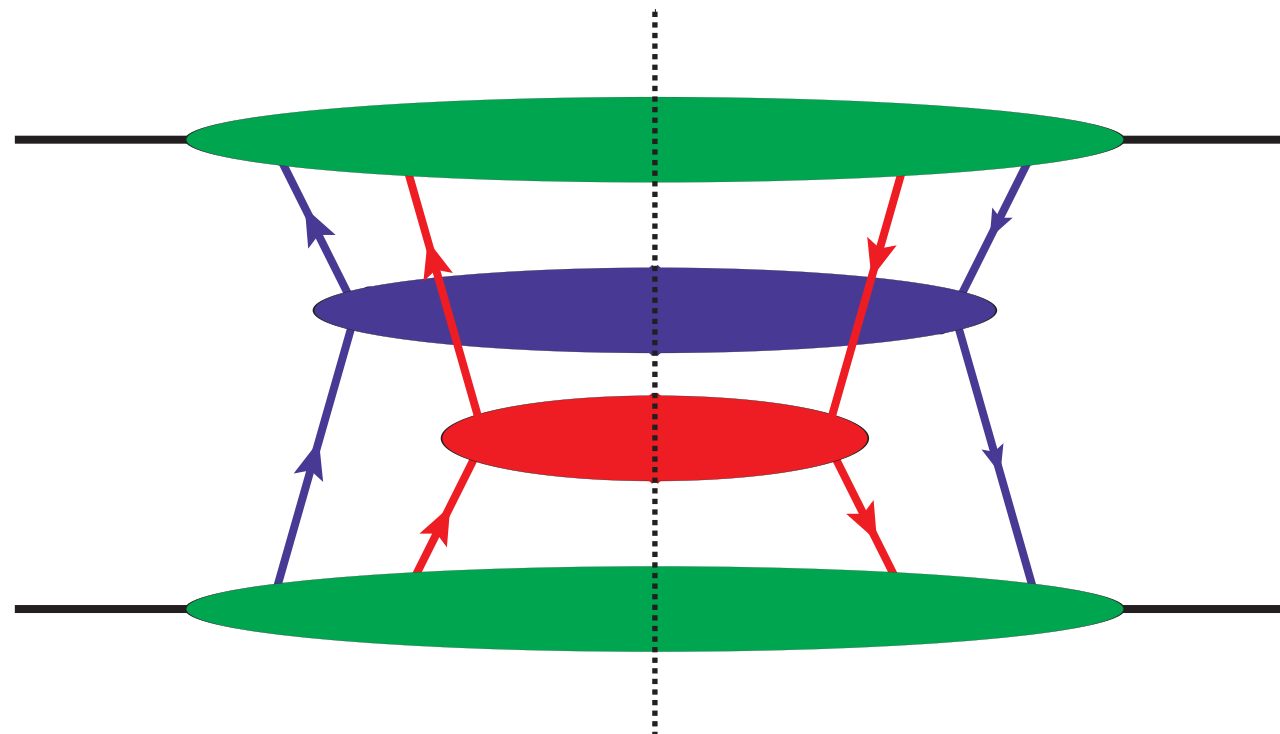


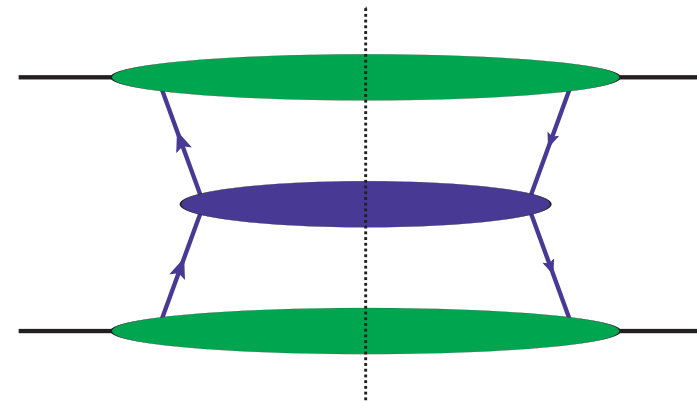
Polarization in Double Parton Scattering



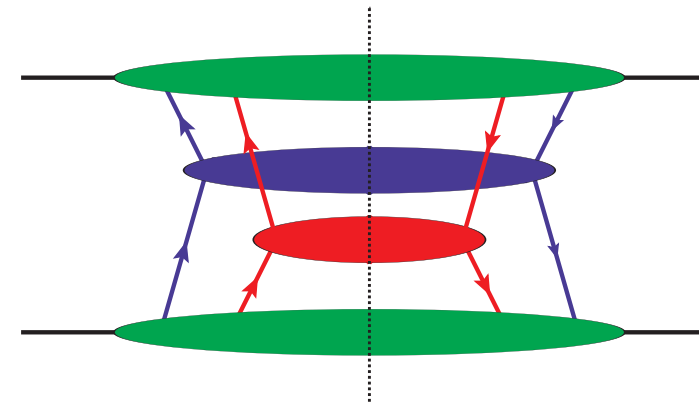
Tomas Kasemets
Nikhef / VU



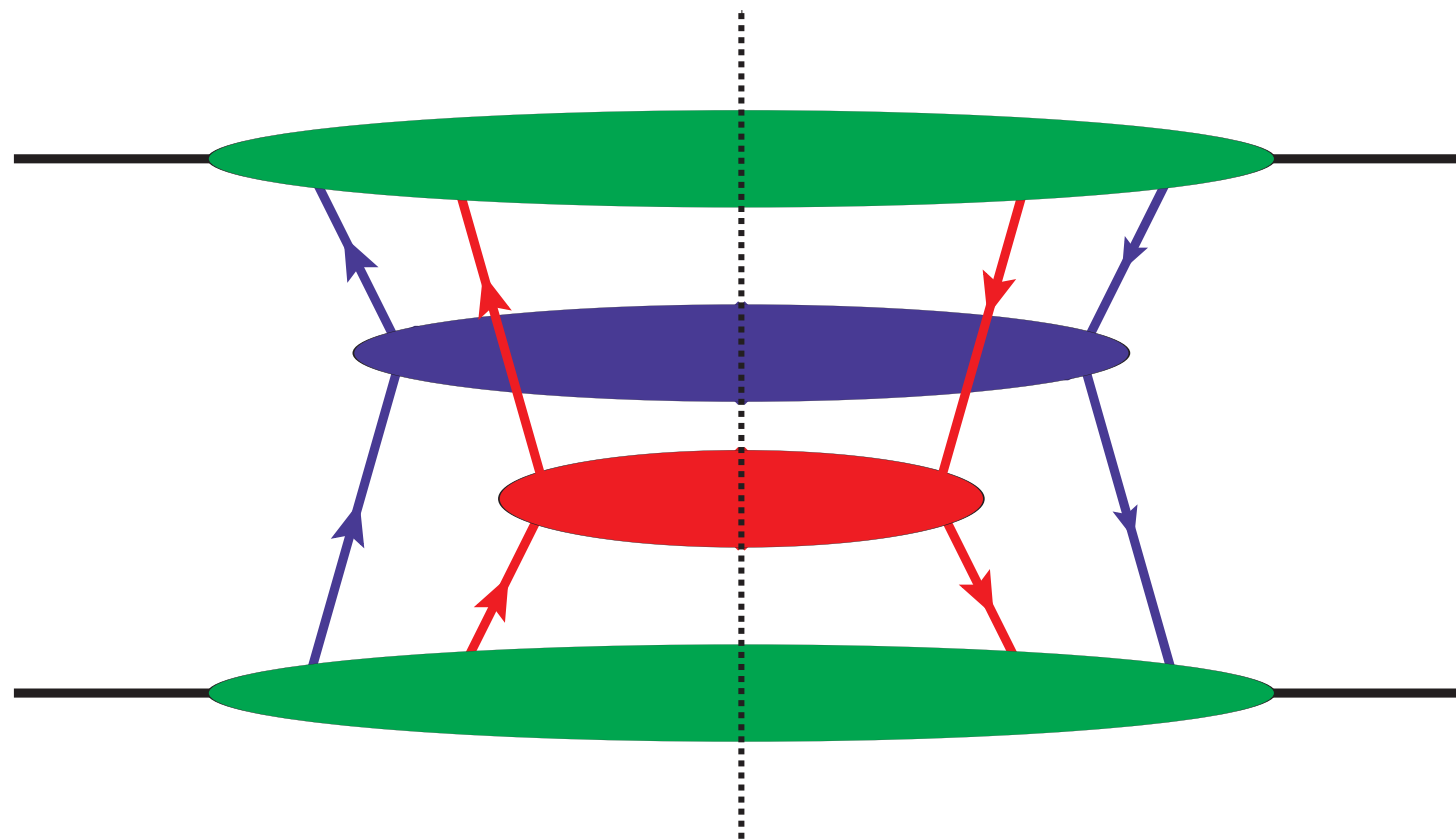
What is Double Parton Scattering..



