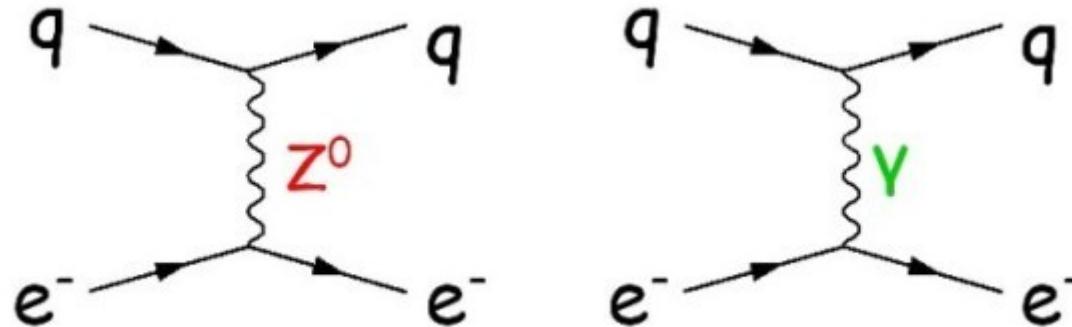


# Parity Violation Inelastic Scattering Experiments at Jlab



Vincent Sulkosky

University of Virginia

**XXIII International Workshop on Deep-Inelastic Scattering and  
Related Subjects (DIS 2015)**

April 29<sup>th</sup>, 2015

Acknowledgement: X. Zheng



# Outline

- Electron scattering basics
- PVDIS and electron-quark effective couplings
- The JLab 6 GeV PVDIS experiment
- DIS results - electron-quark effective VA couplings
- Resonance results
- Summary and Perspectives



# Basics of Inclusive Electron Scattering

Energy transfer:

$$\nu = E - E'$$

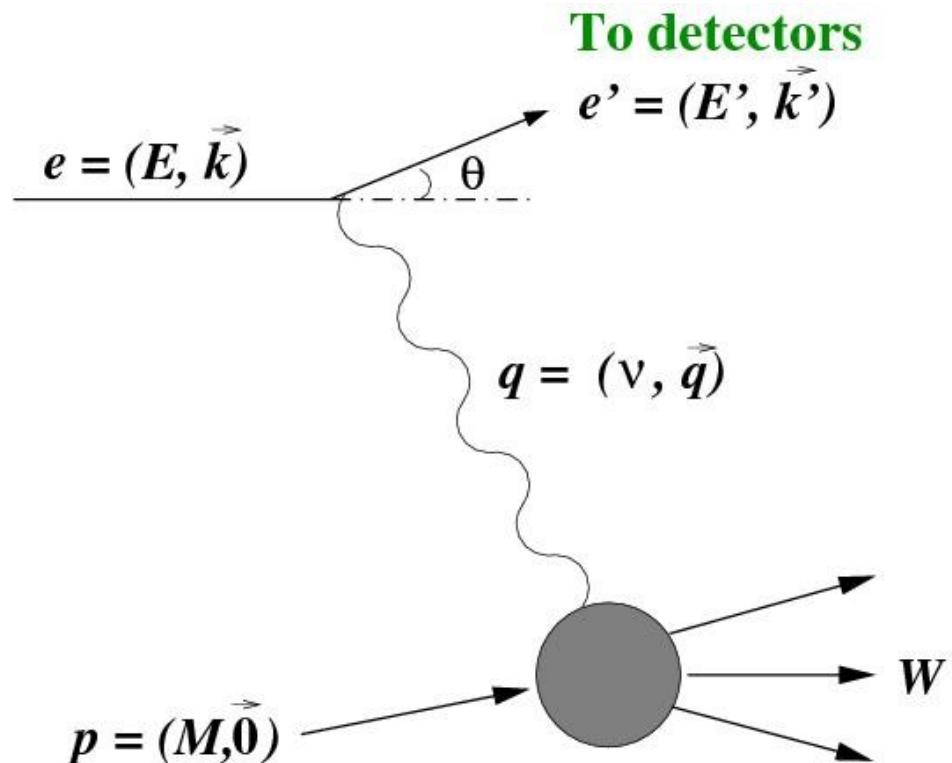
Momentum transfer:

$$\vec{q} = \vec{k} - \vec{k}'$$

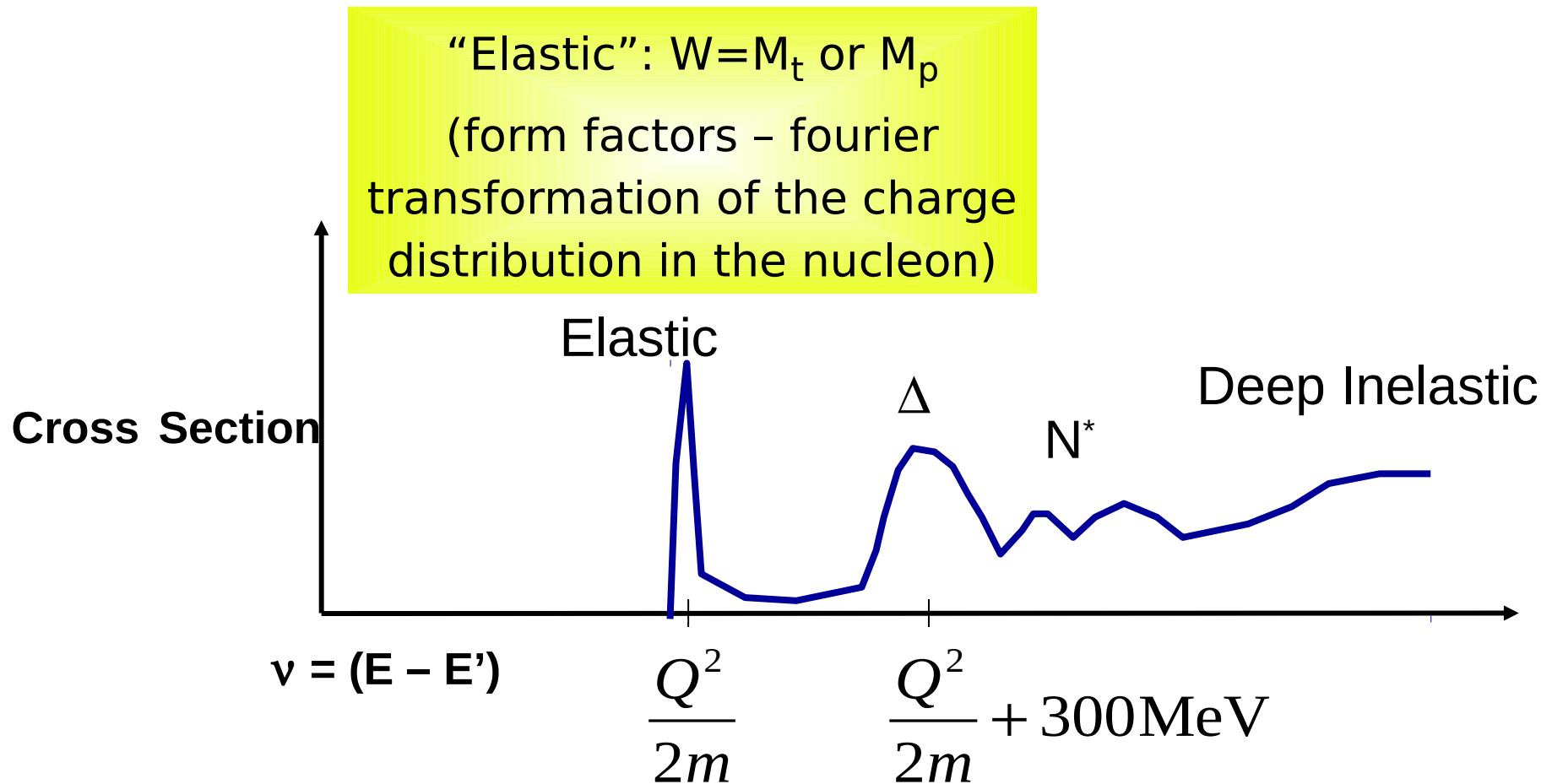
4-momentum transfer squared:

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

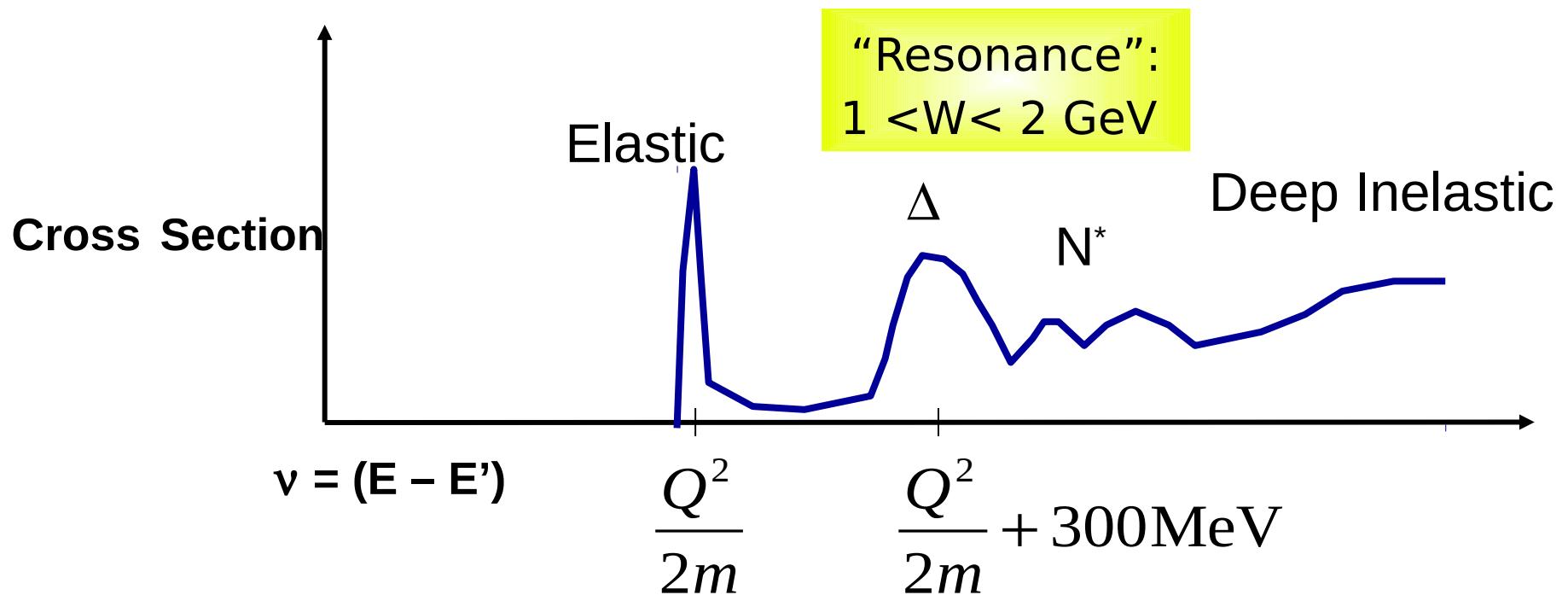
One-photon exchange (Born approximation) for e-p scattering



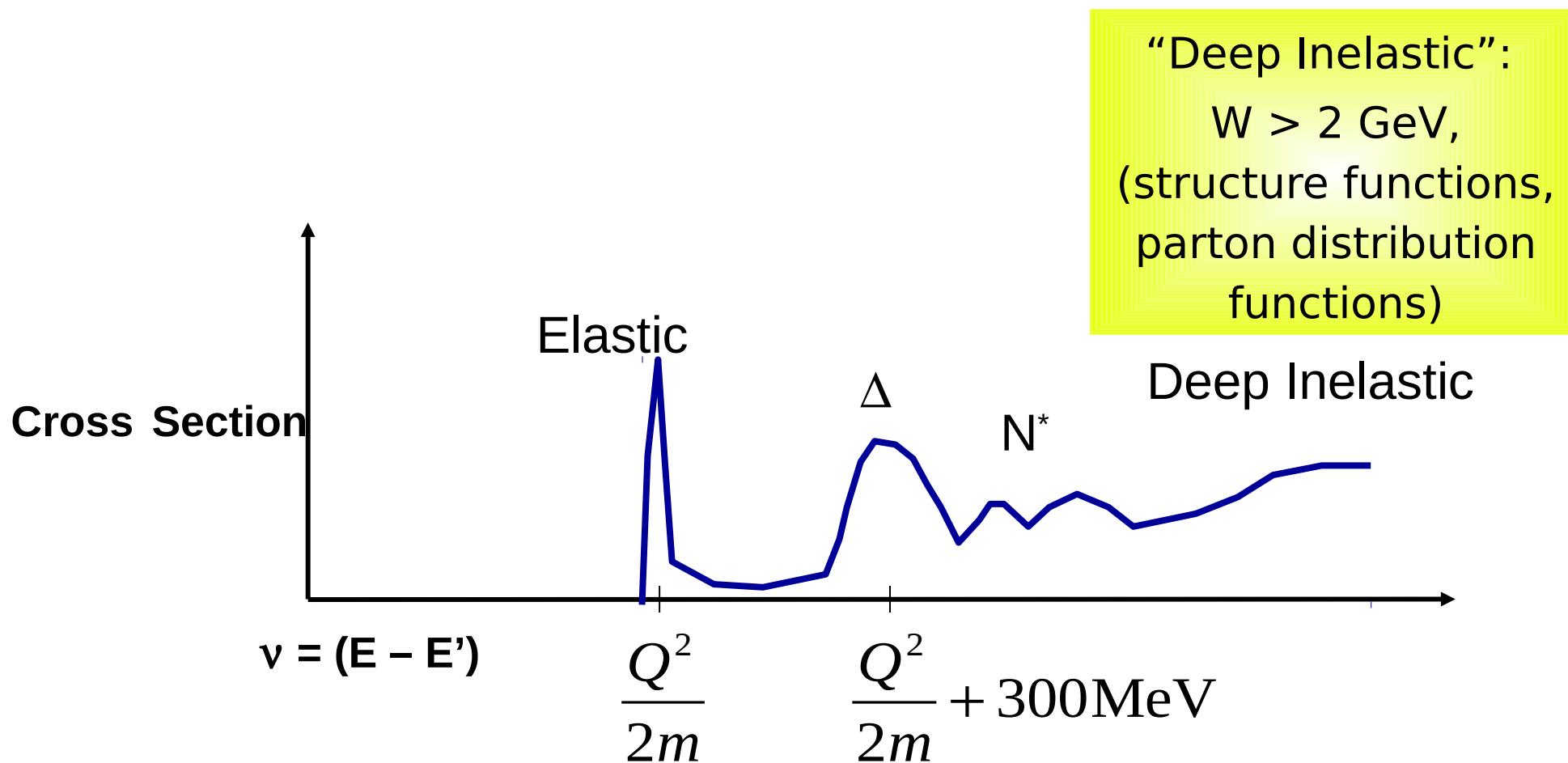
# Inclusive Electron Scattering at Fixed Momentum ( $Q^2$ )



