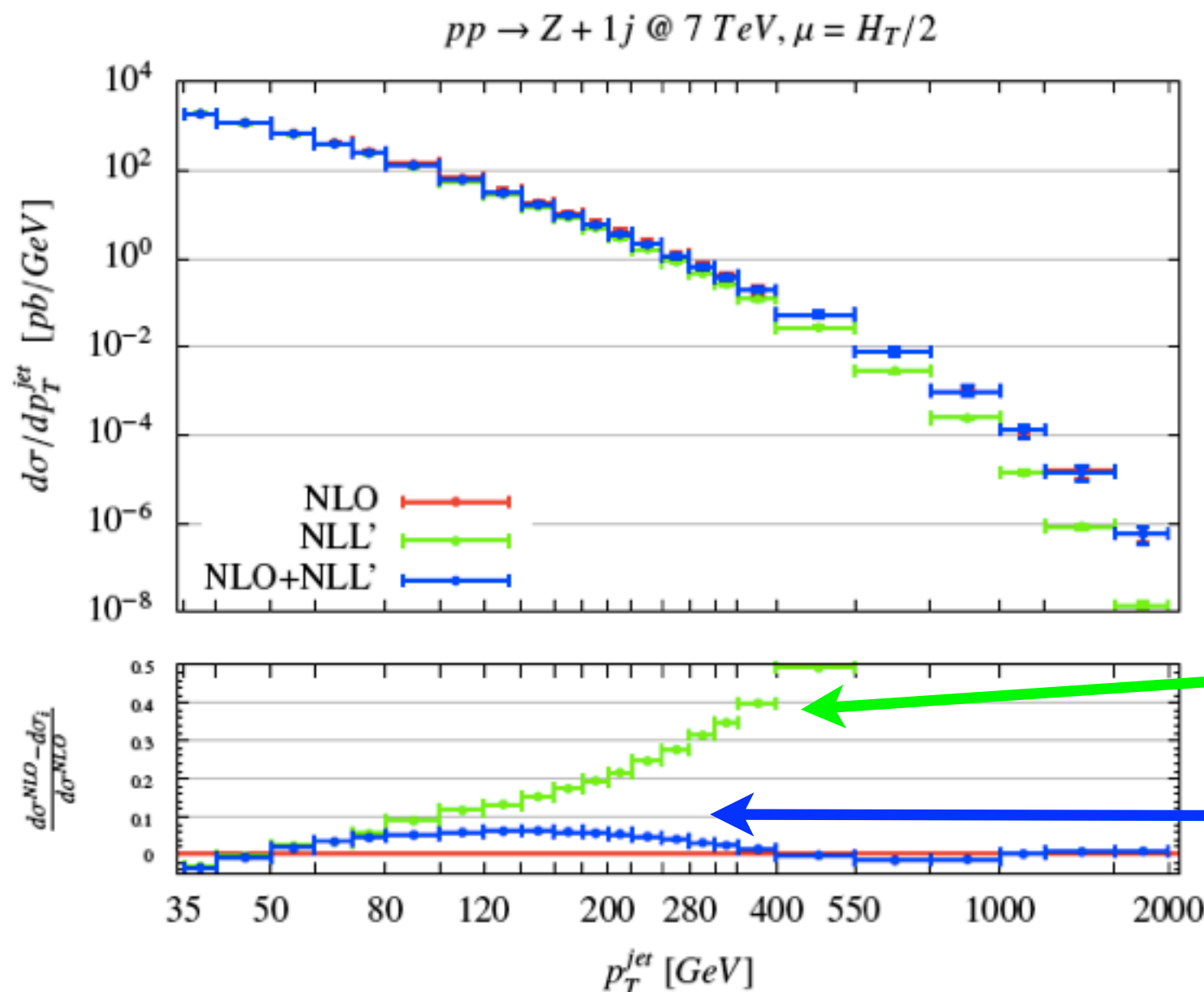
- Validate resummation formalism with exclusive V+1-jet. Color factor is smaller (C_F vs. C_A), but at p_T =few hundred GeV logs should dominate.



- Agreement with NLO up to 500 GeV!
- Seemingly contradicts expectation that logs dominate the cross section

The exclusive Z+1-jet puzzle

- Two competing effects: jet-veto logarithms and a giant K-factor
- ATLAS unfolding procedure reintroduces 2-jet events with one jet collinear to a final-state lepton, via a Monte-Carlo correction; very large at high p_T !



- Need to modify the unfolding procedure in order to access the resummation region

large correction
from jet-veto logs

reduced by 2-jet
events at high p_T

Boughezal, Focke, Liu 1501.01059

Conclusions

- There can be flowers in the desert if one looks carefully; we have the tools to do so!
- Multi-particle NLO has become a mature field
- NNLO has undergone rapid advances in the past year; NNLO precision jet phenomenology now possible!
- High-precision resummation in the presence of final-state jets has become possible
- QCD theory is ready for the upcoming data!