What is Double Parton Scattering..



What is Double Parton Scattering..



What is Double Parton Scattering..



What is Double Parton Scattering..



DPS in hadron-hadron collisions

- Cross section calculations based on factorization
cross section = parton distribution \times partonic cross section

- single parton example: $pp \rightarrow Z + X \rightarrow l^+ l^- + X$

- Spectator-spectator interactions

- cancel in inclusive cross sections (unitarity)

- affects final state X

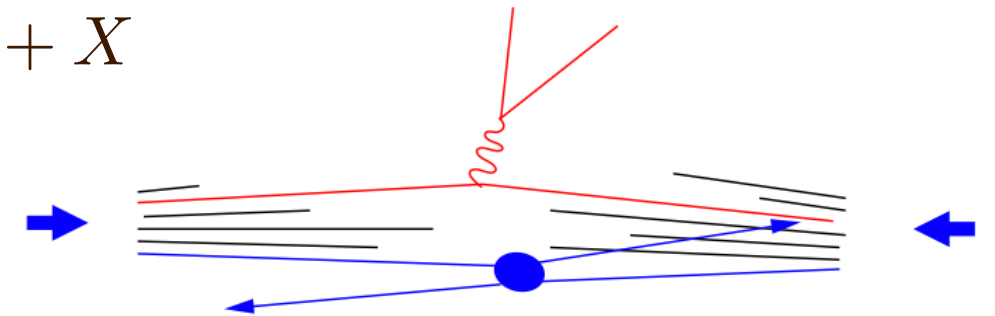


figure from M. Diehl, QCD Evolution 2014

- Ask questions about X , gives sensitivity to additional interaction
- Second interaction hard — **Double Parton Scattering**
example: $pp \rightarrow Z + H + X \rightarrow l\bar{l} + b\bar{b} + X$

Proton collisions at LHC

- Double parton scattering contribute both to signal and background

- $pp \rightarrow H + Z + X \rightarrow b\bar{b} + \mu^+\mu^- + X$

Del Fabbro, Treleani, 1999

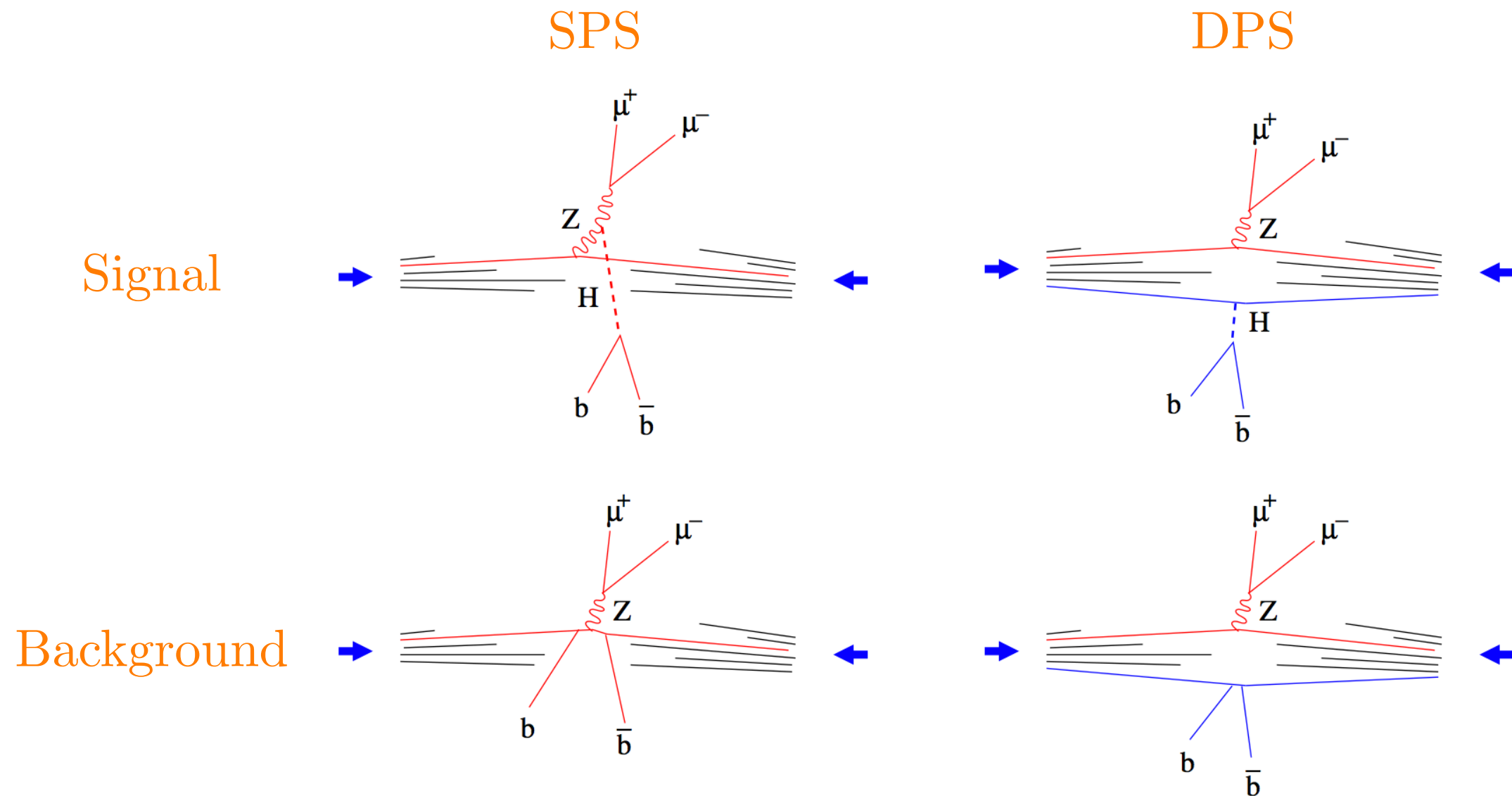


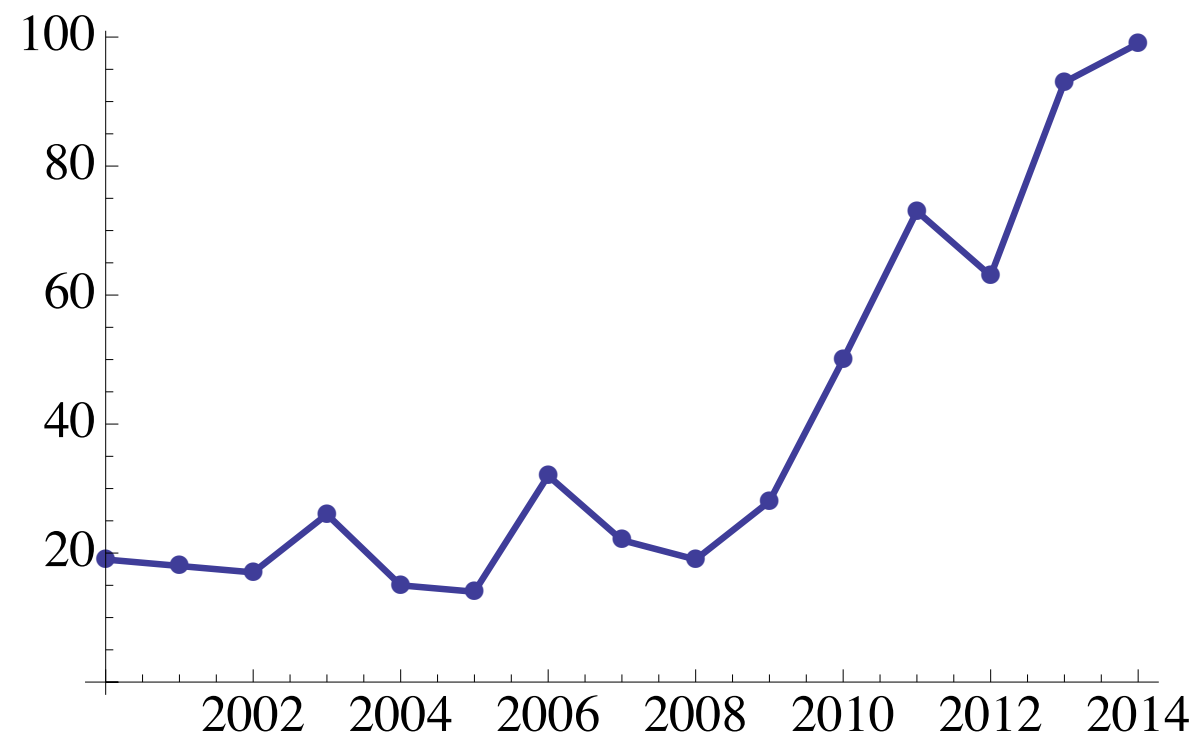
figure from Diehl, QCD Evolution 2014

When should one care about DPS?