# Inclusive Electron Scattering at Fixed Momentum ( $Q^2$ )



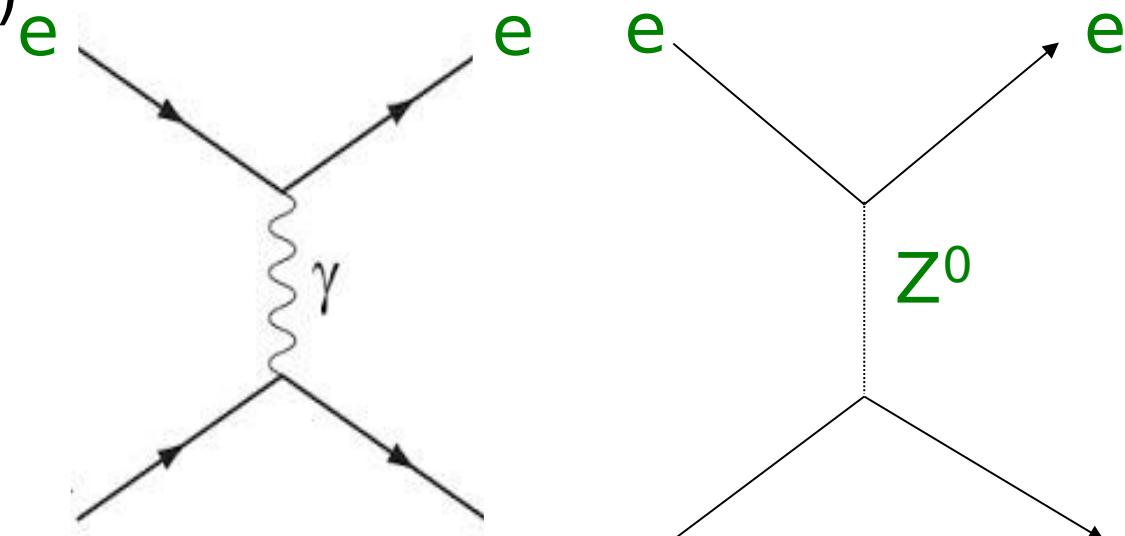
# Inclusive Electron Scattering at Fixed Momentum ( $Q^2$ )



# Parity-Violating Electron Scattering (PVES)

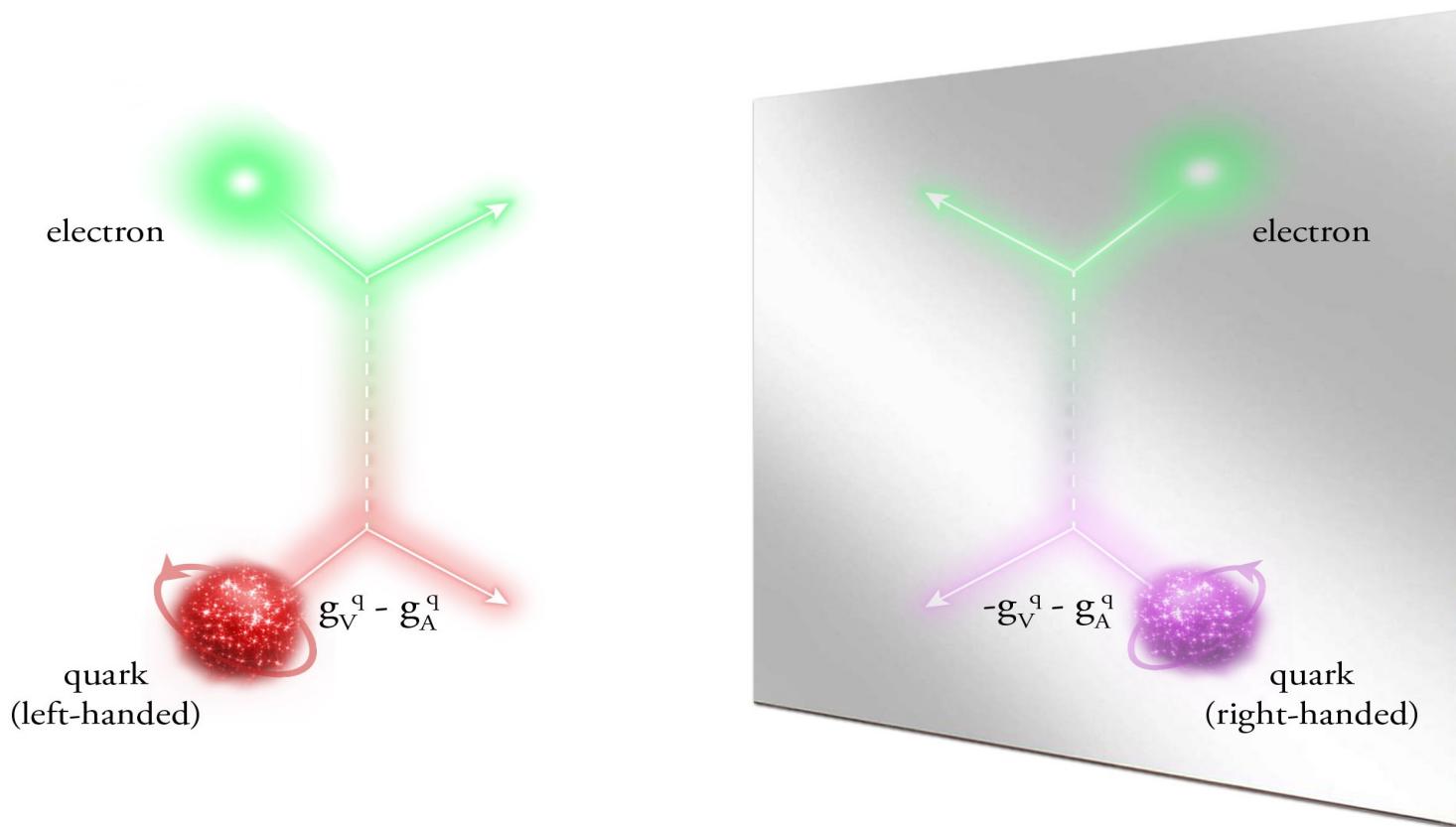
- To study nucleon structure not accessible in the electromagnetic interaction:
  - ✚ elastic PVES: nucleon strange form factors (SAMPLE@MIT/Bates, A4@MAINZ, HAPPEX, G0 @ JLab); “neutron skin” in heavy nucleus (PREX@JLab)
- To test the electroweak Standard Model:
  - ✚ e-e (E158@SLAC)
  - ✚ PVDIS

$$A_{PV} \approx \frac{Q^2}{Q^2 + M_Z^2} \approx 10^{-4} Q^2$$



interference causes parity-violating asymmetry

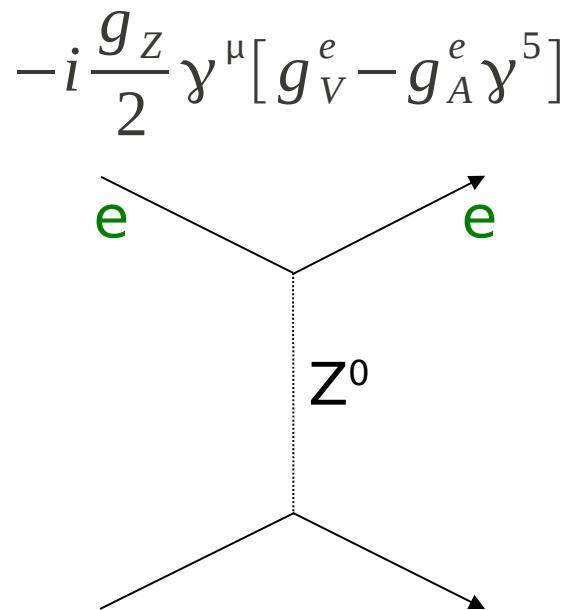
# Parity Violation in the Standard Model



- In weak interaction, all elementary fermions behave differently under parity transformation.  
↓
- They have a preferred chiral state when coupling to the  $Z^0$

# Parity Violation in the Standard Model

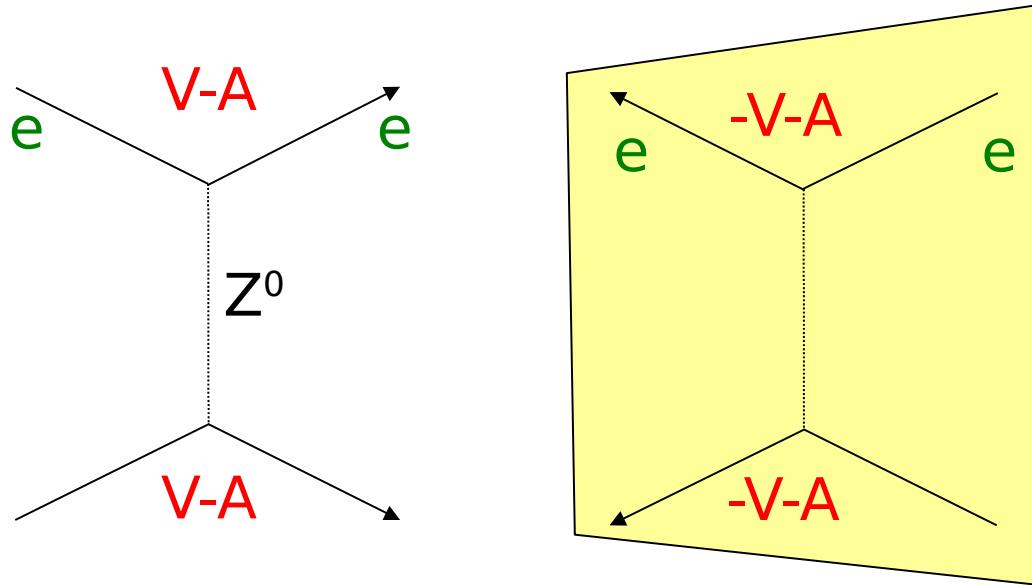
- Unlike electric charge, two charges (couplings) are needed for the weak interaction:  $g_L$ ,  $g_R$   
or “vector” and “axial” weak charges:  $g_V \sim (g_L + g_R)$ ,  $g_A \sim (g_L - g_R)$



fermions	$g_A^f = I_3$	$g_V^f = I_3 - 2Q \sin^2 \theta_W$
$\nu_e, \nu_\mu$	$\frac{1}{2}$	$\frac{1}{2}$
$e^-, \mu^-$	$-\frac{1}{2}$	$-\frac{1}{2} + 2 \sin^2 \theta_W$
$u, c$	$\frac{1}{2}$	$\frac{1}{2} - \frac{4}{3} \sin^2 \theta_W$
$d, s$	$-\frac{1}{2}$	$-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_W$

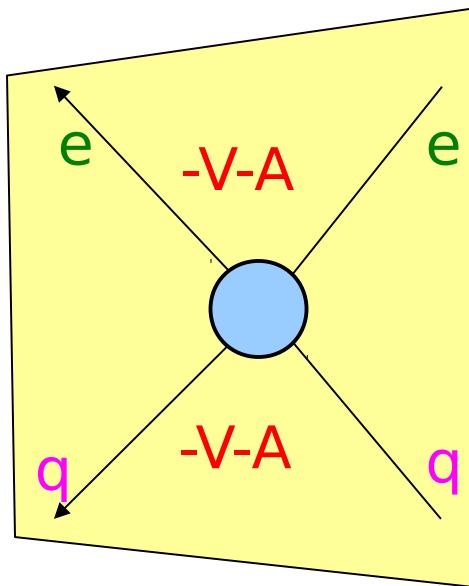
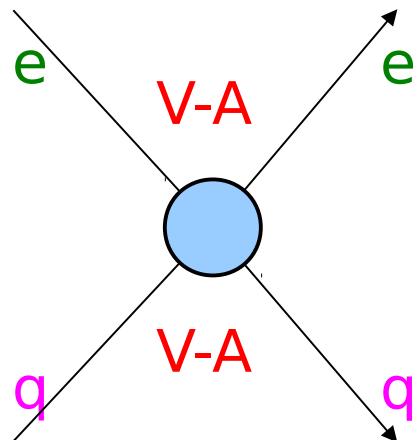
# Parity Violation in the Standard Model

- Unlike electric charge, two charges (couplings) are needed for the weak interaction:  $g_L$ ,  $g_R$   
or “vector” and “axial” weak charges:  $g_V \sim (g_L + g_R)$ ,  $g_A \sim (g_L - g_R)$
- PVES asymmetry comes from  $\mathbf{V}(e) \times \mathbf{A}(\text{targ})$  and  $\mathbf{A}(e) \times \mathbf{V}(\text{targ})$   
“electron-quark effective couplings”  $C_{1q} \equiv 2 g_A^e g_V^q$ ,  $C_{2q} \equiv 2 g_V^e g_A^q$



# Effective Couplings and New Contact Interactions

- Unlike electric charge, two charges (couplings) are needed for the weak interaction:  $g_L$ ,  $g_R$  or “vector” and “axial” weak charges:  $g_V \sim (g_L + g_R)$ ,  $g_A \sim (g_L - g_R)$
- PVDIS asymmetry comes from: “electron-quark effective couplings”



$$C_{1q} = g_{AV}^{e q}, C_{2q} = g_{VA}^{e q}$$

Erler and Su, Prog. Part. Nucl. Phys. 71, 119 (2013)

# Accessing $C_{1q,2q}$

- Polarized electron beam on hadronic target, compare scattering between left-handed electron beam vs. right-handed.
- Elastic PVES:
  - directly probes  $C_{1q}$ , electrons' parity-violating property;
  - quarks' parity-violation  $\leftrightarrow$  nucleon axial form factor  $G_A$ , and extracting  $C_{2q}$  from  $G_A$  is model-dependent
- Only in PVDIS, electron probes the quark and PVDIS asymmetry depends on  $C_{2q}$  directly.



# Formalism for Parity Violation in DIS

$$A_{PV} = \frac{G_F Q^2}{\sqrt{2} \pi \alpha} [a(x) + Y(y) b(x)]$$

$$x \equiv x_{Bjorken} \quad y \equiv 1 - E' / E$$
$$q_i^+(x) \equiv q_i(x) + \bar{q}_i(x)$$
$$q_i^-(x) = q_i^V(x) \equiv q_i(x) - \bar{q}_i(x)$$

**For an isoscalar target  
( ${}^2\text{H}$ ), structure  
functions largely  
simplify:**

$$a(x) = \frac{3}{10} (2C_{1u} - C_{1d}) \left( 1 + \frac{0.6 s^+}{u^+ + d^+} \right)$$

$$b(x) = \frac{3}{10} (2C_{2u} - C_{2d}) \left( \frac{u_v + d_v}{u^+ + d^+} \right)$$



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$$A_{PV} = \frac{G_F Q^2}{\sqrt{2} \pi \alpha} [a(x) + Y(y) b(x)]$$

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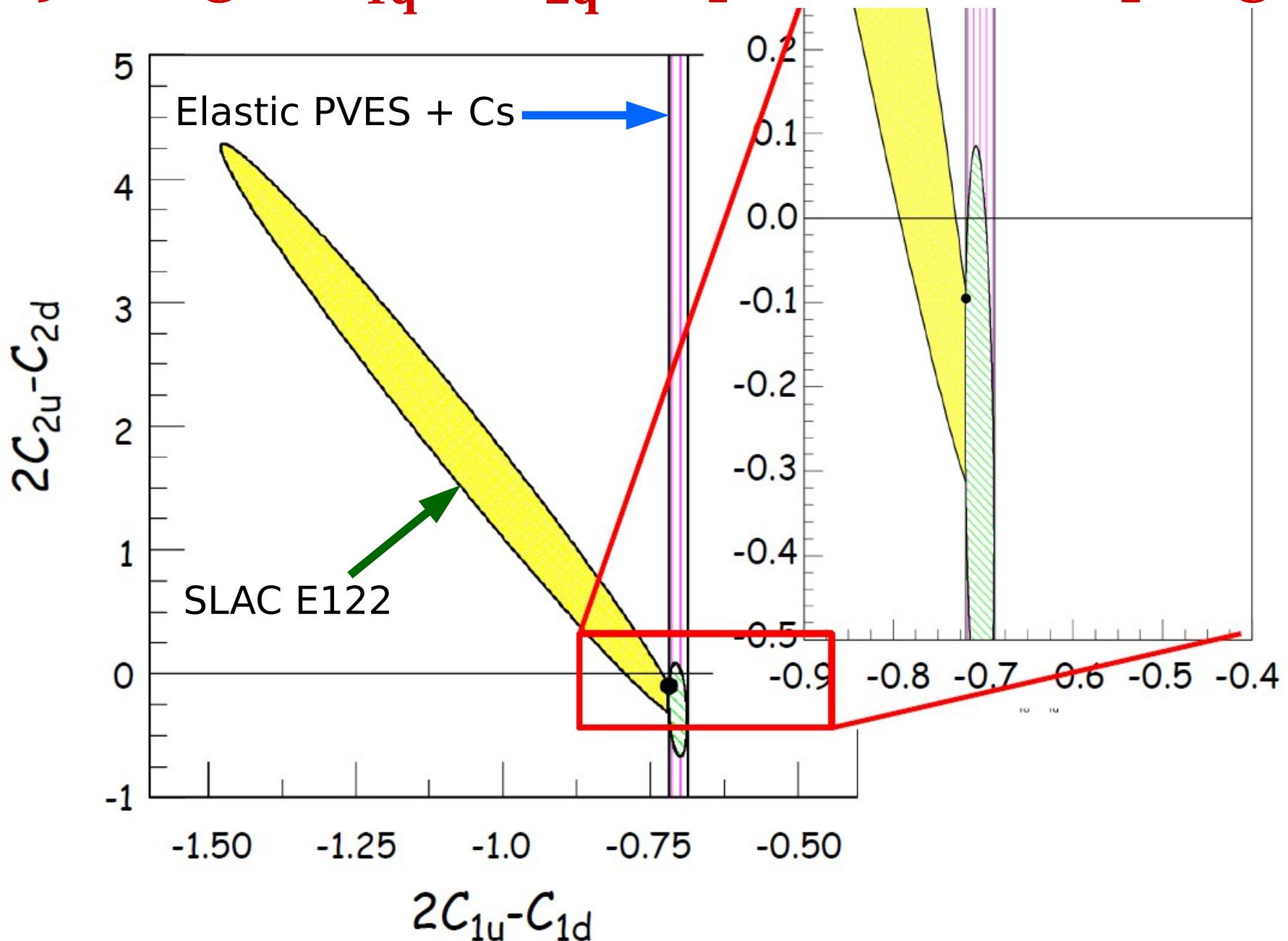
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$$b(x) = \frac{3}{10} (2C_{2u} - C_{2d}) \left( \frac{u_v^+ + d_v^+}{u^+ + d^+} \right)$$