- Rule of thumb:
 - Several particles in the final state (typically 4 or more)
 - High energy hadron collisions
 - where low momentum fractions are probed (low x)
 - And/or SPS is suppressed — two single production cross sections are large compared to their “combination”
- These conditions are often fulfilled for processes studied at the LHC
- Some examples:
 - Two same sign W's (small cross section but very clean)
 - Double open charm production ($D^0\bar{D}^0$) - Double dominates single parton scattering
Hameren, Maciula, and Szczurek, 2014
 - Double J/Psi production,
 - $W+b$ (rough estimates about 20% DPS)
ATLAS Collaboration, 2013
 - double meson productions, $W+b\bar{b}$, 4 jets, photon + 3 jets, etc. etc.

Increase in activity - still a lot to be done

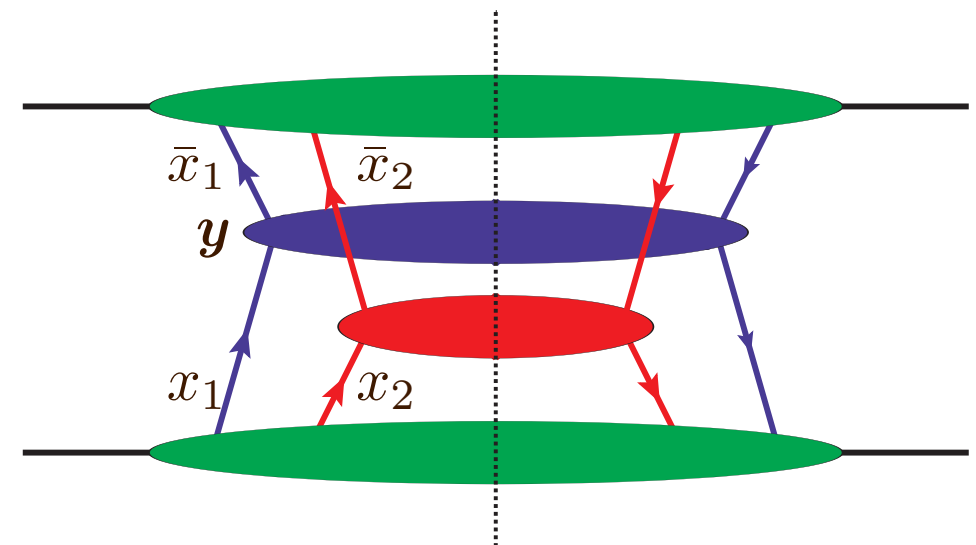
- Inspire search for *double parton scattering* organized per year



- Spurred by the realization that it is an important background to several other processes of interest at the LHC and contains a rich and largely unexplored area of hadron collisions.
- Still much! to do regarding the spin structure (and other correlations) as the vast majority of studies neglects all polarizations

How does one do DPS phenomenology

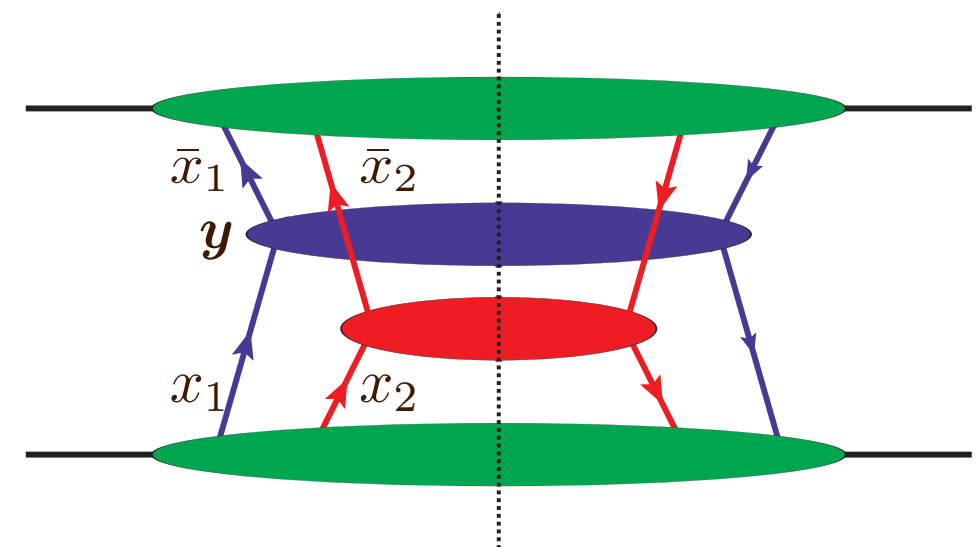
- Write down the cross section in a factorized form
cross section = parton distributions \times partonic cross section
 - The normal PDFs are replaced by Double Parton Distributions (DPDs)
- DPDs describe the probability to find two partons inside the proton, at a given transverse distance and with momentum fractions x_1 and x_2
- Schematically (leading order)



$$\frac{d\sigma_{DPS}}{dx_1 d\bar{x}_1 dx_2 d\bar{x}_2} = \frac{1}{C} \hat{\sigma}_1 \hat{\sigma}_2 \int d^2 \mathbf{y} F(x_1, x_2, \mathbf{y}) F(\bar{x}_1, \bar{x}_2, \mathbf{y})$$

How does one do DPS phenomenology

- Write down the cross section in a factorized form
cross section = parton distributions \times partonic cross section
- The normal PDFs are replaced by Double Parton Distributions (DPDs)
- DPDs describe the probability to find two partons inside the proton, at a given transverse distance and with momentum fractions x_1 and x_2
- Schematically (leading order)



$$\frac{d\sigma_{DPS}}{dx_1 d\bar{x}_1 dx_2 d\bar{x}_2} = \frac{1}{C} \hat{\sigma}_1 \hat{\sigma}_2 \int d^2 \mathbf{y} F(x_1, x_2, \mathbf{y}) F(\bar{x}_1, \bar{x}_2, \mathbf{y})$$

transverse distance

momentum fractions

and then..

- Double parton distributions unknown, so how to continue..
- Simplest possible approach to DPS
 - **Assume** the DPD factorize into normal PDFs and a transverse dependence

$$F_{ij}(x_1, x_2, \mathbf{y}) = f_i(x_1)f_j(x_2)G(\mathbf{y}) \qquad 1/\sigma_{\text{eff}} = \int d^2\mathbf{y} G(\mathbf{y})^2$$

- **Assume** complete universality of $G(\mathbf{y})$
- Then the cross section become extremely simple:

$$\sigma_{DPS} \sim \frac{\sigma_1 \sigma_2}{\sigma_{\text{eff}}}$$

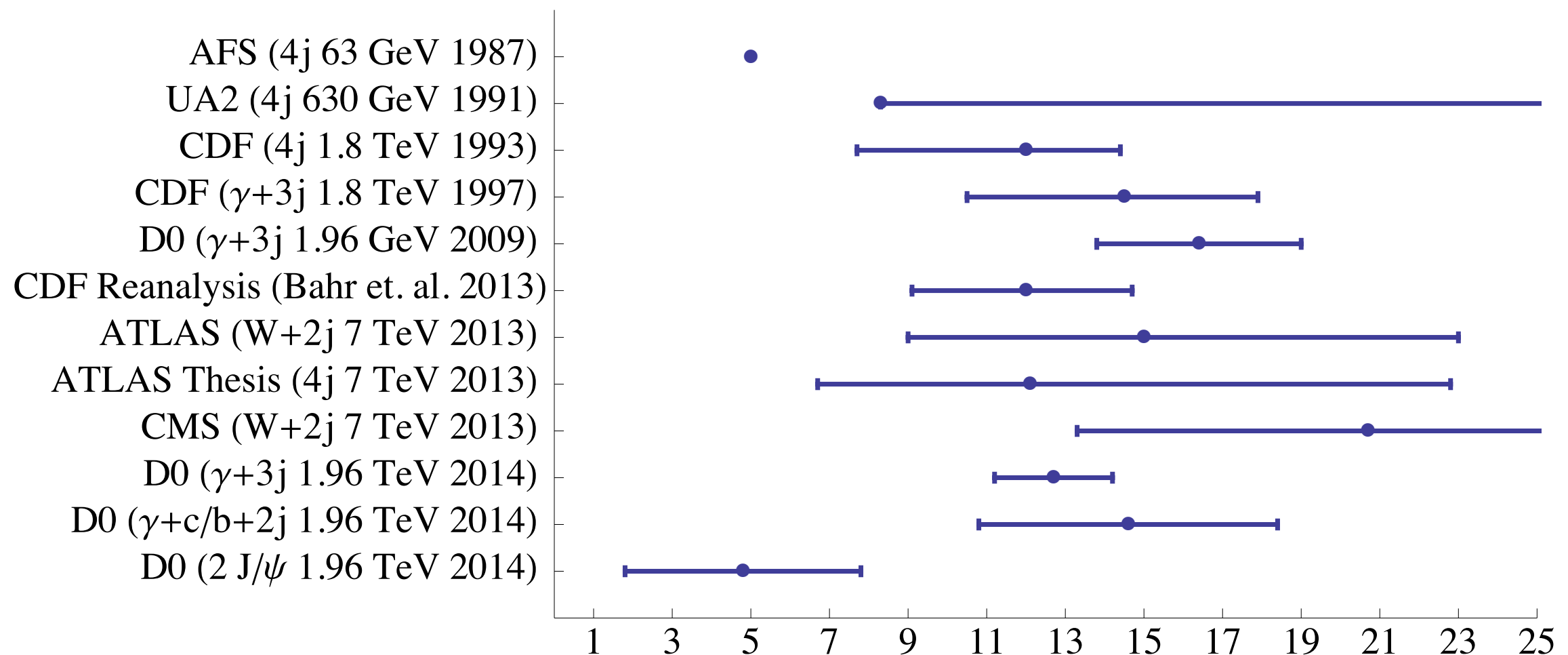
- Extract σ_{eff} from measurements (typically set to 15 mb)
- In this approximation, the DPS cross section is known as soon as we know the single parton cross sections
- Study rates, distributions, variables for DPS extraction etc.

Several such studies along these lines..

- A few recent ones are..
 - Double quarkonium, J.-P. Lansberg, H.-S. Shao, 2015;
 - $W + D^*$, S.P. Baranov et. al., 2015;
 - 2-gamma + 2-jets, J. Tao et. al. 2015;
 - Charm- + bottom-mesons, A.K. Likhoded et. al., 2015;
 - J/Psi pair production, J.-P. Lansberg, H.-S. Shao, 2015;
 - 4-jets, R. Maciuła, A. Szczurek, 2014;
 - Double c-cbar, A. Hameren, R. Maciula, A. Szczurek, 2014;
 - Quarkonia + vector bosons, D. d'Enterria, A. M. Snigirev, 2014;
 - Heavy quarks, E.R. Cazaroto, V.P. Goncalves and F.S. Navarra1. 2013;
 - $W+2$ -jets G. Calucci, S. Salvini and D. Treleani, 2013;
 - etc...

Experimental measurements

- Extractions of σ_{eff} , $\sigma_{DPS} \sim \frac{\sigma_1 \sigma_2}{\sigma_{\text{eff}}}$



- Neglecting parton correlations, gives $\sigma_{\text{eff}} \sim 40$ mb
 - Much larger than experimental measurements of 5-20 mb
 - complete independence between partons disfavored

see Calucci, Treleani 1999; Frankfurt, Strikman, Weiss 2003; Blok et al 2013

Polarized DPDs

- Spin of the two partons can be correlated \rightarrow polarized DPDs

Describe correlations between the spin of
and distance between the two partons



- Example: DPD for two longitudinally polarized quarks

$$f_{\Delta q \Delta q} \sim \begin{array}{c} \text{Diagram 1: Green oval with two red arrows pointing right} \\ \text{Diagram 2: Green oval with two red arrows pointing left} \\ \text{Diagram 3: Green oval with two red arrows pointing right} \\ \text{Diagram 4: Green oval with two red arrows pointing left} \end{array}$$

- Quarks: unpolarized q , longitudinally polarized Δq and transversely polarized δq
- Gluons: unpolarized g , longitudinally polarized Δg and linearly polarized δg
- Linear/transverse polarization from helicity interference

Similar description, different physics than TMDs!

Polarized quark DPDs

- The different polarized quark DPDs:

Diehl, Schäfer, Ostermeier, 2011

$$F_{qq}(x_1, x_2, \mathbf{y}) = f_{qq}(x_1, x_2, \mathbf{y}) ,$$

$$F_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) = f_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) ,$$

$$F_{q\delta q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{q\delta q}(x_1, x_2, \mathbf{y}) ,$$

$$F_{\delta q q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{\delta q q}(x_1, x_2, \mathbf{y}) ,$$

$$\begin{aligned} F_{\delta q \delta q}^{jj'}(x_1, x_2, \mathbf{y}) &= \delta^{jj'} f_{\delta q \delta q}(x_1, x_2, \mathbf{y}) \\ &\quad + (2\mathbf{y}^j \mathbf{y}^{j'} - \mathbf{y}^2 \delta^{jj'}) M^2 f_{\delta q \delta q}^t(x_1, x_2, \mathbf{y}) \end{aligned}$$

- Appreciate the similarity to, for example, the decomposition of TMDs
- Note: All for distributions for an **unpolarized proton**

Polarized quark DPDs

- The different polarized quark DPDs:

unpolarized



Diehl, Schäfer, Ostermeier, 2011

$$F_{qq}(x_1, x_2, \mathbf{y}) = f_{qq}(x_1, x_2, \mathbf{y}) ,$$

$$F_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) = f_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) ,$$

$$F_{q\delta q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{q\delta q}(x_1, x_2, \mathbf{y}) ,$$

$$F_{\delta q q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{\delta q q}(x_1, x_2, \mathbf{y}) ,$$

$$F_{\delta q \delta q}^{jj'}(x_1, x_2, \mathbf{y}) = \delta^{jj'} f_{\delta q \delta q}(x_1, x_2, \mathbf{y}) \\ + (2\mathbf{y}^j \mathbf{y}^{j'} - \mathbf{y}^2 \delta^{jj'}) M^2 f_{\delta q \delta q}^t(x_1, x_2, \mathbf{y})$$

- Appreciate the similarity to, for example, the decomposition of TMDs
- Note: All for distributions for an unpolarized proton

Polarized quark DPDs

- The different polarized quark DPDs:

unpolarized

Diehl, Schäfer, Ostermeier, 2011

longitudinally polarized

$$F_{qq}(x_1, x_2, \mathbf{y}) = f_{qq}(x_1, x_2, \mathbf{y}),$$

$$F_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) = f_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}),$$

$$F_{q\delta q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{q\delta q}(x_1, x_2, \mathbf{y}),$$

$$F_{\delta q q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{\delta q q}(x_1, x_2, \mathbf{y}),$$

$$F_{\delta q \delta q}^{jj'}(x_1, x_2, \mathbf{y}) = \delta^{jj'} f_{\delta q \delta q}(x_1, x_2, \mathbf{y}) \\ + (2\mathbf{y}^j \mathbf{y}^{j'} - \mathbf{y}^2 \delta^{jj'}) M^2 f_{\delta q \delta q}^t(x_1, x_2, \mathbf{y})$$

- Appreciate the similarity to, for example, the decomposition of TMDs
- Note: All for distributions for an unpolarized proton

Polarized quark DPDs

- The different polarized quark DPDs:

unpolarized

Diehl, Schäfer, Ostermeier, 2011

$$F_{qq}(x_1, x_2, \mathbf{y}) = f_{qq}(x_1, x_2, \mathbf{y}),$$

longitudinally polarized

$$F_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) = f_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}),$$

$$F_{q\delta q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{q\delta q}(x_1, x_2, \mathbf{y}),$$

mixed unpolarized/
transversely polarized

$$F_{\delta q q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{\delta q q}(x_1, x_2, \mathbf{y}),$$

$$F_{\delta q \delta q}^{jj'}(x_1, x_2, \mathbf{y}) = \delta^{jj'} f_{\delta q \delta q}(x_1, x_2, \mathbf{y}) \\ + (2\mathbf{y}^j \mathbf{y}^{j'} - \mathbf{y}^2 \delta^{jj'}) M^2 f_{\delta q \delta q}^t(x_1, x_2, \mathbf{y})$$

- Appreciate the similarity to, for example, the decomposition of TMDs
- Note: All for distributions for an unpolarized proton

Polarized quark DPDs

- The different polarized quark DPDs:

unpolarized

Diehl, Schäfer, Ostermeier, 2011

$$F_{qq}(x_1, x_2, \mathbf{y}) = f_{qq}(x_1, x_2, \mathbf{y}),$$

longitudinally polarized

$$F_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}) = f_{\Delta q \Delta q}(x_1, x_2, \mathbf{y}),$$

$$F_{q\delta q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{q\delta q}(x_1, x_2, \mathbf{y}),$$

mixed unpolarized/
transversely polarized

$$F_{\delta q q}^j(x_1, x_2, \mathbf{y}) = \epsilon^{jj'} \mathbf{y}^{j'} M f_{\delta q q}(x_1, x_2, \mathbf{y}),$$

$$F_{\delta q \delta q}^{jj'}(x_1, x_2, \mathbf{y}) = \delta^{jj'} f_{\delta q \delta q}(x_1, x_2, \mathbf{y}) \\ + (2\mathbf{y}^j \mathbf{y}^{j'} - \mathbf{y}^2 \delta^{jj'}) M^2 f_{\delta q \delta q}^t(x_1, x_2, \mathbf{y})$$

transversely polarized

- Appreciate the similarity to, for example, the decomposition of TMDs
- Note: All for distributions for an unpolarized proton

What has been done for polarized DPS?