If neglecting sea quarks, asymmetry is no longer sensitive to PDFs  $\rightarrow$  “static limit”

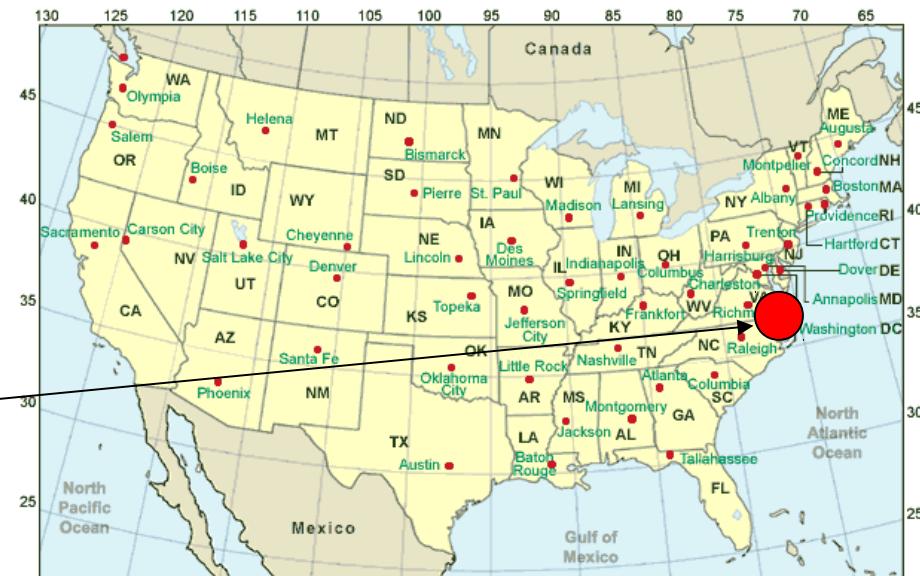
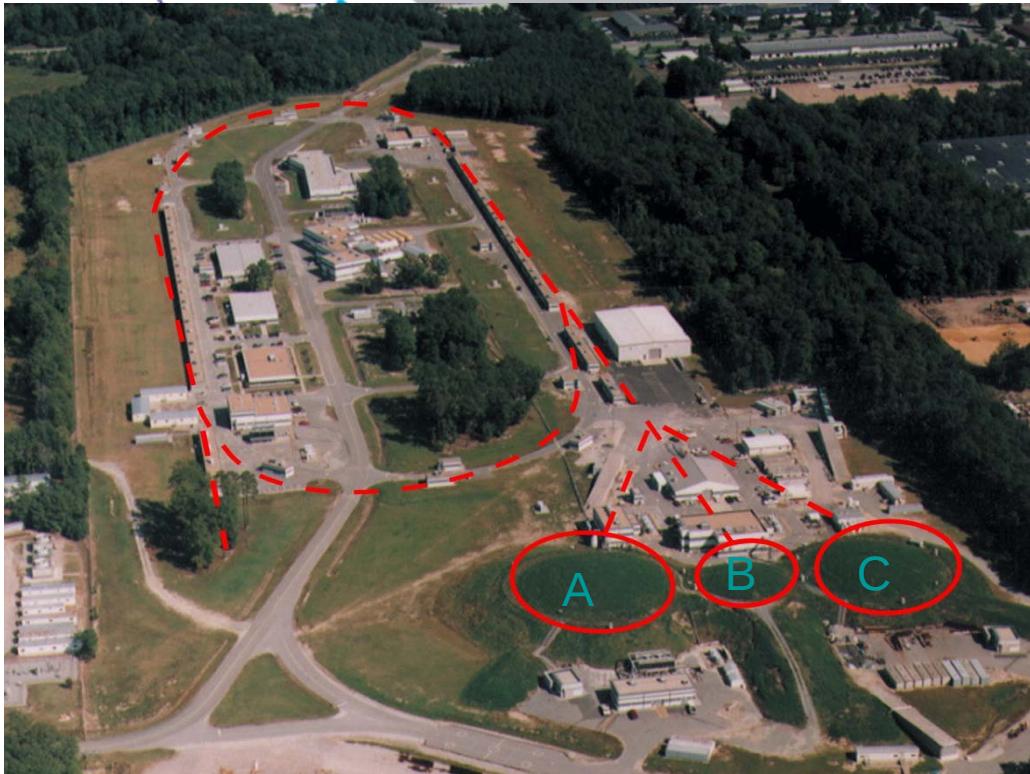
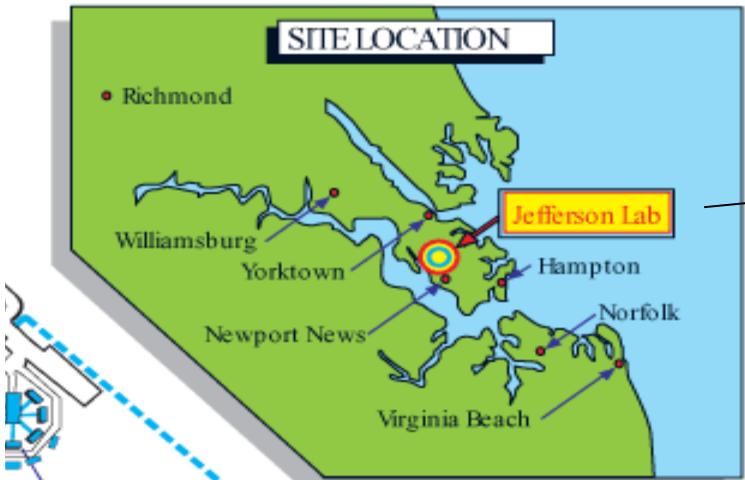


# Projecting to $C_{1q}$ vs $C_{2q}$ (e-q AV vs. VA couplings)



# Jefferson Lab

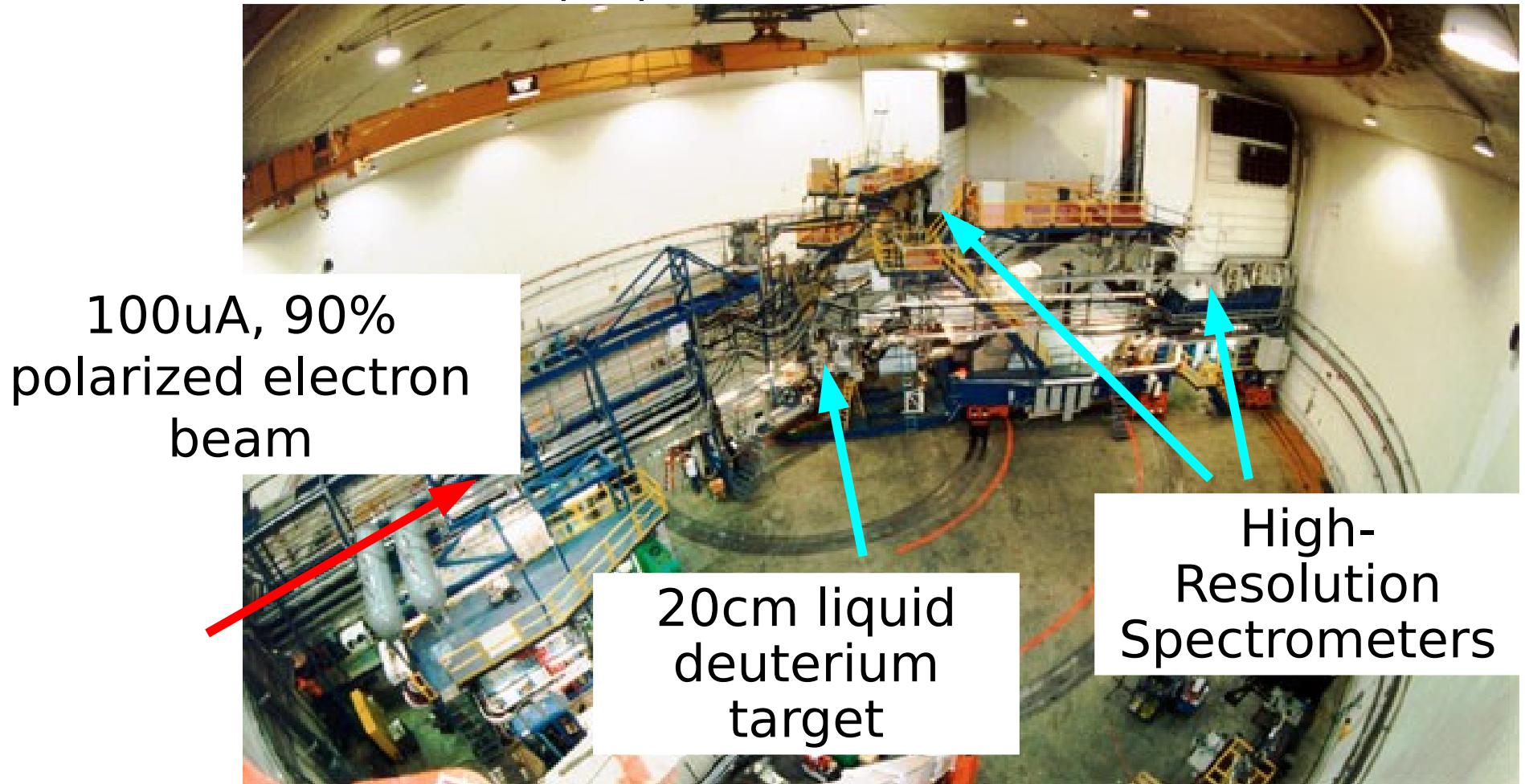
Thomas Jefferson National Accelerator Facility



- **Staff: ~700**
- **User community: ~1300**
  - Beam first delivered in 10/95
  - ~1/3 of US PhDs in Nuclear Physics
  - Energy: 6 GeV, 12 GeV ongoing
  - **The first and largest superconducting RF accelerator in the world, the highest polarized luminosity.**

# PVDIS at 6 GeV (JLab E08-011, ran in Oct-Dec. 2009)

- Measured two DIS points:  $Q^2=1.085$  and  $1.901 \text{ (GeV/c)}^2$
- Collected 170 billion (E9) electrons in total



- Students: Xiaoyan Deng, Kai Pan, Diancheng Wang (PhD)
- Postdoc: Ramesh Subedi

# From Measured to Physics Asymmetry

$$A_{Q^2=1.085, x=0.241}^{raw} = -78.45 \pm 2.68 \pm 0.07 \text{ ppm}$$

$$A_{Q^2=1.901, x=0.295}^{raw} = -140.30 \pm 10.43 \pm 0.16 \text{ ppm (L)}$$

$$A_{Q^2=1.901, x=0.295}^{raw} = -139.84 \pm 6.58 \pm 0.46 \text{ ppm (R)}$$

- beam polarization
- counting deadtime
- EM radiative correction
- box correction
- target aluminum endcap
- beam depolarization
- beam-normal asym
- $Q^2$  determination
- pair production
- target impurity
- charged pion background

$$A_{Q^2=1.085, x=0.241}^{phys} = -91.10 \pm 3.11 \pm 2.97 \text{ ppm}$$

$$A_{Q^2=1.901, x=0.295}^{phys} = -160.80 \pm 6.39 \pm 3.12 \text{ ppm}$$



# Compare to Standard Model?

---

$$A_{Q^2=1.085, x=0.241}^{phys} = -91.10 \pm 3.11 \pm 2.97 \text{ ppm}$$

$$A^{SM} = (1.156 \times 10^{-4}) [ (2C_{1u} - C_{1d}) + 0.348 (2C_{2u} - C_{2d}) ] = -87.7 \text{ ppm}$$

---

$$A_{Q^2=1.901, x=0.295}^{phys} = -160.80 \pm 6.39 \pm 3.12 \text{ ppm}$$

$$A^{SM} = (2.022 \times 10^{-4}) [ (2C_{1u} - C_{1d}) + 0.594 (2C_{2u} - C_{2d}) ] = -158.9 \text{ ppm}$$