Polarization in DPS

- Setting up the framework for polarized DPS
Mekhfi, 1985; Diehl, Schäfer, 2011;
Diehl, Schäfer, Ostermeier, 2011; Manohar, Waalewijn, 2012;
- Polarization limited by positivity bounds combined with scale evolution
Diehl, TK, 2013; Diehl, TK, Keane 2014
- DPDs studied in a number of different quark models
 - Correlations typically found to be sizable
Chang, Manohar, Waalewijn, 2012;
Rinaldi, Scopetta, Traini, Vento, 2014
- Have been included in cross section calculations of double vector boson production
(γ, Z, W) and double $c\bar{c}$
Manohar, Waalewijn, 2012; Diehl, TK, 2012;
Echevarria, TK, Mulders, Pisano, 2015
- So far, limited literature on polarization effects in DPS
 - room for improvement

Polarization in DPS

- Longitudinal polarization:
 - Changes rate as well as rapidity and $|p_T|$ distributions
- Transverse quark/linear gluon polarization
- Leads to azimuthal asymmetries
- Double Drell-Yan

$$d\sigma_{DPS}(pp \rightarrow ZZ \rightarrow l_1 \bar{l}_1 l_2 \bar{l}_2) \subset A \cos(2\Delta\phi) f_{\delta q \delta q} f_{\delta \bar{q} \delta \bar{q}}$$

TK, M. Diehl, 2012

for transversely polarize quarks

- Double $q\bar{q}$ production

$$d\sigma_{DPS}(pp \rightarrow c_1 \bar{c}_1 c_2 \bar{c}_2) \subset B \cos(2\Delta\phi) f_{\delta g \delta g} f_{g \delta g} \\ + C \cos(4\Delta\phi) f_{\delta g \delta g} f_{\delta g \delta g}$$

for linearly polarized gluons

Echevarria, TK, Mulders, Pisano, 2015

- Linearly polarized gluons also affect the overall rate

Getting quantitative..

- Standard approach

$$F_{ij}(x_1, x_2, \mathbf{y}) = f_i(x_1) f_j(x_2) G(\mathbf{y})$$

- Build on this, but lets add polarization
- Simple model for upper estimates of polarization effects

- Use the above formula for unpolarized partons
- Saturate positivity bounds for polarized DPDs at a low initial scale

$$f_{ab} + h_{\delta a \delta b} - h_{\delta a \delta b}^t \pm \sqrt{(h_{\delta a b} + h_{a \delta b})^2 + (f_{\Delta a \Delta b} - h_{\delta a \delta b} - h_{\delta a \delta b}^t)^2} \geq 0$$

$$f_{ab} - h_{\delta a \delta b} + h_{\delta a \delta b}^t \pm \sqrt{(h_{\delta a b} - h_{a \delta b})^2 + (f_{\Delta a \Delta b} + h_{\delta a \delta b} + h_{\delta a \delta b}^t)^2} \geq 0$$

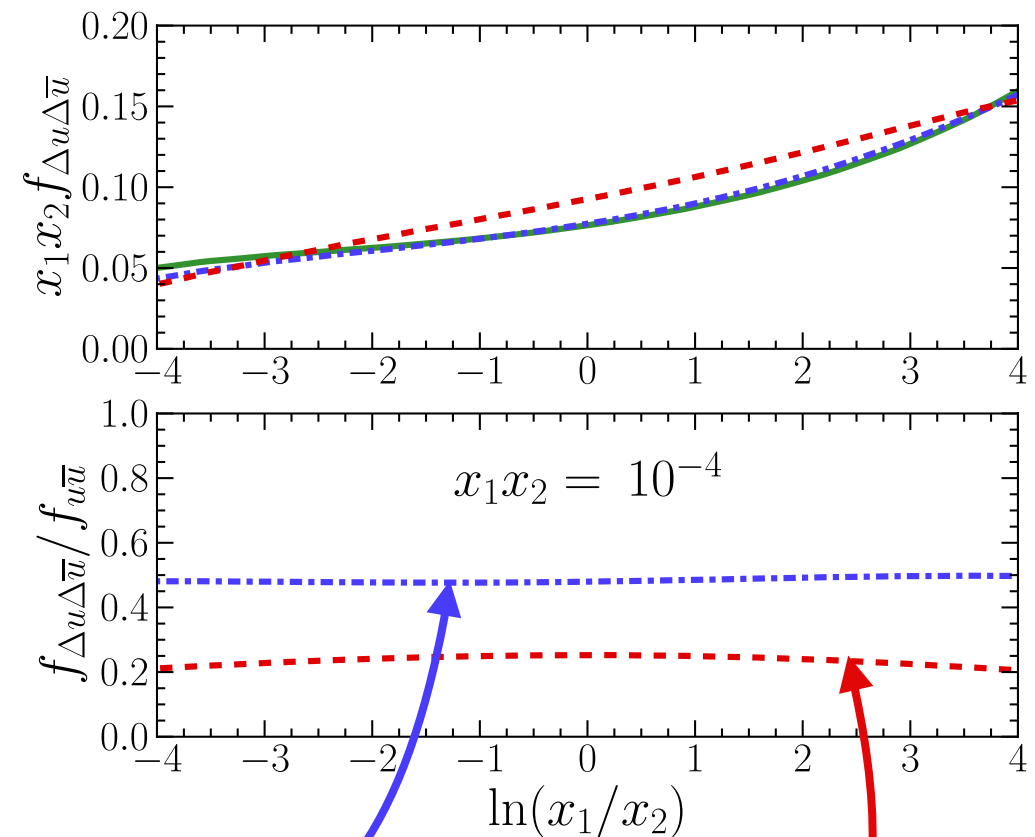
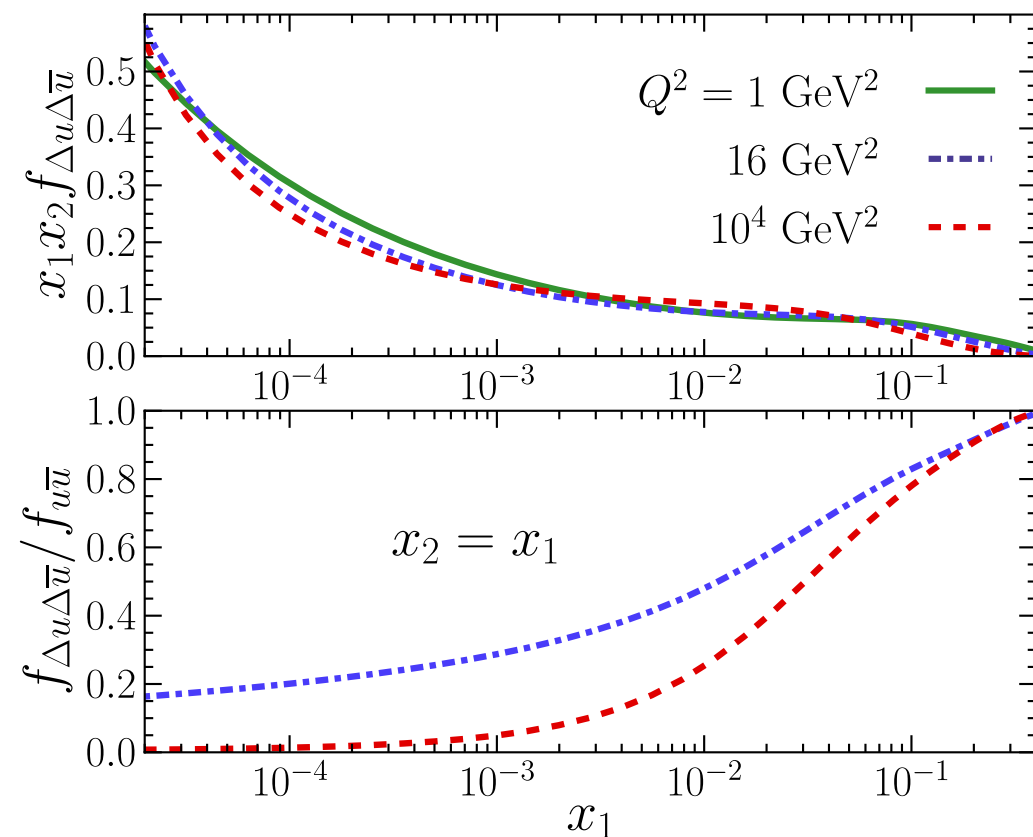
M. Diehl, TK, 2012

- *Max scenario* - each polarized DPD as large as possibly allowed

\Rightarrow Polarized DPDs equal to unpolarized at starting scale

- Evolve with double DGLAP evolution to higher scales

Longitudinal quark polarization

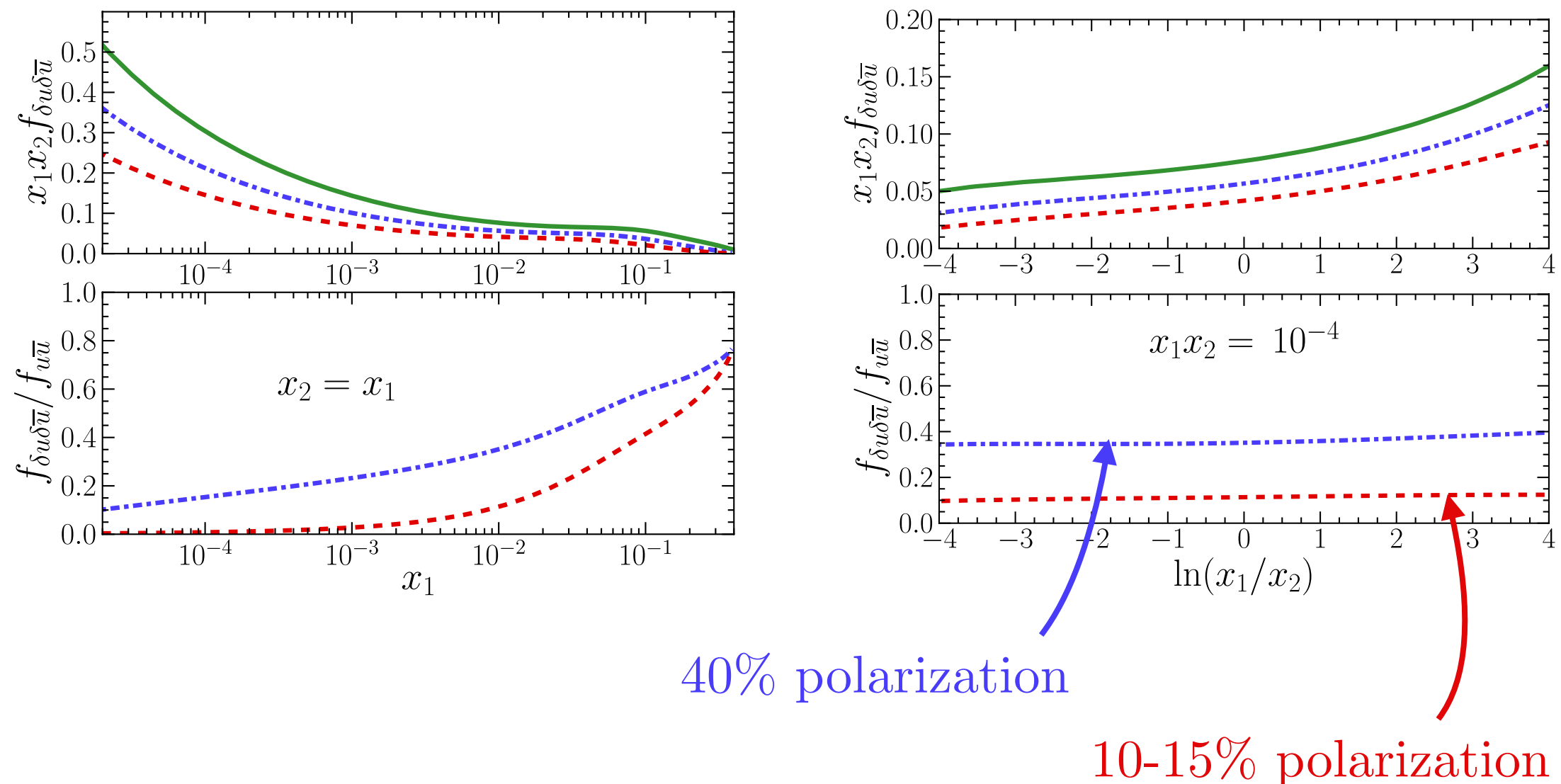


50% polarization

20% polarization

- *Max scenario:* Diehl, TK, Keane 2014
 - Large longitudinal polarization up to high scales in wide range of x_i
 - Degree of polarization flat in rapidity - generic feature in *max scenario*

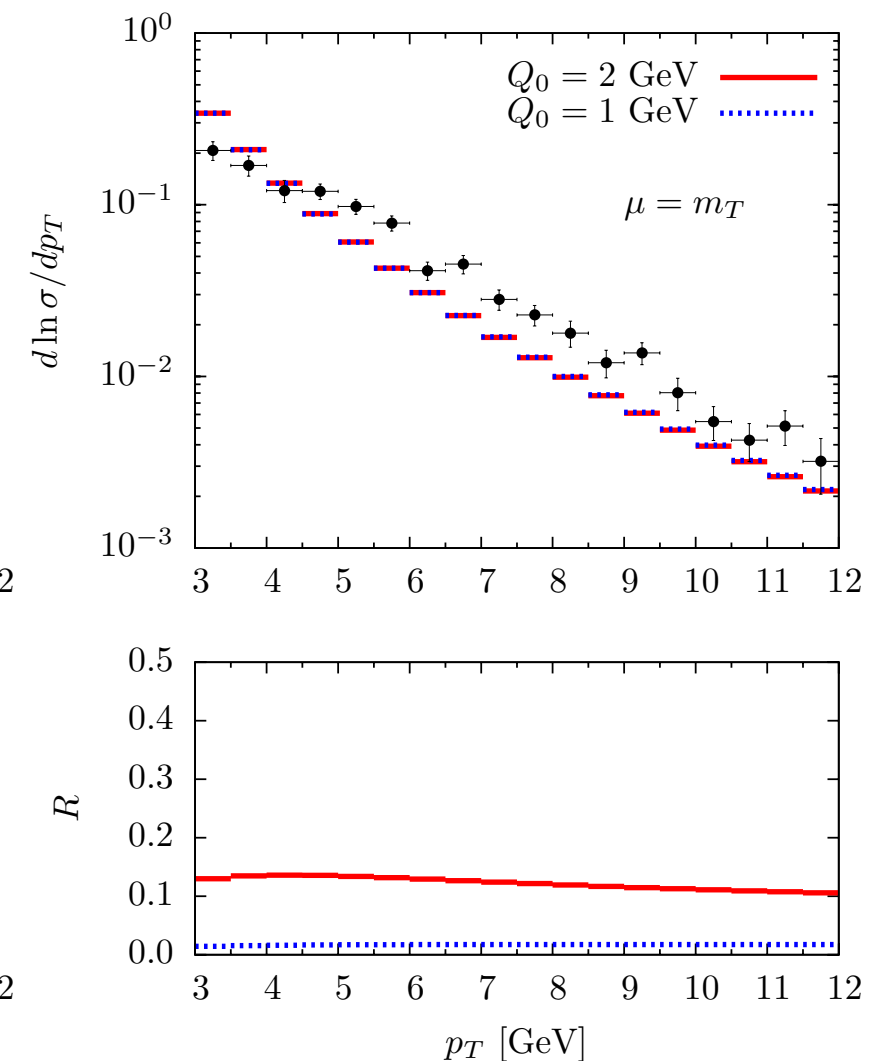
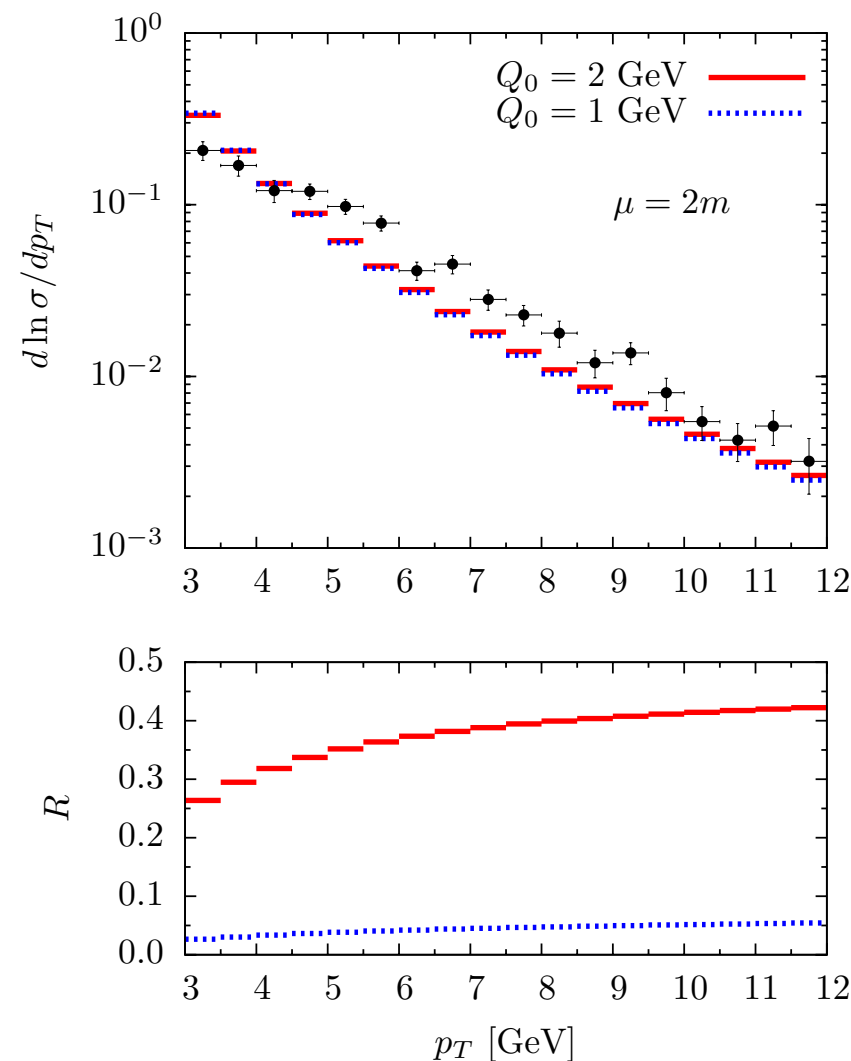
Transverse quark polarization