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uncertainty due to PDF: 0.5% 5%

uncertainty due to HT: 0.5%/ $Q^2$ , 0.7 ppm

$$A_{Q^2=1.901, x=0.295}^{phys} = -160.80 \pm 6.39 \pm 3.12 \text{ ppm}$$

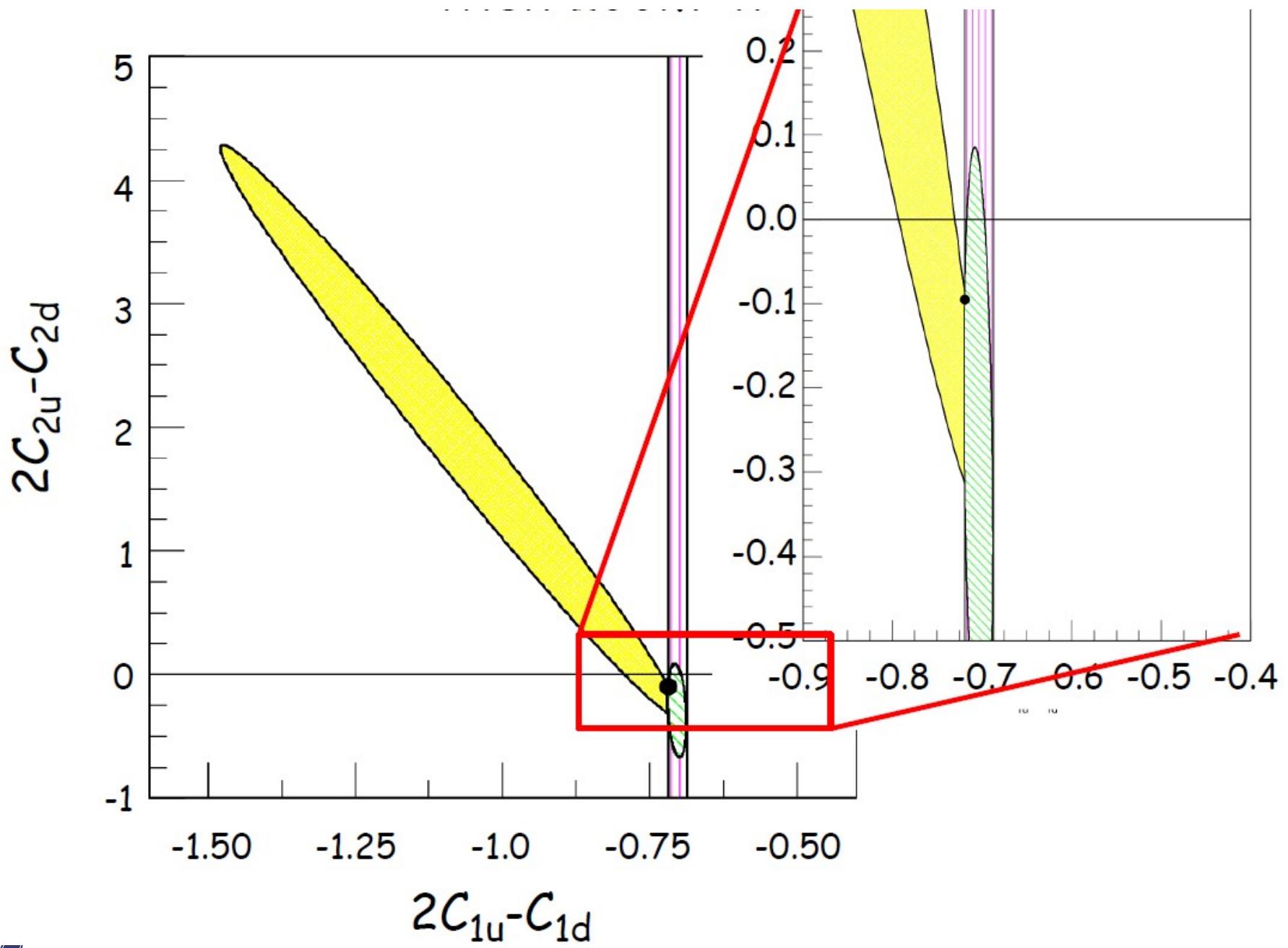
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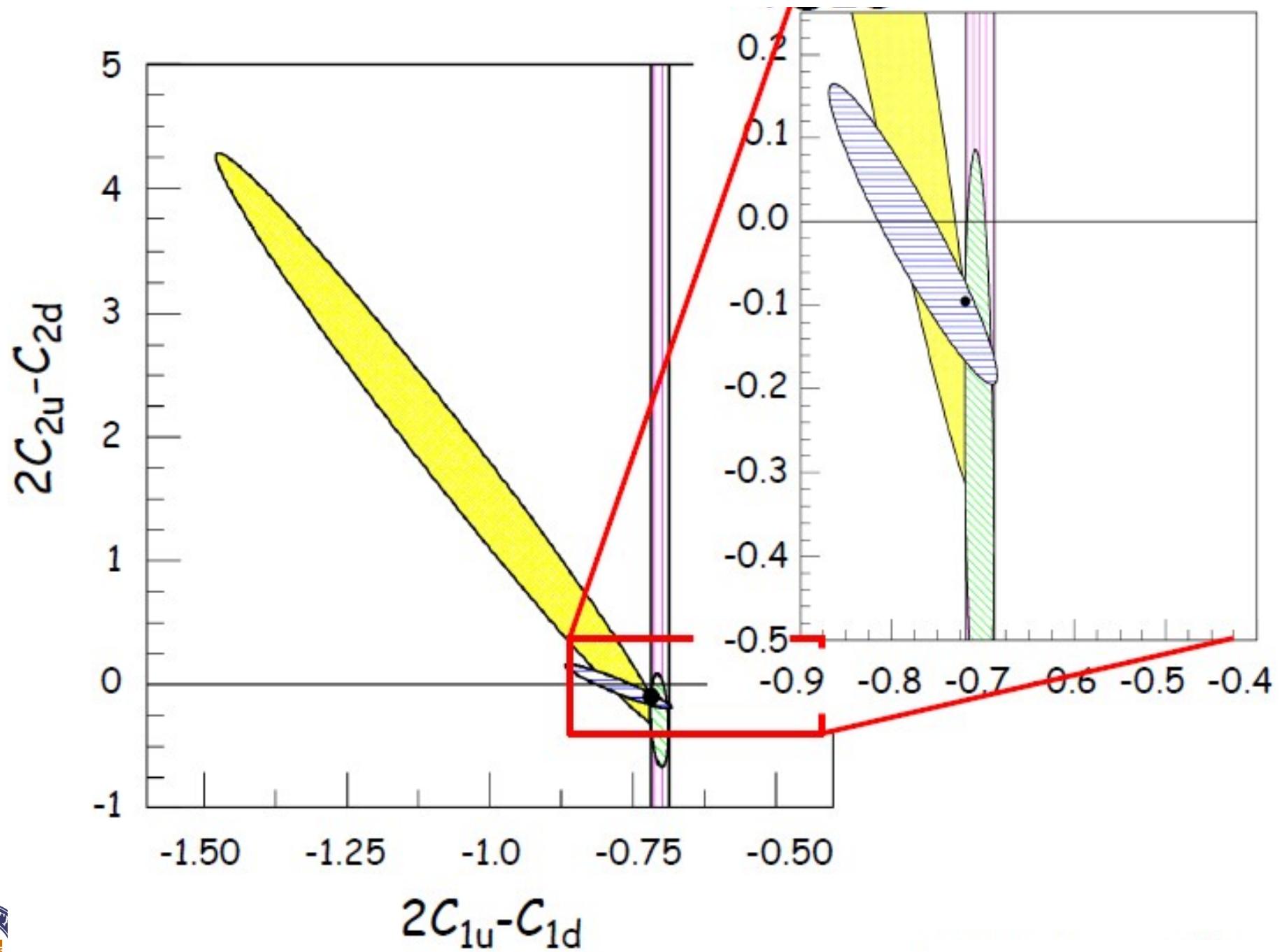
uncertainty due to HT:  $0.5\%/\text{Q}^2$ , 1.2 ppm



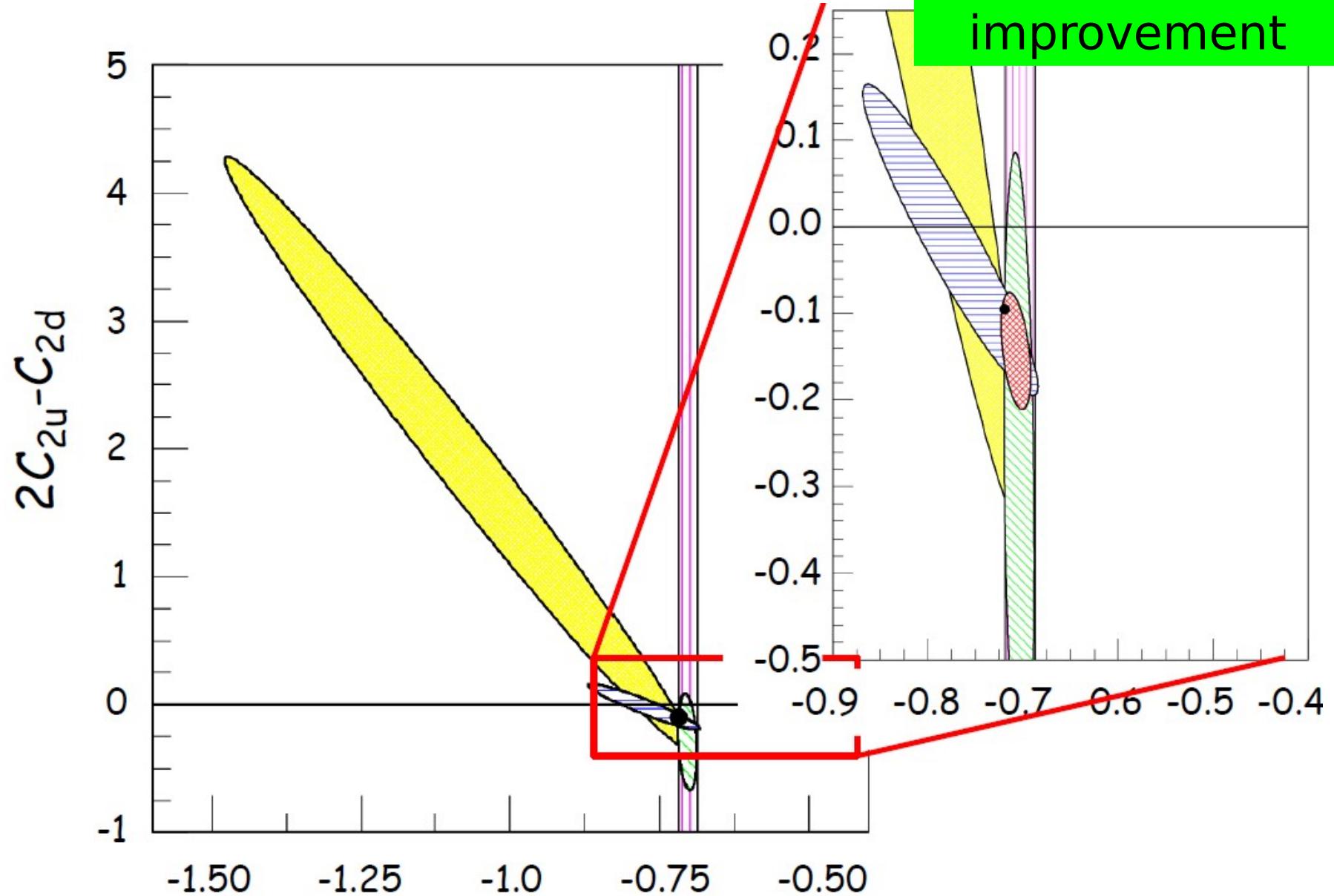
# Previous data: Elastic PVES + APV



# Add Jlab 6 GeV PVDIS



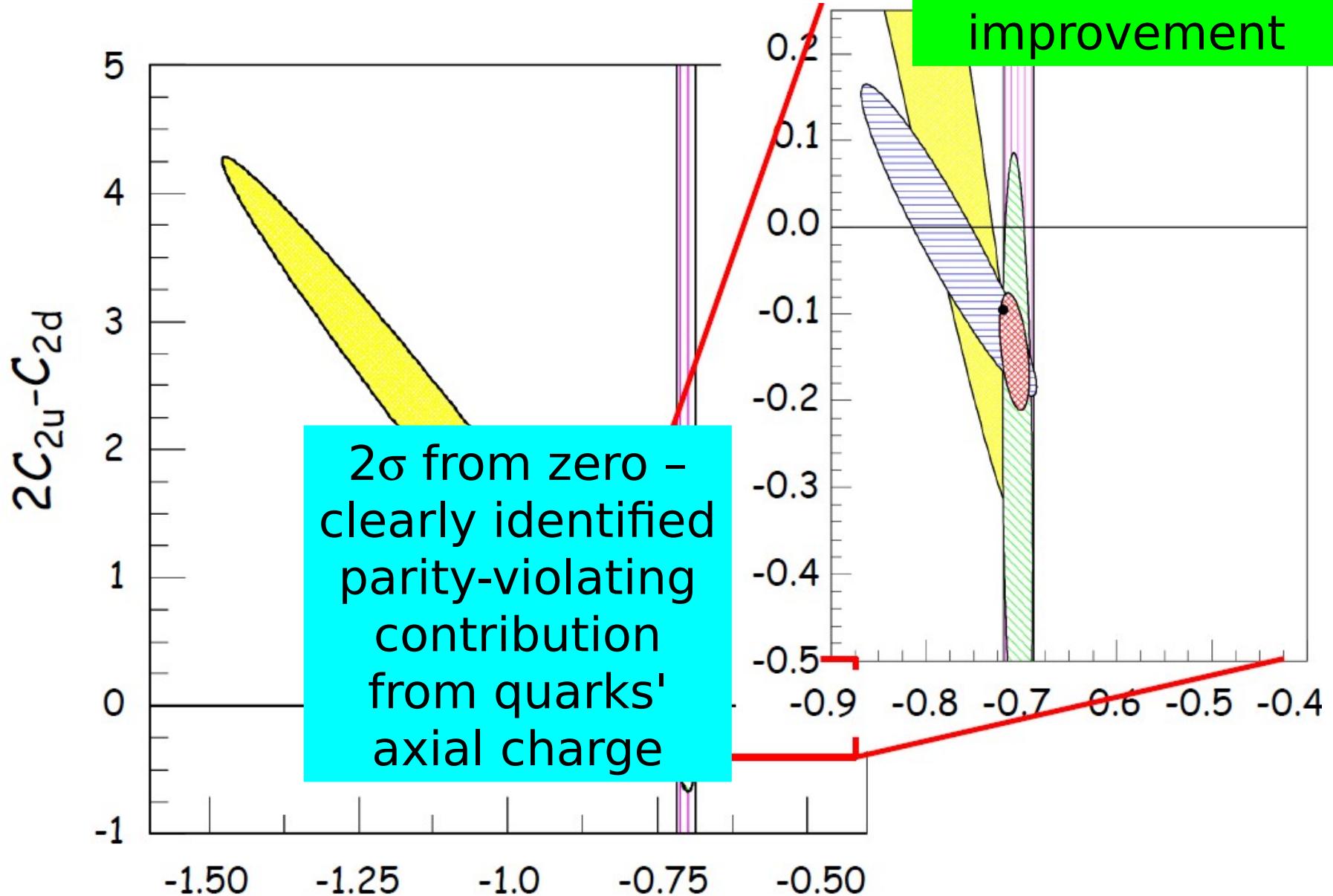
# Best Fit



$2C_{1u}$  Wang et al., Nature 506, no. 7486, 67 (2014);



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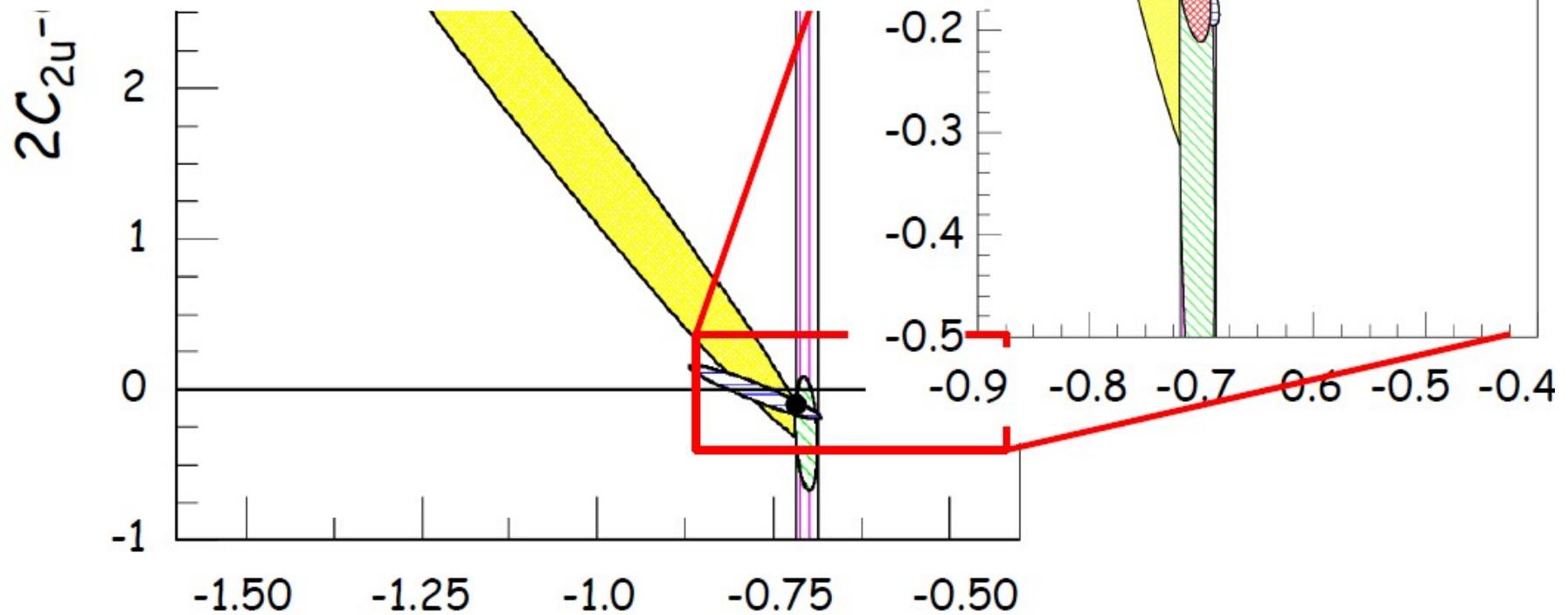
# Best Fit

PARTICLE PHYSICS

## Quarks are not ambidextrous

By separately scattering right- and left-handed electrons off quarks in a deuterium target, researchers have improved, by about a factor of five, on a classic result of mirror-symmetry breaking from 35 years ago. SEE LETTER P.67

Marciano., Nature 506, no. 7486, 43  
(2014);



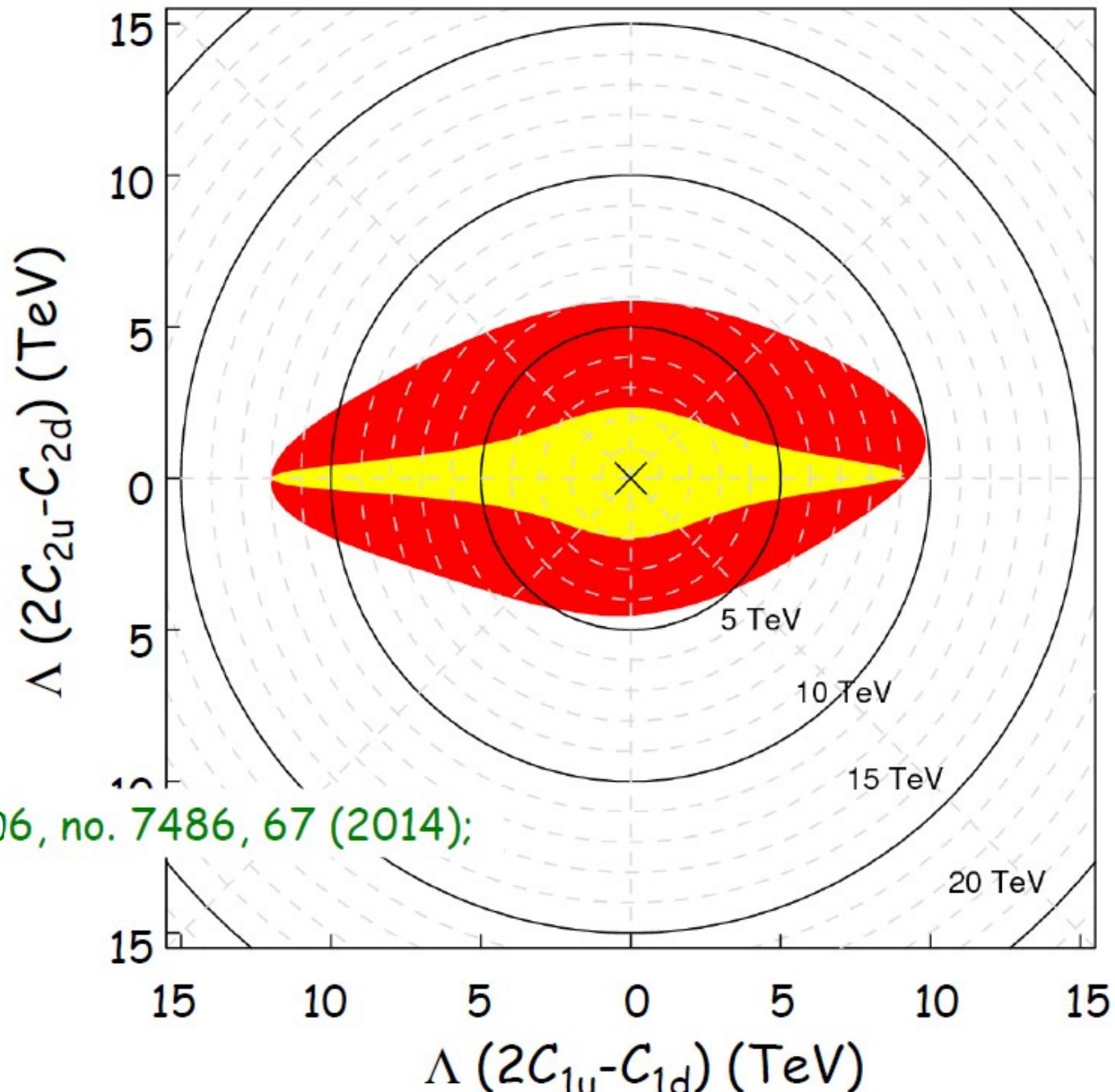
$2C_1$  Wang et al., Nature 506, no. 7486, 67 (2014);



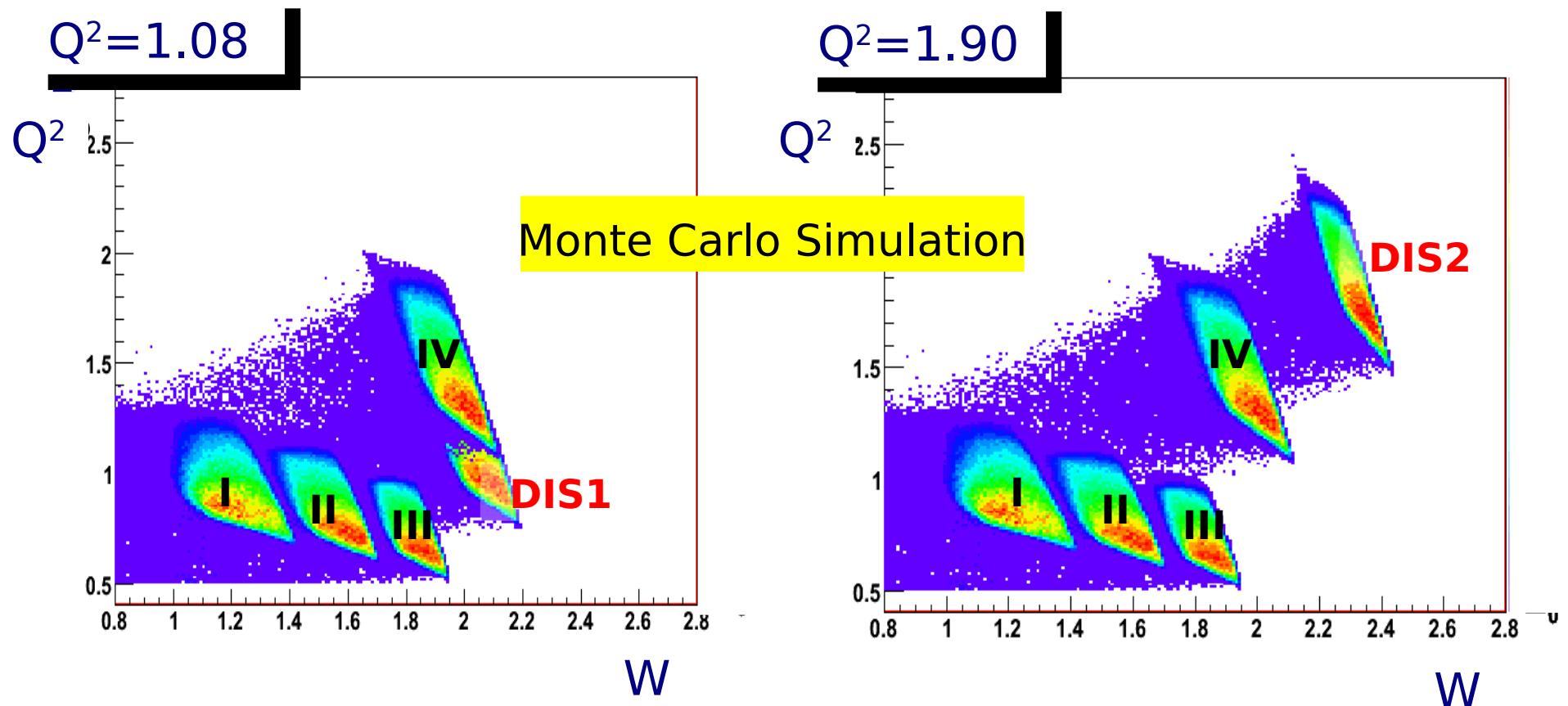
# BSM Mass Limit on e-q VA contact interaction

Complementary  
to LHC results  
on the mass  
limit of electron-  
quark contact  
interactions

Wang et al., Nature 506, no. 7486, 67 (2014);



# Resonance Background Data Coverage



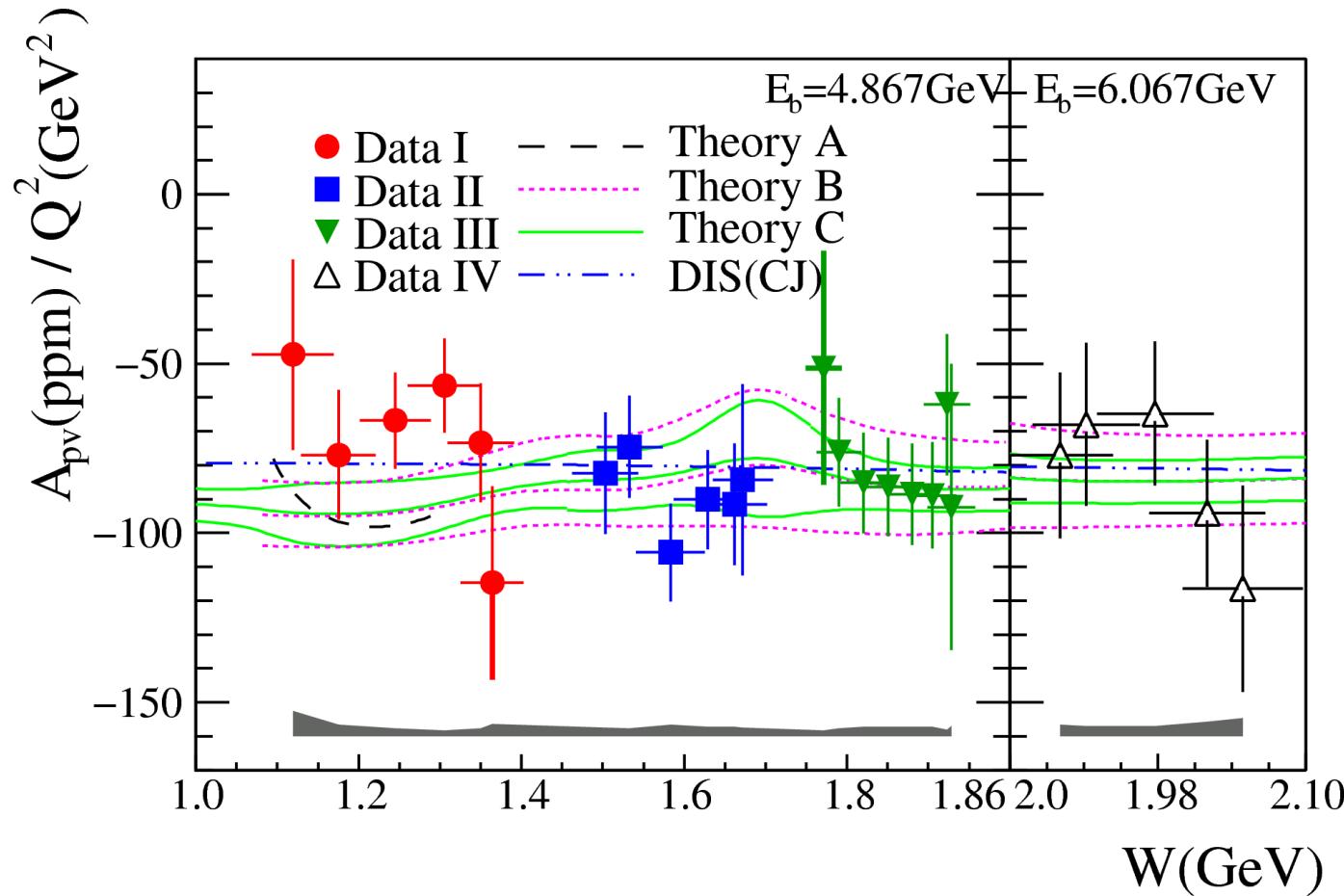
- ◆ Four settings covered the full resonance region;
- ◆ “Grouping” of lead glass blocks allowed a reasonable study of the  $W$ -dependence;

# Resonance PV Asymmetry Results

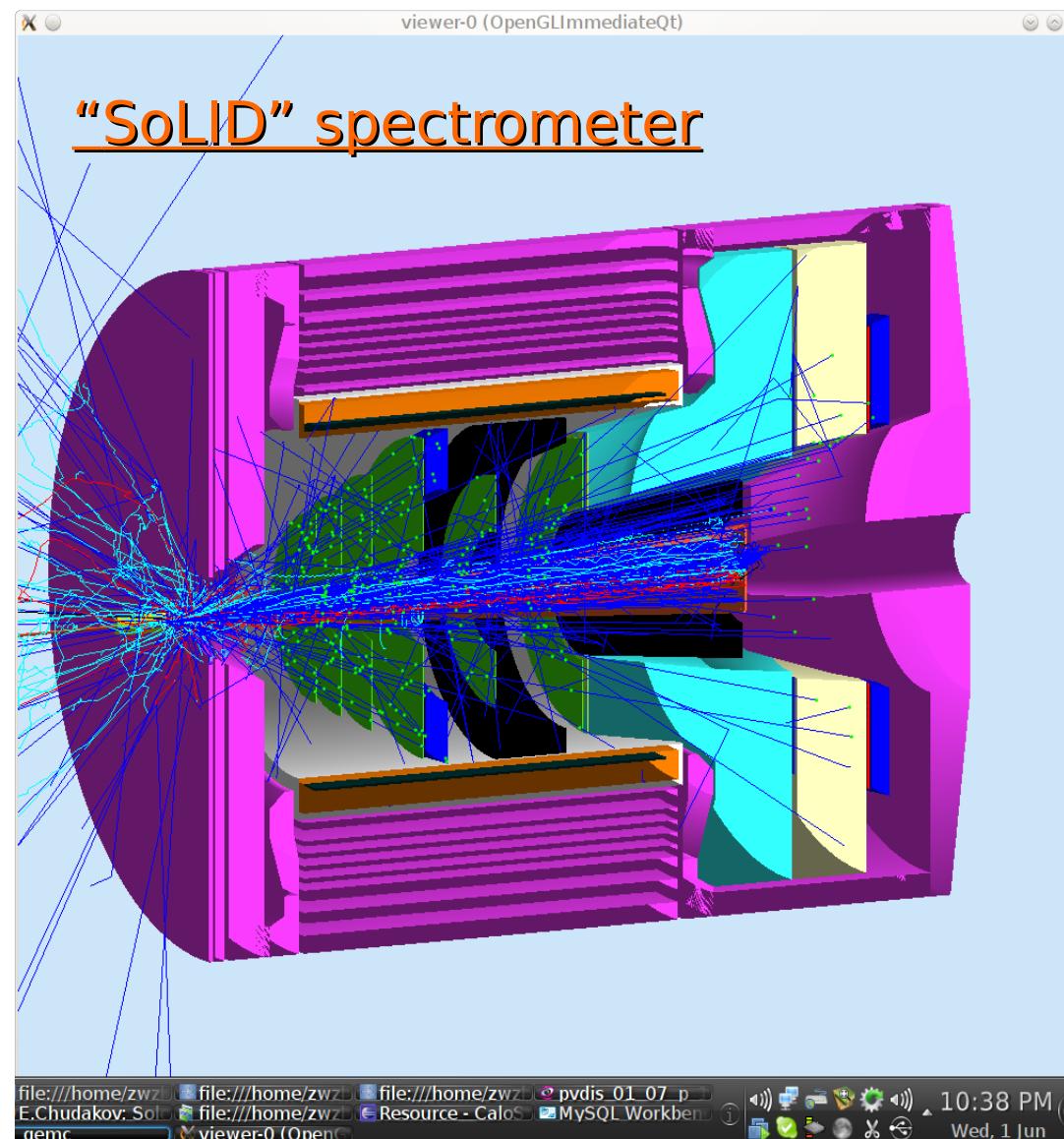
A: Matsui, Sato, Lee, PRC72,025204(2005)