- *Max scenario:* Diehl, TK, Keane 2014
- Sizable transverse polarization up to high scales in wide range of x_i
- Degree of polarization flat in rapidity - generic feature in *max scenario*

Double open charm at LHCb

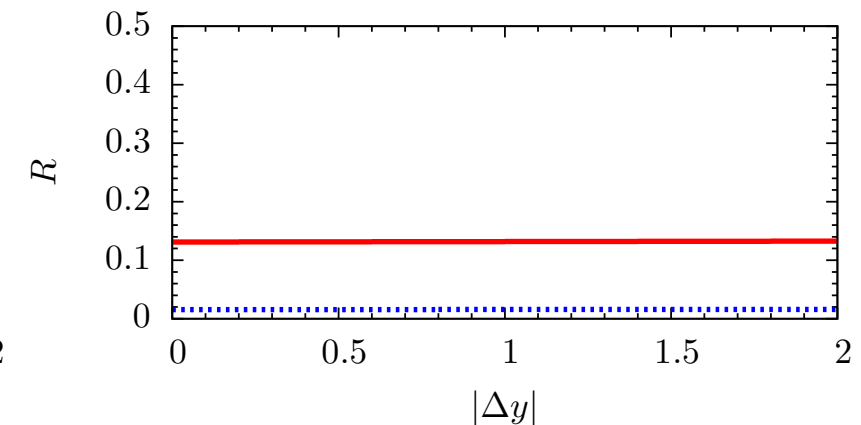
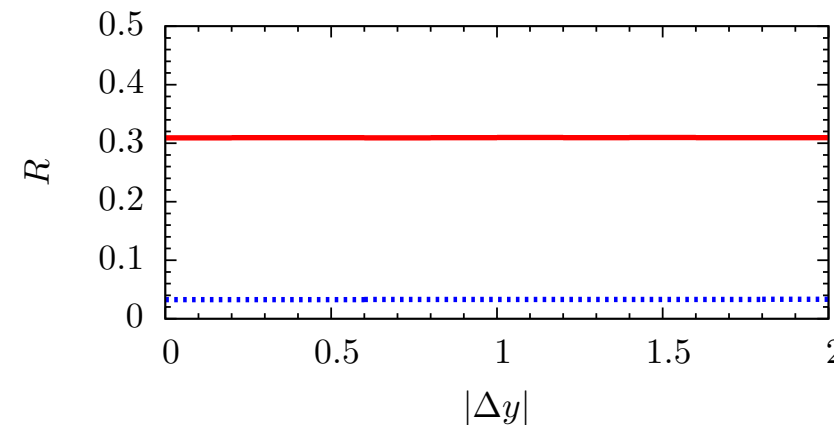
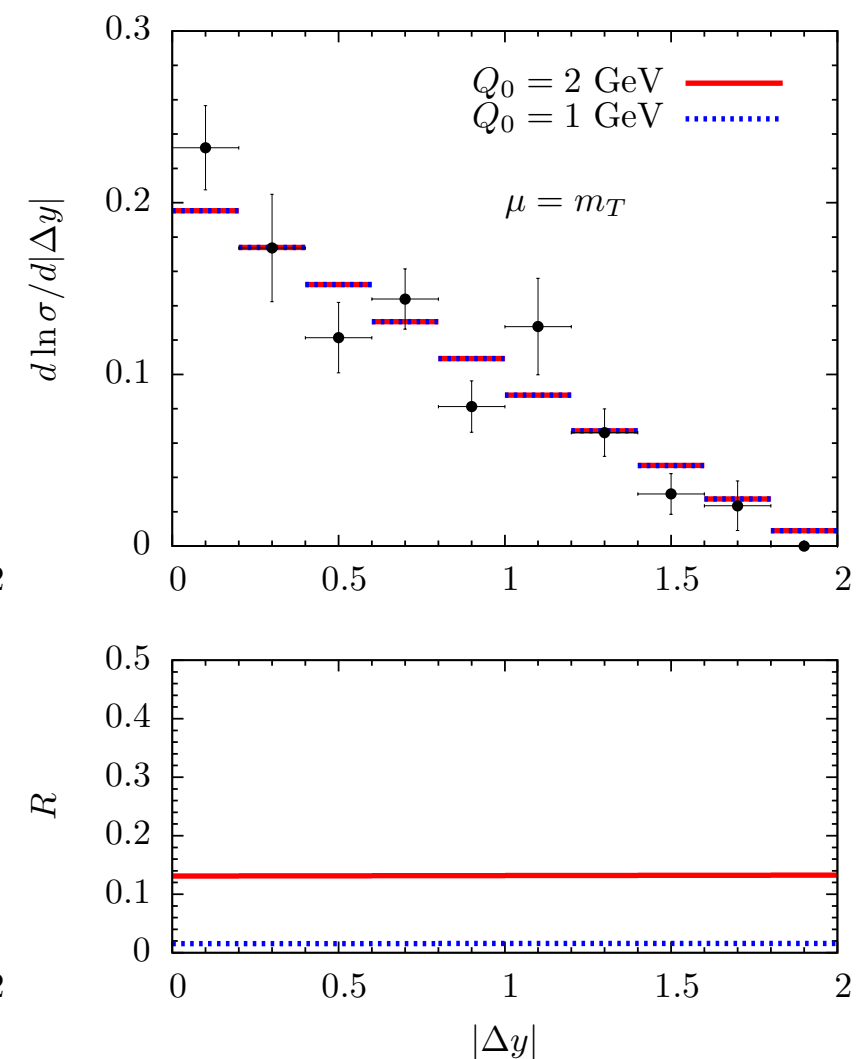
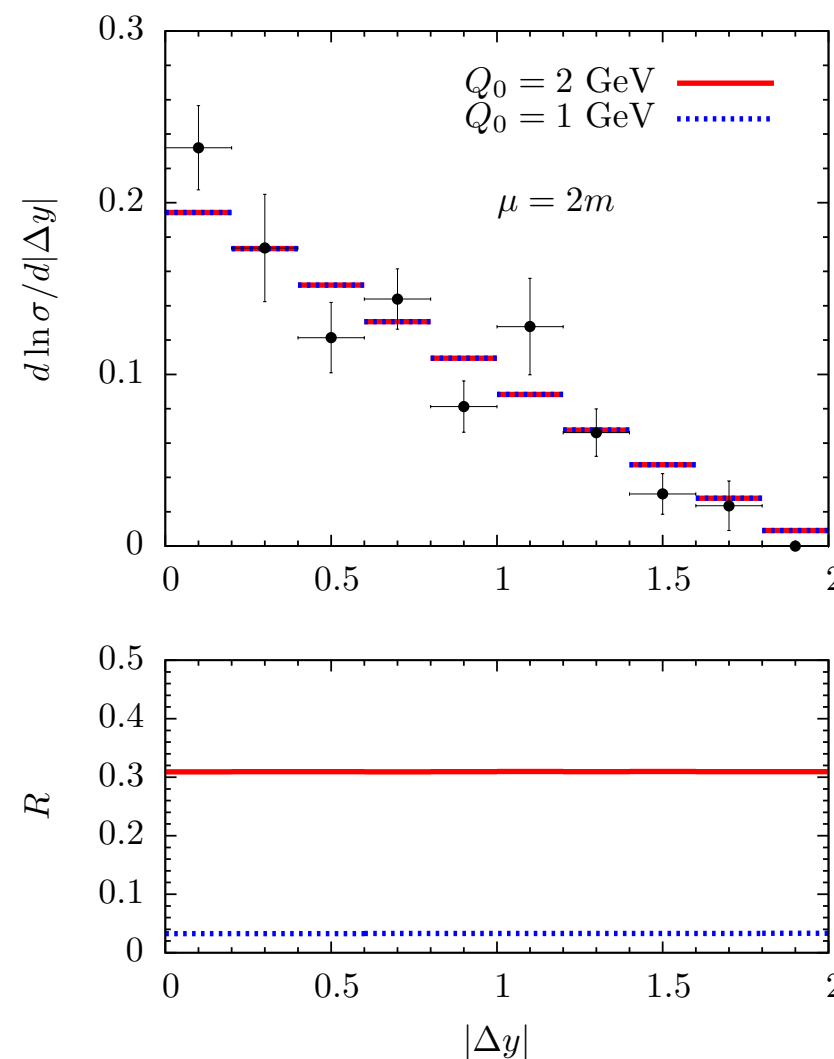
- $D^0 D^0$ data from LHCb
- Polarization does not affect shape of distribution
- With $Q_0 = 1$ GeV small contribution of polarized gluons
- With $Q_0 = 2$ GeV large contribution of polarized gluons
- Strong dependence on scale choice



Echevarria, TK, Mulders, Pisano, 2015

Double open charm at LHCb

- $D^0 D^0$ data from LHCb
- Polarization does not affect shape of distribution
- With $Q_0 = 1$ GeV small contribution of polarized gluons
- With $Q_0 = 2$ GeV large contribution of polarized gluons
- Strong dependence on scale choice

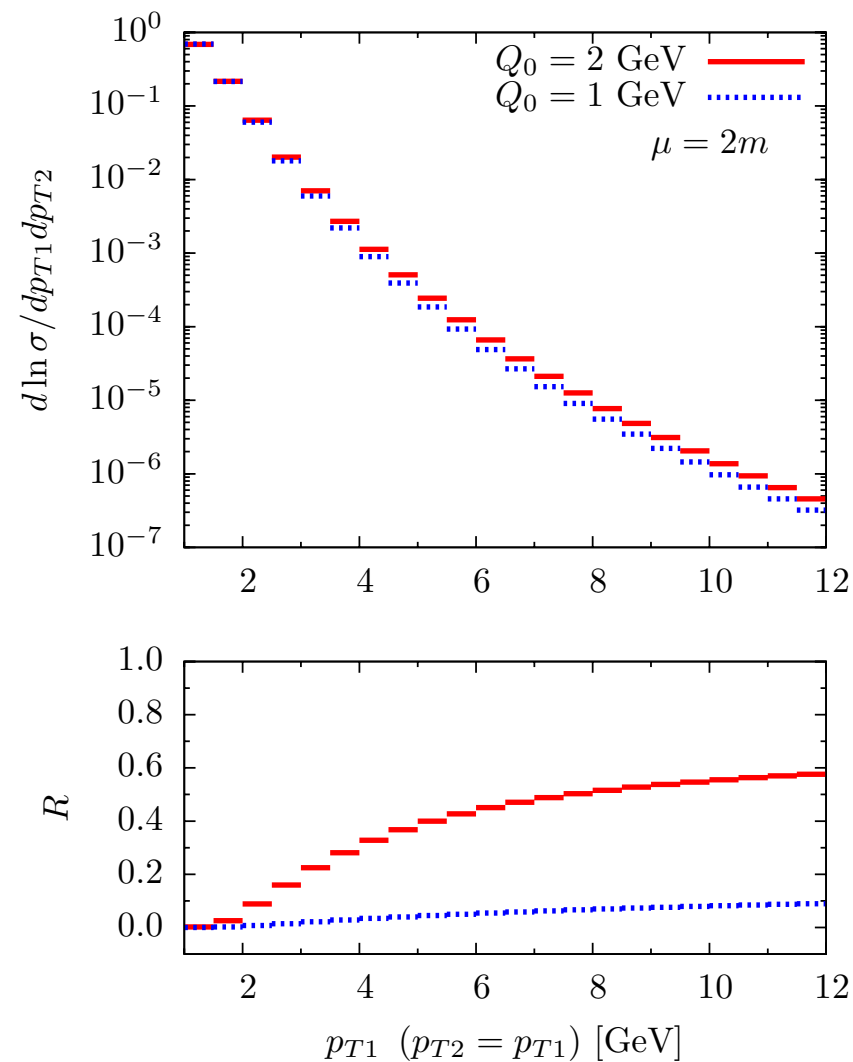


Echevarria, TK, Mulders, Pisano, 2015

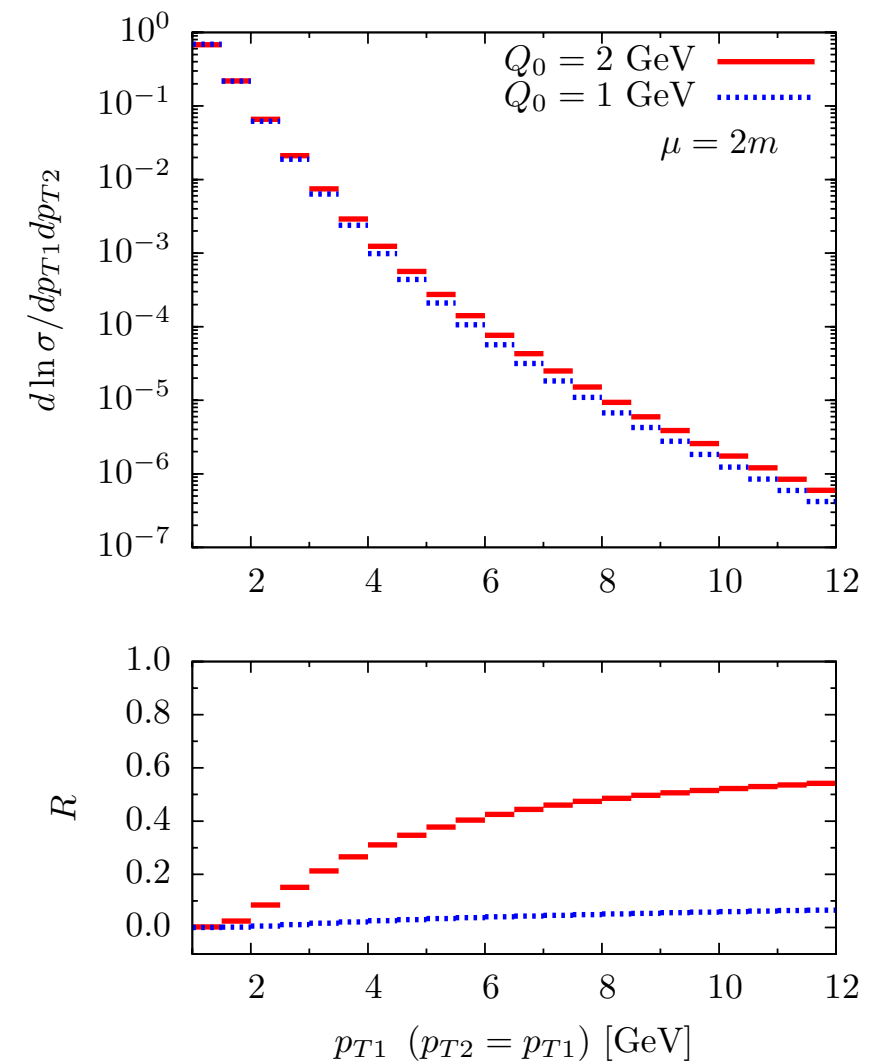
Double open charm at LHCb

- Double differential cross section - shows strong shape dependence

7 TeV



14 TeV



Echevarria, TK, Mulders, Pisano, 2015

Summary

- Double parton scattering is an increasingly relevant topic, with the energy of the collider and the large luminosity/search for rare events.
- DPDs are interesting (non-perturbative) descriptions of the proton
- Ignoring correlations gives simple, order of magnitude, estimates for DPS cross sections
- Bulk of DPS phenomenology so far based on this simplified approach
- But, spins can be correlated
 - ⇒ Gives polarized double parton distributions
- A few studies has included polarization, but there is much work still to be done.
- Much of the knowledge, and even calculations, from TMD community can be directly used in calculations of spin asymmetries etc. in double parton scattering