B: Gorchtein, Horowitz, Ramsey-Musolf, PRC84,015502(2011)

C: Hall, Blunden, Melnitchouk, Thomas, Young, PRD88, 013011 (2013)



# Coherent PVDIS Program with SoLID @ 11 GeV



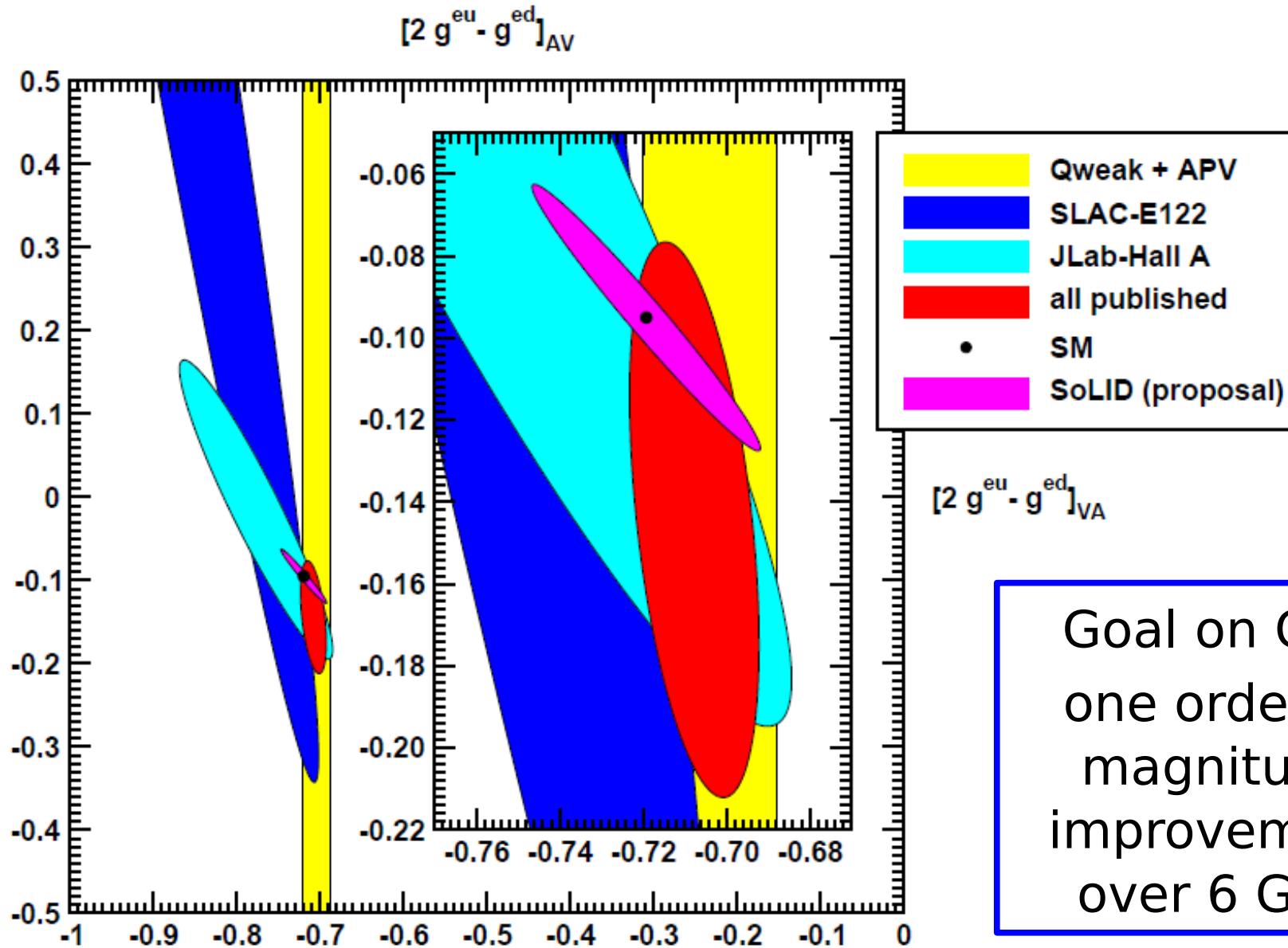
## SoLID Physics topics:

- PVDIS deuteron (180 days)  
–  $C_2$ ,  $\sin^2\theta_W$ , CSV, diquarks,
- PVDIS proton (90 days) – d/u  
→
- PV with  ${}^3\text{He}$  (LOI)
- SIDIS
- J/ $\psi$
- Presentations:

K. Allada, WG6, April 30, 11:10

Z. Ye, WG6+WG7, April 30,  
8:30

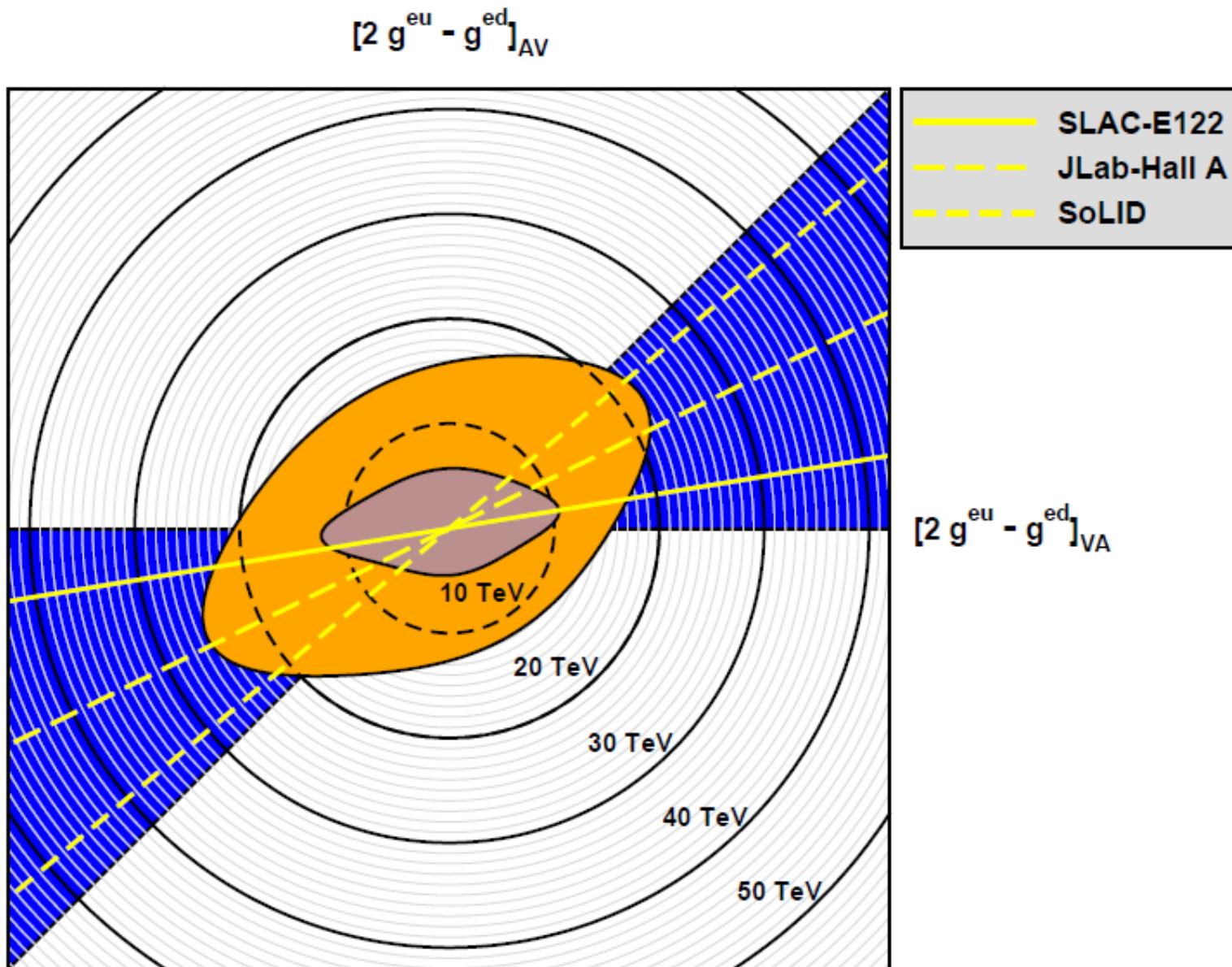
# Coherent PVDIS Program with SoLID @ 11 GeV



See Rakitha Beminiwattha's talk WG3+WG7 joint session  
at 9:45 (April 29<sup>th</sup>)



# Coherent PVDIS Program with SoLID @ 11 GeV



# Summary and Perspectives

The 6 GeV PVDIS from JLab:

- Improved world data on the eq VA effective coupling term  $2C_{2u}-C_{2d}$  by factor of five
- agrees with the SM
- showed  $2C_{2u}-C_{2d}$  is  $2\sigma$  from zero - indicating a nonzero contribution to PVDIS asymmetry due to quark's chirality preference
- BSM mass limits complimentary to collider experiments.

“New construction” experiments at JLab 12 GeV:

- PVDIS @ 11 GeV (SoLID) will improve  $C_{2q}$  by another order of magnitude.

Subedi et al, NIM-A 724, 90 (2013);

Wang et al., PRL 111, 082501 (2013);

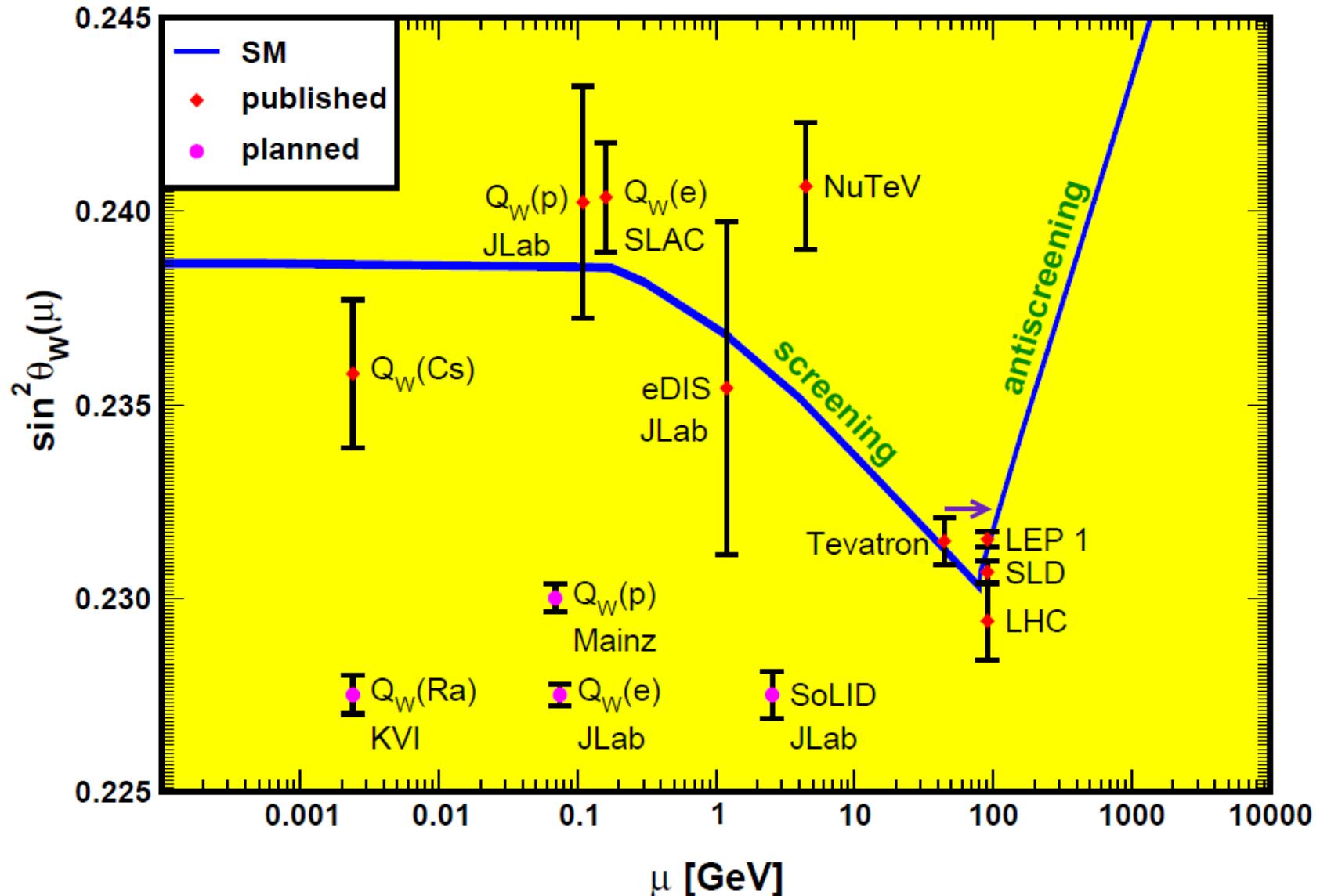
Wang et al., Nature 506, no. 7486, 67 (2014);

Wang et al., PRC91 (2015) 4, 045506.





# Running of $\sin^2 \theta_W(\mu)$



# E08-011 Kinematics

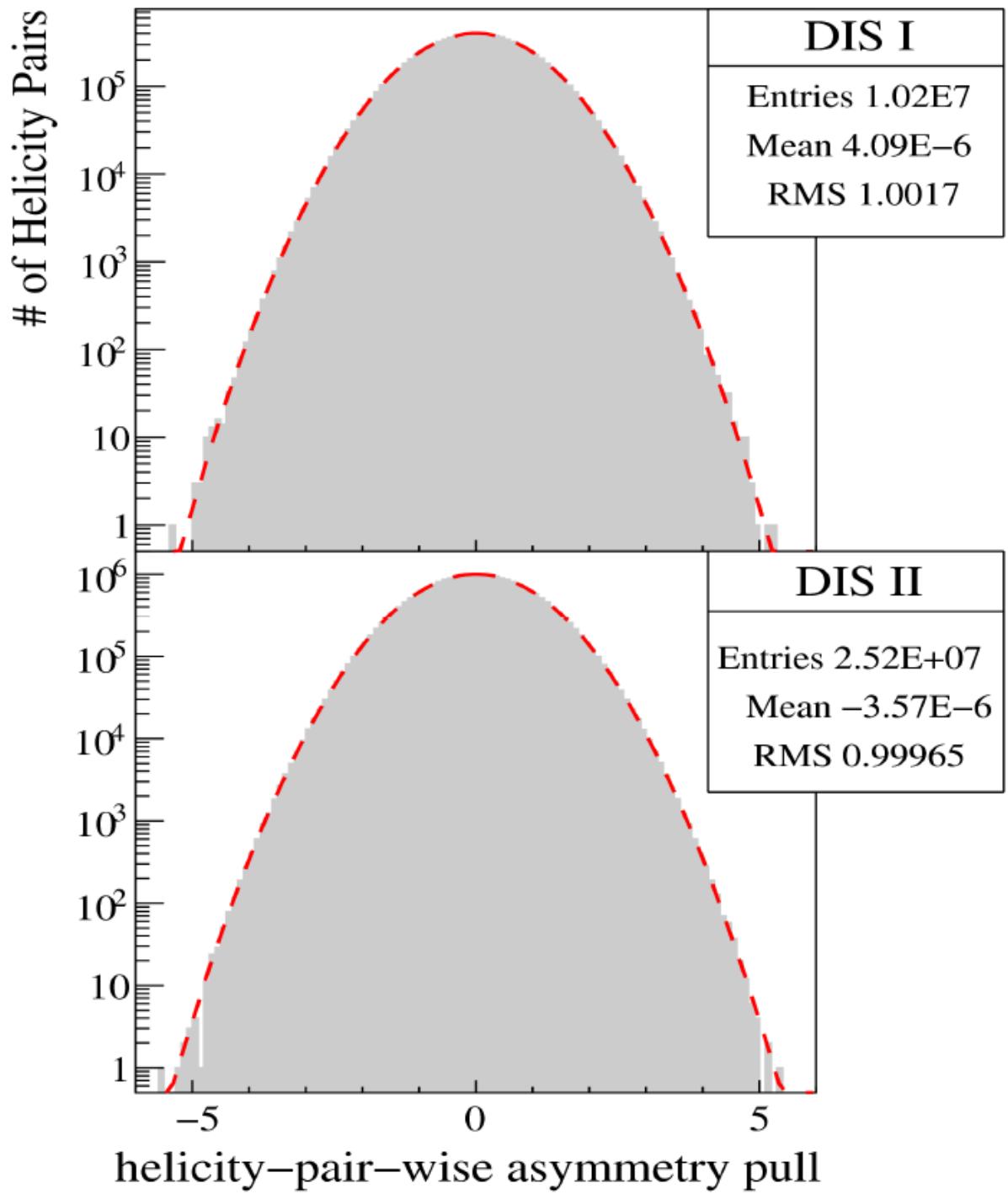
Kine#	HRS	$E_b$ (GeV)	$\theta_0$ (deg)	$E'_0$ (GeV)	$R_e$ (kHz)	$R_{\pi^-}/R_e$
DIS#1	Left	6.067	12.9	3.66	≈210	≈0.5
DIS#2	Left & Right	6.067	20.0	2.63	≈18	≈3.3
RES I	Left	4.867	12.9	4.0	≈300	<≈0.25
RES II	Left	4.867	12.9	3.55	≈600	<≈0.25
RES III	Right	4.867	12.9	3.1	≈400	<≈0.4
RES IV	Left	6.067	15	3.66	≈80	<≈0.6
RES V	Left	6.067	14	3.66	≈130	<≈0.7



# Data Quality

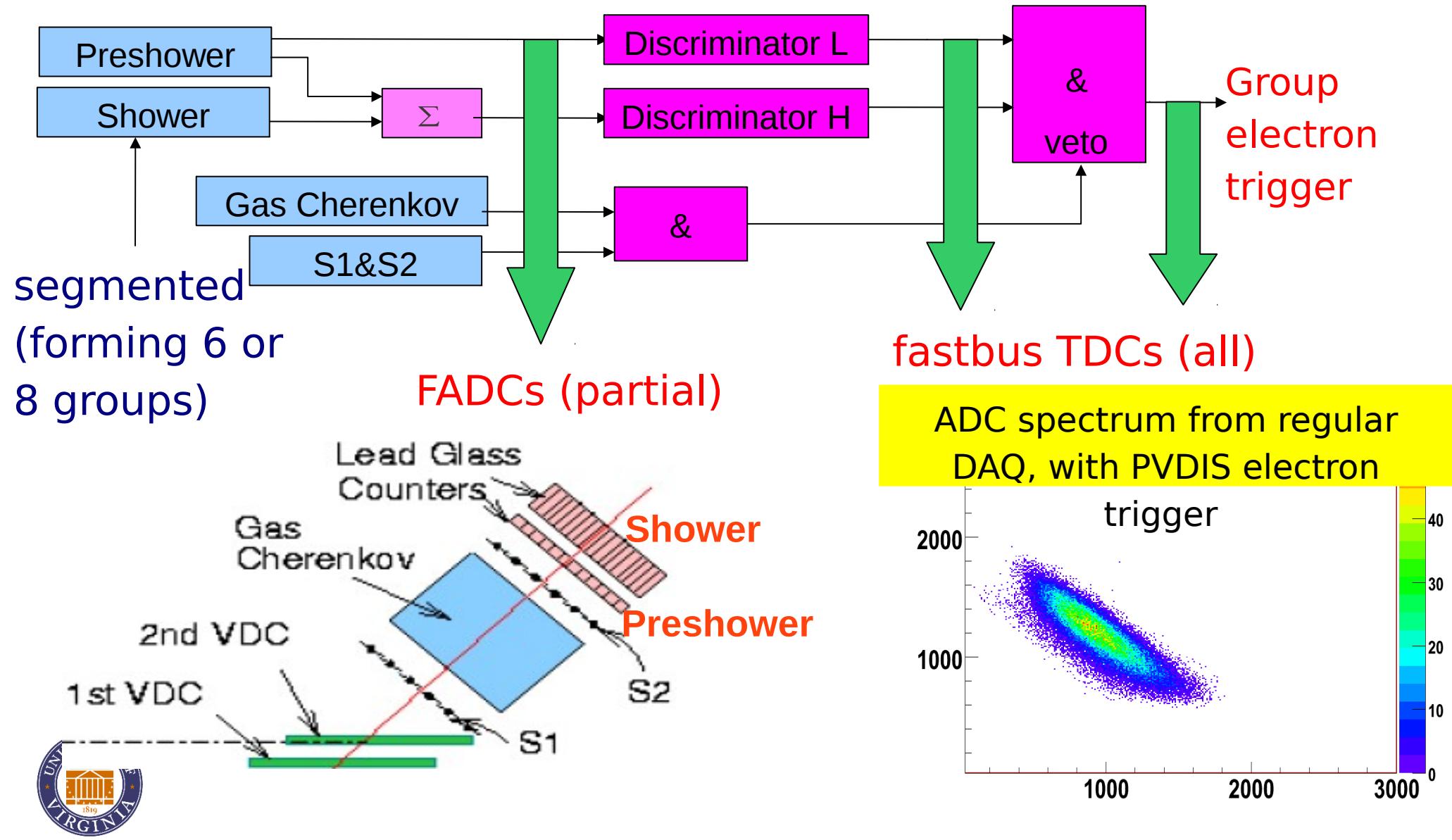
(pair-wise  
asymmetry pull plots):

$$pull = \frac{A_i - \langle A \rangle}{\Delta A_i}$$



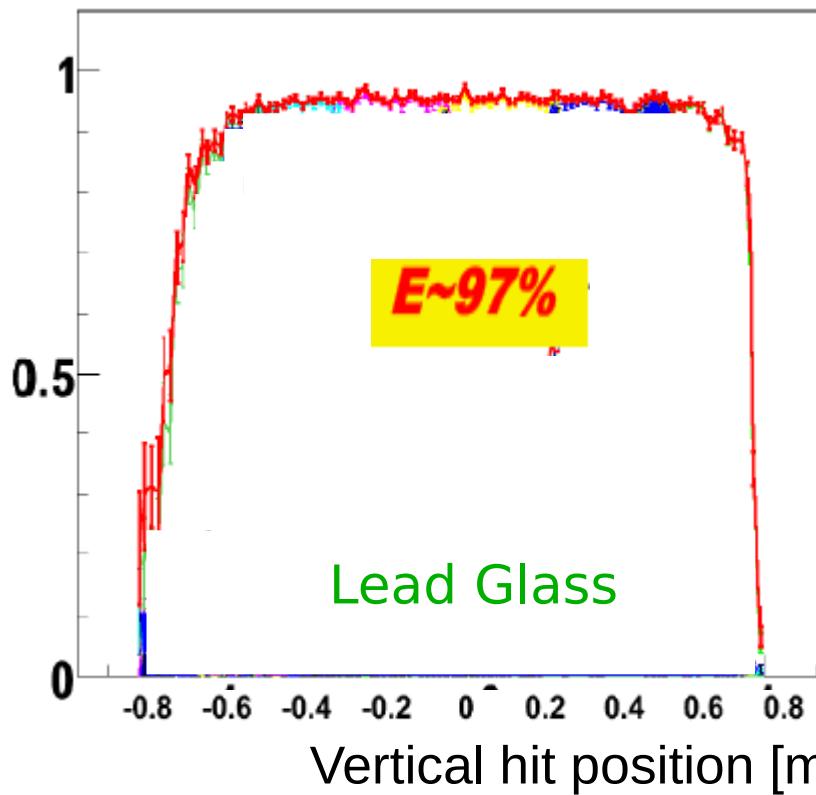
# Scaler-Based Counting DAQ with online (hardware) PID

- DIS region, pions contaminate, can't use integrating DAQ.
- High event rate ( $\sim 500\text{kHz}$ ), exceeds Hall A regular DAQ's Limit (4kHz)

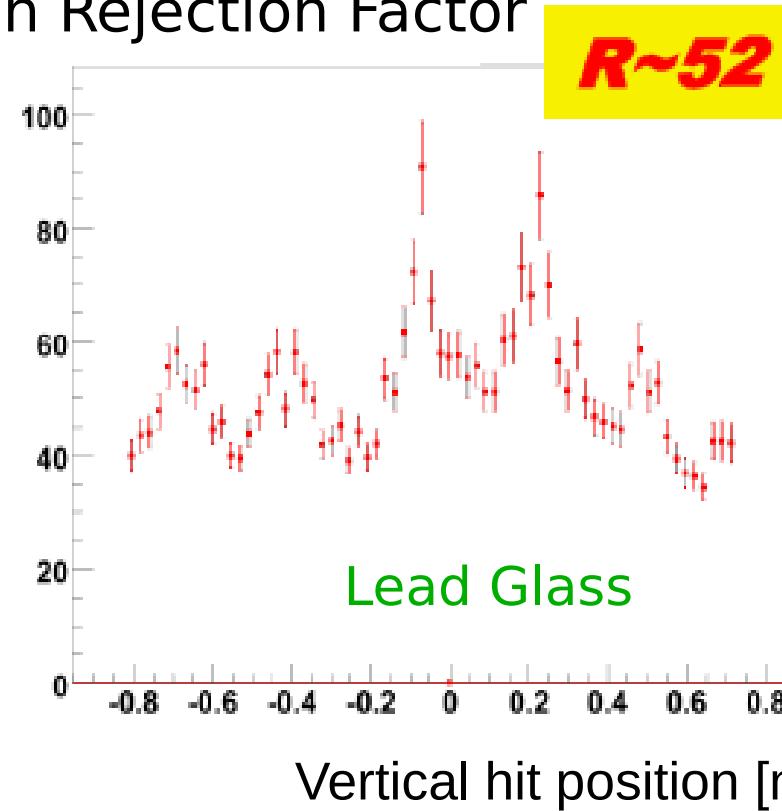


# PID Performance – Single Run

Electron Detection Efficiency



(work of K. Pan)  
Pion Rejection Factor



Affects measured asymmetry ( $Q^2$ ) if it varies over the acceptance or if there are “holes”

Combined with Cherenkov, pion contamination  $< 2 \times 10^{-4}$

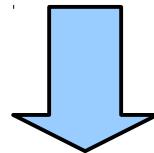
Detector efficiencies extracted from VDC-on runs, taken daily



# From Measured to Physics Asymmetry

- correcting for background  $f_i$  with asymmetry  $A_i$ :

$$A^{phys} = \frac{\left( \frac{A^{raw}}{P_b} - \sum_i A_i f_i \right)}{1 - \sum_i f_i}$$



$$A^{phys} \approx \frac{A^{raw}}{P_b} \prod_i (1 + \bar{f}_i)$$

$$\bar{f}_i \equiv f_i \left( 1 - \frac{A_i}{A^{raw}} P_b \right)$$



# From Measured to Physics Asymmetry

$$A_{Q^2=1.085, x=0.241}^{raw} = -78.45 \pm 2.68 \pm 0.07 \text{ ppm}$$

$P_b$	88.18%
$\Delta P_b$	$\pm 1.76\%$
$1 + f_{\text{depol}}$ (syst.)	1.0010 $< 10^{-4}$
$1 + f_{\text{Al}}$ (syst.)	0.9999 $\pm 0.0024$
$1 + f_{dt}$ (syst.)	1.0147 $\pm 0.0009$
$1 + f_{rc}$ (syst.)	1.015 $\pm 0.020$
$1 + \bar{f}_{\gamma\gamma, \gamma Z \text{ boxes}}$ (syst.)	0.998 — $\pm 0.002$

$\Delta f_{\pi^-}$	$\pm 0.009\%$
$\Delta \bar{f}_{\text{pair}}$	$\pm 0.04\%$
$\Delta f_{A_n}$	$\pm 2.5\%$
$\Delta Q^2$	$\pm 0.85\%$
rescatt bg	$\ll 0.2\%$
target impurity	$\pm 0.06\%$

$A^{\text{phys}}$ (ppm)	-91.10
(stat.)	$\pm 3.11$
(syst.)	$\pm 2.97$
(total)	$\pm 4.30$



# From Measured to Physics Asymmetry

$$A_{Q^2=1.901, x=0.295}^{raw} = -140.30 \pm 10.43 \pm 0.16 \text{ ppm (LHRS)}$$

$$A_{Q^2=1.901, x=0.295}^{raw} = -139.84 \pm 6.58 \pm 0.46 \text{ ppm (RHRS)}$$

$P_b$	89.29	88.73%	$\Delta f_{\pi^-}$	$\pm 0.006\%$	$\pm 0.003\%$
$\Delta P_b$	1.19%	$\pm 1.50\%$	$\Delta \bar{f}_{\text{pair}}$	$\pm 0.4\%$	$\pm 0.2\%$
$1 + f_{\text{depol}}$ (syst.)	1.0021 $< 10^{-4}$		$\Delta \bar{f}_{A_n}$	$\pm 2.5\%$	$\pm 2.5\%$
$1 + f_{\text{Al}}$ (syst.)	0.9999 $\pm 0.0024$	0.9999 $\pm 0.0024$	$\Delta Q^2$	$\pm 0.64\%$	$\pm 0.65\%$
$1 + f_{dt}$ (syst.)	1.0049 $\pm 0.0004$	1.0093 $\pm 0.0013$	rescatt bg	$\ll 0.2\%$	$\ll 0.2\%$
$1 + f_{rc}$ (syst.)	1.019 $\pm 0.004$		target impurity	$\pm 0.06\%$	$\pm 0.06\%$
$1 + f_{\gamma\gamma\text{box}}$	0.997	—	Asymmetry		
$1 + \bar{f}_{\gamma\gamma, \gamma\text{Zboxes}}$ (syst.)	— $\pm 0.003$	1.005 $\pm 0.005$	$A^{\text{phys}} \text{ (ppm)}$ (stat.)	-160.80	
			(syst.)	$\pm 6.39$	
			(total)	$\pm 3.12$	
				$\pm 7.12$	



# SLAC E122 vs. JLab E08-011

	SLAC E122 (1978)	JLab E08-011 (2009)
Beam	37%, 16.2-22.2 GeV	90%, 6.0674 GeV, 100uA
Target	30-cm LD2, LH2	20-cm LD2
Spectrometer	4°	12.9° and 20°
Q <sup>2</sup>	1-1.9 GeV <sup>2</sup>	1.1 and 1.9 GeV <sup>2</sup>
Data collection	Integrating gas Cerenkov and lead glass detectors, (two highest energies only) independently $A/Q^2 = (-9.5 \pm 1.6) \times 10^{-5} \text{ (GeV/c)}^{-2}$	Counting DAQ using both GC and lead glass for PID at the hardware level
$\sin^2\theta_W = 0.20 \pm 0.$ results 03	$\pm 0.86 \times 10^{-5} \text{ (stat)} \pm 5\% \text{ (Pb)}$ $\pm 3.3\% \text{ (beam)} \pm 2\% \text{ (\pi contamination)}$ $\pm 3\% \text{ (radiative corrections)}$ $A/Q^2 = (-9.7 \pm 2.7) \times 10^{-5} \text{ (GeV/c)}^{-2}$	$\pm (3-4)\% \text{ (stat)}$ $\pm \text{syst.}$



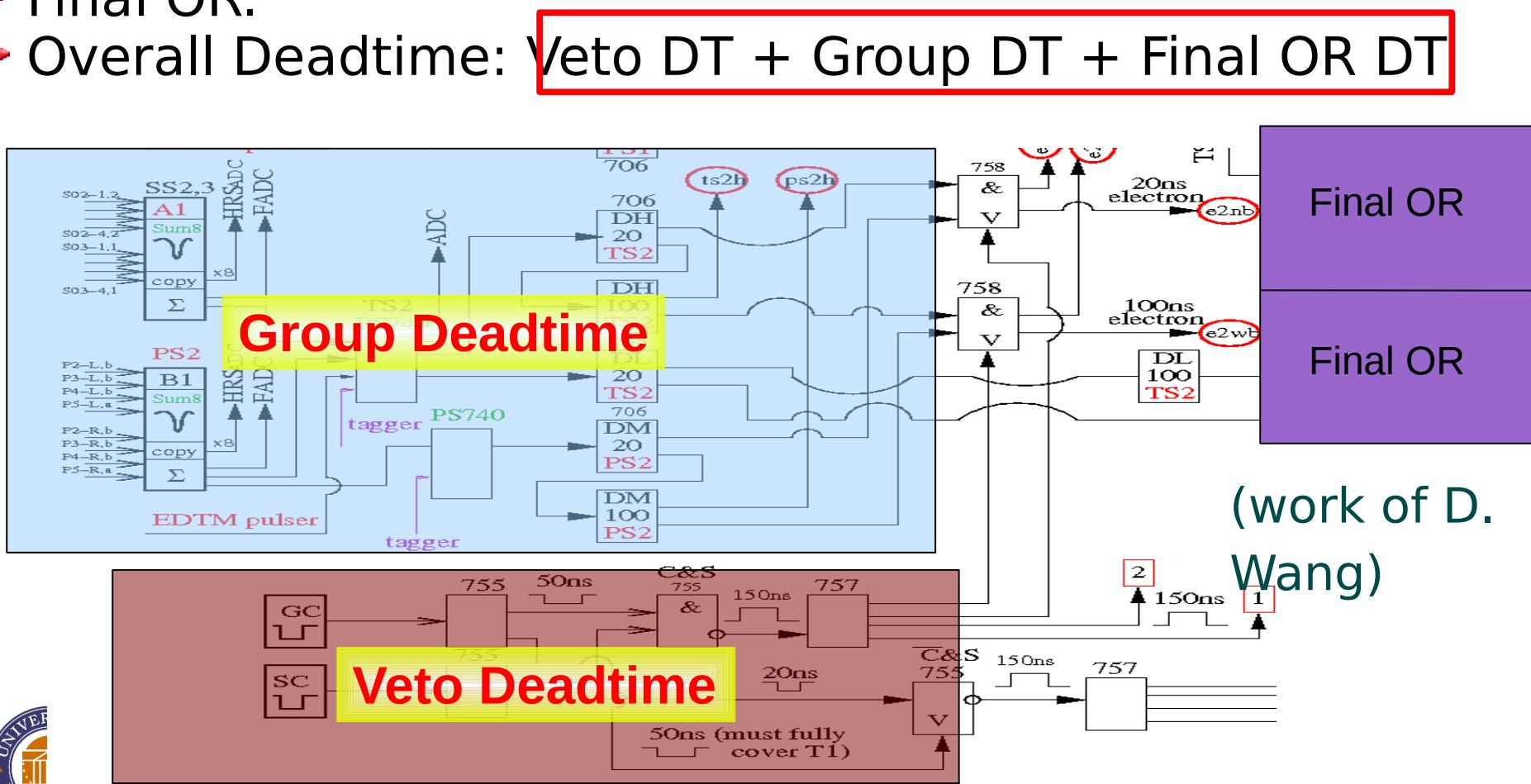
# DAQ Deadtime Correction

Deadtime correction to asymmetry:

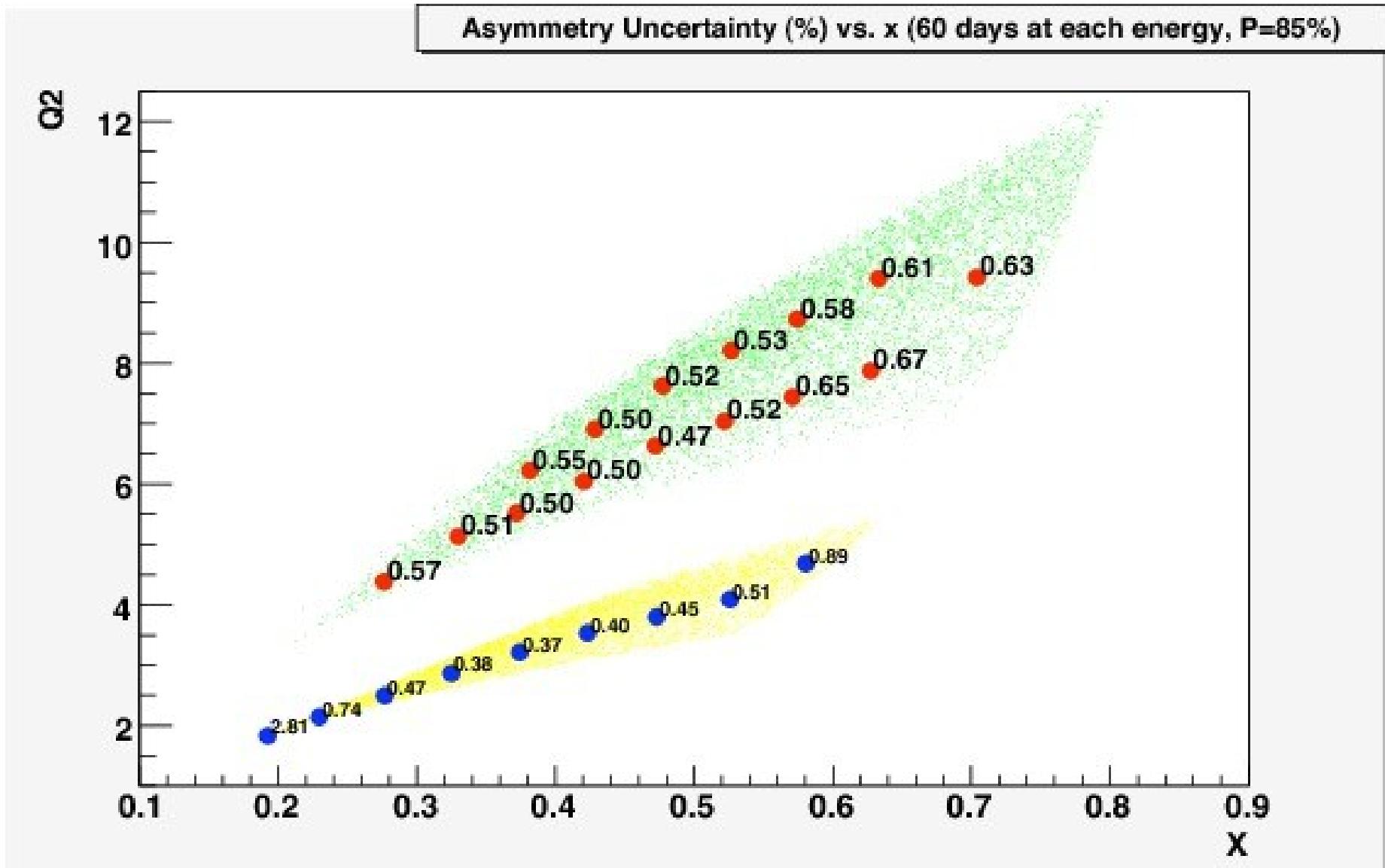
$$A_{\text{measured}} = A_{\text{phys}} (1 - \text{deadtime loss})$$

## Deadtime Decomposition:

- Group Deadtime: proportional to group rate; narrow/wide.
- Veto Deadtime: T1/GC rate; the same for all groups.
- Final OR.
- Overall Deadtime: Veto DT + Group DT + Final OR DT



# Coherent PVDIS Program with SoLID @ 11 GeV



Goal on  $C_{2q}$ : one order of magnitude improvement over 6 GeV



# Pion Asymmetries

HRS, Kinematics	Left DIS#1	Left DIS#2	Right DIS#2
narrow path			
$A_\pi^{\text{meas}} \pm \Delta A_\pi^{\text{meas}}$ (total) (ppm)	$-48.8 \pm 14.0$	$-22.0 \pm 21.4$	$-20.3 \pm 6.0$
$A_{e,\text{dit}}^{\text{bc,raw}} \pm \Delta A_{e,\text{dit}}^{\text{bc,raw}}$ (stat.) (ppm)	$-78.5 \pm 2.7$	$-140.3 \pm 10.4$	$-139.8 \pm 6.6$
$f_{\pi/e} \pm \Delta f_{\pi/e}$ (total) ( $\times 10^{-4}$ ) $\left( \frac{\Delta A_e}{A_e} \right)_{\pi^-, n}$	$(1.07 \pm 0.24)$ $0.89 \times 10^{-4}$	$(1.97 \pm 0.18)$ $0.63 \times 10^{-4}$	$(1.30 \pm 0.10)$ $0.27 \times 10^{-4}$
wide path			
$A_\pi^{\text{meas}} \pm \Delta A_\pi^{\text{meas}}$ (total) (ppm)	$-41.3 \pm 12.8$	$-23.7 \pm 21.4$	$-20.3 \pm 6.0$
$A_{e,\text{dit}}^{\text{bc,raw}} \pm \Delta A_{e,\text{dit}}^{\text{bc,raw}}$ (stat.) (ppm)	$-78.3 \pm 2.7$	$-140.2 \pm 10.4$	$-140.9 \pm 6.6$
$f_{\pi/e} \pm \Delta f_{\pi/e}$ (total) ( $\times 10^{-4}$ ) $\left( \frac{\Delta A_e}{A_e} \right)_{\pi^-, w}$	$(0.72 \pm 0.22)$ $0.54 \times 10^{-4}$	$(1.64 \pm 0.17)$ $0.55 \times 10^{-4}$	$(0.92 \pm 0.13)$ $0.21 \times 10^{-4}$

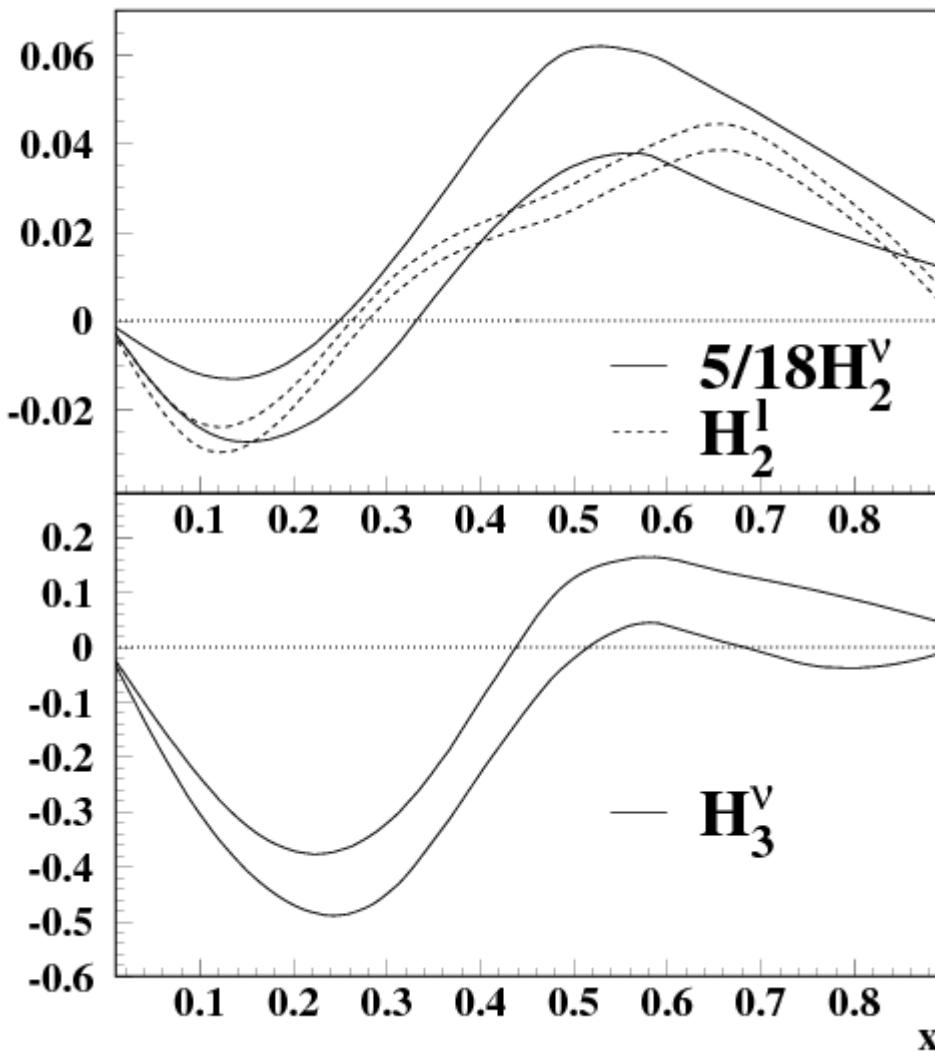
# Pair Production Background

- Took reversed-polarity runs, mostly to determine  $e^+/e^-$ -ratio. Positron asymmetry from those runs have very large error;
- Assumed positron asymmetry to be similar to  $\pi^-$ -asymmetry;
- Effect on the measurement is about 10 times larger than  $\pi^-$ -background.

# Estimation of HT on the $a_3$ term

We could use HT results on  $F_{_3}^{\gamma Z}$  from neutrino data in 0710.0124 (hep-ph) to correct the  $a_3$  term:

isoscalar target



$$F_{2,T,3}(x, Q^2) = F_{2,T,3}^{t=2}(x, Q^2) + \frac{H_{2,T,3}^{t=4}(x)}{Q^2} + \frac{H_{2,T,3}^{t=6}(x)}{Q^4} + \dots$$

for  $F_2^v$  and  $F_2^l$

for any target

$$F_3^v = 2[d + s - \bar{u} - c]$$

for deuteron

$$F_3^v = 2[u_V + d_V + 2s - 2\bar{c}]$$

# Formalism for Parity Violation in DIS

$$A_{PV} = \frac{G_F Q^2}{\sqrt{2} \pi \alpha} [a(x) + Y(y) b(x)]$$

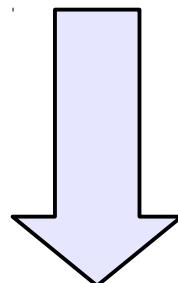
$$x \equiv x_{Bjorken} \quad y \equiv 1 - E'/E$$

$$q_i^+(x) \equiv q_i(x) + \bar{q}_i(x)$$

$$q_i^-(x) = q_i^V(x) \equiv q_i(x) - \bar{q}_i(x)$$

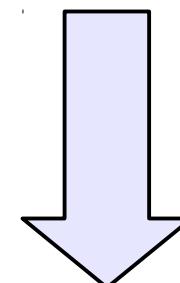
$$a(x) = \frac{1}{2} g_A^e \frac{F_1^{\gamma Z}}{F_1^\gamma} = \frac{1}{2} \frac{\sum_i C_{1i} Q_i q_i^+(x)}{\sum_i Q_i^2 q_i^+(x)}$$

$$b(x) = g_V^e \frac{F_3^{\gamma Z}}{F_1^\gamma} = \frac{1}{2} \frac{\sum_i C_{2i} Q_i q_i^-(x)}{\sum_i Q_i^2 q_i^-(x)}$$



**For an isoscalar target ( ${}^2\text{H}$ ), structure functions largely simplifies:**

$$a(x) = \frac{3}{10} (2C_{1u} - C_{1d}) \left( 1 + \frac{0.6 s^+}{u^+ + d^+} \right)$$



$$b(x) = \frac{3}{10} (2C_{2u} - C_{2d}) \left( \frac{u_v^+ + d_v^-}{u^+ + d^+} \right)$$

If neglecting sea quarks, asymmetry is no longer sensitive to PDFs  $\rightarrow$  “static limit”